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Plane-wave many-body corrections to the conductance in bulk tunnel junctions

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The conductance of bulk metal–insulator–metal junctions is evaluated by the Landauer formula using an *ab initio* electronic structure calculated using a plane-wave basis set within density functional theory and beyond, i.e., including exact nonlocal exchange using hybrid functional (HSE) or many-body G_0W_0 and Coulomb-hole screened exchange (COHSEX) quasiparticle schemes. We consider an Ag/MgO/Ag heterostructure model and we focus on the evolution of the zero-bias conductance as a function of the MgO film thickness. Our study shows that the correction of the electronic structure beyond semilocal density functionals goes in the right direction to improve the agreement with experiments, significantly reducing the zero-bias conductance. This effect becomes more evident at larger MgO thickness, that is, in increasing tunneling regime. We also observe that the reduction of the conductance seems more related to the correction of wave functions rather than energies, and thus not directly related to the correction of the band gap of bulk MgO. G_0W_0 and HSE both provide a band gap in agreement with experiments, but only HSE gives a significant reduction of the conductance. COHSEX, while overestimating the band gap, gives a reduction of the conductance very close to HSE.

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I. INTRODUCTION

Metal–insulator–metal junctions are of high technological interest since they are used in currently developed electronic devices, like new generation memories based on the variation of the electric resistance (RRAM [1,2]) or magnetoresistive devices [3–5]. First-principles calculations of the tunneling conductance in these junctions can provide an important understanding to drive technological developments. With the downscaling of microelectronics, the typical size of devices can reach a few nanometers, which calls for an atomistic and quantum treatment of the electronic transport. In particular, the calculation of the transmission of electrons through an interface between two materials requires an accurate description of the electron wave functions at the atomic scale.

The prevalent approach to study quantum transport at the atomic scale is the *ab initio* “DFT + Landauer” scheme. Density functional theory (DFT) [6,7] is used to calculate the electronic structure of the junction and of the leads. The probability of transmission of electrons through the junction is then calculated using the Green’s function method, and the zero-bias conductance is obtained via the multichannel Landauer formula [8–11]. Several available codes, e.g., the ones documented in Refs. [12–14], implement DFT + Landauer on spatially localized basis sets (atomic orbitals, Wannier func-

tions), which are more convenient to compute the quantum transmission.

This approach has two main limitations. First, the Landauer formalism only holds in the coherent regime of transport, which means that inelastic scattering such as electron–electron and electron–phonon interactions cannot be taken into account. Second, only calculations close to the zero-bias limit are formally correct since so far there exist no exact formulation of DFT for out-of-equilibrium and open systems (i.e., varying number of electrons).

However, some DFT + Landauer codes, such as TRANSIESTA [12], allow applying a finite-bias voltage between the electrodes, still using the equilibrium density functional. Despite the incompleteness of such approach [15], it allows addressing realistic devices within a reasonable computing time and provides valuable information about the transmission of electrons through interfaces, for instance when the symmetries of the wave functions in each material strongly impact the transmission [3]. The DFT + Landauer method should also provide a good estimation of the elastic scattering of electrons by defects and impurities. This holds in the coherent regime, which is a reasonable approximation for short junctions (a few nanometers) and at very low temperature, so that the electrons do not lose their phase coherence between the two electrodes.

Unfortunately, in the coherent regime and at zero-bias voltage, DFT + Landauer turns out to catch only a qualitative description of transport, and to systematically overestimate conductances by one or even several order of magnitudes in the tunneling regime. This was pointed out by Vignale and Di Ventra [15], and there are several hypotheses about this failure. One of them [16–19] attributes the systematic

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overestimation of the conductance to the systematic underestimation of the HOMO-LUMO gap in molecules, and analogously of the band gap in insulators, by DFT [20]. On the contrary, when inelastic scattering becomes dominant, DFT + Landauer often underestimates the tunneling conductance. Electron-phonon and electron-electron scatterings can be added on top of *ab initio* calculations [21,22]. This is not the topic of this work, which focuses on the limitation of DFT + Landauer in the coherent regime and at zero bias.

For this purpose, this study goes beyond DFT toward many-body quasiparticle (MB-QP) approaches, including the *GW* [23] or the COHSEX [23] (Coulomb-hole screened exchange) approximations. We also consider the Heyd-Scuseria-Ernzerhof (HSE) hybrid functional [24] which, rigorously speaking, cannot be considered an approximation within DFT like the local density approximation (LDA) or generalized gradient approximation (GGA), and should be rather considered as a semiempirical MB approximation, with a modified Hartree-Fock exchange Fock operator mimicking the COHSEX statically screened exchange nonlocal self-energy. With respect to DFT LDA or GGA, these QP approaches certainly provide a more physical electronic structure, and this should translate into an improved description of quantum transport properties. The approach used in this work is still based on the Landauer formalism, but with a corrected electronic structure. Along these lines, several authors have already attempted to go beyond DFT + Landauer to describe quantum transport in molecular junctions, for example, by using semiempirical models like the image-charge DFT + Σ model [17], or the Hubbard model with an adjustable U parameter local interaction term placed only on chosen correlated electrons solved by dynamical mean-field theory (DMFT) [25–27], or recent out-of-equilibrium approaches based on the time-dependent-DFT formalism (TDDFT) [28], but also fully *ab initio* approaches [29–31] like *GW* or COHSEX. Such attempts remain rare in the literature. The main reason is that MB-QP calculations on bulk materials are not implemented in the available DFT codes using localized basis sets, which are the most suitable for transport calculations. Moreover, MB-QP corrections on bulk tunnel junctions, such as the Ag/MgO/Ag heterostructure studied here, are barely explored so far. By bulk junctions, we mean junctions with macroscopic dimensions along the directions parallel to the interfaces. Faleev *et al.* [32] have studied the Fe/MgO/Fe junction within a MB-QP framework, but making use of an empirical formula [Ref. [32], Eq. (1)] instead of a full Landauer formula to compute the transmission function.

By relying on a quantum transport implementation based on plane waves and Wannier functions (see Sec. II), we compute the quantum transmission spectra and zero-bias conductances of metal–insulator–metal junctions made of a thin film of MgO sandwiched between two bulk Ag electrodes. This model of heterostructure is reasonable since, experimentally, thin layers of MgO can be epitaxially deposited on an Ag substrate [33]. Considering ferromagnetic electrodes would be of higher technological interest as they form magnetic tunnel junctions with MgO [3–5]. However, we have chosen Ag electrodes to avoid the additional complexity of spin-polarized transport and to focus only on the effect of MB corrections on the tunneling conductance.

We study the transport properties of the junction as a function of the oxide thickness, from 1 to 4 MgO cubic cells, and we consider four different approximations: DFT in the GGA PBE approximation; G_0W_0 [23] on top of DFT, which takes into account only a diagonal *GW* self-energy and allows recalculating only the QP energies, keeping the DFT wave functions unchanged; the self-consistent COHSEX approximation, which instead recalculates both QP energies and wave functions; the HSE hybrid functional, which also updates both energies and wave functions. In Sec. III, we present the simulation results and we analyze the effect of the different approximations on the transport properties in the tunneling regime.

II. METHOD AND COMPUTATIONAL DETAILS

In this section we describe the method and the computational details used to calculate the tunneling conductance through Ag/MgO/Ag junctions. The procedure is divided into three parts.

(1) The electronic structure of Ag/MgO/Ag supercells is computed self-consistently on a plane-wave basis set. The calculations are performed within DFT or using various MB corrections on top of DFT in order to compare their impact on electronic transport.

(2) A basis-set transformation is performed from plane waves to maximally localized Wannier functions [34–36], using the WANNIER90 code [37]. The Hamiltonian expressed in this basis is convenient for transport calculations.

(3) The electron transport through Ag/MgO/Ag junctions is computed by the Landauer formalism [10] and the Green's functions method, using our in-house code which allows calculating the transmission for any transverse wave vector \mathbf{k}^{\parallel} parallel to the Ag/MgO interfaces. This is necessary for evaluating the conductance through junctions with macroscopic surface area.

A. DFT computational details

Ab initio calculations based on DFT are carried out using the VASP code [38,39] with the PBE [40] functional. The core-valence interaction is described by projector augmented wave (PAW) data sets including $4d$ and $5s$ states for Ag, $2s$ and $2p$ for O, and $3s$ for Mg. Electron wave functions are expanded in a plane-wave basis set with a kinetic energy cutoff of 415 eV. HSE calculations and MB corrections are detailed in Sec. II C.

For comparison purpose, DFT calculations have also been performed using the SIESTA code [41,42]. The chosen functional is also PBE, while the pseudopotentials are of norm-conserving Troullier-Martins type [43] and include the same states as the VASP PAW data sets. A polarized double-zeta basis set of atomic orbitals is used, with a cutoff radius yielding an energy shift of 25 meV. The plane-wave cutoff for the real-space grid is taken equal to 450 Ry.

