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Carbon tax and sustainable facility location: The role of production technology

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Abstract

Recent studies on facility location highlight that increasing the carbon price can ensure meaningful reductions in transport-related greenhouse gas emissions (GHGs). In this paper, we propose to revisit the Production-Location Problem considering transport-related carbon emission mitigation due to carbon taxation and production technologies that allow complementarity or substitution among input quantities. We first show that cost-minimizing location may differ from carbon emission minimizing location, regardless of the production technology type. We also find that gradual changes in carbon tax affect the relative delivered prices of inputs such that the firm has an incentive to relocate its facility and substitute among input quantities, leading to new shipping patterns that do not necessarily cause a lower pollution.

Keywords:

Location; transport-related carbon emissions; carbon tax; production technology; sustainability.

1. Introduction

Freight transport accounts for a significant proportion of carbon emissions and represented approximately 14% of total emissions in 2010, which had increased by 11% over the period of 2000 – 2010 (IPCC, 2014). Thus, it is a major challenge for policy makers to deploy efficient regulations to restrict the carbon emissions from logistic activities of companies (Hoen et al., 2014). One way to curb the transport-related carbon emissions would be to influence the location choice of companies since the spatial organization of firms affects directly distances traveled by commodities; and transport modes selection and therefore the ecological footprint stemming from commodity shipping (Daniel et al., 1997; Gagné et al., 2012; Lim et al., 2016).

Recent studies on facility location under a carbon pricing scheme highlight that increasing the carbon price can lead to firm relocation, which creates better transport environmental performances (see, e.g., Ramudhin et al., 2010; Chaabane et al., 2012; Rezaee et al., 2017).¹ Such a result is obtained by assuming, either explicitly or implicitly, an assembly supply chain modeled by a bill of materials (BOM). The BOM of a manufactured product is a concept of the late seventies in which all product components are listed in a structured way (Hegge and Wortmann, 1991). It is classically represented by a tree structure and assumes a *fixed* coefficient for each component in each subset (Pochet and Wolsey, 2006). Consequently, an increase in carbon price will have no effect on the quantities' supply choices because the demand for each input is fixed *a priori*. It will in fact enhance the total transport costs, thus prompting the firm to relocate to sustainable alternative places (lower level of emissions). In this paper, we argue that the positive environmental result of a higher carbon price may be weakened or may cease to hold when possible substitutions are allowed among the input quantities. The effect of substituting raw materials can be observed in some industrial sectors

¹Currently, there are two main types of economic regulatory instruments that could impact transport-related emissions: carbon taxation and carbon emissions trading (Hoen et al., 2013). These regulations are often advocated by international institutions as effective instruments for carbon emissions mitigation (Zhang and Baranzini, 2004; Zakeri et al., 2015).

such as the food industry (e.g. preparation of culinary products), the animal feed industry (e.g. mixture of livestock feed), or the chemical industry (e.g. primary products made at the mine's exit), where it is often possible for a firm to vary the share of input quantities for regulatory, marketing or even raw material relative prices change reasons (Balakrishnan and Geunes, 2000). In this context, firms may have access to different combinations of input quantities (input mixes) to produce a given level of output.

Motivated by the increasing importance to assess the effects of carbon taxes, the objective of this paper is to investigate the facility location problem of a manufacturing firm under a carbon tax policy on transport-related emissions when the input quantities may be substituted. Specifically, the firm incurs sourcing and transportation costs. In addition, the firm also incurs a carbon tax, based on the distance and the carbon intensity of transportation mode. We consider two production technologies, namely Leontief and Cobb-Douglas that express the relationship between the inputs and the produced quantity. In the Leontief technology (a benchmark case), the two inputs are used in a fixed (exogenous) proportion to produce the output. The second technology considers a Cobb-Douglas production function under which the two inputs are substitutes.²

It is worth stressing that the objective of our paper is not to build a comprehensive firm location model under carbon taxation but rather to develop a simple model to clearly identify the mechanisms at work and highlight the crucial role of production technology and

² There are many ways to represent a company's production possibilities, as well as ways to describe technology aspects. In this article, we adopt the term of production technology in its *economic* definition: a production function describes the technological relationship between the quantities of inputs and the quantities of produced outputs (Varian and Repcheck, 2010). In this way, we remain consistent with the concept used and developed by Peeters and Thisse (2000). Thus, the Leontief and Cobb-Douglas production technologies correspond respectively to the fixed and to the flexible BOM (see Balakrishnan and Geunes, 2000). Nevertheless, the flexible BOM is defined on a finite set whereas Cobb-Douglas function is theoretically on an infinite space. However, the term of production technology in some operations management literature may be more general by considering not only the aspects of the relationship between inputs (complementarity or substitution) but also other aspects such as operations costs (see, e.g., Ramudhin et al., 2010).

location choice in the evaluation of the carbon taxation policies. These mechanisms are still ambiguous in the literature, as reported by Wu et al. (2017). It is therefore relevant and appropriate to clarify them across a simple structure rather than a general and more complicated structure.

We first show that the cost-minimizing and emissions-minimizing solutions do not always overlap, regardless of the production technology type. Furthermore, in the case of Leontief technology, a higher tax leads to a lower or the same level of emissions, depending on the mode of transportation. When input proportions can be varied under a Cobb-Douglas structure, the tax effects can be ambiguous. To disentangle the various effects at work, we must distinguish between two cases: in the former, the facility location is given (short term), and in the latter, the facility location adjusts to changes in carbon tax (long term). Our analysis relies on the following trade-off. On the one hand, for a given location, an increase in carbon tax reduces transport-related carbon emissions of the supply planning as the *relative delivered prices* of inputs converge to the relative delivered prices, leading to the lowest level of carbon emissions.³ In this case, higher carbon tax rates raise total shipping cost and shift the input proportions in the direction that lowers emissions. On the other hand, by affecting the relative delivered prices of inputs, a higher carbon tax can trigger the firm to relocate to re-optimize its cost, inducing a new substitution among input quantities and, thus, a new shipping pattern. Hence, when a facility location reacts to changes in carbon tax, a marginal increase in the carbon tax rate may generate a higher level of pollution or may cause a large fall in emissions. This result is sufficient to show that the desirability of carbon taxation is more complex than suggested by its proponents, primarily because this recommendation disregards its impact on the location of production and the substitution among inputs. Accounting for these effects makes the impact of a higher carbon tax more ambiguous because their net effects depend on whether the new spatial pattern is better or worse from an environmental viewpoint.

³The relative delivered price refers to the per-unit procurement and transportation costs of an input compared to the costs of another.

The remainder of this paper is organized as follows. In the next section, we present a literature review on sustainable facility location. In section 3, we revisit the production-location problem (PLP). Subsequently, we propose to study the extended PLP model under specific production technology forms. Section 4 focuses on Leontief technology, and section 5 focuses on Cobb-Douglas technology. The last section discusses the robustness of our results and provides several further conclusions.

2. Literature review

For many years now, researchers have focused increasing attention on the sustainability behind facility location decisions by considering not only the economic criteria but also environmental and social criteria. A comprehensive description and classification of the most recent studies and contributions can be found in some reviews (see, e.g., Terouhid et al., 2012; Chen et al., 2014; Eskandarpour et al., 2015). The carbon footprint is generally used as a measurement metric to qualify ecological performance (Hassini et al., 2012). It corresponds to the amount of carbon dioxide emitted by a company during all stages of a product's life-cycle or in some stages such as production and/or transport. Some of the existing studies that integrated GHG emissions in location modeling generally seek a trade-off between minimizing economic costs (or maximizing profit) and carbon footprint by using a single economic objective model. In this case, the GHG emissions are converted into their monetary equivalent (Elhedhli and Merrick, 2012). In addition to the single objective models, many researchers develop bi-objective models to generate a set of Pareto-optimal solutions (see, eg., Bouzembrak et al., 2011; Harris et al., 2011; Xifeng et al., 2013). However, few researchers in operations management have incorporated regulations such as carbon tax, carbon emissions trading, and carbon cap in their location models and analyzed the impact of these mechanisms on facility location decisions and the resulting GHG emissions.

Our paper contributes to the literature on facility location under environmental regulations related to carbon emissions mitigation (see for a survey Dekker et al., 2012; Waltho et al., 2019). Using a Mixed-Integer Linear Programming model (MILP), Ramudhin et al. (2010)

consider the problem of sustainable supply chain configuration (e.g. suppliers, subcontracting, distribution, production and transport technology choices) and introduce emission constraints (emissions cap) imposed by law (or by the company itself) with a given carbon price. The analyses of an example from the steel industry reveal that when the emission cap shrinks or the carbon price increases, decision-makers select production schemes and transport modes that are more environmentally friendly. Chaabane et al. (2012) extend the previous model to a Multi-Objective Linear Programming approach (MOLP) and consider the Life-Cycle Assessment (LCA) method to measure carbon emissions. They study the effect of carbon emission allowance and tradable carbon credits and conclude from a case study of the aluminum industry that supply managers have two options. First, when reducing GHG emissions cost through clean technology investments and sustainable supply chain configuration (internal mechanisms) is more expensive than buying carbon credits (external mechanisms), decision-makers buy carbon credits to be compliant with the regulatory limits. Otherwise, they should opt for the greener production and transport strategies. Diabat and Simchi-Levi (2009) consider a MILP model for a supply chain network design with a cap on the amount of CO_2 emitted. They use an experimental example to show that when the cap becomes tighter, the total supply chain cost increases as the firm opens more manufacturing and distribution centers (increasing fixed costs) to reduce transport emissions. Rezaee et al. (2017) propose a discrete location problem with uncertainty on demand and carbon price. They conclude from an office furniture industry case study that a higher carbon price leads to a sustainable supply chain design. Diabat et al. (2012) present a Carbon-Sensitive Closed Loop Supply Chain problem formulated as a MILP model. Using a numerical study, the authors analyzed the effect of carbon price changes on the design of both forward and reverse supply chains. Cachon (2014) considers the problem of downstream supply chain design (retail store location, density, and size) under a carbon price scheme. The findings of this study indicate that the carbon price must reach a very high level for a significant carbon emissions reduction. Martí et al. (2015) propose a green supply chain network design with uncertainty on demand. They analyzed the responsiveness of the supply chain config-

uration to different carbon policies (namely caps on supply chain carbon footprints, caps on market carbon footprints, and carbon taxes) by taking into consideration the innovative or functional nature of the products. Wu et al. (2017) investigate the effect of rising carbon prices on off-shoring and near-shoring decisions for a single producer between two distinct regions (north and south) according to different scenarios of production costs, emissions, and the distance that separates the two regions. Turken et al. (2017) address the facility location and capacity acquisition problem under two forms of carbon emissions regulatory mechanisms: a carbon tax and a command-and-control policy that involves taxation after exceeding the emissions limit. They investigate the various effects of the limit on carbon emissions and carbon tax on centralization or decentralization of optimal production network and the resulting emissions.

Most of these publications have concluded that a higher carbon prices could lead to reduce carbon emissions resulting from transport, more or less significant depending on the context and nature of the studied problem. However, when assessing the ecological outcomes, the existing literature has neglected one major issue: the role of the production technology on the relation between carbon tax, location, and pollution. As noted in the introduction, they did not pay attention to the substitution effect through input quantities. Peeters and Thisse (2000) are among the first to emphasize the importance of a raw material substitution effect on facility location decision. They show that small variations on the elasticity of substitution among input quantities may lead to significant change in the optimal firm location. However, the environmental issues related to the transport of commodities are left aside on their study. Hence, there is a lack of location models that address the role of production technology in the relationship between location decision and environmental regulations. Our research contributes to the related literature by investigating the efficiency of carbon tax to reduce transport-related emissions when firms can adjust their locations and have access to different types of production technologies.

