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Templates of Expected Measurement Uncertainties

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Abstract

The covariance committee of CSEWG (Cross Section Evaluation Working Group) established templates of expected measurement uncertainties for neutron-induced total, (n,γ) , neutron-induced charged-particle, and (n,xn) reaction cross sections as well as prompt fission neutron spectra, average prompt and total fission neutron multiplicities, and fission yields. Templates provide a list of what uncertainty sources are expected for each measurement type and observable, and suggest typical ranges of these uncertainties and correlations based on a survey of experimental data, associated literature, and feedback from experimenters. Information needed to faithfully include the experimental data into the nuclear-data evaluation process is also provided. These templates could assist (a) experimenters and EXFOR compilers in delivering more complete uncertainties and

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measurement information relevant for evaluations of new experimental data, and (b) evaluators in achieving a more comprehensive uncertainty quantification for evaluation purposes. This effort might ultimately lead to more realistic evaluated covariances for nuclear-data applications. In this topical issue, we cover the templates coming out of this CSEWG effort—typically, one observable per paper. This paper here pre-faces this topical issue by introducing the concept and mathematical framework of templates, discussing potential use cases, and giving an example on how they can be applied (estimating missing experimental uncertainties of $^{235}U(n,f)$ average prompt fission neutron multiplicities), and their impact on nuclear-data evaluations.

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1 INTRODUCTION

Evaluated nuclear data are informed by either experimental data, nuclear models, or both. The accuracy and precision of these nuclear data strongly rely on the quality of available experimental data and the magnitude of their associated covariances. Experimental covariances not only bound the evaluated uncertainties in many cases, they also provide a weight of individual experimental data points with respect to nuclear model calculations and other data sets if applicable. This weight can only be appropriate if all pertinent uncertainty sources are consistently provided for all experimental data used in the evaluation. However, more often than not, one or more uncertainty sources that are expected based on knowledge of similar measurements are missing for a specific data set in the EXFOR database [1]—an experimental low- and intermediate-energy nuclear reaction data library and the go-to database for experimental data for nuclear-data evaluations. Up to now, it has been up to the evaluator to identify the missing uncertainties and estimate a reasonable value for them. If evaluators choose to not estimate those values, they make the very strong and implicit assumption that such missing uncertainties are null. In some cases, this assumption might be justified. But, if a non-negligible uncertainty source was forgotten, the experimental data set will have an incorrect higher weight compared to other experimental data sets used for the evaluation. This will ultimately lead to a biased evaluation. It has been shown in Refs. [2,3] that neglecting these missing experimental uncertainties potentially impacts evaluated data and uncertainties such that these biases adversely affect application calculations considerably.

To mitigate the issue of missing experimental uncertainties and their adverse impact on evaluated nuclear-data mean values and covariances, templates of expected measurement uncertainties were established as part of a multi-year effort led by the covariance committee of CSEWG (Cross Section Evaluation Working Group). Several international experts on nuclear-data experiments and evaluations joined in this project, making it an international effort. Templates were established for neutron-induced total, capture, charged-particle, and (n,xn) cross sections as well as prompt fission neutron spectra, average prompt and total fission neutron multiplicities, and fission yields. They are described in detail in separate journal publications within this topical issue that is prefaced by this paper and was worked on for total, capture and fission yields as part of PhD theses [4–11]¹. All templates provide a comprehensive list of uncertainty sources, ranges of expected uncertainties and suggested correlations for each of these sources. In addition to these templates, recommendations are given on what information should be supplied by experimenters for evaluation purposes.

¹We focus on standard measurement techniques and do not cover experiments specifically designed to validate them. While these are key in ensuring that our standard measurement techniques yield reliable results, there is insufficient information (*i.e.*, too few measurements of the same type) to establish templates. We also do not cover integral experiments. For some types of integral experiments (*e.g.*, criticality experiments in the "International Handbook of Evaluated Criticality Safety Benchmark Experiments" (ICSBEP) [12]), stringent uncertainty-quantification rules and template-like tables have been developed [13]. They are rigorously applied as part of the review process to data entering ICSBEP since the release of Ref. [13]. This process significantly enhances the quality of uncertainties in that database and serves as an example of the benefit of applying templates such as the ones presented here.

This paper here serves as preface to this special issue on templates for various observables; we introduce in Sec. 2 the concept of templates, their history, and discuss potential use cases. Section 3 covers the mathematical basis for establishing templates. A specific example, 235 U(n,f) average prompt fission neutron multiplicities, is given in Sec. 4 to illustrate how templates can be applied to estimate missing experimental uncertainties for evaluation purposes and their impact on evaluated mean values and covariances. Section 5 provides conclusions and an outlook to future work.

