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A Computational Study of a Two-fluid Atomizing Coaxial Jet: Validation against Experimental Back-lit Imaging and Radiography and the Influence of Gas Velocity and Contact Line Model

Lam Vu^{*1}, Nathanaël Machicoane^{2,4}, Danyu Li³, Timothy B. Morgan³, Theodore J. Heindel³, Alberto Aliseda², Olivier Desjardins¹

¹Department of Mechanical and Aerospace Engineering, Cornell University, Ithaca, USA

²Department of Mechanical Engineering, University of Washington, Seattle, USA

³Center for Multiphase Flow Research and Education and Department of Mechanical Engineering, Iowa State University, Ames, USA

⁴Univ. Grenoble Alpes, CNRS, Grenoble INP, LEGI, 38000 Grenoble, France

*Corresponding author email: lxv2@cornell.edu

11 Abstract

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Numerical simulations of liquid atomization in a two-fluid coaxial geometry have been performed using a geometric Volume-of-Fluid method. Experimental measurements have been obtained using visible light back-lit imaging and X-ray radiography. Simulations are validated against experiments, using the same geometry and fluid injection rates of air and water, by showing excellent agreement in quantities such as liquid mass distribution in the spray formation region and the liquid jet length statistics and temporal dynamics. At the nozzle exit, the coflowing liquid and gas streams are separated by a cylindrical splitter plate. The liquid is laminar and modeled using a Poiseuille flow while the gas inflow model and the contact line model are varied. For the gas velocity models, the vorticity thickness is shown to have a strong influence on the downstream liquid distribution; the difficulty of its modeling and routes to overcome them are discussed. For the contact line model, pinning the interface to the inner wall of the splitter plate leads to an initial increase in the diameter of the liquid jet just downstream of the nozzle exit. In contrast, pinning to the outer wall of the splitter plate or allowing for a free moving contact line results in a monotonic decrease in the diameter of the liquid jet as the downstream distance is increased, in agreement with the experimental observations and measurements. A sub-grid scale contact line model based on a static contact angle is increased.

12 Keywords: Air-blast Atomization, Contact Line Modeling, Liquid-Gas Flows, Validation

13 1. Introduction

Two-fluid coaxial atomizers utilize a high-speed gas stream to destabilize a coflowing low-speed liquid jet. These devices are widely used in engineering systems such as spray dryers and fuel injectors. Accurate modeling of the liquid jet's initial destabilization and break up is of the upmost importance as it serves as an initial condition for the spray dispersion process. Because of the inherent difficulties associated with modeling primary atomization computationally [12], studies have mostly been limited to highly simplified and academic cases. Moreover, few studies have explored *Preprint submitted to Elsevier*

in detail the modeling of the nozzle exit. In particular, the impact of different modeling strategies for the high-speed
gas, low-speed liquid, and the splitter plate separating the two streams, warrants careful investigation.

Liquid atomization has been studied extensively both through experiments and simulations but have had limita-21 tions based on the methods used. A non-exhaustive list of such methods are described below along with some of 22 their limitations. Experimentally, the flow inside the nozzle cannot be easily quantified using standard particle image 23 velocimetry (PIV) and hot-wire measurements. Back-lit imaging is an effective technique for visualizing the spray 24 and can be used to accurately extract quantitative measurements of the liquid presence in a region where the liquid 25 stays mostly intact [20]. However, such measurements struggle in areas where the liquid is broken up and multiple 26 liquid structures intersect a line of sight. In contrast, X-ray radiography penetrates the liquid, enabling the study of 27 additional physics, such as bubble entrainment and contact line dynamics in extreme atomization conditions [21]. 28 Recently, it has been used to extract quantitative measurements such as the integrated liquid depth along a line of 29 sight [3]. Simulations have had their own challenges such as robust numerical methods capable of handling topology 30 change, discontinuous fluid properties across the interface and singular forces at the interface, and computational de-31 mand owing to the wide range of length and time scales [12]. Front tracking methods [37], which transport a surface 32 mesh, are viable techniques but have difficulty with topology change as heuristics are needed for the deletion and 33 re-population of surface elements. Diffuse interface methods [2] are also viable techniques, but diminish the sharp-34 ness of the discontinuities since the interface is smeared over a few computational cells. Level-set methods, which 35 transport a signed distance function away from the interface, have been used extensively [35] but suffer from mass 36 conservation issues. These issues have been addressed by improvements such as the conservative level-set method 37 [5] and the refined grid level-set method [14]. Volume-of-Fluid (VOF) methods, using complex geometric transport 38 operations [29], have had success in handling topology change, ensuring discrete mass conservation and maintaining 39 the sharp discontinuities. 40

Validating simulations against experiments is a crucial step in computational studies of sprays and the majority 41 of past validation exercises of two-fluid atomizers have compared indirect quantities or reduced the modeling com-42 plexity because of the computational and experimental challenges described above. Demoulin et al. [8] simulated 43 primary break up by solving equations for a single fluid representing a liquid-gas mixture under the assumptions 44 of high Reynolds and Weber numbers and compared centerline liquid volume fraction profiles against experiments. 45 Gorokhovski et al. [12] modeled the primary atomization by solving for the gas phase using a large-eddy simulation 46 (LES) and the liquid phase using a stochastic liquid depletion modeling. This study yielded satisfactory agreement 47 of liquid volume fraction distributions against experiments but most comparisons were qualitative. Fuster et al. [11] 48 presented simulations in a planar configuration at a lower viscosity and density ratio and compared droplet size dis-49 tributions, as a function of mesh size, against experimental data. Fuster et al. [10] studied the influence of the splitter 50 plate thickness on the peak frequency and made comparisons against linear stability analysis at low density ratios. For 51 a single case, the frequency was compared against experiments and linear stability analysis at air-water conditions. 52 The study showed that at low gas-to-liquid dynamic pressure ratios, a convective instability is observed whereas at 53

high dynamic pressure ratios, the instability is absolute. Xiao et al. [39] simulated primary atomization at air-water 54 conditions and showed great agreement in the average liquid core length, where the liquid core is defined to be the 55 large coherent liquid structure attached to the nozzle, but generated the gas inflow using synthetic turbulence. This 56 57 study showed the turbulent eddies in the liquid phase play a leading role on the interfacial instabilities. Muller et al. [28] simulated primary break up of a high-viscosity fluid and showed excellent agreement in liquid core length and 58 dominant frequency against experiments using the same geometry. Agbaglah et al. [1] presented 3D simulations in a 59 planar geometry at experimental air-water conditions and compared well the liquid cone length and the most unstable 60 frequency. This study showed that inclining the gas inflow enhanced the formation of interfacial waves. Ling et al. 61 [19] performed massively resolved simulations at a lower density and viscosity ratio and reported on droplet size 62 distributions, as a function of mesh size, and compared them against log-normal and Gamma distribution fits. The 63 simulations qualitatively discussed the expansion of punctured holes in liquid sheets and the ligaments generated at 64 the edge of their rims. Carmona et al. [4] performed simulations of a pre-filmed air-blast atomizer and made qualita-65 tive comparisons and drop size comparisons as a function of VOF iso-surface value. Even with current studies, more 66 detailed and direct comparisons under realistic configurations are needed to validate computational capabilities. 67

