

On the key role of electrolyte-electrode van der Waals interactions in the simulation of ionic liquids-based supercapacitors

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The performance of supercapacitors is governed by the structure and dynamics of ions at the solid/liquid interface. At the molecular scale, these properties result from a subtle combination of electrolyte–electrolyte and electrolyte–electrode interactions. Although the former are well captured by conventional force fields, validated against experiments, the latter are much more difficult to parameterize accurately. In this work, by using constant potential classical molecular dynamics, we investigate the effect of the strength of the electrode-electrolyte van der Waals interactions on the interfacial properties for a system composed of the 1-ethyl-3-methylimidazolium bis(trifluoromethylsulfonyl)imide ionic liquid and a graphite electrode. We show that stronger van der Waals interactions lead to a decrease in the exchange of co-ions by counter-ions with the increase of potential difference and, thus, to a lower capacitance of the devices. The ion exchange dynamics is strongly affected, but the charging rate remains constant over the whole range of studied parameters. This study emphasizes the need for a careful parameterization of force fields for electrode materials in future classical molecular dynamics studies.

I. INTRODUCTION

Supercapacitors (SCs) are electrochemical energy storage devices that operate by adsorption and reorganization of ions from an electrolyte on the electrode surface.¹ SCs exhibit high power density and long cycle life, but lower energy density than batteries.² The two devices can complement each other since they are used in different applications. Several experimental and theoretical studies have been conducted over the years to increase the energy density stored in SCs.

In order to obtain devices with both high energy and power density, a deep understanding of the electrode–electrolyte interface at a molecular scale, complementing electrochemical experiments, is required. In this respect, molecular dynamics (MD) simulations appear as a promising tool. In particular, classical MD simulations are employed in the case of SCs because they allow to simulate large systems ($> 10,000$ atoms) for long times (several nanoseconds).^{3–5} One of the crucial aspect of classical molecular dynamics is the force field used to describe the electrolyte–electrolyte and electrode–electrolyte interactions. This force field has to be carefully chosen in order to accurately account for the complex interactions in the system and produce realistic structural and dynamical properties of the interface.

For the bulk electrolytes, generic force fields such as the ones developed by Canongia Lopes, Pádua and co-workers for Ionic Liquids (ILs)^{6–8} were shown to reproduce accurately the structure and thermodynamics of the

system. The dynamical properties are generally more difficult to capture, a problem that could be solved by introducing rescaled charges⁹ or polarization effects.^{8,10} The interactions between the electrolyte and the electrode are less well known and studied, despite their importance for accurately determining the physical properties of the interface, but the same force fields are generally used without further reparameterization.^{11–14}

However, previous simulations have shown that modifying the short-range water-carbon interaction energy changes the contact angle of a water droplet on a graphite surface,¹⁵ and similar results have been found for ILs on graphene.¹⁶ Other studies have shown that the van der Waals (vdW) strength modulates the structure of the electrochemical double layer (EDL), as well as the capacitance of aqueous electrolytes or pure ILs in contact with planar electrodes.^{17–19} In particular, Yang *et al.* have found a non-monotonic evolution of the capacitance when increasing the strength of the ion–electrode attraction for an aqueous electrolyte.¹⁷ Jin *et al.* have observed a decrease of the capacitance when the strength of the ion–electrode short-range interaction is reduced for the BMIM-PF₆ IL at 450 K. However, both studies used constant charges on the electrodes, instead of a more realistic constant potential approach,²⁰ which could lead to different interfacial properties. Kondrat and co-workers have also widely studied the case of so-called “ionophobic” pores, showing that such systems could improve both the energy and the power density of supercapacitors, but their simulations were not explicitly considering carbon materials.^{21,22}

In this work, we employ constant potential classical MD to investigate the effect of the electrode–

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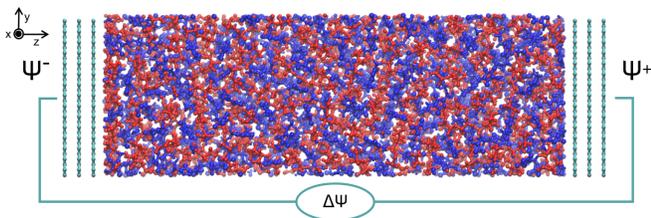


FIG. 1. Snapshot of the simulated system: neat EMIM-TFSI ionic liquid in contact with planar carbon electrodes (electrodes in light green, cations in blue, anions in red).

electrolyte vdW interactions on the capacitance, interfacial structure and dynamics of a neat IL (1-ethyl-3-methylimidazolium bis(trifluoromethylsulfonyl)imide, EMIM-TFSI) in contact with planar carbon electrodes. To focus on ions - electrode interactions, planar electrode have been chosen. Our results show that the effect of the electrode-electrolyte vdW interactions is far from being negligible since all interfacial properties are modified: ion packing, capacitance and ion adsorption dynamics vary noticeably with the vdW interaction strength.