2 Introduction to the concept of templates

2.1 What Are Templates of Expected Measurement Uncertainties?

The templates cover many common direct measurement techniques typically employed to provide experimental data for a specific nuclear-data observable. A minimal set of uncertainty sources that are expected to be addressed in the uncertainty quantification of an experiment is then tabulated for each of these measurement types. They are split out according to measurement type as some uncertainty sources might not apply to all measurement techniques. For instance, in a ratio measurement, both samples—the one under investigation and the monitor sample²—are irradiated by the same neutron flux. Hence, the neutron flux does not need to be determined and no associated uncertainties apply for ratio measurements. However, they do apply for measurements of the same observable where the neutron flux is quantified directly.

The template also provides reasonable, conservative ranges of uncertainties for each of those sources. We give, unless otherwise noted, conservative ranges because if an uncertainty source was forgotten to be quantified, it is possible that the associated correction might not have been investigated in great detail. Also, one has to consider that some uncertainties reported in the literature might be overly optimistic or very low as considerable effort was spent to reduce them. We choose here to give uncertainties for partial uncertainty sources that were selected to be mutually independent, where possible, following the mathematical framework discussed in Sec. 3.

In addition to that, the templates list estimates of correlation coefficients between uncertainties of a specific source within the same and between different experiments. While the former information is rarely found in the EXFOR database or the experimental literature, correlations between uncertainty sources of different experiments are even less likely to be provided by experimenters. Estimating the latter correlations is usually the evaluator's task. To aid this endeavor, correlation values for templates were mostly established based on discussion of the underlying physics processes of the correction and its impact on the final deduced experimental observable.

2.2 Use Cases and Users

Templates were designed with the following users in mind: nuclear-data experimenters, nuclear-data evaluators, EXFOR compilers, and journal editors or reviewers.

One aim of the template project is to maintain and enhance best practices on what should be documented (including uncertainties) for a measurement. Following these best practices should help ensure that experimental data can be used more efficiently by the community for a long time. More specifically, an experimenter can use these templates as a checklist when planning the experiment and during the data-reduction phase, or at least before publishing the final data set. Counter-checking their reported uncertainties with these lists makes sure that all relevant uncertainty sources and information needed by evaluators are provided. It is highly recommended that experimenters clearly state, in the

 $^{^{2}}$ A monitor can be, for instance, a reference cross section into which considerable experimental and evaluation effort has been put [14]. Because these monitor cross sections are among the most accurate ones, a comparable total uncertainty for the measurement in ratio to the monitor can be achieved with far less effort.

EXFOR entry and/or the associated journal article, whether an uncertainty source is practically zero, as this might not be obvious to an evaluator.

EXFOR compilers can utilize these templates as guidelines sanctioned by the broad experimental and evaluator community on what information would be of high importance to include in an EXFOR entry. The templates can be used to ask for this information in a targeted manner as input to EXFOR entries. Of course, we acknowledge that in some cases such request by the EXFOR compilers might not always be fully satisfied by the authors. However, if applied over time, these templates will help improve the completeness and usability of new EXFOR entries with the help of EXFOR compilers and experimenters.

Journal editors and reviewers can also use the guidelines presented here to ask for the information needed by evaluators to be presented in an article. This should increase the usability of the resulting journal article.

These templates were designed to help evaluators in making better informed choices to fill in missing uncertainty and correlation information comprehensively across the whole experimental database used for an evaluation. These templates are provided by means of large literature reviews and in discussion with the experimental community. Given that, the estimated values are expected to be better justified for many cases than those evaluators come up on their own. Also, they can help evaluators pinpoint missing uncertainty sources and estimate them. They can also help identify unrealistically low uncertainties. Systematically using these templates for evaluations will lead to a more balanced uncertainty quantification across different data sets. In addition to that, if experimenters provide more complete uncertainties, as they use these templates as checklists, the need for assumptions on experimental data on the part of the evaluator will reduce. Hence, applying these templates can ultimately lead to more realistic evaluated uncertainties for nuclear-data libraries and applications.

2.3 What a Template Should Not Be

It should be emphasized that these templates are neither applicable to all types of measurements, nor are they to be construed as immutable laws. They are rather guidelines that will change with advancing our understanding regarding these measurements. For instance, if a novel measurement technique is designed to go beyond the standard methods discussed in Refs. [4–11], some uncertainty sources might not apply at all for this new measurement type or instead new ones need to be considered. However, it would be best practice to mention what uncertainty sources are practically zero in this case compared to the standard technique. Also, the quantitative template values are not intended to be target or acceptable uncertainty values for future measurements of techniques discussed here. They are only a guide value to be used when historic measurements are not described in full detail. We want to encourage continuous improvement in experimental methods.

