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Multiscale Modelling of Polycrystalline UO₂: Full-Field Simulations (FFT) and Model Reduction Technique (NTFA)

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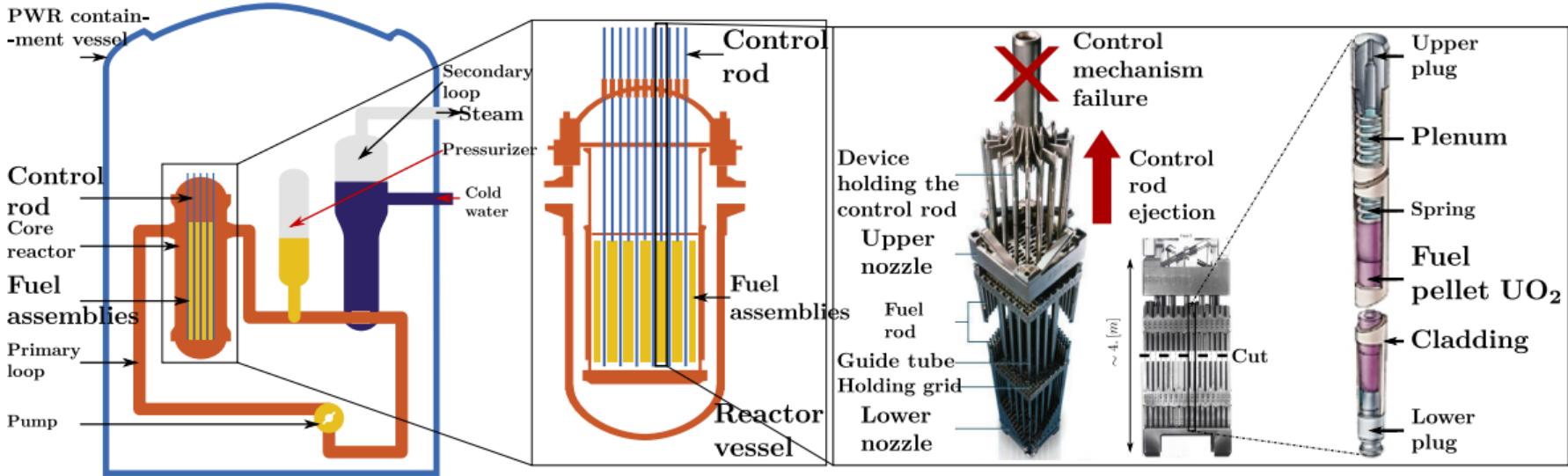
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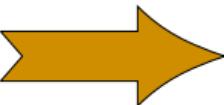
Industrial Context



RIA - Reactivity Initiated Accident (Class 4)

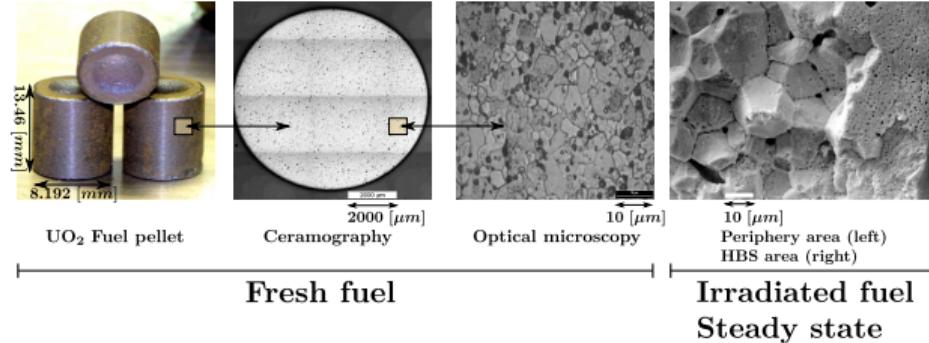
◊ Specific thermo-mechanical loading:

- $T \in [1000, 2600] \text{ } ^\circ\text{C}$
- $\dot{\varepsilon} \in [10^{-6}, 10^{-1}] \text{ } [\text{s}]^{-1}$



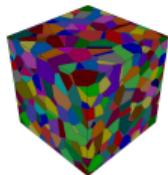
Behaviour law of UO_2 is highly dependent on the loading conditions ($T, \dot{\varepsilon}$)

Method



Scale of the UO₂ pellet

- ◊ Non uniform Transformation Field Analysis (NTFA) model at each integration point
- ◊ Access to the local fields



Polycrystal: 500 Grains

Scale of a single crystal

- ◊ 1 Grain ($\sim 10 [\mu\text{m}]$)
- ◊ Elasto viscoplastic behaviour law with isotropic strain hardening