3. Model description

In this section, we propose to revisit the PLP model under a carbon tax policy on transport-related carbon emissions. Consider a firm F that must deliver a unique transformed product to one downstream market noted M which has a deterministic demand q^0 . Downstream demand is assumed to be fixed to focus only on carbon emissions generated by the transport phases. Consider also two different upstream markets, in which each raw material input i is provided from a fixed market S_i with an amount noted s_i , with $i = 1, 2$. All stakeholders have a fixed and determined location on a one-dimensional linear network space. Without loss of generality, the two input markets are on the left side of the output market M with S_1 closer to M than S_2 . The distances between stakeholders are: $d(S_2, M) = z$, $d(S_2, S_1) = x$ and $d(S_2, F) = y$. The firm F must define its best location as y , which is necessarily on the line segment $[S_2, M]$ (convex hull), as proven by Wendell and Hurter (1973), when the transport costs are non-negative and non-decreasing with distance. Thus, the optimal location can be either between S_2 and S_1 (case a) or between S_1 and M (case b). We consider a single facility problem with a mono-product setting to focus on the interrelations between carbon price and firm location choice through the production decisions; besides, these interactions can be clarified and explained more easily with a linear representation and a limited number of suppliers and output markets.

The firm produces the market demand in one shot (static period) without constituting inventories and with an infinite capacity system. The firm has access to different production techniques modeled by a production function $f : R^2 \rightarrow R$ that links the total production level to raw material needs such as: $q^0 = f(s_1, s_2)$.⁴

Each unit of raw material i has a mill price w_i , a transport cost per unit of distance and per unit of input t_i supported by the firm, and a carbon footprint coefficient per unit of distance

⁴ In *economics*, production techniques describe the feasible combinations of inputs to produce a given quantity of output. The production function (technology) considers only the maximum possible output for a given level of inputs. Therefore, it describes a boundary representing the maximum output that can be obtained from each feasible combination of inputs (Varian and Repcheck, 2010).

and per unit of input α_i from S_i to F , with $i = 1, 2$. Each unit of output has a transport cost per unit of distance and per unit of output t_0 borne by the firm and a carbon footprint coefficient per unit of distance and per unit of output α_0 from F to M . Fixed transport costs are not considered since that the firm is at an aggregate strategic level of decision; that is, no economies of scale emerge. In addition, the firm is in a price taker situation and therefore has no influence on output or input prices. Let d_i with $i = 0, 1, 2$ be the distances between the firm location y , and the output market and input markets respectively with $d_0 = z - y$, $d_1 = |x - y|$, and $d_2 = y$. Let τ be the unit carbon price per unit of carbon emissions. The initial rate τ is often fixed by public authorities. However, its effectiveness depends on its evolution. Thus, it is expected that the carbon tax will increase gradually over time since the damage caused by GHG emissions will have a greater negative impact in the future than currently (Zhang and Baranzini, 2004).

Following Peeters and Thisse (2000), the objective of the firm is to identify the best location y and define its supply strategy, determined by the vector $s = (s_1, s_2)$, to minimize its cost function while respecting its production technology. The firm cost function $C(y, s)$ can then be expressed as:

$$C(y, s) = \sum_{i=1}^2 w_i s_i + \sum_{i=1}^2 t_i d_i s_i + t_0 d_0 q^0 + \tau \left(\alpha_0 d_0 q^0 + \sum_{i=1}^2 \alpha_i d_i s_i \right),$$

where $\sum_{i=1}^2 w_i s_i$ is sourcing cost; $\sum_{i=1}^2 t_i d_i s_i$ is upstream transportation cost; $t_0 d_0 q^0$ is downstream transportation cost; and $\tau \left(\alpha_0 d_0 q^0 + \sum_{i=1}^2 \alpha_i d_i s_i \right)$ is transport-related carbon emissions cost based on the distance, the quantity of freight carried, and the carbon intensity of transportation mode.

Let $T_i \equiv t_i + \tau \alpha_i$ with $i = 0, 1, 2$ be the total unit transportation cost, which includes a variable unit transportation cost part t_i and an environmental transportation unit cost part of carbon emissions $\tau \alpha_i$. Therefore, establishing a carbon tax on carries means increasing the variable unit transport cost t_i with $i = 0, 1, 2$. In a sustainability context, fuel taxes can also be seen as a scenario of increasing transport costs to reduce carbon emission from transportation as each unit of fuel used generates a certain amount of emissions. Firm cost

can be rewritten as follows:

$$C(y, s) = T_0 d_0 q^0 + \sum_{i=1}^2 (w_i + T_i d_i) s_i,$$

where $w_i + T_i d_i$ represents *the delivered price of a shipped input unit*, composed of the the per-unit procurement and total transportation costs. The optimal economic efficient location that minimizes firm cost C is then described by

$$C^* = \underset{y,s}{\text{Min}} C(y, s) \tag{1}$$

subject to

$$q^0 = f(s_1, s_2) \tag{2}$$

$$y \geq 0 \tag{3}$$

$$s \geq 0 \tag{4}$$

Constraint (2) requires that production possibilities should be respected, which means that the firm will use the production techniques that will allow it to meet the total demand (technology constraint). Constraints (3) and (4) impose variable positivity. This model also encapsulates an interesting formulation representing the total carbon footprint generated during upstream and downstream transport phases noted E and expressed as follows:

$$E(y, s) = \alpha_0 d_0 q^0 + \sum_{i=1}^2 \alpha_i d_i s_i$$

Transport-related carbon emissions minimizing location is then given by

$$E^* = \underset{y,s}{\text{Min}} E(y, s)$$

with respect to constraints (2), (3) and (4). The establishment of this second formulation would enable us to compare optimal firm location circumstances according to two scenarios: (i) The location y^* that minimizes the firm's total cost (economic efficiency), and (ii) the location y^e that minimizes transport's carbon footprint (environmental efficiency). The

aim of this comparison is to examine whether the carbon tax can be used as an effective instrument to induce a cost-minimizing location to arrive at an emission-minimizing outcome. In the sequel, we first assume a Leontief production function (complementary essential inputs) and then we consider that inputs are combined with a Cobb-Douglas technology. For the rest of the paper, indexes i and j will be equal to 1 or 2 when they are not explicit.

4. Leontief technology

The Leontief production function is characterized by a linear relationship between inputs and outputs, a fixed proportion between inputs and a constant return to scale (Varian and Repcheck, 2010). Then, with two inputs, to produce an output unit, it is necessary to have a_1 units of input 1 and a_2 units of input 2. These positive parameters, called technical coefficients, correspond to the number of each required per unit of component in the classical notion of BOM. The latter has been specifically used in some location models under the carbon pricing scheme as the basis of the available manufacturing technologies (see, e.g., Ramudhin et al., 2010; Chaabane et al., 2012).⁵

4.1. Cost minimizing and emission-minimizing locations

The demand of each input s_i is fixed as the production volume q^0 is given and the technical coefficients a_i are defined by the technology so that $s_i = a_i q^0$. These supply quantities are independent from the input mill price w_i because each input is available only at one input source (no competition between suppliers or geographical substitution into the market structure). The firm cost function $C(y)$ is then given by

⁵In Ramudhin et al. (2010), the planned production is determined by the BOM. However, the potential technologies differ in terms of operations costs and output emissions. That goes back to the difference between the definition of production technology in economics and operations management as explained in footnote 2. Technologies influence the operations costs as well as the generated emissions. In our study, we consider that the modification of the combination of inputs in the same technology will have a negligible impact on operations costs and output emissions. Without loss of generality, we disregard these costs and emissions.

$$C(y) = \left[T_0 d_0 + \sum_{i=1}^2 (w_i + T_i d_i) a_i \right] q^0.$$

Because the firm's objective function is linear in one-dimensional space, the solutions are necessarily at the segments' corners, then $y^* = 0$, $y^* = x$, or $y^* = z$. Therefore, it is sufficient to consider the following two cases: Case a: if $0 \leq y \leq x$, then: $\frac{dC^a}{dy} = -(T_0 + a_1 T_1 - a_2 T_2) q^0$ and Case b: if $x \leq y \leq z$, then: $\frac{dC^b}{dy} = -(T_0 - a_1 T_1 - a_2 T_2) q^0$. These results show that optimal location depends only on production technology parameters and the relative per-unit total transport prices parameters. **Lemma 1** determines the conditions for the cost-minimizing locations (proof: see Appendix A.1).

Lemma 1. *The location that minimizes the cost is given by $y^* = 0$ if and only if $a_2 \geq \frac{T_1}{T_2} a_1 + \frac{T_0}{T_2}$, $y^* = x$ if and only if $\frac{T_1}{T_2} a_1 + \frac{T_0}{T_2} \geq a_2 \geq -\frac{T_1}{T_2} a_1 + \frac{T_0}{T_2}$ and $y^* = z$ if and only if $a_2 \leq -\frac{T_1}{T_2} a_1 + \frac{T_0}{T_2}$.*

Set $P_{0x}(a_1) \equiv \frac{T_1}{T_2} a_1 + \frac{T_0}{T_2}$ so that the firm is indifferent to being located in $S_2(0)$ or in $S_1(x)$ when $a_2 = P_{0x}(a_1)$, and $P_{xz}(a_1) \equiv -\frac{T_1}{T_2} a_1 + \frac{T_0}{T_2}$ so that the firm is indifferent to being located in $S_1(x)$ or in $M(z)$ when $a_2 = P_{xz}(a_1)$. We draw the lines $P_{0x}(a_1)$ and $P_{xz}(a_1)$ in Figure 1 which is a representation of all possible firm's cost-minimizing locations in the space of all combinations of the technical coefficients $(a_1; a_2)$. It is shared in three zones: in the north part, the firm must be located in S_2 , in the east part, the firm must be located in S_1 , and in the south part, the firm must be located in M . The surfaces of these three zones are delimited by the thresholds of optimal location choice P_{0x} and P_{xz} on which the firm is indifferent to being located in two neighboring zones. The location in the final market is more likely to occur when the total transport unit cost of the output T_0 is high enough relatively to the total transport unit cost of the inputs T_1 and T_2 (then, the ratios $\frac{T_0}{T_1}$ and $\frac{T_0}{T_2}$ will be higher and the surface area of the zone $y^* = z$ in Figure 1 will increase) and when the technical coefficients are low enough which indicates that firm uses few inputs. The location in the input source S_1 is more likely to occur when the total transport unit cost T_1 is high

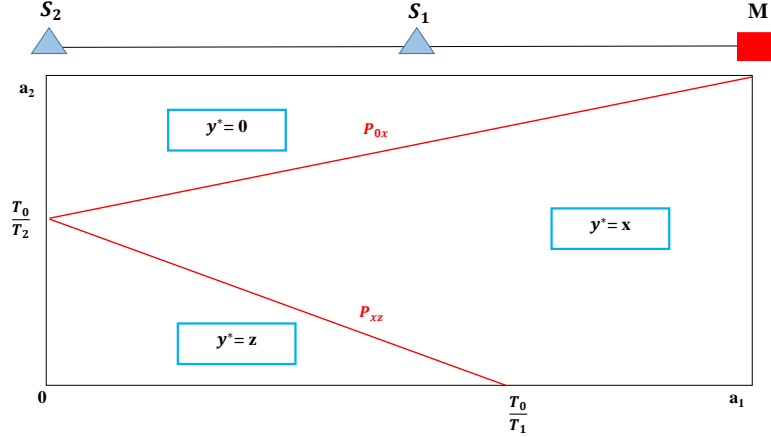


Figure 1: *Cost minimizing location in $(a_1 - a_2)$ space.*

enough relatively to the total transport unit cost T_0 and T_2 (then, the ratios $\frac{T_1}{T_2}$ and $\frac{T_0}{T_1}$ will be higher and the surface area of the zone $y^* = x$ in Figure 1 will increase) and when the technical coefficient a_1 is high compared to the technical coefficient a_2 which indicates that firm uses more input 1 than input 2. As a result, the location in input source S_2 is more likely to emerge for firm that is more tolerant to the increasing technical coefficient a_2 .

From **Lemma 1**, when the marginal transport cost of the input 1 weighted by its technical coefficient is strictly higher than the marginal transport cost of the finished product ($a_1 T_1 > T_0$), the optimal location will not occur at the final market M . In addition, when the marginal transport cost of the input 2 weighted by its technical coefficient is strictly less than the marginal transport cost of the finished product ($a_2 T_2 < T_0$) the optimal location will not occur at the input source S_2 .