It is equally important to understand that these templates should not be used by evaluators to **replace** a detailed analysis of experimental data. Template uncertainty values should only be used **as a last resort** if no experimental information is available that could enable the evaluator to estimate expected, but missing, uncertainty sources. This point is important as experimenters might spend considerable time analyzing their measurement and quantifying uncertainties. If template values are used instead of these carefully estimated uncertainties, the weight of the experimental data might, once again, become unjustified, thus adversely impacting evaluated nuclear data. Also, it is assumed that experimental data are updated to the latest monitor standard and decay data, and adjusted for obvious and easy-to-correct mistakes. Template uncertainties should not be used to cover differences between data sets due to failing to undertake straightforward corrections.

It is obvious that there are limitations to how much templates can help. If major corrections are simply missing for a data set, the experimental data might be too biased to use them for evaluation purposes. In such cases, it might be more adequate to reanalyze and correct historic data, or reject them, rather than add uncertainties accounting for the bias. The same applies if inadequate (*e.g.*, only total uncertainties with no hint of their make-up) or no uncertainty information is provided for a measurement of an observable that needs to be evaluated to high precision. Then, the conclusion might be that new measurements are needed that avoid the pitfalls of previous ones and supply adequate information for evaluations.

2.4 History of Templates and How They Were Established

The idea of these templates was based on the work of P. Schillebeeckx *et al.* [15] that created templates for information that ought to be provided in EXFOR entries of transmission experiments. These templates included recommendations on how to document uncertainties and detailed associated procedures but was not limited to uncertainty quantification only. P. Helgesson *et al.* [16] created a first version of templates for experimental uncertainties for ⁵⁹Ni a few years later. This work also encompasses tables of uncertainties and correlations encountered for selected observables ((n,tot), (n,p), (n, α) and (n, γ) cross sections) based on the limited set of EXFOR entries found for ⁵⁹Ni. It did not distinguish between different measurement types when a template was created and did not include fission observables, nor did it do a broad literature survey across many isotopes and measurement techniques as done for Refs. [4–11]. In the preparation of this paper, the uncertainty values obtained in Ref. [16] for the ⁵⁹Ni observables (rare isotope) were compared to pertinent template values.

Out of these ideas and out of the need for a comprehensive uncertainty quantification for Neutron Data Standards evaluations [14], a template of expected measurement uncertainties in fission chamber measurements was developed and published in an early version in Ref. [17]. It was finalized and systematically applied to updating 239 Pu(n,f) cross-section covariances in the database underlying the Neutron Data Standards evaluation. This work presented in Ref. [2] highlighted clearly that considering all pertinent uncertainties in this database changed the evaluated 239 Pu(n,f) mean values and covariances so significantly that application calculations were impacted. This conclusion motivated a larger CSEWG covariance committee effort to provide templates for more observables.

Initial versions of most templates in this issue and in PhD theses, Refs. [4–11], were established based on discussions between experimenters, evaluators, and EXFOR representatives at a mini-CSEWG meeting that took place April 29, 30 and May 1st, 2019 in Los Alamos, NM, USA. After introductions to the observables at hand and measurement techniques, evaluators stated what information they need to include data and their uncertainties correctly and effectively into evaluations. Experimenters provided input on typical measurement types, their typical uncertainty sources, and conservative ranges of these uncertainties and correlations. EXFOR representatives weighed in on what uncertainty information can be realistically stored given the format. In addition to that, these templates were established based on the information found in multiple EXFOR entries and a broad literature review, and further in-depth discussions with experimenters and evaluators over a period of one year.

3 Mathematical Basis of Templates of Expected Measurement Uncertainties

Here, we formally examine the various assumptions and mathematical approximations that support the use of the template approach in quantifying experimental uncertainties and their correlation grounded in the mathematical ideas of Refs. [18–20].

Let $\mathbf{x} = (x_1, \ldots, x_i, \ldots, x_n)$ denote a set of all the *primary parameters* of an experiment. These should be mostly very basic parameters, not partially derived ones. Basic parameters, \mathbf{x} , could, for instance, be counts of the main measurement, background counts, measured impurities, *etc.* Clearly *n* is likely to be a very large number, even for relatively simple experiments. Then, let $\mathbf{y} = (y_1, \ldots, y_k, \ldots, y_m)$ represent *derived parameters* which the experiment seeks to determine. The variable \mathbf{y} could be, for instance, a collection of energy-dependent cross sections for a particular reaction. The number m may or may not be large. The combined experimental and data-analysis procedures can be embodied in a specific experiment algorithm \mathbf{A} . This algorithm is usually more complicated than can be expressed by simple mathematical functions. The process of deducing \mathbf{y} from \mathbf{x} can be symbolized by $\mathbf{A}\{\mathbf{x}\} \to \mathbf{y}$. The template approach seeks to assess uncertainties on the level of independent primary parameters \mathbf{x} .

