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Twist-angle dependent dehybridization of momentum-indirect excitons in MoSe₂/MoS₂ heterostructures

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Supplementary material for this article is available [online](#)

Abstract

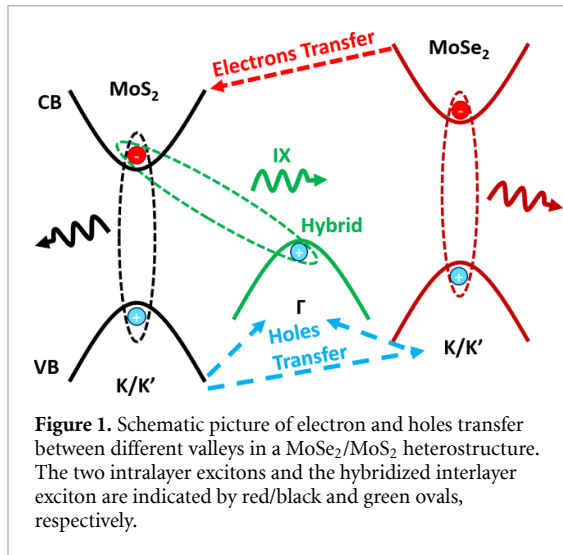
The moiré superlattice has emerged as a powerful way to tune excitonic properties in two-dimensional van der Waals structures. However, the current understanding of the influence of the twist angle for interlayer excitons (IXs) in heterostructures is mainly limited to momentum-direct K - K transitions. In this work, we use a judicious combination of spectroscopy and many-particle theory to investigate the influence of the twist angle on momentum-indirect IXs of a MoSe₂/MoS₂ heterostructure. Here, the energetically lowest state is a dark and strongly hybridized Γ K exciton. We show that increasing the twist angle from an aligned structure (0° or 60°) gives rise to a large blue shift of the IX, which is a manifestation of the strong dehybridization of this state. Moreover, for small twist angle heterostructures, our photoluminescence measurements reveal contributions from two IX states, which our modelling attributes to transitions from different moiré minibands. Our finding contributes to a better fundamental understanding of the influence of the moiré pattern on the hybridization of momentum-dark IX states, which may be important for applications in moiré-tronics including novel quantum technologies.

1. Introduction

Two-dimensional (2D) van der Waals crystals, with their inherent weak interlayer bonding, have enabled a new paradigm of heterostructure engineering [1, 2]. For 2D materials, lattice-matching constraints are no longer obstacles (in contrast to the case of epitaxial heterostructures), while the twist angle between the layers provides a convenient handle to tune their electronic properties, facilitating access to exotic physics phenomena [3–13]. A prominent example is provided by the transition metal dichalcogenides (TMDs) homo- and heterostructures. These represent a unique system in which spin, valley, excitonic,

and many-body physics are heavily intertwined and investigated [3, 9–21]. Initially, these heterostructures were described as simple type II quantum wells with electrons and holes located in the adjacent TMD layers. This band alignment leads to the formation of the interlayer exciton (IX) [14, 19, 22–26]. However, more detailed investigations of this excitonic complex have quickly shown that the simple type II quantum well picture is not sufficient to capture all of the intriguing physics of TMD heterostructures.

Currently, it is generally accepted that the optoelectronic properties of TMD stacks are determined by the interplay of two effects: (i) the formation of a moiré pattern [7, 8, 16–18, 20, 27–30], and



(ii) the interlayer hybridization of the states [31–36]. A moiré pattern is created due to the mismatch of the TMD lattice constants and/or to the twist between two adjacent layers. It results in a slowly varying periodic potential, which can be treated as an in-plane superlattice of quantum dots [16, 20, 28], which affects locally the optical selection rules [17, 18, 37]. On the other hand, the hybridization arises from the overlap of the atomic wave functions of the two adjacent layers. Therefore, it mostly affects states derived from the chalcogen atomic orbitals, such as the states around the Γ point in the Brillouin zone. This interlayer coupling is well recognized for the TMD homobilayers (and thicker forms) as it is responsible for their indirect band gap character [38–40]. Band structure modelling shows that a similar situation occurs in MoSe₂/MoS₂ [41] and MoS₂/WS₂ [34] heterostructures, where the hybridization locates the valence band maximum at the Γ point, while the minimum of the conduction band remains at the K point (spatially, electrons are located in MoS₂), as schematically shown in figure 1. Therefore, the lowest energy excited state is a hybrid exciton, indirect both in real and k -space [34]. This feature distinguishes these heterostructures from the most often investigated MoSe₂/WSe₂ heterostructures, which are well described as type II quantum wells, with the valence and conduction bands extrema located in adjacent layers but still at the same K points of the Brillouin zone [34, 42]. Thus, in terms of the band structure, we can expect that MoSe₂/MoS₂ and MoS₂/WS₂ heterostructures should be more related to TMD homobilayers [33, 43–46], rather than to the direct bandgap MoSe₂/WSe₂ stack, which leads to very different optical properties.