In the same way as for cost-minimizing location, we determine the firm location y^e that minimized the transport-related emissions $E(y)$ for a given level of production q^0 (see Appendix A.2). More precisely, **Lemma 2** determines the conditions for the emissions-minimizing locations.

Lemma 2. *The location minimizing emissions is given by $y^e = 0$ if and only if $a_2 \geq$*

$\frac{\alpha_1}{\alpha_2}a_1 + \frac{\alpha_0}{\alpha_2}$, $y^e = x$ if and only if $\frac{\alpha_1}{\alpha_2}a_1 + \frac{\alpha_0}{\alpha_2} \geq a_2 \geq -\frac{\alpha_1}{\alpha_2}a_1 + \frac{\alpha_0}{\alpha_2}$ and $y^e = z$ if and only if $a_2 \leq -\frac{\alpha_1}{\alpha_2}a_1 + \frac{\alpha_0}{\alpha_2}$.

Set $E_{0x}(a_1) \equiv \frac{\alpha_1}{\alpha_2}a_1 + \frac{\alpha_0}{\alpha_2}$ so that the firm is indifferent to being located in $S_2(0)$ or in $S_1(x)$ when $a_2 = E_{0x}(a_1)$, and $E_{xz}(a_1) \equiv -\frac{\alpha_1}{\alpha_2}a_1 + \frac{\alpha_0}{\alpha_2}$ so that the firm is indifferent to being located in $S_1(x)$ or in $M(z)$ when $a_2 = E_{xz}$. Therefore, to minimize the environmental function, the firm's location is explained by the values of the technical coefficients of its inputs and the ratios of the unit carbon intensity of the transportation modes linked by the linear relationships E_{0x} and E_{xz} . The conditions of the firm's emission-minimizing locations are completely independent from the carbon tax τ . Thus, an increase in τ will not directly improve the ecological outcome but it would only react through a firm location change.

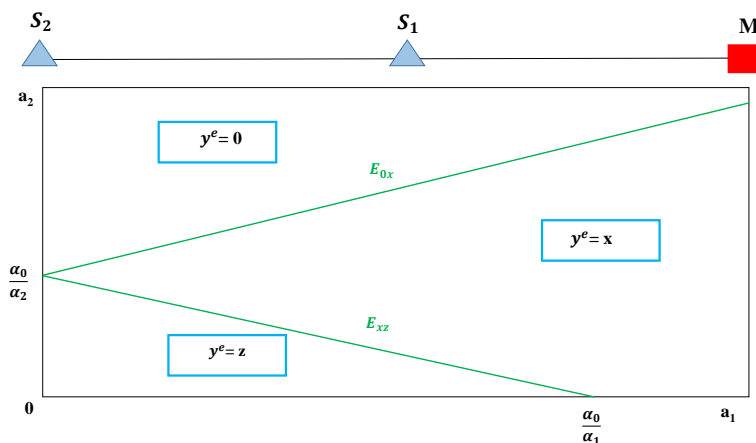


Figure 2: *Pollution minimizing location in $(a_1 - a_2)$ space.*

Figure 2 represents all possible firm's emission-minimizing locations in the space $(a_1; a_2)$. The surface zones ($y^e = 0$, $y^e = x$, and $y^e = z$) are delimited by the environmental thresholds E_{0x} and E_{xz} . The surface size of a zone in this case depends on the ratios between carbon emissions units $\frac{\alpha_i}{\alpha_j}$ with $i = 0, 1$, $j = 1, 2$ and $i \neq j$. The mechanisms underlying cost-minimizing location are the same for emissions-minimizing location by considering α_0, α_1 , and α_2 instead of T_0, T_1 , and T_2 respectively.

4.2. Ecological outcome vs economic outcome: the role of carbon tax

In this subsection, we analyze when the conditions of the firm's cost-minimizing and emissions-minimizing locations do coincide (or deviate), under the Leontief setting. All the results are resumed in the next proposition (proof: see Appendix A.3) and illustrated in Figure 3.

Proposition 1. *Regardless of a carbon tax ($\tau \geq 0$), the cost-minimizing location corresponds to the emission-minimizing location if and only if one of the three following conditions holds: $a_2 > \max\{P_{0x}(a_1), E_{0x}(a_1)\}$, $a_2 < \min\{P_{xz}(a_1), E_{xz}(a_1)\}$, $\min\{P_{0x}(a_1), E_{0x}(a_1)\} > a_2 > \max\{P_{xz}(a_1), E_{xz}(a_1)\}$.*

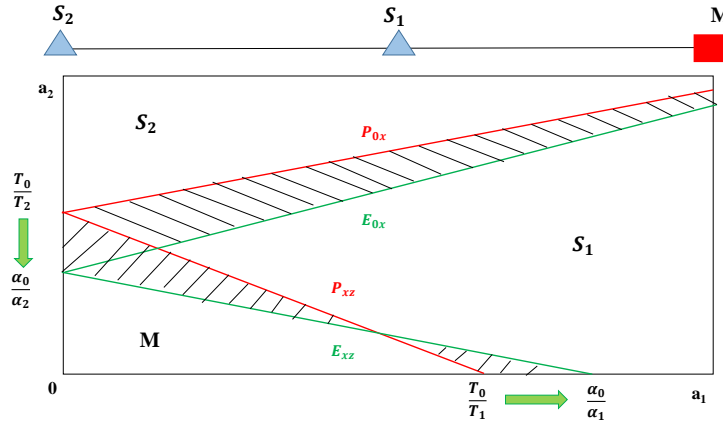


Figure 3: *Crossing economic and environmental location conditions in $(a_1 - a_2)$ space.*

First of all, when $\frac{\alpha_1}{\alpha_2} = \frac{T_1}{T_2}$ and $\frac{\alpha_0}{\alpha_1} = \frac{T_0}{T_1}$, and $\frac{\alpha_0}{\alpha_2} = \frac{T_0}{T_2}$, then the thresholds P_{0x} and E_{0x} (resp P_{xz} and E_{xz}) are identical (curves in Figure 3 are confounded). In that case, all combinations (a_1, a_2) lead to both economic and environmental efficiency. In particular, in a mono-modal transport scheme, the firm chooses the best location in both dimensions regardless of the level of carbon tax. When $\frac{\alpha_1}{\alpha_2} \neq \frac{T_1}{T_2}$ or $\frac{\alpha_0}{\alpha_1} \neq \frac{T_0}{T_1}$, or $\frac{\alpha_0}{\alpha_2} \neq \frac{T_0}{T_2}$, the cost-minimizing and emissions-minimizing solutions do not always overlap because the per-unit monetary transportation costs of the commodities are not proportional to the corresponding per-unit emissions. As a

result, the cost-minimizing location may induce excess pollution. This theoretical result is supported by some empirical studies in the biomass industry (You and Wang, 2011) and in the steel industry (Ramudhin et al., 2010).

We now consider the impacts of changes in carbon tax at reducing the gap between the two objectives. It can be easily shown that an increasing carbon tax makes cost-minimizing thresholds P_{0x} and P_{xz} converge to meet pollution-minimizing thresholds E_{0x} and E_{xz} , respectively as $\lim_{\tau \rightarrow +\infty} P_{0x} = E_{0x}$ and $\lim_{\tau \rightarrow +\infty} P_{xz} = E_{xz}$. This triggers firm that has a conflict between the economic and environmental criteria to relocate toward the emission-minimizing location. Otherwise, for firm that does not have a conflict, a higher carbon tax cannot hurt the ecological outcome, regardless of the combination (a_1, a_2) , but it does increase the overall cost. In other words, a firm remains in S_1 , S_2 or M when the carbon tax increases. To summarize,

Proposition 2. *Assuming a Leontief production technology, an increase in carbon tax makes it more likely that the cost-minimizing location corresponds to the pollution-minimizing location.*

5. Cobb-Douglas technology

The technology studied in this section is fundamentally different from that in the previous section. It is another polar specification of the production function f in which the inputs are imperfectly substitutable and numerous technological combinations may exist to produce goods (Varian and Repcheck, 2010). For example, feed mixture for livestock requires combining several quantities of cereals (e.g. wheat, barley, soy) to cover livestock nutritional needs. Then, the quantities of the cereals in a food recipe may be varied but to a limited extent to respect the nutritional intake (this is a classical problem of blending inputs).

5.1. Technology and Input demand

The Cobb-Douglass functional form is defined as follows in our case with two inputs:

$$q^0 = f(s_1, s_2) = a_0 \prod_{i=1}^2 s_i^{a_i},$$

where $a_0 > 0$ is the Total-Factor Productivity (TFP). It is defined as the part of production that is not explained by the amount of inputs used in production as technical progress (Solow, 1957). Its value is exogenous and determined by the available technology. $a_i > 0$ is a partial production elasticity coefficient and refers to the change produced in output level q^0 due to the change in input quantity s_i while keeping input quantity s_j constant with $j \neq i$. The value of a_i is also exogenous and is determined by the available technology. Furthermore, $a_1 + a_2$ is called the total production elasticity. The Cobb-Douglass production function exhibits constant returns to scale when $a_1 + a_2 = 1$ (meaning that doubling the usage of s_1 and s_2 will also double output q^0) and decreasing (respectively increasing) returns to scale when $a_1 + a_2 < 1$ (respectively $a_1 + a_2 > 1$). In the latter, we will assume that $a_1 + a_2 = 1$, which implies a constant return to scale and log-linear form possibility for the Cobb-Douglass production function. This choice is justified by the fact that the Leontief production function is characterized by a constant return to scale and a linear form. Then, it would be better to assume the same properties for the Cobb-Douglass production function to isolate and emphasize the role of the input substitution effect.

In Cobb-Douglas production setting, the firm not only optimizes its location but it also determines the allocation between the two inputs (input mix). Given the level of production q^0 , the firm minimizes the upstream costs regardless of firm location y under the Cobb-Douglas technological constraint, which leads to the following individual demand for each input (see Appendix B.1):

$$s_i^* = \left(\frac{q^0}{a_0} \right) \left[\frac{a_i(w_j + T_j d_j)}{a_j(w_i + T_i d_i)} \right]^{a_j} \quad (5)$$

with $i \neq j$, and where the ratio $\frac{w_i + T_i d_i}{w_j + T_j d_j}$ represents *the relative delivered price* between the two inputs. Thus, an increase in the carbon tax (through an increase in total transport unit

cost T_i) will alter the relative delivered price of a shipped input. Consequently, the firm will adjust its input quantity choices for each level of carbon tax τ .

5.2. Cost-minimizing location and ecological outcome

Having specified the functional form of the Cobb-Douglass production function and identified the optimal set of supply quantities that are combined, we can determine the optimal firm location. Replacing s_1^* and s_2^* (5) in firm cost leads to:

$$C(y) = \nu(y)q^0,$$

with

$$\nu(y) \equiv T_0 d_0 + \Psi \prod_{i=1}^2 (\zeta_i d_i + 1)^{a_i}, \quad \Psi \equiv \frac{1}{a_0} \prod_{i=1}^2 w_i^{a_i} \sum_{i \neq j} \left(\frac{a_i}{a_j} \right)^{a_j}, \quad \text{and} \quad \zeta_i \equiv \frac{T_i}{w_i},$$

where $\nu(y)$ is the marginal cost of production related to the location y , Ψ is a bundle of exogenous parameters that are independent from distances and ζ_i is the ratio of the total transport unit cost to the purchasing unit cost.

The cost function $C(y)$ is concave over the intervals $[0, x]$ and $[x, z]$ as $\frac{d^2 C}{dy^2} < 0$ (see Appendix B.2). Hence, there are three candidates for the cost-minimizing location: $y^* = 0$, $y^* = x$, and $y^* = z$. The firm cost associated with each optimal location candidate is expressed as follows:

$$\begin{aligned} C_0 &= \nu_0 q^0 = [T_0 z + \Psi (\zeta_1 x + 1)^{a_1}] q^0, \\ C_x &= \nu_x q^0 = [T_0 (z - x) + \Psi (\zeta_2 x + 1)^{a_2}] q^0, \\ C_z &= \nu_z q^0 = [\Psi (\zeta_1 (z - x) + 1)^{a_1} (\zeta_2 z + 1)^{a_2}] q^0. \end{aligned}$$

The cost-minimizing locations are not necessarily those that minimize the total transportation costs as for Leontief technology because a compromise emerges between the transportation and purchase costs (see Appendix B.3).