The elements of \mathbf{x} and \mathbf{y} are assumed to be random variables with statistical properties governed by two probability density functions (PDFs), $p_x(\mathbf{x})$ and $p_y(\mathbf{y})$. These functions are not known. However, it must be assumed that specific values \mathbf{x}_0 for the primary parameters \mathbf{x} are known *a priori*, or are measurable. If not, the experiment is futile. The determination of \mathbf{x} does not yield the true value of the underlying physical quantity but rather an estimate \mathbf{x}_0 due to the determination process being affected by random errors of, *e.g.*, a measurement or Monte Carlo simulation. How realizations of \mathbf{x} scatter around the true value is reflected in the PDF $p_x(\mathbf{x})$. \mathbf{x}_0 should also not be confused with the PDF mean values $\langle \mathbf{x} \rangle$. They can only approximately approached by many repetitions of and otherwise unbiased experiment, which is very impractical. While it is often assumed that $\langle \mathbf{x} \rangle \approx \mathbf{x}_0$ is an adequate approximation, the possible discrepancy should then be quantified by the covariance matrix for \mathbf{x} , \mathbf{V}_x . Given this assumption, the experiment is usually represented symbolically by $\mathbf{A}\{\mathbf{x}_0\} \to \mathbf{y}_0$. Again, \mathbf{y}_0 is not comparable to the mean value $\langle \mathbf{y} \rangle$, but we assume that $\langle \mathbf{y} \rangle \approx \mathbf{y}_0$ and assess the discrepancy in \mathbf{V}_y , the covariance matrix for \mathbf{y} . Quantifying \mathbf{V}_x is required before comparable values for \mathbf{y} and \mathbf{V}_y can be generated. The two methods for estimating \mathbf{V}_y to be considered here are *stochastic* and *deterministic*.

Stochastic method for estimating \mathbf{V}_y : If the knowledge of $p_x(\mathbf{x})$ is limited to $\langle \mathbf{x} \rangle$ and \mathbf{V}_x , the Maximum Entropy Principle suggests that $p_x(\mathbf{x})$ is most likely to be multivariate normal (Gaussian) [19]. The stochastic approach involves generating a large collection of samples $\{\mathbf{x}_{\lambda}\}(\lambda = 1, \Lambda)$ by Monte Carlo governed by PDF $p_x(\mathbf{x})$. A collection $\{\mathbf{y}_{\lambda}\}$ is produced by repeated application of $\mathbf{A}\{\mathbf{x}_{\lambda}\} \to \mathbf{y}_{\lambda}$. Then, $\langle \mathbf{y} \rangle$ and \mathbf{V}_y can be estimated from

$$\langle y_k \rangle \approx \left(\sum_{\lambda=1,\Lambda} y_{k\lambda} \right) / \Lambda \quad (k=1,m),$$
 (1)

$$v_{ykl} \approx \left(\sum_{\lambda=1,\Lambda} y_{k\lambda} y_{l\lambda}\right) / \Lambda - \langle y_k \rangle \langle y_l \rangle \quad (k,l=1,m).$$
 (2)

The v_{ykl} are elements of \mathbf{V}_y . The stochastic method is conceptually simple, but rarely undertaken due to the computational cost involved. Also, it does not lend itself to utilizing the template approach to categorizing experimental uncertainties if applied to estimating total experimental uncertainties.

Deterministic method for estimating \mathbf{V}_y : This approach linearizes the relationships between all the y_k and x_i . Thus, a very small shift $\Delta \mathbf{y}$ of derived \mathbf{y} due to a very small shift $\Delta \mathbf{x}$ in \mathbf{x} is calculated using the matrix expression $\Delta \mathbf{y} \approx \mathbf{T} \Delta \mathbf{x}$, where \mathbf{T} is an $m \times n$ sensitivity matrix. An element t_{ki} is obtained by computing the small shift in y_k due only to shift Δx_i in x_i , with all other components of \mathbf{x} held constant, and then dividing that shift in y_k by Δx_i . The $m \times m$ covariance matrix \mathbf{V}_y for the derived results \mathbf{y} is given approximately by

$$\mathbf{V}_y \approx \mathbf{T} \mathbf{V}_x \mathbf{T}^+,\tag{3}$$

where \mathbf{T}^+ is the transpose of \mathbf{T} . This is the well-known Law of Error Propagation.