In this work, we perform simulations of primary atomization in a coaxial two-fluid atomizer using the Volume-68 of-Fluid method and validate them against experiments. A novelty of our validation exercise is that we make direct 69 comparisons of quantities obtained from experimental back-lit imaging and X-ray radiography under identical oper-70 ating conditions, using the same geometry. Furthermore, the validation is comprehensive, including comparisons of 71 liquid mass distribution and temporal dynamics of the liquid jet. Following the validation, we study the effect of using 72 different gas inflow models which range from using an analytical velocity profile to a nozzle simulation. The liquid 73 is laminar and modeled as a Poiseuille flow and a cylindrical splitter plate separates the liquid and gas streams. We 74 discuss the influence of the contact line model which ranges from pinning the interface to a specified location on the 75 splitter plate (fixed triple point) to a free moving contact line. For free moving contact lines, we employ a sub-grid 76 scale (SGS) contact line model that assumes a static contact angle [38]. We vary the static contact angle to understand 77 the effect of nozzle tip wettability. These inflow modeling strategies are easily implementable and do not require large 78 amounts of mesh resolution, making them particularly desirable from a practical engineering standpoint. 79

The paper is organized as follows: Section 2 discusses the experimental and numerical methods used, Section 3 validates our computational model against experiment, Section 4 discusses the influence of the gas velocity model, Section 5 discusses the influence of the contact line model, and conclusions are drawn in Section 6.

83 2. Methods

84 2.1. A Canonical Atomizer and Flow Conditions

Figure 1 shows the two-fluid coaxial atomizer [21] used in both simulations and experiment. Air enters the nozzle through four upstream ports perpendicular to the wall and flows through an annular passage at a total flow

rate Q_g . Liquid water flows through a straight circular pipe at a flow rate Q_l . The outer wall of the liquid nozzle 87 separates the two streams and its annular section at the exit plane, with inner and outer nominal diameter $d_l = 2$ 88 mm and $D_l = 3$ mm, will be referred to as the splitter plate. The liquid and gas bulk exit velocities are defined as 89 $U_l = Q_l/A_l$ and $U_g = Q_g/A_g$, where $A_l = \pi d_l^2/4$ and $A_g = \pi (d_g^2 - D_l^2)/4$ are the liquid and gas nozzle exit flow-90 through areas and $d_g = 10$ mm is the gas nozzle inner diameter. The fluid properties used are kinematic viscosities of 91 $v_g = 1.45 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$ and $v_l = 1.137 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$, densities of $\rho_g = 1.226 \text{ kg m}^{-3}$ and $\rho_l = 1000 \text{ kg m}^{-3}$, and 92 a surface tension coefficient $\sigma = 72 \text{ mN m}^{-1}$ where subscripts g and l denote gas and liquid properties respectively. 93 Table 1 summarizes the non-dimensional parameters used in this case. 94



Figure 1: (Color online) Nozzle schematic cut longitudinally (left) and transversely (right). Water is injected through a round pipe while gas is injected through four gas ports into a converging nozzle. Note that the inset indicating the exit diameters in a) has been scaled up by a factor of two for visibility.

Table 1: Simulation's non-dimensional parameters: gas Reynolds number (Re_g), liquid Reynolds number (Re_l), gas-to-liquid dynamic pressure ratio (M), Weber number based on the liquid jet diameter but gas density and slip velocity between the two phases (We), density ratio (ρ^*) and viscosity ratio (μ^*).

$Re_g \equiv \frac{4Q_g}{\sqrt{4\pi A_g v_g}}$	$Re_l \equiv \frac{\rho_l U_l d_l}{\mu_l}$	$M\equivrac{ ho_g U_g^2}{ ho_l U_l^2}$	$We \equiv \frac{\rho_g (U_g - U_l)^2 d_l}{\sigma}$	$ \rho^* \equiv \frac{\rho_l}{\rho_g} $	$\mu^* \equiv \frac{\mu_l}{\mu_g}$
21400	1200	6.4	39.1	815	65

95 2.2. High-speed Back-lit Imaging and X-ray Radiography

96 High-speed back-lit imaging is used to produce 2D projections of the liquid presence in the near-field. The images 97 are post-processed using a sequence of operations that binarize the liquid core, defined to be the portion of the liquid jet that is still fully connected to the nozzle, such that a liquid pixel value is 1 and a gas pixel value is 0. The temporal and spatial resolutions for this study are 0.1 ms and 27 μ m respectively. Details of this method are discussed further in [20].

Synchrotron X-ray radiography of the resulting spray was performed at the Advance Photon Source (APS) at 101 Argonne National Laboratory, 7-BM beamline [17]. As opposed to binarized liquid data obtained from back-lit 102 imaging, focused-beam radiography enables the point-wise measurement of the integrated liquid depth along a line of 103 sight, referred to as the equivalent path length (EPL). The measurement technique relies on a monochromatic X-ray 104 beam that is sent through the liquid and measured by a receiving pin-diode at 270 kHz. Based on the attenuation of 105 the signal caused by the liquid, the EPL is deduced from Beer-Lambert's Law: $EPL = (1/\mu_a) \ln(I_0/I)$ where I_0 is 106 the incident beam intensity, I is the beam intensity after passing through the spray, and μ_a is the X-ray attenuation 107 coefficient of water at the X-ray wavelength. These point measurements can be raster-scanned across the spray to 108 gather longitudinal or transverse profiles of the liquid depth. Details of this technique are further described in [3, 13], 109

and the experimental configurations and liquid phase visualization are detailed in [21].