As the twist between the layers modifies their spatial separation [47], it is natural to expect that the energy of the hybridized states strongly depends on the twist angle. Simultaneously, states close to K points should be only weakly affected by

interlayer hopping (coupling), since the corresponding orbital functions are mostly localized on the transition metal atoms situated in the central layer of the chalcogenide-metal-chalcogenide sandwich. These expectations are supported by band structure calculations [33, 34] and corroborated by experimental studies of homobilayers and MoSe₂/WSe₂ heterostructure [28, 42–46]. The characteristic feature for the hybridized states (K - Γ or K - Λ) is a strong blue shift of the IX energy with increasing twist angle (when moving away from high symmetry alignment – 0° or 60°) [43–46], which is absent (very weak) for direct K - K transitions [28, 42]. While so far the effect of hybridization has been investigated mainly in homobilayers [33, 43–46, 48], here we report on the distinct fingerprint of the hybridized nature of the ground excitonic transition in MoSe₂/MoS₂ heterostructures, which distinguishes it from the much more intensively investigated MoSe₂/WSe₂ stack. We show that the photoluminescence (PL) spectrum of the MoSe₂/MoS₂ heterostructure reveals a strong blue shift of the ground excitonic transition, with increasing twist angle. This can be understood as a process of layer decoupling and dehybridization of the bands, which is fully confirmed by our theoretical modelling. We conclude that the band structure and optical spectrum of the investigated stacks resemble those observed for twisted homobilayers. Finally, we demonstrate that the optical spectrum of the hybridized exciton is affected by the moiré pattern. For highly aligned samples, we observe a double peak structure of the hybridized IX. Our measured excitation power and temperature dependence, together with band structure calculations, suggests that the double peak originates from the state filling of the moiré bands.

2. Results and discussion

Atomically thin flakes were obtained by mechanical exfoliation and stacked using a deterministic transfer method [49]. We fabricated six MoS₂/MoSe₂ heterostructures with different interlayer twist angle, encapsulated with hexagonal boron nitride (hBN) on a SiO₂ substrate (for fabrication details see section 4.1). Figure 2(a) shows an optical microscope image of one of the heterostructures (Sample A, characterized by a twist angle of 57.2°). Details of Samples B–F are in SI. 1–3). The contour of the MoSe₂ and MoS₂ monolayers are indicated by black and red curves, and the overlap region of the TMD layers is indicated by a green dashed line with chequered pattern. We determine the interlayer twist angle between monolayers by comparing the second harmonic generation (SHG) intensity as well as polarization-resolved SHG of the monolayers and the heterostructure, which are presented in figure S1 [27, 50].

