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Structural and elastic properties of perovskite HoMnO₃ crystal

structures from ab-initio calculations

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Moussa Sougoti ¹, Sié Zacharie Kam ¹, Jun Chen ², and Pierre Ruterana ³

Abstract

The structural and elastic properties of the oxide perovskite $HoMnO_3$ have been investigated by density-functional theory (DFT) implemented on the Quantum ESPRESSO code for the hexagonal, orthorhombic, rhombohedral and cubic crystal structures in the non-magnetic (NM), ferromagnetic (FM) and antiferromagnetic (AFM) configurations. The results show that all these compounds are thermodynamically stable, the hexagonal and the orthorhombic being the most stables in agreement with experimental results. The calculated bulk modulus, B, is about 168.5 ± 1.0 GPa and 178.9 ± 1.0 GPa for hexagonal structure in FM and configurations, respectively, and 188.7 ± 0.6 GPa and 175.6 ± 2.1 GPa for orthorhombic structure in FM and AFM configurations, respectively. These values and those of the elastic constants C_{ij} in the present work are comparable to values recently obtained with DFT calculations and experimentally for other perovskites RMnO₃ (R=Eu, Gd, Tb and Dy). The calculated Poisson's ratio is about 0.19; 0.27; 0.23 and 0.3 for hexagonal, orthorhombic, rhombohedral and cubic structure, respectively. The calculated Pugh's ratio is about 1.30; 1.77-1.98; 1.54-1.60 and 2.11, respectively. These results show that the perovskite HoMnO₃ tends to be brittle in hexagonal

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- 27 phase and ductile in cubic phase. In the orthorhombic or rhombohedral phase, it is near brittle-
- 28 ductile boarder line.
- 29 Keywords: HoMnO₃; manganite crystal structures; manganite elastic constants; ab initio
- 30 calculations; Quantum Espresso

I. INTRODUCTION

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The manganese-based perovskite oxides of the RMnO3 type recognized as multiferroic materials have attracted technological interest because they exhibit at least two ferroic orders, (anti)ferroelectricity, (anti)ferromagnetism and ferroelasticity, within a single phase offering the possibility of controlling the electrical polarization under a high magnetic field, or vice versa. They offer a wide range of potential applications such as high-density magnetic recording, magnetoresistive sensors and magnetic refrigeration [1], [2]. Under normal temperature and pressure conditions, the RMnO₃ perovskites can be structurally divided into three subgroups depending on the size of the rare earth element R. The former subgroup with small rare earth ionic radius (R = Sc, Y, Ho, Er, Tm, Yb and Lu), these perovskite crystallize in a hexagonal lattice named h-RMnO₃, mainly in the P6₃cm space group. The second subgroup, with large rare earth ionic radius, crystallizes in an orthorhombic structure and is designated o-RMnO₃, mainly in the *Pnma* space group. They are the compounds with R = La, Ce, Pr, Nd, Pm, Sm, Eu, Gd, Tb and Dy. The last subgroup (R = Ho, Y or Dy), with medium rare earth ionic radius, crystallizes either in hexagonal or orthorhombic structure depending on the synthesis conditions. Experimentally, it has been reported that the hexagonal phase of RMnO₃ can be transformed into orthorhombic phase at high temperature and pressure [3], [4]. To our knowledge, there is no systematic study including different crystal systems (cubic, hexagonal, orthorhombic, rhombohedral, etc.) of such perovskite RMnO₃ since some were synthesized under specific experimental conditions [5]. Indeed, previous theoretical works on HoMnO₃ reported the following crystal structures: hexagonal [6], [7]; orthorhombic [8], [9]; rhombohedral [10], and none of these works dealt with different crystal systems. In this work, we have carried out a systematic DFT study based on Quantum ESPRESSO calculations of the structural and elastic properties of perovskite HoMnO₃ in its hexagonal (h-HMO), orthorhombic (o-HMO), rhombohedral (r-HMO) and cubic (c-HMO) structures. They

- are in $P6_3cm$, Pnma, $R\overline{3}c$ and $Pm\overline{3}m$ space groups, respectively. It has to be noticed that
- 57 there is a lack of experimental or theoretical data on elastic constants of this perovskite.
- Therefore, the objective of this study is to provide a better comparability of the obtained results.

II. THEORETICAL APPROACHES

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2.1. Potential and structural properties

- The Quantum Espresso code for first-principles calculations based on density functional
- 62 theory (DFT) is employed as potential. This performs electronic structure calculations and
- materials (metals, insulators and semiconductors) modelling with high accuracy.
- Quantum Espresso supports Norm-Conserving (NC), Ultrasoft (US), and Projector-
- 65 Augmented Wave (PAW) pseudopotentials (PPs). It also supports exchange-correlation
- 66 functions of the local density approximation (LDA), generalized gradient approximation
- 67 (GGA), or more advanced type.
- To run Quantum Espresso, some parameters are fixed. This includes, (i) the valence states
- describing the atomic cores; (ii) the pseudopotential describing the ion-electron interactions;
- 70 (iii) the exchange-correlation functional; (iv) the convergence criterion on total energy for ionic
- 71 minimization (etot conv thr); (v) the convergence criterion on forces for ionic minimization
- 72 (forc conv thr); (vi) the k-point mesh to determine the first Brillouin zone; (vii) the kinetic
- energy cutoff for wavefunctions (ecutwfc) and (viii) the kinetic energy cutoff for charge density
- and potential (ecutrho). For this work, (i) the valence states are set to $(5s^26s^{1.5}5p^66p^{0.5}5d^1)$,
- 75 $(3s^23p^63d^54s^2)$, and $(2s^22p^4)$ for the Ho, Mn, and O atoms, respectively; (ii) the ion-electron
- interactions are described by the PAW method [11]; (iii) the exchange-correlation functional
- employed is that of Perdew-Burke-Ernzerhof parameterization of the generalized gradient
- 78 approximation (PBE-GGA) [12]; (iv) the energy convergence criterion for electronic self-
- 79 consistency is set to 10^{-6} u.a; (v) the atomic forces convergence criterion is set to 10^{-4} u.a; (vi)

the k-point mesh is set to $9 \times 9 \times 9$; (vii) the kinetic energy cutoff for wavefunctions is set to 80 Ry and (viii) the kinetic energy cutoff for charge density and potential is set to 400 Ry. It has to be noticed that the values of these last three parameters are fixed after the energy convergence test calculations (Fig 1).