Furthermore, the ecological outcome is given by:

$$E(y) = \theta(y)q^0$$

with

$$\theta(y) \equiv \alpha_0 d_0 + \Psi \prod_{i=1}^2 (\zeta_i d_i + 1)^{a_i} \left(\sum_{i=1}^2 \frac{\alpha_i d_i}{T_i d_i + w_i} \right),$$

where $\theta(y)$ is the marginal emission of production related to the location y .⁶

The environmental function E shows an interesting feature. Unlike the Leontief setting, where the emissions level were completely independent from τ , the carbon tax affects directly the level of emissions through the input quantities (s_1^*, s_2^*) under a Cobb-Douglas substitution structure. Although the tax is identical for both inputs, it changes the *relative delivered price* of a shipped input and therefore its demand quantity which changes the level of emissions. Because it is difficult to explore analytically the environmental function in order to determine pollution minimizing location, we associated to each cost-minimizing location candidate: $y^* = 0$, $y^* = x$, and $y^* = z$ the following level of pollution, respectively:

$$\begin{aligned} E_0 = \theta_0 q^0 &= \left[\alpha_0 z + \Psi \frac{\alpha_1 x}{T_1 x + w_1} (\zeta_1 x + 1)^{a_1} \right] q^0, \\ E_x = \theta_x q^0 &= \left[\alpha_0 (z - x) + \Psi \frac{\alpha_2 x}{T_2 x + w_2} (\zeta_2 x + 1)^{a_2} \right] q^0, \\ E_z = \theta_z q^0 &= \left[\Psi \left(\frac{\alpha_1 (z - x)}{T_1 (z - x) + w_1} + \frac{\alpha_2 z}{T_2 z + w_2} \right) (\zeta_1 (z - x) + 1)^{a_1} (\zeta_2 z + 1)^{a_2} \right] q^0. \end{aligned}$$

Thereafter, we perform some simulations to determine whether the cost-minimizing location matches at least the lowest pollution level observed among these three candidates. Several numerical examples reveal that the cost-minimizing solutions would not always coincide with the lowest level of emissions because the per-unit procurement and monetary transportation costs of the commodities are not proportional to the corresponding per-unit emissions. Figure 4 represents the results of one of these situations. We have considered $q^0 = 100$, $a_0 = 1$, $a_1 = 0.5$, $a_2 = 0.5$, and $\tau = 10$. The per-unit procurement and monetary transportation

⁶The minimization of the cost function C (resp. environmental function E) returns to minimize the marginal cost ν (resp. marginal emissions θ) of production of an output unit at the location y . This characteristic of the cost function has already been proved for production-location problems when the production function is homogeneous under the name of "separability theorem" and whose statement is as follows: "the location which minimizes the total cost for a unit of output must minimize the total cost for all levels of production" (Hurter and Venta, 1982).

costs; and the per-unit emissions values of the commodities are reported in Table 1.⁷ The left side of Figure 4 shows the firm costs at the locations $y = 0$, $y = x$, and $y = z$, regardless of the position x of the supplier S_1 on the normalized segment $[S_2(0), M(1)]$ (i.e. $0 \leq x \leq 1$). Then, cost-minimizing location is at supplier S_1 because the marginal cost t_l is high relatively to t_0 and t_2 . The right side of Figure 4 depicts the associated pollution levels. It indicates that the lowest level of pollution is at supplier S_2 . This finding is not surprising given that the per-unit emissions α_2 is relatively high. Thus, the location that minimizes cost does not correspond to the lowest level of pollution among the three stakeholder locations, and therefore also to the pollution-minimizing location.

Table 1: *Sourcing, transport and emissions parameter values.*

Parameter	w_1	w_2	t_0	t_1	t_2	α_0	α_1	α_2
Value	1	1	1	2	1	0.1	0.1	0.3

We now consider the impacts of changes in carbon tax. To disentangle the various effects at work, it is both relevant and convenient to distinguish between two cases: first, a short-run equilibrium, in which firm location is assumed to be fixed (i.e. y is exogenous). In this case, the location decision is already made, and adjustments can only be performed on input quantity choices in response to a change in carbon tax (effect on tactical decision). Second, a long-run equilibrium, in which a firm is free to relocate (i.e. y is endogenous). Then, the firm can adjust both its location and input quantity choices in response to a change in carbon tax (effect on both strategic and tactical decisions).

⁷ The calibration of technological and cost parameters in this example is based upon the numerical studies carried out by Peeters and Thisse (2000). For the calibration of the units emissions (in kg CO_2 per unit shipped), we referred to the emissions calculation for air, road, rail and water transport conducted by Hoen et al. (2014). The authors of that study underlined that these emissions parameters are calculated by applying the NTM methodology. They observe that “...there are large differences in emissions and in the ratio of the emissions of two modes. For air and road, it is in the range 8–15, for road and rail 2–5, and for rail and water always 1.6. The ratio of air and water emissions is at most 100”.

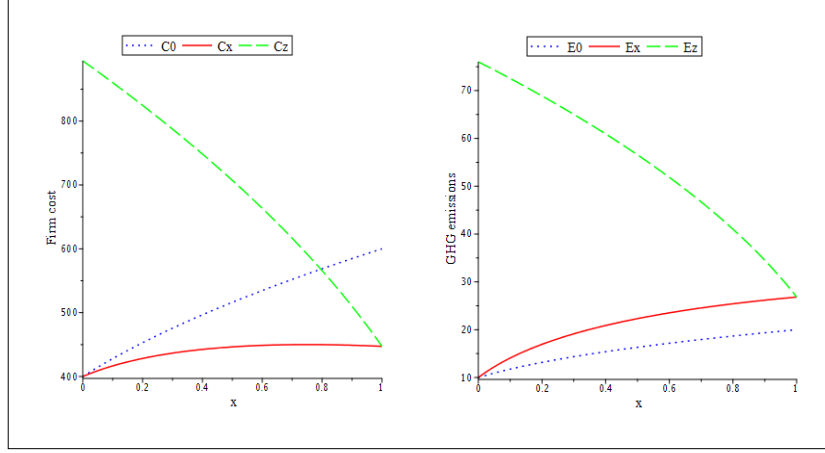


Figure 4: *Costs and pollution levels according to S_1 location.*

5.3. Short-run analysis

When facility location y is given, the impact of the carbon tax on transport-related emissions can be written as follows:

$$\frac{dE}{d\tau} = \alpha_1 d_1 \frac{ds_1^*}{d\tau} + \alpha_2 d_2 \frac{ds_2^*}{d\tau} = -\frac{1}{w_2 + T_2 d_2} s_2^* a_1 \chi^2 < 0$$

with

$$\chi \equiv \frac{\alpha_2 d_2 (w_1 + T_1 d_1) - \alpha_1 d_1 (w_2 + T_2 d_2)}{(w_1 + T_1 d_1)(w_2 + T_2 d_2)}.$$

Thus, the level of transport-related emissions shrinks with a higher carbon tax regardless of the combination choice of the input quantities (s_1, s_2) . Let us examine the adjustment mechanism of the input quantities in response to a change in carbon tax rate. From firm's viewpoint, the production combinations (s_1, s_2) correspond to the upstream cost noted c :

$$c = (w_1 + T_1 d_1) s_1 + (w_2 + T_2 d_2) s_2$$

that can be written as

$$s_2 = -\frac{w_1 + T_1 d_1}{w_2 + T_2 d_2} s_1 + \frac{c}{w_2 + T_2 d_2}.$$

In the space (s_1, s_2) , that equation defines a *isocost* line of slope $-\frac{w_1 + T_1 d_1}{w_2 + T_2 d_2}$ that corresponds to the relative delivered price between the two inputs. When we change the value of c ,

we obtain a set of isocost lines. All the points of an isocost line correspond to the same cost c , and higher isocost lines are associated with higher costs. Conversely, the firm must choose the set of input quantities that allows it to produce exactly the output level q^0 that corresponds to the isoquant. It represents the set of all combinations of input quantities (s_1, s_2) that leads to the same level of output q^0 . The form of this isoquant is hyperbolic and therefore decreasing and convex (see Figure 5). The isoquant slope is given by $-\frac{ds_2}{ds_1}$ that measures the rate at which the firm must substitute one input for the other while keeping the quantity of output q^0 constant. This rate is called the *Marginal Rate of Substitution (MRS)*. It measures the trade-off between the two input quantities at the production level. Minimizing the cost c can therefore be expressed as follows: this is to find the point A on the isoquant curve associated with the lowest possible isocost line. Such a point A is represented in Figure 5. Point A is characterized by a tangency condition: the slope of the isoquant curve must be equal to the slope of the isocost line. In other words, the MRS must be equal to the relative delivered price between the two inputs:

$$-\frac{ds_2}{ds_1} = -\frac{w_1 + T_1d_1}{w_2 + T_2d_2}$$

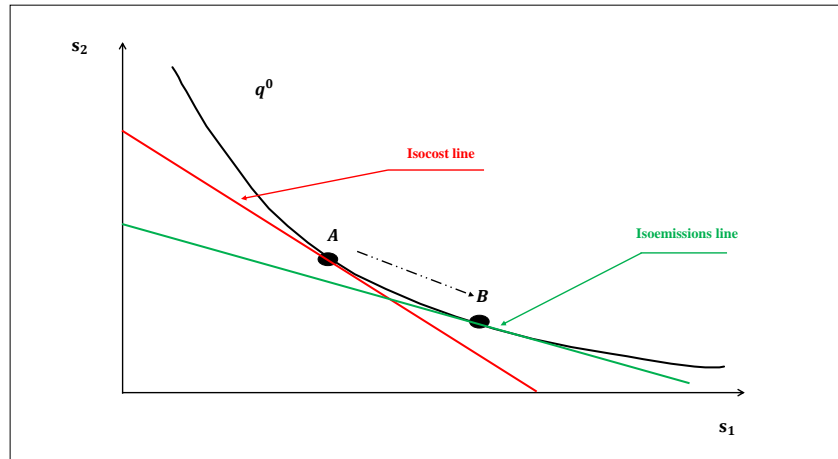


Figure 5: *Isoquant, isocost and isoemissions representations.*

In the same way, but from an ecological standpoint, the input combinations (s_1, s_2) corre-

spond to the carbon emissions level e :

$$e = (\alpha_1 d_1) s_1 + (\alpha_2 d_2) s_2$$

which can be written as

$$s_2 = -\frac{\alpha_1 d_1}{\alpha_2 d_2} s_1 + \frac{e}{\alpha_2 d_2}.$$

In the space (s_1, s_2) , that equation defines an *isoemissions* line of the slope $-\frac{\alpha_1 d_1}{\alpha_2 d_2}$ that corresponds to the ratio of carbon emissions between the two inputs. When we change the value of e , we obtain a set of isoemissions lines. Minimizing carbon emissions from the supply side returns to find the point B on the isoquant curve associated with the lowest possible isoemissions line. Such a point B is represented in Figure 5 and characterized by a tangency condition that is:

$$-\frac{ds_2}{ds_1} = -\frac{\alpha_1 d_1}{\alpha_2 d_2}$$

The point A (respectively B) corresponds to the choice of input quantities (s_1^*, s_2^*) (resp. (s_1^e, s_2^e)) that minimizes the upstream cost function c (resp. the upstream carbon emissions function e) (see Appendix B.1 and Appendix B.4). When carbon tax rises, the optimal input quantities (s_1^*, s_2^*) converge toward input quantities (s_1^e, s_2^e) that generates the lowest emission that can be emitted as $\lim_{\tau \rightarrow +\infty} s_i^* = s_i^e$. Thus, even when input substitution is possible, a larger weight on emissions (due to a higher carbon tax) in the effective shipping cost shifts the input proportions in the direction that lowers emissions. To sum up,

Lemma 3. *For a given firm location, when the firm has substitution opportunities among input quantities, an increased carbon tax reduces transport-related carbon emissions as the relative delivered prices of inputs converge to the system of relative prices, inducing the lowest level of carbon emissions.*

