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Population of ground and lowest excited states of Sulfur via the dissociative recombination of SH^+ in the diffuse interstellar medium

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Our previous study on dissociative recombination of ground state SH^+ into $^2\Pi$ states of SH is extended by taking into account the contribution of $^4\Pi$ states recently explored by quantum chemistry methods. Multichannel quantum defect theory is employed for the computation of cross sections and rate coefficients for dissociative recombination, but also for vibrational excitation. Furthermore, we produce the atomic yields resulting from recombination, quantifying the generation of sulfur atoms in their ground (3P) and lowest excited (1D) states respectively.

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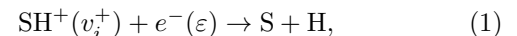
I. INTRODUCTION

SH^+ (sulfoniumylidene or sulfanylium) is ubiquitous in the Interstellar Medium (ISM). It has been detected in emission in W3 IRS 5, a region of high-mass star formation [1], in absorption in the diffuse interstellar medium, towards various distant star-forming regions [2, 3] and in emission in the Orion Bar, a typical high UV-illumination warm and dense photon-dominated region (PDR) [4].

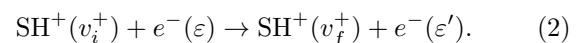
Thanks to this ubiquity, the SH^+ ion provides unique physical and chemical constraints on models that are applied to the environments where it is observed. SH^+ is suggested to form from the reaction of atomic S^+ with H_2 . However this reaction is highly endothermic by 0.86 eV (9860 K). To overcome this endothermicity in the diffuse ISM, turbulent dissipation, shocks, or shears are invoked. As a consequence, SH^+ is suggested as an important probe of turbulence [3, 5] of the diffuse ISM. In photon dominated region where H_2 is vibrationally excited, it is suggested that this excess of vibrational energy allows the formation of SH^+ from S^+ and H_2 [6], providing information on the temperature of such environments. However, for SH^+ to be used as a tracer of the physical conditions of the media where it is observed, its chemistry needs to be known in detail and in particular

its destruction mechanisms. SH^+ does not react quickly with H_2 [7] the most abundant interstellar molecule due to the endothermicity of the reaction, and therefore it is not severely depleted through this reaction. It is therefore considered that dissociative recombination (DR) of this ion with electrons (eq. (1)) is an efficient destruction pathway, and a rate constant of $10^{-6} \text{ cm}^3 \cdot \text{s}^{-1}$ is assigned to this reaction in the KIDA and UMIST astrochemical data bases [8, 9]. To validate this assumption we have started few years ago an extensive and accurate study of the DR of SH^+ using methods of theoretical chemistry and quantum dynamics [10]. The large variety of theoretical studies undertaken on SH^+ as well as on SH can be found in our previous papers [10, 11].

In the present article, we aim to increase the accuracy of our previous computations [10] on the dissociative recombination of the ground-state SH^+ :



taking into account the new molecular structure data characterizing the states of $^4\Pi$ symmetry of SH [11]. In addition, we calculate atomic yields produced via the DR process, resulting in the formation of the atomic sulphur in its ground state - 3P - and in its lowest excited state - 1D - and we produce cross sections and thermal rate coefficients for the vibrational excitation (VE) of the ion:



in competition with its DR. Here v_i^+/v_f^+ stand for the initial/final vibrational quantum numbers of the cation

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and ε/ε' the kinetic energy of the incident/scattered electrons.

The paper is organized as follows: Section II describes the MQDT method and the molecular data set used in the dynamical calculations. Section III presents the obtained dissociative recombination and vibrational excitation cross sections and thermal rate constants, as well as the estimated atomic yields and branching ratios. Section IV contains the concluding remarks.

II. THEORETICAL BACKGROUND

The MQDT approach has been proven to be a powerful method for the evaluation of the cross sections of the DR [12–14] and competitive processes like ro-vibrational and dissociative excitations. It was applied with great success to several diatomic systems like H_2^+ and its isotopologues [15–22], O_2^+ [23, 24], NO^+ [25–29], CO^+ [30], N_2^+ [31, 32], BF^+ [33], triatomics like H_3^+ [34–36], BF_2^+ [37] and complex organic molecules [38].

A. MQDT method

The theoretical summary given below is limited to the account of the *vibrational* structure and couplings of SH^+ and SH , the rotational effects being neglected, and focuses on DR - equation (1). However, the reader should keep in mind that the other competitive processes (eq. (2)) - such as *superelastic collision or vibrational de-excitation* (SEC or VdE) ($v_i^+ > v_f^+$), and *inelastic collision or vibrational excitation* (IC or VE) ($v_i^+ < v_f^+$) - occur simultaneously and display quite similar features.

The DR results from the quantum interference between the *direct* mechanism, involving the doubly excited resonant states SH^{**} and the *indirect* one, occurring via Rydberg singly-excited predissociating states SH^* .

The MQDT treatment of DR and VE requires the a priori knowledge of the potential energy curves (PECs) of the ion (ground and excited states), the relevant doubly excited dissociative states of the neutral molecule, and the series of mono-excited Rydberg states - of ground and excited ionic core - conveniently represented by their quantum defects. The driving forces of the DR and VE are the electronic couplings connecting the ionization continuum to the dissociation one.

A detailed description of our theoretical approach was given in [31, 38], its main steps are the following:

i) Building of the interaction matrix \mathcal{V} : For a given symmetry Λ of the neutral (electron + ion (*core*)) system and assuming that only one partial wave of the incident electron contributes to the relevant interactions, the geometry(R)-dependent electronic coupling of an ionization channel relying on the electronic-core state c_β ($\beta = 1$ for the ground state (core 1) and $\beta = 2$ for the excited state (core 2)) with the dissociation channel d

can be written:

$$\mathcal{V}_{d,c_\beta}^{(e)\Lambda}(R) = \langle \Phi_d | H_{el} | \Phi^{el,c_\beta} \rangle, \quad \beta = 1, 2, \quad (3)$$

where $\mathcal{V}_{d,c_\beta}^{(e)\Lambda}(R)$ is assumed to be independent of the energy of the external electron.

The integration is performed over the electronic coordinates of the neutral system. Here H_{el} denotes the electronic Hamiltonian, Φ_d is the electronic wave function of the dissociative state and Φ^{el,c_β} is the wave function describing the molecular system “Rydberg electron + ion in its c_β electronic state”.