II. METHODS

Constant potential MD simulations of neat EMIM-TFSI between two graphite electrodes have been performed using the MetalWalls software.²³ A representative snapshot of the system is shown in Figure 1. The electrolyte consists in 322 ion pairs and two electrodes made of three rigid parallel graphene sheets separated by 0.34 nm. The box dimensions are $L_x = 3.4$ nm, $L_y = 3.7$ nm and $L_z = 11.2$ nm, with 2D-periodic boundary conditions applied in the x and y directions. In the constant potential method, the carbon atoms of the electrode carry a Gaussian charge distribution of width of 0.40 Å. The value of the charge is allowed to fluctuate in order to meet the constant potential condition.

The all-atom CL&P^{6,24} force field has been adopted to represent EMIM-TFSI. Atomic charges are scaled by a factor of 0.8 in order to mimic polarizable effects, as suggested in previous studies of bulk liquids.^{25–27} VdW interactions are modelled using a Lennard-Jones (LJ) potential, with two parameters for each interaction, ϵ and σ , according to the following equation:

$$U_{ij} = 4\epsilon_{ij} \left[\left(\frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}} \right)^6 \right] \quad (1)$$

The Lorentz-Berthelot mixing rules are used to obtain cross LJ parameters between different atom types.

For the carbon atoms of the electrodes, three sets of LJ parameters are used in this work. The first set of parameters ($\epsilon_{cc} = 0.23$ kJ mol⁻¹, $\sigma_{cc} = 3.37$ Å) is taken from Ref. 28, and we will refer to it as “weak” (interactions)

set. These parameters were adjusted for graphite in contact with a noble gas, and have already been used for previous simulations of supercapacitors.^{29,30} For the two other sets of LJ parameters, σ_{cc} is kept unchanged while ϵ_{cc} is increased to 0.51 kJ mol⁻¹ and 1.00 kJ mol⁻¹, respectively. We will refer to these sets of LJ parameters as “moderate” (interactions) and “strong” (interactions), respectively. Since Lorentz-Berthelot mixing rules are used to calculate the ‘cross’ pair interactions (σ_{ij} and ϵ_{ij}), modifying ϵ_{cc} from one set to another means that all the interactions between the graphene carbon atoms and the electrolyte are modified. Figure 2 shows the resulting LJ potentials for the interaction between the carbon atom of the electrode and the nitrogen atom of the EMIM⁺ cation, as an example.

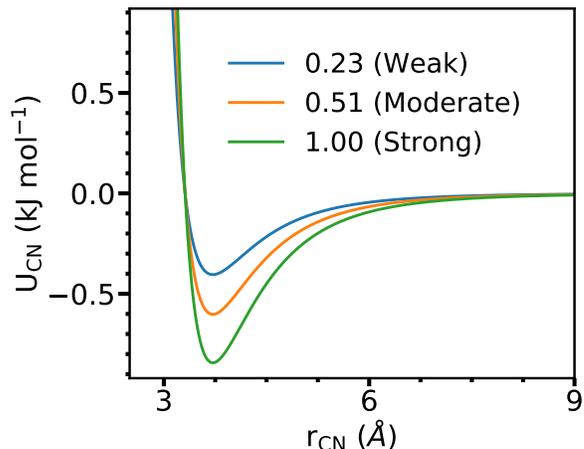


FIG. 2. Lennard-Jones potential curves describing the van der Waals interactions between a carbon atom of the electrode and a nitrogen atom of the EMIM⁺ cation for the three values of ϵ_{cc} studied in this work: 0.23 kJ mol⁻¹ (blue), 0.51 kJ mol⁻¹ (orange) and 1.00 kJ mol⁻¹ (green) .