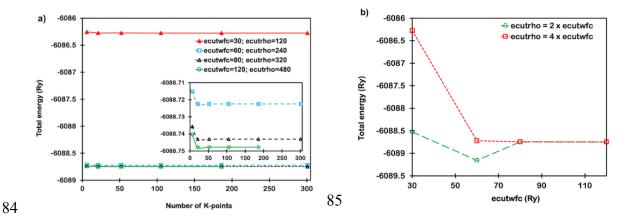


Fig1: Convergence test of total energy as a function of: a) k-points mesh; b) kinetic energy cutoff for wavefunctions (ecutwfc). In (a), the convergence is assumed to occur with 52-points that correspond to a $6 \times 6 \times 6$ k-points grid and undependably of the ecutwfc value. In (b), the convergence is assumed to occur with ecutwfc=80 Ry and undependably of the ecutrho value.

Geometry optimizations are performed in the supercell method using the Broyden–Fletcher–Goldfarb–Shanno (BFGS) quasi-newton algorithm [13]; all atoms were allowed to relax and reach minimum energies when the atomic forces become less than 10⁻⁴ u.a. as previously mentioned.

When the lower energy relaxed structure is obtained, the formation energy is calculated to ensure that the system is thermodynamically stable. For compound materials such as $HoMnO_3$ in equilibrium with a reservoir of Ho, Mn and O atoms, the formation energy $E_{form}(D)$ of a given structure D is defined as [14]:

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$$E_{form}(D) = E_{total}(D) - \mu_{H_O} \times n_{H_O} - \mu_{M_n} \times n_{M_n} - \mu_O \times n_O$$
 (1)

where $E_{total}(D)$ is the total energy of the supercell while μ_{H_O} μ_{M_n} and μ_O are the Ho, Mn and O chemical potentials, respectively. The values of these chemical potentials have been obtained from Quantum Espresso calculations in the C19_alpha_Sm prototype (space group = R-3m) for holmium (Ho), Mn(c158) prototype (space group = I-43m) for manganese (Mn) and BaP3 prototype (space group = C2/m) for oxygen (O). The quantities n_{H_O} , n_{M_n} , and n_O correspond to the numbers of Ho, Mn and O atoms, respectively. The numbers of atoms per unit cell and its repartition per atomic specie, $n_{tot}(n_{H_O}, n_{M_n}, n_O)$ are: 30(6, 6, 18) for h-HMO or r-HMO; 20(4, 4, 12) for o-HMO and 5(1, 1, 3) for c-HMO.

The most stable structure is obtained by comparing the energy of a given structure (i) to a reference structure (ref) by evaluating the relative energy $\Delta E(i)$ defined as:

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$$\Delta E(i) = E_{form}(i) - E_{form}(ref)$$
 (2)

where $E_{form}(i)$ and $E_{form}(ref)$ are the formation energies of the structure (i) and the reference structure, respectively. In present calculations, the reference structure is set to the h-HMO structure in the FM configuration.

2.2. Elastic constant calculations

The elastic properties of a crystal can be characterized by independent elastic constants, namely C_{ij} . The total number of independent components of the elastic constant tensor depends on the symmetry of the crystal. There are two approaches for calculating elastic constants: the energy-strain $(E-\varepsilon)$ method and the stress-strain $(\sigma-\varepsilon)$ method. For more details on these methods, see the publications of [15], [16], [17]. From these two methods, the energy-strain is a more common-place for calculations using DFT approach. In this method, the energy of the crystal is calculated for different values of the strain ε . Then, its evolution curve is fitted as a function of ε by a polynomial and the value of the second derivative at $\varepsilon = 0$ related to those of C_{ij} is deduced. It should be noted that there are two parameters to be chosen for this method:

the polynomial degree and the ε region on which the adjustment is performed. In the present work, the study focuses on ε region ranging from -0.06 to 0.06 with a step of 0.02. This gives rise to seven self-consistent energy calculations for a given C_{ij} calculation or their combination. The fitting of polynomial of order 3 and 4 was performed, allowing the determination of average values and deviations.

It is well known that the elastic computation via the energy-strain relationship can lead to erroneous results at non-zero pressure. Then, when the elastic constants are calculated, the elastic stabilities of the four investigated structures are tested according to the stability criteria presented in Table 1.

Table 1: Elastic stability of crystal systems

Crystal systems	Point groups	Space groups	Born stability criteria [18]
Cubic	m3m	Pm3m	$C_{11} - C_{12} > 0; C_{11} + 2C_{12} > 0; C_{44} > 0$
Hexagonal	6mm	P6 ₃ cm	$ \begin{cases} C_{11} > C_{12} ; \ 2C_{13}^2 < C_{33}(C_{11} + C_{12}) \\ C_{44} > 0; \ C_{66} > 0 \end{cases} $
Orthorhombic	Mmm	Pnma	$\begin{cases} C_{11} > 0; \ C_{11}C_{22} > C_{12}^2; \\ C_{11}C_{22}C_{33} + 2C_{12}C_{13}C_{23} - C_{11}C_{23}^2 - C_{22}C_{13}^2 - C_{33}C_{12}^2 > 0 \\ C_{44} > 0; \ C_{55} > 0; C_{66} > 0 \end{cases}$
Rhombohedral	3m	R3c	$\begin{cases} C_{11} > C_{12} ; \ C_{44} > 0 \\ C_{13}^2 < \frac{1}{2}C_{33}(C_{11} + C_{12}) \\ C_{14}^2 < \frac{1}{2}C_{44}(C_{11} - C_{12}) = C_{44}C_{66} \end{cases}$

To predict the plastic behavior of materials, the most widely used criteria are the Poisson's ratio, $\nu = \frac{3B-2G}{2(3B+G)}$, and the Pugh's ratio, $\frac{B}{G}$, where B is the bulk modulus and G is the shear modulus. Each of these ratios is related to the competition between two mechanical processes, fracture and plasticity. For a given material, if plasticity (fracture) is easier, then it will tend to

be ductile (brittle). The critical value is 0.26 and 1.75 for the Poisson's ratio and the Pugh's

ratio, respectively [19][20]. The material is considered ductile (brittle) for a value of the Poisson's ratio or Pugh's ratio greater (smaller) than the corresponding critical value. In the present work, the Poisson's ratio and the Pugh's ratio are calculated according to Voigt-Reuss-Hill approximations [21].

