

A Survey of Modeling of Lattice Structures Fabricated by Additive Manufacturing

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Abstract

The lattice structure is a type of cellular material with truss-like frames which can be optimized for specific loading conditions. The fabrication of its intricate architecture is restricted by traditional manufacturing technologies. However, Additive Manufacturing (AM) enables the fabrication of complex structures by aggregation of materials in a layer-by-layer fashion, which has unlocked the potential of lattice structures. In the last decade, lattice structures have received considerable research attention focusing on the design, simulation and fabrication for AM techniques. And different modeling approaches have been proposed to predict the mechanical performance of lattice structures. This review introduces the aspects of modeling of lattice structures and the correlation between them; summarizes the existing modeling approaches for simulation; and discusses the strength and weakness in different simulation methods. This review also summarizes the characteristics of AM in manufacturing cellular materials and discusses their influence on the modeling of lattice structures.

Keyword: Additive Manufacturing, Finite Element Analysis, Homogenization, Lattice Structure

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1. Introduction

The word ‘lattice’ derives from old French ‘latte’ and it is defined as a structure consisting of strips of wood or metal crossed and fastened together with square or diamond-shaped spaces left between [1]. In this review, the lattice structure refers to a type of cellular materials [2] that has a truss-like structure with interconnected struts and nodes in a three-dimensional (3D) space. Compared to other cellular materials such as random foams and honeycombs, the lattice structure exhibits better mechanical performance [3]. By tailoring the material, the lattice structure can be optimized to satisfy specific functional requirements, which means the mechanical properties are more flexible to be controlled.

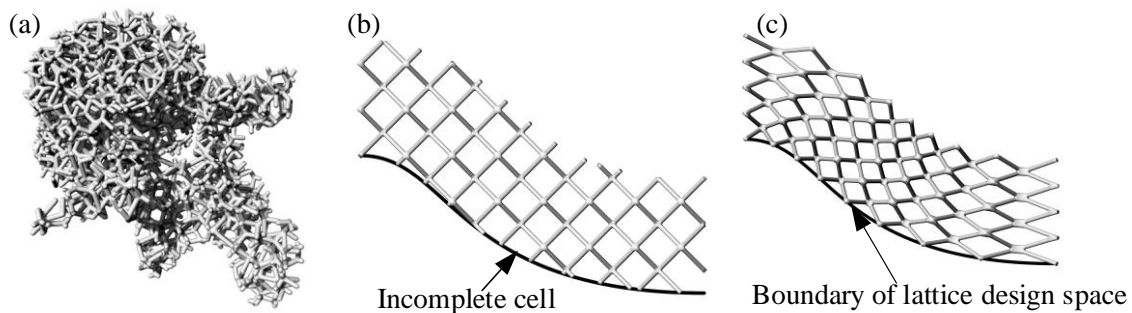


Figure 1. Examples of different types of lattice structures based on the degree of order, (a) Disordered lattice structures, (b) Periodic lattice structures, (c) Conformal lattice structures

According to literatures [4-6], there are more than one methods to classify the lattice structures. In this paper, lattice structures are categorized based on their degree of order of the lattice frame. Generally, they can be classified into three categories. The first type is called disordered lattice structures or randomized lattice structures. The unit cells of this type of lattice structures are randomly distributed inside the design space with different topologies and cell size. An example of disordered lattice structures is shown in

Figure 1(a). The second type of lattice structures is called periodic lattice structure as shown in Figure 1(b). This type of lattice structures can be regarded as a structure created by a regular periodic repetition of a unit cell with certain shape, topology and size in a three-dimensional Euclidean space. Thus, every cell in this type of lattice structures is in the same topology and size. Besides disordered lattice structures and periodic lattice structures, another type of cellular structure is called pseudo-periodic lattice structures. In this type of lattice structures, lattice cell only share the same topology but different size and shape. For example, the conformal lattice structure which is firstly proposed by Wang and Rosen [7] is a typical pseudo-periodic lattice structure. Conformal lattice structures are capable of keeping the integrity of their unit cells on the boundary as shown in Figure 1(c), which can stiffen or strengthen a complex and curved surface than periodic lattice structures [8, 9]. Both the periodic and the pseudo-periodic lattice structures can be further divided into two sub-types based on the uniformity of strut's thickness. They are homogenous lattice structures and heterogenous lattice structures.

Due to tailorable properties, the periodic and pseudo-periodic lattice structures are more widely used in engineering applications. In most cases, the lattice structure is applied as lightweight core materials in a sandwich structure to transverse shear and compression loads. Compared to honeycombs, the lattice structure has the potential to improve compressive and shear strengths when designed to suppress buckling [10, 11]. Heterogeneous lattice structures with spatially graded density matched to the local loads can further save the weight of traditional cores with uniform density and properties. The lattice structures can also be used as energy-absorbing materials for protection from impact and shockwaves. Schaedler et al. [12] have investigated different types of metallic

microlattice structures for energy absorber by quasi-static compression tests. It was shown that the lattice structure offers more flexibility in tailoring the response to impulsive loads than conventional materials can. Because lattice structures have high surface area-to-volume ratio, they are ideal materials for thermal management [13, 14]. The periodic lattice cores have shown better cooling performance than textiles and foams by comparing various heat sink technologies [15]. Besides, the lattice structure can also be used as biocompatible materials to repair tissue, cartilage and bone. It has the flexibility to satisfy the patient-specific defect geometry and biological features as well as mechanical properties [16].

Lattice structures with sophisticated geometries are successfully fabricated by several manufacturing techniques. Among them, Additive Manufacturing (AM) is especially well suited for the fabrication of complex lattice structures. AM is defined as ‘the process of joining materials to make objects from 3D model data, usually layer upon layer’ [17]. Because AM does not require specialized tooling. Structures with complex geometries can be fabricated by AM without dramatically increasing the manufacturing cost. Lattice structures designed for engineering applications have been successfully fabricated by different types of AM techniques such as Stereolithography (SLA) [18], Fused Deposition Modeling (FDM) [19, 20], Binder Jetting(BJ) [21], Selective Laser Melting (SLM) [22], Selective Laser Sintering (SLS) [23], and Electron Beam Melting (EBM) [24, 25]. Schaedler and Carter [2] summarized and compared different types of AM for lattice structures with respect to the geometry, material, graded properties, feature size, application performance and production rate. AM techniques can also be combined with metal casting, which is called “Indirect AM Based Casting”, to fabricate lattice structures

[26]. Even though this technique takes more steps to fabricate lattice structures, it can remove several existing constraints on the AM process such as thermal residual stress, poor surface finish and limited material selection. Recently, ultralight metallic microlattices have been fabricated by depositing thin-film metallic materials on the AM produced polymer template which is subsequently removed by chemical etching [27]. Apart from AM, lattice structures can also be fabricated by traditional manufacturing methods. One type of 3D carbon fiber reinforced plastic (CFRP) lattice is assembled by 2D building blocks of [0/90] CFRP laminate with reversible snap-fit connectors [28]. 3D metallic and composite lattices can also be fabricated by weaving, braiding, and knitting fibers and wires. However, these approaches are only able to manufacture lattice structures with simple topology which limits the freedoms of design. AM is still the most ideal and prevalent way to manufacture lattice structures currently.