112 We consider an LES approach to the two-phase, incompressible Navier-Stokes equations

113

$$\nabla \cdot \tilde{\boldsymbol{u}} = 0, \tag{1}$$

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$$\frac{\partial \rho \tilde{\boldsymbol{u}}}{\partial t} + \nabla \cdot (\rho \tilde{\boldsymbol{u}} \tilde{\boldsymbol{u}}) = -\nabla \tilde{p} + \rho \boldsymbol{g} + \nabla \cdot (\mu [\nabla \tilde{\boldsymbol{u}} + \nabla \tilde{\boldsymbol{u}}^{\mathsf{T}}]) + \nabla \cdot \boldsymbol{\tau}_{SGS} + \boldsymbol{F}_{ST},$$
(2)

where $(\tilde{\cdot})$ denotes a spatially filtered (resolved) quantity on the mesh, \boldsymbol{u} is the velocity, p is the pressure, ρ is the density, μ is the dynamic viscosity, \boldsymbol{g} is the gravitational acceleration, τ_{SGS} is the sub-grid scale (SGS) stress, \boldsymbol{F}_{ST} is the surface tension force and t is time. We also consider the volume fraction transport equation

$$\frac{\partial \tilde{\alpha}}{\partial t} + \tilde{\boldsymbol{u}} \cdot \nabla \tilde{\alpha} = 0, \tag{3}$$

where α is the ratio of liquid volume to cell volume in a computational cell and sub-grid scale effects have been neglected. The fluid properties are weighted based on the liquid volume fraction

$$\rho = (1 - \tilde{\alpha})\rho_g + \tilde{\alpha}\rho_l,\tag{4}$$

$$\mu^{-1} = (1 - \tilde{\alpha})\mu_g^{-1} + \tilde{\alpha}\mu_l^{-1},\tag{5}$$

where subscripts 'g' and 'l' refer to gas and liquid quantities respectively.

The two-phase Navier-Stokes equations are solved using an in-house, conservative, finite-volume flow solver for low Mach number flows [9]. The solver employs second-order accurate methods in time and space. Away from the interface, the flow solver is discretely kinetic energy conserving. At the interface, local discontinuities degrade the methods and although mass is still discretely conserved and momentum is approximately conserved, kinetic energy conservation is lost. The volume fraction equation is solved with a geometric, semi-Lagrangian Volume-of-Fluid method [29]. Inside each computational cell, the interface is represented locally as a plane using the piece-wise linear interface construction (PLIC) [33], with the plane normal calculated using LVIRA [30]. A dynamic Smagorinsky turbulence model [27] is used to close τ_{SGS} . The surface tension force is calculated through

$$F_{ST} = \sigma(\tilde{\kappa} + \kappa_{SGS})\nabla\tilde{\alpha}$$
(6)

where σ is the surface tension coefficient, $\tilde{\kappa}$ is the resolved curvature and κ_{SGS} is a sub-grid scale curvature. The surface tension force is embedded as a source term in the pressure Poisson equation using a continuous surface force approach [31]. The resolved curvature of the interface is calculated using parabolic surface fits [34]. κ_{SGS} is used to model surface wettability effects that exist at scales far below the mesh size and is controlled through a static contact angle θ_s (see [38]). Figure 2 shows a schematic of a grid cell that contains the triple point. In that cell, the mismatch between the interface angle resolved by the mesh (θ_d) and the angle at the wall (θ_s) is used to compute a SGS curvature

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$$\kappa_{SGS} = \frac{\cos\theta_s - \cos\theta_d}{\varDelta},\tag{7}$$

137 where Δ is the mesh spacing. If a cell does not have a triple point, then κ_{SGS} is set to 0.



Figure 2: (Color online) Schematic of sub-grid scale contact line. The model adds a sub-grid scale curvature based on an assumed static contact angle θ_s to the resolved curvature based on θ_d .

138 2.4. Simulation Set Up

139 2.4.1. Domain

The atomization domain is a rectangular box of size $11.16D_l \times 10D_l \times 10D_l$, discretized on a Cartesian mesh uniformly spaced by $n_x \times n_y \times n_z$ cells. Cells are cubic with sides of length $\Delta/d_l = 0.066$. *x* is the downstream direction while *y* and *z* are the lateral directions with the origin of the domain located at the center of the nozzle exit plane. The liquid is laminar and given a parabolic velocity profile. The gas inflow condition is either specified by a Dirichlet condition according to an analytical profile or a supplementary nozzle simulation. All other boundaries are
 treated as Neumann outflow conditions.

For some of the atomization simulations presented herein, an auxiliary nozzle simulation of the internal gas flow 146 of the nozzle is used to generate realistic inflow conditions. The domain size of this nozzle simulation is $10d_g \times$ 147 $10d_g \times 10d_g$ and the mesh is Cartesian with a uniform spacing $\Delta_n/d_g = 0.05$. The gas nozzle simulation is indicated 148 in terms of the gas diameter d_g since it is the relevant quantity here, and we remind that $D_l/d_g = 0.3$. The nozzle 149 plenum is the furthest point upstream in the domain and the furthest point downstream is at a distance d_g past the 150 nozzle exit. The liquid injection is masked out as a solid and a single-phase solver is used, significantly reducing 151 the computational cost. The converging nozzle walls are created by stair-stepping full cells that are treated as solid 152 boundaries and the gas inflow is injected through the four normal ports upstream to match the gas flow rate Q_g . This 153 approach matches the nozzle 3D geometry used in the experiment and available at http://depts.washington. 154 edu/fluidlab/nozzle.shtml. All other boundaries are treated as Neumann outflow conditions. The gas velocity 155 field at $x = -1.16D_l$ is then used as a Dirichlet inflow condition for the atomization simulation. 156



(a) Atomization Domain Only

(b) Atomization and Nozzle Domains Coupled

Figure 3: (Color online) Illustration of the computational set up. Contour of $\alpha = 0.5$ representing the interface is plotted in blue, pseudo-color of velocity magnitude are plotted on the cut planes with different normalization inside and outside the nozzle. a) Domain excludes the nozzle and utilizes an analytical profile to model the gas velocity and b) a separate nozzle simulation is coupled to the atomization domain.