Similarly, the electronic coupling between the two ionization continua is:

$$\mathcal{V}_{c_1,c_2}^{(e)\Lambda}(R) = \langle \Phi^{el,c_1} | H_{el} | \Phi^{el,c_2} \rangle. \quad (4)$$

Integrating these couplings over the internuclear distance leads to the non-vanishing elements of the interaction matrix $\mathcal{V}(E)$:

$$V_{d,v_{c_\beta}}^\Lambda(E) = \langle F_d(E) | \mathcal{V}_{d,c_\beta}^{(e)\Lambda}(R) | \chi_{v_{c_\beta}} \rangle, \quad \beta = 1, 2. \quad (5)$$

$$V_{v_{c_1},v_{c_2}}^\Lambda = \langle \chi_{v_{c_1}} | \mathcal{V}_{c_1,c_2}^{(e)\Lambda}(R) | \chi_{v_{c_2}} \rangle. \quad (6)$$

Here $\chi_{v_{c_\beta}}$ ($\beta = 1, 2$) is the vibrational wave function associated with an ionization channel relying on the core c_β , F_d is the regular radial wave function of the dissociative state d and E is the total energy of the molecular system. This interaction is effective at small electron-ion and internuclear distances, in the reaction zone.

ii) Computation of the reaction matrix \mathcal{K} : Using the second-order perturbative solution of the Lippmann-Schwinger integral equation [29, 39, 40], written in operator form as:

$$\mathcal{K} = \mathcal{V} + \mathcal{V} \frac{1}{E - \mathbf{H}_0} \mathcal{V}, \quad (7)$$

where \mathbf{H}_0 is the Hamiltonian of the molecular system under study, with the inter-channel interactions neglected. The reaction matrix \mathcal{K} in block form is:

$$\mathcal{K} = \begin{pmatrix} \mathcal{K}_{\bar{d}\bar{d}} & \mathcal{K}_{\bar{d}\bar{v}_{c_1}} & \mathcal{K}_{\bar{d}\bar{v}_{c_2}} \\ \mathcal{K}_{\bar{v}_{c_1}\bar{d}} & \mathcal{K}_{\bar{v}_{c_1}\bar{v}_{c_1}} & \mathcal{K}_{\bar{v}_{c_1}\bar{v}_{c_2}} \\ \mathcal{K}_{\bar{v}_{c_2}\bar{d}} & \mathcal{K}_{\bar{v}_{c_2}\bar{v}_{c_1}} & \mathcal{K}_{\bar{v}_{c_2}\bar{v}_{c_2}} \end{pmatrix}, \quad (8)$$

where the collective indices \bar{d} , \bar{v}_{c_1} , \bar{v}_{c_2} span the ensembles of all individual indices d , v_{c_1} and v_{c_2} , which respectively label dissociation channels, ionization channels built on core 1 and ionization channels built on core 2.

An extensive and rigorous derivation of the structure of each block of the \mathcal{K} -matrix in second order for a multi-core case was provided in our earlier work [41]. For SH^+ , with two attractive ion cores, a natural application of our

earlier work leads to the following form of the \mathcal{K} -matrix in second order:

$$\mathcal{K} = \begin{pmatrix} \mathbf{O} & \mathbf{V}_{\bar{d}\bar{v}_{c_1}} & \mathbf{V}_{\bar{d}\bar{v}_{c_2}} \\ \mathbf{V}_{\bar{v}_{c_1}\bar{d}} & \mathcal{K}_{\bar{v}_{c_1}\bar{v}_{c_1}}^{(2)} & \mathbf{V}_{\bar{v}_{c_1}\bar{v}_{c_2}} \\ \mathbf{V}_{\bar{v}_{c_2}\bar{d}} & \mathbf{V}_{\bar{v}_{c_2}\bar{v}_{c_1}} & \mathcal{K}_{\bar{v}_{c_2}\bar{v}_{c_2}}^{(2)} \end{pmatrix}, \quad (9)$$

where the elements of the diagonal blocks of \mathcal{K} are:

$$K_{v_{c_\beta} v_{c_\beta}}^{\Lambda(2)} = \frac{1}{W_d} \int \int \left[\chi_{v_{c_\beta}}^\Lambda(R) \mathcal{V}_{c_\beta, d}^{(e)\Lambda}(R) F_d(R_{<}) \times G_d(R_{>}) \mathcal{V}_{d, c_\beta}^{(e)\Lambda}(R') \chi_{v_{c_\beta}}^\Lambda(R') \right] dR dR'. \quad (10)$$

Here W_d is the Wronskian between the regular (F_d) and irregular (G_d) solutions at the origin of the nuclear Schrödinger equation, $R_{<} = \min(R, R')$ and $R_{>} = \max(R, R')$, while $\beta = 1, 2$.

iii) Computation of the eigenchannel wave functions: It relies on the eigenvectors and eigenvalues of the reaction matrix \mathcal{K} , i.e. the columns of the matrix \mathbf{U} and the elements of the diagonal matrix $\mathbf{tan}(\boldsymbol{\eta})$ respectively:

$$\mathcal{K}\mathbf{U} = -\frac{1}{\pi} \mathbf{tan}(\boldsymbol{\eta})\mathbf{U}, \quad (11)$$

where the non-vanishing elements of the diagonal matrix $\boldsymbol{\eta}$ are the phase shifts introduced into the wave functions by the short-range interactions.

iv) Frame transformation from the Born-Oppenheimer representation to the close-coupling one: It is performed via the matrices \mathbf{C} and \mathbf{S} , built on the basis of the matrices \mathbf{U} and $\boldsymbol{\eta}$ and on the quantum defect characterizing the incident/Rydberg electron, $\mu_i^\Lambda(R)$. The elements of these matrices are:

$$C_{v_{c_\beta}^+, \Lambda\alpha} = \sum_{v_{c_\beta}} U_{v_{c_\beta}, \alpha}^\Lambda \left\langle \chi_{v_{c_\beta}^+}^\Lambda(R) \left| \cos\left(\pi\mu_{c_\beta}^\Lambda(R) + \eta_\alpha^\Lambda\right) \right| \chi_{v_{c_\beta}}^\Lambda(R) \right\rangle, \quad (12)$$

$$C_{d, \Lambda\alpha} = U_{d, \alpha}^\Lambda \cos \eta_\alpha^\Lambda, \quad (13)$$

$$S_{v_{c_\beta}^+, \Lambda\alpha} = \sum_{v_{c_\beta}} U_{v_{c_\beta}, \alpha}^\Lambda \left\langle \chi_{v_{c_\beta}^+}^\Lambda(R) \left| \sin\left(\pi\mu_{c_\beta}^\Lambda(R) + \eta_\alpha^\Lambda\right) \right| \chi_{v_{c_\beta}}^\Lambda(R) \right\rangle, \quad (14)$$

$$S_{d, \Lambda\alpha} = U_{d, \alpha}^\Lambda \sin \eta_\alpha^\Lambda, \quad (15)$$

where α denotes the eigenchannels built through the diagonalization of the reaction matrix \mathcal{K} , while $\beta = 1, 2$.