B. Structures studied in *ab initio*

Ag and MgO both have face-centered-cubic structure and are stacked along the [100] direction. O atoms are located in front of Ag atoms, which is known to be the most stable configuration [33]. In the following, m Ag/ n MgO/ m Ag denotes

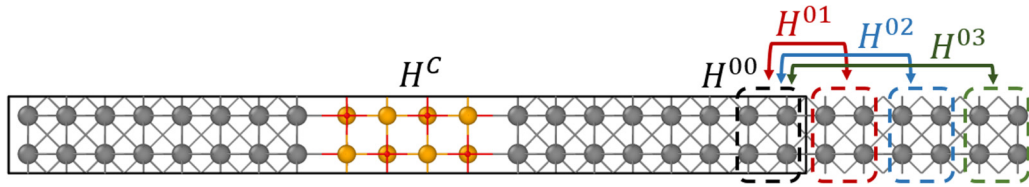


FIG. 1. 4 Ag/2 MgO/4 Ag supercell (outlined by a solid line rectangle) studied in *ab initio*. 3Ag cubic cells of its right-side periodic replica are also represented. The Hamiltonian blocks used for transport calculations are schematized: H^C is the Hamiltonian of the central region and the blocks H^{0i} define the semi-infinite periodic Ag electrodes. See Sec. II F for details.

a supercell with n MgO cubic cells surrounded on both sides by m Ag cubic cells.

Cell volume relaxations are performed on bulk Ag and bulk MgO, yielding lattice constants of 4.14 and 4.20 Å, respectively. Then, structural relaxations of 2 Ag/ n MgO/2 Ag supercells are performed, n ranging from 1 to 4. The Brillouin zone is sampled using a $1 \times 4 \times 4$ Monkhorst-Pack (MP) grid. The lattice constants along directions [010] and [001], parallel to the interfaces, are fixed to the lattice constant of bulk Ag (4.14 Å) in order to mimic thin layers of MgO epitaxially sandwiched between thick unstrained Ag layers. Hence, the MgO layer is compressively strained in the in-plane directions. The length of the supercell along [100] is relaxed. The interfacial distance turns out to be $d \simeq 2.69$ Å between the Ag and MgO atomic planes, in good agreement with previous studies [33]. The MgO lattice constant is elongated to about 4.33 Å along [100].

Supercells with thicker Ag layers are needed to define the semi-infinite periodic electrodes in transport simulations (see Fig. 1 and Sec. II F). These supercells are built from the relaxed systems discussed above, by keeping the relaxed atomic positions of the MgO layer and of 1 cubic cell of Ag on each side of MgO, and by adding 3 Ag cubic cells on each side, with an interplane distance fixed to the bulk value, 2.07 Å. This ensures the perfect periodicity of the first 3 and last 3 Ag unit cells, which will be used to define the Hamiltonian of the semi-infinite electrodes. In the following, all *ab initio* calculations are performed on these 4 Ag/ n MgO/4 Ag supercells, with a $2 \times 4 \times 4$ MP grid containing Γ . Given that each MgO cubic cell contains 8 atoms, and each Ag cubic cell contains 4 atoms, the supercells contain 40, 48, 56, and 64 atoms for $n = 1, 2, 3, 4$, respectively.

C. HSE calculations and many-body corrections

HSE calculations are carried out using VASP with the HSE06 hybrid functional [44]. According to Viñes *et al.* [45], HSE06 requires an α mixing parameter higher than 0.4 to reproduce the MgO experimental gap. Here, α is fixed to 0.43, which gives an electronic band gap at Γ of 7.77 eV for the MgO primitive cell, in agreement with the experimental value which lies between 7.67 and 7.83 eV [45]. The screening parameter is fixed to 0.2 \AA^{-1} .

MB effects are accounted for by using G_0W_0 (correction of eigenvalues only) and self-consistent COHSEX (correction of both eigenvalues and eigenfunctions) on top of DFT. The use of a full self-consistent GW calculation on both eigen-

values and eigenfunctions is not considered here, due to the high computational cost. COHSEX is an approach halfway between Hartree-Fock [46] and GW . The HF bare exchange is statically screened in COHSEX, and it considers an additional ‘‘Coulomb-hole’’ term which accounts for a classical response of the medium after the addition of a point charge (electron or hole). It requires less computational resources than GW , but it systematically overestimates the band gap. For G_0W_0 calculations, we use a cutoff energy of 210 eV for the response function, and 64 frequency grid points. The number of empty bands used in the dielectric function and for the Green’s function is 6144 for the structures with 1 and 2 MgO cubic cells, and 6656 for the structures with 3 and 4 MgO cubic cells. For self-consistent COHSEX the number of bands is reduced to 2048, except for the biggest structure (4 MgO), which uses 3072 bands. The number of self-consistent cycles is taken equal to 3.

D. Transformation to a Wannier basis set

The transformation from Bloch waves to maximally localized Wannier functions is performed with the WANNIER90 code [37] and its interface with VASP. The bands around the Fermi level are not isolated in the energy spectrum. Hence, we use the method of Souza *et al.* [35]: The bands within a ‘‘frozen’’ energy window are completed by an optimal subspace of higher-energy bands. The Wannier functions describe exactly the bands within the frozen window, which is chosen here between the bottom of the valence band up to 3 eV above the Fermi level.

A set of trial orbitals is needed as a starting point for the WANNIER90 code. For Ag, we choose the set of orbitals proposed by Souza *et al.* [35] for copper: $5d$ orbitals centered on each atom, and interstitial s orbitals. For MgO, we choose $1s$ and $3p$ orbitals on oxygen atoms, and also interstitial s orbitals. Hence, there are 28 Wannier functions per Ag cubic cell and 24 Wannier functions per MgO cubic cell, which yields 320 Wannier functions for the largest structure (4 Ag/4 MgO/4 Ag). The number N_b of *ab initio* bands included in the optimization of the Wannier subspace is chosen at least twice the number N_w of Wannier functions. Using 100 iterations for optimizing the subspace (‘‘disentanglement’’ step) and 100 iterations for optimizing the Wannier functions, we obtained well-localized functions with quadratic spreads not exceeding 2 \AA^2 .

We give here some notations and recall some basic properties of Wannier functions [36] which will be used in the following. Let \mathbf{a}_i denote the real lattice basis vectors of the *ab initio* supercell, which will be referred to as the ‘‘ref-

erence supercell” (RS). Here, \mathbf{a}_1 , \mathbf{a}_2 , and \mathbf{a}_3 are chosen along the crystal directions [100], [010], and [001], respectively. Let \mathbf{g}_i denote the reciprocal lattice basis vectors. The *ab initio* Bloch states $|\psi_{n\mathbf{k}}\rangle$ are computed for \mathbf{k} points in a MP grid containing Γ with N_i mesh points along each direction \mathbf{g}_i . Hence, these states satisfy periodic boundary conditions over an extended supercell (ES) made of N_i replicas of the RS along each direction \mathbf{a}_i . The replicas are indexed by their translation vector \mathbf{R} with respect to the RS:

$$\mathbf{R} = p_1\mathbf{a}_1 + p_2\mathbf{a}_2 + p_3\mathbf{a}_3, \quad (1)$$

where p_i are integers. The Wannier functions are optimized linear combinations of Bloch states:

$$|\mathbf{R}n\rangle = \frac{1}{N} \sum_{\mathbf{k}} e^{-i\mathbf{k}\cdot\mathbf{R}} \sum_{m=1}^{N_b} U_{mn}^{(\mathbf{k})} |\psi_{m\mathbf{k}}\rangle, \quad (2)$$

where n indexes the N_w Wannier functions of each cell \mathbf{R} , and N is the number of \mathbf{k} points. The $U^{(\mathbf{k})}$ are $N_b \times N_w$ complex matrices with orthonormal columns, optimized by the WANNIER90 code to maximize the localization of the Wannier functions. The average position of $|\mathbf{0}n\rangle$, called Wannier center, is denoted as $\bar{\mathbf{r}}_n$. The phases of the $U^{(\mathbf{k})}$ matrices are chosen so that the $\bar{\mathbf{r}}_n$ are within the RS. $|\mathbf{R}n\rangle$ is the translation by \mathbf{R} of $|\mathbf{0}n\rangle$, hence, its center is at $\bar{\mathbf{r}}_n + \mathbf{R}$.