We proceed further by examining the primary variable covariance matrix \mathbf{V}_x whose elements are $v_{xij} = e_{xi}c_{xij}e_{xj}$ (i, j = 1, n). The variables e_{xi} and e_{xj} are the uncertainties (standard deviations)

in \mathbf{x} , while the c_{xij} are the correlation coefficients between all these uncertainties. Since n is likely to be a very large number, we proceed to seek ways to simplify \mathbf{V}_x . Some uncertainties e_{xi} and/or sensitivity factors t_{ki} may be very small. Then, we can eliminate certain x_i from the primary variable set for the purpose of estimating uncertainties, but not for calculating the derived y_{0k} . Furthermore, many correlation coefficients c_{xij} may be zero or nearly so since many of the primary variables are mutually independent. Finally, reorganizing of the primary variables (*i.e.*, re-assigning the *i* positions) may enable grouping of the primary variables into Q (with Q < n) subsets, each one representing a mostly independent experiment *attribute* (such as sample mass, a specific background source, *etc.*). This *partitioning* exercise results in off-diagonal regions, where the elements of \mathbf{V}_x are either zero or nearly so. Then, we decompose \mathbf{V}_x into a sum of $Q \ n \times n$ independent submatrices \mathbf{V}_{xq} :

$$\mathbf{V}_x \approx \sum_{q=1,Q} \mathbf{V}_{xq}.$$
 (4)

Combining Eqs. (3) and (4) leads to

$$\mathbf{V}_{y} \approx \sum_{q=1,Q} \mathbf{T}_{q} \mathbf{V}_{xq} \mathbf{T}_{q}^{+} = \sum_{q=1,Q} \mathbf{V}_{yq}.$$
 (5)

The \mathbf{T}_q are submatrices of \mathbf{T} that interact in a significant way with submatrices \mathbf{V}_{xq} . All other elements of \mathbf{T} multiply with zero values of \mathbf{V}_x . Thus, the elements v_{ykl} of \mathbf{V}_y are given by

$$v_{ykl} \approx \sum_{q=1,Q} e_{yqk} c_{yqkl} e_{yql},\tag{6}$$

where e_{yqk} is the partial uncertainty in y_k due to attribute q and the c_{yqkl} are correlations only between these partial uncertainties. They are sometimes referred to as *micro-correlations*. The total uncertainty in y_k is thus given by

$$e_{yk} = \left[\sum_{q=1,Q} e_{yqk}^2\right]^{1/2}.$$
 (7)

The correlation matrix for the derived results \mathbf{y} has elements c_{ykl} which are given by

$$c_{ykl} = v_{ykl} / \left(v_{ykk} v_{yll} \right)^{1/2}.$$
 (8)

Equations (6)–(8) provide formulas used to characterize the uncertainties and correlations for a derived experimental data set \mathbf{y} in a manner compatible with applying the template approach in cataloguing partial uncertainties and their correlations for all the significant sources of uncertainty in an experiment. The present discussion shows that many approximations and assumptions are required to reduce complex experiments to this level of simplicity.

It is instructive to consider an even stronger simplification in modeling an experiment for uncertainty analysis purposes. First, assume that $\mathbf{x} = (x_1, \ldots, x_q, \ldots, x_Q)$. Each x_q is an independent positive variable which alone characterizes a particular independent experiment attribute q. Then, assume that algorithm $\mathbf{A}\{\mathbf{x}\} \to y$ for deriving a single physical quantity y reduces to the formula

$$y = \prod_{z=1,Z} f_z(\mathbf{x}),\tag{9}$$

where the f_z are Z simple functions of the parameters x_q . Examples are: $f_z(\mathbf{x}) = x_q$, or $1/x_q$, or $(x_q-x_{q'})$, or $1/(x_q-x_{q'})$, or $\exp(-c_q x_q)$. Here, x_q and $x_{q'}$ signify two distinct primary variables and c_q is a constant. Sensitivity parameters t_q (q = 1, Q) are calculated analytically as the partial derivatives $t_q = (\partial y/\partial x_q)$. Equation (9) symbolizes many of the formulas given in this paper for discussions of particular experimental types.

In summary, many assumptions and approximations are involved in justifying the use of templates to catalog experimental uncertainties and correlations. The most important of these is the notion that significant sources of experimental uncertainty can be attributed to various attributes of the experiment treated as mutually independent. Hence, care was taken here to group uncertainty sources such that they are mutually independent where possible.

