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Article

M-Ary Direct Modulation Chirp Spread Spectrum for Spectrally Efficient Communications

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Abstract: Spread spectrum techniques, such as the Chirp Spread Spectrum (CSS) used by LoRa technology, are important for machine-to-machine communication in the context of the Internet of Things. They offer high processing gain, reliable communication over long ranges, robustness to interference and noise in harsh environments, etc. However, these features are compromised by their poor spectral efficiency, resulting in a very low data transmission rate. This paper deals with a spectrally efficient variant of CSS. The system uses M-ary phase keying to modulate the data and exploits CSS's properties to transmit the modulated symbols as overlapping chirps. The overlapping of chirp signals may affect the system performance due to inter-symbol interference. Therefore, we analyse the relationship between the number of overlaps and the effect of inter-symbol interference (ISI), and we also determine the BER expression as a function of the number of overlaps. Finally, we derive the optimal number of overlapping symbols that corresponds to the minimum error probability.

Keywords: internet of things; chirp spread spectrum; MPSK; overlapping chirps; inter-symbol interference; spectral efficiency



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1. Introduction

The concept of spread spectrum modulation is based on the idea of using more bandwidth than the minimum required to transmit information. Spread spectrum modulation ensures transmission performance in environments with interference and fading, such as dense wireless sensor networks [1–4]. Some of the advantages of spread spectrum systems include selective addressing, code multiplexing, low-power spectral density, message confidentiality, high-resolution range, interference suppression capability, processing gain, and also a jamming margin [5].

Selective addressing possible by using sequences of modulation codes to recognize a particular signal. Assigning a particular code to a given receiver allows it to be contacted only by a transmitter that uses that code to modulate its signal. Code division multiplexing is similar in that some transmitters and receivers can operate on the same frequency at the same time using different codes. Transmitted signals with low-power spectral density are advantageous for preventing interference with other systems and providing a low probability of interception. The low-power spectral density of spread spectrum signals is an inherent property due to bandwidth expansion. Message confidentiality (or privacy) is also inherent in spread spectrum signals because of their coded transmission format. Spread spectrum systems have been built to use all types of codes, from the relatively simple

Information 2023, 14, 323 2 of 15

maximum linear code to truly secure non-linear types of encryption. Direct sequence spread spectrum signals stand out by providing high-resolution range measurements. This property is due to the high-speed codes used for modulation.

Among the spread spectrum techniques, the direct sequence spread spectrum (DSSS) and the chirp spread spectrum are the most studied. The spread spectrum signal of DSSS across the transmission interface is generated by mixing the information with a pseudorandom noise (PN) code, which is a deterministic binary sequence that exhibits good randomness properties [6,7]. The DSSS has strong rejection ability against multi-path propagation interference and has lower-power spectral density. Chirp Spread Spectrum (CSS) modulation was introduced in 1962 by Winkler, who proposed to use a pair of linear chirps containing opposite chirp rates for binary signalling [8]. In CSS, data are encoded with chirps, and a chirp signal can increase (up-chirp) or decrease (down-chirp) in frequency over time.

We distinguish two main types of CSS: Binary Orthogonal Keying (BOK) and Direct Modulation (DM). The conventional BOK CSS system transmits the symbols '1' and '0' as a linear up-chirp and down-chirp, respectively. BOK CSS uses the chirps to encode the information and to spread their frequency band over the transmission bandwidth. The spectral efficiency of the BOK CSS system depends on the quasi-orthogonality of the chirps [9,10]. DM CSS uses some kind of linear chirp to spread the data symbol. DM CSS uses any suitable modulation scheme to encode the input data, and the chirping scheme is used to ensure robust and long-range transmission, as in a radar system. A DM scheme may lead to more complexity compared to BOK, but it can ensure higher spectral efficiency if a powerful modulator is used. Paper [11] presents a linear-chirp-based modulation technique, different from BOK and DM CSS, in which a Doppler frequency shift is implanted in the chirp signal at the transmitter. The M-ary chirping is achieved in a single impulse with this proposed modulation technique, and the peak position in the pulse duration is used for demodulation.

To obtain a fast, reliable CSS system, a tradeoff must be made between interference reduction capability, resistance to multipath effects, and data rate. Several models [12,13] have been proposed to improve device-to-device transmissions [14] and the CSS data rate. The data rate can be increased by overlapping more chirps. For example, with a chirp duration $\tau_{ch}=20~\mu s$ and a symbol rate of 10 MHz, about 200 chirps can be overlapped. A. Pohl et al. [15] demonstrated that a better choice of data rate can lead to better amplifier utilization, while fine-tuning the data rate can reduce the impact of interference. Nevertheless, the upper limit for data rates may depend on the channel response. For instance, a communication channel with a spread delay of 100 ns can transmit up to 10 Mbps without additional signal processing and by using a Rake receiver [15].

Kim et al. proposed in [16] multilinear chirp for simultaneous transmission with direct modulation in [16]. They combined binary shift keying (BSPK) with multilinear DM CSS and proposed orthogonal transmission of BSPK symbols. The receiver uses the cross correlation coefficients (CCC) and frequency spacing to detect the transmitted chirps. B. Reynders et al. [17] presented a detailed model of CSS and proved that the signals are not perfectly orthogonal. They developed a decoder that makes decisions based on maximum correlation. In [18], the authors take advantage of the orthogonality to overlap several Chirp signals.