Wannier functions form an orthonormal basis. They satisfy periodic boundary conditions over the ES. Hence, each Wannier function $|\mathbf{R}n\rangle$ contains periodic replicas centered around positions $\mathbf{R} + \mathbf{T} + \bar{\mathbf{r}}_n$, where \mathbf{T} is any vector of the lattice defined by the periodic repetition of the ES:

$$\mathbf{T} = p_1N_1\mathbf{a}_1 + p_2N_2\mathbf{a}_2 + p_3N_3\mathbf{a}_3. \quad (3)$$

E. Hamiltonian in the Wannier basis

From Eq. (2), one obtains the expression of the *ab initio* Hamiltonian in the Wannier basis:

$$\langle \mathbf{R}n | \hat{H} | \mathbf{R}'n' \rangle = \frac{1}{N} \sum_{\mathbf{k}} e^{i\mathbf{k}\cdot(\mathbf{R}-\mathbf{R}')} \sum_{m=1}^{N_b} U_{mn}^{(\mathbf{k})*} \epsilon_{m\mathbf{k}} U_{m'n'}^{(\mathbf{k})}, \quad (4)$$

where $\epsilon_{m\mathbf{k}}$ are the Bloch state energies. From these matrix elements, a Hamiltonian with finite-range coupling is defined. It is meant to describe the infinite crystal instead of the ES, and it will be used for transport calculations and for interpolating the band structure at \mathbf{k} points which are not in the MP grid. For this purpose, each Wannier function $|\mathbf{R}n\rangle$ is now interpreted as a localized function centered around $\mathbf{R} + \bar{\mathbf{r}}_n$, independent from its periodic replicas centered around $\mathbf{R} + \mathbf{T} + \bar{\mathbf{r}}_n$. Each $|\mathbf{R}n\rangle$ is only coupled to the $|\mathbf{R}'n'\rangle$ whose centers $\mathbf{R}' + \bar{\mathbf{r}}_{n'}$ are in the Wigner-Seitz cell centered around $\mathbf{R} + \bar{\mathbf{r}}_n$ and associated to the ES. In other words, $\mathbf{R}' + \bar{\mathbf{r}}_{n'}$ must be closer to $\mathbf{R} + \bar{\mathbf{r}}_n$ than any of its periodic replicas $\mathbf{R}' + \bar{\mathbf{r}}_{n'} + \mathbf{T}$. This convention for defining the Hamiltonian is an available option in the WANNIER90 code. It implies, in this study, that the maximum coupling range along the transport direction is $N_1 \times L/2$, where L is the RS length.

The accuracy of this Hamiltonian improves rapidly when refining the MP grid of the *ab initio* calculation. For the systems considered here, a $2 \times 4 \times 4$ grid is sufficient. The reason to use two \mathbf{k} points along the transport direction is discussed in Appendix A.

Obviously, the Hamiltonian is modified when performing MB corrections. For G_0W_0 , the Bloch states are unchanged and only the eigenvalues $\epsilon_{m\mathbf{k}}$ are modified. Hence, we keep the same Wannier functions and only recompute the Hamiltonian matrix elements of Eq. (4). For HSE and self-consistent COHSEX, since Bloch states are modified, Wannier functions must be reoptimized.

F. Calculation of the tunneling conductance

The Wannier Hamiltonian allows replacing the periodic repetition of the *ab initio* supercell along the transport direction by semi-infinite Ag electrodes. It also allows interpolating the band structure on a finer grid of transverse \mathbf{k} points. Indeed, the quantum transmission through the Ag/MgO/Ag junction strongly depends on the wave vector parallel to the interfaces $\mathbf{k}^{\parallel} = k_2\mathbf{g}_2 + k_3\mathbf{g}_3$. The 4×4 grid used in our *ab initio* simulations is not fine enough to resolve this dependence. Hence, we consider a finer MP grid of \mathbf{k}^{\parallel} points. Wave functions are developed on the following basis, indexed by the lattice vector $\mathbf{R}^{\perp} = p_1\mathbf{a}_1$ along the transport direction, the Wannier index n , and the transverse wave vector \mathbf{k}^{\parallel} :

$$|\mathbf{R}^{\perp}n\mathbf{k}^{\parallel}\rangle = \frac{1}{\sqrt{N^{\parallel}}} \sum_{\mathbf{R}^{\parallel}} e^{i\mathbf{k}^{\parallel}\cdot(\mathbf{R}^{\perp}+\bar{\mathbf{r}}_n)} |\mathbf{R}^{\perp} + \mathbf{R}^{\parallel}\rangle n, \quad (5)$$

where N^{\parallel} is the number of \mathbf{k}^{\parallel} points, and \mathbf{R}^{\parallel} runs over transverse lattice vectors:

$$\mathbf{R}^{\parallel} = p_2\mathbf{a}_2 + p_3\mathbf{a}_3. \quad (6)$$

These basis states are localized along the transport direction \mathbf{a}_1 , and Bloch type along the transverse directions. The Hamiltonian only couples states with the same transverse wave vector \mathbf{k}^{\parallel} and its matrix elements are computed in terms of the matrix elements of Eq. (4):

$$H_{\mathbf{R}^{\perp}n\mathbf{R}^{\perp}n'}^{(\mathbf{k}^{\parallel})} = \sum_{\mathbf{R}^{\parallel}} e^{i\mathbf{k}^{\parallel}\cdot(\mathbf{R}^{\perp}+\bar{\mathbf{r}}_n-\bar{\mathbf{r}}_{n'})} \langle \mathbf{R}^{\perp}n | \hat{H} | \mathbf{R}^{\perp} + \mathbf{R}^{\parallel}n' \rangle. \quad (7)$$

In some cases, the matrix elements will be neglected beyond a cutoff distance L_{cut} along the transport direction. The cutoff condition reads as

$$|(\mathbf{R}^{\perp} + \bar{\mathbf{r}}_n - \mathbf{R}^{\perp}n' - \bar{\mathbf{r}}_{n'}) \cdot \hat{\mathbf{a}}_1| > L_{\text{cut}}, \quad (8)$$

where $\hat{\mathbf{a}}_1$ is the unit vector along the transport direction.

We can now define the Hamiltonians of the central region and of the electrodes. The central region is defined as the RS and its $N_w \times N_w$ Hamiltonian reads as

$$H_{nn'}^C = H_{0n0n'}^{(\mathbf{k}^{\parallel})}, \quad (9)$$

where we have omitted the transverse wave vector in H^C to lighten the notations. The Hamiltonian of the periodic electrodes is extracted from Ag unit cells which are far enough from MgO so that its influence is screened. We also need to define a cutoff distance beyond which the couplings between orbitals in Ag are negligible. A convergence study has shown that we can neglect the couplings between one cubic unit cell of Ag and its fourth neighbors and beyond. The remaining Hamiltonian blocks, schematized in Fig. 1, are extracted from the Hamiltonian (7). More precisely, the diagonal block of the

last Ag cubic cell H^{00} is made of the matrix elements

$$H_{0n0n'}^{(k^\parallel)} \quad (10)$$

with n and n' restricted to the orbitals of the last cubic cell. Similarly, the coupling blocks H^{0i} between this cell and the first three cells of the right-side RS replica ($\mathbf{R}^\perp = \mathbf{a}_1$) are made of the matrix elements

$$H_{0na_1n'}^{(k^\parallel)} \quad (11)$$

with n and n' restricted to the relevant cubic cells. The blocks H^{0i} have dimension 28×28 . They are used to build the Hamiltonians of the electrodes, which are block-tridiagonal, each block corresponding to three cubic cells. The right electrode Hamiltonian reads as

$$H^R = \begin{pmatrix} D & \tau & \\ \tau^\dagger & D & \ddots \\ & \ddots & \ddots \end{pmatrix} \quad (12)$$

with the diagonal block

$$D = \begin{pmatrix} H^{00} & H^{01} & H^{02} \\ H^{01\dagger} & H^{00} & H^{01} \\ H^{02\dagger} & H^{01\dagger} & H^{00} \end{pmatrix} \quad (13)$$

and the coupling block

$$\tau = \begin{pmatrix} H^{03} & 0 & 0 \\ H^{02} & H^{03} & 0 \\ H^{01} & H^{02} & H^{03} \end{pmatrix}. \quad (14)$$

The Hamiltonian of the left electrode is defined in a similar way, using the same blocks. τ also defines the coupling between the electrodes and the central region. The decimation algorithm of Lopez-Sancho *et al.* [47,48] is used to compute the electrodes' self-energies $\Sigma_L(\mathbf{k}^\parallel, E)$ and $\Sigma_R(\mathbf{k}^\parallel, E)$. Full matrix inversion is used to compute the Green's function of the central region. Then, the sum of transmission coefficients $\mathcal{T}(\mathbf{k}^\parallel, E)$ is obtained from the trace formula [49]

$$\mathcal{T}(\mathbf{k}^\parallel, E) = \text{Tr}[\Gamma_R(\mathbf{k}^\parallel, E) G^r(\mathbf{k}^\parallel, E) \Gamma_L(\mathbf{k}^\parallel, E) G^a(\mathbf{k}^\parallel, E)],$$

$$\Gamma_{R,L}(\mathbf{k}^\parallel, E) = i[\Sigma_{R,L}(\mathbf{k}^\parallel, E) - \Sigma_{R,L}^\dagger(\mathbf{k}^\parallel, E)] \quad (15)$$

and it is averaged over transverse \mathbf{k}^\perp points to obtain the total sum of transmission coefficients per Ag cubic cell area:

$$\mathcal{T}(E) = \frac{1}{N^\perp} \sum_{\mathbf{k}^\perp} \mathcal{T}(\mathbf{k}^\perp, E). \quad (16)$$

In the following, a 10×10 MP grid of \mathbf{k}^\perp points is sufficient to reach convergence of $\mathcal{T}(E)$ around the Fermi energy.