4 Example of Applying a Template for Evaluations

Templates of expected measurement uncertainties were applied to estimate missing experimental uncertainties for measurements of neutron-induced ²³⁵U average prompt fission neutron multiplicities, $\bar{\nu}_p$, listed in Table I. This analysis of experimental data was undertaken for an evaluation of the ²³⁵U $\bar{\nu}_p$ in the fast range for ENDF/B-VIII.1 β_1 [21]. Most measurements employed the ratio liquid-scintillator method. For the uncertainty analysis, the EXFOR entry and literature of each experiment was studied in detail to extract all possible uncertainty sources. The uncertainty sources found through these analyses were compared to those that should be supplied for ratio liquid-scintillator measurements in Table 1 of Ref. [9]. This procedure aids in identifying missing uncertainty sources³. If uncertainty values were found to be missing, they were estimated based on template values. It is obvious from the right-hand side column of Table I (tabulating missing uncertainty sources) that uncertainty sources were missing for *all* of the measurements which, unfortunately, is the rule rather than the exception. Correlation coefficients for specific uncertainty sources were only rarely provided in the experiment literature, and were thus estimated using templates of expected measurement uncertainties in the majority of the cases.

The code ARIADNE [46] was then used to estimate total covariances for each correlated group of experiments. The code starts out by estimating covariances for each individual uncertainty source following the procedures outlined in Sec. 3. The same code was employed to perform two evaluations: One evaluation was undertaken with the generalized-least squares algorithm [47]. It was based on all experimental data and their covariances *including template uncertainties* listed in Table I. ENDF/B-VIII.0 mean values [48] and a diagonal covariance matrix with 100% uncertainties were used as non-informative prior. The second evaluation differed from the first one only in that no template uncertainties were considered for missing uncertainty sources.

The left-hand side of Fig. 1 shows that including these missing uncertainties into the evaluation via the templates of expected measurement uncertainties changes the evaluated ²³⁵U $\bar{\nu}_p$ by up to 1% in the energy range from 0.1–15 MeV. Evaluated uncertainties are increased by up to 25% when template uncertainties are considered. These changes are especially large around 5–7 MeV, the energy region of the opening of second-chance fission, where we know today, thanks to improved nuclear data, that systematic prompt fission neutron spectra and angular-distribution uncertainties for $\bar{\nu}_p$ measurements are usually the largest. There, template uncertainties incorporate our present-day knowledge into estimates of experimental uncertainties for measurements that largely took place from the 60s to the 80s, and significantly change evaluated mean values and uncertainties.

However, even the comparably smaller changes in ²³⁵U $\overline{\nu}_p$ from 0.1–4 MeV, maximally 0.5%, are significant when seen in the context of simulating the effective neutron multiplication factor, $k_{\rm eff}$, of fast highly-enriched uranium benchmarks [12]. To demonstrate this, the two ²³⁵U $\overline{\nu}_p$ evaluations were included in ENDF/B-VIII.0 data⁴ via ENDFtk [49], processed with NJOY-2016 [50], and then used to simulate $k_{\rm eff}$ of the Godiva and Flattop critical assemblies [12] using MCNP-6.2⁵ [51]. If we use

³The following uncertainty sources were identified as missing across several datasets: δc_{DG} are delayed gamma-ray, δb random-background, δc_{ff} false-fission, $\delta \omega$ impurity, $\delta \tau$ deadtime, $\delta \chi$ prompt fission neutron spectrum, δa angular distribution of fission neutrons, δd thickness of sample, and $\delta d_{s/m}$ sample-displacement uncertainties.

⁴The evaluated mean values were not smoothed after the evaluation in order to not artificially enhance or reduce the impact of templates.

⁵MCNP[®] and Monte Carlo N-Particle[®] are registered trademarks owned by Triad National Security, LLC, manager

Table I: ²³⁵U(n,f) $\bar{\nu}_p$ experimental data sets included in the example evaluation are identified with their EXFOR No., first author, and year of publication. The last column lists all uncertainty sources that were added based on templates for $\bar{\nu}$ in Table 1 of [9]. The information presented here was assembled from parts of Table I of LANL Report [21].