Following this intermediate result, we can expect that an increase in the carbon tax would increase the demand for the less polluting input (*i.e.* the input exhibiting the lowest level of transport-related emissions per unit of shipped input $\alpha_i d_i$) at the expense of the more

polluting input. In other words, the firm would purchase more input quantities for which it would pay a lower carbon tax when the latter increases. However, as shown in Appendix B.5, even though the total emissions decline when the carbon tax increases, the demand for the more polluting input may increase under some conditions. More precisely, we show that

Proposition 3. *For a given location and a given level of production, the quantity of the more polluting input (per unit of shipped input $\alpha_i d_i$) increases when the carbon tax increases if and only if the firm location is such that $\frac{\alpha_2}{\alpha_1} d_2 < d_1 < \hat{d}_1$ when S_1 is more polluting or $\hat{d}_1 < d_1 < \frac{\alpha_2}{\alpha_1} d_2$ when S_2 is more polluting with*

$$\hat{d}_1 \equiv \frac{\alpha_2 w_1 d_2}{\alpha_1 w_2 + d_2(\alpha_1 t_2 - \alpha_2 t_1)} > 0.$$

Therefore, by improving its overall cost through an adjustment of its input quantities, the firm will always reduce its carbon emissions level. However, when the amount of the more polluting input increases, the carbon emission mitigation will be relatively lower than if the amount of the less polluting input was increased. In this latter configuration, the carbon emissions reduction would be more significant. The circumstances of **Proposition 3.** have been refined with regard to the transport modes that the firm uses for its input supply (see Appendix B.6).⁸

5.4. Long-run analysis

In this part, we investigate how both firm's location and production decisions are affected in response to a change in the carbon tax rate in a long term perspective. Based on numerical illustrations, we found that increasing carbon taxation may trigger the firm to change its optimal facility location and inputs mix in order to re-optimize its overall cost. Such a relocation decision may coincide with a significant ecological improvement (*a downward jump of the emissions level*) or may worsen the ecological outcome (*an upward jump of the emissions level*). In the sequel, we propose two explicit numerical parameter settings where

⁸Note that the results for the short-run analysis are obtained by assuming firm interior locations.

emissions could change in either direction as the optimal location changes.⁹

A downward jump of emissions level

We built our example by normalizing the line segment $[S_2, M]$ to 1, and we considered the relative location of supplier S_1 in this segment x equal to 0.2. Let the demand level $q^0 = 100$, and the technical production parameters $a_0 = 1$, $a_1 = 0.3$, and $a_2 = 0.7$. The per-unit procurement and monetary transportation costs; and the per-unit emissions values of the commodities are reported in Table 2.

Table 2: *Data for the example of a downward jump of emissions level.*

Parameter	w_1	w_2	t_0	t_1	t_2	α_0	α_1	α_2
Value	1	1	2	1	3	0.4	0.2	0.2

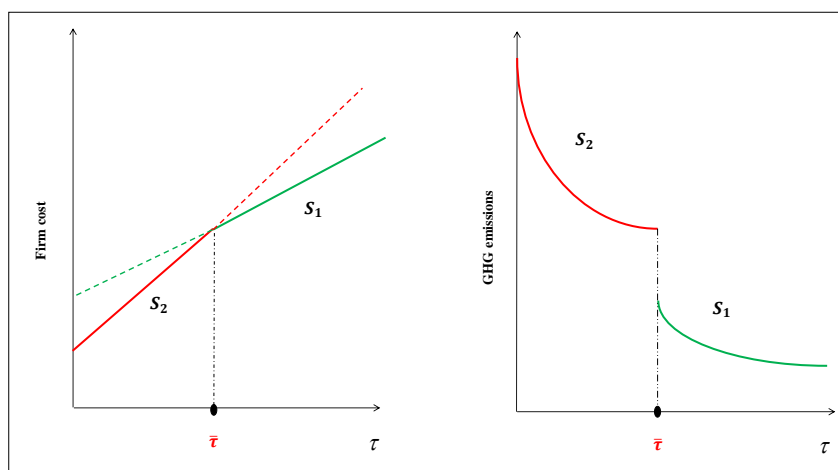


Figure 6: *A double performance relocation.*

Figure 6 provides schematic sketches of the firm's optimal total cost and the resulting GHG emissions graphs as the carbon tax evolves ($\tau \in [0, 30]$). When $\tau < \bar{\tau} = 3.93$ ($\bar{\tau}$ is the critical carbon price which causes firm relocation decision), it is more economically efficient for the firm to locate at the supplier S_2 ; to carry the input 1 from the supplier S_1 ; and to

⁹ The sources for both examples are the same cited in footnote 7.

deliver the output to the market M (see the left side of Figure 6). As already shown in Appendix B.3, S_2 is preferred to S_1 and M is more likely to occur when T_0 is sufficiently low, ζ_2 is sufficiently high, and x is close to 0. These conditions are fulfilled in this example. In fact, supplier S_1 is located relatively near to supplier S_2 ($x = 0.2$). In addition, when the carbon tax is relatively low, output transport ($T_0 = 2 + 0.4\tau$) is sufficiently low and the ratio of the total transport unit cost to the purchasing unit cost of input 2 ($\zeta_2 = 3 + 0.2\tau$) is sufficiently high while the ratio of the total transport unit cost to the purchasing unit cost of input 1 ($\zeta_1 = 1 + 0.2\tau$) is sufficiently low (see Figure 7). Although the total firm cost increases at the supplier S_2 , carbon emissions shrinks with a higher carbon price (see the right side of Figure 6) because the firm gradually substitutes the amount quantity of the input 1 (the more polluting input per unit of shipped input) at the expense of the amount quantity of the local input 2 (the less polluting input) for which it would pay a lower carbon tax.

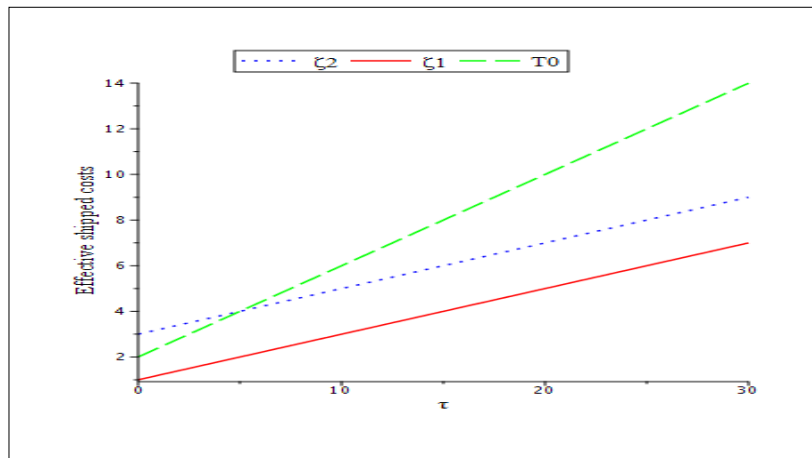


Figure 7: *Effective shipping costs of commodities according to carbon price evolution.*

When $\tau \geq \bar{\tau} = 3.93$, the firm relocates to supplier S_1 to minimize its total cost (see the left side of Figure 6). This may be explained by the fact that when carbon tax is relatively high, the firm would have the incentive to reduce the relatively high increases costs effect in T_0 and ζ_1 compared to ζ_2 (see Figure 7) by moving closer to the output market (i.e, supplier

S_1). Such a relocation is accompanied by a new substitution among the input quantities and, thus, new shipping patterns. The firm purchases a substantial amount of the input 1 obtained at a relatively low delivered price, and reduces the use of the input 2. These new shipping patterns cause a discontinuity and a downward jump of carbon emissions (see the right side of Figure 6). The total rate of reduction of emissions at the critical price triggering the firm relocation is estimated at around 16.80%. Furthermore, the emission reduction rate after the critical price continues to decline as the optimal amount of input 2 (the more polluting input per unit of shipped input in this case) decreases gradually due to a higher carbon tax.

Hence, since the firm can partially influence the input delivered price by adjusting its location, it is more economically beneficial to relocate the production plant towards the increasingly expensive source of input and use more of it. This also allows to a better curb of transport carbon emissions.

Given unit emissions of road and rail transportation modes reported in Table 2 (road transport is at least two times more polluting than rail transport according to Hoen et al. (2014)), we could interpret this configuration where output is delivered by road freight while inputs are shipped by rail transport. Hence, by relocating its production from S_2 to S_1 , the firm reduces its emissions arising from the road transport by getting closer to the market.

An upward jump in emissions level

As in the previous case, we built our example by normalizing the line segment $[S_2, M]$ to 1, and we considered the relative location of supplier S_1 in this segment x equal to 0.9. The demand level $q^0 = 100$, and the production parameters $a_0 = 2$, $a_1 = 0.55$, $a_2 = 0.45$ and the the per-unit procurement and monetary transportation costs; and the per-unit emissions values of the commodities are reported in Table 3.

Table 3: *Data for the example of an upward jump in emissions level.*

Parameter	w_1	w_2	t_0	t_1	t_2	α_0	α_1	α_2
Value	1	1	1	1	7	0.1	0.1	1

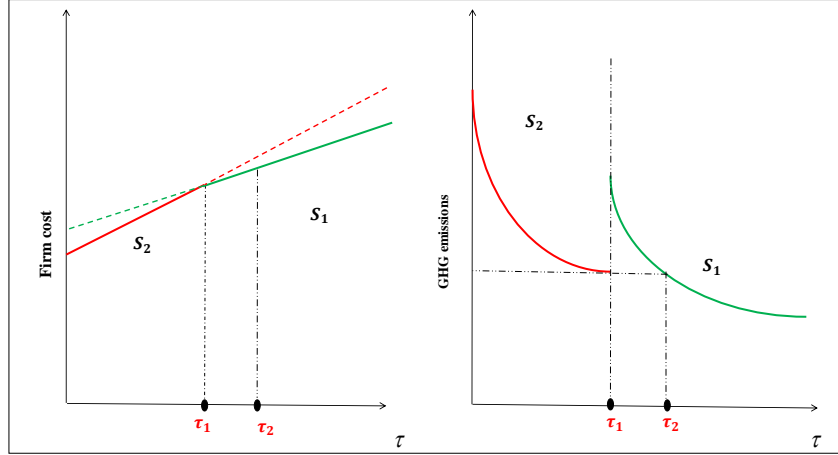


Figure 8: *An increase in carbon tax does not coincide with an ecological improvement.*

Figure 8 is similar to Figure 6 in that it shows how an increase in the carbon tax ($\tau \in [0, 30]$) affects the firm location choice and carbon emission amount. When $\tau < \tau_1 = 8.157$ (τ_1 is the critical carbon price which causes firm relocation decision), firm optimal location is at the supplier S_2 since the effective shipping cost of input 2 ζ_2 is relatively more expensive than output transport T_0 and the effective shipping cost of input 1 ζ_1 (see Figure 9) so that it pays to locate at the input 2 source and to ship input 1 and deliver output. The same effects holds for transport-related carbon emissions mitigation.

When $\tau_1 = 8.157$, firm changes its optimal location to supplier S_1 and its optimal input mix in order to re-optimize its total cost. Such a relocation induces a discontinuity and an upward jump of carbon emissions (see the right side of Figure 8). The total emissions increased by 35.9% compared with that before the jump. After the upward jump, carbon emissions decline with a higher carbon tax (since the firm continues to reduce the proportion of input 2) until they became less than before the upward jump when $\tau > \tau_2 = 25.683$. Therefore, even though the firm location and production adjustments react to *marginal* change in carbon taxation, it does not coincide with an ecological improvement (as long as the rise in carbon tax rate is not too large).