Higher spectral efficiency can also be achieved by overlapping in the time domain. Thus, the authors of [10] proposed a combination of binary offset carrier modulation (BOC) with DM CSS to improve spectral efficiency. The modulator maps the binary data stream to the codeword using 8-BOC with code rate 3/4. Then, two codewords are transmitted simultaneously as up and down chirps with half chirp duration, and the second pair is transmitted in the remaining chirp duration. Despite good broadening of the spread bandwidth, the orthogonality between chirp signals may not be guaranteed. Thus, their proposed model may cause interference between the overlapped signals and cannot maintain the antipodal property in each signal. In [19], the authors proposed a

Information 2023, 14, 323 3 of 15

transceiver design for enhancing the spectral efficiency in downlink CSS communications. Their scheme simultaneously transmits signals to several receivers using the same time–frequency resources. To ensure that each receiver demodulates the incoming symbols properly, ref. [19] considers controlling the level of interference between the different users and the quasi-orthogonality properties between the upstream and downstream chirps. In an effort towards higher spectral efficiency, ref. [20] proposed a dual-mode chirp spread spectrum modulation (DM-CSS) for low-power wide-area networks. The term 'dual mode' refers to the use of even and odd numbers of frequencies. For a given symbol duration, the authors argue, the model will achieve higher spectral efficiency by simultaneously multiplexing even and odd chirp signals using phase shifts of 0 and π radians, respectively, and either an up- or down-chirp signal.

DM CSS allows chirps to overlap in the time domain and uses a simple matched filter for detection [21]. Even though the overlap approach improves spectral efficiency, it may result in increased inter-symbol interference, which severely degrades BER [21–23]. As a consequence, a proper trade-off between the spectral efficiency and ISI is necessary. Inter-symbol interference (ISI) can deteriorate the overall performance of a communication system since it may reduce the signal-to-noise ratio (SNR) at the receiver and thus make it very difficult to accurately detect the transmitted symbols. A variety of techniques have been proposed to mitigate ISI, including equalization, which attempts to cancel the effects of the channel on the transmitted symbols; or the use of pulse shaping filters, which shape the transmitted waveforms to reduce their duration and minimize overlap. T. Yoon et al. [23] provided a theoretical expression for the BER of an overlapping CSS system to further guide the selection of the optimal number of overlaps. In [21], the authors also proposed a BER expression for an overlapping DM CSS system with a finite number of overlaps and investigated in which conditions the ISI can be minimized while nearing the Nyquist rate.

Nevertheless, the majority of the related work on DM CSS focuses solely on the transmission of binary data. In this work, we propose a spectrally efficient direct modulation CSS modulation method that deals with M-ary data. Our approach considers overlapping signals in a single chirp duration τ_{ch} and proposes a mathematical framework to derive the optimal number of overlaps. In addition, we analyse the performance of this approach in terms of BER and ISI during the chirp duration τ_{ch} . Our contributions can be summarized as follows:

- Design of a modulation scheme that transmits multiple overlapping up-chirp signals;
- Mathematical formulation of the symbol time and the number of overlaps;
- Deriving the mathematical expression for the bit error probability of the proposed scheme as a function of inter-symbol interference and number of overlaps;
- Performance evaluation using various metrics to demonstrate the effectiveness of our approach.

The rest of the paper is organized as follows. The DM-CSS is described in more detail in Section 2. Section 3 briefly discusses the M-ary phase shift keying modulation, while Section 4 introduces our contributions. The performance of the system is evaluated in Section 5. The conclusion and future work are presented in Section 6.

2. Direct Modulation CSS

Unlike BOK, in direct modulation CSS, modulation and spreading are performed separately. In the case of high-data-rate transmission, an M-ary coding transforms the input bit sequences into symbols, which are then converted into signals by a modulation scheme such as M-ary phase-shift keying. Finally, DM CSS spreads the modulated signals over the transmission bandwidth. This spreading is done with a single linear up-chirp and aims to increase the signal time from $\frac{1}{B_{ch}}$ to τ_{ch} [24]. The choice of DM CSS offers the designers the

Information 2023, 14, 323 4 of 15

possibility of using any constant-envelope modulation technique to encode the input data. The mathematical representation of a standard chirp waveform is given by Equation (1).

$$c_{+}(t) = \begin{cases} a(t) \exp\{j\theta(t)\}, & -\frac{\tau_{ch}}{2} \le t \le \frac{\tau_{ch}}{2} \\ 0 & \text{elsewhere} \end{cases}$$
 (1)

where a(t) denotes the data sequence, $\theta(t)$ is the phase function of the chirp signal, and τ_{ch} is the chirp duration. The instantaneous frequency of the chirp waveform at time t is given by Equation (2).

$$f(t) = \frac{1}{2\pi} \frac{d\theta}{dt}(t), \qquad \forall \ t \in \left[-\frac{\tau_{ch}}{2}, \frac{\tau_{ch}}{2} \right]. \tag{2}$$

The derivative of f(t) helps to evaluate the rate of change of the instantaneous frequency of the chirp signal with respect to time t. It is usually called chirp (sweep) rate, and its expression is formulated in Equation (3).

$$\mu(t) = \frac{df}{dt}(t) = \frac{1}{2\pi} \frac{d^2\theta}{dt^2}(t), \qquad \forall \ t \in \left[-\frac{\tau_{ch}}{2}, \frac{\tau_{ch}}{2} \right]. \tag{3}$$

In the case of a linear chirp signal, the phase $\theta(t)$ is a quadratic function. Thus, the instantaneous frequency and its chirp rate are linear and constant, respectively. In what follows, we assume $\theta(t)$ is given by Equation (4), and f(t) is bounded by f_{max} (maximum frequency) and f_{min} (minimum frequency) over the interval $\left[-\frac{\tau_{ch}}{2}, \frac{\tau_{ch}}{2}\right]$.

$$\theta(t) = \mu \pi t^2 + 2\pi f_c t + \phi_{i_0}, \qquad \forall t \in \left[-\frac{\tau_{ch}}{2}, \frac{\tau_{ch}}{2} \right], \tag{4}$$

$$\mu = \frac{f_{max} - f_{min}}{\tau_{ch}},\tag{5}$$

where ϕ_{i_0} is the initial phase of the signal (ϕ_{i_0} at t = 0), f_c is the carrier frequency, and μ , given in Equation (5), is the constant frequency sweep rate.