The starting configuration of the system was generated using the PACKMOL software.³¹ In order to obtain the correct liquid density, the electrodes are allowed to move in the z direction for few nanoseconds using a piston, i.e. by applying a pressure of 0 bar on both sides. The temperature applied is 298 K. When the electrode positions are stabilized, a bulk density of 1.576 g cm⁻³ is reached, very close to the experimental value at ambient temperature.³²

For each set of LJ parameters, the system is charged by applying a potential difference at $t = 0$ of 0 V, 1 V, 2 V and 4 V between the two electrodes. The simulations are performed at such constant applied potential in the NVT ensemble using a timestep of 2 fs. A first equilibration of 8 ns is carried out until the total charge on the electrode reaches a plateau (see Figure 3). This equilibration is followed by a production run of 60 ns. The temperature is set to 298 K, and maintained constant using a Nosé-Hoover thermostat chain of length 5 with a relaxation

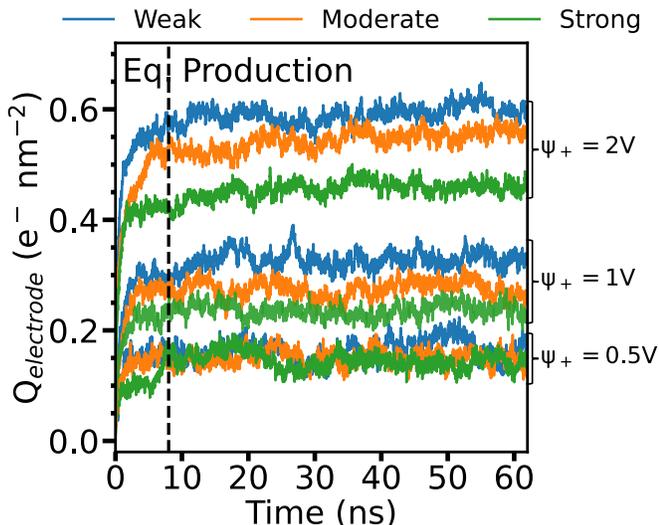


FIG. 3. Time evolution of the total charge. The vertical dashed line shows the transition between the equilibration and the production periods.

time of 500 fs. The cut-off for the vdW interactions is set to 1.48 nm. The Ewald summation method is used to compute long-range interactions, the cut-off distance for real space interactions being of 1.70 nm.

III. RESULTS AND DISCUSSION

To investigate the effect of the carbon–electrolyte vdW interactions on the interfacial properties, we first want to assess the variation of the electrode charge as a function of the applied potential difference. We start by determining the potential profile across the simulation cell for all sets of interactions. This is done along the z direction, perpendicular to the electrode surface (see eq.1 and Figure S1 in SI). This allows us to determine the potential of the bulk liquid, which is used as the reference potential. In the following, $\Delta\Psi = \Psi_{\text{electrode}} - \Psi_{\text{bulk}}$ is defined as the potential drop at each of the interfaces.

Figure 4 displays the total charge at equilibrium on the electrode with respect to $\Delta\Psi$, extracted from the production phase as defined on Figure 3. The strength of the ion–electrode short-range interactions affects the amount of accumulated charge. The average decrease of the total electrode charge when going from $\epsilon_{cc} = 0.23 \text{ kJ mol}^{-1}$ to $\epsilon_{cc} = 0.51 \text{ kJ mol}^{-1}$ is around 11%, and of up to 20% for the larger value of ϵ_{cc} , i.e. 1.00 kJ mol^{-1} . Although the difference looks smaller for the lowest applied potential, this may be attributed to the relatively large error on the potential drop value at such potentials.

The differential capacitance of a single electrode is defined as the derivative of this electrode charge with re-

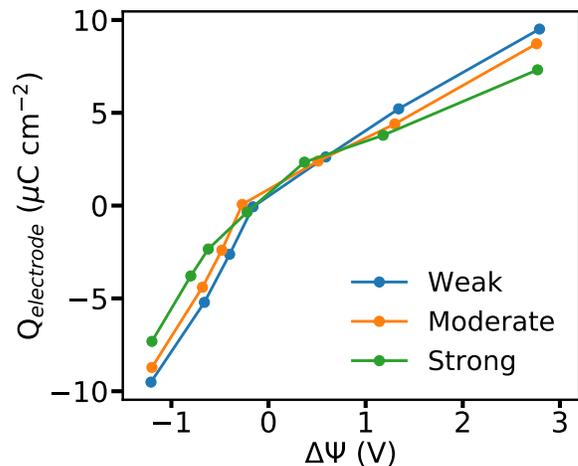


FIG. 4. Total electrode charge as a function of the difference of potential between the electrode and the bulk, for the three sets of ion - electrode vdW interactions. The standard deviations are smaller than the symbols size.