However, there are two reasons that make it a challenge to precisely predict the mechanical performance of lattice structures fabricated by AM process. Firstly, because of the intricate geometry of lattice structures, existing methods may not be suitable for the simulation of the mechanical performance in engineering applications. Both the computational cost and the accuracy need to be improved for the simulation process of lattice structures with complex geometries and properties. Secondly, the AM process has unique characteristics in the fabrication which affect the properties of lattice structures. Although AM has the capability of fabricating complex structures, currently, it still has limitations. Understanding those limitations and characteristics can help designers utilize AM processes to manufacture lattice structures and simulate their mechanical properties more effectively.

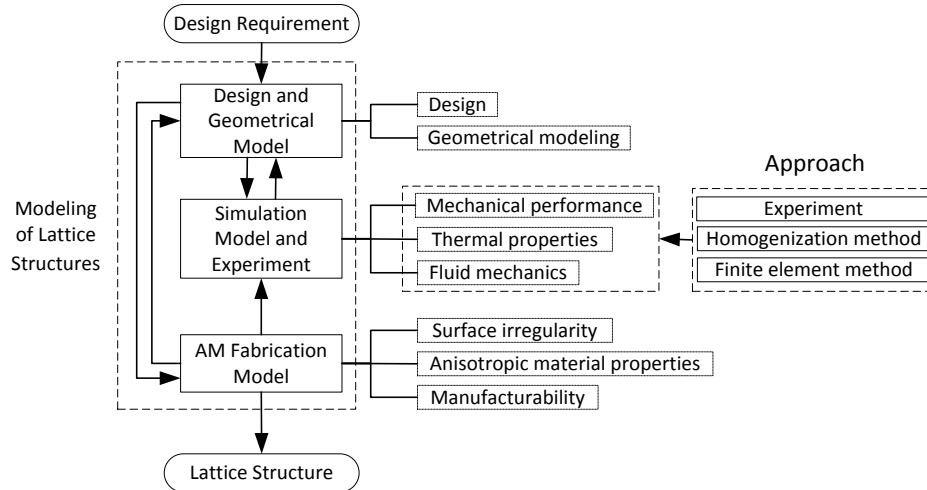


Figure 2. The concept of modeling of lattice structures for AM process

In this paper, a concept called modeling of lattice structures for AM is presented as shown in Figure 2. This concept is based on the design and fabrication methods for Additive Manufacturing proposed by Rosen [29], Yang et al [30], and Seepersad et al [31]. Rosen proposed a concept called Design for Additive Manufacturing (DFAM) that can support part modeling, process planning, and manufacturing simulations. This method includes the solution algorithms, analysis codes, libraries of materials and mesostructures, process planning and analysis of as-manufactured model. Yang et al proposed an approach that combines the analytical modeling, experimentation and simulation for the design of lattice structures. It is concluded that manufacturing factors are coupled with the actual cellular design, which need to be incorporated in to the geometric models to enable more accurate designs.

Based on existing theories, the concept in this paper is divided into three aspects: design and geometrical modeling; simulation modeling; and AM fabrication modeling. Based on functional requirements, the proper lattice structure is designed and generated. Then the

design result is the geometrical input to the simulation modeling step. The simulation result then goes back to the geometrical modeling stage for the optimization of the initial design. The optimized geometrical model is the input to the AM fabrication modeling step. AM fabricated lattice structures need to be examined to check the manufacturability [32]. If it is not manufacturable, the geometrical model should be modified to remove unsuitable features for fabrication. Besides, the manufacturing process may have influence on the mechanical properties of lattice structures such as the irregular surface roughness and the anisotropic material properties, which also needs to be investigated. The influence of AM process should then be imported into the simulation model to improve the accuracy of the simulation result. When simulation results satisfy design requirements and the design model is manufacturable, the lattice structure can be fabricated, which finalize the modeling process.

This paper attempts to provide a comprehensive review of the state-of-the-art modeling approaches of lattice structures for researchers who aim to investigate the mechanical performance of lattice structures by experimental methods or simulations. In Section 2, experimental approaches as well as simulation modeling methods such as homogenization and Finite Element (FE) used in the investigation of mechanical performance of lattice structures will be discussed. Furthermore, manufacturing characteristics of AM have influence on the mechanical performance of lattice structures. These characteristics including surface irregularity and anisotropic material properties will be discussed in Section 3. Finally, these modeling methods are concluded and some future research to improve the existing modeling techniques of lattice structures are given in the last section.

2. Mechanical performance modeling

The mechanical performance of cellular materials has been investigated for decades. In the early stage, restricted by the manufacturing techniques, only simple cellular structures were studied. Gibson et al. [33] investigated the mechanical properties of two dimensional cellular material with beam theory and compared the result with experimental data. The mechanical properties of 3D cellular materials were linked to the relative density ρ/ρ_s , where ρ is the density of the cellular materials and ρ_s is the density of the solid of which the structure is made. The relationships between linear elastic properties and the relative density for open-cell and closed-cell cellular material are given by [4, 34]

$$E/E_s \propto (\rho/\rho_s)^2 \quad (\text{open cell}) \quad (1)$$

$$E/E_s = C_1\phi^2(\rho/\rho_s)^2 + C'_1(1 - \phi)(\rho/\rho_s) \quad (\text{closed cell}) \quad (2)$$

Where E is the elastic modulus of the cellular material and E_s is the elastic modulus of the solid material of which the cellular material is made. ϕ is the fraction of solid in the cell edges. C_1 and C'_1 are simply constants of proportionality. Other mechanical properties including elastic collapse, plastic collapse, creep, brittle crushing and fracture toughness were also correlated with the relative density [35]. Compressive experiments of cellular solids were conducted to get the stress-strain curve which was characterized by three regimes: a linear-elastic regime caused by elastic bending or stretching, a stress plateau caused by buckling, yielding or crushing, a densification caused by the load of the edges and cells against one another [36, 37].

The lattice structure is a type of cellular material which provides more flexibility to control the mechanical properties than the foam and honeycomb structures. Even though the relationship between the relative density and the mechanical performance of lattice structures can give designers a basic standard to choose the porosity of the lattice, it is difficult to precisely determine the mechanical performance of lattice structures only by the relative density. For instance, different topologies with the same porosity may have totally different mechanical properties such as the elastic modulus, shear modulus and Poisson's ratio. In order to predict the mechanical performance more accurately, the experiment, homogenization and FE methods are widely used to simulate lattice structures with different topologies.

