

# Interpretable machine learning model for autogenous shrinkage prediction of low-carbon cementitious materials

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1	Interpretable Machine Learning Model for Autogenous Shrinkage
2	Prediction of Low-Carbon Cementitious Materials
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8	Highlights
9	• A large database about the autogenous shrinkage of concrete with SCM is built
10	• Ensemble machine learning models can predict the autogenous shrinkage efficiently
11	• ML models can perform better than B4 and CEB models modified versions.
12	• SCM influence can be interpreted using SHAP analysis
13	• Insights into blended cement concrete shrinkage behavior can be envisioned.
14	C
15	Abstract
16	Supplementary cementitious materials (SCM) are key components of low-carbon
17	cementitious materials. However, their effects, especially for the emerging high cement
18	replacement ratio formulations, are sometimes very challenging to predict, leading to restrictions
19	in most standards. Through advanced Machine Learning techniques, this study provides novel
20	insights into the autogenous shrinkage properties of concrete containing various kinds of
21	supplementary cementitious materials such as slag, fly ash, silica fume, calcined clay, and filler.
22	Four machine learning models are optimized and their predictions are compared on a dedicated
23	database, including ternary and quaternary cement blends. The Extreme Gradient Boosting
24	(XGBoost) model exhibited the highest accuracy among these models. Interpretative tools such as
25	SHAP analysis are then used to obtain novel information about the relative influence of the SCM
26	on the autogenous shrinkage depending on their dosage. The model is finally compared to the
27	recently modified versions of the B4 and the CEB analytical models to predict the autogenous
28	shrinkage of unknown concrete formulations. The model showed significantly better predictions
29	than the analytical models, and a web application is proposed, paving the way for precise and

30 interpretable autogenous shrinkage predictions of cementitious materials incorporating SCM.

31

Keywords: Concrete; Autogenous Shrinkage; Supplementary Cementitious Material (SCM);
 Machine Learning; XGBoost; Shrinkage Models.

34

# 35 **1 Introduction**

Decreasing cementitious materials' carbon footprint is necessary to limit the overall 36 environmental impact of the construction industry. This decrease can be achieved through several 37 techniques such as the construction and demolition waste (CDW) usage, for example, the use of 38 crushed concrete waste into Recycled Aggregate Concrete (RAC) [1], or the extensive use of 39 40 supplementary cementitious materials, some of them being industrial byproducts [2-4]. However, these additions considerably impact the behavior of cementitious materials, and, because of these 41 rapid evolutions, such novel components are rarely very well understood nor precisely considered 42 43 in the construction standards. More specifically, it is generally admitted that concrete early age deformations can induce severe structural evolutions. Apart from environmental degradations, 44 45 these deformations are mostly due to shrinkage and creep mechanisms [5]. For example, highperformance and ultra-high performance concrete (HPC and UHPC) exhibit significant early age 46 deformations because of their low water-to-cement ratio. Indeed, while deformation of normal 47 48 strength concrete is primarily governed by drying shrinkage, which occurs some weeks or months 49 after setting due to a water loss, deformation in low water-to-cement concrete can develop very 50 quickly at an early age because of the rapid evaporation of water from the surface of the specimen, 51 namely plastic shrinkage, or because of the consumption of water during the hydration directly causing chemical shrinkage, and generating capillary depressions leading to macroscopic 52 53 deformations referred to as autogenous shrinkage. It has been found that autogenous shrinkage can represent more than half of the total deformation in ultra-high performance concrete [6], creating 54 considerable stresses at a microscale that can lead to cracking. As cracking should generally be 55 avoided, either because of structural concerns or aesthetic reasons[7,8], specific attention should 56 be paid to early-age deformation of low water-to-cement ratio high and ultra-high performance 57 58 concrete.

59 Several analytical models have been introduced during the last decades to predict shrinkage. 60 The major construction codes provide quick ways to estimate the shrinkage amplitude of several 61 concrete mixes based on their composition and, in some cases, by considering standard strength 62 characteristics such as the 28-days compressive strength. Power and exponential laws have been introduced to describe the shrinkage amplitude evolution relatively to time [9,10]. Thanks to these 63 64 laws, the quick increase in autogenous shrinkage amplitude during the first weeks can be grasped. Most of these models are a combination between empirical laws and advanced theories. For 65 example, B4 model [10] is supported by the solidification theory, the theory of microprestress 66 relaxation, activation energy concepts, the moisture diffusion theory, and damage models for 67 68 microcracking, and proved very good results in predicting autogenous and drying shrinkage of 69 structural elements [11]. Other models have been proposed in reference codes such as Eurocode 2, fib CEB MC 10 [9,12,13]. Recent improvements of both the B4 and the CEB MC 10 model have 70 been proposed to take into consideration the influence of some supplementary cementitious 71 72 materials [14,15]. These models have been found particularly effective in predicting long-term predictions deformation of concrete, but several shortcomings have been noticed concerning early-73 74 age prediction and regarding actual concrete formulations, which can include a high proportion of additions [15,16]. Moreover, the growing use of various supplementary cementitious materials 75 (SCM), leading to ternary or quaternary concrete mixes is which synergistic effects may arise, is 76 77 rarely taken into consideration.

Indeed, due to economic and environmental considerations, an increasing amount of SCM is 78 79 being used in recent concrete formulations. Various SCM such as calcined clay, fly ash, ground 80 granulated blast furnace slag, later referred to as slag, and silica fume commonly replace cement, 81 while additions like fillers may partially replace cement or only play a physical role in increasing the overall compacity of the mix. These additions influence shrinkage mechanisms to various 82 extents, especially autogenous shrinkage. It is commonly admitted that silica fume, commonly 83 84 used in UHPC due to its filling properties and high pozzolanic activity, increases shrinkage even for small replacement ratios [5]. Conversely, fly ash alone has been reported to decrease shrinkage 85 in most studies because of the slower hydration reaction [17,18]. In most published studies, slag 86 87 increased autogenous shrinkage, especially long-term autogenous shrinkage, because its fineness leads to high reactivity and higher chemical shrinkage than pure cement concrete [19-22]. Some 88 89 uncertainty remains concerning the influence of slag on the autogenous shrinkage of UHPC since it has been reported that the addition of slag increased the autogenous shrinkage in some cases 90 [15]. With the demand for low-cement concrete, calcined clay, which is readily available around 91 92 the globe, has been proved to be an interesting product to cut CO<sub>2</sub> emissions due to concrete formulation. Though calcined clay, generally associated with limestone to produce LC<sup>3</sup> cement, induces novel chemical reactions during hydration, and leads to a fine porosity [23], its influence on the autogenous shrinkage is rarely reported and might not be prejudicial [24–26]. Finally, fillers have been found to decrease shrinkage as they act like small aggregates restricting deformations [27,28], but their interactions with other additions are often only considered from a chemical point of view and are rarely addressed from a shrinkage point of view [27,29].