III RESULTS AND DISCUSSION

3.1 Structural and magnetic properties

The structural properties which have been investigated are the lattice parameters, the formation energies and the relative stabilities of the different structures. The magnetic behaviour is determined by taking into account the non-magnetic (NM), ferromagnetic (FM) and the anti-ferromagnetic (AFM) spin configurations of the studied crystal systems (h-HMO, o-HMO, r-HMO and c-HMO). To this end, geometrical optimization calculations were first performed as described previously. The energy versus volume curves for different crystal phases in FM and AFM configurations of the HoMnO₃ structure is presented in figure 2. It comes that the lowest energy configuration for HoMnO₃ is the hexagonal structure (Ishibashi et al.). The least stable phase is the cubic structure. The minimum energy of the orthorhombic structure is closer to that of the hexagonal structure than the rhombohedral structure. The FM and AFM configurations of the hexagonal, orthorhombic or rhombohedral structure have almost identical evolution curves.

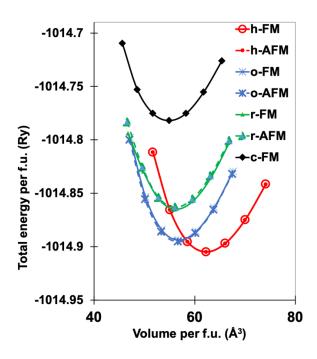


Fig2: Energy versus volume for HoMnO₃ different crystal structures in FM and FM configurations. The number of atoms in the unit cell is 30, 20, 30 and 5 for h-HMO, o-HMO, r-HMO and c-HMO, respectively. This gives rise to the unit formula (f.u.) per unit cell of 6, 4,

6 and 1 for h-HMO, o-HMO, r-HMO and c-HMO, respectively. On the legend, h-FM refers to

h-HMO in FM configuration.

3.1.1. Lattice parameters

The lattice parameters in the FM, AFM and NM configurations of h-HMO, o-HMO, r-HMO and c-HMO relaxed atomic structures (figures 3-6) are presented in Table 2 in comparison with reported theoretical and experimental data. The h-HMO lattice parameters values are in good agreement with the recent experimental results of Ishibashi et al. [4]. Also, the o-HMO lattice parameters are in agreement with the experimental results of Alonso et al. [22] than theoretical results reported in [23], [8]. In the case of r-HMO and c-HMO lattice parameters, in absence of experimental data, our results compare well with those of theoretical reported in [24].

The good agreement of the obtained values with those of experimental demonstrates the accuracy of the quantum expresso calculations.

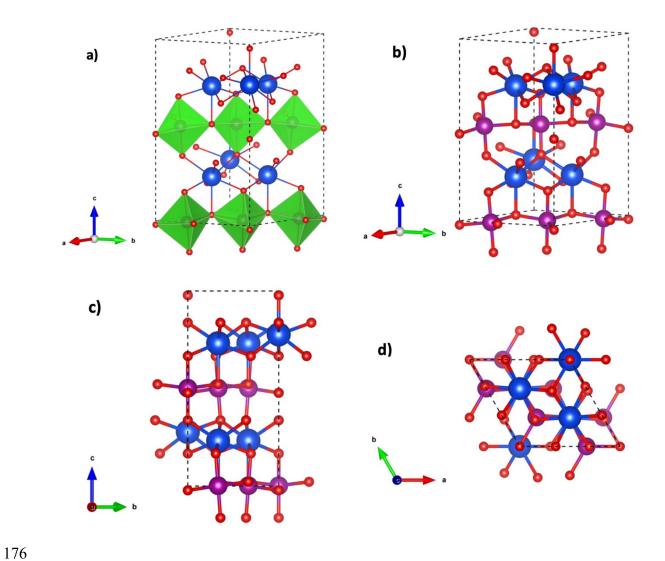


Fig3: Relaxed atomic structure of HoMnO₃ hexagonal crystal phase in FM configuration. a) structure along [001]; (b) the real cell; (c) in a-direction; and in c-direction. The blue, purple and red balls correspond to Ho, Mn and O atoms, respectively. The MnO₅ trigonal bipyramid is represented in green. The unit cell is shown by dashed lines.

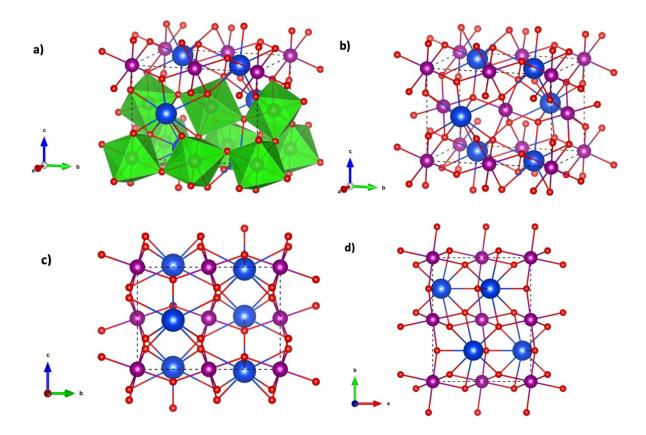


Fig4: Relaxed atomic structure of HoMnO₃ orthorhombic crystal phase in FM configuration. a) structure along [001]; (b) the real cell; (c) in a-direction; and in c-direction. The blue, purple and red balls correspond to Ho, Mn and O atoms, respectively. The MnO₆ octahedra are represented in green. The unit cell is shown by dashed lines.