Table 1a A summary of compressive elastic modulus of lattice structures obtained from experiments





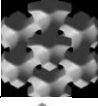

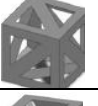

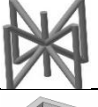
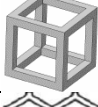
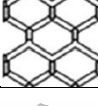
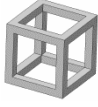
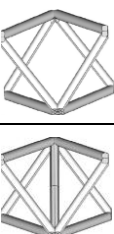

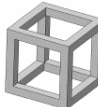
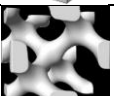



AM process	material	Elastic modulus of bulk material (GPa)	Lattice topology	Relative density (%)	Compressive Elastic modulus (MPa)	Reference	
SLS	polyamide powder	2.4		10	67.2	[38]	
					21.6		
					40.8		
					62.4		
	Polycaprolactone (PCL)	0.122 0.013		45±0.9 ~62.5±1.5	54±3 ~67±4	[39]	
	polyamide EOSINT P/PA2200	1.419 ±0.105		20	49.67±9.93	[23]	
				40	163.19±1.42		
				60	351.91±4.26		
					20		509.42±4.26
					40		175.96±11.35
60					378.87±49.67		
				20	52.50±2.84		
				40	153.25±8.51		
	60	313.60±14.19					
SLA	RenShape™ SL 7510 resin	2.634	1x1x1 octet	35	107	[40]	
			2x2x2 octet		60		
			3x3x3 octet		65		
FDM	Polylactic Acid	1684.87 ±144.7		7	49.07±0.13	[41]	
BJ	316L stainless steel	4.07		25.9	650	[21]	
				50	1480		
EBM	Ti6Al4V	110		5~11	50~225	[42]	
		120		50.25±1.00	570±50	[25]	
				20.78±0.63	2130±210		
				39.59±0.81	2680±120		
				49.25±0.69	2920±170		
		114	Octet as built	7.3	912	[43]	
				14	2041		
				28.5	6407		
				Octet chemically etched	3.9		513
					7		912
21	4560						

Table 1b A summary of compressive elastic modulus of lattice structures obtained from experiments

AM process	material	Elastic modulus of bulk material (GPa)	Lattice topology	Relative density (%)	Compressive Elastic modulus (MPa)	Reference
SLM	Ti6Al4V-ELI	Not mentioned	rhombic dodecahedron unit cells	16	549±76	[44]
				22	1397±115	
				30	2619±64	
				33	3488±137	
	316L stainless steel	140		3.5	10.6	[45]
				5.4	19.8	
				9.7	105	
				13.9	207.5	
				4.0	84.6	
				6.2	804.9	
				11.1	1506.2	
				15.9	2273.2	
		97±10 (Micro strut)		3.5-13.8	17.646~378	[46]
	CoCr alloy	200		20	4143	[47]
				30	6260	
				40	9844	
	AlSi10Mg	72.4		10	177.89~198.39	[48]
	Ti6Al4V	110		5-20	130±20 ~1250±40	[49]
					120±30 ~1250±70	
	Ti6Al4V	114		25	1900±100	[50]
30				900±100		
40				3100±400		
50				4300±100		
			25	1200±400		
			30	1400±200		
			40	3400±300		
			50	4600±200		

2.1 Experimental Method

Experimental method is the most direct way to get the mechanical properties of as-fabricated lattice structures. In the last decade, a number of experiments such as compression [51], bending [52] and tensile [53] tests, impact loading tests [54], dynamic

tests [55], and fatigue test [56] have been done to investigate the performance of lattice structures fabricated by different types of AM techniques. The compressive elastic modulus of lattice structures obtained from experimental methods are summarized in Table 1.

It has been shown by lots of experiments that the mechanical properties of lattice structures fabricated via AM cannot be simply determined by the relative density. Many researchers found that the compressive modulus of lattice structures is related to the strut dimension, the cell size and the surface roughness as well. Parthasarathy et al. [25] studied the strength of Ti6Al4V cube lattice structure made by EBM with porosities ranging from 49.75% to 70.32%. It is found that for nearly same porosities (49.75% and 50.75%) with different strut thickness, the compressive modulus of the lattice structure decreased dramatically from 2.92 GPa to 0.57 GPa, which indicates that the strength of the lattice structure depends not only on the porosity of the structure, but also on the geometrical dimension of the lattice strut. Similar results were found by Yan et al. [48, 57]. They conducted compressive experiment on the AlSi10Mg diamond lattice structure fabricated by SLM. The result showed that with the same volume fraction, the compressive strength was decreasing with the increase of the size of the unit cell. This can be explained by the “effective volume ratio” of the lattice strut that is proposed by Suard et al. [58]. Because the surface roughness of the strut fabricated by EBM is high, which has more influence on the mechanical properties of the thinner strut. Formanoir et al. [43] investigated the influence of the chemical etching on the mechanical properties of EBM fabricated Ti-6Al-4V octet-truss lattice structures by compression tests. The result showed that with the same relative density, the lattice structure after the chemical etching

had a higher stiffness than the as-built structure due to the decrease in the surface roughness.

It is also found by experiments that many types of defects are likely to occur in AM fabricated lattice structures such as the irregular strut size, internal porosity and surface breaking defects. Qiu et al. [59] used optical microscopy (OM), scanning electron microscopy (SEM) and micro-CT to investigate the as-fabricated strut size, morphology and internal porosity of AlSi10Mg diamond lattice structures fabricated by SLM and correlate them with the compressive properties. The primary conclusion is that the diameter of the strut increase monotonically with laser power, which improves the compressive properties, but deviated from the designed geometry. The defects of the Ti6Al4V cube lattice structure fabricated by EBM process have also been studied to understand their effects on the mechanical response [60]. The result shows that the compressive yield strength was not affected much by the horizontal struts even though there are large surface breaking defects in them. Because the load direction is along the vertical struts which means the horizontal struts are redundant. However, the load direction along the horizontal struts is not discussed in this literature. The influence of the surface defect on the compressive yield strength still needs to be investigated.

Even though the experimental method can directly obtain the mechanical properties of lattice structures fabricated via different AM techniques with different geometrical characteristics, there are some obvious limitations to implement the experimental method in engineering applications. Since the fabrication cost of AM techniques is still high, the experimental method requires a certain amount of samples to minimize the error and improve the experimental accuracy, which is not economical for AM processes. Secondly,

the speed of the manufacturing process of AM is relatively slow. It could take hours or days to fabricate a component via most of AM techniques. If a new lattice structure design needs to be verified for its mechanical performance, the experimental method is time-consuming which may delay the whole design process. Thirdly, in the conceptual design level, a comprehensive database is required to select the appropriate topology and relative density. It is not applicable to construct such a database by experimental method due to the cost of the time and money. Finally, to further improve the mechanical properties of lattice structures in engineering applications, the optimization process is vital at the design stage, which may need many rounds of iterations to find the optimal design. The experimental method is impractical to optimize the mechanical performance of the lattice structure. Therefore, it is imperative to simulate the mechanical properties of lattice structures analytically and numerically. Two modeling methods have been widely investigated and applied to estimate the mechanical response of lattice structures, which are the homogenization method and the Finite Element (FE) method.

2.2 Homogenization Method

The homogenization usually refers to a way to replace the composite with a kind of equivalent material model, which can overcome the difficulty in the analysis of the boundary value problem with high heterogeneities [61]. The mathematical theory of homogenization has developed in the 1970s [62, 63]. It is used to obtain the effective properties of homogenized material for periodic heterogeneous continuous media in many physical and engineering applications. It can be divided into two steps. Firstly, the local problem based on a unit cell is solved to get the effective material properties. Secondly, the overall problem is solved by substituting periodic material to the

homogenised material with equivalent properties. Compared with FE methods, the homogenization method can save much computational cost. As shown in Figure 3, the beam FE model comprises of 240000 elements while the solid FE model comprises only 1000 elements. Therefore, a radical reduction of the solution time and cost is achieved by application of the homogenised FE model [64, 65].