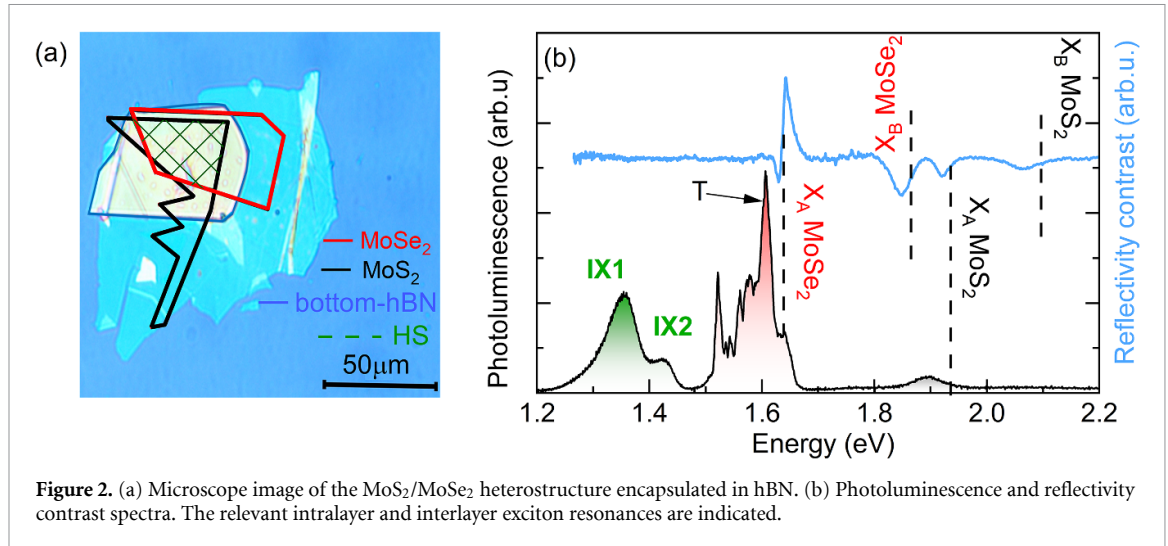


Figure 2. (a) Microscope image of the MoSe₂/MoS₂ heterostructure encapsulated in hBN. (b) Photoluminescence and reflectivity contrast spectra. The relevant intralayer and interlayer exciton resonances are indicated.

Figure 2(b) shows representative optical spectra from the heterostructure area of sample A. In the reflectivity contrast spectrum (RC), both A and B excitons of MoS₂ and MoSe₂ are visible. Similarly, in the PL spectrum, we observe emission related to both monolayers. The peak at ~ 1.9 eV corresponds to MoS₂ and probably stems from a mixture of trion and shallow defect-induced state emission as it is red-shifted by ~ 35 meV from the A exciton resonance that is visible in the RC spectra [38, 51, 52]. In the PL spectrum of MoSe₂ located between 1.5 and 1.66 eV, we observe a peak corresponding to the free X_A exciton at 1.64 eV and a dominating trion peak ~ 30 meV below [51, 53], followed probably by some defect state emission.

At lower energies, we observe a pronounced peak at around 1.3–1.4 eV, which is only visible in the heterostructure region. We attribute this emission to the hybridized IX [25, 34, 41], with the electron located at the *K* point of the MoS₂ layer, and the hole located at the hybridized valence band at the Γ point of the Brillouin zone [41], as schematically depicted in figure 1. The indirect character of the IX transition, together with the spatial separation of electrons and holes, makes the oscillator strength of the IX transition too weak to be observed in the RC spectra. However, this momentum-dark state can be observed in the PL spectrum due to its high occupation as the energetically lowest state. Its emission is indirect and is driven by phonons, resulting in phonon sidebands [34]. Intriguingly, the IX PL spectrum exhibit a double-peak structure, which is further discussed below. First, we discuss the hybridized nature of the IX exciton in the investigated heterostructure focusing on the dominant low-energy IX PL peak.

Figure 3(a) illustrates the evolution of the PL spectrum for different twist angles. The energy of the PL maximum blue shifts when the twist angle

deviates from the 0° or 60° stacking, which corresponds to R-type and H-type stacking, respectively. Fitting the PL peaks with a double Gaussian (dashed lines), we can extract the energy of the ground (dominating) IX1 transition as a function of the twist angle. The shift of the IX1 transition is summarized as open circles in figure 3(b). The blue shift can be as high as 100 meV moving from $\sim 0^\circ$ to 6–7°. This strong dependence of the IX emission energy on the twist angle is in stark contrast with the behavior observed in MoSe₂/WSe₂ heterostructures [28, 42, 47], where the IX recombination stems from a momentum direct *K*–*K* transition. This can be explained by the different character of the IX in the MoSe₂/MoS₂ heterostructure. The strong blue shift of the IX transition in the MoSe₂/MoS₂ heterostructure resembles closely the behavior of IX excitons in twisted homobilayers [33, 43–46], which points to its hybridized nature related to the states close to the Γ point.