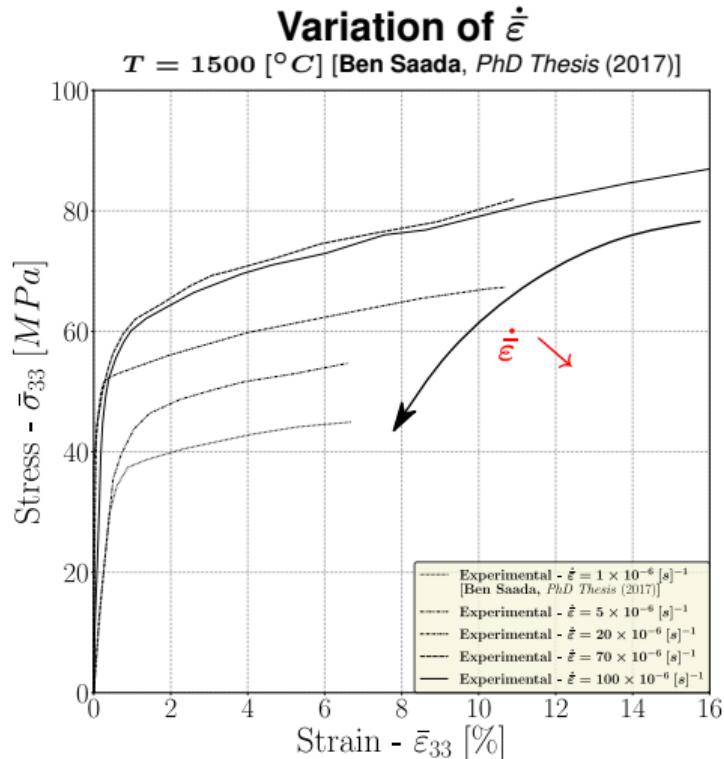
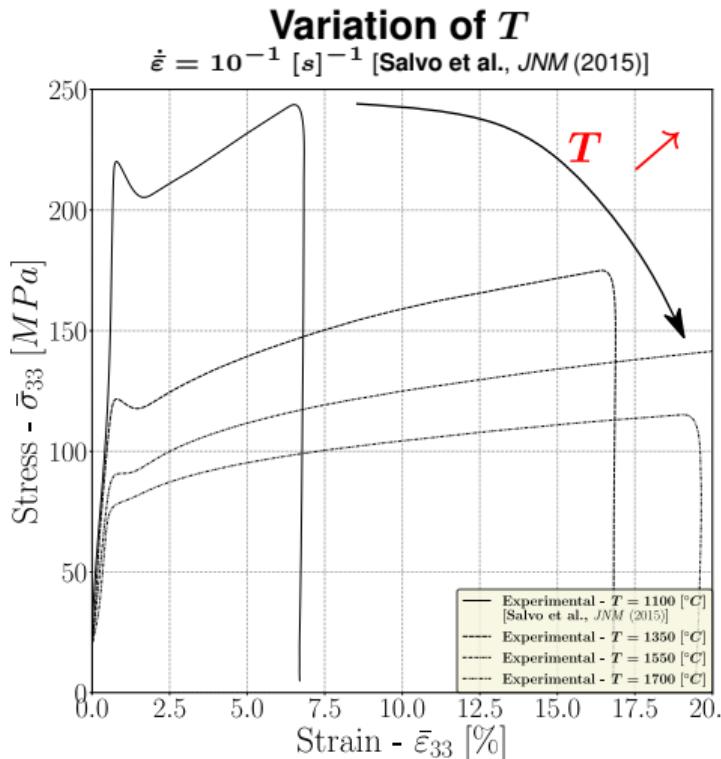
Model reduction: Scale of a polycrystal: RVE

- ◊ ~ 500 Grains (500 single crystals).
- ◊ **Full Field simulation: FFT**
- ◊ Strain incompatibilities

Inverse
calibration

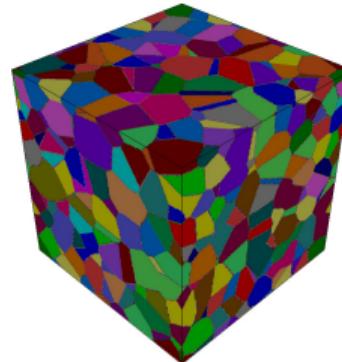
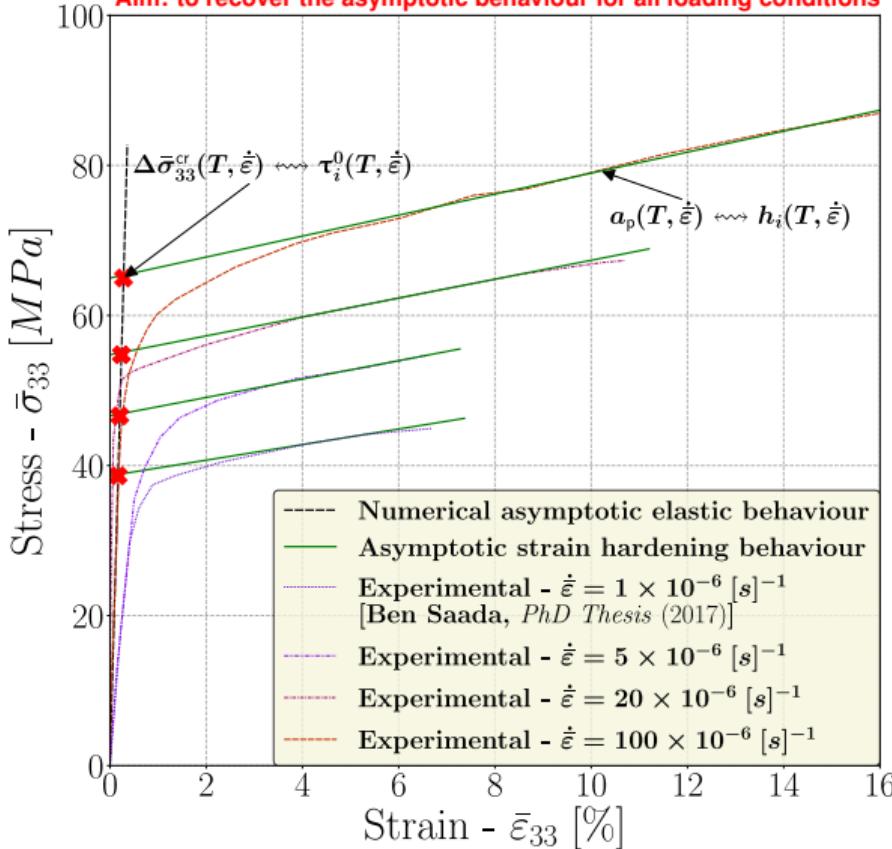
Model reduction:
NTFA