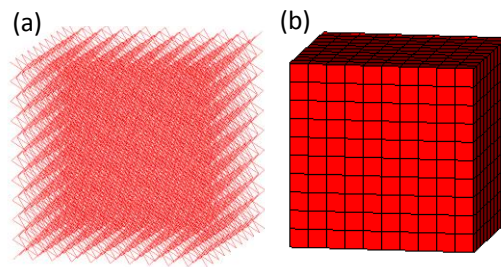


Figure 3. (a) FE model with beam elements, (b) Homogenized FE model with solid elements

The mechanical properties of lattice structures can be analysed by the homogenization method because it is a periodic structure constructed by unit cells. Based on an asymptotic expansion using periodicity, a homogenization approach with a solid model of lattice structures was developed. This approach is implemented to get the effective elastic modulus for a given unit cell. It can also be used in a design procedure to find the optimal topology of a unit cell under a certain boundary condition [66]. Rabczuk et al [67] implemented the homogenization method to represent the core cell of the impulsive load bearing sandwich panel by a continuum constitutive model with the consideration of buckling. The homogenized model was derived from the core cell by making the continuum-stored energy density function equal to a discrete energy associated to a representative core cell. This approach was more computational efficient to the fully discrete models yet results of both models showed very good agreement. Florence and Sab [68, 69] investigated the overall ultimate strength of general elastoplastic periodic 2D

and 3D lattice by using a rigorous homogenization method to solve unit cell problems with finite number of degrees of freedom. The method is restricted to the determination of overall linear elasticity constants and overall ultimate failure envelopes. The advantage of this method is that the non-uniform cell wall thickness and the non-symmetric material distribution in the cell edges can be considered in this method. Arabnejad and Pasini [70] investigated the mechanical properties of 6 different lattice topologies for a whole range of relative density by asymptotic homogenization.

Also, discrete homogenization approaches are widely used to simulate the mechanical properties of periodic lattice structures by using structural elements such as a truss element and a beam element. Tollenaere and Caillerie [71] applied the discrete homogenization method to model the quasi-repetitive lattice structures. The constitutive relation of their equivalent continuum was obtained by utilizing truss elements and pin-jointed nodes. This approach was also used to construct the equivalent macroscopic model for periodic structures such as graphene sheets which can be considered as lattices consisting of atoms and of interatomic bonds [72]. Reis and Ganghoffer [73] improved the discrete homogenization method by applying beam lattices instead of truss lattices. They used this approach to investigate the equivalent mechanical properties of auxetic lattices with two main mechanisms: the re-entrant and the rolling-up mechanism [74]. Because the predicted homogenized properties depend on the slenderness of the beam, and none of the simplifying assumptions are made, it provides more accurate results than those of Gibson and Ashby [36]. To investigate the large deformations of extensible beams and lattice structures, a heuristic homogenization technique was proposed by considering a discrete spring model to formulate a continuum fully nonlinear beam model

[75]. Recently a new homogenization approach using semi-rigid joint frame element shown in Figure 4(a) and as-fabricated model shown in Figure 4(b) for periodic lattice structures was presented in order to incorporate the geometrical discrepancies obtained during the AM process [76]. In this literature, three homogenization approaches were implemented to get the normalized elastic modulus; the proposed approach, the discrete homogenization with conventional frame elements, and the asymptotic homogenization. Two types of lattice structures, the cubic cell lattice and the diamond lattice were investigated by these three methods. The simulation results were compared to experimental result. The discrete homogenization with conventional beams lead more errors than the proposed method. Furthermore, the asymptotic approach yields large error in cubic cell specimens, but it gives relative accurate estimates in diamond unit specimens. The proposed method can estimate the modulus more accurately for both type of lattice structures. These results showed that the geometrical degradation during the AM process has significant impacts on mechanical properties of lattice structures and the proposed method enables accurate estimations of mechanical properties of the as-fabricated samples.

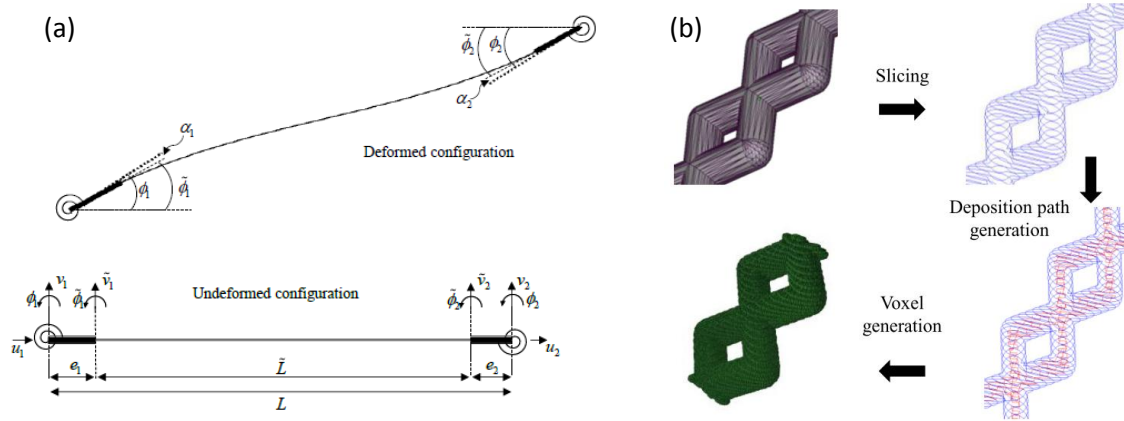


Figure 4. (a) the conceptual configuration semi-joint frame element (b) the as-fabricated voxel modeling procedure [76]

In biomechanics, Assidi et al. [77] implemented the discrete asymptotic homogenization method to calculate the mechanical properties of biological membranes with lattice configurations. The effective moduli are calculated and recorded versus the geometrical and mechanical lattice parameters. Goda et al. [78, 79] proposed a quasi periodical lattice model of the cancellous bone which was discretely homogenized to generate the continuum model. The effective mechanical properties of the bone directly relate to the lattice microgeometry and micromechanical elastic properties. To evaluate fracture of trabecular bone, the overall plastic yield and brittle failure behaviors of three dimensional lattices are investigated by a microstructural modeling approach based on the homogenization of the initially discrete microstructure [80].

Matrix methods of linear algebra have also been used to homogenize the structural mechanics of periodic lattices. Hutchinson and Fleck [81] applied Bloch's theorem in the matrix analysis and formulated a homogenized stiffness matrix by expressing the nodal deformation in a unit cell in terms of the macroscopic strain. This methodology is applied

to the collapse mechanisms of Kagome and triangular-triangular lattice structures. Vigliotti and Pasini [82] developed a general matrix-based homogenization approach for the linear analysis of components made of two dimensional lattice materials with either pin joints or rigid joints. A linear multiscale procedure has been described and validated by comparing the homogenized model of equivalent macroscopic stiffness with the discrete lattice model. The result has illustrated that the homogenised model delivered a correct estimation of the stiffness of the lattice. This procedure is successfully extended to 3D lattice structures [83] and the non-linear constitutive models for lattice structures [84]. Then, in order to consider the manufacturing influence of AM on the effective mechanical performance of lattice structures, a two-step homogenization method [85] was proposed based on the approach proposed by Vigliotti and Pasini [83]. In the first step, a voxel-based model was used to determine the effective structural element parameters by including the shape deviations in fabricated struts. Then the structural element parameter obtained by the voxel-based model was imported into the homogenization method to compute the mechanical properties. Compared with the experiment, the result estimated by the two-step approach showed less error than the direct homogenization method, which means that it is important to consider the shape variation caused by the manufacturing process.