157 2.4.2. Range of Gas Velocity and Contact Line Models

The gas velocity models used in this study were an analytical velocity profile and an additional nozzle simulation of the internal gas flow. The analytical profile [24] and takes the form

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$$u(r) = U_g \operatorname{erf}((r - R_l)/\delta_w) [1 + \operatorname{erf}((r - R_l)/\delta_w)]/2 \qquad R_l \le r \le r_g$$

$$v(r) = w(r) = 0$$
(8)

where $R_l = D_l/2$ and $r_g = d_g/2$ are the lower and upper bounds containing the gas stream, r is the radial location, δ_w is the prescribed gas vorticity thickness and U_g is chosen such that the gas volumetric flow rate integrates to Q_g . Figure 3a shows an atomization simulation run with an analytical gas velocity profile while Fig. 3b shows a simulation where the nozzle and atomization simulations are coupled as described in Section 2.4.1.

The contact line models used in this study were pinning the contact line to the inner wall $(r = r_l = d_l/2)$ pinning 165 to the outer wall $(r = R_l)$ and allowing for an unpinned/free moving contact line. The implementation of each is as 166 follows: when pinning to r_l , the splitter plate is modeled as a fully unwet wall while when pinning to R_l , it is modeled 167 as a fully wet wall. In both cases, the splitter plate cells are treated as a solid boundary for the velocity solver, but 168 either taken to be a full liquid or gas cells when included in the LVIRA interface reconstruction. However, in the case 169 where the contact line is free moving, the splitter plate cells are excluded from the LVIRA interface reconstruction but 170 still treated as a solid boundary for velocity. For freely moving contact lines, the SGS contact line model described in 171 Section 2.3 is employed. It should be noted that although the splitter plate is resolved by 2-3 cells in this study, results 172 presented in the following section show that excellent agreement with experiment is still obtained. More detailed 173 analysis of the contact line in a more highly resolved setting is left for future work. 174

175 3. Validation Against Experiments

The combination of using an additional nozzle simulation to model the gas profile and allowing for a free contact line with a static contact angle of 85° yields the best agreement against experiments; qualitative comparisons are made in Fig. 4 and quantitative comparisons are made against metrics gathered from X-ray measurements in Fig. 5 and from back-lit imaging in Fig. 6. The atomization simulation presented in this section uses a refined mesh of size $\Delta/2$.

Figure 4 shows snapshots of the flow comparing the simulations and experiments; emphasis is placed on the 180 liquid core. At this low gas-to-liquid dynamic pressure ratio, the main instabilities observed are Kelvin-Helmholtz 181 instabilities that develop just past the nozzle exit and a large-scale flapping instability. At large-scales, both exhibit 182 similar liquid core lengths, interface topology, and flapping motion. The three snapshots illustrate the small-scale 183 event of bag break up. The process begins with the development of a thick sheet, the high-speed gas subsequently 184 inflates this sheet which forms a bag, and finally, when the sheet becomes sufficiently thin, the bag bursts. These thin 185 sheets in the experiment can reach scales as small as $O(1 \,\mu m)$ which computations cannot afford to resolve. In our 186 simulations, the mesh sizes are $O(100\mu m)$ and as such, bags prematurely break and leave behind large rims resembling 187 a prong. Running at these mesh sizes allow simulations to be relatively affordable, costing around 100,000 core hours. 188



Figure 4: (Color online) Qualitative comparisons between the simulation (left) and experiment (right). Frames are separated by 1 ms.

Quantitative comparisons of EPL statistics, liquid core length, and dominant frequency are presented to validate 189 simulations against experiments. EPL is calculated in the simulation by integrating the liquid volume fraction along a 190 line of sight, i.e., EPL = $\int \alpha dz$. After the flow has reached a statistically stationary state, statistics are accumulated for 191 $T_{stat} = 113 d_l / U_l = 450$ ms, i.e., 113 characteristic liquid time scales, while experimental measurements are gathered 192 for 10 seconds, corresponding to 45 and 1000 flapping events respectively. Figure 5a shows a 2D map of EPL averaged 193 in time. Figure 5b shows the comparison of mean EPL sampled along x, at the centerline (y = 0). The mean centerline 194 EPL is a proxy for the liquid diameter at distances close to the nozzle exit and decreases in value downstream either 195 because the flapping instability displaces the liquid core transversely away from the line of sight or the liquid core 196 has deformed or fragmented. EPL measurements presented herein are normalized by D_l since we will later pin the 197 contact line to the outer wall of the liquid pipe, leading to a value of approximately 1 at the nozzle exit, $x/D_l = 0$ 198 (Note: it will not be exactly 1 because of the inexact nature associated with approximating a cylindrical geometry 199 using a Cartesian mesh). Simulations are in excellent agreement with experiments as they are able to match well 200 the centerline decay of mean EPL. Figure 5c shows that the simulations also match well the experimental standard 201 deviation (std) of centerline EPL. Peaks in the standard deviation of EPL occur where variations in the integrated 202 volume fraction over time are largest and in the case of the centerline EPL, are visually confirmed to be a result 203 of large-scale flapping motion. Figures 5d to 5k show excellent agreement in transverse EPL mean and standard 204 deviation profiles. Figures 5d to 5g show that the simulations matches the transverse mean profiles well, capturing the 205 spreading of the liquid jet. Figure 5h shows two peaks in the standard deviation transverse profile at the top and bottom 206

edges of the jet and can be explained by the variation in volume fraction caused by interfacial perturbations generated by Kelvin-Helmholtz instabilities [23, 32]. Figures 5i to 5k show that as the downstream distance is increased, the centerline value and the two off-center peaks also increase, indicating a transition from a surface Kelvin-Helmholtz instability to a large-scale flapping instability.



Figure 5: (Color online) Simulations compared against experiments. a) 2D mean EPL map with sampling locations marked, b-k) Transverse profiles of the mean (middle row) and standard deviation (bottom row) EPL, comparing the simulation (----) and the experimental measurements (•).

Figure 6a shows a time instance of a binarized image of the liquid core and mimics an experimental back-lit image. The quantities illustrated on the figure are the liquid core length L_B , defined to be the instantaneous longitudinal extent of the liquid core, and the *y* liquid presence barycenter (y_{bary}) at a downstream location. Figure 6b shows that the simulations agree well with experimental results for the normalized probability density functions (PDF) of L_B . Figure 6c shows a spectrum of a Fourier transform taken of a time signal of y_{bary} (see [16] for more details). A flapping Strouhal number is calculated through $St = f_{dom}d_l/U_g$ where f_{dom} is the dominant frequency taken to be the frequency at which the spectrum peaks. $y_{bary} x/D_l = 3$, x/D_l [7]. Note that this normalization does not claim any

218 physical scaling but is done for non-dimensionalization purposes. Table 2 summarizes the comparison of the mean

and standard deviation of L_B and the flapping Strouhal number between the simulations and the experiments.