Experimental Results



Inverse Calibration Process

Aim: to recover the asymptotic behaviour for all loading conditions



Calculation of $(\Delta\bar{\sigma}_{33}^{\text{cr}}, a_p)$ linked to the local parameters (τ_i^0, h_i)

$$\dot{\gamma}_s^{\text{vp}} = \dot{\gamma}_i^0 \times \left(\frac{|\tau_s|}{r_i} \right)^{n_i} \times \text{sgn}(\tau_s),$$

$$r_i(\mathbf{x}, t) = \tau_i^0(T, \dot{\varepsilon}) + h_i(T, \dot{\varepsilon}) \times p_i(\mathbf{x}, t),$$

$$\dot{p}_i = \sum_{s \in S_i} \dot{\gamma}_s^p, \quad \dot{\gamma}_s^p = |\dot{\gamma}_s^{\text{vp}}|, \quad (1)$$

with: $\dot{\gamma}_s^{\text{vp}}$ evolution law inspired by [Knezevic et al., IJP (2013)], $(\tau_i^0, h_i)(T, \dot{\varepsilon})$ functions to be calibrated.

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Results

Single Crystal Scale: Elasto Viscoplastic Behaviour with Isotropic Strain Hardening

$$w(\boldsymbol{\varepsilon}, \boldsymbol{\varepsilon}_{vp}, p) = \frac{1}{2} (\boldsymbol{\varepsilon} - \boldsymbol{\varepsilon}_{vp}) : \mathbf{L} : (\boldsymbol{\varepsilon} - \boldsymbol{\varepsilon}_{vp}) + w^{iso}(p), \quad \boldsymbol{\sigma} = \frac{\partial w}{\partial \boldsymbol{\varepsilon}} (\boldsymbol{\varepsilon}, \boldsymbol{\varepsilon}_{vp}, p),$$

with: | w local free-energy,

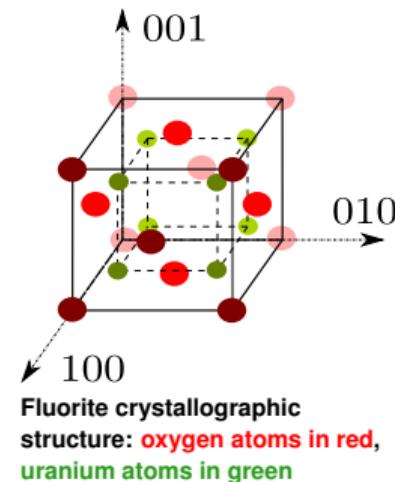
$$\boldsymbol{\varepsilon}(\mathbf{x}, t) = \boldsymbol{\varepsilon}_e(\mathbf{x}, t) + \boldsymbol{\varepsilon}_{vp}(\mathbf{x}, t), \quad \boldsymbol{\varepsilon}_{vp}(\mathbf{x}, t) = \sum_s \gamma_s^{vp}(\mathbf{x}, t) \mathbf{m}_s(\mathbf{x}),$$

with: | \mathbf{m}_s Schmid tensor UO₂ fluorite crystallographic structure [Soulacroix, PhD Thesis (2014)],
 γ_s^{vp} slip on the considered system (s).

$$\psi_{vp} = \sum_s \psi_{vp,s}, \quad \psi_{vp,s}(\mathcal{A}_{vp}, \mathcal{A}_{p,i}) = \dot{\gamma}_i^0 \times \frac{-\mathcal{A}_{p,i}}{n_i + 1} \times \left(\frac{|\mathcal{A}_{vp,s}|}{-\mathcal{A}_{p,i}} \right)^{n_i + 1},$$

$$\psi_p = \sum_s \psi_{p,s}, \quad \psi_{p,s}(\mathcal{A}_{vp}, \mathcal{A}_{p,i}) = \dot{\gamma}_i^0 \times \frac{|\mathcal{A}_{vp,s}|}{(n_i - 1)} \times \left(\frac{|\mathcal{A}_{vp,s}|}{-\mathcal{A}_{p,i}} \right)^{n_i - 1},$$

with: | (ψ_{vp}, ψ_p) dissipation potentials $\rightsquigarrow (\dot{\boldsymbol{\varepsilon}}_{vp}, \dot{p})$,
 $(\mathcal{A}_{vp}, \mathcal{A}_{p,i})$ thermodynamic forces $\longleftrightarrow (\boldsymbol{\varepsilon}_{vp}, p_i)$.