Finally, we obtain the zero-bias conductance per Ag cubic cell area, at zero temperature:

$$\mathcal{G} = \mathcal{G}_0 \mathcal{T}(E_f), \quad (17)$$

where $\mathcal{G}_0 = 2e^2/h = 7.75 \times 10^{-5} \Omega^{-1}$ is the quantum of conductance and E_f is the Fermi energy, defined here as the charge neutrality point of the electrodes. This allows a

more reliable comparison between structures with different MgO thicknesses. E_f is obtained as the energy at which the integrated density of states (DOS) of the bulk infinite electrode gives charge neutrality. The DOS is computed from the Green's function on a fine energy grid starting below the valence bands.

G. Range of the Wannier Hamiltonian and cutoff distance

Figure 2 shows how the maximum modulus of the Wannier Hamiltonian matrix elements (7) decreases with the distance between Wannier centers along the transport direction, defined by the left-hand side of Eq. (8). The Hamiltonian is computed in DFT-PBE and with the three different MB corrections, using a $2 \times 4 \times 4$ MP grid. The decay is exponential and similarly fast for all approximations up to a distance where it saturates to constant values. This distance is around 30 Å to saturation values around 10^{-5} eV for all approximations except G_0W_0 , which saturates before the others, around 13 Å, to much higher values, around 10^{-2} eV. This is at first sight surprising since the Wannier functions are exactly the same than in DFT-PBE and well localized. However, the modification of the eigenvalues by the G_0W_0 correction is equivalent to a modification of the Hamiltonian which is local in energy, hence nonlocal in space. It induces long-range couplings between Wannier functions. This was already noticed by Ferretti *et al.* [50] who studied the impact of G_0W_0 corrections in conjugated polymers. This effect is also proven in Appendix B for a simple one-dimensional, two-level, tight-binding model. These long-range couplings have a strong influence on the transmission spectra, which turn out to be noisy. An analysis detailed in Appendix A shows that, if the Hamiltonian accuracy is sufficient, transmission spectra should be nearly insensitive to long-range couplings, which could be safely discarded. We conclude that the high G_0W_0 long-range couplings may be not physical, and we decide to discard them beyond a cutoff distance $L_{\text{cut}} = 13$ Å, after which the G_0W_0 matrix elements become higher than in the

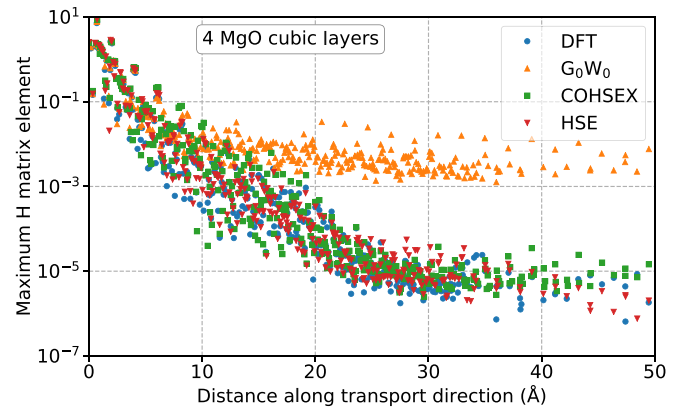


FIG. 2. Maximum modulus of the Wannier Hamiltonian matrix elements (7) as a function of the distance between Wannier centers along the transport direction, as calculated by various approximations, here shown for the longest system (4 Ag/4 MgO/4 Ag). The difference between DFT and G_0W_0 is only due to the change of eigenvalues in Eq. (4). On the contrary, for HSE and COHSEX, the matrix $U_{mn}^{(k)}$ also changes.

other approximations. However, in the following, one should keep in mind that G_0W_0 spectra are subject to caution, and that G_0W_0 does not seem to be a reliable method to compute the transport properties of tunnel junctions.

III. RESULTS

A. Transmission spectra in the DFT approximation

The transmission values computed at the level of DFT-PBE are expected to be consistent with existing codes based on localized functions basis set. Such comparison is interesting to see if the results are robust with respect to the basis choice. Figure 3 shows the transmission spectra $\mathcal{T}(E)$ calculated for different MgO thicknesses, in the DFT-PBE approximation. As expected, the plane-waves/Wannier results are in very good agreement with those obtained with TRANSIESTA.

We will now provide an interpretation of the transmission curves. At low energies we are in the valence band (VB) of MgO, and the transmission is high and independent of the MgO thickness. The VB edge lies at about -2.2 eV below E_f . Beyond the VB, in the MgO band gap, we enter into the tunneling regime and the transmission decreases exponentially with the thickness. The values of the zero-bias conductance are given in Table I and its exponential decay with the MgO thickness is shown in Fig. 5.

The analysis, not shown here, of the \mathbf{k}^{\parallel} -resolved transmission $\mathcal{T}(\mathbf{k}^{\parallel}, E_f)$, shows that the main contribution comes from transverse wave vectors close to zero. This is similar to what is obtained in DFT + Landauer simulations of Fe/MgO/Fe magnetic tunnel junctions with parallel magnetizations [3]. The decay rate of the conductance with the MgO thickness is also in very good agreement with Ref. [3]. The decay is associated to evanescent states in the gap of MgO, discussed in Appendix C. These states have Δ_1 symmetry at $\mathbf{k}^{\parallel} = \mathbf{0}$ [3]. The first conduction band of MgO has the same symmetry. However, the conduction band edge, which is expected to be at about 2.5 eV above E_f , is not visible on the transmission plot. This is due to the transition, at $E > E_f + 1.6$ eV, to an Ag band with a different symmetry, which cannot be transmitted

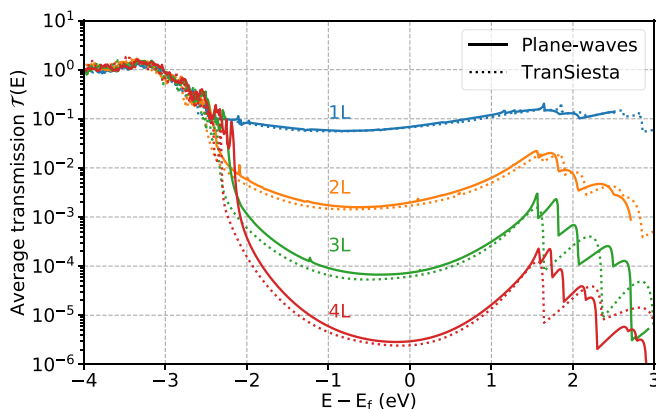


FIG. 3. Transmission spectra $\mathcal{T}(E)$ through MgO barriers of different thicknesses, from 1 cubic layer (1L) to 4 cubic layers (4L). The calculations are done in the DFT-PBE approximation. The results obtained by the plane-wave/Wannier method are compared to those obtained by TRANSIESTA.

through the Δ_1 states of MgO. This symmetry analysis is detailed in Appendix D.

B. Effect of MB corrections on the tunneling transmission

Figure 4 shows how G_0W_0 , self-consistent COHSEX (simply referred as COHSEX in this section) and HSE modify the DFT transmission function, for the four structures with increasing MgO thickness, from 1 to 4 cubic layers. For the lowest transmission spectra, that is HSE and COHSEX applied to the thickest MgO structure, the long-range Hamiltonian couplings were discarded by applying a cutoff distance $L_{\text{cut}} = 13$ Å. This has eliminated some moderate numerical noise occurring at these very low tunnel transmissions below 10^{-7} . This point is detailed in Appendix A.

We expect to observe a reduction of the transmission spectra with respect to the DFT ones. This is confirmed for COHSEX and HSE, which for the 3 and 4 MgO structures reduce the $\mathcal{T}(E_f)$ value of more than one order of magnitude. For a more complete analysis it is interesting to compare our results to the experimental results of Gangineni *et al.* [5]. In this work, measurements of the tunneling conductance have been performed on Fe/MgO/Fe junctions at different MgO thicknesses, up to four cubic cells. The experimental conductances for parallel magnetizations of the Fe electrodes have been then compared to the theoretical values obtained by Butler *et al.* [3] with the DFT + Landauer approach. For 4 MgO cubic cells, the deviation between experiment and theory turns out to be between one and two orders of magnitude (Fig. 3 of Ref. [5]). Similar results were also obtained by Yuasa *et al.* [51]. This is comparable to the deviation observed in our Ag/4 MgO/Ag system between DFT and COHSEX or HSE. It indicates that the correction introduced by COHSEX and HSE goes in the right direction to improve the agreement with experiments. This comparison is qualitative since the electrodes considered in the experiment are made of Fe. But, it remains physically relevant since, for both Ag electrodes and Fe electrodes with parallel magnetizations, the exponential decay of the conductance with the MgO thickness is related to evanescent states of symmetry Δ_1 in MgO.