Given unit emissions of road and air transportation modes reported in Table 3 (air transport

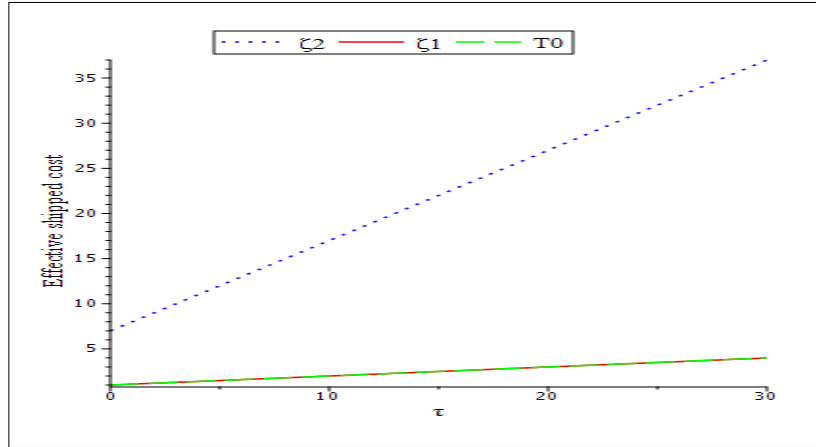


Figure 9: *The effective shipping costs of commodities according to carbon price evolution.*

is at least eight times more polluting than road transport according to Hoen et al. (2014)), we could interpret this configuration where output and input 1 are delivered by road freight while input 2 is shipped by air transport. Hence, by relocating its production from S_2 to S_1 , the firm creates more carbon emissions by using air transportation for carrying raw material from supplier S_2 .

Basic intuitions

To better understand our results, we examine the change in the combination of input quantities along the isoquant curve before and after a firm relocation decision in the previous two examples (location change from supplier 2 to supplier 1). Before the firm decides to change its optimal facility to supplier S_1 , the input mix that minimizes the upstream cost function c (resp. upstream carbon emissions function e) corresponds to the point A (respectively B) (see Figure 10). When the carbon tax rate gradually increases, point A converges toward point B (the optimal amount of input 1 decreases gradually) as *the relative delivered price* of input 2 converges to the relative delivered price leading to the lowest level of carbon emissions (same mechanism as in the short-term case where the location is given (see Figure 5)). However, when carbon tax rate crosses above some threshold, this convergence stops as the firm relocates its facility to supplier 1. Thus, the optimal input mix changes dramatically

as the relative delivered prices between inputs change. Remember that the relative change in the use of the inputs is determined by their relative delivered prices at any location and the delivered prices (the mill price plus the transportation cost) vary with the location of the firm. Hence, when the firm changes its location to the supplier S_1 , there is a substantial change in the relative delivered prices between the inputs and creates a substitution back toward input 1. The new input mix is represented in the isoquant curve by the point A' . This latter leads to new shipping patterns that can generate either a lower level of carbon emissions (a downward jump of the emissions level) or a higher level of carbon emissions (an upward jump of the emissions level). Nevertheless, a larger weight on emissions (due to a higher carbon tax) in the effective shipping costs shifts the new input proportions A' in the direction that lowers emissions at point B' (the optimal amount of input 2 decreases gradually).

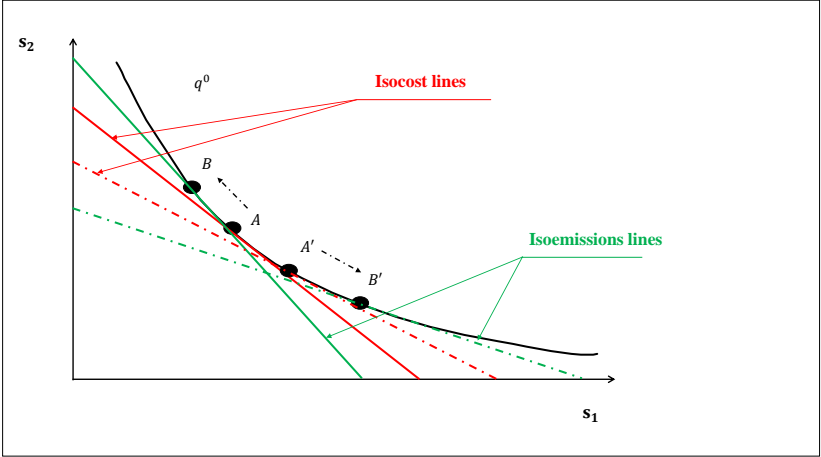


Figure 10: *Effect of carbon tax on changing the relative delivered price of inputs.*

These results illustrate how a marginal change in carbon tax can cause dramatic changes in firm optimal location, the combination of inputs, and the ecological outcome. Accounting for these effects makes the impact of a higher carbon tax more ambiguous when the input materials are substitutable. Mainly, because their net effects depend on whether the new spatial pattern is better or worse from an environmental viewpoint.

6. Discussion and conclusion

This paper studies the effect of carbon taxation on firms' facility location decisions. Based on a stylized facility location model on a linear network, we evaluate the cost-minimizing and emissions-minimizing facility location decisions and analyze when they do/do not coincide, under two alternative production technology settings, namely Leontief and Cobb-Douglas. In the Leontief case where input proportions are fixed, no tax is required in a mono modal scheme because economic and environment locations match.¹⁰ In a multi modal scheme, carbon taxation encourages the firm to relocate its facility in a way that generates lower levels of transport related emissions. Our framework also allows us to derive some unsuspected results when producers can change the combination of inputs to produce their commodities (Cobb-Douglas technology). For a given location, an increase in carbon tax reduces transport-related carbon emissions of the supply order as the *relative delivered prices* of inputs converge to the relative delivered prices, leading to the lowest level of carbon emissions. When the firm is free to relocate, by affecting the relative delivered prices of inputs, a small change in carbon tax rates may trigger the firm to relocate to re-optimize its cost, inducing a new substitution among input quantities and, thus, a new shipping pattern that may either yield large environmental benefits or increase transport-related pollution. Therefore, when implementing carbon taxation, one must account for their impacts on the location of economic activities. Taxes are known to produce unintended consequences, and this appears to be one such instance especially because multiple variables (input mix and location) are allowed to vary simultaneously.

Our paper addresses a major issue. When assessing the merits of carbon taxation policies, the existing literature disregards one major problem: *a higher carbon tax may change the combination of inputs*. Thus, our finding implies that the studies of carbon taxation policy should be *also* conducted within a framework in which production technology can allow sub-

¹⁰Such a result arises because unit costs of transport T_i do not vary with the volume of commodities to be shipped.

stitution among inputs. For example, in the case of a given location, our analysis reveals that even though the total emissions decline when the carbon tax increases, the demand for the more polluting input may increase under some conditions regardless of modal transportation schemes. Such a result may arise because changes in carbon taxation modify the relative delivered prices of inputs. The relative prices of more polluting inputs may become lower as a rise in carbon taxation applies to all inputs. In addition, when the firm adjusts the location of its facility, it may also reduce the relative delivered price for the more polluting input. This explain why a relocation of facility may generate a higher level of pollution.

We expect that our paper touches on an important research topic and sheds new light on facility location analysis when we study the efficiency of environmental policies. It is worth stressing that our main findings do not depend on assumptions associated with the representation of space and the number of suppliers/markets. Indeed, we could consider a more general economic space. Our results remain valid even if we assume a network defined by a finite set of topological arcs which connect different pairs of vertices that correspond to locations endowed with some degree of centrality in the transportation system. In this case, the distance between two places is given by the length of the shortest path that connects these locations and the firm chooses the arc ℓ and the location $y \in \ell$ that minimize its cost. In addition, our results hold if we consider more inputs and final markets in a context of two-dimensional space. Even though the optimal location does not necessarily match with a supplier or a final market, Peeters and Thisse (2000) have showed that, when the production-location problem is extended to allow for the substitution between input sources, substantial jumps in the optimal firm location can occur (their simulations consider ten final markets and five inputs). Of course, such assumptions would influence the magnitude of effects. The fact that a marginal increase of the carbon tax may lead either to an increase of the emissions or to a large fall in emissions depends on two key assumptions: *(i)* the firm can substitute between inputs (there exist different technological combinations of inputs to produce a given quantity of output) and *(ii)* relocation of facility in response to changes in total transport costs (the demand for inputs depends on the delivered price, i.e., the mill price plus the

transportation cost, which varies with the location of the firm). Hence, we show that the type of production technology and facility location merits more attention when we study the carbon footprint of firms.

Our approach, however, has limitations that can provide guidance for further research and warrants in-depth studies in the field. For instance, we assume that access to output and inputs markets is the first-order effect on facility location decisions and firms adjust the location of their facilities in response to changes in carbon tax on transportation. In our approach, regional labor cost/availability and profit taxation are left aside. In a survey of empirical evidence concerning the determinants of location choices by multinational firms for their production affiliates, Fontagné and Mayer (2005) find that accessibility to customers and input suppliers are powerful attractors of firms. Even though low labor costs and taxes matter in location decisions, empirical works have shown that such factors are relatively less important than the accessibility to intermediate goods and to customers. Regarding taxation on profits, it may have a little incidence because of tax optimization by multinationals allowing them to relocate their profits significantly (location of profits differs from the location of facilities). The United States and the Euro area remain the largest recipients of foreign investments in 2017 (see the World Investment Report 2018 ¹¹). Within countries, a good access to suppliers and customers is the key driver of the location of activities (Combes and Overman, 2004). As a result, extending our framework by considering spatial differences in taxation and the price/availability of labor should not alter our main findings. Furthermore, the model only considers carbon emissions from transportation but not from production. As the driver of the main result is the possibility of input substitution, it might be interesting to explore the emission implications due to changes in location by including the production-related emissions. Our model could be augmented by introducing emissions stemming from the production of output and inputs. Introducing a tax on pollution generated on production does not affect our results, as output level is an exogenous parameter. However, taking account the pollution arising from input production induces an additional

¹¹A report published by UNCTAD (2018).

effect. Each modification of combination of inputs changes the total amount of supply and then will induce a change in upstream emission levels. We do not know a priori if the effect of a change in facility change on total carbon emissions is magnified or reversed when pollution stemming from input production is also considered. It depends on the assumption on the amounts of pollution generated by one unit of production for each input. Indeed, if the more distant input supplier is also the more polluting supplier in terms of production, our results hold. It depends also on whether the price of input (w_i) internalizes the cost of pollution stemming from production. If the prices of inputs accurately reflect the environmental externality generated by the production of inputs, then our results remain qualitatively valid. Hence, it is unclear how the total level of pollution emissions adjusts to carbon taxation when both transportation- and production-related emissions are considered in our framework. The implications are difficult to forecast as it is necessary to perform case-by-case analysis (according to the features of industries). Nevertheless, a location jump due to a marginal increase of the carbon tax will still occur in this context.

Our theoretical contribution is in accordance with some empirical works. For example, in the case of the cement industry, Bosco and Altomonte (2013) showed that the EU cap-and-trade system on emissions could generate relocations leading to higher transport flows and therefore more emissions. Our work must be viewed as a first step toward a general model of sustainable facility location. For example, our model could be extended to account for uncertain demand, capacity constraint, and more general production function. We believe, however, that our results are sufficiently convincing to encourage researchers and engineers to pay more attention to the role played by the substitution among inputs and facility location in various implications of carbon taxation.

Appendix A. Appendix Leontief case

Appendix A.1. Proof of Lemma 1

Consider the situation where the firm is indifferent to being located between two endpoints of the segments $[S_2, S_1]$ and $[S_1, M]$.¹²

- If $\frac{dC^a}{dy} = 0$, the firm is indifferent to being located at $S_2(0)$ or $S_1(x)$, and

$$a_2 = P_{0x}(a_1) \equiv \frac{T_1}{T_2}a_1 + \frac{T_0}{T_2}$$

- Likewise, if $\frac{dC^b}{dy} = 0$, the firm is indifferent to being located at $S_1(x)$ or $M(z)$, and

$$a_2 = P_{xz}(a_1) \equiv -\frac{T_1}{T_2}a_1 + \frac{T_0}{T_2}$$

Thus, we can determine the optimal location conditions of each corner solution in each segment by defining the following thresholds:

- If $a_2 < P_{0x}(a_1)$ then $S_2(0)$ is preferred to $S_1(x)$; that is $y^* = 0$.
- If $a_2 > P_{0x}(a_1)$ then $S_1(x)$ is preferred to $S_2(0)$; that is $y^* = x$.
- If $a_2 < P_{xz}(a_1)$ then $S_1(x)$ is preferred to $M(z)$; that is $y^* = x$.
- If $a_2 > P_{xz}(a_1)$ then $M(z)$ is preferred to $S_1(x)$; that is $y^* = z$.