99 Therefore, with the increasing complexity of concrete formulations, a better understanding of 100 fundamental evolutions such as autogenous shrinkage is needed. Recent studies have proposed 101 adaptation to the aforementioned analytical models to consider the use of SCM and their eventual 102 combination [15,30]. In [15], CEB Model Code 2010 has been improved by introducing correction 103 factors using an extensive experimental campaign. However, such parameters might not represent 104 other concrete formulation behaviors, and more extensive shrinkage databases should be built.

Recent developments in Machine Learning (ML) have provided novel insights into concrete 105 106 properties-related issues [31]. Since the publication of the first Artificial Neural Network model (ANN) to predict concrete compressive strength [32], numerous research works have been 107 published to predict concrete compressive strength with ML-based models [33-36]. ML-based 108 109 models have also proved their interest in predicting other concrete properties such as fresh properties [37], creep [38,39], chloride [40], carbonation resistance [41], frost resistance [42] and 110 shrinkage [43,44]. They can also be used for microscale properties determination and 111 enhancement, such as during indentation [45,46], image analysis [47–50], or large-scale structural 112 113 monitoring [51,52]. While ML models might have initially appeared as black-box models, recent 114 advances such as features analysis and dubbed SHapley Additives exPlanations (SHAP) introduced novel ways to explore the impacts of the model inputs on the final predictions [53]. 115 116 Such tools have been used recently in several studies related to concrete [44,54] and might help build advanced autogenous shrinkage prediction models comparable to the existing most 117 118 performant analytical models such as B4 and CEB models.

This study develops an interpretable ensemble ML model to predict the autogenous shrinkage evolution in low-carbon cementitious materials with SCM. An extensive dedicated database is built, including ternary and quaternary formulations, and optimized ML models are compared to the classic and improved versions of B4 and CEB Model Code models using interpretative tools such as SHAP. Then, a web application is proposed to provide fast and precise shrinkage 124 predictions to the Civil Engineering community. The manuscript is structured as follows: a first 125 section describes the new shrinkage database developed during this study, then a section presents 126 the numerical methods employed before analyzing and discussing the results and a conclusion.

127

## 128

# 2 Autogenous Shrinkage Database description and analysis

129 To develop an accurate model for autogenous shrinkage prediction of concrete incorporating 130 SCM, a comprehensive experimental database is required. To this end, we adopted the method published in [44]. The original NU database containing various creep and shrinkage evolutions of 131 132 cementitious materials has been extended by low water-to-cement ratio cement paste, mortar or 133 concrete samples autogenous shrinkage curves. This database has been further extended to include more autogenous shrinkage data of various concrete of binary, ternary or quaternary formulations 134 135 from various sources [15,26,55-60]. In total, a database comprising 347 autogenous shrinkage observations and 28d compressive strength of various concrete mixes has been built. To the authors 136 137 knowledge, this is the most comprehensive autogenous shrinkage database to date. The final database covers a wide range of water-to-cement and water-to-binder ratios (from normal strength 138 to ultra-high strength concrete) as well as a wide variety of binary, ternary and quaternary 139 formulations. These shrinkage curves were interpolated to obtain 1d, 2d, 7d, 14d, and 28d 140 shrinkage values. Twelve input variables have been considered: water-cement ratio (W/C), water-141 binder ratio (W/B), aggregate-cement ratio (A/C), cement content (kg/m<sup>3</sup>), silica fume content (% 142 143 cement mass), fly ash content (% cement mass), slag content (% cement mass ), calcined clay content (% cement mass ) (denoted as metakaolin content), filler content (kg/m<sup>3</sup>), amount of 144 superplasticizer (% cement mass), time since the beginning of shrinkage measurements (days) and 145 28-d compressive strength (MPa). After removing data points with missing data, a database with 146 1482 datapoints ha been finally obtained. The descriptions and statistical attributes of the input 147 variables are given in Table 1, and Fig. 1 displays their statistical distributions. It can be seen that 148 a wide range of compositions has been investigated as water-to-binder ratios range from 0.16 to 149 0.86, cement content ranges from 167.4 kg/m<sup>3</sup> to 1632 kg/m<sup>3</sup> (cement paste) with a large 150 proportion of values between 167 kg/m<sup>3</sup> and 700 kg/m<sup>3</sup> for concretes. Supplementary cementitious 151 materials contents reflect the actual wide variety of formulations, some of them with important 152 153 substitution amounts. Indeed silica fume content, fly ash content, slag content, calcined clay and 154 filler content up to 50%, 150%, 400%, 57.4% and 125% relatively to cement mass were

155 considered. A maximum shrinkage value of around -2089  $\mu\epsilon$  has been obtained and a median 156 shrinkage value of -114.7  $\mu\epsilon$  can be calculated. Common autogenous shrinkage features can be 157 retrieved from the 2D scatter plots exposed in Fig. 1 by plotting linear regressions: shrinkage 158 increases with smaller W/B and A/C values, while it generally increases with higher cement or 159 silica fume content as well as higher compressive strength as they are generally associated to low 160 W/B values.

161 Correlations between the model parameters were calculated too. Fig. 2 gives a graphical 162 representation of the correlation matrix. As expected, strong positive correlations can be observed 163 between, W/B, A/C and shrinkage, and strong negative correlations can be observed between 164 shrinkage and fc28, cement content or silica fume content. However, no strong correlations 165 between input variables, and as such, all these variables were used as the input for ML.

166

10/ <b>Table 1.</b> Description of the database used in this stu	167	Table 1. Des	cription of t	the database	used in this stud
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	1			2					
	Unit	Min	Q25%	Mean	Median	Q75%	Max	Std	Skw
W/C	-	0.180	0.320	0.444	0.390	0.500	1.600	0.188	2.807
W/B	-	0.160	0.290	0.360	0.336	0.400	0.860	0.117	1.295
A/C	-	0.00	3.28	3.90	3.90	4.73	11.56	1.77	0.36
Cement content	kg/m <sup>3</sup>	167.4	360.0	472.1	440.0	496.0	1632.0	222.3	2.9
Silica fume content	% cem	0.0	0.0	3.0	0.0	0.0	50.0	7.2	3.7
Fly Ash	% cem	0.0	0.0	8.2	0.0	0.0	150.0	18.3	3.1
Slag content	% cem	0.0	0.0	9.8	0.0	0.0	400.0	40.6	6.7
Metakaolin content	% cem	0.0	0.0	1.6	0.0	0.0	57.4	8.2	5.7
Filler content	% cem	0.0	0.0	4.7	0.0	0.0	125.0	14.5	4.1
Superplasticizer									
content	% cem	0.0	0.0	1.5	0.8	1.8	11.8	2.2	2.3
Compressive strength									
fc28	MPa	16.5	45.9	67.1	63.0	85.7	162.0	29.4	0.8
Time of measurement	days	1.0	2.0	9.7	7.0	14.0	28.0	9.6	1.0
Shrinkage/Swelling	μm	-2089.600	-243.000	-182.832	-114.700	-28.650	78.900	237.617	-2.576
1 ( ) ~ ~ ~ ~ ~	~								

168 Skw=Skewness; Std=Standard deviation;



Fig. 1. Data distribution of each input variable and the output variable (shrinkage/swelling).