The values of zero-bias conductance (at zero temperature), that is $\mathcal{T}(E_f)$, are shown in Table I for the four structures and four approximations. Figure 5 shows that the decay with the MgO thickness is exponential, with a net separation between DFT/ G_0W_0 and HSE/COHSEX. For DFT the decay rate is very close to what was found in Ref. [3]. We have

TABLE I. Zero-bias tunneling conductance (in $\Omega^{-1} \mu\text{m}^{-2}$) through a MgO barrier of different thickness, from 1 to 4 cubic cells, with Ag electrodes, as calculated by various approximations. The conductances are evaluated at zero temperature by Eq. (17). Their values at room temperature, not given here, do not differ by more than a few percent.

Method	1 MgO	2 MgO	3 MgO	4 MgO
DFT-PBE	31	8.9×10^{-1}	3.3×10^{-2}	1.5×10^{-3}
PBE + G_0W_0	27	5.8×10^{-1}	2.3×10^{-2}	1.1×10^{-3}
COHSEX	14	1.6×10^{-1}	2.6×10^{-3}	3.9×10^{-5}
HSE	13	1.6×10^{-1}	2.7×10^{-3}	4.7×10^{-5}

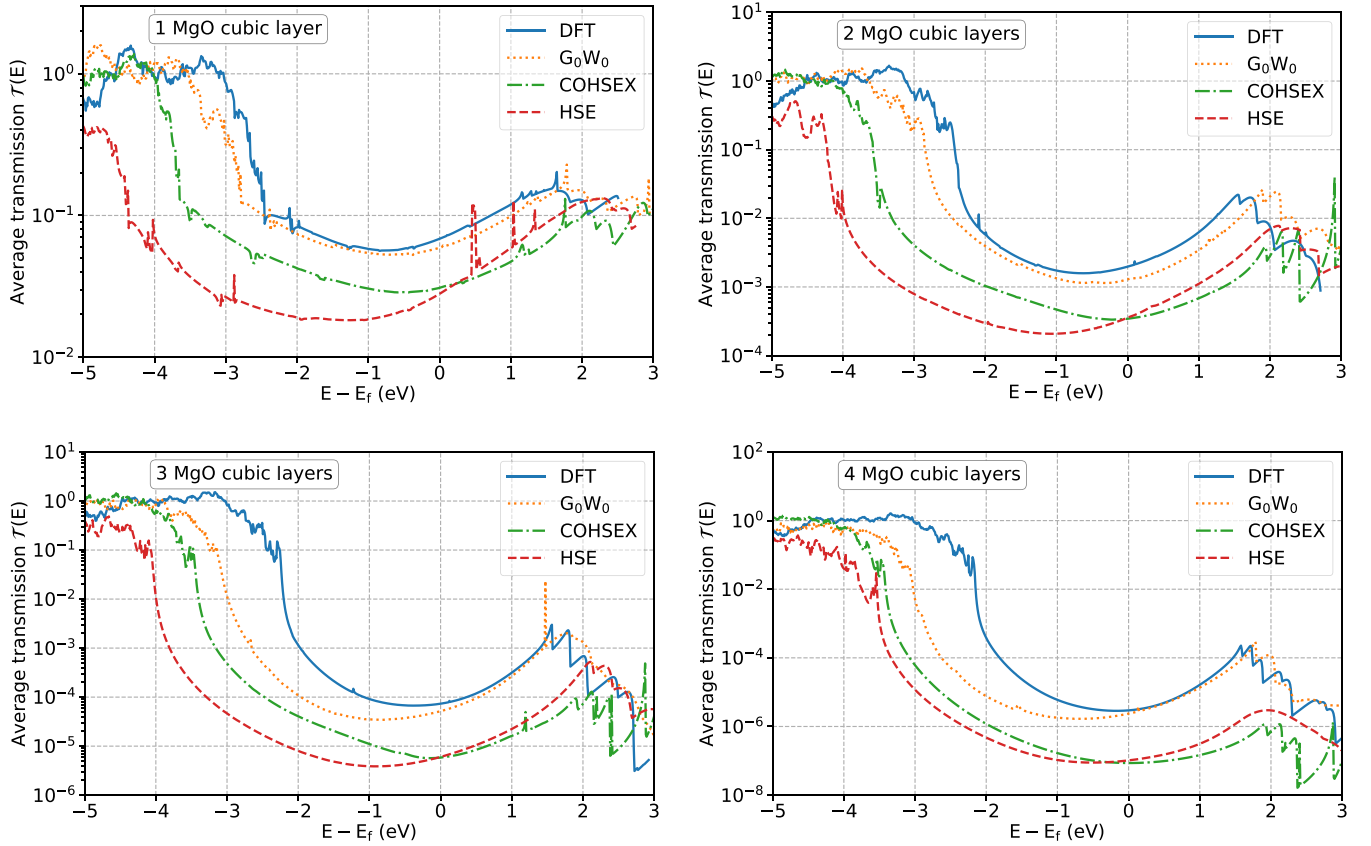


FIG. 4. Transmission spectra calculated by various approximations, for different MgO thicknesses (1 to 4 cubic layers). All the G_0W_0 transmission functions, and the HSE and COHSEX ones for the thickest structure (4 MgO), are calculated by applying a Hamiltonian cutoff distance L_{cut} of 13 Å (see Sec. II G and Appendix A).

$\mathcal{G} \propto \exp(-2\kappa a \times n_{\text{MgO}})$, where n_{MgO} is the number of MgO cubic cells and $2\kappa a \simeq 3.3$. κ is related to the decay rate of evanescent wave functions in MgO, and a is the lattice constant of MgO. $2\kappa a$ increases for HSE and COHSEX to values around 4.2. This entails that the overestimation error of the DFT + Landauer approach becomes more important in

higher tunneling regimes. The decay rate obtained in HSE and COHSEX ($2\kappa a \simeq 4.2$) is also in good agreement with the rate obtained for the A sample in Ref. [5]. On the contrary, the decay rate obtained in DFT ($2\kappa a \simeq 3.3$) is closer to the B sample (Fig. 3 of Ref. [5]). A comparison of the decay rates with the ones obtained from the complex band structure of bulk MgO is performed in Appendix C.

The fact that G_0W_0 does not provide a significant reduction of transmission and conductance (Figs. 4 and 5) leads to another interesting analysis. The DFT systematical underestimation of the insulators' band gap [20] is suspected to be the main cause of the overestimation of the tunneling transmission. This is inferred by assuming that the band offsets between the Fermi level E_f of the electrodes and the valence and conduction band edges of MgO are both underestimated by DFT. This underestimation of the energy barriers should lead to an overestimation of tunneling. MB corrections on eigenvalues are thus expected to give more accurate conductance values. Table II shows the electronic band gap of bulk MgO calculated in different approximations: DFT-PBE, G_0W_0 , COHSEX, and HSE. G_0W_0 gives a band gap close to the experimental values, whereas COHSEX, as expected, overestimates the band gap. Our observation is that the decrease of the tunneling transmission is not simply correlated to the opening of the MgO band gap. In the G_0W_0 approximation, the zero-bias conductances remain close to the DFT values, despite the band-gap opening from 4.72 to 7.44 eV. The HSE

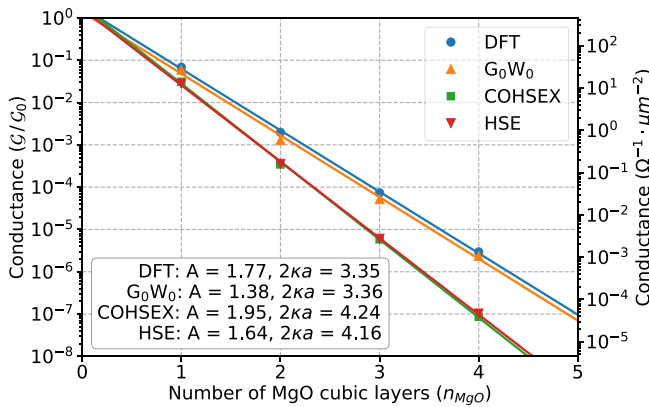


FIG. 5. Values of Table I in logarithmic scale with respect to the number of MgO layers in the central region. The left y axis shows values in unit of $G_0 = 7.75 \times 10^{-5} \Omega^{-1}$, that is $\mathcal{T}(E_f)$, while the right y axis shows values in $\Omega^{-1} \mu\text{m}^{-2}$. The straight lines are linear regressions on the data logarithm. Therefore, the conductance goes as $\mathcal{G} = A \exp(-2\kappa a \times n_{\text{MgO}})$. The fit parameters are also shown.