3. M-Ary Phase Shift Keying

The M-ary techniques are a type of digital modulation scheme used for high-data-rate transmission, where several bits are transmitted at a time rather than one bit. M-ary PSK (MPSK) is a multilevel phase shift keying modulation technique that encodes input signals containing several bits.

The general form of an MPSK modulated signal is given in Equation (6), where $\Re\{.\}$ denotes the real part, with $M=2^k$, $\omega_c=2\pi f_c$, $h_{\tau_{ch}}(t)$ is a filter whose pulse response is given in Equation (8), and the random symbols are coded using the values of the phase ϕ_{m_i} provided in Equation (9).

$$s(t) = \Re\{s_e(t)\exp(j\omega_c t)\},\qquad \qquad -\frac{\tau_{ch}}{2} \le t \le \frac{\tau_{ch}}{2}$$
 (6)

$$s_e(t) = \sqrt{\frac{2E_s}{\tau_{ch}}} \sum_{i=-\infty}^{+\infty} h_{\tau_{ch}}(t - i\tau_{ch}) \exp(j\phi_{m_i}),$$
 (7)

$$h_{\tau_{ch}}(t) = \bigcap_{\left[-\frac{\tau_{ch}}{2}, \frac{\tau_{ch}}{2}\right]}(t) = \begin{cases} 1 & \text{if } -\frac{\tau_{ch}}{2} \le t \le \frac{\tau_{ch}}{2} \\ 0 & \text{elsewhere} \end{cases}$$
(8)

$$\phi_{m_i} = \frac{m_i \pi}{M} \qquad m_i \in \{0, 1, \dots, M - 1\} \quad (9)$$

In order to generate more insights from the modulated signal, we apply some trigonometric expansion to Equation (6) to obtain a new signal expression. Equation (10) is the quadra-

Information 2023, 14, 323 5 of 15

> ture representation of an MPSK modulated signal, where $\cos(\omega_c t)$ and $\sin(\omega_c t)$ are the orthogonal carrier signals. This representation leads to a standard method of generating MPSK signals as a linear combination of the quadrature signals $\cos(\omega_c t)$ and $\sin(\omega_c t)$. On the horizontal axis of the constellation diagram lies the cosine coefficient (in-phase, or *I* signal), while the sine coefficient (quadrature or Q signal) is on the vertical axis. The I and Q signals are multiplied by $\cos(\omega_c t)$ and $\sin(\omega_c t)$. Then, the MPSK modulated signal is the sum of the mixers' outputs.

$$s(t) = \sqrt{\frac{2}{\tau_{ch}}} \sum_{i=-\infty}^{\infty} h_{\tau_{ch}}(t - i\tau_{ch}) \left(s_{m_i I} \cos(\omega_c t) + s_{m_i Q} \sin(\omega_c t) \right), \tag{10}$$

$$s_{m_i I} = \sqrt{E_s} \cos(\phi_{m_i}), \text{ and } s_{m_i O} = -\sqrt{E_s} \sin(\phi_{m_i}), \qquad m_i \in \{0, 1, \dots, M-1\}$$
 (11)

4. Proposed Model

4.1. Modulation Scheme

In this section, we introduce the DM CSS modulated signal. It derives from a general expression of an M-ary chirp modulated signal, which is given in Equation (12), with Equation (13) representing its phase function and E_s its energy in the symbol duration τ . It combines the benefits of M-ary Phase Shift Keying (PSK) and those of chirp signalling to provide high-spectral-efficiency transmission. Figure 1 presents the block diagram of the proposed modulation scheme.

MPSK divides and transmits the data stream as a group of k bits ($k \in \mathbb{N}$), called a symbol, with a specific initial phase. The total possible number of symbols is $M=2^k$. Each one of the *M* symbols is transmitted within the timeframe τ_{ch} (we assume that $\tau \leq \tau_{ch}$), which means a total transmission time of $N\tau_{ch}$ for N symbols. However, CSS enables transmission of η ($\eta \in \mathbb{N}$, $\eta > 1$) symbols per τ_{ch} , leading to an overall transmission time of $\frac{N}{\eta}\tau_{ch}$. Therefore, for a given M-ary PSK modulator, we study the maximum number of overlaps at which the intersymbol interference is lower, the mathematical relations between the number of overlaps, the spectral efficiency, and the ISI.

Choosing an M-ary scheme that guarantees a better tradeoff between spectral efficiency and BER performance is also an important design consideration for the proposed DM CSS. The signal model of the proposed MPSK CSS during the chirp duration τ_{ch} is given in Equation (14).

$$s(t) = \Re \left\{ \sum_{i=1}^{\eta} h_{\tau}(t - i\tau) \sqrt{\frac{2E_s}{\tau}} \exp \left\{ j\theta_{m_i}(t) \right\} \right\}, \qquad -\frac{\tau_{ch}}{2} \le t \le \frac{\tau_{ch}}{2}$$
 (12)

$$\theta_{m_i}(t) = \mu \pi t^2 + \omega_c t + \phi_{m_i},$$
 $m_i \in \{0, 1, \dots, M-1\}$ (13)

$$m_{i}(t) = \mu \pi t^{2} + \omega_{c} t + \phi_{m_{i}}, \qquad m_{i} \in \{0, 1, \dots, M - 1\}$$

$$s(t) = \sum_{i=1}^{\eta} h_{\tau}(t - i\tau) \{ s_{m_{i}I} U_{I}(t) + s_{m_{i}Q} U_{Q}(t) \}, \qquad -\frac{\tau_{ch}}{2} \le t \le \frac{\tau_{ch}}{2}$$

$$(14)$$

$$U_I(t) = \sqrt{\frac{2}{\tau}} \cos\left\{\omega_c t + \mu \pi t^2\right\}, \qquad -\frac{\tau}{2} \le t \le \frac{\tau}{2} \qquad (15)$$

$$U_{Q}(t) = \sqrt{\frac{2}{\tau}} \sin\left\{\omega_{c}t + \mu \pi t^{2}\right\}, \qquad -\frac{\tau}{2} \le t \le \frac{\tau}{2} \qquad (16)$$

