

Final report of the new BIPM comparison BIPM.RI(II)-K1.Ra-223 of activity measurements of the radionuclide ²²³ Ra including the 2014 result of the NPL (United Kingdom), the 2014 result of the PTB (Germany) and the 2018 result of the LNE-LNHB (France)

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Final report of the new BIPM comparison BIPM.RI(II)-K1.Ra-223 of activity measurements of the radionuclide ²²³Ra including the 2014 result of the NPL (United Kingdom), the 2014 result of the PTB (Germany) and the 2018 result of the LNE-LNHB (France)

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Abstract Since 2014, 3 laboratories have submitted 3 samples of ²²³Ra to the International Reference System (SIR) for activity comparison at the Bureau International des Poids et Mesures (BIPM), with comparison identifier BIPM.RI(II)-K1.Ra-223. The NPL (United Kingdom), the PTB (Germany) and the LNE-LNHB (France) participated in the comparison and the key comparison reference value (KCRV) has been calculated for the first time. The degrees of equivalence between each equivalent activity measured in the SIR and the KCRV have been calculated and the results are given in the form of a table. A graphical presentation is also given.

1. Introduction

The SIR for activity measurements of γ -ray-emitting radionuclides was established in 1976. Each national metrology institute (NMI) may request a standard ampoule from the BIPM that is then filled with 3.6 g of the radioactive solution. For radioactive gases, a different standard ampoule is used. Each NMI completes a submission form that details the standardization method used to determine the absolute activity of the radionuclide and the full uncertainty budget for the evaluation. The ampoules are sent

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to the BIPM where they are compared with standard sources of 226 Ra using pressurized ionization chambers. Details of the SIR method, experimental set-up and the determination of the equivalent activity $A_{\rm e}$, are all given in [1].

From its inception until 31 December 2019, the SIR has been used to measure 1016 ampoules to give 771 independent results for 72 different radionuclides. The SIR makes it possible for national laboratories to check the reliability of their activity measurements at any time. This is achieved by the determination of the equivalent activity of the radionuclide and by comparison of the result with the key comparison reference value determined from the results of primary standardizations. These comparisons are described as BIPM continuous comparisons and the results form the basis of the BIPM key comparison database (KCDB) of the Comité International des Poids et Mesures Mutual Recognition Arrangement (CIPM MRA) [2]. The comparison described in this report is known as the BIPM.RI(II)-K1.Ra-223 key comparison.

2. Participants

Laboratory details are given in Table 1. The dates of measurement in the SIR given in Table 1 are used in the KCDB and all references in this report.

NMI or	Previous	Full name	Country	RMO	Date of
labora-	acronyms				$egin{array}{c c} \mathbf{SIR} & \mathbf{mea-} \\ \mathbf{surement} \end{array}$
tory					yyyy-mm-dd
LNE-	LMRI,	Laboratoire National de	France	EURAMET	2018-03-15
LNHB	LPRI,	métrologie et d´Essais			
	BNM-	-Laboratoire National			
	LNHB	Henri Becquerel			
NPL	-	National Physical Labora-	United King-	EURAMET	2014-06-04
		tory	dom		
PTB	-	Physikalisch-Technische	Germany	EURAMET	2014-07-08
		Bundesanstalt			

Table 1: Details of the participants in the BIPM.RI(II)-K1.Ra-223.

3. NMI standardization methods

Each NMI that submits amoules to the SIR has measured the activity either by a primary standardization method or by using a secondary method, for example a calibrated ionization chamber. In the latter case, the traceability of the calibration needs to be clearly identified to ensure that appropriate correlations are taken into account.

A brief description of the standardization methods used by the laboratories, the activities submitted, the relative standard uncertainties and the half-life used by the participants are given in Table 2. The uncertainty budget for the new submission is given in Appendix D attached to this report. The list of acronyms used to summarize

the methods is given in Appendix E.

The half-life used by the BIPM is 11.43(3) days as published in BIPM Monographie 5 vol. 6 [3].