- Step 3: Interpretation of XGB black box with SHAP value
   In this step, the SHAPley Additive exPlanations (SHAP) [61] based on the best ML
   model is used for the interpretation of predicted Shrinkage/swelling values. The effect
   of each feature is quantified by SHAP global and SHAP local.
- Step 4: Comparison of predicted value based on the best ML model with B4 and CEB
   analytical models
- 197The concrete formulations in the original database have been divided into a training198and a test set to guarantee that no shrinkage value from any concrete with all time of199measurement in the test set is known. Then the best Machine Learning model is fitted200on this training set, and its performance is compared to the performance of the201analytical models on the test set.



202 203

Fig 3. Conception of shrinkage/swelling investigation

#### 205 **3.2 Machine learning models**

#### 206 **3.2.1** Support Vector Machine (SVM)

The support vector machine algorithm introduced by Vapnik [62] can be used to address 207 208 classification difficulties. For the solution of regression and prediction issues, the support vector 209 machine was further modified and dubbed support vector machine regression (SVR) [63]. The SVR method sought to reduce the generalization error and get the best solution using the structural risk 210 minimization concept. The Gaussian radial basis function was used in this work to transition from 211 a lower-dimensional feature space to a higher one, allowing for linear regression and improved 212 fitting of the training dataset. The following linear function can be used to represent the output 213 214 variable:

$$f(x) = \langle \omega \cdot \varphi(x) \rangle + b$$

where  $\langle \cdot \rangle$  denotes the dot function;  $\varphi(x)$  is a transformation that translates the input feature to a higher dimensional feature space; b is the function's parameter vector (model bias);  $\omega$  are the minimum values derived from the following equation:

$$\begin{array}{l} \text{minimise} \left[ \frac{1}{2} \|\omega\|^2 + C \sum_{j=i}^n (\xi_j + \xi_j^*) \right] \\ \\ \left\{ \begin{array}{l} y_j - \omega \cdot \varphi(x_j) - b \leq \varepsilon + \xi_j \\ \omega \cdot \varphi(x_i) + b - y_i \leq \varepsilon + \xi_i^* \end{array} \right. \end{array}$$
(2) 
$$\begin{array}{l} \end{array}$$

(1)

msidering 
$$\begin{cases} \omega \cdot \varphi(x_j) + b - y_j \le \varepsilon + \xi_j^* \\ \xi_j, \xi_j^* \ge 0 \end{cases}$$
(3)

where  $\xi_j$ ,  $\xi_j^*$  are the slack variables; C is the regularization parameter;  $\varepsilon$  is the insensitive loss function (error between the test and forecast values);  $y_j$  is the test result; and *n* is the sample size.

220

#### 221 **3.2.2** Artificial Neural Network (ANN)

The most widely used machine learning model is ANN, which is based on biological neural 222 223 networks. It is made up of input neurons (similar to synapses), multiplied by weights representing the intensities of the relevant impulses, and then determined by the neuron's activation function. 224 225 Finally, the required result will be computed by another function (perhaps an identity function). It is feasible to acquire the output matching to certain inputs by altering the weight of the artificial 226 227 neuron. However, when there are too many neurons, calculating these weights becomes problematic. 228 At this time, numerous ways are being developed to modify the weights of the neurons in order to 229 get the output as rapidly as feasible. In this study, the solver for weight optimization contains three methods including 'LBFGS' Limited-Memory Broyden-Fletcher-Goldfarb-Shanno method of 230 231 quasi-Newton methods, 'SGD' refers to stochastic gradient descent and the last 'ADAM' referring

to a Stochastic Gradient-Based Optimizer proposed by Kingma et al. [64]. In this investigation, the
best optimization solver will be selected by the metaheuristic algorithm in the process of tuning
hyperparameters.

235

#### 236 **3.2.3 Gradient Boosting (GB)**

Gradient Boosting (GB) improves predictions by using a method called as augmentation. The algorithm in boosting attempts to examine and correct predictions that are not acceptable on the first iteration [65]. The algorithm's iterative process for correction then continues until the desired prediction is obtained. Increased assistance for decreasing bias and variation in order to strengthen poor learners.

Gradient Boosting is the process of combining several weak predictive models into a single strong model [66]. In this case, a poor prediction model may perform somewhat better than random guesses.

245

The model using the Boosting ensemble learning strategy can be expressed as follows:

$$F_N(x) = \sum_{n=1}^M \alpha_n f_n(x) \tag{4}$$

The ensemble learning model  $F_N(x)$  is generated by the linear combination of N basic learning machine models, where  $f_n(x)$  represents the mth basic learning machine and n represents the weight of the nth basic learning machine.

The gradient boosting algorithm operates on the gradient descent approach, which is based on the functional. To begin, the goal function is as follows:

$$E = \sum_{t=1}^{T} L(y_t, F_N(x_t)) = \sum_{t=1}^{T} L(y_t, \alpha_n \times f_n(x_t))$$
(5)

The number of samples is T, the number of basic learning machines is N, and the loss function is L. The training procedure is to train each basic learning machine fn, n-1, 2,..., N in turn so that the objective function value E is the smallest, that is, the training outcomes for the nth basic learning machine are as follows.

$$\sum_{t=1}^{T} L\left(y_{t}, F_{n-1}\left(x_{t}\right) + \alpha_{n} \times f_{n}\left(x_{t}\right)\right) \cong \sum_{t=1}^{T} L\left(y_{t}, F_{n-1}\left(x_{t}\right) + \sum_{t=1}^{T} \frac{\partial L}{\partial F_{n-1}\left(x_{t}\right)} \times f_{n}\left(x_{t}\right)\right)$$
(6)

According to the principle of gradient descent, the optimal model should be the negative gradient direction of the objective function, that is:

$$f_n^*(x) = \arg\min_{f,\alpha} \sum_{t=1}^T L \left( -\frac{\partial L}{\partial F_{n-1}(x_t)} - \alpha \times f(x_t) \right)^2$$
(7)

After obtaining the best A, coefficient S can be found by minimizing the objectivefunction, namely:

$$\alpha_n^* = \arg\min_{\alpha_n} \sum_{t=1}^{I} L\left(y_t, F_{n-1}\left(x_t\right) + \alpha_n \times f_n^*\left(x_t\right)\right)$$
(8)

The preceding steps are repeated until all N basic learning machines and coefficients have been trained, and a learning model based on Equation 1 has been generated. The gradient boosting approach is used in the learning model, and the next fundamental machine learning model may further increase the accuracy based on the previous underlying machine learning models, reducing the model's deviation. This is the distinction with the Bagging. Basic machine learning can be a lowaccuracy model; through the improvement approach, the accuracy of the entire model can be steadily increased, but there is a certain degree of fit at the same time.