(2)

Local Problem to be Solved for RVE V : Equation System (3) Coupled with Evolution Laws (4)

$$\left. \begin{array}{l} \boldsymbol{\sigma}(\boldsymbol{x}, t) = \mathbf{L}(\boldsymbol{x}) : (\boldsymbol{\varepsilon}(\boldsymbol{x}, t) - \boldsymbol{\varepsilon}_{\text{vp}}(\boldsymbol{x}, t)), \quad \boldsymbol{\varepsilon}_{\text{vp}}(\boldsymbol{x}, t) = \sum_s \gamma_s^{\text{vp}}(\boldsymbol{x}, t) \mathbf{m}_s(\boldsymbol{x}), \\ \operatorname{div} \boldsymbol{\sigma}(\boldsymbol{x}, t) = 0, \quad \boldsymbol{\sigma}(\boldsymbol{x}, t) \cdot \mathbf{n}(\boldsymbol{x}) \text{ antiperiodic on } \partial V, \\ \boldsymbol{\varepsilon}(\boldsymbol{x}, t) = \bar{\boldsymbol{\varepsilon}}(t) + \frac{1}{2}(\nabla \mathbf{u}^*(\boldsymbol{x}, t) + \nabla \mathbf{u}^{*T}(\boldsymbol{x}, t)), \quad \mathbf{u}^*(\boldsymbol{x}, t) \text{ periodic on } \partial V. \end{array} \right\} \quad (3)$$

$$\dot{\gamma}_s^{\text{vp}} = \frac{\partial \psi_{\text{vp},s}}{\partial \mathcal{A}_{\text{vp},s}} (\mathcal{A}_{\text{vp},s}, \mathcal{A}_{\text{p},i}), \quad \dot{\gamma}_s^{\text{p}} = \frac{\partial \psi_{\text{p},s}}{\partial \mathcal{A}_{\text{p},i}} (\mathcal{A}_{\text{vp},s}, \mathcal{A}_{\text{p},i}), \quad s \in S_i,$$

with:

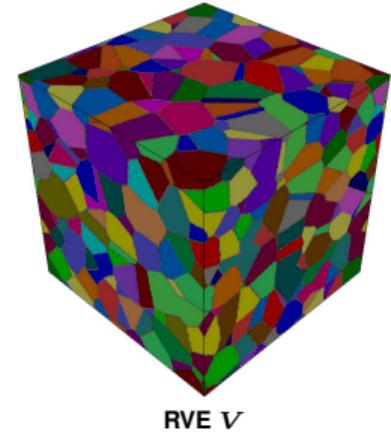
| | |
|---|-----|
| $\boldsymbol{\varepsilon}_{\text{vp}}$ associated with its thermodynamic force $\mathcal{A}_{\text{vp}} (\equiv \boldsymbol{\sigma})$, | $ $ |
| $p = (p_i)$ associated with its thermodynamic force $\mathcal{A}_{\text{p}} = (\mathcal{A}_{\text{p},i})$, | |
| $i \in \{\{100\}, \{110\}\}$ referring to a slip family of the studied material [Soulacroix, PhD Thesis (2014)], | |

(4)

$$\mathcal{A}_{\text{p},i}(\boldsymbol{x}, t) = -r_i(\boldsymbol{x}, t),$$

$$r_i(\boldsymbol{x}, t) = \tau_i^0(T, \dot{\boldsymbol{\varepsilon}}) + h_i(T, \dot{\boldsymbol{\varepsilon}}) \times p_i(\boldsymbol{x}, t),$$

$$\dot{p}_i = \sum_{s \in S_i} \dot{\gamma}_s^{\text{p}} (\mathcal{A}_{\text{vp}}, \mathcal{A}_{\text{p}}), \quad \dot{\gamma}_s^{\text{p}} = |\dot{\gamma}_s^{\text{vp}}|.$$



RVE V

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Calibration of $\tau_i^0(T, \dot{\varepsilon})$

Calibration of $h_i(T, \dot{\varepsilon})$

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Results

Calibration of $\tau_i^0(T, \dot{\varepsilon})$

$n_{\{100\}} = 4$, $\dot{\gamma}_{\{100\}}^0(\dot{\varepsilon}) = 0.7 \times \dot{\varepsilon}$ and $n_{\{110\}} = 4$, $\dot{\gamma}_{\{110\}}^0(\dot{\varepsilon}) = 0.5 \times \dot{\varepsilon}$,

with: n_i deduced from observations,
 $\dot{\gamma}_i^0(\dot{\varepsilon})$ determined using numerical tests at the single crystal scale.

$$\tau_i^0(T, \dot{\varepsilon}) = A_i^f(\dot{\varepsilon}) \times \exp(-b_i^f \times T) + C_i^f(\dot{\varepsilon})$$

$$A_i^f(\dot{\varepsilon}) = \text{Max} \left[a_i^{f,0} - a_i^{f,1} \times \exp \left[-a_i^{f,2} \times \log_{10}(\dot{\varepsilon}) \right], 0 \right],$$

with: $C_i^f(\dot{\varepsilon})$ same strain rate dependence as $A_i^f(\dot{\varepsilon})$,
 (A_i^f, b_i^f, C_i^f) obtained by minimising error using LM algorithm
[Levenberg, QAM (1944)] [Marquardt, JSIAM (1963)],
 $\tau_i^0(T, \dot{\varepsilon})$ targeted function.