NMI or	Method used and the	Activity	Relativ	e	Reference	Half-life
labora-	acronym	$A_i/{f kBq}$	standar	$^{\mathrm{d}}$	date	$ $ $/\mathbf{d}$
tory			uncerta	inty		
			$/10^{-2}$			
			A	В	yyyy-mm-	
					dd	
LNE-	TDCR (4P-LS-BP-00-00-	1239.1	0.01	0.19	2018-03-15	
LNHB	TD)				12:00 UT	
NPL	$4\pi \text{LS-}\gamma$ coincidence (4P-LS-	1193.2	0.1	0.26	2014-05-08	
	MX-GH-GR-CO)				12:00 UT	
PTB	CIEMAT/NIST (4P-LS-	4149.0 ^a	0.04	0.22^{a2}	2014-07-01	11.43(3)
	MX-00-00-CN)				00:00 UT	
	TDCR (4P-LS-MX-00-00-					
	TD [4])					

Table 2: Standardization methods of the participants for ²²³Ra.

Details regarding the solutions submitted are shown in Table 3, including any impurities, when present, as identified by the laboratories. When given, the standard uncertainties on the evaluations are shown.

Relative activity of NMIChemical Solvent conc. Carrier Density any impurity^b laboratory composiconc. tion $/(g \, \text{cm}^{-3})$ $/(\mu g g^{-1})$ / (mol dm⁻³) / SIR year LNE-LNHB Barium in HCl: 1 NaCl: Ba: 22 1.016 None detected 2018 HCl 0.054with NaCl ²²³Ra in HCl^a None detected NPL 2014 1.02 227 Ac: < 0.03 % 223 RaCl₂, PTB 2014 unknown but unknown but approx. NaCl, low concentralow concen-1.000 sodium tration tion citrate dihydrate, calcium chloride dihydrate in HCl

Table 3: Details of each solution of ²²³Ra submitted.

^a The final result is the weighted mean of the results of the two methods.

 $^{^{}a2}$ The relative combined uncertainty (0.23 %) of the TDCR result is adopted for the final result. This is larger than the internal and external relative uncertainties of the weighted mean.

^b The result is the mean of the different methods.

^{a 223}Ra in equilibrium with progeny

^b the ratio of the activity of the impurity to the activity of ²²³Ra at the reference date

4. Results

All the submissions to the SIR since its inception in 1976 are maintained in a database known as the "master-file". The activity measurements for 223 Ra now have a total of 3 ampoules. The SIR equivalent activity, A_{ei} , for each ampoule received from each NMI, i, including both previous and new results, is given in Table 4.

The relative standard uncertainties arising from the measurements in the SIR are also shown. This uncertainty is additional to that declared by the NMI $(u(A_i))$ for the activity measurement shown in Table 2. Although submitted activities are compared with a given source of 226 Ra, all the SIR results are normalized to the radium source number 5 [1]. No recent submission has been identified as a pilot study so the most recent result of each NMI is normally eligible for inclusion on the KCDB platform of the CIPM MRA [2].

Measurements repeated at the BIPM after periods of up to one day, seven days and eight days later produced comparison results in agreement within standard uncertainty for the NPL, PTB and LNE-LNHB, respectively.

NMI or labo-	m_i	A_i	226 Ra	$A_{\mathbf{e}i}$	Relative	$u_{\mathbf{c}i}$	$A_{\mathbf{e}i}$ for
ratory			source		uncert.		KCRV
					from		
					SIR		
/ SIR year	$/\mathbf{g}$	$/k\mathbf{Bq}$		/kBq	$/10^{-4}$	/kBq	$/k\mathbf{Bq}$
LNE-LNHB	3.674 7	1239.1	2	54 400	11	120	54 400(120)
2018							
NPL 2014	3.623 95	1193.2	1	54 740	46 ^a	300	54 740(300)
PTB 2014	3.629 9	4149	2	54 590	16 ^a	150	54 590(150)

Table 4: Results of SIR measurement of ²²³Ra.