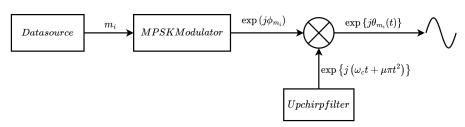


Figure 1. Block diagram describing the proposed MPSK CSS modulation scheme.

Information 2023, 14, 323 6 of 15

In the following section, we establish a relationship between the number of signals that can be overlapped and the number k bits per symbol. This also helps in selecting the ideal MPSK scheme.

4.2. Overlapping Chirps

DM allows signals to overlap to increase the data rate. The overlap is achieved when the symbol duration τ is less than the chirp duration τ_{ch} . Therefore, the pulse for the next symbol is sent by the transmitter before the signal of the current symbol has fully propagated [24]. The number η of overlapping chirps in a chirp duration is given by Equation (17).

$$\eta = \frac{\tau_{ch}}{\tau} \tag{17}$$

We consider a DM CSS system with fixed bandwidth B_{ch} and chirp duration τ_{ch} . We aim to determine an optimal symbol time τ for which several symbols can be transmitted within a single chirp time without altering the overall system performance. Obviously, the smaller the symbol period, the more signals can be transmitted in a single chirp duration, as illustrated in Figure 2.

However, transmitting many overlapped signals may cause adjacent signals to interfere, thus making detection difficult at the receiver.

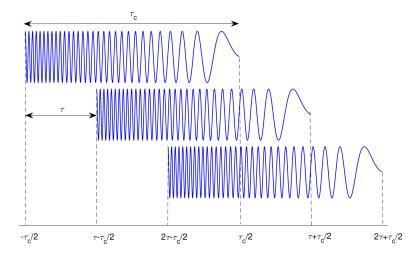


Figure 2. Illustration of overlapping transmission with the number of overlapped signals $\eta = 3$.

To determine the optimal symbol duration τ , we model as a right triangle the time-frequency representation of the instantaneous frequency of a linear chirp. The hypotenuse, opposite side, and adjacent side of the right triangle represent the instantaneous frequency of the chirp signal, the system bandwidth, and the chirp duration, respectively. Figure 3 illustrates a model representation wherein two chirps with symbol durations $\tau < \tau_{ch}$ and $\tau = \tau_{ch}$ are displayed. The angle α is inversely proportional to the symbol duration τ and, hence, to the time–bandwidth product $B_{ch}\tau$. Let us denote by α_{\min} the value of α at which $\tau = \tau_{ch}$, and by α_{\max} the value at which τ is the smallest ($\tau << \tau_{ch}$). At $\alpha = \alpha_{\max}$, τ becomes smaller such that the area $A = \frac{1}{2} \frac{B_{ch}}{f_c} \frac{1}{\eta_{\max}}$ of the triangle of Figure 3 is smaller than 1. Since $\frac{B_{ch}}{f_c} < \frac{1}{2}$ (we assume the Nyquist criterion, $f_c > 2B_{ch}$, is met) and $\eta_{\max} >> 1$, chirp signals will overlap in the time frame τ_{ch} .

From Figure 3, we derive η as function of $\tan \alpha$. However, the tangent function $\tan (.)$ is not defined for $\alpha = \frac{(2p+1)\pi}{2}$ with $p \in \mathbb{N}$ and is periodic with a period of π . In addition, the total sum of the angles in the right triangle of Figure 3 is π (or 180°). This restricts the value of α to $0 < \alpha < \frac{\pi}{2}$. Given that the bandwidth B_{ch} and chirp duration τ_{ch} are fixed and

Information **2023**, 14, 323 7 of 15

known, we express in Equations (18) and (19) η and τ as a function of α , where the interval $\left[\frac{5\pi}{34}; \frac{\pi}{2}\right)$ is an approximation. One can easily observe that $\eta \approx 1$ when $\alpha = \frac{5\pi}{34}$.

$$\eta = \frac{f_c}{B_{ch}} \tan \alpha,\tag{18}$$

$$\tau = \frac{B_{ch}\tau_{ch}}{f_c} \frac{1}{\tan \alpha'}, \qquad \frac{5\pi}{34} \le \alpha < \frac{\pi}{2}$$
 (19)

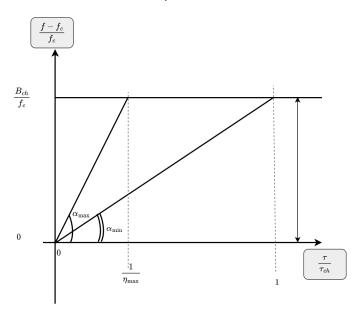


Figure 3. Time–frequency representation of the instantaneous frequency of up-chirp signals with normalized time and frequency axes.