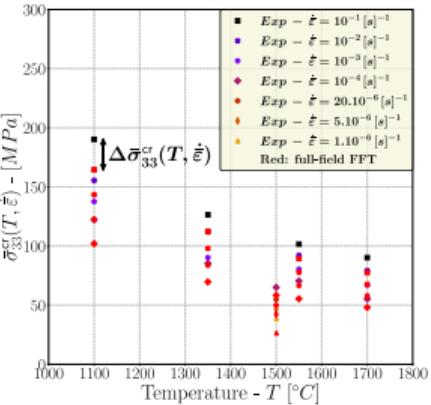
$$\tau_i^{0,(n+1)}(T, \dot{\varepsilon}) = \tau_i^{0,(n)}(T, \dot{\varepsilon}) + f_s \times {}^{(n)}\Delta\bar{\sigma}_{33}^{\text{cr}}(T, \dot{\varepsilon}), \quad f_s = 0.5,$$

with: $\tau_i^{0,(n+1)}$ input data used in the LM algorithm,

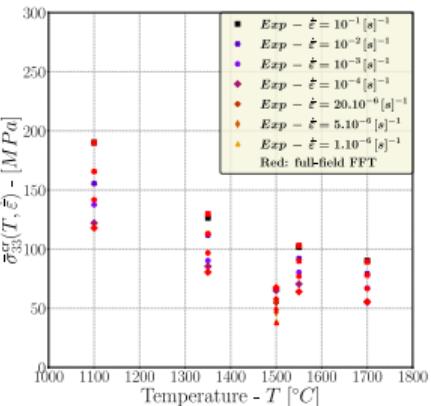
$$Er^{(n)} = \frac{1}{N} \times \sum |{}^{(n)}\Delta\bar{\sigma}_{33}^{\text{cr}}(T, \dot{\varepsilon})|, \quad |Er^{(n)} - Er^{(n-1)}| < \delta \times Er^{(n-1)},$$

with: ${}^{(n)}\Delta\bar{\sigma}_{33}^{\text{cr}}(T, \dot{\varepsilon})$ error at given loading conditions,
 $(Er^{(n)}, \delta = 10^{-3})$ relative error and stopping criterion.

Beginning of the iterative process



End of the iterative process



Calibration of $h_i(T, \dot{\varepsilon})$

$$h_{\{100\}} = h_{\{110\}} = h$$

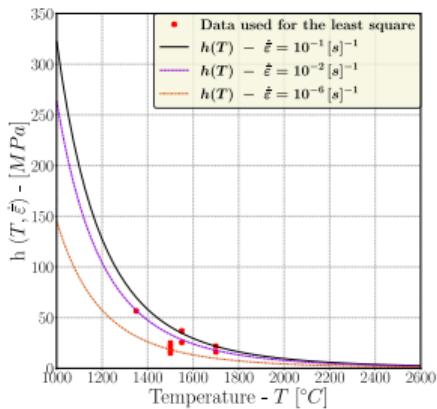
$$h^{(n+1)} = \frac{a_{p,\text{exp}} \times h^{(n)}}{a_{p,\text{simu}}^{(n)}}, \quad |a_{p,\text{simu}}^{(n)} - a_{p,\text{exp}}| < \delta \times a_{p,\text{exp}},$$

with: $\begin{cases} a_{p,\text{exp}} & \text{experimental strain hardening slope,} \\ a_{p,\text{simu}}^{(n)} & \text{numerical strain hardening slope,} \\ \delta (= 10^{-4}) & \text{relative stopping criterion.} \end{cases}$

$$h(T, \dot{\varepsilon}) = \frac{a^h \times \ln(b^h \times \dot{\varepsilon} + f^h)}{(c^h \times T + d^h)^{e^h}},$$

with: $\begin{cases} h^{(n)} & \text{input data used in the LM algorithm,} \\ (a^h, b^h, c^h, d^h, e^h, f^h) & \text{coefficients determined by using LM} \\ & \text{algorithm [Levenberg, QAM (1944)] [Marquardt, JSIAM (1963)].} \end{cases}$

End of the iterative process



(6)