spect to the corresponding potential drop,

$$C_{\text{diff}}(\Delta\Psi) = \frac{\partial Q_{\text{electrode}}}{\partial \Delta\Psi} \quad (2)$$

Although it would be possible to do polynomial fits of the $Q_{\text{electrode}} = f(\Delta\Psi)$ plot, in practice, due to the insufficient number of $\Delta\Psi$ values sampled, it is difficult to extract a value for each point. However, by approximating the curve with two different linear functions for the negative and positive $\Delta\Psi$ values, we can extract average C_{diff}^+ and C_{diff}^- values for the positive and negative electrodes, respectively. These are reported in Table I.

$\epsilon_{CC} \text{ (kJ mol}^{-1}\text{)}$	0.23	0.51	1.00
$C_{\text{diff}}^- \text{ (}\mu\text{F cm}^{-2}\text{)}$	6.9	7.1	5.6
$C_{\text{diff}}^+ \text{ (}\mu\text{F cm}^{-2}\text{)}$	2.4	2.2	1.8

TABLE I. Average differential capacitances on the positive and negative electrode depending on the ϵ_{CC} LJ parameter.

We observe a decrease of the differential capacitance when the LJ parameter becomes stronger. Albeit, the values for weak interactions²⁹, it is difficult to compare properly with experiments since the latter results show important discrepancies: as discussed by Tu and McDaniel³³, the experimental results depend on the measurement method and on the model used to extract the differential capacitance values. However, we note that numbers ranging between 6 and 20 $\mu\text{F cm}^{-2}$ were obtained for planar electrodes and the EMIM-TFSI ionic liquid^{34–37}. The agreement is therefore better for the weaker interaction potential, albeit the numbers obtained for the positive electrode are certainly too low. This points towards the existence of additional interactions between the electrode and the

TFSI anion, and will be the subject of future studies. This result shows that one must use properly parameterized LJ parameters to describe the interactions between the ions and the electrode in order to improve the accuracy of capacitance estimations. In addition, Tu *et al.* have recently shown that accounting for the surface roughness can lead to significant increase of the capacitance due to anion-anion pairing.³⁸ Here we used perfectly flat surfaces, which is probably not the case in experimental studies.

To understand the origin of the variation in the amount of charge stored on the electrode, the number of ions adsorbed at the interface has been determined. An ion is considered adsorbed if at least one of its atoms is closer than 5 Å from the electrode surface. This value is chosen because it corresponds to the distance for which all the ions in contact with the electrode are included but not the ions in the second layer (defined as ions separated from the electrode by at least another ion, see Figure 5). Using such an atom-based criterion is more reliable than selecting the ions only depending on the position of their center of mass, as is usually done,^{39,40} because the latter definition leaves out some ions which only have a small portion in contact with the electrode (Figure S2 in SI).

The top panels of Figure 6 show the evolution of the number of cations and anions adsorbed on the electrode as a function of the electrode potential for the three sets of LJ interaction parameters. In all cases, the charging mechanism observed corresponds mainly to an exchange of co-ions with counter-ions. This means that when the electrode becomes negatively charged, some anions desorb and are replaced by cations, in an approximately equivalent number. The first layer of ions thus

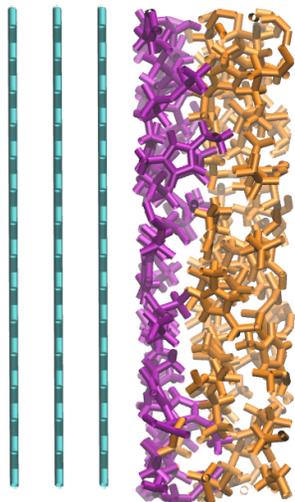


FIG. 5. Snapshot of one configuration of the studied system with a zoom at one interface. Carbon atoms are represented in light blue, adsorbed ions in purple and ions in the other layers in orange.

becomes positively charged, with the total charge on the electrode almost exactly counterbalancing the charge of the electrode. An opposite phenomenon takes place when the electrode becomes positively charged. For the more attractive electrodes, fewer exchanges are detected, i.e. fewer co-ions are replaced by counter-ions leading to the observed reduction of the total charge of the first layer of ions.