v) Construction of the generalized scattering matrix $\boldsymbol{\chi}$, eventually split in blocks associated with energetically open and closed (o and c respectively) channels:

$$\boldsymbol{\chi} = \frac{\mathbf{C} + i\mathbf{S}}{\mathbf{C} - i\mathbf{S}} \quad \boldsymbol{\chi} = \begin{pmatrix} \mathbf{X}_{oo} & \mathbf{X}_{oc} \\ \mathbf{X}_{co} & \mathbf{X}_{cc} \end{pmatrix}. \quad (16)$$

vi) Construction of the physical scattering matrix \mathbf{S} , whose elements link mutually the open channels exclusively, given by [13]:

$$\mathbf{S} = \mathbf{X}_{oo} - \mathbf{X}_{oc} \frac{1}{\mathbf{X}_{cc} - \exp(-i2\pi\nu)} \mathbf{X}_{co}, \quad (17)$$

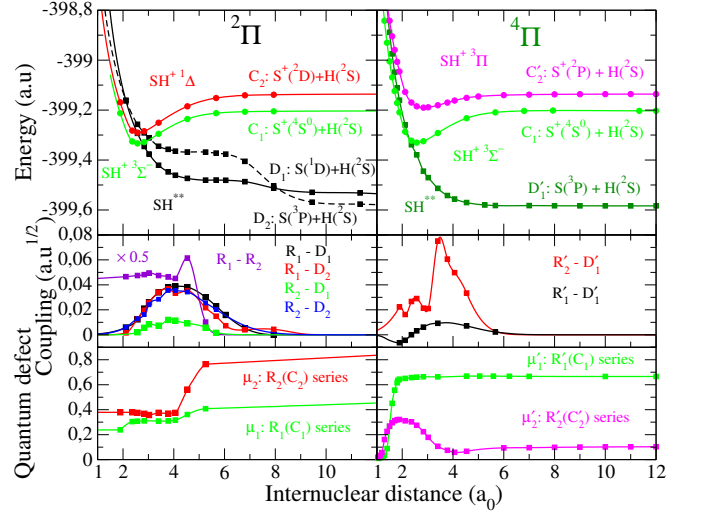


FIG. 1: Molecular structure data set: Left panels: $^2\Pi$ symmetry of SH [10], right panels: $^4\Pi$ symmetry of SH [11]. First row: PECs; Second row: Rydberg-valence and Rydberg-Rydberg electronic couplings; Third row: Quantum defects. Symbols stand for the quantum chemistry data points while solid and dashed lines represent the interpolated and extrapolated data.

where the matrix $\exp(-i2\pi\nu)$ is diagonal and relies on the effective quantum numbers ν_{v^+} associated to the vibrational thresholds of the closed channels.

vii) Computation of the cross-sections: Given the target cation on its level v_i^+ , its impact with an electron of energy ε results in DR according to the formula:

$$\sigma_{\text{diss} \leftarrow v_i^+} = \sum_{\Lambda, \text{sym}} \frac{\pi}{4\varepsilon} \rho^{\Lambda, \text{sym}} |S_{d, v_i^+}|^2, \quad (18)$$

or results in VE following the formula:

$$\sigma_{v_f^+ \leftarrow v_i^+} = \sum_{\Lambda, \text{sym}} \frac{\pi}{4\varepsilon} \rho^{\Lambda, \text{sym}} |S_{v_f^+, v_i^+} - \delta_{v_f^+, v_i^+}|^2, \quad (19)$$

where $\rho^{\Lambda, \text{sym}}$ stands for the ratio between the multiplicity of the involved electronic states of the neutral and that of the target ion.

B. Molecular data

The molecular data required by MQDT method is as follows: the PECs of the ground and excited ion states (C_1 , C_2 and C_2' in Fig.1), the PECs of the relevant dissociative autoionizing states of the neutral molecule (D_1 , D_2 and D_1'), the quantum defects characterizing the different Rydberg series of bound predissociated states (R_1 , R_2 , R_1' and R_2'), and the valence-Rydberg (R_1 - D_1 , etc.) and Rydberg-Rydberg (R_1 - R_2 , etc.) electronic couplings between the dissociation and/or the ionization channels of the neutral system.

TABLE I: Fitting parameters D and C_n used in the long-range multipole formula $D+C_n/R^n$ for the different molecular states.

Molecular state n		D	C_n
system		(Hartree)	(Hartree \times Bohr n)
SH $^+$ $^3\Sigma^-$	C_1	4 -399.20323325	-16.769107
SH $^+$ $^3\Pi$	C'_2	4 -399.13555828	-6.073002
SH** $^4\Pi$	D'_1	6 -399.58373325	89.132274
SH* $^4\Pi$	R'_1	6 -399.29465171	-232.669573
SH* $^4\Pi$	R'_2	6 -399.27473902	-146.713317

The DR cross section (Eq. 18) is extremely sensitive to the position of the crossing point between the PECs of the neutral dissociative states with respect to the PECs of the target ion. A slight change in the position of the crossing point can lead to a significant change in the predicted cross section. Furthermore, the PECs of the dissociative states must also converge to the correct asymptotic limits for large values of the internuclear distance in order to be able to clearly define them as either energetically open or closed channels. Thus special care need to be done calculating these data sets.

Only a few theoretical methods are able to provide all the necessary molecular data with the desired accuracy. Among these is the R-matrix theory [42], the complex Kohn variational method [43] and in the present case the block diagonalization method [44] combined with GAMESS suite [45].

The molecular data sets relevant for our DR and VE calculation are summarized in Fig. 1: On the left panels we present those calculated before for the $^2\Pi$ symmetry of SH [10], while on the right panel those obtained recently for the $^4\Pi$ symmetry [11]. The details for the $^2\Pi$ symmetry were given in [10] and, consequently, here we are focusing on the $^4\Pi$ symmetry. In the first row we displayed the PECs for the ground ion core (SH $^+$ X $^3\Sigma^-$: C_1 , green), for the excited ion core with $^3\Pi$ symmetry (C'_2 , magenta) and for the dissociative state of SH having $^4\Pi$ symmetry (D'_1 , dark green). In the second row we give the electronic couplings of the highly-excited Rydberg states (R'_1 in black and R'_2 in red) to the dissociative continuum (D'_1). These coupling terms are $\mathcal{V}_{d,c\beta}^{(e)\Lambda}(R)$ defined in Eqs. (3). The terms of $\mathcal{V}_{c_1,c_2}^{(e)\Lambda}(R)$ in Eqs. (4) representing the coupling between the two Rydberg series as a result of the diabaticization procedure are zero [11]. In the third row we have the quantum defects: μ'_1 (green) and μ'_2 (magenta) that describe the infinite Rydberg series of PECs, converging to the ground core (C_1) and the excited core (C'_2), respectively. The quantum defects were extracted from the Rydberg PECs, provided by the block diagonalization method.