Numerical homogenization is an alternative homogenization method to determine effective mechanical properties over a unit-cell with periodic boundary conditions using Finite Element Analysis (FEA). The educational description of this method has been provided based on a short Matlab implementation by Andreassen [86]. It is initially aimed to determine composite material properties, but single-phase lattice structures can

be simulated by assigning a very soft second materials. This approach can be easily extended to the homogenization of conductivity, thermal expansion and fluid permeability. Dirrenberger et al. [87] used the numerical homogenization technique combined with FEA to compute the elastic moduli tensor and investigate the anisotropy of three auxetic periodic lattices. Van Dijk [88] presented an approach in the geometrically nonlinear regime for stress or strain driven homogenization which is straightforward in combination with FEA. Schwerdtfeger et al. [89] used a standard FEA in conjunction with a well known pseudo density approach to homogenize the linear elastic stiffness tensor of lattice structures with negative Poisson's ratio. It is found that the Poisson's ratio is strongly dependent on the relative density. Even though the numerical homogenization easier to be implemented, when the unit cell of the structure is relatively complicated, the computational cost could be considerable.

2.3 Finite Element Analysis

The development of AM technology provides more freedom for designers to create lattice structures with complex geometries and versatile functions, whose properties could be difficult to simulate with homogenization methods. Instead, Finite Element Analysis (FEA) has the capability of estimating the mechanical performance of complex structures. Recently, FE modeling of lattice structures has attracted plenty of attention from researchers and has been implemented to investigate the mechanical performance of lattice structures. Generally, FE modeling of lattice structures is constructed by beam elements or 3D solid elements as shown in Figure 5. It can be seen that the computation time of beam elements model is much less than that of the 3D solid mesh model because the quantity of beam elements is less than 1% of the quantity of 3D elements for the same

structure. But in some cases, the lattice struct cannot be modeled by beam elements. 3D solid elements have to be applied to construct the FE model. To more clearly compare the methods that investigate the mechanical properties of lattice structures, both the advantages and disadvantages of experimental and simulation methods are summarized in Table 2. In this subsection, the applications of FE modeling techniques to investigate the mechanical properties of lattice structures will be discussed in detail.

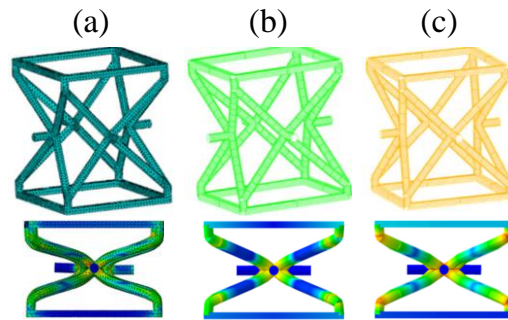


Figure 5. 3D tetrahedral elements compared with beam elements, (a) 3D solid mesh using 19830 elements and 2h 44mins computational time, (b) 1D beam mesh using 160 elements and 51s computational time, (c) 1D beam mesh using 96 elements and 12s computational time.

Table 2 Advantages and disadvantages of experimental and simulation methods

	Advantages	Disadvantages
Experimental Method	<ul style="list-style-type: none"> • It reflects the as-fabricated mechanical properties • It can be used as benchmarks to verify the simulation result 	<ul style="list-style-type: none"> • High cost of the manufacturing process • It is difficult to test functional components with complex shapes by standard testing machine
Homogenization Method	<ul style="list-style-type: none"> • Low computational cost • It can be used in Lattice-Solid hybrid materials to represent lattice structure 	<ul style="list-style-type: none"> • It is not applicable to heterogeneous lattice structures • It is not easy to incorporate the manufacturing defects • It is mathematically difficult to implement on a new topology
FE Model with Beam Elements	<ul style="list-style-type: none"> • Relatively low computational cost • It can model heterogeneous lattice structures • It can model irregular strut thickness by varying the diameter and stiffness of the beam element 	<ul style="list-style-type: none"> • The assumption of beam element requires slender strut, which is not applicable to stout strut • It cannot accurately model the manufacturing defects. • The joint of the strut cannot be accurately modeled by beam elements

FE Model with 3D Solid Elements	<ul style="list-style-type: none"> • As-fabricated model by X-ray image can accurately reflect the manufacturing influence • It can model lattice structures with solid skins • It can reflect geometry of the joint of the lattice structure 	<ul style="list-style-type: none"> • High computational cost for large lattice structures • Difficult to mesh the thin strut • Mesh quality might be poor
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2.3.1 Beam element model

In the early stage, beam elements are prevalently used in FE modeling of lattice structures [38, 90-94]. To determine the effective elastic properties of random lattice structures, the homogenization modeling approach is inappropriate because it does not account for the natural variation in microstructure for random lattices. To overcome this difficulty, Zhu et al. [90, 91] used FEA to determine the equivalent Young's modulus, shear modulus and bulk modulus of 2D Voronoi honeycombs and 3D open-cell foams. Each strut was meshed with one to five Timoshenko beam elements according to the length of the strut. The effect of structural irregularity on the elastic properties was investigated. It is found that higher irregularity will increase the Young's modulus and shear modulus, but decrease the bulk modulus of the structure. The effects of the topological and microstructural irregularity of lattices are further investigate by the FE model to understand the stretch and bending mechanical response [95, 96]. Then, a similar FE model was proposed to investigate the relationship between the elastic properties and the relative density of 3D Voronoi models [93]. It was found that the Kelvin foams can represent Voronoi foams in the low density regime. And the elastic modulus is sensitive to the imperfections while the compressive plateau stress is less sensitive. Furthermore, the elastic buckling of cell edges at the microscopic level is the dominant mechanism for compressive failures. Zhou et al. [92] found that the tensile strengths of individual struts of a lattice structure exhibit significant scatter which is attributed to the presence of defects or voids. They used Timoshenko beam elements to

construct the finite element model with various mechanical property input data to reflect the measured strength of individual struts. The result showed that the variations in the input data strongly influence the predicted stress-strain behavior.