In addition to the difference in the number of co-ions and counter-ions exchanged, the strength of the ion–electrode vdW interactions also influences the orientation of the adsorbed species with respect to the surface of the electrode. To characterize this, a representative angle θ is defined for both ions. For the cation, it is the angle between a vector perpendicular to the imidazolium ring plane and the z direction (perpendicular to the electrode surface). For the anion, the angle is defined between the vector connecting the two carbon atoms and the z direction. Figure S3 in SI illustrates the definition of these angles. Following the probability distribution of the angle of the adsorbed ions (Figure S4 in the SI), the cation is considered to be oriented perpendicular when θ is comprised between 45° and 135° , and parallel otherwise. The anion is considered as parallel for angle values in the range 70° - 110° and perpendicular otherwise. This interval allows to take into account angle variations of the anion due to the rotation of the S-N-S-C dihedral, i.e. cis and trans configurations.

Percentages of ions in the perpendicular orientation for all the ion–electrode interactions and all potentials studied are shown in the bottom panels of Figure 6. It is clear from this figure that large re-orientation effects take place when the potential of the electrode is changed. The percentage of cations perpendicular to the electrode decreases for negative potentials and increases for positive potentials. On the contrary, the percentage of anions perpendicular to the electrode increases for negative potentials and decreases for positive ones. This behavior is in agreement with previous theoretical and experimental studies on the same system.^{39,41–43}

Remarkably, the ions orientation is also strongly affected by the strength of the attraction between the ions and the electrode. For all potential differences applied, less ions are oriented perpendicular to the electrode for stronger attractions. This variation in the orientation is more pronounced for the cations. Similarly, for the BMIM–PF₆ IL, Jin *et al.* see more cations oriented parallel to the surface when the force of the interactions between the ions and the electrode is increased at both the positive and negative surfaces.¹⁸ The structure of such systems consists in successive layers of dense fluid, up to a few nanometers, as was evidenced in many studies (see Figure S5 in the SI).^{39,41,42,44,45} For EMIM-TFSI here, the change in orientation leads to an increase in the intensity observed for the first peak in the ion density profiles. This is expected as increasing ϵ_{cc} enhances the attraction between the atoms of the ions and the atoms of the electrode, and a larger number of atoms can be found in