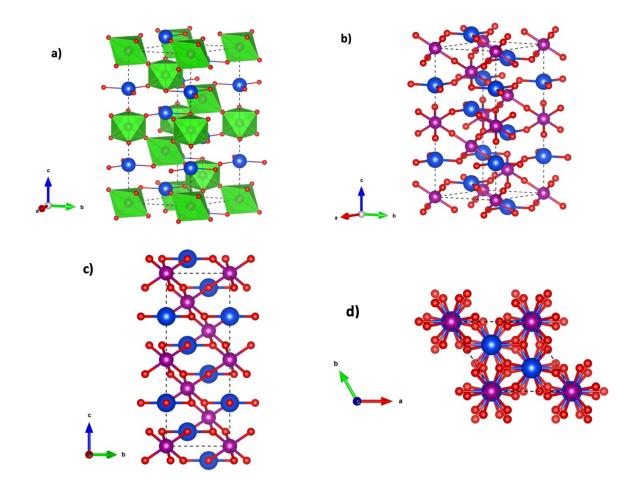


Fig5: Relaxed atomic structure of HoMnO₃ rhombohedral crystal phase in FM configuration. a) structure along [001]; (b) the real cell; (c) in a-direction; and in c-direction. The blue, purple and red balls correspond to Ho, Mn and O atoms, respectively. The MnO₆ octahedra are represented in green. The unit cell is shown by dashed lines.

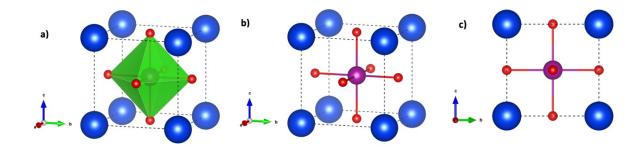


Fig6: Relaxed atomic structure of HoMnO₃ cubic crystal phase in FM configuration. a) structure along [001]; (b) the real cell; (c) in a-direction; and in c-direction. The blue, purple and red balls correspond to Ho, Mn and O atoms, respectively. The MnO₆ octahedra is represented in green. The unit cell is shown by dashed lines.

Table 2: Lattice parameters, a, b and c, in angstrom (\red{A}), equilibrium unit cell volume, V, in \red{A}^3 , formation energy, E_{form} , in electron-volt per atom (\red{eV} /atom), and relative energy, ΔE , in millielectron-volt per atom (\red{meV} /atom) obtained with PBE-GGA-APW pseudopotentials DFT calculations for HoMnO₃ crystal structures in non-magnetic (NM), ferromagnetic (FM) and antiferromagnetic (AFM) configurations.