Results of Inverse Calibration

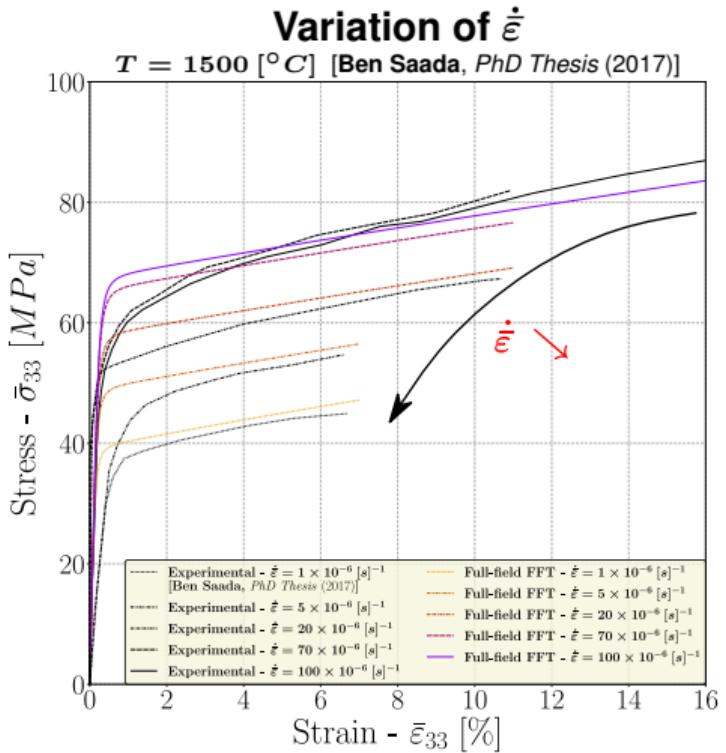
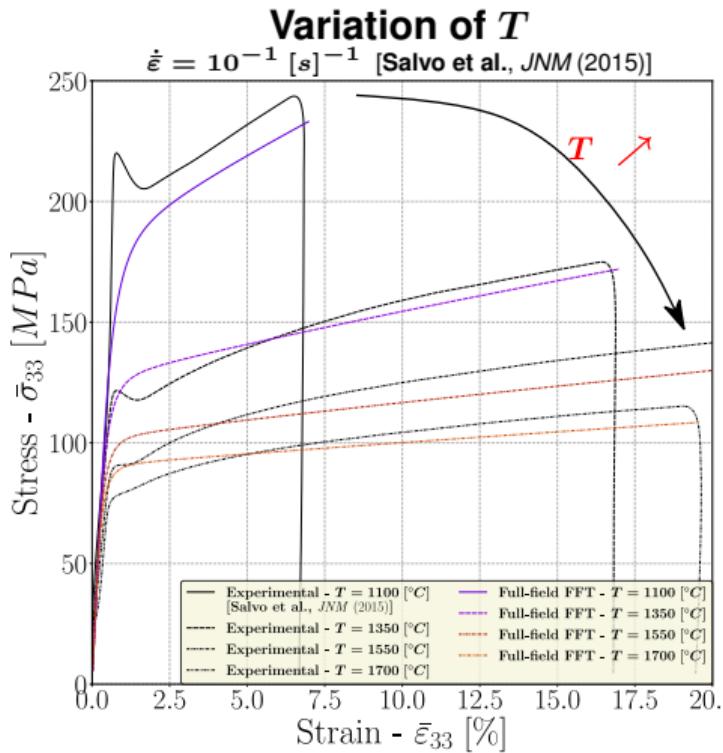


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Decomposition of the internal variable

Influence tensors

Macroscopic state law

Effective dissipation potential approximation

Results

NTFA Decomposition of Internal Variables

$$\varepsilon_{vp}(x, t) = \sum_k^{M_{vp}} \xi_{vp}^{(k)}(t) \mu_{vp}^{(k)}(x),$$

|| NTFA decomposition [Michel and Suquet, JMPS (2016)],

$$p_i(x, t) = \begin{cases} \sum_l^{M_{p,i}} \xi_{p,i}^{(l)}(t) \mu_{p,i}^{(l)}(x) - [\text{Decomposed}], \\ \sum_g \xi_{p,i}^{(g)}(t) \chi^{(g)}(x) - [\text{Constant per grain}]. \end{cases} \quad (7)$$

|| [Constant per grain] - decomposition [Michel and Suquet, CM (2016)],
|| [Decomposed] - tested decomposition,

with: $\begin{cases} (\mu_{vp}^{(k)}, \mu_{p,i}^{(l)}) & \text{modes used for the internal-variables decomposition,} \\ (\xi_{vp}, \xi_{p,i}) & \text{reduced internal variables.} \end{cases}$

Local Fields Expressed with Mode Decomposition

$$\blacktriangleright \boldsymbol{\varepsilon}(\boldsymbol{x}, t) = \mathbf{A}(\boldsymbol{x}) : \bar{\boldsymbol{\varepsilon}}(t) + \sum_l^{M_{\text{vp}}} \mathbf{D} * \mu_{\text{vp}}^{(l)}(\boldsymbol{x}) \xi_{\text{vp}}^{(l)}(t),$$

|| induced by NTFA decompostion,

with: $\left| \begin{array}{ll} \boldsymbol{\varepsilon}(\boldsymbol{x}, t) & \text{using the superposition principle: solution to the} \\ & \text{linear thermoelastic problem [local problem (3)-(4)]}, \\ \bar{\boldsymbol{\varepsilon}} & \text{macroscopic strain tensor}, \\ \mathbf{A}(\boldsymbol{x}) & \text{strain concentration tensor}, \\ \mathbf{D} * \mu_{\text{vp}}^{(l)}(\boldsymbol{x}) & \text{strain influence tensor}, \end{array} \right.$