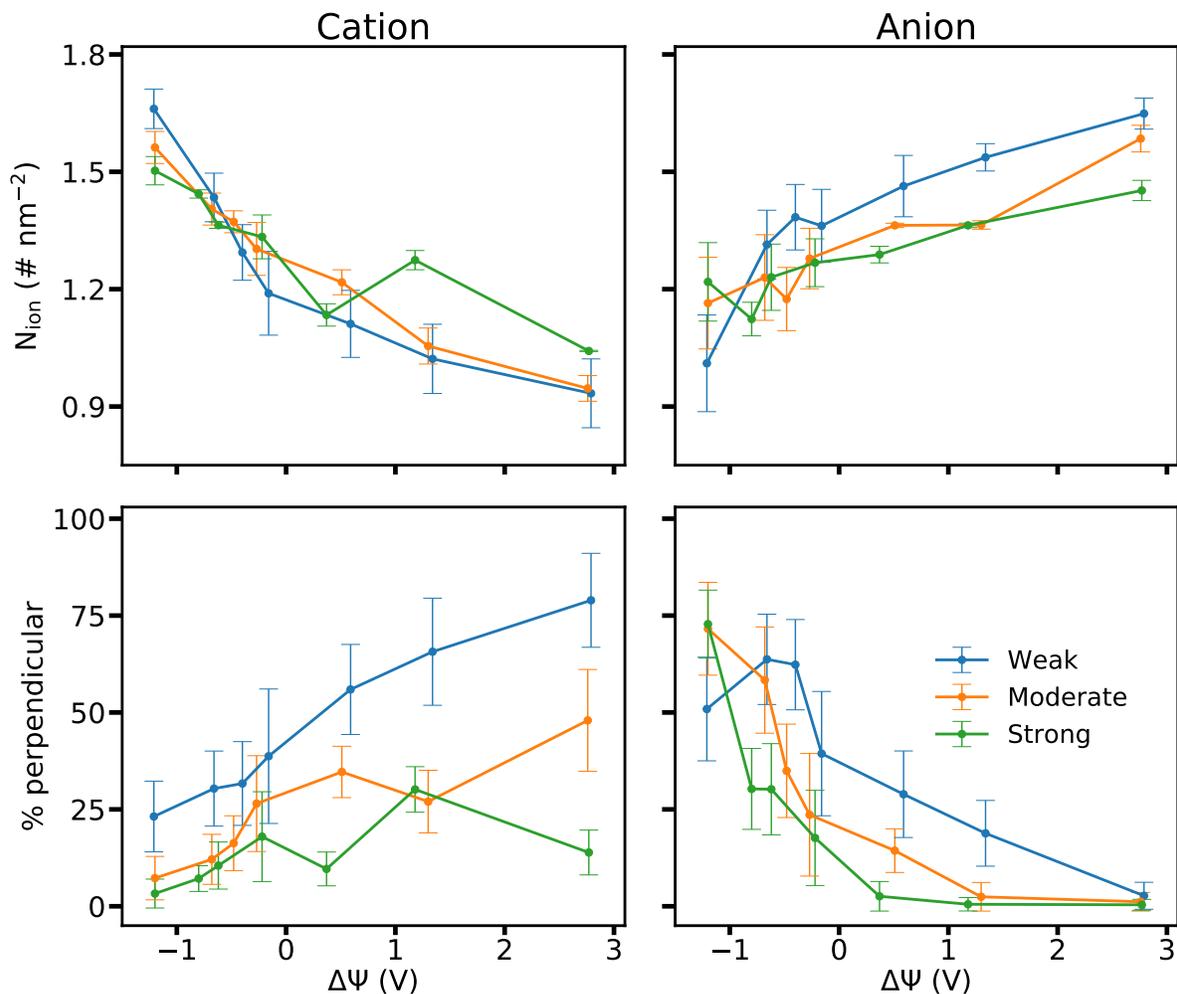


FIG. 6. Top panels: number of cations (left) and anions (right) adsorbed on the electrode per nm^2 as a function of the potential difference between the electrode and the bulk, for the three values of ϵ_{cc} . Bottom panels: percentage of adsorbed cations (left) and anions (right) oriented perpendicular to the electrode with respect to the potential difference between the electrode and the bulk. Error bars shown correspond to the standard deviations.

contact with the electrode if the ions are oriented parallel. It should be noted however that the number of ions parallel to the electrode does not depend only on vdW interactions. It results from a balance between vdW interactions, electrostatic interactions and steric effects.

Surprisingly, the total number of ions adsorbed on the electrode (see Figure S6 in the SI) remains constant, on average, for any value of ϵ_{cc} . This is due to the presence of more ions parallel to the surface, and means that the enhancement of the short-range attraction strength between the ions and the electrode changes the relative balance between electrostatic and steric interactions at the interface.

Apart from the changes in the first layer of ions adsorbed on the electrode surface, it is interesting to see whether modifying the strength of the ions-electrode short-range interactions also affects the layering adopted

by the liquid at longer range. Upon application of a non-zero potential on the electrode, the first layer becomes enriched in counter-ions, while the second one becomes enriched in co-ions and so on, up to typically 3 or 4 layers of liquid depending on the system. Ionic density profiles for anions and cations for applied potential differences of 1 V and 4 V are shown in Figure 7. In the case of the weak interaction potential, the ionic density oscillations at both interfaces are enhanced when the applied potential difference increases. A similar behavior is observed at the negative interface for the moderate and strong interaction sets. Interestingly, it is much less pronounced at the positive electrode. In fact, for the moderate and strong interactions the oscillations remain almost identical independently of the potential at the positive interface. Such results are surprising as short-range vdW interactions vanish after less than a nanometer (see Fig-