To obtain a deeper insight into the mechanism driving the evolution of the IX states with the twist angle, we employ the exciton density-matrix formalism, using input from density functional theory (DFT) calculations [8, 33, 34] (see also SI. 6). The Hamiltonian operator of excitons in twisted rigid lattices consists of three different contributions,

$$H \propto E + V(\Theta, r) + T(\Theta, r). \quad (1)$$

Here, E is the exciton dispersion for the decoupled monolayers, $V(\Theta, r)$ is the spatially periodic electrostatic potential and $T(\Theta, r)$ is the hybridization Hamiltonian taking into account the overlapping electronic wave functions giving rise to hybrid exciton states [34]. Similarly to $V(\Theta, r)$, $T(\Theta, r)$ is also spatially periodic as the interlayer distance varies within the moiré supercell. Therefore, both components

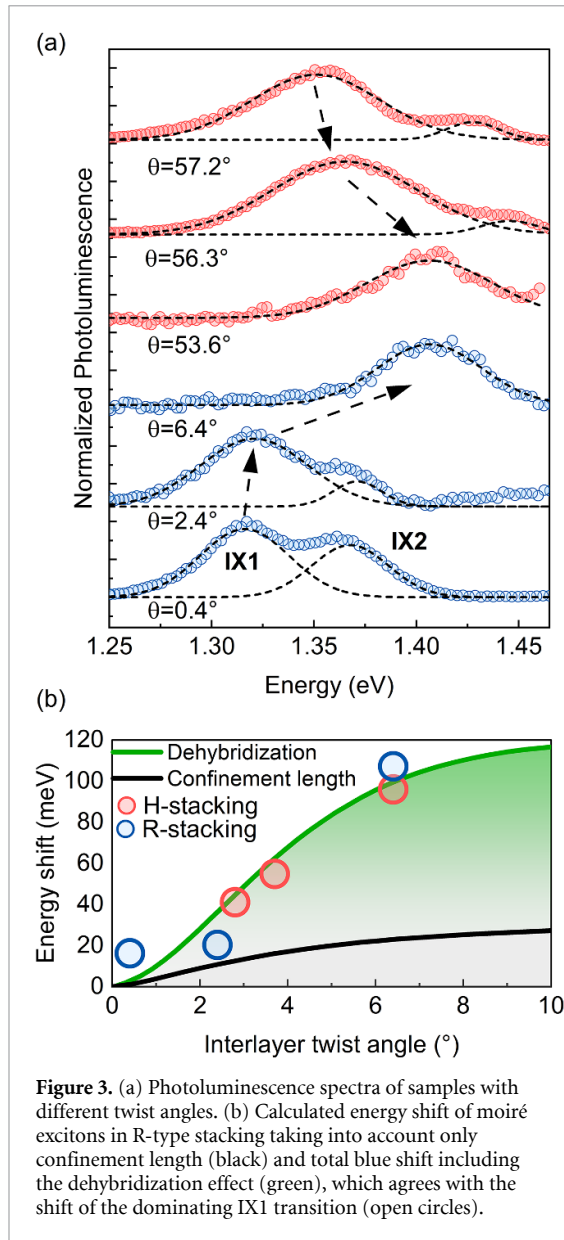


Figure 3. (a) Photoluminescence spectra of samples with different twist angles. (b) Calculated energy shift of moiré excitons in R-type stacking taking into account only confinement length (black) and total blue shift including the dehybridization effect (green), which agrees with the shift of the dominating IX1 transition (open circles).

determine the twist-angle dependent moiré potential. With the increasing twist angle, the period of the moiré superlattice decreases, which induces delocalization of the IX over many moiré supercells. This results in a spectral blue shift of the exciton transitions [8, 33] (see also figure 4). However, the confinement length increase (the wave function delocalization) gives rise to only a moderate blue shift of the IX transition, as shown by the black curve in figure 3(b). The most significant contribution to the blue shift arises from the increase of the average interlayer distance throughout the supercell when increasing the twist angle. This consequently leads to a significant dehybridization of the moiré excitons and a major blue shift (see also SI.6). The sum of both, moiré period and dehybridization contributions in R-type stacking, is represented by the green line in figure 3(b), which nicely reproduces the observed blue shift. This result strongly supports the