(8)

$$\mathbf{D} * \mu_{\text{vp}}^{(l)}(\boldsymbol{x}) = \frac{1}{|V|} \int_V \mathbf{D}(\boldsymbol{x}, \boldsymbol{x}') : \mu_{\text{vp}}^{(l)}(\boldsymbol{x}') d\boldsymbol{x}', \quad \mathbf{D}(\boldsymbol{x}, \boldsymbol{x}') = \boldsymbol{\Gamma}(\boldsymbol{x}, \boldsymbol{x}') : \mathbf{L}(\boldsymbol{x}'),$$

with: | $(\mathbf{D}, \boldsymbol{\Gamma})$ nonlocal and nonlocal Green operators,

$$\blacktriangleright \boldsymbol{\sigma}(\boldsymbol{x}, t) = \mathbf{L}(\boldsymbol{x}) : \mathbf{A}(\boldsymbol{x}) : \bar{\boldsymbol{\varepsilon}}(t) + \sum_l^{M_{\text{vp}}} \rho_{\text{vp}}^{(l)}(\boldsymbol{x}) \xi_{\text{vp}}^{(l)}(t),$$

with: | $\rho_{\text{vp}}^{(k)}(\boldsymbol{x}) = \mathbf{L}(\boldsymbol{x}) : \left((\mathbf{D} * \mu_{\text{vp}}^{(k)})(\boldsymbol{x}) - \mu_{\text{vp}}^{(k)}(\boldsymbol{x}) \right).$

Macroscopic State Law

$$\begin{aligned}
 \frac{\partial \bar{w}}{\partial \bar{\varepsilon}} &= \bar{\sigma}, \quad \bar{\sigma} = \tilde{\mathbf{L}} : \bar{\varepsilon} + \sum_k^{M_{vp}} < \rho_{vp}^{(k)} > \xi_{vp}^{(l)}, \\
 -\frac{\partial \bar{w}}{\partial \xi_{vp}^{(k)}} &= a_{vp}^{(k)}, \quad a_{vp}^{(k)} = \bar{\varepsilon} : \mathbf{a}^{(k)} + \sum_l < \mu_{vp}^{(k)} : \rho_{vp}^{(l)} > \xi_{vp}^{(l)}, \\
 -\frac{\partial \bar{w}}{\partial \xi_{pi}^{(k)}} &= a_{pi}^{(k)}, \quad a_{pi}^{(k)} = \begin{cases} - \left(\tau_i^0 < \mu_{pi}^{(k)} > + h_i \times \sum_l^{M_{pi,i}} \xi_{pi}^{(l)} < \mu_{pi}^{(k)} \mu_{pi}^{(l)} > \right) & \text{- [Decomposed]}, \\ - \left(\tau_i^0 + h_i \times \xi_{pi}^{(k)} \right) \times c^{(k)} & \text{- [Constant per grain]}, \end{cases} \\
 \text{with: } & \begin{cases} \mathbf{a}^{(k)} & = < \mu_{vp}^{(k)} : \mathbf{L} : \mathbf{A} >, \\ \tilde{\mathbf{L}} & = < \mathbf{L} : \mathbf{A} >. \end{cases}
 \end{aligned} \tag{9}$$

Evolution of the Reduced Thermodynamic Variables

$$\dot{a}_{\text{vp}}^{(k)}(\bar{\varepsilon}, \xi_{\text{vp}}) = \frac{\partial a_{\text{vp}}^{(k)}}{\partial \bar{\varepsilon}} : \dot{\bar{\varepsilon}} + \sum_l^{M_{\text{vp}}} \frac{\partial a_{\text{vp}}^{(k)}}{\partial \xi_{\text{vp}}^{(l)}} \times \dot{\xi}_{\text{vp}}^{(l)}, \text{ with } \dot{\xi}_{\text{vp}}^{(l)} = \frac{\partial \psi_{\text{vp}}^{\text{hom}}}{\partial a_{\text{vp}}^{(l)}} \implies \dot{a}_{\text{vp}}^{(k)} = \frac{\partial a_{\text{vp}}^{(k)}}{\partial \bar{\varepsilon}} : \dot{\bar{\varepsilon}} + \frac{\partial \psi_{\text{vp}}^{\text{hom}}}{\partial \xi_{\text{vp}}^{(k)}},$$

$$\psi^{\text{hom}} = \tilde{\psi}, \quad \tilde{\psi} = \langle \psi \rangle, \quad \langle \psi \rangle = \sum_g c^{(g)} \sum_s \langle \psi_s \rangle^{(g)},$$

|| approximation of the effective dissipation potential [Fritzen and Leuschner, CMAME (2013)],