NM	Structure	a (Å)	b (Å)	c (Å)	V (Å ³)	E _{form} (eV/atom)	ΔE (meV/atom)	Ref.
NM	h-HMO							
N1	NIM		6.0562	11.3160	359.68	-2.435		$P.W.^{1}$
FM 6.1300 6.1300 11.4340 372.06 -2.965 0 [24] 6.1450 6.1450 11.4190 373.62 NI NI NI [4] 6.1382 6.1382 11.4118 372.61 NI NI NI [25] 6.1413 6.1314 11.4122 372.75 NI NI NI [26] 6.1477 6.1477 11.4898 376.07 NI 0 [7] AFM 6.1412 6.1412 11.4147 373.42 -2.746 0 P.W. 6.1522 6.1522 11.5125 377.36 NI -24 3 [7] O-HMO NM 5.5440 7.3756 5.1065 208.81 -2.515 230 P.W. 5.8461 7.3742 5.2681 227.11 -2.716 30 P.W. FM 5.7100 7.4640 5.2570 224.06 -2.874 31 [24] 5.8354 7.3606 5.2572 225.81 [22] 5.7790 7.4410 5.2130 224.20 [23] AFM 5.9039 7.3292 5.2387 226.68 -2.720 26 P.W. 5.7500 7.2530 5.1800 216.01 679 4 [8] F-HMO NM NI NI NI NI NI NI NI 631 [10] FM 5.4700 5.4700 12.8230 332.27 -2.874 122 [24] 5.5960 5.5960 13.1210 355.84 NI NI NI [10] AFM NI [10] AFM 5.4700 5.4701 12.8230 332.27 -2.874 122 [24] 5.5960 5.5960 13.1210 355.84 NI NI NI [10] AFM NI [10] AFM 5.4771 5.4771 12.9567 336.61 -2.632 114 P.W. NM 3.7344 3.7344 3.7344 52.08 -2.240 506 P.W. FM 3.8042 3.8042 3.8042 54.92 -2.411 334 P.W.	INIVI	NI^2	NI	NI	NI	(A') (eV/atom) (meV/atom) 59.68	[7]	
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FM		6.1300	6.1300	11.4340	372.06	-2.965	0	[24]
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AFM 6.1522 6.1522 11.5125 377.36 NI -24 ³ [7] o-HMO NM 5.5440 7.3756 5.1065 208.81 -2.515 230 P.W. 5.8461 7.3742 5.2681 227.11 -2.716 30 P.W. 5.7100 7.4640 5.2570 224.06 -2.874 31 [24] 5.8354 7.3606 5.2572 225.81 [22] 5.7790 7.4410 5.2130 224.20 [23] AFM 5.9039 7.3292 5.2387 226.68 -2.720 26 P.W. r-HMO NM NI NI NI NI NI NI 679 ⁴ [8] r-HMO NM 5.3910 5.3910 12.4293 312.84 -2,450 296 P.W. M NI NI NI NI NI NI 631 [10] FM 5.4894 5.4894 12.9427 337.76 -2.637		6.1477	6.1477	11.4898	376.07	NI	0	[7]
6.1522 6.1522 11.5125 3/7.36 NI -24 3 [7] O-HMO NM 5.5440 7.3756 5.1065 208.81 -2.515 230 P.W. 5.8461 7.3742 5.2681 227.11 -2.716 30 P.W. 5.7100 7.4640 5.2570 224.06 -2.874 31 [24] 5.8354 7.3606 5.2572 225.81 [22] [23] AFM 5.9039 7.3292 5.2387 226.68 -2.720 26 P.W. FHMO 5.3910 7.2530 5.1800 216.01 679 4 [8] r-HMO NM NI NI NI NI NI NI NI One 679 4 [8] r-HMO NM 5.3910 5.3910 12.4293 312.84 -2,450 296 P.W. FM 5.4894 5.4894 12.9427 337.76 <td< td=""><td>AEM</td><td>6.1412</td><td>6.1412</td><td>11.4147</td><td>373.42</td><td>-2.746</td><td>0</td><td>P.W.</td></td<>	AEM	6.1412	6.1412	11.4147	373.42	-2.746	0	P.W.
NM 5.5440 7.3756 5.1065 208.81 -2.515 230 P.W. 5.8461 7.3742 5.2681 227.11 -2.716 30 P.W. FM 5.7100 7.4640 5.2570 224.06 -2.874 31 [24] 5.8354 7.3606 5.2572 225.81 [22] 5.7790 7.4410 5.2130 224.20 [23] AFM 5.9039 7.3292 5.2387 226.68 -2.720 26 P.W. r-HMO NI NI NI NI NI NI NI NI 679 4 [8] r-HMO NI NI NI NI NI NI NI NI NI 09 P.W. FM 5.4894 5.4894 12.9427 337.76 -2.637 109 P.W. AFM 5.4771 5.4771 12.9567 336.61 -2.632 114 P.W. AFM NI	ArW	6.1522	6.1522	11.5125	377.36	NI	311 394 ³ 0 0 0 NI NI NI 0 0 -24 ³ 230 30 31 26 679 ⁴ 296 631 109 122 NI 114 28; 112	[7]
FM	o-HMO							
FM 5.7100 7.4640 5.2570 224.06 -2.874 31 [24] 5.8354 7.3606 5.2572 225.81 [22] 5.7790 7.4410 5.2130 224.20 [23] AFM 5.9039 7.3292 5.2387 226.68 -2.720 26 P.W. 5.7500 7.2530 5.1800 216.01 679 4 [8] r-HMO NI	NM	5.5440	7.3756	5.1065	208.81	-2.515	230	P.W.
FM 5.8354 7.3606 5.2572 225.81 [22] 5.7790 7.4410 5.2130 224.20 [23] AFM 5.9039 7.3292 5.2387 226.68 -2.720 26 P.W. 5.7500 7.2530 5.1800 216.01 679 4 [8] r-HMO NM NI NI NI NI NI NI NI One 296 P.W. M NI NI NI NI NI NI NI 631 [10] FM 5.4894 5.4894 12.9427 337.76 -2.637 109 P.W. FM 5.4700 5.4700 12.8230 332.27 -2.874 122 [24] 5.5960 5.5960 13.1210 355.84 NI NI NI [10] c-HMO NM 3.7344 3.7344 3.7344 52.08 -2.240 506 P.W.	h-HMO	5.8461	7.3742	5.2681	227.11	-2.716	30	P.W.
S.8354 7.3606 S.2572 225.81 [22] 5.7790 7.4410 5.2130 224.20 [23] AFM 5.9039 7.3292 5.2387 226.68 -2.720 26 P.W. 5.7500 7.2530 5.1800 216.01 679 \(^4\) [8] F-HMO NI		5.7100	7.4640	5.2570	224.06	-2.874	31	[24]
AFM 5.9039 7.3292 5.2387 226.68 -2.720 26 P.W. 5.7500 7.2530 5.1800 216.01 679 4 [8] r-HMO NM 5.3910 5.3910 12.4293 312.84 -2,450 296 P.W. NI NI NI NI NI 631 [10] 5.4894 5.4894 12.9427 337.76 -2.637 109 P.W. 5.4700 5.4700 12.8230 332.27 -2.874 122 [24] 5.5960 5.5960 13.1210 355.84 NI NI [10] AFM 5.4771 5.4771 12.9567 336.61 -2.632 114 P.W. NI NI NI NI NI NI NI 28; 112 [10] c-HMO NM 3.7344 3.7344 3.7344 52.08 -2.240 506 P.W. EM 3.8042 3.8042 54.92 -2.411 334 P.W.	FIVI	5.8354	7.3606	5.2572	225.81			[22]
AFM 5.7500 7.2530 5.1800 216.01 679 4 [8] r-HMO NM 5.3910 5.3910 12.4293 312.84 -2,450 296 P.W. NM NI NI NI NI NI NI 631 [10] 5.4894 5.4894 12.9427 337.76 -2.637 109 P.W. FM 5.4700 5.4700 12.8230 332.27 -2.874 122 [24] 5.5960 5.5960 13.1210 355.84 NI NI NI [10] AFM NI NI NI NI NI NI NI 28; 112 [10] c-HMO NM 3.7344 3.7344 3.7344 52.08 -2.240 506 P.W. FM 3.8042 3.8042 54.92 -2.411 334 P.W.		5.7790	7.4410	5.2130	224.20			[23]
r-HMO 5.3910 5.3910 12.4293 312.84 -2,450 296 P.W. NM NI NI NI NI NI NI NI NI 100 FM 5.4894 5.4894 12.9427 337.76 -2.637 109 P.W. FM 5.4700 5.4700 12.8230 332.27 -2.874 122 [24] 5.5960 5.5960 13.1210 355.84 NI NI NI I0] AFM 5.4771 5.4771 12.9567 336.61 -2.632 114 P.W. c-HMO NI NI NI NI NI NI NI NI 28; 112 [10] c-HMO NM 3.7344 3.7344 3.7344 52.08 -2.240 506 P.W. EM 3.8042 3.8042 54.92 -2.411 334 P.W.	A EM	5.9039	7.3292	5.2387	226.68	-2.720	26	P.W.
NM 5.3910 5.3910 12.4293 312.84 -2,450 296 P.W. NI NI NI NI NI NI NI 631 [10] 5.4894 5.4894 12.9427 337.76 -2.637 109 P.W. FM 5.4700 5.4700 12.8230 332.27 -2.874 122 [24] 5.5960 5.5960 13.1210 355.84 NI NI NI I0] AFM 5.4771 5.4771 12.9567 336.61 -2.632 114 P.W. c-HMO NI NI NI NI NI NI NI NI 28; 112 [10] c-HMO NM 3.7344 3.7344 52.08 -2.240 506 P.W. SM 3.8042 3.8042 54.92 -2.411 334 P.W.	ArW	5.7500	7.2530	5.1800	216.01		311 394 ³ 0 0 NI NI NI 0 0 -24 ³ 230 30 31 26 679 ⁴ 296 631 109 122 NI 114 28; 112 506 334	[8]
NM NI NI NI NI NI NI 631 [10] 5.4894 5.4894 12.9427 337.76 -2.637 109 P.W. FM 5.4700 5.4700 12.8230 332.27 -2.874 122 [24] 5.5960 5.5960 13.1210 355.84 NI NI NI [10] AFM 5.4771 5.4771 12.9567 336.61 -2.632 114 P.W. C-HMO NI NI NI NI NI NI 28; 112 [10] c-HMO NM 3.7344 3.7344 52.08 -2.240 506 P.W. FM 3.8042 3.8042 54.92 -2.411 334 P.W.	r-HMO							
NI NI NI NI NI NI NI 631 [10] 5.4894 5.4894 12.9427 337.76 -2.637 109 P.W. FM 5.4700 5.4700 12.8230 332.27 -2.874 122 [24] 5.5960 5.5960 13.1210 355.84 NI NI NI I0] AFM 5.4771 5.4771 12.9567 336.61 -2.632 114 P.W. c-HMO NI NI NI NI NI NI NI 28; 112 [10] c-HMO NM 3.7344 3.7344 52.08 -2.240 506 P.W. FM 3.8042 3.8042 54.92 -2.411 334 P.W.	NIM	5.3910	5.3910	12.4293	312.84	-2,450	296	P.W.
FM 5.4700 5.4700 12.8230 332.27 -2.874 122 [24] 5.5960 5.5960 13.1210 355.84 NI NI NI I0] AFM 5.4771 5.4771 12.9567 336.61 -2.632 114 P.W. NI NI NI NI NI NI NI 28; 112 [10] c-HMO NM 3.7344 3.7344 52.08 -2.240 506 P.W. FM 3.8042 3.8042 3.8042 54.92 -2.411 334 P.W.	INIVI	NI	NI	NI	NI	NI	631	[10]
5.5960 5.5960 13.1210 355.84 NI NI [10] AFM 5.4771 5.4771 12.9567 336.61 -2.632 114 P.W. NI NI NI NI NI NI 28; 112 [10] c-HMO NM 3.7344 3.7344 52.08 -2.240 506 P.W. FM 3.8042 3.8042 3.8042 54.92 -2.411 334 P.W.		5.4894	5.4894	12.9427	337.76	-2.637	109	P.W.
AFM 5.4771 5.4771 12.9567 336.61 -2.632 114 P.W. NI NI NI NI NI NI 28; 112 [10] c-HMO NM 3.7344 3.7344 3.7344 52.08 -2.240 506 P.W. 3.8042 3.8042 54.92 -2.411 334 P.W.	FM	5.4700	5.4700	12.8230	332.27	-2.874	122	[24]
AFM NI NI NI NI NI 28; 112 [10] c-HMO NM 3.7344 3.7344 52.08 -2.240 506 P.W. FM 3.8042 3.8042 3.8042 54.92 -2.411 334 P.W.		5.5960	5.5960	13.1210	355.84	NI	NI	[10]
NI NI NI NI NI 28; 112 [10] c-HMO NM 3.7344 3.7344 52.08 -2.240 506 P.W. FM 3.8042 3.8042 3.8042 54.92 -2.411 334 P.W.	A EM	5.4771	5.4771	12.9567	336.61	8 -2.435 311 NI 394 ³ 1 -2.746 0 6 -2.965 0 2 NI NI 1 NI 5 NI NI 7 NI 0 2 -2.746 0 6 NI -24 ³ 1 -2.515 230 1 -2.716 30 6 -2.874 31 1 0 8 -2.720 26 1 679 ⁴ 4 -2,450 296 NI 631 6 -2.637 109 7 -2.874 122 4 NI NI 1 NI 1 -2.632 114 NI 28; 112	114	P.W.
NM 3.7344 3.7344 52.08 -2.240 506 P.W. 3.8042 3.8042 54.92 -2.411 334 P.W.	ArW	NI	NI	NI	NI	NI	28; 112	[10]
EM 3.8042 3.8042 3.8042 54.92 -2.411 334 P.W.	с-НМО							
H/N/I	NM	3.7344	3.7344	3.7344	52.08	-2.240	506	P.W.
ΓΙΝΙ 2.0250 2.0250 2.0250 55.07 2.620 2.67 [0.4]	FM AFM O-HMO NM FM AFM r-HMO NM FM AFM c-HMO NM	3.8042	3.8042	3.8042	54.92	-2.411	334	P.W.
3.8250 3.8250 35.8250 35.97 -2.639 357 [24]	FM	3.8250	3.8250	3.8250	NI NI 394 ³ 373.51 -2.746 0 372.06 -2.965 0 373.62 NI NI 372.61 NI NI 372.75 NI NI 376.07 NI 0 373.42 -2.746 0 377.36 NI -24 ³ 208.81 -2.515 230 227.11 -2.716 30 224.06 -2.874 31 225.81 224.20 226.68 -2.720 26 216.01 679 ⁴ 312.84 -2,450 296 NI NI 631 337.76 -2.637 109 332.27 -2.874 122 355.84 NI NI 336.61 -2.632 114 NI NI 28; 112	[24]		