2.3.2 Solid element model

Even though the FE model constructed by the beam element has a lower computational cost, not all types of the lattice structures can be meshed with beam elements. For instance, if the strut of the lattice structure is stout, it does not satisfy the assumptions of the beam element in FEA. It has been shown that with the decrease of porosity, which means the lattice struts get thicker, the mechanical property obtained from beam element model deviates from the experimental result [97]. Besides, in some cases, the lattice structure is connected with skin [98] or solid parts to serve certain functions [47]. Therefore, 3D solid elements are alternative choices in the FE modeling process to mesh the lattice structure. Chantarapanich et al. [99] used ten-node tetrahedron elements to investigate the mechanical response and the connectivity of different types of lattice topologies. Because the lattice cells were not connected by sharing nodes, it cannot be simulated by beam elements. Another advantage of 3D element FE model is that it can analyse the influence of the notch effect and the material concentration in the connection area of lattice struts which can predict a more accurate stress distribution in these locations [23]. It has been shown by the solid element FE model that, with the same porosity, the effective Young's modulus of the lattice structure will change dramatically by shifting the material from the edge to the vertices [100]. Besides, for the large deformation and nonlinear explicit dynamic analysis, the linear 3D elements with lumped mass matrix are required. Tetrahedral, triangular prism and brick elements were used together by Ullah et al. [101] to minimize the stress jump at the transition point in the

explicit dynamic analysis of Kagome lattice core structures. Salonitis et al. [102] implemented a hybrid FE model to simulate the mechanical performance of the lattice structure combined with the solid material. Firstly, the effective Young's modulus and Poisson's ratio of the lattice structure are calculated by a beam element FE model. Then the lattice cells are modeled as representative volume elements (RVEs) with the estimated mechanical properties and the solid material is modeled with tetrahedral elements. The computational cost is reduced by using the RVEs for lattice structures. A similar approach was taken by Huo et al. [103] as shown in Figure 6. The mechanical properties of the lattice structure were obtained by a local FE model with tetrahedral elements in the first step. Then the lattice structure was substituted by a solid material with the homogenised mechanical properties. Finally, the homogenised lattice was connected to other solid materials and the global FE model is constructed. This approach is similar to the homogenization method. The difference is that the homogenised property is calculated by FE methods and the lattice structure is meshed with solid elements. The computational cost of the RVE model is higher than the homogenization method due to the fine mesh on the RVE. But this method is easy to implement because the homogenization is relatively complicated from a mathematical perspective.

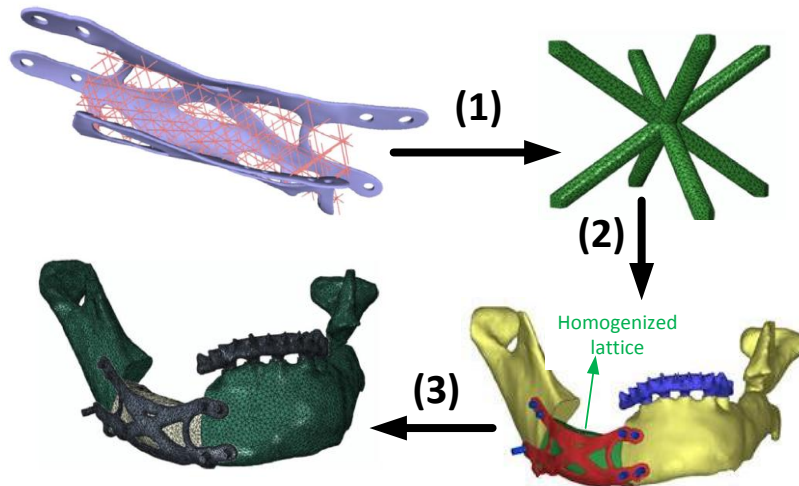


Figure 6. Hybrid FE model to analysis the lattice structure connected to solid materials

In the field of orthopaedic tissue engineering, AM techniques allow for the production of lattice structures for tissue replacement. FE modeling is needed for virtual design and characterization to improve both the biological functionality and mechanical longevity of the lattice structure. Wettergreen et al. [104] proposed characterization and documentation of a library of micro-architectures and meshed the building blocks by polyhedral element in FE modeling process. The effect of the unit block porosity on the equivalent mechanical properties has been investigated through FE models. Malek et al. [47] implemented the FE model with tetrahedral elements to investigate the mechanical properties of cubical lattice structures made by medical grade CoCr alloy with porosity ranging from 60% to 80% fabricated by SLM process. They compared the estimated elastic modulus to the experiment result which showed good agreement.

2.3.3 Improvement of FE models

However, in some investigations, discrepancies are found comparing the numerical simulation to the experimental result [105-107]. This is due to the difference between manufactured and designed lattice structures in shapes, sizes, micro-porosities [108] and

complex strut joint geometry [46]. Therefore, existing FE models still need further refinements to obtain more accurate results.

A common feature of the AM fabricated lattice structures is the material concentration in the nodal region [51]. There are two ways to consider this feature in the beam element model. One is that the beam element in the vicinity of the joint can be increased to the real thickness of the lattice strut [45, 51]. Another way is to increase the stiffness of the beam element near the nodal region to compensate for the material aggregation [38]. Because the thickness of the strut near the nodal region can be directly measured, the first method is easier to be implemented.

The presence of microvoid in lattice struts and the nonuniform strut thickness caused by surface roughness will also lead to inaccurate simulation result. The FE model of two scaffolds with the same porosity are shown in Figure 7. It is found that the effective modulus of the scaffold with smooth surfaces is 68% higher than the model with rough surfaces. Using the measured dimension of fabricated samples to update the CAD model dimensions can improve the simulation accuracy for FEA [109]. Another way to consider the variation of the strut thickness is to use beam elements [41, 44, 110] with different diameters to discretize the lattice strut as shown in Figure 8. Campoli et al. [44] used Scanning Electron Microscopy (SEM) and Gaussian distribution to determine the diameter of each beam. Then the FE model was simulated several times to get the mean and standard deviation of the mechanical properties which means the lattice structure may have a range of mechanical properties due to the structural irregularity.

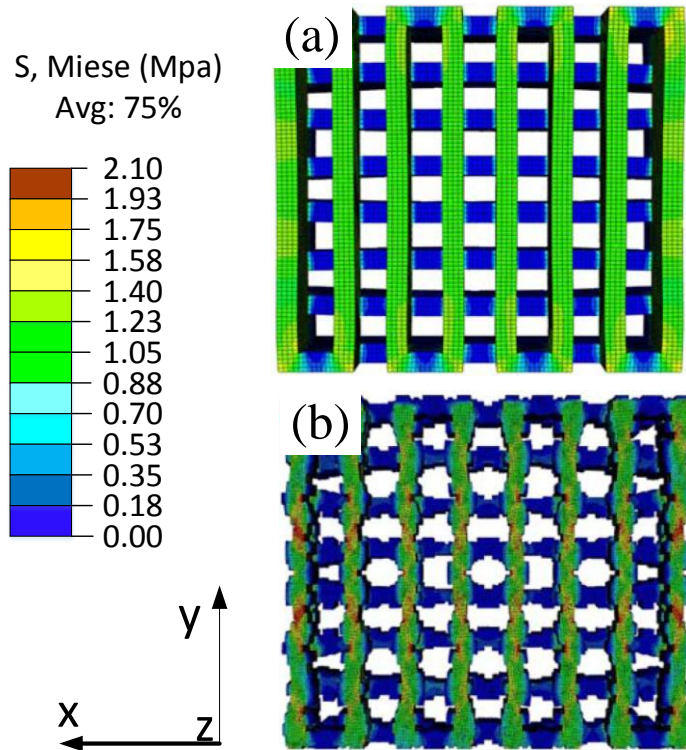


Figure 7. Contour plot of von Mises stress distribution (MPa) for two scaffolds with exactly the same porosity that were compressed in the y direction, (a) smooth surface, (b) irregular surface