TABLE II. Electronic band-gap of bulk MgO, calculated by various approximations. The lattice parameter equals 4.212 Å, which is the experimental value at room temperature [52]. Values are in eV.

Method	This work	Other works
DFT-PBE	4.72	4.68 [53]; 4.45 [54]
PBE + G_0W_0	7.44	7.08 [53]; 7.41 [55]
COHSEX	9.37	
HSE	7.77	7.67 [45]
Experimental		7.67–7.83 [45]

approximation gives similar gap opening but a smaller transmission. The COHSEX approximation gives conductances very close to the HSE ones, while the band gap is much larger. The band offset between E_f and the VB edge of MgO is also not simply correlated to the band-gap opening. In particular, the offset is larger in HSE than in COHSEX. The HSE offset is around 4 eV, which is close to the experimental value obtained by scanning tunneling spectroscopy on thin MgO layers deposited on an Ag substrate [33].

These results point to the fact that it is not the correction of the band gap and energies which drives the reduction of the zero-bias conductance, but rather the correction of wave functions. Indeed, G_0W_0 , which keeps the Kohn-Sham eigenfunctions unmodified, does not provide any significant correction to the DFT zero-bias conductance, while HSE and COHSEX, which update also eigenfunctions, provide significant and similar corrections to the zero-bias conductance, despite the different MgO band gap. Figure 6, which shows how DFT eigenvalues of the 4 Ag/1 MgO/4 Ag supercell are modified by the different MB corrections, also supports this argument. Eigenvalues close to the Fermi energy correspond to wave functions mainly located in Ag, with evanescent tails in MgO. Eigenvalues of a metal, which form a continuous spectrum, are not very sensitive to QP corrections, and remain almost unmodified with respect to DFT. Modifications occur only far away from the Fermi energy and for Bloch states with contributions which start to come from Mg and O electrons. This means that a change in the transmission function around the Fermi energy is necessarily caused by the modification of eigenfunctions. This follows by the fact that the trace formula

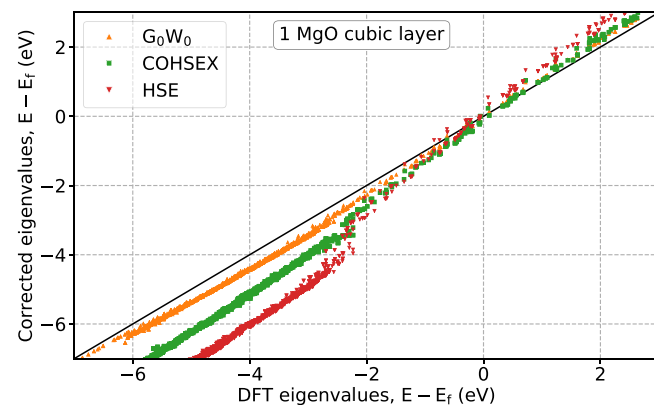


FIG. 6. Quasiparticle energies as function of the DFT-PBE eigenvalues shown for the 4 Ag/1 MgO/4 Ag structure.

(15) used to compute the transmission is local in energy. Indeed, the transmission $\mathcal{T}(E)$ only depends on the Green's functions $G(E)$. But, the Green's functions for DFT and G_0W_0 can be written as

$$G^{\text{DFT}}(E) = \sum_m \frac{|\psi_m^{\text{DFT}}\rangle\langle\psi_m^{\text{DFT}}|}{E - \epsilon_m^{\text{DFT}}}, \quad (18)$$

$$G^{G_0W_0}(E) = \sum_m \frac{|\psi_m^{\text{DFT}}\rangle\langle\psi_m^{\text{DFT}}|}{E - \epsilon_m^{G_0W_0}}, \quad (19)$$

that is, the wave functions ψ_m are kept at the level of DFT and only the eigenvalues ϵ_m are updated. Now, the Green's function at $E = E_f$ only depends on the poles/eigenvalues ϵ_j close to E_f . If G_0W_0 does not introduce significant corrections to these eigenvalues, as Fig. 6 shows, then $G^{G_0W_0}(E_f) \simeq G^{\text{DFT}}(E_f)$. Therefore, the G_0W_0 zero-bias conductance cannot be very much different from the DFT one. Only with a Green's function where also the wave functions are updated, one might expect that, even if the eigenvalues close to E_f are substantially uncorrected, the wave functions can significantly change the Green's function.

This argument can be formulated in an alternative manner. The transmission at energy E can be obtained by building diffusion eigenstates made of incident, reflected, and transmitted waves. These states are linear combinations of the *ab initio* Bloch eigenfunctions at energy E . Hence, a modification of these wave functions is needed to modify the DFT transmission close to E_f since eigenvalues remain basically unmodified.

A final comment is worth on the comparison between COHSEX and HSE. The agreement of HSE with COHSEX on the zero-bias conductance shown in Fig. 5 and Table I might be fortuitous. Indeed, COHSEX and HSE differ on all other quantities, e.g., eigenvalues, band gaps, so that it looks unlikely that HSE and COHSEX could provide the same eigenfunctions, even those located at the Fermi energy.

IV. CONCLUSION

The tunneling transmission spectra and zero-bias conductances of Ag/MgO/Ag junctions have been computed using DFT-based *ab initio* calculations. A methodology combining plane-wave DFT and transformation to a Wannier basis set has been used to compute the quantum transmission. Since DFT systematically underestimates the band gap of insulators, it is expected that the tunneling transmission in the coherent regime is overestimated. This should be improved by MB corrections. For this purpose, the impact of different MB corrections to DFT has been evaluated. Our conclusion is that MB corrections of energies and band offsets have nearly no impact on the zero-bias conductance if the DFT eigenfunctions are not updated. The conductance is significantly reduced only if the eigenfunctions are updated in the MB correction scheme. Ferretti *et al.* [50] gave a similar conclusion about the decay lengths of evanescent states in the band gap of conjugated polymers. Here, we have reinforced this conclusion by evaluating MB corrections on a bulk tunneling heterojunction. Indirect comparison of our simulations with experiments (Gangineni *et al.* [5]) indicate that MB corrections go toward more accurate tunneling conductances.

HSE and self-consistent COHSEX seem the most practical options for performing MB corrections of the tunneling transmission since these corrections are available in many DFT codes. Self-consistent GW would be in principle more accurate but it is more computationally demanding. An interesting but ambitious perspective would be to include MB corrections directly inside the nonequilibrium Green's functions (NEGF) formalism, starting from a DFT Hamiltonian in a localized basis set (Wannier functions or atomic orbitals). This should correct the band gap and zero-bias conductance, and would allow considering finite-bias voltages and electron-phonon interaction.

The plane-waves Wannier methodology used in this work is applicable to larger supercells, with transverse dimensions up to about 1.5×1.5 nm, in the DFT-PBE and HSE approximations. Beyond this size, we reach the limits of *ab initio* calculations and also of transport simulations, which scales to the third power of each transverse dimension. Such supercells are sufficient to study, e.g., the impact of a point defect or of a conducting filament on the electron transmission through the oxide layer.

APPENDIX A: ACCURACY OF THE WANNIER HAMILTONIAN AND CUTOFF DISTANCE

During the first tests of the plane-wave/Wannier methodology, we used a $1 \times 4 \times 4$ MP grid in the *ab initio* calculations. Using a single \mathbf{k} point Γ along the transport direction seemed sufficient, given the long length of the considered supercells. However, for the thickest oxide, we have encountered accuracy issues in transport calculations. Figure 7 shows the DFT transmission spectra obtained with different values of the cutoff distance L_{cut} . The couplings at distances around 20 \AA strongly modify the tunneling transmission, and there is no evident justification for discarding them. The problem was solved by using a $2 \times 4 \times 4$ MP grid. Figure 7 shows that the DFT transmission spectrum is then nearly insensitive to the cutoff. This proves that the couplings at distances beyond

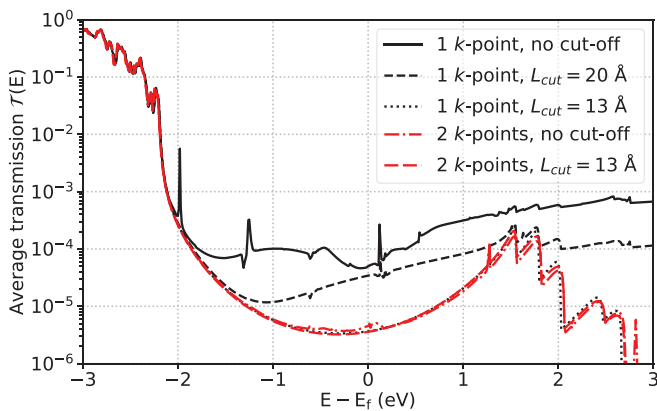


FIG. 7. Transmission spectrum of the Ag/4 MgO/Ag structure in DFT-PBE, using the plane-wave/Wannier method. If a single \mathbf{k} point is used along the transport direction, the spectrum depends on the cutoff distance L_{cut} . If two \mathbf{k} points are used, the spectrum becomes nearly independent on L_{cut} down to $\sim 13 \text{ \AA}$. Moreover, the spectra with one or two \mathbf{k} points are nearly identical at $L_{\text{cut}} = 13 \text{ \AA}$.