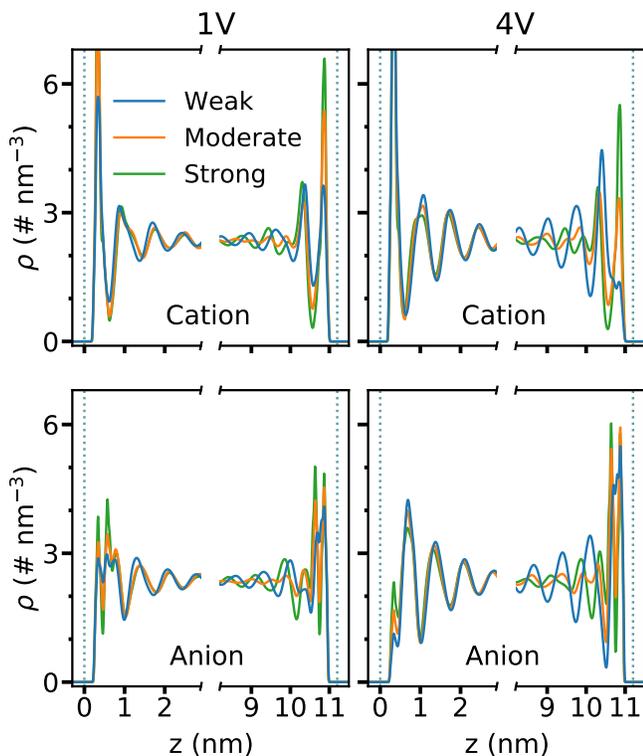


FIG. 7. Ionic density profiles in the direction perpendicular to the electrode (z) for the cations (top panels) and for the anions (bottom panels), for applied potential differences of 1 V (left panels) and 4 V (right panels). The negative electrode is on the left, with the graphite sheet in contact with the electrolyte at $z = 0$ nm. The positive electrode is on the right. See Figure S7 for the same quantities at applied potentials of 0 and 2 V.

ure 2), so they are not expected to perturb ionic densities at a longer range.

The layered structure of the electrolyte at the interface is mostly due to packing constraints, which induce a preferential organization of the ions in terms of orientation. Figure 8 shows the profile of the mean value of $\cos \theta$ along the z axis at 4 V. The oscillations in the orientation profile, which were already observed in previous studies,⁴¹ resemble the oscillations of the ionic density profiles reported in Figure 7, which means that the layers observed correspond to a perturbation in the orientation of the ions due to the interface. When comparing the orientation profiles obtained for the three sets of LJ parameters, one can see that the oscillations in the case of the cations are reduced at the positive interface when the ion–electrode interactions are stronger, while they remain similar at the negative interface. This behavior is similar to the one observed for the density profiles. On the contrary, the orientation profiles for the anions seem to be independent on the strength of the ion–electrode interactions.

Finally, the dynamic properties have also been investi-

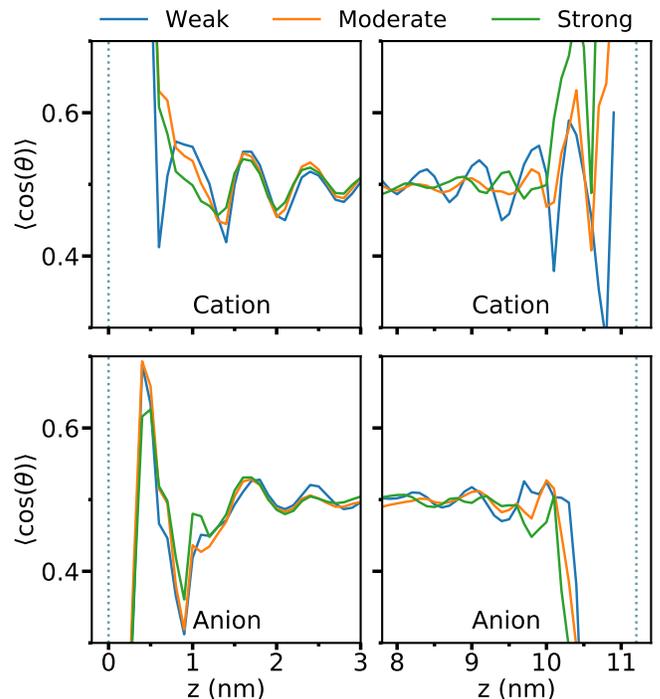


FIG. 8. Mean orientation profiles along the z direction for the cations (top panels) and for the anions (bottom panels) for an applied potential difference of 4 V. $\cos(\theta) = 1$, respectively 0, corresponds to the ions oriented parallel, respectively perpendicular, to the electrode.