266

#### 267 **3.2.4 Extreme Gradient Boosting (XGB)**

The Extreme Gradient Boosting (XGB) algorithm is a cutting-edge method for solving 268 supervised learning problems with high precision [26]. If Deep Learning only accepts raw data in 269 numerical form (which must typically be converted to n-vectors in the real number space), XGB 270 accepts tabular datasets of any size, including categorical data. Furthermore, XGB has a rapid 271 272 training speed, can scale for parallel computing on several servers, and can be GPU-accelerated, 273 therefore Big Data is not an issue for this model. The earliest and most well-known model of the 274 most recent generation of tree booster ensembles is the XGB; a representation of this approach is the Gradient Boosting Decision Tree (GB) or Multiple Additive Regression Tree (MART). 275

The basic idea behind XGB is to first train a tree with the training set and the real value of the sample (i.e. the standard response), and then use that tree to forecast the training set to acquire the proper value. The residuals are the predicted value of each sample, as well as the difference between the forecast and the real value. The second tree is then trained, but this time instead of using the real number, use the residual as the standard response. After training two trees, the residuals of the sample can be used to train more trees. To stop training, the total number of trees can be selected explicitly or based on particular indicators.

283 The XGB algorithm can be thought of as a K-tree additive model:

$$\hat{\mathbf{y}}_i = \sum_{k=1}^{K} f_k(\mathbf{x}_i), f_k \in F$$
(9)

The gradient boost model does not learn the weights of the d-dimensional space but directly learns the decision tree set, where F is a function space consisting of all trees (here the regression tree is also a partial function and the varied values of the different portions form a tree). The objective function of XGB is a sum of a particular loss function assessing overall predictions and a sum of all predictors' regularization terms (K trees).

289 Mathematically:

$$obj(\theta) = \sum_{i}^{n} l(y_i - \hat{y}_i) + \sum_{k=1}^{K} \Omega(f_k)$$
(10)

290 Where *l* is the loss function, which is the difference between the expected and actual outputs  $\hat{y}_i$  and 291  $y_i$ . While is a measure of how complicated the model is, it aids in preventing model over-fitting and

292 is determined using:

$$\Omega(f_k) = \gamma T + \frac{1}{2} \lambda \|w\|^2$$
(11)

The number T in the preceding equation reflects the number of leaves on the tree, and w represents the weight of each leaf.

295

### 296 **3.2.5** Simulated Annealing Optimization algorithm (SA)

Kirkpatrick et al. [67] pioneered simulated annealing (SA) in 1983. This metaheuristic method is based on physical phenomena seen in continuum mechanics. To avoid becoming stuck in local minima, SA employs a random search engine represented by Markov chains. SA employs solution variants to increase the objective function while still maintaining the solutions, albeit the least efficient, within specified constraints. Any adjustment that improves the objective function, J, is permitted in the minimization problem; however, candidates that raise J are also included in the solution set with probability p, which is known as the transition probability [68]:

$$p = \exp\left[-\frac{\Delta E}{k_B T}\right] \tag{12}$$

304 where  $k_B$  is Boltzmann's constant, T is the annealing process temperature, and E is the energy level, 305 is connected with the goal function modification by the constant, [68].

$$\Delta E = \gamma \Delta J \tag{13}$$

A random threshold, r, such that p > r, determines whether a solution modification is acceptable. T lowers and the system cools down during optimization. A high T indicates a highenergy system that is difficult to reduce, whereas a low T indicates a low-energy system that may be trapped in a local minimum [69]. The proper decision T may be to first search the space for the global minimum and then, as the system cools down, converge to a solution with sufficient accuracy [68]. Stopping conditions, such as limiting the number of repeats or focusing on the improvement of the goal function, are incorporated in t<sub>f</sub> [70].

313

#### 314 **3.2.6** Performance evaluation of models

315 In order to evaluate the performance of ML models, three popular statistical metrics, such as 316 coefficient of determination R<sup>2</sup>, Root Mean Square Error (RMSE), and Mean Absolute Error 317 (MAE), are introduced in following:

$$R^{2} = \frac{\sum_{j=1}^{N} (p_{0,j} - \overline{p_{0}}) (p_{t,j} - \overline{p_{t}})}{\sqrt{\sum_{j=1}^{N} (p_{0,j} - \overline{p_{0}})^{2} \sum_{j=1}^{N} (p_{t,j} - \overline{p_{t}})^{2}}}$$
(16)
$$RMSE = \sqrt{\frac{1}{N} \sum_{j=1}^{N} (p_{0,j} - p_{t,j})^{2}}$$
(17)

$$MAE = \frac{1}{N} \sum_{j=1}^{N} \left| p_{0,j} \cdot p_{t,j} \right|$$
(18)

Where  $p_{0,i}$  is the shrinkage/expansion value of the i-th sample point in the database;  $p_{t,i}$  is 318 the machine learning model prediction value for the i-th sample point;  $\overline{p_0}$  is the averaged 319 experimental value of shrinkage/expansion; and  $\overline{p_t}$  is the mean predicted value. Both MAE and 320 321 RMSE explicitly quantify the residual error at each sample point and thus provide an accurate assessment of model performance. R2 normalizes the squared residual error with the database 322 323 variance and generates dimensionless values ranging from 0 to 1. Because RMSE is often seen to be more understandable because it is equivalent to measured values and handy for comparing the 324 325 performance of different models, it was chosen as the primary metric index.

#### 326 **3.2.7 K-Fold Cross Validation technique**

To tune hyperparameters in machine learning algorithms, K-fold cross-validation (CV) is 327 utilized. Choosing k affects the variance; a low k value results in significant variance or bias. 328 329 Furthermore, while deciding on k, the data quantity and computational capabilities of the system must be taken into account. The value of k in this study is set to 10 [71,72], indicating that the number 330 331 of training and testing rounds is ten . The dataset is split into two parts: training and testing. The training data area is partitioned into k sections of equal size. The model is then trained with different 332 hyperparameters on k-1 subsets and evaluated on the last subset. The process is repeated k times 333 before averaging the evaluation results as illustrated in Figure 4. 334



338

# 339 3.3 Comparison with Analytical Models

Three analytical models are also adopted for comparison to examine the prediction accuracy of the machine learning models detailed above. These models are the B4 model [10], CEB MC 10 [9] model and a modified version of CEM MC 10 model to include the effect of SCM which has been introduced recently [15] and will be referred to as 'CEBMC10SCM' model in this study. The autogenous shrinkage model prediction are given as follows:

- Modified B4 model [73]:
- 346 Using this composition-based model, the autogenous shrinkage can be calculated at any time:

$$\epsilon_{au}(t) = k_{\gamma}k_{s}Ct^{n} \tag{19}$$

348 where  $k_{\gamma}$  depends on the cement type,  $k_s = \left\{1 + 3\left(\frac{SiO_2}{Cement}\right)\right\} \left\{1 + 2\left(\frac{Slag}{Cement}\right)\right\}$  takes into 349 account the cement substitution by silica fume or slag, the prefactor *C* depends on the water-to-350 cement and aggregate-to-cement ratios :  $C = \frac{100}{(w/c)^{2.5} + \left(\frac{a/c}{10}\right)^{1.5}}$  and the exponent factor *n*, close to 0.2,

351 reads  $n = 1.2 - 0.1(a/c) + (-0.14 + 0.005(a/c)) \ln C$ .