The original diabatic potential energy curves are given by full symbols in Fig. 1. The ion and neutral PECs have been extended towards large internuclear distances by adding a $D + C_n/R^n$ multipole term to the curves.

The details for each molecular state are summarised in table I. Moreover, in order to get the NIST atomic dissociation limits we have performed a global shift of $\Delta_{\text{NIST}} = 1.45708$ Hartree for each of the PECs of the $^4\Pi$ symmetry set by preserving all other characteristics (e.g. ionization energies) of the electronic states.

The quantum chemistry electronic couplings were fitted with gaussian functions chosen to match their peak values. This procedure provides smooth functions on both ends, by considering the behaviour of the calculated couplings at small internuclear distances (left end) and by assuring a steep but continuous fall as soon as the resonant dissociative state crosses the electronic ground state of the ion (right end).

III. RESULTS AND DISCUSSION

The cross sections quantifying the major features of the DR of SH $^+$ are displayed in Figures 2 and 4. Their corresponding thermal rate coefficients - Figures 3 and 5 - are derived by convoluting the cross sections with the Maxwell distribution function for velocities v (related to incident energy of the electrons by $\varepsilon = \frac{1}{2}mv^2$) of the free electrons,

$$k(T) = \frac{8\pi}{\sqrt{m}(2\pi k_B T)^{3/2}} \int_0^{+\infty} \sigma(\varepsilon) \varepsilon \exp(-\varepsilon/k_B T) d\varepsilon, \quad (20)$$

where $\sigma(\varepsilon)$ is given by (Eq. 18), k_B is the Boltzmann constant and T is the absolute temperature of the electrons.

Figure 6 gives the yields for the produced atomic fragments S (3P)+H (2S) and S (1D) +H (2S) via the DR process by considering the most relevant $^2\Pi$ and $^4\Pi$ symmetries of SH.

Finally, Figures 7 and 8 present the vibrational excitation cross sections and rate coefficients respectively from the ground vibrational level of the ion to its two lowest excited vibrational levels, in comparison with those of the DR.

The calculations include 33 ionization channels in total corresponding to 18 vibrational levels belonging to the ground SH $^+$ X $^3\Sigma^-$ state (C_1 in Figure 1) and 15 vibrational levels belonging to the excited SH $^+$ A $^3\Pi$ state (C'_2 in Figure 1). For the incident electron we consider the p partial wave only. The calculations are performed in second order of the K-matrix and include both *direct* and *indirect* mechanisms of the studied processes. The explored range for the incident electron energy is 1 – 500 meV (with a step of 0.01 meV) and the temperature range is 10 – 1000 K.

A. Dissociative recombination

The calculated total (*direct* and *indirect* mechanisms) DR cross section for the $^4\Pi$ symmetry - blue curve in

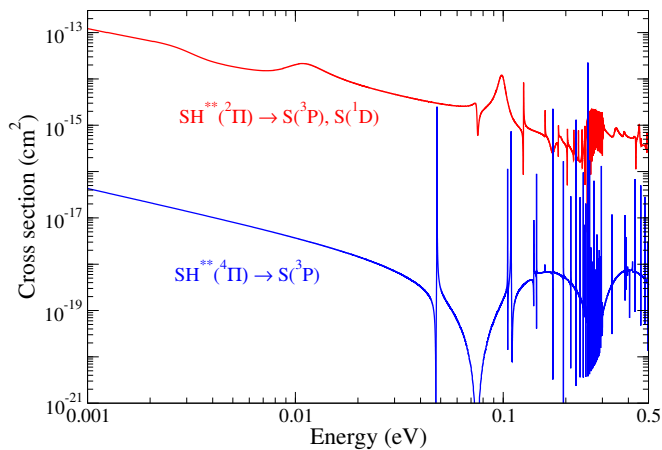


FIG. 2: Cross section for SH^+ DR into the state of $^4\Pi$ symmetry (D_1 in Figure 1, blue line) compared to that for DR into the states of $^2\Pi$ symmetry (D_1 and D_2 in Figure 1, red line).

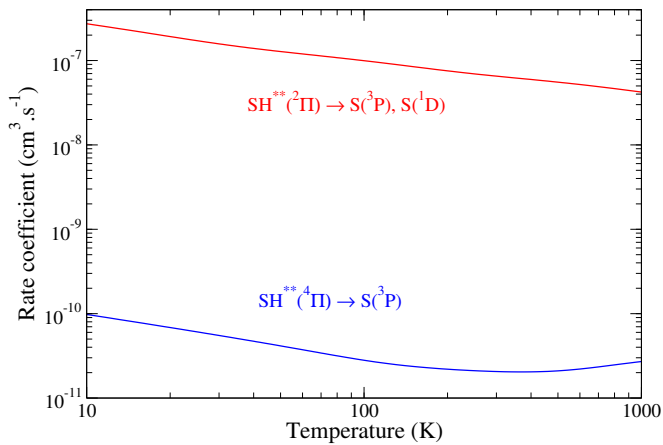


FIG. 3: Thermal rate coefficients calculated from the cross sections presented in Fig. 2.

Figure 2 - is presented and compared with the previously obtained cross sections for the $^2\Pi$ symmetry - red curve on the same figure, computed in our previous study [10]. One can clearly observe the $1/\text{energy}$ background behaviour of the DR cross sections at low collision energies for both molecular symmetries. Another typical characteristic of the total cross sections is the presence of resonance structures. They originate from the temporary capture of the incident electron into highly excited Rydberg states built on the ionic cores of PEC's C_1 and C_2 for the $^2\Pi$ symmetry and C_1 for the $^4\Pi$ one (see Figure 1).