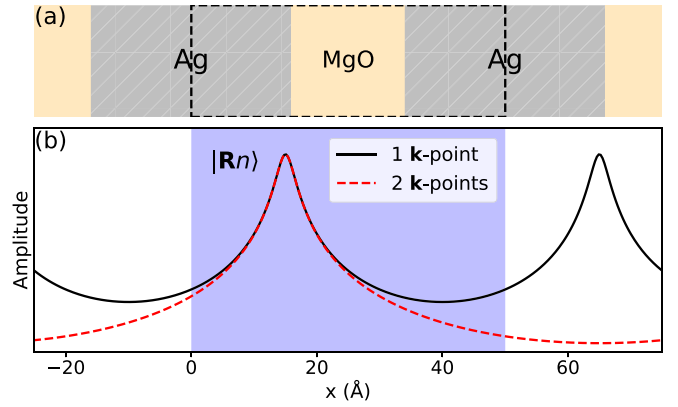


FIG. 8. (a) 4 Ag/4 MgO/4 Ag supercell, delimited by a dashed line, and portions of its periodic replicas. (b) Sketch of a Wannier function computed with one and two \mathbf{k} points along the transport direction (log scale). By using one single \mathbf{k} point, the period of the Wannier function equals the supercell length L . The Hamiltonian matrix element between the two functions is impacted by the tails of the periodic replicas, leading to an overestimate of the direct coupling between Ag electrodes. By using two \mathbf{k} points, the Wannier replicas are moved away at distance $2L$ (not shown here) and have much less influence.

13 \AA have negligible impact on the transmission and can be safely discarded.

The explanation is that the distant couplings are impacted by the periodicity of the Wannier functions along the transport direction. When using a single \mathbf{k} point, this period equals the length L of the supercell, and the influence of the replicas can be strong, as illustrated in Fig. 8. When using two \mathbf{k} points, the period of the Wannier functions is $2L$ and the periodic replicas have much less impact. The coupling of the Wannier function $|\mathbf{R}_n\rangle$ in Fig. 8(b) with another function $|\mathbf{R}'_n\rangle$ is defined as an integral over the ES. Hence, in the one \mathbf{k} -point case, the coupling calculation requires to integrate the black plain line over the blue area in Fig. 8(b), whereas it requires to integrate the red dashed line over the whole x -axis range when using two \mathbf{k} points. It is evident that, in the first case, the impact of the closer periodic replicas leads to an overestimation of the coupling. This overestimation can be negligible for strong, short-distance couplings, but dominant for weak, long-distance ones.

This interpretation is supported by Fig. 9, which shows the decrease of Ag-Ag DFT Hamiltonian couplings with the distance between Wannier centers. This is the same analysis as in Fig. 2, but restricted to Wannier functions belonging to the Ag electrodes. The couplings beyond 17 \AA are direct tunneling Ag-Ag couplings through MgO. These couplings, which are expected to be very weak, are much larger with one \mathbf{k} point than with two \mathbf{k} points. This overestimation when using one \mathbf{k} point is due to the effect of replicas, which dominates the true, physical, weak couplings. On the contrary, for short-distance strong Ag-Ag couplings inside the electrode ($< 17 \text{ \AA}$), the effect of replicas is negligible. The overestimated direct Ag-Ag couplings beyond 17 \AA are nonphysical, and introduce some noise in the transmission spectrum.

Hence, to ensure a good accuracy, we have performed all *ab initio* calculations of this study with a $2 \times 4 \times 4$ MP

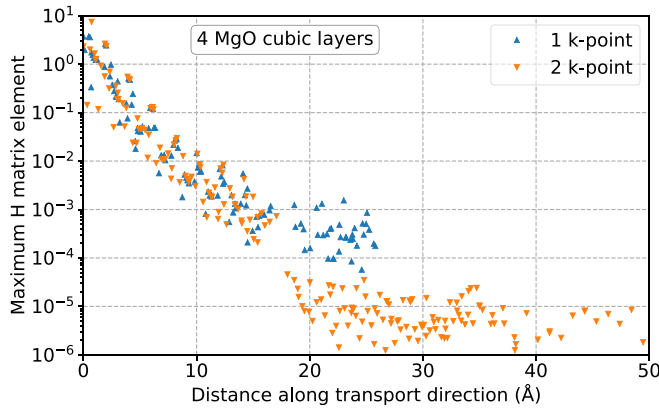


FIG. 9. Decay of the Hamiltonian couplings between Ag Wannier functions with the distance. The calculation is done on a 4 Ag/4 MgO/4 Ag supercell in the DFT-PBE approximation, using either one or two \mathbf{k} points along the transport direction.

grid. In the DFT-PBE, HSE, and self-consistent COHSEX approximations, the transmission is nearly insensitive to an increase of L_{cut} beyond 13 Å. Only for the thickest oxide, where Ag-Ag direct couplings are extremely weak, we observe small fluctuations in the tunneling transmission when L_{cut} approaches the maximum coupling distance $L \simeq 50$ Å. Such fluctuations are visible in Fig. 7, when using two \mathbf{k} points and no cutoff. These very distant couplings are related to the periodicity $2L$ of the Wannier functions and must be discarded. Hence, we have used a cutoff distance of 13 Å to suppress these fluctuations when necessary. This cutoff distance is shorter than the MgO thickness, thus, all the Ag-Ag couplings through MgO are forced to zero.

Using two \mathbf{k} points does not solve the problem of long-range interactions in the G_0W_0 approximation. As discussed in Sec. II G, these interactions are intrinsic to the method.

APPENDIX B: EFFECT OF A G_0W_0 -LIKE CORRECTION ON A 1D TIGHT-BINDING MODEL

We consider the 1D, two-band, tight-binding model considered by Tomfohr and Sankey [56]. It is an infinite 1D pe-

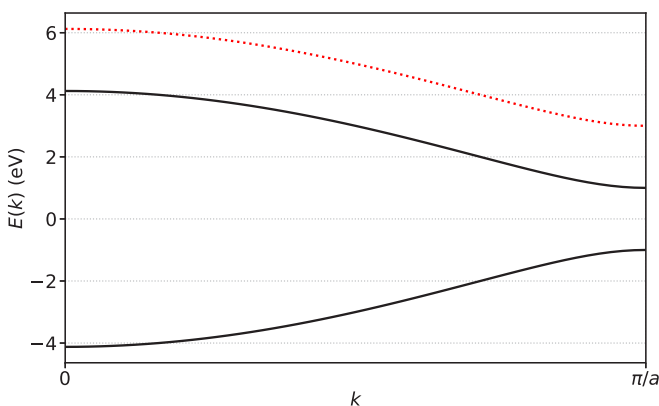


FIG. 10. Black lines: Band structure of the 1D tight-binding model (see text). Red dotted line: Rigid shift of the conduction band after application of a scissor operator of +2 eV.

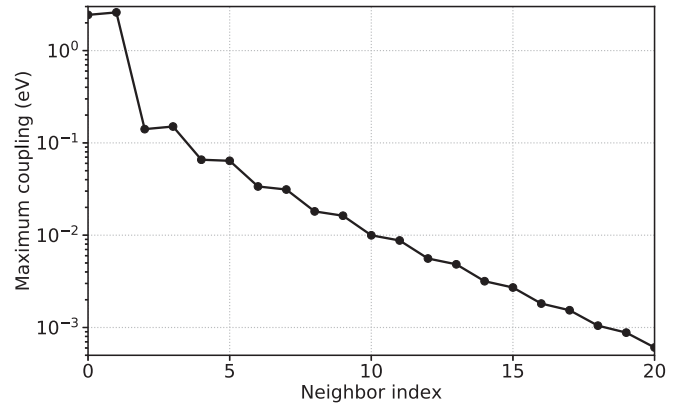


FIG. 11. Maximum modulus of the Hamiltonian matrix element vs distance between orbitals, after application of the scissor operator in Bloch space. See model parameters in the main text.

riodic chain with alternating A and B orbitals, onsite energies E_A and E_B , and nearest-neighbor coupling $-t$ between A and B . The band structure is given by

$$E(k) = \Sigma \pm \sqrt{\Delta^2 + 2t^2[1 + \cos(ka)]}, \quad (\text{B1})$$

where $\Sigma = (E_A + E_B)/2$, $\Delta = (E_B - E_A)/2$, and a is the lattice constant. Figure 10 shows the band structure for $E_A = -1$ eV, $E_B = 1$ eV, $t = 2$ eV. It also shows the band structure after application of a “scissor operator” which rigidly shifts the conduction band by +2 eV.