• Modified B4 S model [73]:

The autogenous shrinkage value can be calculated using the 28d compressive strength without any information regarding the formulation and reads:

$$\epsilon_{au}(t) = 12f_c(1-g)^{1.7}t^{0.2}$$
(20)

where  $f_c$  is the 28d compressive strength and  $g = (volume \ of \ aggregates)/$ (volume of concrete) (default values of 0.7 and 0.0 can be used for concrete and cement pastes respectively).

• CEB MC 10 model:

$$\epsilon_{cas}(t) = \epsilon_{cas0}(f_{cm}) \cdot \beta_{as}(t) \tag{21}$$

where  $\beta_{as}(t) = 1 - \exp(-0.2\sqrt{t})$  the time function of autogenous shrinkage and  $\epsilon_{cas0}(f_{cm}) = -\alpha_{as} \left(\frac{0.1f_{cm}}{6+0.1f_{cm}}\right)^{2.5} \cdot 10^{-6}$  the notional autogenous shrinkage coefficient, where  $\alpha_{as}$ is a coefficient depending on cement type and  $f_{cm}$  is the 28-d compressive strength.

362

CEB MC 10 modified for SCM consideration [15]:

$$\epsilon_{cas}(t) = k_{SCM} \cdot \epsilon_{cas0}(f_{cm}) \cdot \beta_{as}(t)$$
(22)

where  $k_{SCM}$  is a correction factor to included the impact of SCM which, in the case of autogenous shrinkage, reads  $k_{SCM} = (1 + 0.24f + 0.4m - 0.35s) \cdot 4M$  where *f* is the replacement ratio of fly ash (%), *m* the replacement ratio of calcined clay (%), *s* the replacement ratio of slag and *M* the multi-SCM coefficient (binary M = 0.95, single M = 1.0).

## 368 4 Results and Discussion

#### 369 4.1 Models hyperparameters tuning

The ML model parameters have been tuned using the Simulated Annealing (SA) optimization 370 371 to obtain the most performant model considering R<sup>2</sup> metric. Surface plots of the R<sup>2</sup> values for several hyperparameter values of the XGB model are reported in Fig. 5. As illustrated in these 372 figures, extended zones of optimized parameter values could be found in most cases. For example, 373 374 as illustrated in Fig. 5 a), R<sup>2</sup> values higher than 0.91 could be obtained for learning rates lower than 0.5 and more than 500 iterations. A maximum depth of 4 led to the best results as illustrated in 375 Fig. 5 b) while various values of the minimum loss reduction required to make a partition on a leaf 376 377 node of the tree (min split loss) could generate good results, as illustrated in Fig. 5 c) and d). Based on this optimization analysis carried out by SA, the best hyperparameters values of the four ML 378 379 models were selected. These values are reported in Table 2.





**Fig 5.** Tuning XGBoost hyperparameters: surface plots of R<sup>2</sup>-values using 10-fold cross-validation.



**Table 2.** Tunned hyperparameters of the ML models.

XGB	Nb of	Learning	Max depth	Min split	777		R <sup>2</sup>
	trees	rate	10	loss			0.9311
	1197	0.6680		4			
GB	Nb of	Learning	Max depth	Max	Min	Min	R <sup>2</sup>
	trees	rate	10	features	samples	samples	0.9284
	887	0.2740		10	split	leaf	
					0.0560	0.0580	
SVM	С	γ	3	Kernel			R <sup>2</sup>
	1491	0.3610	0.0610	RBF			0.8089
ANN	Nb of	Activation	Solver	Max			R <sup>2</sup>
	neurons	RELU	LBFGS	iteration			0.8054
	(19,9)			4000			

# 384 4.2 Machine learning models typical predictions

The results obtained by the four models on the training and test sets are displayed in Fig. 6. As illustrated in the figure, all models performed well on the training sets with R<sup>2</sup> values higher than 0.94. Most training set predictions fall within the interval between 0.8 times and 1.2 times the measurement shrinkage value, except for very small shrinkage values. However, Gradient Boosting and XGBoost algorithms outperformed SVM and ANN models. The first two models provided high-quality predictions for various shrinkage values, while the latter two models were relatively prone to errors, even for small 391 shrinkage values. The detailed metrics corresponding to the model results are reported in Table 3. XGB 392 model performed better than the other models, and the  $R^2$  value associated with its prediction of the test 393 set was 0.9733, which corresponds to an RMSE of around 38.9 µe.

The mean absolute error (MAE) distribution has been analyzed for the four models, as illustrated in Fig. 7. It can be seen that the MAE remained limited for the XGB model as compared to the SVM and ANN models. Moreover, the maximum MAE measured for the XGB model, close to 200 µe was almost twice as small as the maximum MAE obtained by the SVM and the ANN model.



Fig. 6. Shrinkage/Swelling predicted by different ML models: a) XGB, b) GB, c) SVM and d) ANN models

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399

401 concrete incorporating SCM.

	Train			Test		
		RMSE			RMSE	
	$\mathbb{R}^2$	(με)	ΜΑΕ (με)	$\mathbb{R}^2$	(με)	ΜΑΕ (με)
XGB	0.999	6.341	3.993	0.973	38.909	25.249
GB	0.998	7.816	4.620	0.965	45.797	31.039
SVM	0.941	57.085	21.974	0.915	71.775	40.764
ANN	0.949	50.695	37.303	0.910	79.288	56.594

Table 3. Comparison of machine learning algorithms for autogenous shrinkage prediction of

402



Fig 7. Distribution of the absolute error: a) XGB, b) GB, c) SVM, and d) ANN models.