4.3. Inter-Symbol Interference Due to Overlap

Although the overlap technique increases the spectral efficiency, it may cause more inter-symbol interference, leading to serious degradation of BER [21–23,25,26]. Therefore, a reasonable tradeoff between spectral efficiency and ISI is required. T. Yoon et al. [23] proposed a theoretical expression for the BER of a CSS overlap system to help choose the optimal number of overlaps. The authors in [21] also proposed a BER expression for a DM CSS system with a finite number of overlaps and investigated the conditions under which the ISI can be minimized while approaching the Nyquist rate. In [22], T. Yoon et al. proposed an explicit expression for ISI due to overlaps in DM CSS with BPSK and discussed the relationship between ISI and the number of overlaps.

The time-shift property of chirp signals helps mitigate inter-symbol interference between successive signals, which are transmitted every τ . DM CSS with MPSK sends each signal $\Delta \tau = \tau_{ch} - \tau$ before the previous signal evaporates from the filter. In this case, ISI is more likely to occur when $\Delta \tau$ is larger. We consider transmission over channels with additive white Gaussian noise. The expression of the received signal x(t) during the chirp duration τ_{ch} is given in Equation (20). Since DM CSS involves only an up-chirp for spreading, the impulse response of the matched filter at the receiver side is a down-chirp, which is expressed as $c_-(t) = \exp\left\{j(\omega_c t - \mu \pi t^2)\right\}$.

$$x(t) = \Re \left\{ \sum_{i=1}^{\eta} h_{\tau}(t - i\tau) \left(s_{m_i I}(t) U_I(t) + s_{m_i Q}(t) U_Q(t) \right) + n(t) \right\} - \frac{\tau_{ch}}{2} \le t \le \frac{\tau_{ch}}{2} \quad (20)$$

When the received signal passes through the matched filter, the output $y(m\tau) = y_s(m\tau) + y_n(m\tau)$, sampled at $t = m\tau$, is obtained. Figure 4 illustrates the signal detection process of the MPSK CSS: $y_s(m\tau)$ is the signal component described by Equation (22), where

Information 2023, 14, 323 8 of 15

 $y_e(m\tau)$ is the complex envelope of $y(m\tau)$, $y_n = \Re\{y_{n_e}(m\tau)\}$ is the noise component, and $\Gamma = \omega_c + \mu \pi m \tau$. For more details on $y(m\tau)$, see Appendix A.

$$y_e(m\tau) = \underbrace{\int_{-\infty}^{\infty} s(t)c_-(t-m\tau)dt}_{y_{s_e}(m\tau)} + \underbrace{\int_{-\infty}^{\infty} n(t)c_-(t-m\tau)dt}_{y_{n_e}(m\tau)}$$
(21)

$$y_s(m\tau) = \Re\{y_{s_e}(m\tau)\} = \Re\left\{\sum_{i=1}^{\eta} \sqrt{\frac{2E_s}{\tau}} \exp\left(j\phi_{m_i}\right) \exp\left\{-j\Gamma m\tau + 2j\Gamma i\tau\right\} \frac{\exp\left\{j\tau\Gamma\right\} - \exp\left\{-j\tau\Gamma\right\}}{2j\Gamma}\right\}$$

$$y_s(m\tau) = \Re\left\{\sum_{i=1}^{\eta} \sqrt{\frac{2E_s}{\tau}} \exp\left\{j\phi_{m_i}\right\} \exp\left\{j(2i-m)\tau\Gamma\right\}\tau sinc(\tau\Gamma)\right\}$$
 (22)

Let
$$y_{s_{m_i}} = \sqrt{E_s} \exp(j\phi_{m_i})$$
 and $z_{i-m} = \sqrt{\frac{2}{\tau}} \exp\{j(2i-m)\tau\Gamma\}\tau sinc(\tau\Gamma)$.

$$\Rightarrow y_s(m\tau) = \Re\left\{ y_{s_{m_m}} z_0 + \underbrace{\sum_{i=1, i \neq m}^{\eta} y_{s_{m_i}} z_{i-m}}_{\Delta_m} \right\}, \tag{23}$$

where Λ_m is the inter-symbol interference due to the overlap of the m-th symbol with the others.

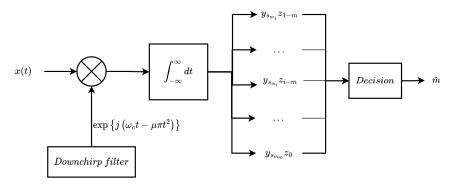


Figure 4. Block diagram illustrating the MPSK CSS detection process.

4.4. Zero-ISI Transmission

According to the Nyquist criterion for zero-ISI transmission, $z_{i-m} = 0$ for m > 0. If this condition is satisfied, the symbol duration should satisfy Equation (25).

$$\forall i \neq m, \quad z_{i-m} = 0 \Rightarrow sinc(\tau\Gamma) = 0,$$

$$\sin\left\{2\pi f_c \tau + \mu \pi m \tau^2\right\} = \sin\left\{p'\pi\right\}, \quad \forall p' \in \mathbb{N}$$

$$\Rightarrow 2\pi f_c \tau + \frac{B_{ch}}{\eta} \pi m \tau = p'\pi$$

$$\tau = \frac{\eta p'}{2f_c \eta + m B_{ch}},$$
(25)

where the number of overlaps η was formulated in Equation (18).

Information **2023**, 14, 323 9 of 15

4.5. Probability of Bit Error

This section provides the theoretical bit error rate derivation. For simplicity and without any loss of generality, we denote the index of the symbol being detected as m. We recall $y(m\tau) = y_{s_m}z_0 + \Lambda_m + y_n(m\tau)$ is the receiver output at time $t = m\tau$, where $y_n = \Re\{y_{n_e}\}$ and $y_n \sim \mathcal{N}(0, \frac{N_0}{2})$.