Figure 6: (Color online) a) Simulation binarized image of the liquid core with relevant quantities, b) PDF of liquid core length comparing the simulation (\blacklozenge) and the experiment (\blacklozenge), and c) y x/D_l = 3, f_{dom}.

Table 2: Comparisons between the simulation and the experiment of mean and standard deviation of L_B and flapping Strouhal number obtained from binarized images.

	$\langle L_B \rangle / D_l$	$L_{B,std}/D_l$	St.
Simulation	5.24	1.15	7.52×10^{-3}
Experiment	4.67	0.937	6.63×10^{-3}
Normalized Difference	12%	22%	13%

220 We now look at the effect of mesh resolution on the statistics presented above. Two additional simulations using larger mesh resolutions Δ and 2Δ are presented. Figure 7 shows the mean and standard deviation centerline EPL 221 statistics and the PDF of liquid core length at these different mesh sizes. Mean and standard deviation centerline EPL 222 statistics indicate that a simulation with a mesh resolution \varDelta is relatively well converged because differences between 223 Δ and $\Delta/2$ are small compared to differences between 2 Δ and Δ . Furthermore, Fig. 7c shows that the liquid core length 224 is not strongly affected by the mesh size. Although discrepancies are still present in statistics between mesh sizes 225 Δ and $\Delta/2$, we conclude that a mesh size Δ is sufficient to draw inferences from. As such, to reduce computational 226 resources, future simulations presented will maintain a mesh size of Δ . 227

228 4. Impact of Gas Velocity Model

229 4.1. Gas Velocity Profiles

Figure 8 shows velocity profiles at the nozzle exit plane for the experiment, the auxiliary nozzle simulation and the analytical velocity profiles according to Eq. (8) at different vorticity thicknesses. For the analytical profiles, the vorticity thicknesses used are $2\delta_w$, δ_w and $\delta_w/2$ where $\delta_w = 5.6h/\sqrt{Re_h}$ is the vorticity thickness obtained from the correlation proposed by [23], $h = (D_l - d_g)/2$ and $Re_h = U_g h/v_g$. No turbulent fluctuations are added to the inflow



Figure 7: (Color online) Mesh convergence of a-b) EPL statistics and c) liquid core length PDFs for simulations with mesh sizes 2Δ (--,), Δ (--,), $\Delta/2$ (--,), Δ

velocity profile. The experimental gas velocity profiles were measured a small distance downstream of the nozzle 234 using hot-wires without any liquid present while the statistics in the simulation were sampled in the atomization 235 domain. Various mesh sizes of the auxiliary nozzle simulation were tested and minimal changes in the stream-wise 236 velocity statistics were observed. Figure 8a shows that the mean stream-wise velocity profile of the nozzle simulation 237 and the analytical velocity profile with $\delta_w/2$ match the experimental vorticity thickness at the inner wall while the 238 velocity profiles with vorticity thicknesses of δ_w and $2\delta_w$ are a worse match. Figure 8b shows that the stream-wise 239 standard deviation velocity predicted from the nozzle simulation match the experiment well at the inner wall, which 240 can be expected to be most relevant for atomization, but are under-predicted within the outer gas shear layer. 241



Figure 8: (Color online) Comparisons of velocity statistics between analytical profiles with vorticity thicknesses $2\delta_w$ (•••), δ_w (•••), $\delta_w/2$ (••••), additional nozzle simulation (••) and experiment (•). Note that $D_l/d_g = 0.3$.

242 4.2. Influence of Vorticity Thickness

Figures 9a and 9b show the mean and standard deviation centerline EPL and Fig. 9c shows the liquid core length PDF of simulations using an analytical velocity profile at three different gas vorticity thicknesses (i.e., $2\delta_w$, δ_w and $\delta_w/2$). The contact line model used in these simulations was a free contact line with a static contact angle 85°. The

simulation presented in Section 3 using a mesh size $\Delta/2$ will serve as a benchmark. Considering the simulation using 246 a gas vorticity thickness δ_w , the mean centerline EPL profile and liquid core length PDF have larger values compared 247 to the benchmark case, suggesting that the jet breaks further downstream than in that case. Reducing the vorticity 248 thickness by a factor of 2 more closely matches the vorticity thickness produced from the nozzle simulation used 249 in the benchmark case and therefore, we observe better agreement in the mean centerline EPL profile. However, 250 discrepancies still remain as the standard deviation centerline EPL for $x/D_l > 3$ and the liquid core length PDF 251 exhibits larger values. This can likely be attributed to the turbulence coming from the nozzle which is known to have a 2.52 destabilizing effect [15] and absent in the analytical inflow velocity profiles. Mean centerline EPL statistics and liquid 253 core length for $2\delta_w$ have much larger values than all cases, confirming that increasing vorticity thickness increases the 2.54 liquid core length. Table 3 summarizes the mean and standard deviation liquid core length and the flapping Strouhal 255 number. Results show that decreasing the vorticity thickness decreases the mean liquid core length while increasing 256 the dominant frequency. The latter is a trend consistent with past studies [10, 24] and related to studying the influence 257 258 of gas velocity deficits on temporal dynamics [24, 25]. However, using an analytical profile seems to under-predict the flapping Strouhal number by approximately 30% under the range of vorticity thicknesses presented here. This is 259 further evidence that turbulent fluctuations play a key role on the break up processes and in particular, on the dominant 260





Figure 9: (Color online) Influence of velocity model on a-b) EPL statistics and c) $2\delta_w$ (•••, •), δ_w (•••, •) and $\delta_w/2$ (•••, •) compared against the benchmark (---, •).

Table 3: Summary of mean and standard deviation of L_B and flapping Strouhal number obtained from binarized images for gas velocity profiles at different vorticity thicknesses.