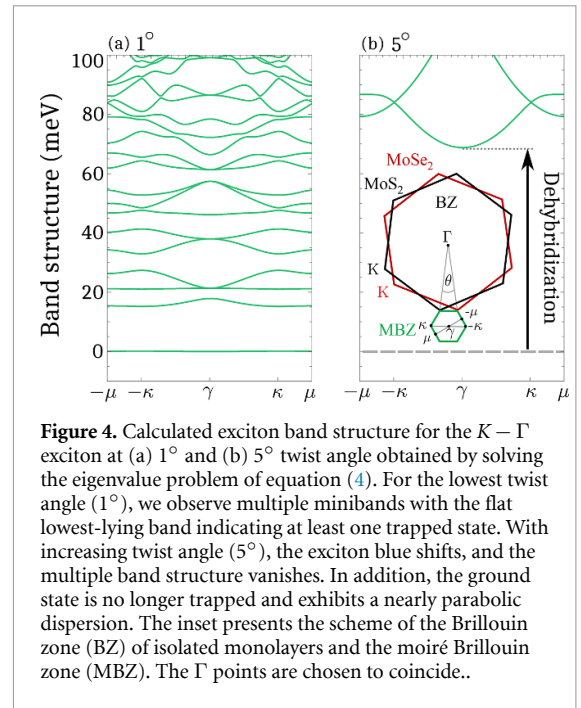


Figure 4. Calculated exciton band structure for the K- Γ exciton at (a) 1° and (b) 5° twist angle obtained by solving the eigenvalue problem of equation (4). For the lowest twist angle (1°), we observe multiple minibands with the flat lowest-lying band indicating at least one trapped state. With increasing twist angle (5°), the exciton blue shifts, and the multiple band structure vanishes. In addition, the ground state is no longer trapped and exhibits a nearly parabolic dispersion. The inset presents the scheme of the Brillouin zone (BZ) of isolated monolayers and the moiré Brillouin zone (MBZ). The Γ points are chosen to coincide..

hybrid nature of the IX transition in the MoSe₂/MoS₂ heterostructure.

Our model also allows us to explain the double-peak structure of the PL spectrum for small twist angles. The exciton band structure calculations presented in figure 4 show a change in the band dispersion and in the number of bands with the twist angle. For small twist angles (1°), our calculations predict multiple exciton bands separated by several to tens meV. Flat bands indicate that the exciton is spatially localized within the moiré trapping potential [8], while dispersive bands correspond to the spatially delocalized IX. We attribute the double peak structure of IX PL spectrum observed for small twist angles heterostructure to the recombination of excitons related to the different bands. For larger twist angles, the IX exciton band blue shifts and the multiband structure vanishes. This yields a single parabolic delocalized band, which results in a single PL peak.

To support our finding, we have performed measurements as a function of the excitation power. Figure 5(a) shows the normalized PL spectra (from sample B with a 0.4°) for different excitation powers. For the lowest excitation powers, the PL is composed of only one peak. With increasing power, an additional peak on the high energy side emerges. The intensity increases with excitation power for both peaks, as demonstrated in figure 5(b). To quantify this effect, we fit the power dependence of IX1 and IX2 with a power law. The lower energy peak exhibits a sublinear power dependence with an exponent $\alpha_{IX1} = 0.71$, characteristic of a trapping potential (with a low density of states), which experiences a gradual saturation (state filling) with increasing excitation power [14, 37, 54, 55]. The increase of the

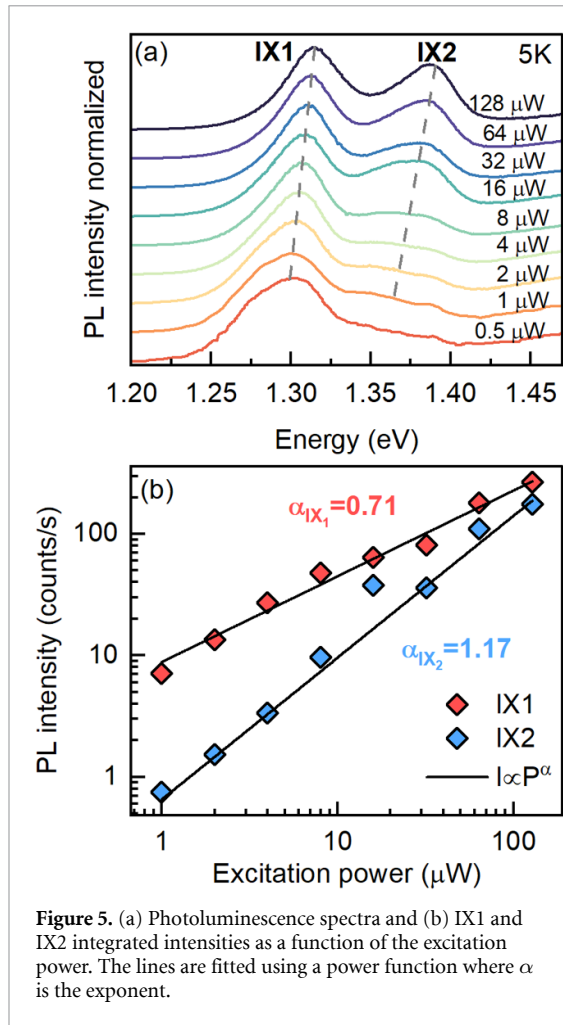


Figure 5. (a) Photoluminescence spectra and (b) IX1 and IX2 integrated intensities as a function of the excitation power. The lines are fitted using a power function where α is the exponent.