4.1. The key comparison reference value

In May 2013, the CCRI(II) decided to calculate the key comparison reference value (KCRV) by using the power-moderated weighted mean [5] rather than an unweighted mean, as had been the policy. This type of weighted mean is similar to a Mandel-Paule mean in that the NMIs' uncertainties may be increased until the reduced chisquared value is one. In addition, it allows for a power α smaller than two in the weighting factor. As proposed in [5], α is taken as 2-3/N where N is the number of results selected for the KCRV. Therefore, all SIR key comparison results can be selected for the KCRV with the following provisions:

(a) only results for solutions standardized by primary techniques are accepted, with the

^a uncertainty dominated by the contribution from the decay correction

exception of radioactive gas standards (for which results from transfer instrument measurements that are directly traceable to a primary measurement in the laboratory may be included);

- (b) each NMI or other laboratory may only use one result (normally the most recent result or the mean if more than one ampoule is submitted);
- (c) results more than 20 years old are included in the calculation of the KCRV but are not included in data shown in the KCDB or in the plots in this report, as they have expired;
- (d) possible outliers can be identified on a mathematical basis and excluded from the KCRV using the normalized error test with a test value of 2.5 and using the modified uncertainties;
- (e) results can also be excluded for technical reasons; and
- (f) the CCRI(II) is always the final arbiter regarding excluding any data from the calculation of the KCRV.

The data set used for the evaluation of the KCRVs is known as the KCRV file and is a reduced data set from the SIR master-file. Although the KCRV may be modified when other NMIs participate, on the advice of the Key Comparison Working Group of the CCRI(II), such modifications are made only by the CCRI(II) during one of its biennial meetings, or by consensus through electronic means (e.g., email) as discussed at the CCRI(II) meeting in 2013.

Consequently, a first KCRV for 223 Ra of **54 531(96)** kBq with the power $\alpha = 1.0$ has been calculated using the results, selected as shown in Table 4, for the NPL (2014), PTB (2014), and the LNE-LNHB (2018) result.

4.2. Degrees of equivalence

Every participant in a comparison is entitled to have one result included in the KCDB as long as the NMI is a signatory or designated institute listed in the CIPM MRA and the result is valid (i.e., not older than 20 years). Normally, the most recent result is the one included. An NMI may withdraw its result only if all other participants agree.

The degree of equivalence of a given measurement standard is the degree to which this standard is consistent with the KCRV [2]. The degree of equivalence is expressed quantitatively in terms of the deviation from the key comparison reference value and the expanded uncertainty of this deviation (k = 2). The degree of equivalence between any pair of national measurement standards is expressed in terms of their difference and the expanded uncertainty of this difference and is independent of the choice of key comparison reference value.

4.2.1. Comparison of a given NMI result with the KCRV

The degree of equivalence of the result of a particular NMI, i, with the key comparison reference value is expressed as the difference D_i between the values

$$D_i = A_{ei} - KCRV \tag{1}$$

and the expanded uncertainty (k = 2) of this difference, U_i , known as the equivalence uncertainty; hence

$$U_i = 2u(D_i) \tag{2}$$

When the result of the NMI i is included in the KCRV with a weight w_i , then

$$u^{2}(D_{i}) = (1 - 2w_{i})u_{i}^{2} + u^{2}(KCRV)$$
(3)

However, when the result of the NMI i is not included in the KCRV, then

$$u^2(D_i) = u_i^2 + u^2(KCRV) \tag{4}$$

4.2.2. Comparison between pairs of NMI results

The degree of equivalence between the results of any pair of NMIs, i and j, is expressed as the difference D_{ij} in the values

$$D_{ij} = D_i - D_j = A_{ei} - A_{ej} \tag{5}$$

and the expanded uncertainty (k=2) of this difference, $U_{ij}=2u(D_{ij})$, where

$$u^{2}(D_{ij}) = u_{i}^{2} + u_{j}^{2} - 2u(A_{ei}, A_{ej})$$
(6)

where any obvious correlations between the NMIs (such as a traceable calibration, or correlations normally coming from the SIR or from the linking factor in the case of linked comparison) are subtracted using the covariance $u(A_{ei}, A_{ej})$ (see [6] for more detail). However, the CCRI decided in 2011 that these pair-wise degrees of equivalence no longer need to be published as long as the methodology is explained.