¹ Present work

² Not indicated in the publication

³ According to [7], the h-HMO relative energies with respect to the AFM configuration are 0.72 and 12.53 eV in FM and NM configurations, respectively. When taking the FM configuration as reference and considering that its supercell contains 30 atoms, we deduce that the h-HMO relative energies with respect to the FM configuration are -24 and 394 meV/atom in the AFM and NM configurations, respectively.

⁴ According to [8], the o-HMO total energies are -112105.73656421 and -112104.738371 Ry in FM and AFM configurations, respectively. When considering that its supercell contains 20 atoms, we deduce that the o-HMO relative energy with respect to the FM configuration is 679 meV/atom in the AFM configuration.

Table 3 shows a comparison between the Mn-O and Ho-O interatomic distances. The notation for Ho (Ho1 and Ho2), O (O1, O2, O3 and O4) and Mn is similar to those adopted in Refs.[4]. As results, we obtain that the calculated interatomic distances in this present work are in good agreement with reported experimental [4] and theoretical [8] works. In general, the Ho-O interatomic distances are larger than the Mn-O distances, mainly the distances along of the c-axis (Ho-O3 and Ho-O4). The results show small changes for interatomic distances and tilting angles of the MnO₅ polyhedron in the FM and AFM configurations. Experimental analysis of the chemical bonding is needed in order to explain these constatations.

Table 3: Interatomic distance (Mn-O and Ho-O) and angles (O-Mn-O) of the MnO_n polyhedron for HoMnO₃ relaxed atomic structures in ferromagnetic (FM) and antiferromagnetic (AFM) configurations.