One may notice that at low collision energies the contribution of the $^4\Pi$ symmetry is between three and four orders of magnitude smaller than that of the $^2\Pi$ symmetry, as illustrated in Fig. 3. Indeed, the $^2\Pi$ symmetry contributes with a rate around $10^{-7} \text{ cm}^3 \cdot \text{s}^{-1}$, while the $^4\Pi$ symmetry provides around a few $10^{-11} \text{ cm}^3 \cdot \text{s}^{-1}$ at

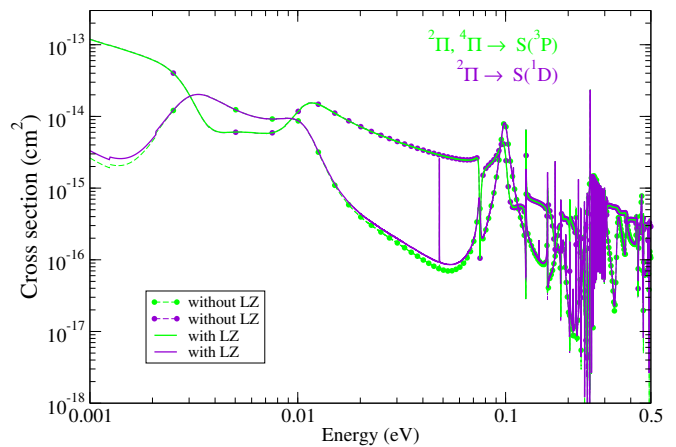


FIG. 4: DR cross sections contributing to the formation of $\text{S}(^3\text{P})+\text{H}(^2\text{S})$ (green) and $\text{S}(^1\text{D})+\text{H}(^2\text{S})$ (violet) atomic fragments. The dashed lines with circles stand for the results without the Landau-Zener (LZ) treatment, whereas the continuous lines stand for the final results, obtained following the Landau-Zener treatment.

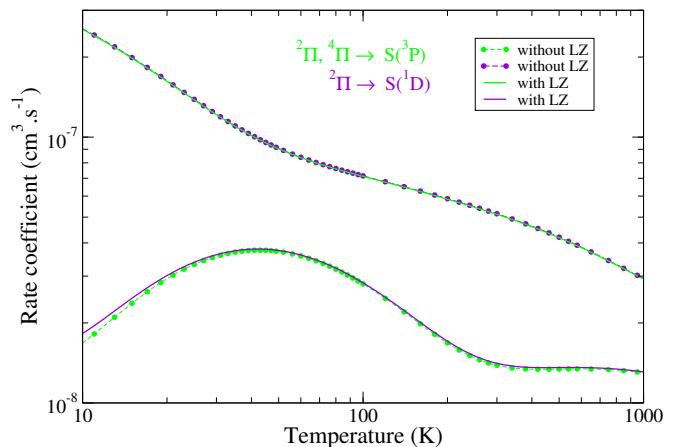


FIG. 5: Thermal rate coefficients of the production of ground and excited sulfur atoms via DR, calculated from the cross sections presented in Fig. 4. The legend is the same as that in this figure.

100 K. This can be now - after performing our calculations - explained by the less favourable crossing of the dissociative state PEC with that of the target ion one - top right-hand side part of Fig. 1 - and the relatively small valence-Rydberg electronic couplings in the Franck-Condon region, middle right-hand-side part of the same figure.

One can conclude that the $^4\Pi$ symmetry states of SH are far less important than the $^2\Pi$ ones, contrary to our expectation [10], and they do not contribute significantly to a better agreement of our theoretical results with the storage-ring experiment at very low energy.

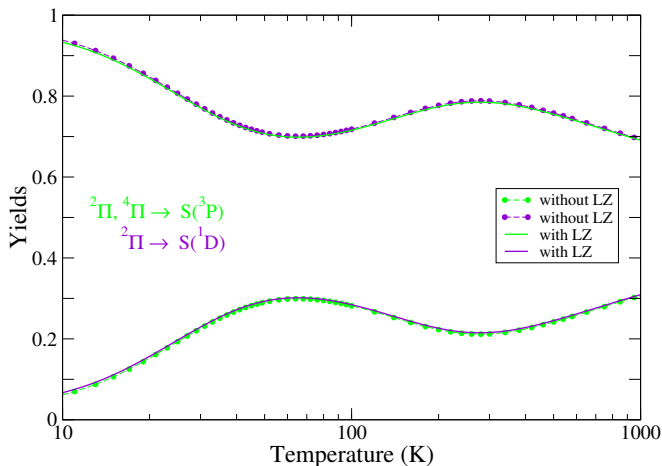


FIG. 6: Yields for the production of ground and excited sulfur atoms via DR, calculated from the rate coefficients of Fig. 5. The legend is the same as that in Fig. 4.

B. Branching ratios

In order to understand the Sulfur chemistry, besides the cross sections and thermal rate coefficients of DR, an important issue is the final state distribution of the S atoms resulting from this process.

According to Fig. 1, and neglecting - in a first step - the possibility of re-distribution of the probability flux at the crossing between the PECs of the two dissociative paths, S atoms in their ground state 3P are produced via the capture into D_2 $^2\Pi$ and D_1 $^4\Pi$ states, whereas the excited state 1D is populated via the D_1 $^2\Pi$ dissociative path.

Figs. 4 and 5 illustrate these branching ratios. One can notice that in the range 0.001–0.5 eV the cross section of generation of $S(^3P)$ atoms - green dashed lines with green circles - is overall smaller than the one obtained for $S(^1D)$ - violet dashed lines with violet circles - up to two orders of magnitude. As an exception, around 0.005 eV and around 0.09 eV collision energies, the DR cross section leading to $S(^3P)$ is higher than that of $S(^1D)$ by about one order of magnitude. The corresponding thermal rate coefficients are presented in figure 5, with the same color and symbol code. The generation of $S(^3P)$ atoms (green dashed line with green circles) has an average rate of $2 \cdot 10^{-8} \text{ cm}^3 \cdot \text{s}^{-1}$ in the temperature range 10 – 200 K. It reaches its peak value of $4 \cdot 10^{-8} \text{ cm}^3 \cdot \text{s}^{-1}$ at about 40 K, having its origin in the behaviour of the cross section in the energy range 4 – 10 meV. This rate is practically constant above 250 K. On the other hand, the rate of production of $S(^1D)$ atoms (violet line with violet circles) monotonically decrease from $2 \cdot 10^{-7} \text{ cm}^3 \cdot \text{s}^{-1}$ at 10 K to $3 \cdot 10^{-8} \text{ cm}^3 \cdot \text{s}^{-1}$ at 1000 K. Obviously, in this first-step approach, the production of $S(^1D)$ atoms dominates largely that of $S(^3P)$ atoms at low temperature.

To better compare the processes of populating the two lowest energy levels of the S atom, we present in Fig. 6

the yields resulting from the branching ratios from Fig. 5, calculated by dividing the corresponding thermal rate coefficients to the sum of both. In average, in the electron temperature range 10-1000 K, the DR process contributes to the generations of $S(^3P)$ atoms as much as 24%, and to that of $S(^1D)$ atoms with 76%.