	$\langle L_B \rangle / D_l$	$L_{B,std}/D_l$	S t
$2\delta_w$	8.59	0.539	4.66×10^{-3}
δ_w	6.92	1.18	4.93×10^{-3}
$\delta_w/2$	6.24	1.16	5.57×10^{-3}
Benchmark	5.24	1.15	7.52×10^{-3}

262 5. Impact of Contact Line Model

263 5.1. Effect of Contact Line Location

The contact line model was varied by pinning the contact line to the splitter plate inner wall, outer wall and allowing for a free moving contact line with a static contact angle of 85°. The gas flow model was maintained as an analytical velocity profile according to Eq. (8) with a vorticity thickness δ_w .

Pinning the interface to the inner wall models the splitter plate as a fully unwet wall. This contact line model creates a gas re-circulation and low pressure region just downstream of the splitter plate. This gives rise to aspiration of the interface in the radial direction towards the gas. The consequence of this is observed in Fig. 10a where the initial mean EPL increases as the downstream distance is increased. It is only after $x/D_l \approx 0.25$, that the interface reaches the bulk of the high-speed gas stream and subsequently exhibits a monotonic decrease in mean EPL.

Pinning the interface to the outer wall models the splitter plate as a fully wet wall. Experimental high-resolution visible light imaging and X-ray imaging have shown that at this operating condition, the contact line lies mostly near the outer wall [13, 32]. Moreover, when adding swirl to the gas, it is observed that the contact line can even wick up into the gas flow region as shown in Fig. 11a. Therefore, pinning to the outer wall more closely matches the local experimental flow configuration. This pinning model results in a mean centerline EPL that decreases monotonically which is experimentally observed (see Fig. 5b).



Figure 10: (Color online) Influence of contact line model on a-b) EPL statistics and c) liquid core length PDFs for pinned to inner wall (--, ▶), outer wall (--, ♦) and a free contact line (--, ■).

One can see in Fig. 10a that using a free contact line with an SGS contact line force with $\theta_s = 85^\circ$ leads to similar mean EPL profiles to pinning to the outer wall. Figure 11b shows the PDF of the normalized radial location for the contact line such that a value of 0 indicates the interface is located at the inner wall while a value of 1 indicates it is at the outer wall. For $\theta_s = 85^\circ$, the contact line radius peaks near the outer wall, serving as an explanation of why pinning to the outer wall and this free contact line have similar mean EPL profiles. It can be observed in Fig. 10b that a free contact line model leads to more interfacial dynamics than pinning the outer wall since its standard deviation EPL profile is uniformly larger.

Figure 10c shows the PDF of the liquid core length and Table 4 summarizes the mean and standard deviation 285 centerline EPL and Strouhal numbers for all three cases. Pinning to the inner wall leads to a liquid that is too stable 286 as quantified by the large mean liquid core length and at times, the liquid core length is observed to exceed the 287 downstream domain boundary. Pinning to the outer wall and having a free contact line have similar PDFs, with the 288 free contact line exhibiting a slightly smaller mean liquid core length. Studies have shown that the vorticity thickness 289 has a strong impact on the dominant frequency [10, 24]. Results show that the flapping Strouhal numbers are all 290 within 2% of each other, suggesting that the dominant frequency is mostly independent of the contact line model for 291 a fixed vorticity thickness. 292



Figure 11: (Color online) a) Experimental image showing an instance where the contact line wicked up the outer wall into the gas flow region in the presence of gas swirl and b) $\theta_s = 70^{\circ}$ (----), $\theta_s = 85^{\circ}$ (----), $\theta_s = 110^{\circ}$ (----).

	$\langle L_B \rangle / D_l$	$L_{B,std}/D_l$	S t
Pin to inner wall	8.50	0.583	4.92×10^{-3}
Pin to outer wall	7.16	0.950	5.06×10^{-3}
Free contact line	6.92	1.18	4.92×10^{-3}

Table 4: Summary of mean and standard deviation of L_B and flapping Strouhal number for different contact line models.

293 5.2. Effect of Static Contact Angle θ_s

The static contact angle depends on many factors such as surface roughness, temperature, nozzle material and treatment. For aluminum, water and air, a reasonable static contact angle is between $70^{\circ} - 90^{\circ}$ [22, 40]. In the present study, we consider the static contact angles 70° , 85° , and 110° which model a moderately hydrophylic, less hydrophylic, and moderately hydrophobic surface respectively. In these simulations, an auxiliary nozzle simulation was used to provide the gas inflow velocity. Figure 11b shows the contact line radius PDFs measured at a fixed arc

location. The PDFs show that the contact lines sit very close to the outer wall for $\theta_s = 70^\circ$, further away from the 299 outer wall for $\theta_s = 85^\circ$ and near the inner wall for $\theta_s = 110^\circ$. Figure 12a shows the mean and standard deviation 300 centerline EPL profiles for simulations using these static contact angles. Because a simulation using $\theta_s = 110^\circ$ results 301 in a contact line close to the inner wall, its EPL profile follows a similar behavior to pinning to the inner wall, with an 302 initial increase in EPL and subsequent monotonic decrease. Similarly, a simulation using $\theta_s = 70^\circ$ results in a contact 303 line close to the outer wall and as such, exhibits a behavior similar to pinning to the outer wall in that a monotonic 304 decrease in EPL is observed. Figure 12b shows that increasing θ_s shifts the standard deviation centerline EPL to the 305 right. Figure 12c shows the PDFs of the liquid core length for simulations using $\theta_s = 70^\circ$ and 85° are similar while 306 110° results in a profile shifted to the right. Table 5 summarizes the mean and standard deviation centerline EPL and 307 flapping Strouhal number showing that as θ_s is increased, the liquid core length and dominant frequency also increase. 308 This highlights the significant impact that the contact angle model can have on the downstream liquid distribution. 309



Figure 12: (Color online) Influence of static contact angle on a-b) EPL statistics and c) liquid core length PDFs for $\theta_s = 70^\circ$ (---, >), 85° (---, (---, -), 85° (----

Table 5: Summary of mean and standard deviation of L_B and flapping Strouhal number for different static contact angles.

θ_s	$\langle L_B \rangle / D_l$	$L_{B,std}/D_l$	S t
70°	4.52	0.810	7.01×10^{-3}
85°	4.65	0.751	6.63×10^{-3}
110°	5.38	0.866	8.56×10^{-3}

310 6. Conclusion

In this study, we have performed simulations of air-blast atomization in a coaxial two-fluid atomizer using a geometric Volume-of-Fluid method. Simulations were validated against experiments under identical air/water conditions and geometries. Excellent agreement of quantities such as the mean equivalent path length of the liquid (EPL), liquid core length, and dominant frequency was observed. A mesh refinement study was also conducted showing that these quantities were reasonably well mesh converged. The liquid was modeled using a Poiseuille flow while the gas inflowand contact line models were studied.