We also denote by H_{m_i} the hypothesis that the symbol s_{m_i} was transmitted and by $f(y|H_{m_i})$ the conditional probability density function of y at H_{m_i} . The random variable y is Gaussian with mean $(y_{s_m}z_0 + \Lambda_m)$ and variance $\frac{N_0}{2}$.

We are interested in finding the bit error probability P_b due to an overlap. Let P_{SER} be the average probability of error for transmitting η overlapped signals. Since the η symbols are equally likely to be sent, then the probability of the symbol s_{m_i} being transmitted is $P(H_{m_i}) = \frac{1}{\eta}$. $P(y|H_{m_i})$ is the probability of detecting the right symbol knowing that H_{m_i} is true.

$$P_{SER} = 1 - \sum_{i=1}^{\eta} P(H_{m_i}) P(y|H_{m_i})$$
 (26)

$$P(y|H_{m_i}) = \iint_{R_{m_i}} f(y|R_{m_i}), \tag{27}$$

where R_{m_i} is the decision region of the symbol s_{m_i} . In [27], it is shown that the average probability P_{SER} is upper bounded as given in Equation (28):

$$P_{SER} \le \sum_{i=1, m_i \ne m}^{\eta} Q\left(\frac{d_{mm_i}}{\sqrt{2N_o}}\right),\tag{28}$$

where d_{mm_i} is the Euclidean distance between s_m and s_{m_i} and is expressed in Equation (29) (Appendix B.1 provides more details).

$$d_{mm_i} = 2\sqrt{E_s \sin^2\left(\frac{(m - m_i)\pi}{2M}\right)} \tag{29}$$

By replacing the expression of d_{mm_i} in Equation (28), we obtain in Equation (30) the new expression of the probability P_{SER} .

$$P_{SER} \approx \sum_{i=1, m_i \neq m}^{\eta} Q\left(\sqrt{2\frac{E_s}{N_o}\sin^2\left(\frac{(m-m_i)\pi}{2M}\right)}\right)$$
(30)

Finally, an approximation of the average probability of bit error is provided by Equation (31).

$$P_b \approx \sum_{i=1, m_i \neq m}^{\eta} \frac{1}{2 \log_2(M)} erfc \left(\sqrt{2 \log_2(M) \frac{E_b}{N_o} \sin^2 \left(\frac{(m-m_i)\pi}{2M} \right)} \right)$$
(31)

5. Performance Analysis and Discussion

5.1. Simulation Environment

The main parameters of the simulations are the bandwidth $B_{ch} = 200$ kHz, the chirp duration $\tau_{ch} = 0.05$ ms, the total number of symbols $M \in \{4, 8, 16\}$, and a data stream of 10^5 bits. The simulation was done on MATLAB and under additive white Gaussian noise (AWGN) channels with a stationary transmitter/receiver over the specified bandwidths. The performance metrics considered are the spectral efficiency and the bit error rate.

Information 2023, 14, 323 10 of 15

5.2. Spectral Efficiency Analysis

In this paper, we aim to prove that for a given bandwidth B_{ch} and chirp duration τ_{ch} , one can achieve better data rate performance if the symbol duration is set efficiently. The bit rate of an MPSK system is given by $R_b = \frac{\log_2(M)}{\tau_{ch}}$. Since we consider overlapping transmission, the symbol duration expressed by $\tau = \frac{\tau_{ch}}{\eta}$ leads to the new theoretical bitrate formulation as in Equation (32).

$$R_b = \frac{f_c \log_2(M)}{B_{ch} \tau_{ch}} \tan \alpha, \qquad \frac{5\pi}{34} \le \alpha < \frac{\pi}{2}$$
 (32)

The choice of the symbol duration τ is a function of η . Since $\tau = \frac{\tau_{ch}}{\eta}$ and τ_{ch} is fixed, the time symbol is inversely proportional to η : τ becomes smaller as η tends to ∞ . Therefore, if we suppose there is no interference, the spectral efficiency depends mainly on η , and the larger η is, the higher the spectral efficiency of the system. The values of η in Table 1 are generated from α , based on Equation (18) with $f_c = 2B_{ch}$. Because in this study the number η of overlaps is an integer, we compute the floor of the real-valued η generated.

Figure 5 illustrates the theoretical bit rates of the system under interference and noise. The plotted results are the Shannon's channel capacities for some α provided in Table 1. These curves represent the number of correctly detected bits against E_b/N_0 for α values in $\{\frac{3\pi}{10}, \frac{\pi}{3}, \frac{3\pi}{8}, \frac{2\pi}{5}, \frac{5\pi}{12}\}$. Figure 5 shows that as the angle α increases, the bit rate decreases. At $E_b/N_0=20$, the bit rate of $\alpha=\frac{3\pi}{10}$ is about 1.5 times more than those of $\alpha=\frac{5\pi}{12}$, which is a gap of about 7 Mbit/s. From these results, we conclude that it is preferable not to overlap more than 4 signals.

Table 1. Number η of overlaps as function of α when $\frac{f_c}{B_{ch}} = 2$.

α	$\frac{\pi}{6}$	$\frac{\pi}{5}$	$\frac{\pi}{4}$	$\frac{3\pi}{10}$	$\frac{\pi}{3}$	$\frac{3\pi}{8}$	$\frac{2\pi}{5}$	$\frac{5\pi}{12}$
tan α	$\frac{\sqrt{3}}{3}$ 1.1547	$\sqrt{5-2\sqrt{5}}$ 1.4531	1 2.0	$\frac{\sqrt{25+10\sqrt{5}}}{5}$ 2.7528	$\sqrt{3}$ 3.4641	$\sqrt{2} + 1$ 4.8284	$\sqrt{5+2\sqrt{5}}$ 6.1554	$2 + \sqrt{3}$ 7.4641
$\lfloor \overset{\prime}{\eta} \rfloor$	1	1	2	2	3	4	6	7

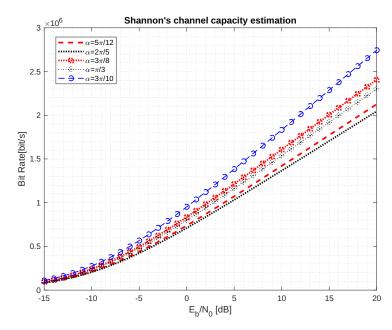


Figure 5. Comparison of Shannon's channel capacity as function of E_b/N_0 and α .