In order to account for the flux redistribution at the crossing point ($R_0 \sim 8 a_0$) between the PECs of the D_1 and D_2 dissociative states, we performed a Landau-Zener calculation [48, 49]. The probability of transition from one diabatic branch to the other - P_{12} - is given by [50]

$$P_{12}(\varepsilon) = 1 - e^{-\frac{2\pi V_{12}^2(R_0)}{\hbar a v}}, \quad (21)$$

where $V_{12}(R_0) = 0.0314$ Hartree is the coupling element between the two dissociative states at their crossing point [10], $a = \frac{dV_1}{dR} - \frac{dV_2}{dR}$ stands for the differences of PEC slopes at the crossing point and v is the relative collisional velocity [50].

Consequently, starting from the dissociative states D_1 and D_2 (cf. the upper-left panel of Fig. 1), one obtain the cross sections $\sigma'_1(\varepsilon)$ and $\sigma'_2(\varepsilon)$ towards the $S(^3P)+H(^2S)$ and $S(^1D)+H(^2S)$ dissociation limits, respectively, according to the formulas:

$$\begin{aligned} \sigma'_1(\varepsilon) &= (1 - P_{12})\sigma_1(\varepsilon) + P_{12}\sigma_2(\varepsilon) \\ \sigma'_2(\varepsilon) &= (1 - P_{12})\sigma_2(\varepsilon) + P_{12}\sigma_1(\varepsilon). \end{aligned} \quad (22)$$

Table II contains these Landau-Zener transition probabilities P_{12} as function of the collision energy. Moreover, we display the branching ratios resulting from the cross sections convoluted with the anisotropic Maxwell distribution of the relative electron/ion velocities corresponding to longitudinal and transversal temperatures $T_{\parallel} = 0.025$ meV and $T_{\perp} = 1.65$ meV respectively, before and after performing the Landau-Zener calculation. This convolution allowed us to compare our branching ratios with those measured in the TSR storage ring for 1 meV collision energy [46, 47].

The re-distribution of the flux of probability at the crossing between D_1 and D_2 results in the cross sections and yields illustrated in thick lines in Figs. 4, 5 and 6, and in the yields displayed in Table II. One may notice in these figures an interchange of the populations in the ground and lowest excited state of the Sulfur atoms, due to this re-distribution. The good agreement with the TSR-measurements at very low energy supports this interchange, whereas the theoretically-computed yields at 1 meV without the Landau-Zener treatment disagree with the experimental ones.

C. Vibrational excitation

In addition to the DR cross sections and rate coefficients we have calculated vibrational excitations (VE) of the relaxed ($v_i^{\dagger} = 0$) molecular target into the lowest excited vibrational states ($v_i^{\dagger} = 1, 2$) via the capture into states of both $^2\Pi$ and $^4\Pi$ symmetries of the neutral.

TABLE II: Landau-Zener probabilities (eq. (21)) for the transition between the two lowest dissociative $^2\Pi$ diabatic states of the SH molecule - D_1 and D_2 in the upper-left panel of fig. 1 - and corresponding branching ratios as function of the collision energy. Our MQDT/Landau-Zener results are compared with the TSR measured data, when available [46, 47].

Energy (eV)	P_{12}	MQDT-no LZ		MQDT-LZ		TSR		
		$n(^3P)$	$n(^1D)$	$n(^3P)$	$n(^1D)$	$n(^3P)$	$n(^1D)$	$n(^1S)$
0.001	0.99403	0.274	0.726	0.724	0.276	0.61	0.33	0.06
0.01	0.99400	0.140	0.860	0.856	0.144	—	—	—
0.1	0.99373	0.616	0.384	0.386	0.614	—	—	—
0.5	0.99246	0.320	0.680	0.678	0.322	—	—	—

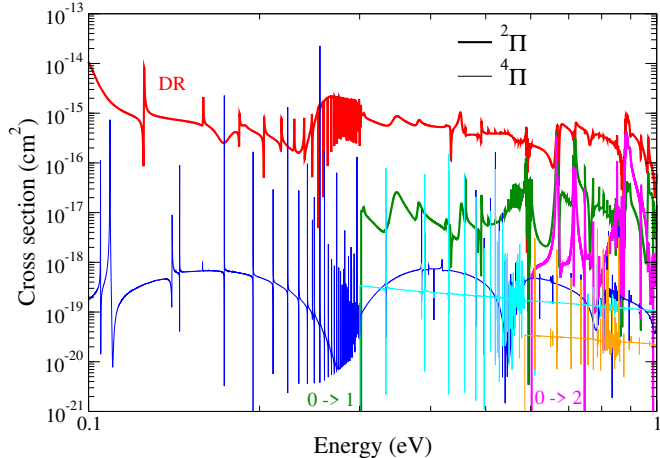


FIG. 7: Vibrational excitation and dissociative recombination cross sections of the vibrationally relaxed SH^+ molecular cation by considering both $^2\Pi$ and $^4\Pi$ symmetries of the formed molecular complex. The red and blue curves stand for DR, the dark green and cyan ones for $0 \rightarrow 1$ VE and those in turquoise and maroon give VE for $0 \rightarrow 2$. Finally, the thick curves correspond for the $^2\Pi$ while the thin curves for the $^4\Pi$ molecular symmetry of the neutral.

The cross sections over symmetries and the global thermal rate coefficients summed over all symmetries, can be seen in Figs. 7 and 8 respectively, together with those obtained for DR.

According to Fig. 7 the VE cross sections show sharp thresholds corresponding to the excitation energies of the ion. Similarly to DR, they are driven by the Rydberg resonances and for this process too we found smaller cross sections for the $^4\Pi$ molecular symmetry. However the magnitude of the obtained difference for the two symmetries is different, while for the DR we get a difference of about two orders of magnitude, the VE cross sections differ only by one order of magnitude.

Figure 8 shows that while the DR rate coefficient is smoothly decreasing as a function of the temperature, the VE ones have a monotonically increasing behaviour due to the sharp thresholds. One can clearly see that the DR dominates over VE for all electronic temperatures up to 1000 K.