high energy peak (IX2) with the excitation power is slightly superlinear ($\alpha_{IX2} = 1.17$), which may point to the delocalized exciton character of this transition or to a much higher density of states. Therefore, the power-dependent measurements corroborate the assignment of the double-peak structure to a moiré induced multiband structure of the IX exciton for heterostructures with a small twist angle. In addition, both IX transitions exhibit a blue shift with increasing excitation power (figure S3), which can be attributed to the repulsive dipolar interactions between IXs caused by their permanent out-of-plane dipole moments [56, 57]. To further support our claim, in figure S4 we present the temperature-dependent PL measurements performed on the same sample. With increasing temperature we observe that the IX2-related emission quenches faster as compared to IX1. This observation is consistent with the power-dependent measurements and support the stronger localization of the IX1 transition as compared with IX2.

3. Conclusion

Combining experiment and theory, we have shown that the ground exciton state in the MoSe₂/MoS₂

heterostructure is a momentum dark and strongly hybridized interlayer Γ K exciton state. Its properties are determined by the combined effect of the moiré potential and the hybridization of MoS₂ and MoSe₂ valence bands around the Γ point. We observe a strong blue shift of the K - Γ transition with increasing twist angle. This can be explained by the dehybridization of the exciton when the twist angle moves away from 0° or 60°. This behavior resembles twisted homobilayers and distinguishes MoSe₂/MoS₂ from the most intensively investigated MoSe₂/WSe₂ heterostructure. We also show that the multiple peaks we observe in the PL spectrum of MoSe₂/MoS₂ heterostructures with a small twist results from the moiré pattern-driven exciton miniband formation.

4. Methods

4.1. Samples fabrications

TMD monolayers and hBN flakes were obtained by the mechanical exfoliation technique. The TMDs and part of hBN used in the fabrication are commercially available. Synthetic MoSe₂ grown by chemical vapor transport has been purchased from HQ graphene. Natural MoS₂ from Molly Hill mine, Québec, Canada, hBN for samples E and F is provided from Japan. For the remaining samples, hBN was purchased from HQ Graphene. For all the exfoliations, we used Nitto tape (Nitto Denko corp. SPV 224). Monolayer thickness of MoS₂ and MoSe₂ was confirmed by transmittance and reflection measurements before their transfer [58]. The heterostructures were stacked by dry pick-up method [49, 59, 60] and deposited on SiO₂ substrates.

4.2. Spectroscopy measurements

To perform spectroscopy measurements, the samples were mounted on the cold finger of a helium flow cryostat. All of the measurements were performed at a temperature of $T = 5$ K unless otherwise specified. The excitation laser was focused and the PL was collected by a 50 × microscope objective (Mitutoyo Inc.) having a numerical aperture of 0.55. The resulting spot size had a diameter of approximately $\simeq 1 \mu\text{m}$. For PL measurements, the excitation was provided by a continuous-wave frequency-doubled solid-state laser emitting at 532 nm. A fs-pulsed Ti:Sapphire laser with an average power of 15 mW was used for SHG measurements. Additionally, for polarization resolved SHG, was polarized by means of a Glan-Thompson polarizer and an achromatic half-wave plate. The polarization state of the second harmonic signal was controlled by making use of the same half-wave plate and was analyzed by a linear polarizer. The reflectance, PL and SHG signals were spectrally resolved by a 30 cm long monochromator equipped with a 150 grooves mm^{-1} grating and detected by a liquid nitrogen cooled CCD camera.