Information 2023, 14, 323 11 of 15

5.3. BER Performance Analysis

The overlap of symbols can lead to inter-symbol interference, which can affect the system performance. Therefore, the effects of interference due to overlapping are taken into account when evaluating the spectral efficiency. The curves of the theoretical bit error, obtained from Equation (31), are plotted against the E_b/N_0 in Figure 6 along with the measured values in order to analyse the effects of inter-symbol interference caused by the number of chirp overlaps η . Several values of η (from 1 to 5) are considered, as well as 3 values of M (4, 8, and 16) of the MPSK modulation.

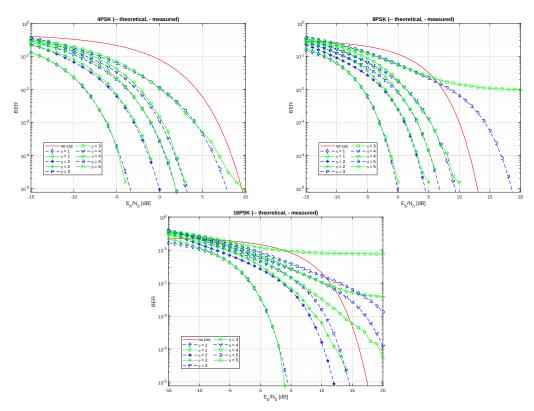


Figure 6. Theoretical and measured BER as a function of E_b/N_0 for MPSK CSS with $B_{ch}=200$ kHz.

It is worth noting that for a relatively reduced number of overlaps, the theoretical curves fit well with the measured ones, but there are also some discrepancies, especially for higher-order modulations (M=16). Indeed, although the proposed approach is able to mitigate the effects of inter-symbol interference due to chirp overlaps, as demonstrated in Section 4.4, in practice, the interference is not completely removed due to some signal processing imperfections. Actually, these discrepancies are due to the residual inter-symbol interference, which increases as the number of chirp overlaps and the modulation order increase. The effect of the residual inter-symbol interference is more visible for high signal-to-noise ratios (SNRs), while it is masked by the noise for low SNRs.

Along with the results presented in Section 5.2, the curves in Figure 6 can be used to select an appropriate value for the number of chirp overlaps. Thus, for example, we can conclude that a 16-PSK CSS system with a bandwidth of 200 kHz is likely to achieve higher spectral efficiency and a good tradeoff between BER and bit rate performance when the number of chirps overlapped $\eta \in \{2,3\}$.

A comparison of the proposed model with modulation schemes such as the quadrature amplitude modulation (QAM) is also provided in Figure 7.

Information 2023, 14, 323 12 of 15

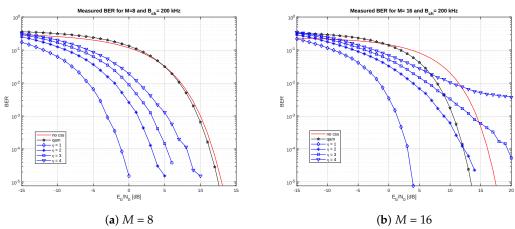


Figure 7. Measured BER as a function of E_b/N_0 for PSK, QAM, and PSK CSS with $\eta \in \{2,3,4\}$.

6. Conclusions

This work arose from the requirement to optimize data transmission as well as to minimize energy consumption in wireless sensor networks. Our previous article [3] addressed the same optimization challenges and proposed a routing protocol based on hypergraph clustering. However, the routing scheme might not be effective if the physical layer of each sensor node comprises a high-bandwidth radio transceiver, such as 5G.

Therefore, in this work, we combined M-ary phase shift keying and chirp spread spectrum modulation techniques to develop bandwidth-efficient modulation for wireless sensors networks. MPSK modulation enables the transmission of $\log_2(M)$ bits per symbol, while CSS helps transmit η symbols in a single chirp time τ_{ch} . The time–frequency representation of the instantaneous frequency of a chirp, along with some mathematical properties, are used to model the time symbol τ and the number η of overlaps as a function of a non-right angle α . We derived the expression BER as a function of η to analyse and mitigate the effects of inter-symbol interference due to overlaps. We evaluated the proposed model in terms of spectral efficiency and bit error probability. Simulation results showed that the best system performance, in terms of tradeoff between the bit rate and BER, is achieved when $2 \le \eta \le 3$ for a 16-PSK CSS with a 200 kHz-bandwidth. As future work, we plan to develop a standard mathematical formulation of the optimal number η of overlaps for a given bandwidth B_{ch} , chirp time τ_{ch} , number of symbols M, signal-to-noise E_b/N_0 , and data stream size. We also plan to take into account user mobility and study its impact on the system's BER.