In order to facilitate the use of our recombination

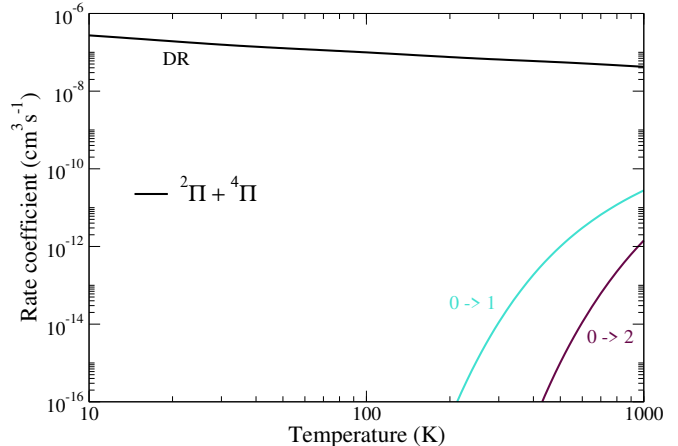


FIG. 8: Vibrational excitation and dissociative recombination rate coefficients of the vibrationally relaxed SH^+ molecular cation: sum of the contributions via the SH states of $^2\Pi$ and $^4\Pi$ symmetries.

and excitation rate coefficients for kinetic modelling, we have fitted their temperature dependence by using the Arrhenius-type formula:

$$k(T) = a_0 \left(\frac{T}{300} \right)^{a_1} e^{-\frac{a_2}{T}}, \quad (23)$$

where the temperature T is in Kelvin and the rate coefficient k in $cm^3 s^{-1}$. The fitting parameters for the DR of the ground vibrational state of the target and for the VE into the lowest two vibrationally-excited states are summarized in Table III. For all the processes, the fitted values reproduce well our MQDT rate coefficients, according to the RMS values given in the fourth column of each table in the whole temperature range from 10 to 1000 K.

IV. CONCLUSIONS

In this paper we studied by MQDT the relevance of the $^4\Pi$ symmetry states of SH for the dissociative recombination of SH^+ at low energy/temperature. We have found that this symmetry has a far smaller contribution to the cross sections/rates than the $^2\Pi$ ones. Therefore,

TABLE III: Fitting parameters for the formula (23), corresponding to the rate coefficients summed over $^2\Pi$ and $^4\Pi$ symmetries for dissociative recombination and vibrational excitation of vibrationally relaxed ($v_i^+ = 0$) molecular cation. The fit applies for temperatures for which the rate coefficient is higher than $10^{-16} \text{ cm}^3 \text{ s}^{-1}$.

	v_i^+	v_f^+	Temperature range (K)	a_0 ($\text{cm}^3 \text{ s}^{-1} \text{ K}^{-A_1}$)	a_1	a_2 (K)	RMS
DR	0		$10 \leq T \leq 1000$	6.53104×10^{-8}	-0.348405	-2.59354	0.00855
VE	0	1	$220 \leq T \leq 400$	1.46041×10^{-9}	-0.432013	3535.88	0.00273
			$400 < T \leq 1000$	3.83266×10^{-10}	0.364274	3063.89	0.02488
VE	0	2	$440 \leq T \leq 1000$	8.44578×10^{-10}	0.464803	6941.58	0.01119

the comparison between theory and experiment did not change after the present study: an overall good agreement from 10 meV to 1 eV, and a disagreement increasing progressively up to one order of magnitude when the energy is decreased from 10 to 0.1 meV.

We produced the branching ratios, and we took into account the redistribution of the probability fluxes at the crossing between the PECs of the two dissociative states. A spectacular inversion in the branching ratios takes place, resulting in a satisfactory agreement between our theoretical MQDT-Landau-Zener final results and those produced by the storage ring TSR at very low energy. More than two third of the recombination events result in ground state sulfur atoms.

We also computed vibrational excitation cross sections and rate coefficients. This process is largely dominated by the dissociative recombination below 1000 K.

Further studies will be devoted to the account of the rotational effects, which may result in a better agreement between theory and experiment, especially in the very low energy range.

DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding authors.

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- [1] A. O. Benz, S. Bruderer, E. F. van Dishoeck, *et al*, *A&A* **521**, L35, (2010).
 - [2] K. M. Menten, F. Wyrowski, A. Belloche, R. Güsten, L. Dedes, and H. S. P. Müller, *A&A* **525**, A77, (2011).
 - [3] B. Godard, E. Falgarone, M. Gerin, D. C. Lis, M. De Luca, J. H. Black, J. R. Goicoechea, J. Cernicharo, D. A. Neufeld, K. M. Menten, and M. Emprechtinger, *A&A* **540**, A87, (2012).
 - [4] Z. Nagy, F. F. S. Van der Tak, V. Ossenkopf, M. Gerin, F. Le Petit, J. Le Bourlot, J. H. Black, J. R. Goicoechea, C. Joblin, M. Röllig, and E. A. Bergin, *A&A* **550**, A96, (2013).
 - [5] B. Godard, E. Falgarone, and G. Pineau des Forêts, *A&A* **570**, A27, (2014).
 - [6] A. Zanchet, M. Agundez, V. J. Herrero, A. Aguado, and O. Roncero, *Astron. J.* **146**, 125 (2013).
 - [7] T. J. Millar, N. G. Adams, D. Smith, W. Lindinger, and H. Villinger, *MNRAS* **221**, 673 (1986).
 - [8] V. Wakelam, E. Herbst, J.-C. Loison, *et al*, *Ap.J. Suppl.Ser.* **199**, 21 (2012).
 - [9] D. McElroy, C. Walsh, A. J. Markwick, M. A. Cordiner, K. Smith, and T. J. Millar, *A&A* **550**, A36 (2013).
 - [10] D. O. Kashinski, D. Talbi, A. P. Hickman, O. E. Di Nallo, F. Colboc, K. Chakrabarti, I. F. Schneider, and J. Zs. Mezei, *J. Chem. Phys.* **146**, 204109 (2017).
 - [11] D. O. Kashinski, J. Bohnemann, A. P. Hickman, and D. Talbi, *Theoretical Chemistry Accounts* **140**, 64 (2021).
 - [12] A. Giusti-Suzor, *J. Phys. B: At. Mol. Phys.* **13**, 3867 (1980).
 - [13] M. J. Seaton, *Rept. Prog. Phys.* **46**, 167 (1983).
 - [14] C. Jungen, ed., *Molecular Applications of Quantum Defect Theory* (Institute of Physics Publishing, Bristol, 1996).
 - [15] A. Giusti-Suzor, J. N. Bardsley, and C. Derkits,