The gas inflow models considered were analytical velocity profiles at different vorticity thicknesses with no tur-317 bulent fluctuations added and an auxiliary nozzle simulation. Simulations using analytical velocity profiles were 318 benchmarked against a simulation using the nozzle simulation. Results showed that decreasing the vorticity thickness 319 decreased the mean liquid core length, the mean centerline EPL, and increased the dominant frequency of the liquid 320 jet motions. While one analytical profile had a vorticity thickness that was close in value to the experiment and nozzle 321 simulation, quantities such as the mean liquid core length remained larger. Furthermore, although decreasing the 322 vorticity thickness increased the dominant frequency, a trend reported in other studies [10, 24], the dominant frequen-323 cies for the presented vorticity thicknesses yielded systematically lower values than the experiment. These results 324 confirmed that turbulent fluctuations in the gas play an important role. 325

The contact line models considered were pinning to the inner wall of the splitter plate, the outer wall of the splitter 326 plate, and allowing for a free contact line with a (SGS) contact line model using a static contact angle of 85°. This 327 study showed that the contact line model has a key influence on the liquid jet development and on the liquid distribution 328 downstream. In particular, pinning to the outer wall or using a free moving contact line yielded better experimental 329 agreement of quantities such as mean and standard deviation centerline EPL and mean liquid core length than pinning 330 to the inner wall. Pinning to the inner wall resulted in an initial increase in mean centerline EPL downstream of the 331 nozzle because of a re-circulation region created by the gas. In contrast, pinning to the outer wall or having a free 332 moving contact line resulted in the monotonic decrease in EPL observed in the experiment. Results also indicated 333 that when using an analytical gas velocity profile with a fixed vorticity thickness, the contact line model does not have 334 a significant impact on the dominant frequency. The static contact angle was varied between $\theta_s = 70^\circ$, $\theta_s = 85^\circ$, 335 and $\theta_s = 110^\circ$. Results showed in the $\theta_s = 70^\circ$ case, i.e., modeling a hydrophylic surface, the mean centerline EPL 336 exhibited similar trends to pinning to the outer wall while in the $\theta_s = 110^\circ$ case, i.e., modeling a hydrophobic surface, 337 trends were similar to pinning to the inner wall. 338

As the near-field region has been validated in this study and a better understanding of the impact of the gas velocity 339 and contact line models have been gained, several research questions remain open. Since computational tools now 340 result in strong agreement of liquid distribution compared against experiment, our research efforts will now shift 341 to modeling the conversion of broken liquid structures in atomization simulations to Lagrangian particles in spray 342 dispersion simulations. Promising research efforts have been made in this direction (e.g., [18, 36]) ([6]). The inflow 343 modeling of the gas has been studied in various forms which include modeling the velocity profile just downstream 344 of the nozzle exit using a velocity deficit (e.g., [24, 25]). However, current literature has not considered in detail the 345 influence of the contact line which this study has shown to have an impact. Thus, a more detailed study of the contact 346 line physics and different modeling strategies for the contact line would be useful. 347

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356 References

- G Agbaglah, R. Chiodi, and O. Desjardins. Numerical simulation of the initial destabilization of an air-blasted liquid layer. *Journal of Fluid Mechanics*, 812:1024–1038, 2017.
- [2] D. M. Anderson, G. B. McFadden, and A. A. Wheeler. Diffuse-interface methods in fluid mechanics. *Annual Review of Fluid Mechanics*, 30(1):139–165, 1998.
- [3] Julie K Bothell, Nathanael Machicoane, Danyu Li, Timothy B Morgan, Alberto Aliseda, Alan L Kastengren, and Theodore J Heindel.
 Comparison of X-ray and optical measurements in the near-field of an optically dense coaxial air-assisted atomizer. *International Journal of Multiphase Flow*, 125:103219, 2020.
- Julien Carmona, N. Odier, Olivier Desjardins, Benedicte Cuenot, A. Misdariis, and A. Cayre. A comparative study of direct numerical
 simulation and experimental results on a prefilming airblast atomization configuration. *Atomization and Sprays*, 31(8):9–32, 2021.
- R. Chiodi and O. Desjardins. A reformulation of the conservative level set reinitialization equation for accurate and robust simulation of
 complex multiphase flows. *Journal of Computational Physics*, 343:186–200, 2017.
- [6] Robert Chiodi and Olivier Desjardins. General, robust, and efficient polyhedron intersection in the interface reconstruction library. *Journal* of Computational Physics, 449:110787, 2022.
- [7] Antoine Delon, Alain Cartellier, and Jean-Philippe Matas. Flapping instability of a liquid jet. Phys. Rev. Fluids, 3:043901, Apr 2018.
- [8] F. Demoulin, P. Beau, G. Blokkeel, A. Mura, and R. Borghi. A new model for turbulent flows with large density fluctuations: Application to
 liquid atomization. *Atomization and Sprays*, 17:315–345, 2007.
- [9] O. Desjardins, G. Blanquart, G. Balarac, and H. Pitsch. High order conservative finite difference scheme for variable density low Mach
 number turbulent flows. *Journal of Computational Physics*, 227:7125–7159, 2008.
- [10] D. Fuster, J.P. Matas, Marty S., Popinet S., J Hoepffner, Cartellier A., and Zaleski S. Instability regimes in the primary breakup region of
 planar coflowing sheets. *J. Fluid Mech.*, 736:150–176, 2013.
- [11] Daniel Fuster, Anne Bagué, Thomas Boeck, Luis Le Moyne, Anthony Leboissetier, Stéphane Popinet, Pascal Ray, Rubenand Scardovelli,
 and Stéphane Zaleski. Simulation of primary atomization with an octree adaptive mesh refinement and VOF method. *International Journal* of Multiphase Flow, 35:550–565, 2009.
- [12] M. Gorokhovski and M. Herrmann. Modeling primary atomization. Annual Review of Fluid Mechanics, 40:343–366, 2008.
- [13] Theodore J. Heindel. X-ray imaging techniques to quantify spray characteristics in the near-field. *Atomization and Sprays*, 28:1029–1059,
 2018.
- [14] M. Hermann. A balanced force refined level set grid method for two-phase flows on unstructured flow solver grids. *Journal of Computational Physics*, 227:2674–2706, 2008.
- [15] D. Jiang and Y. Ling. Impact of inlet gas turbulence on the formation, development and breakup of interfacial waves in a two-phase mixing
 layer. *Journal of Fluid Mechanics*, 921:A15, 2021.
- [16] Maxime Kaczmarek, Rodrigo Osuna-Orozco, Peter Dearborn Huck, Alberto Aliseda, and Nathanaël Machicoane. Spatial characterization of
 the flapping instability of a laminar liquid jet fragmented by a swirled gas co-flow. *International Journal of Multiphase Flow*, 152:104056,
 2022.
- [17] Alan Kastengren, Christopher F. Powell, Dohn Arms, Eric M. Dufresne, Harold Gibson, and Jin Wang. The 7BM beamline at the aps: a
 facility for time-resolved fluid dynamics measurements. *Journal of Synchrotron Radiation*, 19(4):654–657, July 2012.
- [18] Dokyun Kim and Parviz Moin. Subgrid-scale capillary breakup model for liquid jet atomization. *Combustion Science and Technology*,
 192:1334–1357, 2010.
- [19] Y. Ling, D. Fuster, S. Zaleski, and G. Tryggvason. Spray formation in a quasi-planar gas-liquid mixing layer at moderate density ratios: A
 numerical closeup. *Phys. Rev. Fluids*, 2:014005, 2017.
- [20] N. Machicoane, G. Ricard, R. Osuna-Orozco, P. Huck, and A. Aliseda. Influence of steady and oscillating swirl on the near-field spray
 characteristics in a two-fluid coaxial atomizer. *International Journal of Multiphase Flow*, 129:103318, 2020.
- [21] Nathanael Machicoane, Julie K. Bothell, Danyu Li, Timothy B. Morgan, Theodore J. Heindel, Alan L. Kastengren, and Alberto Aliseda.