#### 404 **4.3** Feature importance and sensitivity analysis

#### 405 4.3.1 Global interpretation

The most influential features on the shrinkage predictions have been obtained from the model 406 407 using SHAP. The global SHAP values are reported in Fig. 8, the features classified in descending 408 order based on their influence from top to bottom. The results align with the previous study published by the authors dedicated to autogenous shrinkage prediction of cementitious materials 409 incorporating SAP and SCM even if the database has been largely extended and the model results 410 411 improved [44]. Indeed, the most influential parameters are the A/C ratio, time, W/B ratio, cement 412 content, the 28d compressive strength, silica fume content, superplasticizer content, W/C ratio, fly ash, slag, filler, and last calcined clay content. The relative influence of the most influential 413 parameters can still be easily determined: 414

- 415
- increasing A/C ratio increases SHAP value, e.g., decrease shrinkage
- increasing time values correspond to higher shrinkage values
- increasing W/B and W/C ratios tend to decrease shrinkage
- 418 419
- high silica fume replacement ratio or cement content predominantly induces higher shrinkage

However, the global influence of the other parameters, mainly SCM other than silica fume, 420 might not be that clear at first sight. Most fly ash highest values are associated with positive SHAP 421 422 values, which means that a high fly ash content globally decreases shrinkage. Similarly, the highest 423 filler contents are associated with positive SHAP values, i.e., decreased shrinkage. Since the 424 highest calcined clay contents are associated with the most negative SHAP values, its adverse effect on autogenous shrinkage can be confirmed for high replacement ratios. Last, slag and 28d 425 compressive strength effects cannot be analyzed easily from this global perspective. To this end, 426 427 more detailed insights are needed using the features dependance plots.

SHAP can also give information about the feature dependency of the results, as illustrated in Fig. 9. Indeed, feature dependence plots reveal how the SHAP values change depending on the values of the features. As illustrated in Fig. 9 a), the SHAP values largely increase when the A/C values increase, especially when A/C values increase from around 1.0 to 4.0, corresponding to the transition from mortar to concrete. This increase of around 800 με highlights the relative influence 433 of the A/C ratio on the autogenous shrinkage phenomenon. For A/C values higher than 4.0, SHAP 434 value is almost constant, meaning there is no interest in further increasing the A/C ratio to reduce 435 the autogenous shrinkage. The water-to-binder ratio's influence can be analyzed using Fig. 9 b). From this figure, it can be seen that the SHAP value increases from the minimum w/b considered 436 437 in this study, e.g. 0.16, to approximately 0.5. This gradual increase from around -300 µE to around 50 µε confirms that autogenous shrinkage arises in cementitious materials of W/B ratio smaller 438 439 than 0.5. However, it is worth noting that the W/B relative influence is around twice as small as the A/C influence. 440



441

442 **Fig. 8.** Global SHAP values of the tuned XGB model

Based on Fig. 9 c), it can be seen that the increasing strength values up to around 100MPa 443 444 negatively influence SHAP values, which means that transitioning from normal strength to high strength concrete leads to more autogenous shrinkage, independently from the other parameters 445 such as the W/B ratio. Conversely, SHAP values increase for strength higher than around 100MPa 446 up to final values around 140 µɛ, which means that autogenous shrinkage for this type of high 447 performance and ultra-high performance concrete would have been more pronounced if their 448 449 strength had been smaller. This novel insight might correlate to the quick strength and Young's 450 modulus increase of these concretes, limiting early age autogenous shrinkage.

451 The influence of silica fume can be analyzed using Fig. 9 d). Based on this figure, it can be observed that increasing silica fume values, from 0% to 50% cement replacement, largely 452 decreases SHAP values. However, a spread should be noticed when the silica fume replacement 453 454 ratio is larger than 20%, and it should be noticed that a 50% replacement ratio can influence SHAP values less than a 20% replacement ratio in the case of some concretes. Therefore, although silica 455 456 fume is known to increase considerably autogenous shrinkage, novel routes might be found to limit its influence. The other supplementary cementitious materials have a smaller influence on SHAP 457 values. As illustrated in Fig. 9 e), fly ash influence on SHAP values becomes visible on this feature 458 dependence plot for replacement ratios higher than 50%. In this case, cement substitution by fly 459 ash leads to smaller autogenous shrinkage values explained by the slower hydration. Based on Fig. 460 9 f), it can be observed that slag influence on SHAP values is relatively limited as most of the 461 values belong to the  $[-100 \ \mu\epsilon, 50 \ \mu\epsilon]$  interval. However, it is worth noting that, according to this 462 detailed analysis, slag negatively influences shrinkage for all the substitution ratios smaller than 463 464 around 50%, which agrees with the literature [19,74]. On the opposite, different behaviors can be observed for replacement ratios higher than 50%: slag can positively affect shrinkage sometimes, 465 while it still negatively influences shrinkage for other concrete mixes. It can be hypothesized that 466 two competing interests are at stake: the refined pore structures that increase shrinkage and the 467 slower hydration that decrease shrinkage at a given time. As illustrated in Fig. 9 g), filler globally 468 469 slightly increases shrinkage for substitution rates smaller than 25%, which can be explained by the increased hydration speed. However, substitution ratios higher than 25% systematically positively 470 influence SHAP values, highlighting the restraining effect of filler on the autogenous shrinkage. 471

Finally, though the effect of calcined clay is relatively small according to the model, it can be observed that calcined clay does not influence SHAP values a lot for replacement ratios smaller than 20%, while increasing the substitution rate, the SHAP values decrease. This observation agrees with the literature [24,58]. To conclude, since SHAP gives the influence rules of the different features on the autogenous shrinkage predictions of the model, it can be used to provide novel insights into the shrinkage phenomenon.



479 Fig. 9. Feature dependence plots associated with SHAP for the influential features: a) A/C, b) W/B, c) fc28, d) silica fume, e) fly ash, f) slag, g) filler, and h) calcined clay. 480

#### 481 **4.3.2 Local interpretation**

Besides global interpretations, SHAP also provides useful information to explain the model predictions on individual samples as SHAP decomposes the final prediction into a sum of contributions by all the input variables. Various 28d autogenous shrinkage predictions were thus analyzed for several unknown concrete samples containing various types of SCM. Fig. 10 illustrates explanations for four typical samples.

As shown in Fig. 10 a), the base prediction on the entire set is -229  $\mu\epsilon$ . For this sample, the most significant reason for the final autogenous shrinkage prediction of -76  $\mu\epsilon$  is the A/C ratio, whose individual contribution amounts to +152  $\mu\epsilon$ , meaning this value decreases shrinkage compared to lower A/C ratios. Then time negatively influences the autogenous shrinkage prediction, which can be explained by the fact that 28 days is the final prediction associated with larger shrinkage deformations. The water to binder ratio is the third most influential parameter, as expected based on the global interpretation.

For concrete incorporating silica fume, its relative influence on the outputs can be quantified
as illustrated in Fig. 10 b). The presence of silica fume can considerably influence the model
prediction. Indeed, as illustrated in the figure, silica fume content becomes the most influential
parameter, and, at 28 days, the SHAP value associated to silica fume is around -160 με.