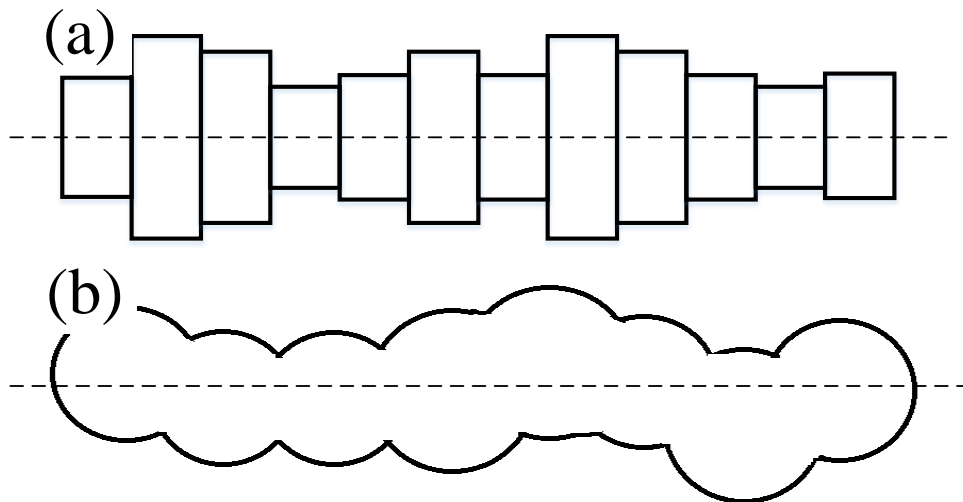


Figure 8. Beam elements with varied diameters to model the irregular strut, (a) implementation in FE model, (b) actual irregularity

Image-based FEA has also been used to simulate the mechanical properties of lattice structures. This approach is the most accurate way to capture the as-fabricated geometry, because the FE model is directly built on the Micro-CT images through which the manufacturing deflection can be precisely reflected. Williams et al. [39] experimentally and computationally tested the lattice structure made by Polycaprolactone (PCL) which is a bioresorbable polymer. It is concluded that the image-based FE model can estimate the mechanical properties of tissue lattice structure, bypassing the need for experimental testing. Suard et al. [58] used X-ray tomography to get the image of single strut of the lattice structure and computed the effective stiffness of strut with different build orientations by FEA. A concept called “effective volume ratio” was defined to set the lower bound of the stiffness. Then, the lattice structure was modeled by struts with effective volume ratio instead of the desired geometry. The result showed 5% difference of Young’s modulus between different build orientations. Except for the stiffness, it was found from the X-Ray tomography and corresponding FE model that the failure mechanism is also influenced by the poor build quality of AM process [111].

3. AM Fabrication modeling

3.1 Manufacturing Discrepancy

To design and simulate the lattice structure, the manufacturing influence of AM cannot be neglected. In the early stage, the design and simulation of lattice structures mainly focus on the geometrical parameters. The design model is directly imported into the simulation process. However, manufacturing discrepancy is a critical issue in the fabrication process of AM techniques [50]. Recently, extensive literatures have investigated the influence of the manufacturing discrepancy on the mechanical properties

of lattice structures by experiments. And researchers have incorporated the manufacturing influence of AM in the simulation process as summarized in Table 3. Therefore, the understanding of the manufacturing discrepancy is crucial in the design and simulation process of lattice structures.

Table 3 Manufacturing influence considered in the simulation process

		Manufacturing influence
Homogenization method	Park et al. [85]	Layer deposition parameter and as-fabricated cross sections
	Park and Rosen [76]	Semi-rigid joint and layer deposition pattern
FE model with beam elements	Zhou et al. [92]	Various mechanical properties of individual lattice struts
	Labeas and Sunaric [51] Smith et al. [45]	Increase thickness of beam elements in the vicinity of the joint for material aggregation
	Luxner et al. [38]	Increase stiffness of beam elements in the vicinity of the joint for material aggregation
	Campoli et al. [44] Zargarian et al. [110] Ravari et al. [41]	Irregular surface modeled by beam elements
FE model with 3D solid elements	Yang et al. [109]	Average value of measure dimension to update the dimension of the CAD model
	Cansizoglu et al. [42]	The influence of strut angles on the thickness
	Williams et al. [39] Sercombe et al. [111]	Image-based FE model to incorporate manufacturing defects
	Suard et al. [58]	X-ray tomography is used to get the effective volume ratio of lattice struts
	Cahill et al. [105] Ravari et al. [41]	Irregular surface of lattice strut modeled by 3D solid elements
	Park and Rosen [112]	Stair-step irregularities between layers and the air gaps generated among the filaments

The irregularity of the surface finishing is one of the most common discrepancies of the AM fabricated components. Because of the layer by layer principle, the AM fabricated model generally has the stair-step irregularities corresponding to the slicing process. Recently, a voxel-based as-fabricated modeling technique is implemented to consider the stair-step irregularities between layers and the air gaps generated among the filaments in

the AM process [112]. Besides, the accuracy of the printing head is limited and the manufacturing process is unstable, which will also cause discrepancies and defects on the surface of the as-fabricated part. For the lattice structure, the manufacturing discrepancy problem becomes even more significant. Because the dimension of the lattice strut is relatively small and the stair-step irregularities will appear on the inclined strut. Cansizoglu et al. [42] found that the fabricated strut thickness grows larger if the angle between the strut and the horizontal plane increases. And there could be a significant change in modulus for variations as small as 0.1mm in the strut thickness. Consequently, the FEA predicted stiffness based on the CAD model could be slightly lower than the actual stiffness. It is also found that the strut lying normal to the build direction is more likely to have defects on the surface [60].

Another reason causing the surface irregularity is the presence of unmelted powder attached to the surface of AM fabricated component [22]. It has been found that process parameters of laser based AM techniques have strong influence on the surface roughness [113, 114]. By optimizing the process parameters, the surface roughness of AM fabricated components can be reduced. Nevertheless, the influence of the surface roughness on the mechanical properties still cannot be neglected. Everhart et al. [115] investigated the effect of surface roughness on the tensile behavior of bars fabricated by AM. The result showed that the unfinished tensile bar, which has a rougher surface, exhibited lower yield strength than the machined one. And the elongation of the unfinished sample is much lower than that of the machined sample. It is also mentioned that additional data for the surface characterization process need to be implemented in the FE model to reduce the error in the plastic region. Because the AM fabricated lattice

structure consists of unfinished single struts, it is difficult to accurately predict the mechanical property if the effect of the unfinished surface is neglected.

Post-processing is able to reduce the surface roughness and the defects of the lattice structure fabricated by AM. Formanoir et al. [43] use chemical etching to decrease the roughness of octet-truss lattice structures manufactured by EBM. This approach can improve the mechanical efficiency of the structure by removing the unmelted powders on the surface. It was also found that the elongation was increased because the critical surface defects are removed during the etching process which was more resistant to the crack initiation. However, this process reduced the strut thickness by almost 30%. The diameter of the strut in the simulation model should be modified.

3.2 Anisotropic Mechanical Behavior

Apart from the manufacturing discrepancy, the anisotropic material property of AM fabricated parts is another important aspect that needs to be considered in design and simulation of lattice structures. It is found in the literature that the mechanical properties are different in directions parallel and perpendicular to the building direction among most AM processes.