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Information 2023, 14, 323 13 of 15

Abbreviations

The following abbreviations are used in this manuscript:

AWGN Additive White Gaussian Noise
BER Bit Error Rate
BOC Binary Offset Carrier
BOK Binary Orthogonal Keying
CCC Cross Correlation Coefficients

CSS Chirp Spread Spectrum
DM CSS Direct Modulation Chirp Spread Spectrum

ISI Inter-Symbol Interference MPSK M-ary Phase Shift Keying

Appendix A. Expression of the Receiver Output

The signal of interest at the input of the matched filter during the chirp duration τ_c can be expressed as:

$$s(t) = \Re\left\{\sum_{l=1}^{\eta_c} \sqrt{\frac{2E_s}{\tau}} h_{\tau}(t - l\tau) \exp\left\{j\phi_i\right\} \exp\left\{j\left(\omega_c t + \mu \pi t^2\right)\right\}\right\}$$
(A1)

Consequently, the signal at the receiver output at $t = m\tau$ is given by:

$$y_{e}(m\tau) = \int s(t)c_{-}(t-m\tau)dt + \int n(t)c_{-}(t-m\tau)dt$$

$$= \underbrace{\int \sum_{l=1}^{\eta_{c}} h_{\tau}(t-l\tau)s_{i}(t)c_{-}(t-m\tau)dt}_{y_{s_{e}}(m\tau)} + \int n(t)c_{-}(t-m\tau)dt$$
(A2)

Let us now develop the first term of (A2):

$$y_{s_e}(m\tau) = \sum_{l=1}^{\eta_c} \int_{-\infty}^{\infty} h_{\tau}(t - l\tau) s_i(t) \exp\left\{j(\omega_c(t - m\tau) - \mu\pi(t - m\tau)^2)\right\} dt$$

$$= \sum_{l=1}^{\eta_c} \sqrt{\frac{2E_s}{\tau}} \int_{-\infty}^{\infty} h_{\tau}(t - l\tau) \exp\left(j\phi_i\right) \exp\left\{2\omega_c t + 2\mu\pi m\tau t - \omega_c m\tau - \mu\pi m^2\tau^2\right\}$$

$$= \sum_{l=1}^{\eta_c} \sqrt{\frac{2E_s}{\tau}} \exp\left\{j\phi_i\right\} \exp\left\{-j\Gamma m\tau\right\} \int_{-\infty}^{\infty} h_{\tau}(t - l\tau) \exp\left\{2j\Gamma t\right\} dt \tag{A3}$$

with $\Gamma = \omega_c + \mu \pi m \tau$, and $h_{\tau}(t - l\tau) = \begin{cases} 1 & \text{if } l\tau - \frac{\tau}{2} \leq t \leq l\tau + \frac{\tau}{2} \\ 0 & \text{elsewhere} \end{cases}$.

Thus, we further obtain:

$$y_{s_e}(m\tau) = \sum_{l=1}^{\eta_c} \sqrt{\frac{2E_s}{\tau}} \exp(j\phi_i) \exp\{-j\Gamma m\tau\} \exp\{2j\Gamma l\tau\} \frac{\exp\{j\tau\Gamma\} - \exp\{-j\tau\Gamma\}}{2j\Gamma}$$
$$= \sum_{l=1}^{\eta_c} \sqrt{\frac{2E_s}{\tau}} \exp(j\phi_i) \exp\{j(2l-m)\Gamma\tau\} \tau sinc\{\tau\Gamma\}$$
(A4)

Information 2023, 14, 323 14 of 15

Let $y_{s_i} = \sqrt{\frac{2E_s}{\tau}} \exp\{j\phi_i\}$ and $z_{l-m} = \exp\{j(2j-m)\tau\Gamma\}\tau sinc\{\tau\Gamma\}$. We finally obtain:

$$y_{s_e}(m\tau) = y_{s_{m_m}} z_0 + \sum_{l=1, i \neq m}^{\eta_c} y_{s_i} z_{i-m}$$
(A5)

Appendix B. Probability of Bit Error

Appendix B.1. Euclidean Distance between s_m and s_{s_m}

The Euclidean distance between $s_m(\sqrt{E_s}\cos(\phi_m), -\sqrt{E_s}\sin(\phi_m))$ and $s_{m_i}(\sqrt{E_s}\cos(\phi_{m_i}), -\sqrt{E_s}\sin(\phi_{m_i}))$ is:

$$d_{mm_i} = \sqrt{\left(\sqrt{E_s}cos(\phi_m) - \sqrt{E_s}\cos(\phi_{m_i})\right)^2 + \left(-\sqrt{E_s}\sin(\phi_m) + \sqrt{E_s}\sin(\phi_{m_i})\right)^2}$$

Simplifying this expression, we obtain:

$$\begin{split} d_{mm_{i}} &= \sqrt{E_{s}(\cos(\phi_{m}) - \cos(\phi_{m_{i}}))^{2} + E_{s}(-\sin(\phi_{m}) + \sin(\phi_{m_{i}}))^{2}} \\ &= \sqrt{E_{s}(\cos^{2}(\phi_{m_{i}}) + \sin^{2}(\phi_{m_{i}}) + \cos^{2}(\phi_{m}) + \sin^{2}(\phi_{m}))} \\ &+ \sqrt{E_{s}(-2\cos(\phi_{m})\cos(\phi_{m_{i}}) - 2\sin(\phi_{m})\sin(\phi_{m_{i}}))} \\ &= \sqrt{E_{s}(2 - 2\cos(\phi_{m})\cos(\phi_{m_{i}}) - 2\sin(\phi_{m})\sin(\phi_{m_{i}}))} \\ &= \sqrt{2E_{s}(1 - \cos(\phi_{m})\cos(\phi_{m_{i}}) - \sin(\phi_{m})\sin(\phi_{m_{i}}))} \\ &= \sqrt{2E_{s}(1 - \cos(\frac{m\pi}{M} - \frac{m_{i}\pi}{M}))} \end{split}$$

Therefore, the Euclidean distance between s_m and s_{m_i} is:

$$d_{mm_i} = 2\sqrt{E_s \sin^2\left(\frac{(m-m_i)\pi}{2M}\right)} \tag{A6}$$

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