Structural	Experimental	Prese	nt work	Previously		
parameter	[4]	FM	AFM	calculated [8]		
Hexagonal phase						
Ho1-O1/Å	2.308 x 3	2.312 x 3	2.312 x 3			
Ho1-O2/Å	2.324 x 3	2.270 x 3	2.270 x 3			
Ho1-O3/Å	2.380 x 1	2.292 x 1	2.292 x 3			
Ho2-O1/Å	2.244 x 3	2.308 x 3	2.308 x 3			
Ho2-O2/Å	2.359 x 3	2.263 x 3	2.263 x 3			
Ho2-O4/Å	2.410 x 1	2.405 x 1	2.405 x 1			
Mn-O1/Å	1.865 x 1	1.885 x 1	1.885 x 1			
Mn-O2/Å	1.960 x 1	1.890 x 1	1.889 x 1			
Mn-O3/Å	1.993 x 1	2.068 x 1	2.080 x 1			
Mn-O4/Å	2.092 x2	2.062 x 2	2.056 x 2			
01-Mn-O2/°		179.835	179.47			
03-Mn-04/°		120.392	119.18			
Orthorhombic ph	iase					
		2.225 x 1	2.226 x 1	2.313		
		2.279 x 2	2.270 x 2	2.266		
Ho-O/Å		2.292 x 1	2.293 x 1			
		2.501 x 2	2.509 x 2			
		2.586 x 2	2.560 x 2			
		1.922 x 4	1.904 x 2	1.898		
Mn-O/Å			1.956 x 2	1.984		
		2.228 x 2	2.269 x 2			
Rhombohedral pl	hase					

Structural	Experimental	Prese	ent work	Previously
parameter	[4]	FM	AFM	calculated [8]
Ho-O/Å		2.195 x 3	2.213 x 3	
Mn-O/Å		1.994 x 6	1.964 x 3	
WIII-O/A			2.010 x 3	
Cubic phase				
Ho-O/Å		2.890 x 6		
Mn-O/Å		1.902 x 6		

3.1.2. Magnetic behavior

The formation energies E_{form} in the FM, AFM and NM configurations of h-HMO, o-HMO, r-HMO and c-HMO crystal structures are presented in Table 2. The obtained values compare well with those reported in [24]. The negative sign of the formation energies means that all these crystal structures in different spin configurations are thermodynamically stable.

The magnetic behavior is discussed by evaluating the stability of corresponding configuration compared with FM state. It appears from the relative energies ΔE deduced from formation energies (Table 2) that whatever the considered crystal structure, its magnetic configuration (FM or AFM) is the most stable whereas its non-magnetic configuration (NM) is the most unstable. Also, with respect to the orders of magnitude of the absolute values of the relative energies, it appears unambiguous that the h-HMO structure is energetically more favorable than the o-HMO, r-HMO and c-HMO structures. Our results also show that the FM configuration is more energetically favorable than the AFM configuration for all crystal structures, in agreement Hamioud et al. [8] for the case of o-HMO, using Wien2k code. However, this is in opposite with the result reported by Chadli et al. [7] for the case of h-HMO which calculations are done with the VASP code.

3.1. Elastic properties

The calculated elastic constants and bulk modulus are presented in Table 4. To our knowledge, there is no experimental data on these parameters for HoMnO₃ crystal structures. The existing results of the perovskite HoMnO₃ based on DFT calculations concern its bulk

modulus [7], [8], but not for the elastic constants C_{ij} . The present work is the first evaluation of the elastic constants of the perovskite HoMnO₃ based on ab-initio calculations. Consequently, the calculated values could not be compared with experimental data. Also, the theoretical data on perovskite similar to RMnO₃ type [23], [27], [28], [29] are given in Table 4 to serve for comparison.

3.1.1. Bulk modulus

The h-HMO bulk modulus is 168.5 ± 1.0 and 178.9 ± 1.0 GPa for FM and AFM configurations, respectively. These values agree with those of 162.23 GPa and 169.34 GPa reported by Chadli et al. [7]. For the o-HMO structure, the calculated bulk modulus is 188.7 ± 0.6 GPa and 175.6 ± 2.1 GPa for the FM and AFM configurations, respectively. These values are smaller than the value of 201.64 GPa reported by Hamioud et al. [8]. However, they are in agreement with experimental data reported by Muthu et al. [27] for others perovskites RMnO3 that include EuMnO3 (185 ± 6 GPa), GdMnO3 (190 ± 16 GPa), TbMnO3 (188 ± 9 GPa) and DyMnO3 (192 ± 8 GPa) in orthorhombic phase. From these four perovskites, the DyMnO3 is classified in the same subgroup as the HoMnO3. The bulk modulus value of HoMnO3 is smaller than that of DyMnO3. This result leads to the conclusion that HoMnO3 is more flexible than DyMnO3.

3.1.2. Elastic constants

According to Tables 4 and 5, the elastic constants of the present work are 1.6 to 2.3 times higher than those given by Shell model calculations reported for the o-HMO structure [23] and for three other perovskites of RMnO₃ type [28]. However, the calculated elastic constants are in the same order with those of DFT calculations and measured elastic constants as reported by Hemme et al. [29]. We conclude that a discrepancy is clear with results obtained from shell-model potential calculations.

Also, the calculated elastic constants satisfy the necessary and sufficient conditions for elastic stability given in Table 1 for each of the four investigated structures.

3.1.3. Mechanical behavior

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Table 6 displays the calculated bulk modulus (B), shear modulus, (G) Young's modulus E, Poisson's ratio (v) and Pugh's ratio (B/G) for HoMnO₃ different crystal structures in FM and AFM configurations according to Voigt-Reuss-Hill (VRH) approximations [21]. It is interesting to note that the bulk modulus values are comparable with those obtained from the strain-energy method (Table 4). For the FM (AFM) configuration, the deviation is about 1.06% (1.08%) for h-HMO, 0.21% (2.97%) for o-HMO, 0.85% (1.91%) for r-HMO and -0.73% for c-HMO. The calculated values of v and B/G indicate that HoMnO₃ is brittle in the hexagonal phase (v=0.19 and B/G=1.3) and ductile in the cubic phase (v=0.30 and B/G=2.11). In the orthorhombic phase (v=0.26-0.28 and B/G=1.77-1.98) or rhombohedral phase (v=0.23-0.24 and B/G=1.54-1.60), it is difficult to conclude with certainty whether the material is ductile or brittle. They are near brittle-ductile boarder line. According to [30], the calculated values of v predict that HoMnO₃ tends to be ionic material (v~0.1) in the hexagonal phase, metallic material ($v \sim 0.33$) in the cubic phase and covalent material ($v \sim 0.25$) in the orthorhombic or rhombohedral phase. The calculated value of Young's modulus of the hexagonal phase (E=305 GPa) is higher than that of 219.2 \pm 10.6 GPa reported experimentally [31]. The bulk modulus is an indicator of compound's resistance to the volume change. Usually, the bulk modulus increases when the cell volume decrease. Our calculated bulk moduli are about 154, 167, 172 and 181 GPa for the cubic, hexagonal, rhombohedral and orthorhombic phases, respectively. The cell volumes are 10.98, 12.45, 11.26 and 11.36 Å³/atom, respectively.