gated. Figure 9 shows the time evolution of the number of cations and anions adsorbed along the simulation for a potential difference of 0 V. The curve is the running av-

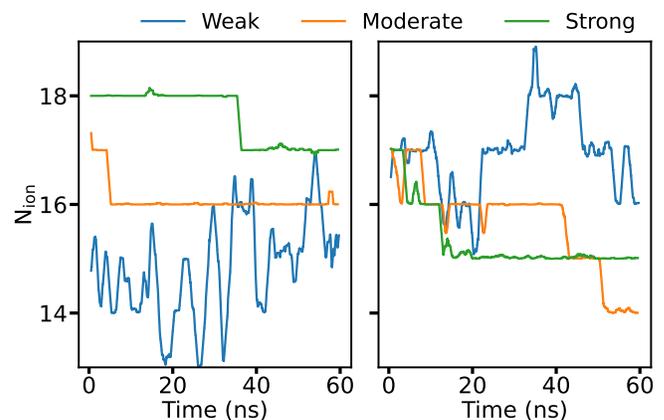


FIG. 9. Time evolution of the number of cations (left panel) and anions (right panel) adsorbed at the interface for an applied potential of 0 V. The running average over 1 ns is displayed in order to reduce the variations due to ions that shortly leave or enter the cut-off distance of 5 Å.

erage over 1 ns in order to remove some of the noise due to ions that shortly leave or enter the cut-off distance

of 5 Å used to define the adsorbed layer. For the same simulation time, fewer adsorption or desorption events are detected when the strength of the attraction between the ions on the electrode is raised. Note that in this case the number of adsorbed ions does not oscillate around a mean value. However, this has no significant impact on the total charge on the electrodes which fluctuates around an equilibrated mean value (see Figure 3). As charging storing is due to adsorption and desorption of ions, the reduction of the dynamics of adsorption is expected to slow down the charging dynamics. However, we do not provide charging times, as in order to obtain reliable values it would be necessary to run several MD simulations in the charging region.

IV. CONCLUSIONS

In this work we have studied the effect of the strength of electrolyte–electrode vdW interactions on the structural, dynamical and capacitive properties of the interface between pure EMIM-TFSI and a planar carbon electrode. The decrease of capacitance resulting from the increase of the ion–electrode attraction observed in this study is related to the limitation of exchanges between co-ions and counter-ions adsorbed at the interface when a difference of potential between the electrodes is applied. In addition, modifying the ion–electrode short-range interactions impacts the structure of the ions at a distance where these interactions are expected to have vanished. In fact, the orientation of the ions adsorbed is modified due to the increase of the adsorption strength, and this modification perturbs the orientation in the subsequent layers of ions.

In the study of electrochemical systems, and in particular when the electrolyte is a pure ionic liquid, it is commonly admitted that Coulomb interactions play a major role in the structural and dynamic properties, with vdW interactions having a minor role. This common assumption has led to put a lot of effort to improve the description of the electrostatic interactions in such system. For example, modeling the electrodes using constant potential²⁰ method is nowadays widely used, as well as, the development of models including explicit polarization for the ions of the electrolyte.^{33,46}

Yet, this work shows that the intensity of the ion–electrode interactions also has a significant impact on the electrode–electrolyte interface, in particular in the determination of the capacitance. As a consequence, the development of a dedicated force field not only for the electrolyte but also for the electrode is of a particular importance in the simulation of electrolyte–electrode interfaces if one wants to determine the capacitance at a quantitative level. Challenges are associated with this endeavour. Modern force fields are generally parameterized using electronic structure calculations at the Density Functional theory (DFT) level, yet in the case of carbon surfaces the vdW interactions are notoriously diffi-

cult to catch.^{47,48} The use of higher level methods, such as Quantum Monte-Carlo, can help to benchmark the DFT calculations and ultimately lead to improved classical force fields between the carbon and ionic species, as was shown recently for lithium.⁴⁹ However the case of organic ions such as the ones constituting typical ionic liquids are even more challenging and thus may require significant amounts of work in the future years.

SUPPLEMENTARY MATERIAL

See the supplementary material for Figures S1-S7 as described in the manuscript.

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