In most analyses, small replacement ratios of other SCM were found only slightly to affect shrinkage values as the A/C and the W/B ratios predominantly influenced the latter, as illustrated in Fig. 10 c) represents the inputs contributions on the autogenous shrinkage prediction of a concrete sample incorporating fly ash with the mass of fly ash equal to 11.1% of the one of cement. However, when larger proportions of cement are replaced, the influence of the SCM can become predominant. Indeed, as illustrated in Fig. 10 d), when half of the cement is replaced by slag, this slag proportion increases shrinkage by around 52 µ $\epsilon$  according to the model.



a)



506

Fig. 10. Local interpretation using SHAP of some of the XGB model autogenous shrinkage predictions: a) normal strength concrete without SCM, b) high strength concrete with silica fume, 507 c) normal strength concrete with fly ash, d) high-strength concrete with 50% of cement replaced 508 509 by slag.

#### Comparison with B4 and CEB analytical models 511 4.4

The developed XGBoost model, the modified B4 and B4s, the CEB MC10, and the CEB MC 512

513 10 model's modified version can be compared globally using their respective predictions on the 514 test set composed of unknown concrete formulations. The performance of these four models has been compared with the observed shrinkage values, as illustrated in Fig. 11. It can be observed 515 516 that, overall, the distribution of the shrinkage values predicted by the developed XGB model is in 517 close agreement with the observed distribution, and the box plots are very similar. Indeed, interquantiles ranges and outliers present similar patterns. The XGB model slightly overestimates 518 519 the overall shrinkage values, which is good regarding safety issues. Last but not least, the XGB 520 model can predict small swelling values that might occur at an early age, while analytical models 521 cannot be captured correctly this trend.

The analytical models' performance considerably varies. Based on the overall distribution of 522 the shrinkage values, the modified B4 model provides a distribution of the predictions that is in 523 good agreement with the observed distribution. However, one can observe that the mean shrinkage 524 525 value predicted by the modified B4 model slightly underestimates the observed shrinkage 526 distribution, which might represent a risk regarding safety. The same conclusion applies to the modified version of the B4 S model. Moreover, the predictions made by this model cannot capture 527 the experimental variability, probably due to its simplicity. CEB MC 10 model results clearly 528 underestimate shrinkage, and the size of the overall distribution is considerably smaller than the 529 530 observed distribution, highlighting the shortcomings of this analytical model. The modified version of the CEB MC 10 model performed better, and the overall distribution of the shrinkage 531 532 values looks like the observed distribution as the interquartile range is close to the experimental 533 one. However, an apparent overestimation of the shrinkage values and a disability to predict large shrinkage values can be noticed. 534





Fig. 11. Box plots of the shrinkage/swelling values predicted by the XGB model compared tothe analytical models and the observed values

539 The model results and the test data can be further compared using the Taylor diagram (Fig. 540 12), which summarizes three valuable characteristics of the models compared to the measured 541 values: the standard deviation associated with the model's predictions, the correlation between the predictions and the experimental values, and the centered root-mean-square (RMS) difference. As 542 mentioned in the previous paragraph, the standard deviation of the simulated patterns reported on 543 544 the X-axis largely differs between the models. The standard deviation of the experimental data is 545 almost reproduced by the XGB and the modified version of the B4 model. Indeed, the standard 546 deviations associated with these models are higher than 200 µɛ, close to the 250 µɛ experimental value. Then, the modified B4 S and modified version of the CEB MC 10 model exhibit a standard 547 deviation of around 150 µɛ, which is in relatively good agreement with the observed values. Last, 548 549 the standard deviation of the classic CEB Model 10 is smaller than 40  $\mu\epsilon$ , clearly underestimating the experimental variation and highlighting the model's shortcomings in predicting shrinkage of 550 concrete incorporating SCM. Concerning the correlation of the models with the experimental 551 values, the best correlation is obtained by the XGB model (0.82). This correlation is largely higher 552 than the second-best correlation obtained by the modified B4 model (0.58). The correlation of the 553 554 modified B4 S model follows. The CEB MC 10 and the modified version of the CEB MC 10 model exhibit correlations close to 0.3-0.4, which is relatively small. Finally, the RMS value of the XGB 555

model (around 160  $\mu\epsilon$ ) is clearly better than the ones of the other models, which are higher than 200  $\mu\epsilon$ . For all these reasons, it can be concluded that the optimized XGB model significantly outperforms the best analytical models that have been proposed up to date.



559

Fig. 12. Taylor diagram representing XGB, B4 and B4s modified, CEB MC 10 and CEB MC
10 modified version models performance.

562 563

Based on the XGB model, the autogenous shrinkage predictions of the eight concrete compositions containing various types of SCM have been compared to the analytical models' predictions, as shown in Fig. 13. The detailed formulations are given in Table 4. As illustrated in these figures, the prediction accuracy of the XGB model globally outperforms that of the analytical models in most cases which agrees with Taylor's analysis.

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- 570
- 571
- 572
- 573

Ref	C1	C2	C3	C4	C5	C6	C7	C8
W/C	0.42	0.38	0.34	0.64	0.29	0.43	0.31	0.44
W/B	0.42	0.304	0.306	0.32	0.28	0.3	0.21	0.3
A/C	4.39	3.95	3.74	6.22	4.21	3.68	3.94	3.74
Cement (kg/m <sup>3</sup> )	400	377	450	263	428	408	497	416
Silica fume (%)	-	25	-	-	-	14.2	10	-
Fly Ash (%)	-	-	11.1	-	-	28.7	-	-
Slag (%)	-	-	-	100	-	-	-	-
Metakaolin (%)	-	-	-	-	5.3	-	-	10.5
Filler (%)	-	-	-	-	-	-	34	36.2
Sp (%)	1.8	-	-	1.8	3.1	2.1	2.07	1.46
fc28 (MPa)	46.1	89.2	53.4	66.7	91.5	69.7	93	84
Time (days)	1-28	1-28	1-28	1-28	1-28	1-28	1-28	1-28

574 **Table 4.** Mortar and concrete compositions of some typical test samples

576 In the case of a normal strength concrete with a water-to-binder ratio of 0.42 and without any 577 SCM, the model's prediction agrees with the experimental values, and only a 20  $\mu\epsilon$  difference is 578 obtained after 28 days, as illustrated in Fig. 13 a). However, the B4 model better predicted the 579 long-term 28-d shrinkage value. The CEB MC 10 model's modified version largely overestimated 580 the autogenous shrinkage values. On the opposite, as observed in the global statistics, the CEB 581 MC 10 model underestimates the autogenous shrinkage at 28 days.

582 The effect of the cement substitution by silica fume is illustrated in Fig. 13 b). Both the XGB 583 model and the modified version of the CEB MC 10 model can provide good predictions, while the 584 modified versions of the B4 model largely underestimate autogenous shrinkage by around 300  $\mu\epsilon$ 585 and the CEB MC 10 model underestimates the shrinkage value by approximately 400  $\mu\epsilon$ .