- Synchrotron radiography characterization of the liquid core dynamics in a canonical two-fluid coaxial atomizer. *International Journal of Multiphase Flow*, 115:1–8, 2019.
- 401 [22] Majid H. Majeed. Static contact angle and large water droplet thickness measurements with the change of water temperature. *Al-Nahrain* 402 *Journal for Engineering Sciences*, 17:114–128, 2014.
- 403 [23] Philippe Marmottant and Emmanuel Villermaux. On spray formation. Journal of Fluid Mechanics, 498:73–111, 2004.
- 404 [24] Jean-Philippe Matas, Antoine Delon, and Alain Cartellier. Shear instability of an axisymmetric air-water coaxial jet. *Journal of Fluid* 405 *Mechanics*, 843:575–600, 2018.
- [25] Jean-Philippe Matas, Sylvain Marty, and Alain Cartellier. Experimental and analytical study of the shear instability of a gas-liquid mixing
 layer. *Physics of Fluids*, 23(9):094112, 2011.
- [26] Jean-Philippe Matas, Sylvain Marty, Mohamed Seydou Dem, and Alain Cartellier. Influence of gas turbulence on the instability of an air-water
 mixing layer. *Phys. Rev. Lett.*, 115:074501, August 2015.
- 410 [27] C. Meneveau, T. S. Lund, and W. H. Cabot. A Lagrangian dynamic subgrid-scale model of turbulence. J. Fluid Mech., 319:353–385, 2000.
- [28] T. Müller, A. Sänger, P. Habisreuther, T. Jakobs, D. Trimis, T. Kolb, and N. Zarzalis. Simulation of the primary breakup of a high-viscosity
 liquid jet by a coaxial annular gas flow. *International Journal of Multiphase Flow*, 87:212–228, 2016.
- [29] M. Owkes and O. Desjardins. A computational framework for conservative, three-dimensional, unsplit, geometric transport with application
 to the volume-of-fluid (VOF) method. *Journal of Computational Physics*, 270:587–612, 2014.
- [30] J. E. Pilliod and E. G. Puckett. Second-order accurate volume-of-fluid algorithms for tracking material interfaces. *Journal of Computational Physics*, 199:465–502, 2004.
- [31] Stephane Popinet and Stephane Zaleski. A front-tracking algorithm for accurate representation of surface tension. *International Journal for Numerical Methods in Fluids*, 30:775–793, 1999.
- Guillaume Ricard, Nathanaël Machicoane, Rodrigo Osuna-Orozco, Peter D. Huck, and Alberto Aliseda. Role of convective acceleration in
 the interfacial instability of liquid-gas coaxial jets. *Phys. Rev. Fluids*, 6:084302, August 2021.
- 421 [33] William J. Rider and Douglas B. Kothe. Reconstructing volume tracking. Journal of Computational Physics, 141(2):112–152, 1998.
- [34] Ruben Scardovelli and Stéphane Zaleski. Interface reconstruction with least-square fit and split Eulerian–Lagrangian advection. *International Journal for Numerical Methods in Fluids*, 41, 2003.
- 424 [35] J. A. Sethian and P. Smereka. Level set methods for fluid interfaces. Annual Review of Fluid Mechanics, 35(1):341–372, 2003.
- 425 [36] G. Tomar, D. Fuster, S. Zaleski, and S. Popinet. Multiscale simulations of primary atomization. Computers & Fluids, 39:1864–1874, 2010.
- [37] G. Tryggvason, B. Bunner, A. Esmaeeli, D. Juric, N. Al-Rawahi, et al. A front-tracking method for the computations of multiphase flow.
 Journal of Computational Physics, 169(2):708–759, 2001.
- [38] Sheng Wang and Olivier Desjardins. 3D numerical study of large-scale two-phase flows with contact lines and application to drop detachment
 from a horizontal fiber. *International Journal of Multiphase Flows*, 101:35–46, 2018.
- [39] F. Xiao, M. Dianat, and J.J. McGuirk. LES of turbulent liquid jet primary breakup in turbulent coaxial air flow. *International Journal of Multiphase Flow*, 60:103–118, 2014.
- 432 [40] Zhi-Qiang Zhu, Yang Wang, Qiu-Sheng Liu, and Jing-Chang Xie. Influence of bond number on behaviors of liquid drops deposited onto
- 433 solid substrates. *Microgravity Science and Technology*, 24, 06 2012.