EXFOR #	First Author & Year	Added Template Unc.
40158.006	Bljumkina 1964 [22]	$\delta c_{DG},\delta b,\delta \omega,\delta au,\delta \chi$, $\delta a,\delta d$
21454.005/7/8	Colvin 1965 [23]	$\delta c_{DG}, \delta b, \delta c_{ff}, \delta \omega, \delta \tau, \delta d_{s/m}$
20025.002	Conde 1965 [24]	$\delta c_{DG}, \delta a, \delta d_{s/m}$
12337.003	Diven 1956 [25]	$\delta c_{DG},\delta \omega,\delta au,\delta a,\delta d,\delta d_{s/m}$
14297.007	Diven 1961 [26]	$\delta c_{DG}, \delta c_{ff}, \delta \omega, \delta \chi, \delta a, \delta d, \delta d_{s/m}$
21252.005	Fieldhouse 1966 [27]	$\delta c_{DG}, \delta b, \delta c_{ff}, \delta \omega, \delta \tau, \delta \chi, \delta a, \delta d$
21252.006	Fieldhouse $1966(2)$ [27]	$\delta c_{DG}, \delta b, \delta c_{ff}, \delta \omega, \delta \tau, \delta \chi, \delta a, \delta d$
20506.002	Frehaut 1980 [28]	$\delta c_{DG}, \delta b, \delta c_{ff}, \delta \omega, \delta \tau, \delta \chi, \delta a, \delta d, \delta d_{s/m}$
21785.003	Frehaut 1982 [29]	$\delta c_{DG}, \delta b, \delta c_{ff}, \delta \omega, \delta \tau, \delta \chi, \delta a, \delta d, \delta d_{s/m}$
13101.003	Gwin 1986 [30]	$\delta\chi, \delta a, \delta d_{s/m}$
12326.004	Hopkins 1963 [31]	$\delta c_{DG}, \delta c_{ff}, \delta \omega, \delta \chi, \dot{\delta a}, \delta d, \delta d_{s/m}$
14051.002	Howe $1976(2)$ [32]	$\delta c_{DG}, \delta b, \delta c_{ff}, \delta \omega, \delta \tau , \delta \chi, \delta a, \delta d, \delta d_{s/m}$
20427.002	Kaeppeler 1975 [33]	$\delta c_{ff},\delta au$
12419.002	Meadows 1962 [34]	$\delta c_{DG}, \delta b, \delta c_{ff}, \delta \omega, \delta \tau, \delta a, \delta d$
12391.002	Meadows 1965 [35]	$\delta c_{DG}, \delta b, \delta c_{ff}, \delta \omega, \delta \tau, \delta a, \delta d$
12399.002/4	Meadows 1967 [36]	$\delta c_{DG}, \delta b, \delta c_{ff}, \delta \omega, \delta \tau, \delta a, \delta d$
40033.002/4/6/8	Nesterov 1970 [37]	$\delta c_{DG}, \delta b, \delta c_{ff}, \delta a, \delta d, \delta d_{s/m}$
40132.002	Prokhorova 1967 [38]	$\delta c_{DG}, \delta b, \delta c_{ff}, \delta \omega, \delta \tau, \delta \chi, \delta a, \delta d, \delta d_{s/m}$
40392.002/3	Protopopov 1958 [39]	$\delta b, \delta c_{ff}, \delta \omega, \delta au, \delta \chi, \delta a, \delta d, \delta d_{s/m}$
40058.004	Savin 1970 [40]	$\delta c_{DG}, \delta c_{ff}, \delta \omega, \delta \tau, \delta a, \delta d, \delta d_{s/m}$
40262.002	Savin 1972 [41]	$\delta c_{DG}, \delta c_{ff}, \delta \omega, \delta \tau, \delta a, \delta d, \delta d_{s/m}$
40493.002	Savin 1979 [42]	$\delta c_{DG}, \delta c_{ff}, \delta \omega, \delta \tau, \delta a, \delta d, \delta d_{s/m}$
40388.006	Smirenkin 1958 [43]	$\delta b, \delta c_{ff}, \delta \omega, \delta au, \delta \chi, \delta a, \delta d$
20568.002	Soleihac 1970 [44]	$\delta c_{DG}, \delta b, \delta c_{ff}, \delta \omega, \delta \tau, \delta \chi, \delta a, \delta d$
30006.002	Walsh 1971 [45]	$\delta \omega, \delta a, \delta d$

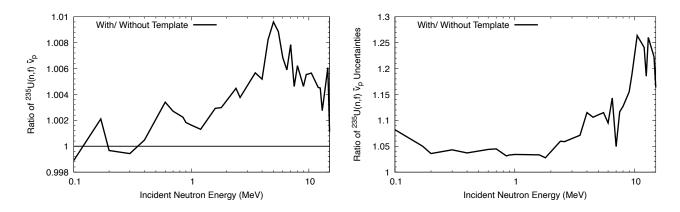


Figure 1: Evaluated mean values (left-hand side) and uncertainties (right-hand side) of 235 U(n,f) $\bar{\nu}_p$ using templates to estimate missing experimental uncertainties are shown as ratios to the evaluated mean values and uncertainties obtained from estimating experimental uncertainties only with information found in EXFOR and the literature of experimental data sets.

the ²³⁵U $\overline{\nu}_p$ with template uncertainties for missing uncertainty sources, the simulated Godiva k_{eff} is 262 pcm (0.262%) higher than if simulated with the evaluated ²³⁵U $\overline{\nu}_p$ without accounting for missing uncertainties by template values. This increase is 192 pcm (0.192%) for simulated Flattop k_{eff} values. This difference in simulated k_{eff} values is significant when compared to the experimental uncertainties for Godiva and Flattop k_{eff} , 100 and 300 pcm, respectively.