586 As illustrated in Fig. 13 c), the XGB model prediction of the shrinkage values of concrete with a relatively low W/B around 0.3 incorporating fly ash closely matches the experimental values, 587 even at an early age. The analytical models' predictions are relatively far from the experimental 588 values at an early age, which might be attributed to these models' absent or relatively recent 589 590 considerations of fly ash effects. It should be noticed that the 28d shrinkage values predicted by the modified versions of the B4 and CEB MC10 model are in relatively good agreement with the 591 experimental values, but their prediction might deviate from the measured values for more 592 extended periods. 593

594

Fig. 13 d) displays the autogenous shrinkage predictions of the models in the case of high-

595 strength concrete, with a water-to-binder ratio of 0.32, in which 50% of cement has been replaced 596 by slag. In this case, exemplifying modern concretes with high substitution rates, the XGB model also performed well, though slightly underestimating the 28d autogenous shrinkage value. The 597 598 modified B4 model provides the best prediction, but the modified version of the B4 S model underestimated the shrinkage values as well. The CEB MC 10 models underestimated the 599 shrinkage values, while the modified version of the CEB MC 10 whose prediction can be qualified 600 as correct, still overestimated the shrinkage value by around 75 µɛ. It would be interesting to 601 combine analytical and machine learning models in such a case. 602

Though more experimental data is needed regarding the influence of calcined clay on drying and autogenous shrinkage, the developed XGB model showed better results than the analytical models in predicting the autogenous shrinkage evolution of concrete mixes incorporating calcined clay, as illustrated in Fig. 13 e). The analytical models which do not consider the effect of calcined clay - modified B4, modified B4 S and CEB MC 10 models - largely underestimated the shrinkage values, while the modified version of the CEB MC 10 models overestimated its influence.

The prediction quality of the models can also be calculated in the case of ternary cement 609 610 blends. As illustrated in Fig. 13 f), the XGB model captured the combined effect of silica fume and fly ash satisfactorily, as the 28d autogenous shrinkage prediction differs by around 60 µε from 611 612 the experimental value, but overestimates early age shrinkage. In this case, the modified version 613 of the B4 model outputs good yet slightly underestimated results. However, the prediction of the 614 autogenous shrinkage of some ternary formulations might be improved in the future. As illustrated in concrete in Fig. 13 g), the XGB and analytical models predictions are pretty far from the 615 616 measured values for concrete in which cement is partially substituted by silica fume and filler. In 617 this particular case, the modified version of the CEB MC 10 model provided the best estimation of the final 28-day shrinkage value. 618

The XGB model's predictions are better in the case of LC<sup>3</sup> concrete incorporating calcined clay and filler, as illustrated in Fig. 13 h) since several formulations of this type are present in the database. In that case, the model predictions are good, especially after 10 days, while the early shrinkage values are overestimated. Other models cannot capture the experimental shrinkage evolution.





Fig. 13. Comparison of the autogenous shrinkage predictions of the XGB model and the analytical models for several unknown concrete formulations detailed in Table 4: a) normal strength concrete without SCM, b) high strength concrete with silica fume, c) normal strength concrete with fly ash, d) high-strength concrete with 50% of cement replaced by slag, e) highstrength concrete incorporating calcined clay, f) high-strength concrete with cement replaced by silica fume and fly ash, g) high-strength concrete with silica fume and filler, h) normal strength concrete incorporating calcined clay and filler (LC<sup>3</sup> concrete).

#### 633 4.5 Web application

A web application has been built using the first model trained on the whole database to provide
 autogenous shrinkage predictions of various concrete formulations. The user can input the concrete

formulation using several sliders whose minimum and maximum values corresponds to the ones from the database, and then predictions of the shrinkage values at 1 day, 2 days, 7 days, 14 days and 28 days are computed online based on the model developed in this study. Default values corresponding to a high-strength concrete formulation incorporating silica fume are considered from a study not included in the database [75]. A graph is plotted to visualize the predictions as illustrated in Fig.14. The web application is available at <u>https://share.streamlit.io/bhilloul/concreteauto-shrinkage-ai-streamlit/main</u>.



643

644

Fig. 14. Web application for autogenous shrinkage prediction of concrete incorporating SCM.

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# 5 **Conclusions**

647 This study examined the usage and potential of several Machine Learning (ML) algorithms to 648 precisely predict the autogenous shrinkage of low-carbon cementitious materials with various 649 types of supplementary cementitious materials (SCM) and compared the results with analytical 650 models, e.g., the modified version of the B4 and B4 S models, the CEB MC 10, and the CEB MC 651 10 modified version. To this end, an extensive database of autogenous shrinkage measurements 652 has been built based on a previous study. First, Gradient Boosting (GB), XG Boost (XGB), Support Vector Machine (SVM), and an Artificial Neural Network (ANN) model have been optimized 653 654 using grid search hyperparameter optimization, and their performance has been assessed using kfold cross-validation. The best model has been further analyzed using the Shapley Additives 655 Explanations (SHAP) to facilitate interpretations and provide novel insights into the autogenous 656 shrinkage mechanism. Finally, the developed model has been compared to the aforementioned 657 analytical models, some recently adapted to consider the effect of SCM. Based on the results, the 658 659 following main conclusions can be drawn:

- An extensive database composed of 1482 autogenous shrinkage curves of various
   binary, ternary and quaternary cement paste, mortar, and concrete incorporating silica
   fume, fly ash, slag, calcined clay, and filler, containing also concrete 28-day
   compressive strength, has been built using data from the literature.
- ML models can accurately predict the autogenous shrinkage, and their
   hyperparameters can be optimized through grid search. Indeed, R<sup>2</sup> values of around
   0.805 to 0.931 have been obtained on the test set. The best model identified in this
   study is XGB.
- The relative influence of the model inputs on the predictions can be analyzed using
  SHAP values. Global SHAP values agreed with the experimental observations, and
  the A/C ratio, time, W/B ratio, and silica fume content are particularly impacting.
  Local SHAP analysis helped identify some evolutions of the shrinkage behavior with
  increasing amounts of SCM, for example, the competition between the shrinkage
  increase due to the pore refinement and the shrinkage delay due to slower hydration.
- The model predictions of completely unknown shrinkage behavior of concretes
  incorporating SCM are significantly better than the predictions of analytical models
  such as the modified B4 models, the CEB MC 10, and the modified version CEB MC
  even though some analytical models can perform better predictions for specific
  formulations. Detailed comparisons of the models' shrinkage predictions of various
  concrete compositions have been studied thoroughly.
- 680
- A web application has been developed to provide fast and precise predictions to the

- 681 scientific and industrial community and drive further low-carbon cementitious 682 materials developments.
- 683 The study might open up novel research and industrial perspectives on shrinkage prediction
- 684 of eco-friendly cementitious materials using advanced Machine Learning techniques.
- 685 **CRediT authorship contribution statement**
- 686 Benoit Hilloulin: Conceptualization, Methodology, Investigation, Software, Formal analysis, Writing -
- 687 original draft, Writing review & editing, Validation.
- 688 Van Quan Tran: Conceptualization, Methodology, Software, Visualization. Writing -original draft,
- 689 Writing review & editing.
- 690
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