Appendix A.2. Pollution minimizing location

Under Leontief technology input demand, the firm transport-related emissions function $E(y)$ is given by

$$E(y) = \left[\alpha_0 d_0 + \sum_{i=1}^2 \alpha_i d_i a_i \right] q^0$$

¹²Notice that when $\frac{dC^a}{dy} = 0$ or $\frac{dC^b}{dy} = 0$, the firm is not only indifferent to being located at the endpoints of the segment $[S_2, S_1]$ or $[S_1, M]$, respectively, but over all the points of each segment. Therefore, interior solutions may exist.

with:

$$d_1 = |x - y| \Leftrightarrow \begin{cases} x - y, & \text{when F is between } S_2 \text{ and } S_1 \text{ Case a : } E^a \\ y - x, & \text{when F is between } S_1 \text{ and } M \text{ Case b : } E^b \end{cases}$$

Because $\frac{d^2E}{dy^2} = 0$, there is no interior solution, and the solutions are necessarily at the segments' corners, so $y^e = 0$, $y^e = x$, or $y^e = z$ are purely ecological equilibrium solutions. This result comes from the shape of the function E , which is linear in y ; thus, the derivative is constant and either positive or negative. The derivative's sign leads to the optimal ecological location of the firm. Therefore, it is sufficient to consider the two cases:

- Case a: if $0 \leq y \leq x$, then: $\frac{dE^a}{dy} = (-\alpha_0 - a_1\alpha_1 + a_2\alpha_2)q^0$
- Case b: if $x \leq y \leq z$, then: $\frac{dE^b}{dy} = (-\alpha_0 + a_1\alpha_1 + a_2\alpha_2)q^0$

Thus, the optimal environmental location depends only on production technology and emission parameters. Consider the situation of indifference between two endpoints of the segments $[S_2, S_1]$ and $[S_1, M]$, similar to the situation of identifying the maximum profit location.

- If $\frac{dE^a}{dy} = 0$, the firm is indifferent to being located in $S_2(0)$ or $S_1(x)$, and

$$a_2 = E_{0x}(a_1) \equiv a_1 \frac{\alpha_1}{\alpha_2} + \frac{\alpha_0}{\alpha_2}.$$

- If $\frac{dE^b}{dy} = 0$, the firm is indifferent to being located in $S_1(x)$ or $M(z)$, and

$$a_2 = E_{xz}(a_1) \equiv -a_1 \frac{\alpha_1}{\alpha_2} + \frac{\alpha_0}{\alpha_2}.$$

Thus, we can determine the optimal location conditions from a purely environmental standpoint of each corner solution in each segment by defining the following thresholds:

- If $a_2 < E_{0x}(a_1)$ then $S_2(0)$ is preferred to $S_1(x)$; that is $y^* = 0$.
- If $a_2 > E_{0x}(a_1)$ then $S_1(x)$ is preferred to $S_2(0)$; that is $y^* = x$.
- If $a_2 < E_{xz}(a_1)$ then $S_1(x)$ is preferred to $M(z)$; that is $y^* = x$.
- If $a_2 > E_{xz}(a_1)$ then $M(z)$ is preferred to $S_1(x)$; that is $y^* = z$.

Appendix A.3. Superposition possibilities of economic and environmental thresholds

Remember that from a firm's standpoint, $a_2 = P_{0x}(a_1)$ occurs when the firm is indifferent to being located in 0 or in x and, $a_2 = P_{xz}(a_1)$ occurs when the firm is indifferent to being located in x or in z . Equally, from a purely ecological view, $a_2 = E_{0x}(a_1)$ occurs when the firm is indifferent to being located in 0 or in x , and $a_2 = E_{xz}(a_1)$ occurs when the firm is indifferent to being located in x or in z . In addition, $P_{0x}(0) = P_{xz}(0) = \frac{T_0}{T_2}$ and $E_{0x}(0) = E_{xz}(0) = \frac{\alpha_0}{\alpha_2}$ whereas $P_{xz}(\frac{T_0}{T_1}) = 0$ and $E_{xz}(\frac{\alpha_0}{\alpha_1}) = 0$, as illustrated in Figure 3.

We have $P_{0x}(0) \geq E_{0x}(0)$ if and only if $t_2\alpha_0 - t_0\alpha_2 \leq 0$ and $P_{0x}(a_1) \geq E_{0x}(a_1)$. Then, we must consider two sub-cases:

- when $t_1\alpha_2 - t_2\alpha_1 > 0$, then $a_1 \geq \hat{a}_1$
- when $t_1\alpha_2 - t_2\alpha_1 < 0$, then $a_1 \leq \hat{a}_1$

with:

$$\hat{a}_1 \equiv \frac{t_2\alpha_0 - t_0\alpha_2}{t_1\alpha_2 - t_2\alpha_1}.$$

Four configurations must be taken into account where $P_{0x}(a_1) \geq E_{0x}(a_1)$.

1. $t_1\alpha_2 - t_2\alpha_1 > 0$ and $t_2\alpha_0 - t_0\alpha_2 \leq 0$
2. $t_1\alpha_2 - t_2\alpha_1 > 0$ and $t_2\alpha_0 - t_0\alpha_2 > 0$
3. $t_1\alpha_2 - t_2\alpha_1 < 0$ and $t_2\alpha_0 - t_0\alpha_2 \leq 0$
4. $t_1\alpha_2 - t_2\alpha_1 < 0$ and $t_2\alpha_0 - t_0\alpha_2 > 0$

The same analysis can be performed for the condition $P_{xz}(a_1) \leq E_{xz}(a_1)$.

Appendix B. Appendix Cobb-Douglas case

Appendix B.1. Input demand

We want to determine the optimal input supply $s^*(s_1^*, s_2^*)$ that minimizes the total cost function $C(s, y)$ under the Cobb-Douglas production function constraint, which can be written

as:

$$s^*(y) = \text{Min}_{s_1, s_2} \sum_{i=1}^2 (w_i + t_i d_i + \tau \alpha_i d_i) s_i$$

subject to

$$\begin{aligned} q^0 &= a_0 s_1^{a_1} s_2^{a_2} \\ s &\geq 0 \end{aligned}$$

Using the functional form of the Cobb-Douglas production function $q^0 = a_0 s_1^{a_1} s_2^{a_2}$, the supply for each input can be written as follows:

$$\begin{cases} s_1 = \left(\frac{q^0}{a_0}\right)^{\frac{1}{a_1}} s_2^{-\frac{a_2}{a_1}} \\ s_2 = \left(\frac{q^0}{a_0}\right)^{\frac{1}{a_2}} s_1^{-\frac{a_1}{a_2}} \end{cases} \quad (\text{B.1})$$

The total cost function can be then rewritten according to only one of each input supply (B.1). Then, the stationary point is determined by solving the following system:

$$\begin{cases} \frac{\partial C(s)}{\partial s_1} = -\frac{a_1}{a_2} (w_2 + T_2 d_2) \left(\frac{q^0}{a_0}\right)^{\frac{1}{a_2}} s_1^{-\frac{1}{a_2}} + w_1 + T_1 d_1 = 0 \\ \frac{\partial C(s)}{\partial s_2} = -\frac{a_2}{a_1} (w_1 + T_1 d_1) \left(\frac{q^0}{a_0}\right)^{\frac{1}{a_1}} s_2^{-\frac{1}{a_1}} + w_2 + T_2 d_2 = 0 \end{cases}$$

We therefore determine the following stationary point:

$$\begin{cases} s_1 = \left(\frac{q^0}{a_0}\right) \left[\frac{a_1(w_2 + T_2 d_2)}{a_2(w_1 + T_1 d_1)}\right]^{a_2} \\ s_2 = \left(\frac{q^0}{a_0}\right) \left[\frac{a_2(w_1 + T_1 d_1)}{a_1(w_2 + T_2 d_2)}\right]^{a_1} \end{cases}$$

The calculation of the second partial derivative shows that this stationary point is a minimum.

$$\left\{ \begin{array}{l} \frac{\partial^2 C(s)}{\partial s_1^2} = \frac{a_1}{a_2^2} (w_2 + T_2 d_2) \left(\frac{q^0}{a_0}\right)^{\frac{1}{a_2}} s_1^{\frac{a_2-2}{a_2}} > 0 \\ \frac{\partial^2 C(s)}{\partial s_2^2} = \frac{a_2}{a_1^2} (w_1 + T_1 d_1) \left(\frac{q^0}{a_0}\right)^{\frac{1}{a_1}} s_2^{\frac{a_1-2}{a_1}} > 0 \end{array} \right.$$

Appendix B.2. Cost-minimizing location

We show that there is no interior solution. Some standard calculations lead to

$$\frac{dC(y)}{dy} = -T_0 q^0 + \Psi q^0 (\zeta_1 d_1 + 1)^{a_1} (\zeta_2 d_2 + 1)^{a_2} \left[\frac{a_1 \zeta_1 \frac{dd_1}{dy}}{\zeta_1 d_1 + 1} + \frac{a_2 \zeta_2}{\zeta_2 d_2 + 1} \right]$$

If $y > x$ then $\frac{dd_1}{dy} = -1$ and

$$\frac{d^2 C(y)}{dy^2} = -\Psi a_1 a_2 q^0 (\zeta_1 d_1 + 1)^{a_1} (\zeta_2 d_2 + 1)^{a_2} \left(\frac{\zeta_1}{\zeta_1 d_1 + 1} + \frac{\zeta_2}{\zeta_1 d_1 + 1} \right)^2 < 0$$

If $y < x$ then $\frac{dd_1}{dy} = 1$ and:

$$\frac{d^2 C(y)}{dy^2} = -\Psi a_1 a_2 q^0 (\zeta_1 d_1 + 1)^{a_1} (\zeta_2 d_2 + 1)^{a_2} \left(\frac{\zeta_1}{\zeta_1 d_1 + 1} - \frac{\zeta_2}{\zeta_1 d_1 + 1} \right)^2 < 0$$

The cost function is concave over the interval $[0, x]$ and the interval $[x, z]$. Then, the cost-minimizing location is given by 0, x or z .

Appendix B.3. Cost-minimizing location circumstances

Set the following differential equations:

$$\Delta_{0x} \equiv C_0 - C_x = [T_0 x + \Psi ((\zeta_1 x + 1)^{a_1} - (\zeta_2 x + 1)^{a_2})] q_0,$$

$$\Delta_{zx} \equiv C_z - C_x = [-T_0(z - x) - \Psi [(\zeta_1(z - x) + 1)^{a_1} (\zeta_2 z + 1)^{a_2} - (\zeta_2 x + 1)^{a_2}]] q_0,$$

$$\Delta_{z0} \equiv C_z - C_0 = [-T_0 z + \Psi [(\zeta_1(z - x) + 1)^{a_1} (\zeta_2 z + 1)^{a_2} - (\zeta_1 x + 1)^{a_1}]] q_0.$$

Hence, for a given optimal solution candidate, the analysis of the signs of two differential equations in which this candidate is considered allows us to deduce sufficient and necessary

conditions for the optimality of this solution. Thus, cost-minimizing location is given by $y^* = 0$ if and only if $\Delta_{0x} < 0$ and $\Delta_{z0} > 0$, $y^* = x$ if and only if $\Delta_{0x} > 0$ and $\Delta_{zx} > 0$ and $y^* = z$ if and only if $\Delta_{zx} < 0$ and $\Delta_{z0} < 0$. However, it is difficult to explore the analytical direction to determine the circumstances for each optimal location candidate. Using some numerical examples and standard calculations, we can deduce the most likely values of parameters for which the previous conditions are met. We focus here on the role of the effective shipping costs (ζ_1 , ζ_2 , and T_0) and the location of supplier S_1 (x). We have considered $q^0 = 10$ and the following technical production parameters: $a_0 = 1$, $a_1 = 0.5$, and $a_2 = 0.5$. The results indicated that

- S_2 is preferred to S_1 and M is more likely to occur when T_0 is sufficiently low, ζ_2 is sufficiently high, and x is close to 0.
- M is preferred to S_1 and S_2 is more likely to occur when T_0 is sufficiently high, ζ_2 is sufficiently low, and x is close to z .
- S_1 is more likely to occur when ζ_2 , T_0 , and x achieve relatively intermediate values.