So, in short, evaluated mean values and uncertainties can change significantly, on the level of these observables as well as for application simulations, if missing experimental uncertainty sources are quantified via templates of expected measurement uncertainties. While the templates are a last resort in the absence of information from the experiment, they are a better option than to assume missing uncertainties are zero which gives data sets with poorly estimated uncertainties an unjustified higher weight and biases evaluations.

5 Conclusions and Outlook

Templates of expected measurement uncertainties were established by the CSEWG covariance committee and with the help of many other international contributors. These templates list expected uncertainty sources for each distinct measurement type of an observable. They also give ranges of uncertainties for most sources and estimates of correlation coefficients between uncertainties of each source. The uncertainty values were estimated conservatively based on information found for a broad range of experiments, from their literature, respective EXFOR entries, and expert judgment from experimenters. In addition to these templates, we list what information (what data, uncertainty information, data descriptors) evaluators need in order to include experimental data faithfully into the evaluation process. Templates were established in this effort for $(n, total), (n, \gamma), (n, xn)$ and (n, cp) reaction cross sections as well as prompt fission neutron spectra, average prompt and total fission neutron multiplicities, and fission product yields; they are separate papers in this issue and PhD theses [4–11]. Here, the general concept of these templates was introduced, their history, use cases (as a checklist for experimenters, EXFOR compilers, and journal editors; for evaluators, to identify and estimate missing uncertainties), and mathematical basis. An example was given using evaluations of ²³⁵U average prompt fission neutron multiplicities. It showcased that estimating missing uncertainties via templates of expected uncertainties, instead of assuming them to be zero, can significantly impact evaluated mean values and uncertainties. In fact, these differences in evaluated mean values lead to changes in

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simulated effective neutron multiplication factors of the Godiva and Flattop critical assemblies that are three times larger or two thirds of their experimental uncertainties, respectively.

In the near future, these templates and the information needed for evaluations will be concisely summarized on the NNDC homepage of BNL for an easy access by both evaluators and experimenters. We also plan to engage journal editors with the hope that they may propose to referees that they use the templates when reviewing papers. This information could help referees point out if information is missing in the journal articles that could potentially improve the usability of the data. If this information would be provided by experimenters, the content of the papers could be more easily used by evaluators for evaluation purposes. Also, if all pertinent information is in the paper or supplemental material, it is more likely to be recorded in the EXFOR database. In addition to that, we will provide these templates for EXFOR compilers in the hope that they ask experimenters for missing information compared to the template leading, thus, to more complete new EXFOR entries for evaluation purposes. These templates will also be used as part of Subgroup 50 of the OECD "Working Party on International Nuclear Data Evaluation Co-operation" at the NEA [52]. This subgroup aims at developing an automatically readable, comprehensive and curated experimental reaction database that starts off from a few selected entries of EXFOR. The structure of this database (especially the uncertainties) will be aligned such that it can contain uncertainty sources expected from the templates and hold information needed by evaluators. The template uncertainties might also be used to provide otherwise missing uncertainties for data sets in the database.

It should be emphasized that the templates should not be understood as immutable laws but rather a snapshot in time. Also, they will not apply to all possible measurement types; experimenters and evaluators should use their judgment in how far they are applicable. They should be also understood as a "living document" in as far as our understanding of uncertainty sources evolves over time as we uncover new physics effects with ever improving technology and research. Consequently, these templates will be updated periodically on the NNDC webpage based on this improved understanding. Templates for additional observables or measurement types might be established. The aim of this continuous update is that the templates help to perform the best possible uncertainty quantification of experimental data for evaluation purposes at a specific time to result in more realistic evaluated mean values and covariances in our nuclear-data libraries.

Conflicts of Interest

The authors declare that they have no competing interests to report.

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Data availability statement

The data that were created associated with this manuscript are all within its main text, figures and tables.

Author contribution statement

DN wrote the original draft, undertook the evaluation and simulation example. DS and SC contributed text to the first draft. All authors reviewed the manuscripts. All authors were involved in the conception of the template idea, investigations and data curation associated with the article and discussions on uncertainty quantification—either by taking part at the CSEWG mini-CSEWG workshop on templates 2019, or by discussions afterwards.

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