Table B1 shows the matrix of all the degrees of equivalence as they will appear in the KCDB. It should be noted that for consistency within the KCDB, a simplified level of nomenclature is used with A_{ei} replaced by x_i . The introductory text is that agreed for the comparison. The graph of the results in Table 5, corresponding to the degrees of equivalence with respect to the KCRV (identified as x_R in the KCDB), is shown in Figure C1. This graphical representation indicates in part the degree of equivalence between the NMIs but obviously does not take into account the correlations between the different NMIs. It should be noted that the final data in this paper, while correct at the time of publication, will become out-of-date as NMIs make new comparisons. The formal results under the CIPM MRA [2] are those available in the KCDB.

5. Conclusion

The new BIPM continuous key comparison for ²²³Ra, BIPM.RI(II)-K1.Ra-223, comprises 3 results. The KCRV has been calculated for the first time to include the result from the LNE-LNHB (France), NPL (United Kingdom), and the PTB (Germany). The results have been analyzed with respect to the calculated KCRV, providing degrees of equivalence for 3 national metrology institutes. The degrees of equivalence have been approved by the CCRI(II) and are published in the BIPM key comparison database. Other results may be added when other NMIs contribute ²²³Ra activity measurements to this comparison or take part in other linked comparisons.

6. References

- [1] Ratel, G. The Système International de Référence and its application in key comparisons, *Metrologia*, 2007, 44(4), S7-S16.
- [2] CIPM MRA: Mutual recognition of national measurement standards and of calibration and measurement certificates issued by national metrology institutes, International Committee for Weights and Measures, 1999, pp. 45, Technical Supplement revised in October 2003 (pages 38-41).
- [3] Bé M.-M., Chisté V., Dulieu C., Mougeot X., Chechev V.P., Kuzmenko N.K., Kondev F.G., Luca A., Galán M., Nichols A.L., Arinc A., Pearce A., Huang X., Wang B., Table of radionuclides, Monographie BIPM-5, 2011, Vol 6.
- [4] Kossert K., Bokeloh K., Dersch R., Nähle O.J., Activity determination of ²²⁷Ac and ²²³Ra by means of liquid scintillation counting and determination of nuclear decay data, Applied Radiation and Isotope, 2015, 95, 143-152.
- [5] Pommé S. and Keightley J., Determination of a reference value and its uncertainty through a power-moderated mean, *Metrologia*, 2015, **52**(3), S200.
- [6] Michotte C. and Ratel G., Correlations taken into account in the KCDB, CCRI(II) working document, 2003, CCRI(II)/03-29.

Appendix A. Introductory text for ²²³Ra degrees of equivalence

Key comparison BIPM.RI(II)-K1.Ra-223

MEASURAND: Equivalent activity of ²²³Ra

Key comparison reference value: the SIR reference value $x_{\rm R}$ for this radionuclide is 54531 kBq, with a standard uncertainty, $u_{\rm R}$ equal to 96 kBq (see Section 4.1 of the Final Report). The value x_i is taken as the equivalent activity for a laboratory i.

and U_i , its expanded uncertainty (k=2), both expressed in MBq, and $U_i=2((1-2w_i)u_i^2+u_{\rm R}^2)^{1/2}$, where w_i is the weight of The degree of equivalence of each laboratory with respect to the reference value is given by a pair of terms: $D_i = (x_i - x_R)$ laboratory i contributing to the calculation of $x_{\rm R}$.

Appendix B. Table of degrees of equivalence for BIPM.RI(II)-K1.Ra-223 $\,$

Table B1: The table of degrees of equivalence for ${\rm BIPM.RI(II)\text{-}K1.Ra\text{-}223}$

NMI i	D_i / \mathbf{MBq}	U_i / \mathbf{MBq}
NPL	0.21	0.52
PTB	0.06	0.25
LNE-LNHB	-0.13	0.21

Appendix C. Graph of degrees of equivalence with the KCRV for ²²³Ra (as it appears in Appendix B of the MRA)