Appendix B.4. Minimizing pollution inputs demand

We want to determine the optimal input supply (s_1^e, s_2^e) that minimizes the total emissions level $E(s, y)$ under the Cobb-Douglas production function constraint, which can be written as:

$$s^e(y) = \text{Min}_{s_1, s_2} \sum_{i=1}^2 \alpha_i d_i s_i$$

subject to

$$q^0 = a_0 s_1^{a_1} s_2^{a_2}$$

$$s \geq 0$$

The total carbon emissions function can be then rewritten according to only one of each input supply (see Equation (B.1)). Then, the stationary point is determined by solving the

following system:

$$\begin{cases} \frac{\partial E(s)}{\partial s_1} = -\frac{\alpha_1}{a_2}(\alpha_2 d_2)\left(\frac{q^0}{a_0}\right)^{\frac{1}{a_2}} s_1^{-\frac{1}{a_2}} + \alpha_1 d_1 = 0 \\ \frac{\partial E(s)}{\partial s_2} = -\frac{\alpha_2}{a_1}(\alpha_1 d_1)\left(\frac{q^0}{a_0}\right)^{\frac{1}{a_1}} s_2^{-\frac{1}{a_1}} + \alpha_2 d_2 = 0 \end{cases}$$

We therefore determine the following stationary point:

$$\begin{cases} s_1^e = \left(\frac{q^0}{a_0}\right) \left(\frac{a_1 d_2 \alpha_2}{a_2 d_1 \alpha_1}\right)^{a_2} \\ s_2^e = \left(\frac{q^0}{a_0}\right) \left(\frac{a_2 d_1 \alpha_1}{a_1 d_2 \alpha_2}\right)^{a_1} \end{cases}$$

The calculation of the second partial derivative shows that this stationary point is a minimum.

$$\begin{cases} \frac{\partial^2 E(s)}{\partial s_1^2} = \frac{\alpha_1}{a_2^2}(\alpha_2 d_2)\left(\frac{q^0}{a_0}\right)^{\frac{1}{a_2}} s_1^{\frac{a_2-2}{a_2}} > 0 \\ \frac{\partial^2 E(s)}{\partial s_2^2} = \frac{\alpha_2}{a_1^2}(\alpha_1 d_1)\left(\frac{q^0}{a_0}\right)^{\frac{1}{a_1}} s_2^{\frac{a_1-2}{a_1}} > 0 \end{cases}$$

Note that pollution minimizing input quantities (s_1^e, s_2^e) do not depend on the tax level τ , unlike the cost minimizing input quantities (s_1^*, s_2^*) .

Appendix B.5. Proof of Proposition 3

The pollution level depends on the distances to suppliers ($d_1 = |x - y|$ and $d_2 = y$), the transport mode and the level of demand for each input. Optimal economic quantities (s_1^*, s_2^*) show that the carbon tax modifies the demand for each input through an increase in its total delivered price $w_i + T_i d_i$ but also through a change in the relative delivered price $\frac{w_i + T_i d_i}{w_j + T_j d_j}$ with $i \neq j$ between inputs, which causes a substitution effect between the amounts of inputs. Indeed:

$$\begin{cases} \frac{ds_1^*}{d\tau} = s_1^* a_2 \left(\frac{1}{\sigma}\right) \left(\frac{d\sigma}{d\tau}\right) \\ \frac{ds_2^*}{d\tau} = -s_2^* a_1 \left(\frac{1}{\sigma}\right) \left(\frac{d\sigma}{d\tau}\right) \end{cases} \quad (\text{B.2})$$

where σ is the ratio between the amount of inputs:

$$\sigma \equiv \frac{s_1^*}{s_2^*} = \frac{a_1(w_2 + T_2 d_2)}{a_2(w_1 + T_1 d_1)} > 0$$

Standard calculations reveal that $\frac{d\sigma}{d\tau} = \sigma\chi$ with $\chi \equiv \frac{\alpha_2 d_2 (w_1 + T_1 d_1) - \alpha_1 d_1 (w_2 + T_2 d_2)}{(w_1 + T_1 d_1)(w_2 + T_2 d_2)}$.

We can already notice that variation signs of optimal input quantities (s_1^*, s_2^*) are opposite, regardless of the variation in carbon tax (see equation (B.2)). In other words, an increase in quantity s_i^* necessarily leads to a decrease in the other one s_j^* with $i \neq j$. The sign of variation of each quantity s_i^* will depend on the sign of the parameter χ . Hence,

- If $\chi > 0$, then the quantity of s_1^* increases and s_2^* decreases
- If $\chi < 0$, then the quantity of s_2^* increases and s_1^* decreases

Suppose that supplier S_1 is the most polluting per unit of shipped input, that is $(\alpha_2 d_2 < \alpha_1 d_1)$. Whereas $\chi > 0$ (the quantity of s_1^* rises) if and only if

$$d_1 < \hat{d}_1 \quad (\text{B.3})$$

with,

$$\hat{d}_1 \equiv \frac{\alpha_2 w_1 d_2}{\alpha_1 w_2 + d_2(\alpha_1 t_2 - \alpha_2 t_1)} > 0$$

Considering the level of emissions per unit of the transported input, the expression (B.3) can be written as $\alpha_1 d_1 < \alpha_1 \hat{d}_1$. As we have assumed $\alpha_2 d_2 < \alpha_1 d_1$, then, $\alpha_2 d_2 < \alpha_1 d_1 < \alpha_1 \hat{d}_1$. Finally, the following condition is obtained:

$$\frac{\alpha_2}{\alpha_1} d_2 < d_1 < \hat{d}_1$$

The same analysis can be performed under the assumption that supplier S_2 is the most polluting per unit of shipped input ($\alpha_1 d_1 < \alpha_2 d_2$). We find the following condition:

$$\hat{d}_1 < d_1 < \frac{\alpha_2}{\alpha_1} d_2$$

Appendix B.6. Transport modes analysis

Let us examine the circumstances of **Proposition 3** with regard to transportation modes. Each mode is achieved by its transport unit cost t_i and emissions unit level α_i per unit of input. Consider that the firm uses the same transport technology for its inputs supply, meaning that $\alpha_1 = \alpha_2$ and $t_1 = t_2$. Then, the most polluting input is necessarily the furthest input. In this case, $\hat{d}_1 = \frac{w_1}{w_2} d_2$; then, $d_2 < \hat{d}_1$ implies $w_2 < w_1$, and $d_2 > \hat{d}_1$ implies $w_2 > w_1$. Hence, from **Lemma 4**, the firm can increase the quantity for the furthest input when the carbon tax increases, provided that its relative price is high enough. This case is more likely to occur when the price gap ($\frac{w_i}{w_j}$ with $i \neq j$ such as input i is the most polluting and input j is the less polluting input) increases. The growth rate of the delivered price ($w_j + T_j d_j$) is higher for the cheaper input when the carbon tax increases. In other words, *the relative* delivered price of the more expensive input declines with carbon tax under these circumstances. This means that a higher tax burden leads to a convergence between the delivered input prices. It follows that in the mono-modal transport scheme, when the carbon tax increases, the relative demand for the furthest and more polluting input i may increase if $w_i - w_j > 0$ with $i \neq j$.

From **Proposition 3**, (a) when $d_2 < d_1 < \hat{d}_1$, then: $y \in]0, d_1]$ such as: $d_1 < \frac{x}{2}$ and (b) when $\hat{d}_1 < d_1 < d_2$, then: $y > d_1$ such as: $d_1 > \frac{x}{2}$. Hence,

Corollary 1. *For a mono-modal transport mode, when the carbon tax increases, the quantity of the more polluting input increases when the firm is located near the cheapest input source.*

Whether the transport technologies for carrying inputs are different, the analysis is richest. Let us consider the configuration $\frac{\alpha_2}{\alpha_1} d_2 < d_1 < \hat{d}_1$ when S_1 is the more polluting supplier. Under this configuration, we must consider two cases.

Case a: When $\alpha_1 t_2 - \alpha_2 t_1 > 0$, $\frac{\alpha_2}{\alpha_1} d_2 < \hat{d}_1$ holds if and only if $w_2 < w_1$ and $d_2 < \underline{d}_2$, with

$$\underline{d}_2 \equiv \frac{\alpha_1(w_1 - w_2)}{\alpha_1 t_2 - \alpha_2 t_1}.$$

Hence, as in the mono-modal transportation scheme, the quantity of the more polluting input increases when the carbon tax increases, provided that its price is high enough (high w_1), and the less polluting supplier (S_2) is not too far ($d_2 < \underline{d}_2$).

Case b: When $\alpha_1 t_2 - \alpha_2 t_1 < 0$, $\frac{\alpha_2}{\alpha_1} d_2 < \hat{d}_1$ holds if and only if $w_1 < w_2$ and $\underline{d}_2 < d_2 < \bar{d}_2$, with

$$\bar{d}_2 \equiv \left| \frac{\alpha_1 w_2}{\alpha_2 t_1 - \alpha_1 t_2} \right|$$

This case reveals that the firm may increase the quantity of the more polluting input provided that its price is cheaper (low w_1), and that the less polluting supplier (S_2) is neither too far nor too close ($\underline{d}_2 < d_2 < \bar{d}_2$).

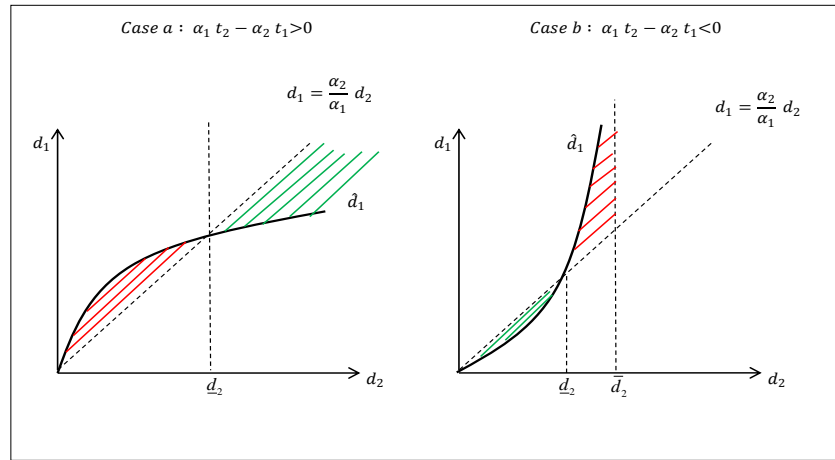


Figure B.11: *Asymmetric effect of carbon tax.*

Figure B.11 illustrates the circumstances of the previous two cases when S_1 is the more polluting supplier per unit of shipped input. In the space $(d_1; d_2)$ is depicted the function

\hat{d}_1 with case a (resp. case b) when $\alpha_1 t_2 - \alpha_2 t_1 > 0$ (resp. $\alpha_1 t_2 - \alpha_2 t_1 < 0$). The area cross-hatched with red fulfills the conditions of case a ($\frac{\alpha_2}{\alpha_1} d_2 < d_1 < \hat{d}_1$ and $d_2 < \underline{d}_2$) and those for case b ($\frac{\alpha_2}{\alpha_1} d_2 < d_1 < \hat{d}_1$ and $\underline{d}_2 < d_2 < \bar{d}_2$). Therefore, a firm's location lying under these conditions of distances should increase the amount of the more polluting input (input 1) when the carbon tax increases.

A similar analysis is obtained when S_2 is the more polluting supplier. In Figure B.11, the area cross-hatched in green fulfills the conditions for which the firm increases the amount of the more polluting input (input 2) when the carbon tax increases.

This outcome demonstrates the asymmetric effect of a higher carbon tax by increasing the share of the most polluting input under some conditions when we allow substitution among inputs.

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