4.3. Theory

In order to obtain access to the moiré exciton energy landscape we consider a Hamiltonian formulated in second quantization. For this purpose, we start in a decoupled monolayer basis and take into account the moiré potential as periodic modifications to the decoupled exciton energies [8, 33, 61]. Importantly, in the rigid lattice case we have two components of the moiré potential [48, 61]: the electrostatic alignment shift [8] and interlayer hybridization [33, 34, 61]. The decoupled exciton energies are obtained by solving the Wannier equation [22], which gives us the binding energies for the intra/IX states. This allows us to write the Hamiltonian in exciton basis as [8, 30, 33, 34, 61]

$$H_0 = \sum_{LQ\xi} E_{LQ}^{\xi} X_{L,Q}^{\xi\dagger} X_{L,Q}^{\xi} + \sum_{LQ\xi, g} V_L^{\xi}(g) X_{L,Q+g}^{\xi\dagger} X_{L,Q}^{\xi} + \sum_{LL', Q\xi g} T_{LL'}^{\xi}(g) X_{L,Q+g}^{\xi\dagger} X_{L',Q}^{\xi} + h.c \quad (2)$$

with $L = (l_e, l_h)$ as a compound layer index, \mathbf{Q} as the center-of-mass momentum, $\xi = (\xi_e, \xi_h)$ as the exciton valley index and $\mathbf{g} = \mathbf{G}_2 - \mathbf{G}_1$ as the reciprocal lattice vectors of the rigid superlattice (given by the difference of the reciprocal lattice vectors of the two different layers). Additionally, $X^{(\dagger)}$ are annihilation (creation) operators for the non-hybrid excitons. Here, E_{LQ}^{ξ} is the non-hybridized exciton dispersion that is calculated from the Wannier equation [22]. Furthermore, $V_L^{\xi}(g)$ is the periodic electrostatic shift of the moiré excitons, determined by the local atomic alignment [8]. In this work, the predominant component of the moiré potential stems from the exciton hybridization that is described by the tunneling term in the Hamiltonian reading [33, 34]

$$T_{LL'}^{\xi}(g) = \left[\delta_{l_h, l'_h} (1 - \delta_{l_e, l'_e}) t_{l_e l'_e}^{\xi_e}(g) \mathcal{F}_{LL'}^{\xi}(\beta_{LL'} g) - \delta_{l_e, l'_e} (1 - \delta_{l_h, l'_h}) t_{l_h l'_h}^{\xi_h}(g) \mathcal{F}_{LL'}^{*\xi}(-\alpha_{LL'} g) \right]. \quad (3)$$

Here, $\mathcal{F}_{LL'}^{\xi}(q) = \sum_{\mathbf{k}} \Psi_L^{\xi*}(\mathbf{k}) \Psi_{L'}^{\xi}(\mathbf{k} + \mathbf{q})$ are the exciton form factors. Furthermore, we have introduced $\alpha_{ij}(\beta_{ij}) = m_{i(j)}^{c(v)} / (m_i^c + m_j^v)$ with the masses extracted from [62]. The Kronecka deltas ensure single carrier tunneling processes. Furthermore, $t_{\lambda\lambda'}^{\xi_\lambda}(g)$ are the Fourier coefficients of the real-space tunneling potential, where $\lambda = (c, v)$ is the band index. The Fourier coefficients take into account the twist-angle dependence of the tunneling strength (cf. figure S5).

We transform equation (2) to a zone-folded hybrid moiré exciton basis [8, 33, 61], $Y_{\xi\eta Q}^{\dagger} = \sum_{gL} C_{Lg}^{\xi\eta*}(\mathbf{Q}) X_{L,Q+g}^{\xi\dagger}$, where \mathbf{Q} is now restricted to the first mini-Brillouin zone. Here, η is the new exciton

band index, $C_{Lg}^{\xi\eta*}(\mathbf{Q})$ are the mixing coefficients determining the relative mixing between sub-bands and intra/IXs. Moreover, $Y_{\xi\eta Q}^{\dagger}$ is the zone-folded moiré exciton creation operator. Consequently, we obtain the following eigenvalue problem

$$E_{LQ}^{\xi} C_{Lg}^{\xi\eta}(\mathbf{Q}) + \sum_{g'} V_L^{\xi}(g' - g) C_{Lg'}^{\xi\eta}(\mathbf{Q}) + \sum_{L'g'} T_{LL'}^{\xi}(g' - g) C_{L'g'}^{\xi\eta}(\mathbf{Q}) = \mathcal{E}_{\eta Q}^{\xi} C_{Lg}^{\xi\eta}(\mathbf{Q}). \quad (4)$$

Solving equation (4) numerically gives a microscopic access to the final hybrid moiré exciton energies $\mathcal{E}_{\eta Q}^{\xi}$.

Data availability statement

All data that support the findings of this study are included within the article (and any supplementary files).

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