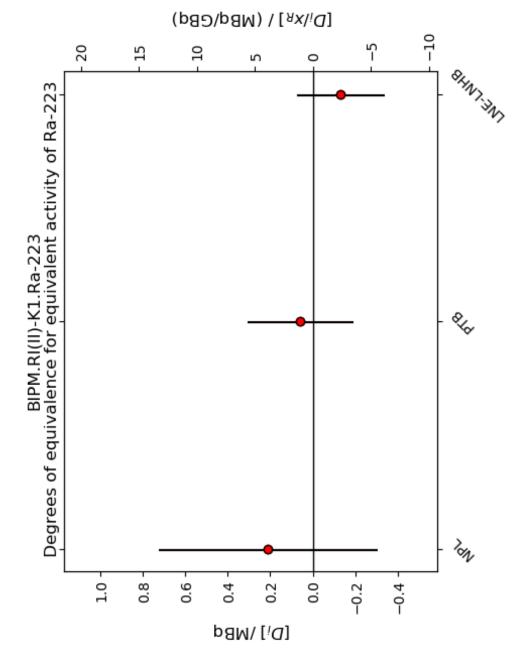


Figure C1. Degrees of equivalence for equivalent activity of ²²³Ra.

Appendix D. Uncertainty budgets for the activity of $^{223}\mathrm{Ra}$ submitted to the SIR

The LNE-LNHB has submitted a detailed uncertainty budget as follows:

Relative standard uncertainties	$u_{rel,i} \times 10^4$	Method of
Contributions due to		evaluation
counting statistics	1.1	A
weighing	10	В
dilution factor	3.9	В
dead time	0.3	В
background	0.8	A
pile-up	0.01	В
counting time (Rb clock)	10^{-5}	В
adsorption	5	В
input parameters and statistical model	3	В
ionization quenching	1	В
alpha counting efficiency	5	В
²¹⁹ Rn loss (potential)	10	В
decay correction	1	В
radionuclide impurities (no impurity found)	10	В
Relative combined standard uncertainty, u_c	1	9

The NPL (2014) has submitted a detailed uncertainty budget as follows:

Relative standard uncertainties	$u_{rel,i} \times 10^4$	Method of	Comments
Contributions due to		evaluation	
counting statistics	10	A	standard deviation of mean of 11 sources
weighing	3	В	
dilution factor	5	В	
background	0.2	В	
pile-up in LS channel	1.5	В	
pile-up in γ channel/s	0.5	В	
LS channel dead time	10	В	after corrections for 1.781 ms half-life of ²¹⁵ Po
γ channel dead time	5	В	
accidental coincidences and finite resolving time	1	В	
decay corrections	5	В	
efficiency extrapolations	10	В	choice of range of fit
choice of γ gates	20	В	
equilibrium and ingrowth calculations	1	В	
impurities	0	В	none detected
Relative combined standard uncertainty, u_c	2	28	

Detailed Uncertainty Budget (4P-LS-MX-00-00-TD)

Laboratory: PTB ;	Radionuclide: _ Ra-	223_; Ampoule number: 20	14-1383 (SIR)		
Uncertainty components*, in % of the activity concentration, due to					
		RemarksEvaluati	ion		
		type (A	or B)		
counting statistics	0.02	std. dev. of mean of 5 samples	A		
weighing	0.07		B		
dead time	0.03		B		
background	0.03		A		
pile-up	_ n.a				
counting time	_ 0.01 _		B		
adsorption	0.10		B		
impurities	_ 0.03	potential ²²⁷ Ac	B		
TDCR value and fit	_ 0.01	including interpolation	B		
model and decay data	0.06		B		
ionization quenching					
and kB (model)	_ 0.01		B		
interpolation from calibration curve decay correction		included in TDCR uncertainty $T_{1/2} = (11.43 \pm 0.03) \text{ d}$	B		
quenching indicator (SQP(E), ISIE)	_ 0.03	*	B		
α-counting efficiency	_ 0.05		B		
potential ²¹⁹ Rn loss	_ 0.1		B		
dilution	_ 0.06		B		
PMT asymmetry	_ 0.02		B		
combined uncertainty	_ 0.23				
(as quadratic sum of all uncertainty components)					

^{*} The uncertainty components are to be considered as approximations of the corresponding standard deviations (see also *Metrologia*, 1981, **17**, 73 and *Guide to expression of uncertainty in measurement*, ISO, corrected and reprinted 1995).