The layer by layer manufacturing principle is one of the reasons causing the anisotropic material properties. Shanjani et al. [116] investigated the effect of the printing orientation on the mechanical characteristics of porous calcium polyphosphate structures fabricated by BJ process. It was found that samples with layers deposited parallel to the compressive loading direction were 48% stronger than those with layers deposited perpendicular to the load. Ladani et al. [117] studied the anisotropic mechanical behavior of EBM process. The result showed that the in-plane properties such as elastic modulus,

yield strength, ultimate tensile strength were much higher than out-of-plane direction due to defects or imperfect bonding between layers. Sridharan et al. [118] analyzed the reason for anisotropic mechanical properties of Al-6061 fabricated via Ultrasonic Additive Manufacturing (UAM). When the load was perpendicular to the interfaces, a brittle failure was observed due to the onset of strain localization during the UAM process instead of the lack of bonding between each layer. For the FDM process, the printing orientation also has significant influence on the mechanical properties such as the tensile, compressive strength [119] and deformation behavior [120]. To predict such properties, an anisotropic FE model for FDM process has been proposed by measuring the material properties of test specimens printed in multiple orientations [121].

In some AM processes, the anisotropic mechanical performance is attributed to the anisotropic microstructure of the component. Anisotropic mechanical properties of Ti6Al4V component fabricated by Directed Energy Deposition (DED) have been studied [122]. The result showed that the elongation in longitudinal direction and transverse direction was 11% and 14% respectively due to the columnar prior- β grain morphology and the grain boundary α . Akerfeldt et al. [123] also found that the microstructural constituents have influence on the anisotropic elongation rate of the Ti6Al4V specimen fabricated by laser metal wire-deposition process. Zhang et al. [124] investigated the correlation between the microstructure and the anisotropic tensile behavior of TC21 alloy fabricated by the DED process. The result shows that the sample vertical to the building platform exhibit better ductility due to the lack of continuous grain boundary α layers. But horizontal samples show inferior ductility because of the columnar β grain morphology and continuous grain boundary α layers.

For AM fabricated lattice structures, the anisotropic material property also has significant influence on the mechanical properties. It was found that the ultimate tensile and yield strength of SLM fabricated 316L stainless steel lattice structures were approximately 60% higher and the elongation were 40% higher in vertical building direction than in horizontal building direction [53]. Similar result was presented by Wauthle et al. [125] that the horizontal strut was weak which should be avoided in SLM process. Reinhart et al. [126] investigated the relationship between the mechanical properties and the geometrical properties of the single lattice strut manufactured by SLM process. The result showed that for different diameters and different polar angles of the strut, the Young's modulus was different, which is shown in Figure 9. Therefore, it is not accurate to simulate the mechanical properties of the lattice structure with isotropic material properties. For EBM fabricated lattice structures, anisotropic mechanical properties were also observed by exerting loads parallel and perpendicular to the build direction [127]. For the BJ process, Galeta et al. [128] investigated the effect of building orientation on the mechanical properties of 2D lattice structures. The result showed that the building axis Y provided better strength than those oriented along X axis. And the 2D sample parallel to the printing bed exhibited slightly better strength than those perpendicular to the printing bed. Castilho et al. [129] also studied the influence of the printing direction of the BJ process and found that the mechanical behavior was highly influenced by the printing direction though the dimensional variation is almost the same. Therefore, a correction factor is needed in the calculation of the mechanical properties to balance the effects of the building direction and the dimensional deviation. Recently, to simplify the anisotropic material properties, a transversely isotropic FE model was proposed to

consider the influence of the printing direction on the mechanical behavior of lattice structures [130]. The result of the simulation was in good agreement with that of the experiment, which suggested that the model can estimate the deformation of the lattice structures quite well. However, it was also found that the failure initiation predicted by the simulation model is less accurate than the mechanical behavior before failure, which indicated that further investigation was still needed.

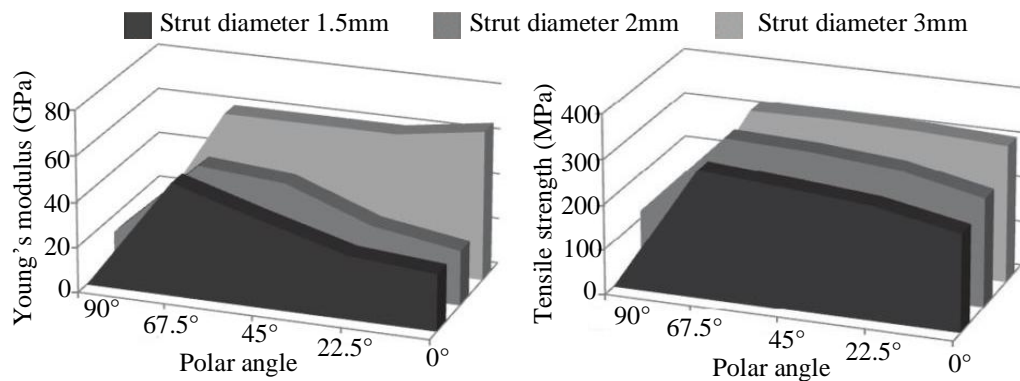


Figure 9. Young's modulus and tensile strength as a function of polar angle and strut diameter

4. Conclusion and Perspectives

Additive Manufacturing has provided designers with not only great opportunities but also enormous challenges in designing and modeling of lattice structures. To evaluate the mechanical properties of lattice structures, experimental methods, homogenization methods and FE models have been proposed and widely used by designers. Due to the high manufacturing cost and time, it is unpractical to obtain the mechanical properties of lattice structures only by conducting experiments in engineering applications. Simulation modeling such as the homogenization and FE methods play significant roles in estimating the mechanical performance of lattice structures. However, each modeling approach has its advantages and disadvantages. Based on the characteristics of lattice structures,

appropriate modeling approach should be implemented to improve the accuracy while minimizing the computational cost.

During simulation of lattice structures, the manufacturing influence of AM processes cannot be neglected by designers. It has been shown by a lot of literatures that the geometrical discrepancy is a critical issue which may cause inferior mechanical properties. The effect of irregular surfaces and shapes on the mechanical properties of lattice structures should be considered in the design and simulation process. It is also acknowledged that the material properties of AM fabricated components exhibit anisotropy, which should also be considered in the simulation process. At last, based on the review, several future works concerning the modeling of lattice structure for the simulation have been pointed out:

- New simulation method for Lattice-Solid hybrid structure should be developed. To serve certain functions, lattice structures are usually connected with solid materials. Though homogenized lattice structure can be represented by an equivalent material. It is not applicable for heterogeneous lattices. Besides, using solid element to model the hybrid structure will result in high computational cost due to the small size of the mesh on the lattice structure. A new approach that can efficiently model Lattice-Solid hybrid structure should be proposed.
- Anisotropic material properties should be implemented in the modeling of the lattice structure. It has been presented by many literatures that the material properties of AM fabricated components are anisotropic, the lattice structure is no exception. And it is also found by experimental methods that the mechanical properties of lattice structures have correlation with the printing orientation.

Therefore, anisotropic material properties should be considered in the simulation of lattice structures.

- Multi-physics design and simulation model is needed for lattice structures including the heat transfer, fluid mechanics and solid mechanics. The lattice structure is promising in serving as multi-functional materials in engineering applications. A multi-physics model that can design and simulate the mechanical properties, thermal properties and fluid dynamics of lattice structures simultaneously will prompt the application of the lattice structure into a higher level.

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