- Phys.Rev. A **28**, 682 (1983).
- [16] I. F. Schneider, O. Dulieu, and A. Giusti-Suzor, J. Phys.B: At. Mol. Phys. **24**, L289 (1991).
- [17] H. Takagi, J. Phys. B: At. Mol. Opt. Phys. **26**, 4815 (1993).
- [18] T. Tanabe, I. Katayama, H. Kamegaya, *et al*, Phys. Rev. Lett. **75**, 1066 (1995).
- [19] I. F. Schneider, C.Strömholm, L.Carata, X.Urbain, M. Larsson, and A. Suzor-Weiner, J. Phys. B: At. Mol. Opt. Phys. **30**, 2687 (1997).
- [20] Z. Amitay, A. Baer, M. Dahan, J. Levin, Z. Vager, D. Zajfman, D. Knoll, M. Lange, D. Schwalm, R. Wester, A. Wolf, I. F. Schneider, and A. Suzor-Weiner, Phys. Rev. A **60**, 3769 (1999).
- [21] M. D. Epée. Epée, J. Zs. Mezei, O. Motapon, N. Pop, and I. F. Schneider, MNRAS **455**, 276 (2016).
- [22] M. D. Epée Epée, O. Motapon, N. Pop, F. Iacob, E. Roueff, I. F. Schneider, and J. Zs. Mezei, MNRAS **512**, 424 (2022).
- [23] S. L. Guberman and A. Giusti-Suzor, J. Chem. Phys. **95**, 2602 (1991).
- [24] S. L. Guberman, in *Dissociative Recombination: Theory, Experiment and Applications IV*, edited by M. Larsson, J. B. A. Mitchell, and I. F. Schneider (World Scientific, Singapore, 2000) p. 111.
- [25] H. Sun and H. Nakamura, J. Chem. Phys. **93**, 6491 (1990).
- [26] B.Vâlcu, I.F.Schneider, M.Raoult, C.Strömholm, M. Larsson, and A. Suzor-Weiner, Eur. Phys. J. D **1**, 71 (1998).
- [27] I. F. Schneider, I. Rabadán, L. Carata, L. H. Andersen, A. Suzor-Weiner, and J. Tennyson, J. Phys. B: At. Mol. Opt. Phys. **33**, 4849 (2000).
- [28] V. Ngassam, O. Motapon, A. Florescu, L. Pichl, I. F. Schneider, and A. Suzor-Weiner, Phys. Rev. A **68**, 032704 (2003).
- [29] O. Motapon, M. Fifrig, A. Florescu, F. O. W. Tamo, O. Crumeyrolle, G. Varin-Bréant, A. Bultel, P. Vervisch, J. Tennyson, and I. F. Schneider, Plasma Sources Sci. Technol. **15**, 23 (2006).
- [30] J. Zs. Mezei, R. B. Backodissa-Kiminou, D. E. Tudorache, V. Morel, K. Chakrabarti, O. Motapon, O. Dulieu, J. Robert, W-U. L. Tchang-Brillet, A. Bultel, X. Urbain, J. Tennyson, K. Hassouni, and I. F. Schneider, Plasma Sources Sci. Technol. **24**, 035005 (2015).
- [31] D. A. Little, K. Chakrabarti, J. Zs. Mezei, I. F. Schneider, and J. Tennyson, Phys. Rev. A **90**, 052705 (2014).
- [32] A. Abdoulanziz, C. Argentin, V. Laporta, K. Chakrabarti, A. Bultel, J. Tennyson, I. F. Schneider, and J. Zs. Mezei, J. Appl. Phys. **129**, 053303 (2021).
- [33] J. Zs. Mezei, F. Colboc, N. Pop, S. Ilie, K. Chakrabarti, S. Niyonzima, M. Lepers, A. Bultel, O. Dulieu, O. Motapon, J. Tennyson, K. Hassouni, and I. F. Schneider, Plasma Sources Sci. Technol. **25**, 055022 (2016).
- [34] I. F. Schneider, A. E. Orel, and A. Suzor-Weiner, Phys. Rev. Lett. **85**, 3785 (2000).
- [35] V. Kokoouline, C. H. Greene, and B. D. Esry, Nature **412**, 891 (2001).
- [36] V. Kokoouline and C. H. Greene, Phys. Rev. A **68**, 012703 (2003).
- [37] V. Kokoouline, M. Ayouz, J. Zs. Mezei, K. Hassouni, and I. F. Schneider, Plasma Sources Sci. Technol. **27**, 115007 (2018).
- [38] J. Zs. Mezei, K. Chakrabarti, M. D. Epée Epée, O. Motapon, C. H. Yuen, M. A. Ayouz, N. Douguet, S. Fonseca dos Santos, V. Kokoouline, and I. F. Schneider, ACS Earth and Space Chem. **3**, 2376 (2019).
- [39] V. Ngassam, A. Florescu, L. Pichl, I. F. Schneider, O. Motapon, and A. Suzor-Weiner, Eur. Phys. J. D **26**, 165 (2003).
- [40] A. I. Florescu, V. Ngassam, I. F. Schneider, and A. Suzor-Weiner, J. Phys. B: At. Mol. Opt. Phys. **36**, 1205 (2003).
- [41] K. Chakrabarti, D. R. Backodissa-Kiminou, N. Pop, J. Zs. Mezei, O. Motapon, F. Lique, O. Dulieu, A. Wolf, and I. F. Schneider, Phys. Rev. A **87**, 022702 (2013).
- [42] J. Tennyson, Phys. Rep. **491**, 29 (2010).
- [43] T. N. Rescigno, C. W. McCurdy, A. E. Orel, and B. H. Lengsfeld, III, in *Computational Methods for Electron-Molecule Scattering*, edited by W. H. Huo and A. Gianturco (Springer US, New York, 1995) pp. 1-44.
- [44] T. Pacher, L. S. Cederbaum, and H. Köppel, J. Chem. Phys. **89**, 7367 (1988).
- [45] M. W. Schmidt, K. K. Baldrige, J. A. Boatz, S. T. Elbert, M. S. Gordon, J. H. Jensen, S. Koseki, N. Matsunaga, K. A. Nguyen, S. Su, T. L. Windus, M. Dupuis, and J. A. Montgomery, Jr., J. Comp. Chem. **14**, 1347 (1993).
- [46] A. Becker, C. Domesle, W. D. Geppert, M. Grieser, C. Krantz, R. Repnow, D. W. Savin, D. Schwalm, A. Wolf, B. Yang, and O. Novotny, J. Phys.: Conf. Ser. **635**, 072067 (2015).
- [47] A. Becker, *Imaging of Neutral Fragmentation Products from Fast Molecular Ion Beams: Paving the Way for Reaction Studies in Cryogenic Environment*, Ph.D. thesis, Combined Faculties for the Natural Sciences and for Mathematics of the Ruperto-Carola University of Heidelberg, Germany (2016).
- [48] C. Zener, Proc. R. Soc. London Ser. A **137**, 696 (1932).
- [49] J. R. Rubbmark, M. M. Kash, M. G. Littman, and D. Kleppner, Phys. Rev A **23**, 3107 (1981).
- [50] A. Larson, C. H. Greene, A. E. Orel, I. F. Schneider, and A. Suzor-Weiner, in *Dissociative Recombination, Theory, Experiment and Applications IV*, edited by M. Larsson, J. B. A. Mitchell, and I. F. Schneider (World Scientific, Singapore New Jersey London Hong Kong, 2000) p. 101.