Keeping the Bloch wave functions unchanged, and just modifying the energies by the scissor operator, we have recomputed the Hamiltonian in the tight-binding basis. Figure 11 shows the decay of the new Hamiltonian matrix elements with the distance between orbitals. We see couplings above 10^{-2} eV up to the 10th neighbor, while the original Hamiltonian was limited to nearest-neighbor couplings.

This scissor operator is analogous to a G_0W_0 correction, where only the eigenvalues are corrected. This simple model illustrates how an operator which is diagonal in Bloch space can increase the range of the Hamiltonian in a basis of localized orbitals. This may explain the long-range couplings of the G_0W_0 Hamiltonian in Fig. 2. Ferretti *et al.* found a similar behavior on a different tight-binding model [50].

APPENDIX C: CONDUCTANCE DECAY RATE FROM BULK MgO COMPLEX BAND STRUCTURE

Figure 12 shows the complex band structure (CBS) of bulk MgO within the four considered approximations. It was computed in the Wannier basis, for a transverse wave vector $\mathbf{k}^{\parallel} = 0$, with an exponential decay of the wave functions along the transport direction: $\exp(-\kappa an)$, where a is the lattice constant and n indexes the cubic cell. The couplings beyond third-nearest-neighboring cubic cells are neglected along the transport direction. The calculation of the CBS involves a quadratic eigenvalue problem. It is solved by transforming it into a generalized eigenvalue problem with doubled dimension [57,58].

The CBS can be used to infer the decay rate of the tunneling conductance of a junction composed by n MgO cubic cells

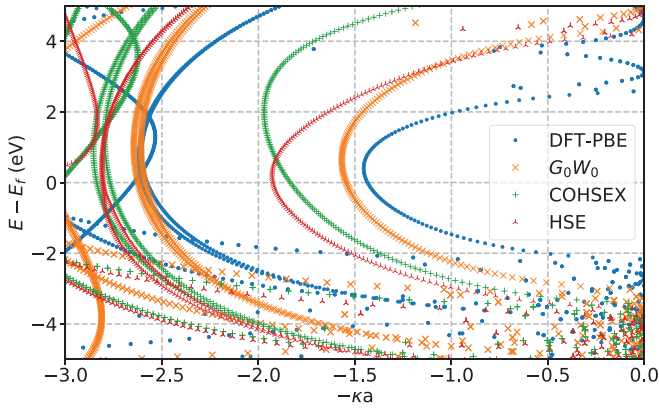


FIG. 12. Complex band structure of bulk MgO calculated at $\mathbf{k}^{\parallel} = 0$ within the four considered approximations. κ is the decay rate of the evanescent wave functions and a is the lattice constant. For each approximation, the difference between the Fermi level and the valence band edge is determined from the transmission spectrum of the Ag/4 MgO/Ag structure (Fig. 4).

between two electrodes, when n increases: $\mathcal{G} \propto \exp(-2\kappa an)$. The factor 2 comes from the fact that the tunneling probability is proportional to the square modulus of the evanescent state. In the MgO band gap, the evanescent states with the slowest decay (i.e., smaller κ) have the same symmetry as the states of the Ag electrodes at the Fermi energy (see Appendix D for details). Hence, the decay rate of the conductance is related to the smallest value of κ at the Fermi energy E_f . However, the position of E_f depends on the band alignment between Ag and MgO. In Fig. 12, we have defined the Fermi level from the band alignment of the thickest structure (Ag/4 MgO/Ag): For each approximation, we have extracted the difference between E_f and the valence band edge from Fig. 4, and reported it in Fig. 12.

Table III shows the values of $2\kappa a$ extracted from the CBS compared to the ones extracted from the transmission spectra of the Ag/MgO/Ag junctions at $\mathbf{k}^{\parallel} = 0$. The values obtained by the two methods are reasonably consistent. The separation between DFT and G_0W_0 on one hand, and COHSEX and HSE on the other hand, is confirmed. Some differences may arise from the presence of the Ag/MgO interface when computing κ from the transmission spectra. It is not surprising that the decay factor of a junction is dependent on the material the electrodes are made of. Thus, we do not expect to find exactly the same values, especially for thin structures as the ones considered here, where the bulk properties of MgO are surely influenced by the presence of the Ag electrodes. Moreover, the offset between the Fermi level of Ag and the

TABLE III. $2\kappa a$ values extracted from the CBS of bulk MgO, and from the transmission functions of Ag/MgO/Ag junctions of different thickness, at $\mathbf{k}^{\parallel} = 0$. The values are computed within the four approximations considered in this work.

Method	DFT	G_0W_0	COHSEX	HSE
CBS	2.87	3.09	3.68	3.85
Transmission	2.73	2.84	3.78	3.62

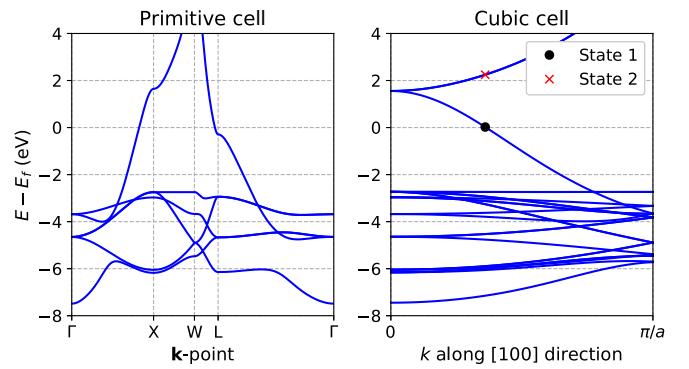


FIG. 13. DFT-PBE band structure of bulk Ag, either computed in the primitive cell, or in the cubic cell along the [100] direction ($\mathbf{k}^{\parallel} = 0$). a is the lattice parameter.

valence band edge of MgO depends on the MgO thickness, as visible in Fig. 4. Taking this into account would shift the CBS curves along the energy axis in Fig. 12 and give slightly different values of κ for each thickness.

APPENDIX D: SYMMETRY MISMATCH BETWEEN Ag AND MgO BLOCH FUNCTIONS AT THE CONDUCTION BAND EDGE

This Appendix details why the conduction band edge cannot be determined from the transmission spectra in Figs. 3 and 4. The DFT-PBE band structure of bulk Ag is shown in Fig. 13. It is computed either in the primitive cell, or in the cubic cell at $\mathbf{k}^{\parallel} = 0$ and with the longitudinal wave vector $k^{\perp} \in [0, \pi/a]$, where a is the lattice constant. The latter shows two different bands joining at Γ at $E \simeq E_f + 1.6$ eV. The upper band is actually the folding of XW paths in the first Brillouin zone of the primitive cell, with X located along the

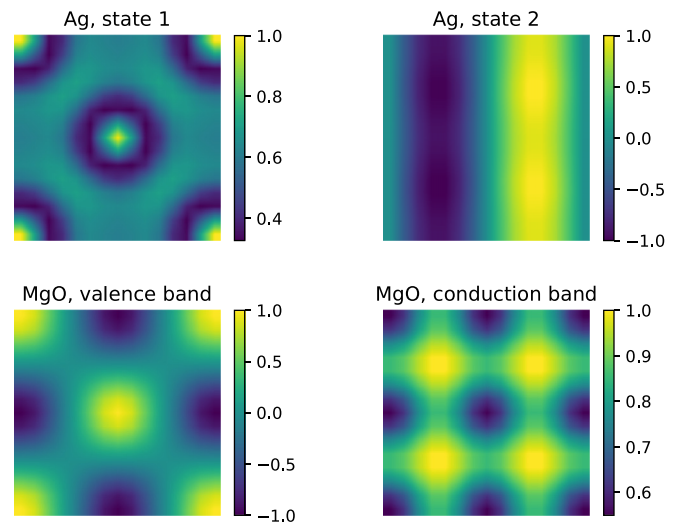


FIG. 14. Color maps of some Bloch wave functions at $\mathbf{k}^{\parallel} = 0$ in a (xy) slice of the cubic cell. State labeled 1 on the band structure plot (Fig. 13) has symmetry Δ_1 while state labeled 2 has symmetry Δ_2 (it is doubly degenerate, the other one having mirror symmetry along the horizontal axis). The highest valence states and lowest conduction states of MgO both have Δ_1 symmetry.

transverse directions [010] and [001]. These X points fold to Γ when considering the cubic cell instead of the primitive one.

Figure 14 shows a symmetry mismatch between the upper band of Ag and the conduction band of MgO. Color maps of the Bloch wave functions show that the lower band has symmetry Δ_1 , the same as the states of MgO, while the

upper band has symmetry Δ_2 . Hence, at the conduction band edge of MgO, which is well above $E_f + 1.6$ eV even in the DFT case, the Ag states cannot be transmitted through the conduction states of MgO. They are probably transmitted by tunneling through evanescent states visible in the complex band structure of MgO (Fig. 12).

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