It appears that the above general trend doesn't correlate for the hexagonal phase which should be expected to have the greater value of bulk modulus in correlation with its cell volume. We conclude that an anomalous decreased as compared to the theoretical predictions is then observed.

Table 4: Elastic constants (C_{ij}) and bulk modulus (B) in GPa obtained with PBE-GGA-APW pseudopotentials DFT calculations for HoMnO₃ crystal structures in ferromagnetic (FM) and antiferromagnetic (AFM) configurations

<u> </u>				Elastic c	onstants				Bulk modulus	D. C
Structure	C ₁₁	C ₂₂	C ₃₃	C ₁₂	C ₁₃	C ₂₃	C44	C ₆₆	В	Ref.
h-HMO										
FM	293.4±1.3	293.4±1.3	385.3 ± 5.6	69.1 ±0.4	103.0 ±4.7	103.0 ± 4.7	175.5 ± 0.2	83.3 ± 0.3	168.5 ± 1.0	P.W. ⁵
AFM	293.1 ±1.3	293.1 ±1.3	384.7 ± 5.9	69.3 ±4.1	103.0 ± 7.4	103.0 ± 7.4	175.8 ± 0.2	83.4 ± 0.4	168.4 ± 1.0	P.W.
o-HMO										
FM	278.4 ± 1.7 178	291.5 ±3.4 143	349.3 ±2.1 201	144.7 ±2.8	123.3 ±4.1	121.3 ±5.4	98.7 ± 1.0 43	108.2 ± 0.6	188.7 ± 0.6	P.W. [23]
AFM	274.0 ± 3.5	303.8 ± 3.8	353.1 ± 3.0	135.0 ± 5.1	115.5 ± 4.8	99.9 ± 2.3	107.3 ± 0.6	110.2 ± 0.5	186.4 ± 2.3	P.W.
r-HMO										
FM	364.6 ± 0.7	364.6 ± 0.7	221.1 ± 2.5	146.2 ± 4.1	93.9 ± 3.3	93.9 ± 3.3	148.5 ± 1.8	80.5 ± 0.9	173.9 ± 14.5	P.W.
AFM	353.3 ± 3.3	353.3 ± 3.3	232.1 ± 0.6	152.9 ± 2.0	98.0 ± 2.0	98.0 ± 2.0	131.5 ± 6.9	75.1 ± 1.5	178.9 ± 9.3	P.W.
c-HMO										
FM	305.5 ± 8.4	305.5 ± 8.4	305.5 ± 8.4	79.5 ±9.2	79.5 ±9.2	79.5 ±9.2	54.7 ±2.3	54.7 ± 2.3	153.7 ±3.7	P.W.

⁵ Present work

Table 5 :Elastic constants in GPa of perovskite RMnO3 (R=Tb, Dy, Sm, Eu and Gd)

Structure		Method	Ref.						
	C11	C ₂₂	C33	C ₁₂	C ₁₃	C ₂₃	C44	Method	Kei.
	185; 209; 174; 249	255; 277; 268; 301	239; 257; 265; 275	131; 147; 141; 173	93; 117; 109; 118	110; 128; 121; 144	87; 91; 43; 76	DFT	[20]
o-TbMnO ₃	,	202±20	181±2	,	,	103±6	71±5	Expt. ⁶	[29]
	227	349	274	141	109	103	71	Expt.	
	170	150	197				48	Shell model	[23]
o-DyMn0 ₃	170	151	196				48		[23]
o-SmMnO ₃	157	149	190				52	Shell model	
o-EuMnO ₃	165	154	194				50	Shell model	[28]
o-GdMnO ₃	166	143	198				45		_

⁶ Experimental

Table 6: Calculated values of Bulk modulus (B), shear modulus G (GPa), Young's modulus E (GPa), Poisson'ratio (v) and Pugh's ratio (B/G) for HoMnO3 different crystal structures in FM and AFM configurations according to Voigt-Reuss-Hill (VRH) approximations [21]

	Bv	B _R	Gv	GR	B _{VRH}	Gvrh	E	ν	B/G
h-HMO									
FM	169.14	164.27	133.33	122.29	166.71	127.81	305.39	0.19	1.30
AFM	169.06	164.21	133.37	122.29	166.63	127.83	305.40	0.19	1.30
o-HMO									
FM	188.64	187.97	96.45	93.97	188.31	95.21	244.43	0.28	1.98
AFM	181.30	180.76	103.66	100.99	181.03	102.33	258.31	0.26	1.77
r-HMO									
FM	179.81	165.06	116.59	107.83	172.43	112.21	276.63	0.23	1.54
AFM	181.83	169.92	106.93	100.78	175.88	103.86	260.33	0.25	1.69
c-HMO									
FM	154.83	154.83	78.02	68.92	154.83	73.47	190.31	0.30	2.11

IV CONCLUSION

In summary, the structural and elastic properties of HoMnO₃ crystal systems have been

investigated using accurate ab-initio calculations. The calculated formation energy shows that

the rhombohedral or cubic structure should exist; however, the hexagonal and orthorhombic

phases are energetically more favorable and the hexagonal crystal system is the most stable.

The elastic properties have been for the first time, systematically studied. Due to the lack of

experimental data, our results are predictive and are comparable to recent results on other

perovskite RMnO₃ systems based on DFT calculations. The discrepancy is clear with results

obtained from shell-model potential calculations. From this work, it may be concluded that

such quantum espresso calculations are suitable and appropriate for the description of

perovskite RMnO₃, mainly the subgroup exhibiting hexagonal or orthorhombic crystal

structure (R=Dy or Ho.)

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