Detailed Uncertainty Budget (4P-LS-MX-00-00-CN)

Laboratory:PTB	; Radionuclide: _ Ra-	-223_; Ampoule number: 2	014-1383 (SIR)		
Uncertainty components*, in % of the activity concentration, due to					
		RemarksEvaluat	ion		
		type (A	or B)		
counting statistics	_ 0.03	std. dev. of mean of 5 samples	A		
weighing	_ 0.07		B		
dead time	_ 0.10		B		
background	_ 0.05		A A		
pile-up	_ n.a				
counting time	_ 0.01 _		B		
adsorption	_ 0.10		B		
impurities	_ 0.03	potential ²²⁷ Ac	B		
Tracer (³ H)	_ 0.01	including interpolation	B		
model and decay data	_ 0.06		B		
ionization quenching					
and kB (model)	_ 0.01		B		
interpolation from calibration curve decay correction		included in tracer uncertainty $T_{1/2} = (11.43 \pm 0.03) \text{ d}$			
quenching indicator (SQP(E),ISIE)	_ 0.03		B		
α-counting efficiency	_ 0.05		B		
potential ²¹⁹ Rn loss	0.1		B		
dilution	_ 0.06		B		
PMT asymmetry	_ 0.02		B		
combined uncertainty	_ 0.25				

(as quadratic sum of all uncertainty components)

^{*} The uncertainty components are to be considered as approximations of the corresponding standard deviations (see also *Metrologia*, 1981, 17, 73 and *Guide to expression of uncertainty in measurement*, ISO, corrected and reprinted 1995).

Appendix E. Acronyms used to identify different measurement methods

Each acronym has six components, geometry-detector (1)-radiation (1)-detector (2)-radiation (2)-mode. When a component is unknown, ?? is used and when it is not applicable 00 is used.

Geometry	acronym	Detector	acronym
4 π	4P	proportional counter	PC
defined solid angle	SA	press. Prop. Counter	PP
2 π	2P	liquid scintillation counting	LS
undefined solid angle	UA	NaI(Tl)	NA
		Ge(HP)	GH
		Ge(Li)	GL
		Si(Li)	SL
		CsI(Tl)	CS
		ionization chamber	IC
		grid ionization chamber	GC
		Cerenkov detector	CD
		calorimeter	CA
		solid plastic scintillator	SP
		PIPS detector	PS
		CeBr3	СВ

Radiation	acronym	Mode	acronym
positron	РО	efficiency tracing	ET
beta particle	BP	internal gas counting	IG
Auger electron	AE	CIEMAT/NIST	CN
conversion electron	CE	sum counting	SC
mixed electrons	ME	coincidence	СО
bremsstrahlung	BS	anti-coincidence	AC
gamma rays	GR	coincidence counting with	СТ
		efficiency tracing	
x-rays	XR	anti-coincidence counting	AT
		with efficiency tracing	
photons $(x + \gamma)$	PH	triple-to-double coincidence	TD
		ratio counting	
${ m photons} + { m electrons}$	PE	selective sampling	SS
alpha particle	AP	high efficiency	HE
mixture of various radi-	MX	digital coincidence counting	DC
ation			

Examples of methods	acronym
$4\pi(PC)\beta-\gamma$ coincidence counting	4P-PC-BP-NA-GR-CO
$4\pi(PPC)\beta-\gamma$ coincidence counting	4P-PP-MX-NA-GR-CT
eff. trac	
defined solid angle α -particle	SA-PS-AP-00-00-00
counting with a PIPS detector	
$4\pi(PPC)AX-\gamma(GeHP)-$	4P-PP-MX-GH-GR-AC
anticoincidence counting	
$4\pi \text{CsI-}\beta, AX, \gamma \text{ counting}$	4P-CS-MX-00-00-HE
calibrated IC	4P-IC-GR-00-00-00
internal gas counting	4P-PC-BP-00-00-IG