$$\begin{aligned} \langle \psi_{\text{vp},s}^{\text{TSO}}(\mathcal{A}_{\text{vp},s}, \mathcal{A}_{\text{p},i}) \rangle^{(g)} &= \left[\psi_{\text{vp},s}(\bar{\mathcal{A}}_{\text{vp},s}^{(g)}, \bar{\mathcal{A}}_{\text{p},i}^{(g)}) + \frac{\partial^2 \psi_{\text{vp},s}}{\partial \mathcal{A}_{\text{vp},s} \partial \mathcal{A}_{\text{p},i}} \times C^{(g)}(\mathcal{A}_{\text{vp},s}^{(g)}, \mathcal{A}_{\text{p},i}^{(g)}) \right. \\ &\quad \left. + \frac{1}{2} \frac{\partial^2 \psi_{\text{vp},s}}{\partial \mathcal{A}_{\text{vp},s}^2} \times C^{(g)}(\mathcal{A}_{\text{vp},s}^{(g)}) + \frac{1}{2} \frac{\partial^2 \psi_{\text{vp},s}}{\partial \mathcal{A}_{\text{p},i}^2} \times C^{(g)}(\mathcal{A}_{\text{p},i}^{(g)}) \right] - [\text{Decomposed}], \end{aligned} \quad (10)$$

|| Tangent Second Order (TSO) linearisation of the effective dissipation potential [Castañeda, Jmps (1996)] [Michel and Suquet, CM (2016)].

with:

| | |
|-----------------|---|
| $C^{(g)}(X, Y)$ | $= \langle (X - \bar{X}^{(g)})(Y - \bar{Y}^{(g)}) \rangle^{(g)},$ |
| $C^{(g)}(X)$ | $= \langle (X - \bar{X}^{(g)})^2 \rangle^{(g)}.$ |

► Similar work has to be done on $\dot{a}_{\text{p}}^{(k)}$, $\dot{a}_{\text{vp}}^{(k)}$ has to be coupled with $\dot{a}_{\text{p}}^{(k)}$.

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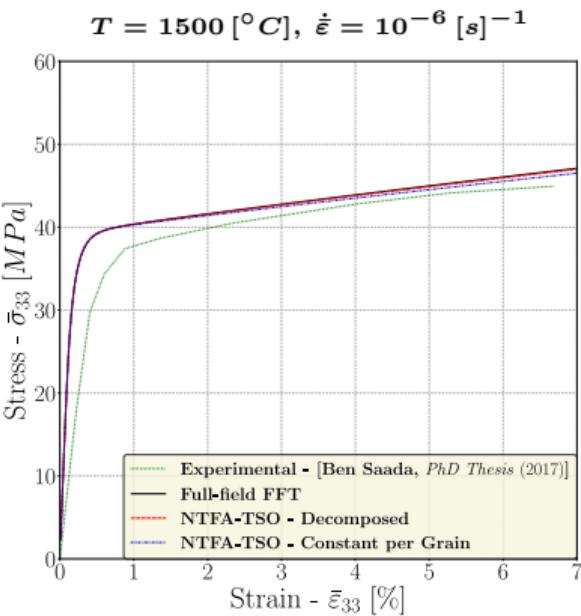
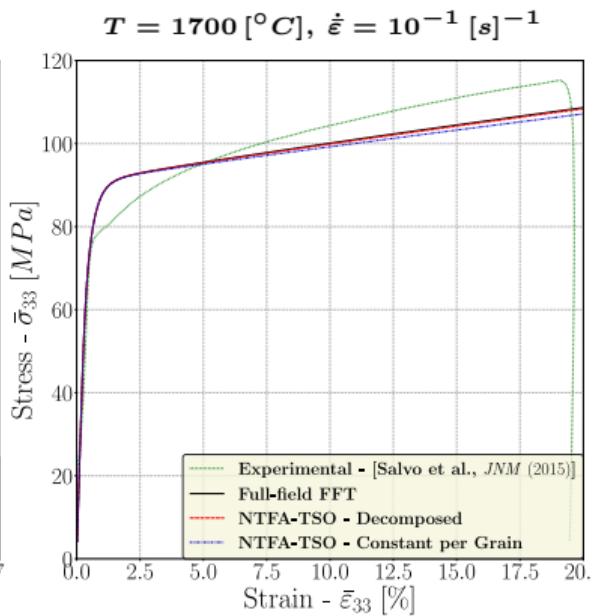
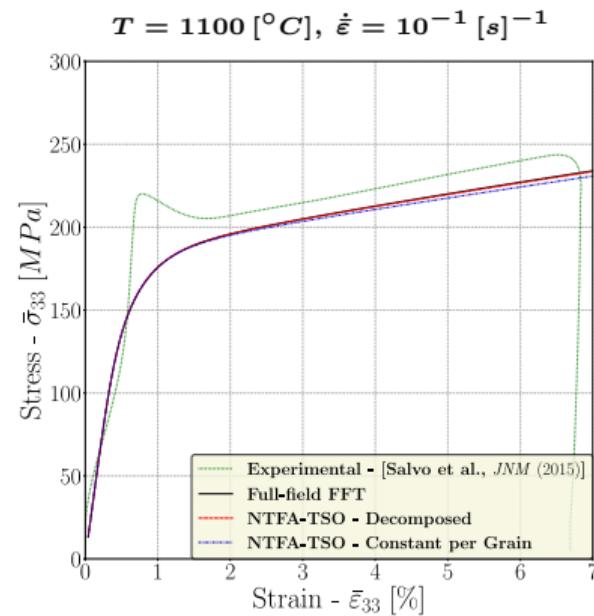
Model reduction: NTFA-TSO

Results

Effective response

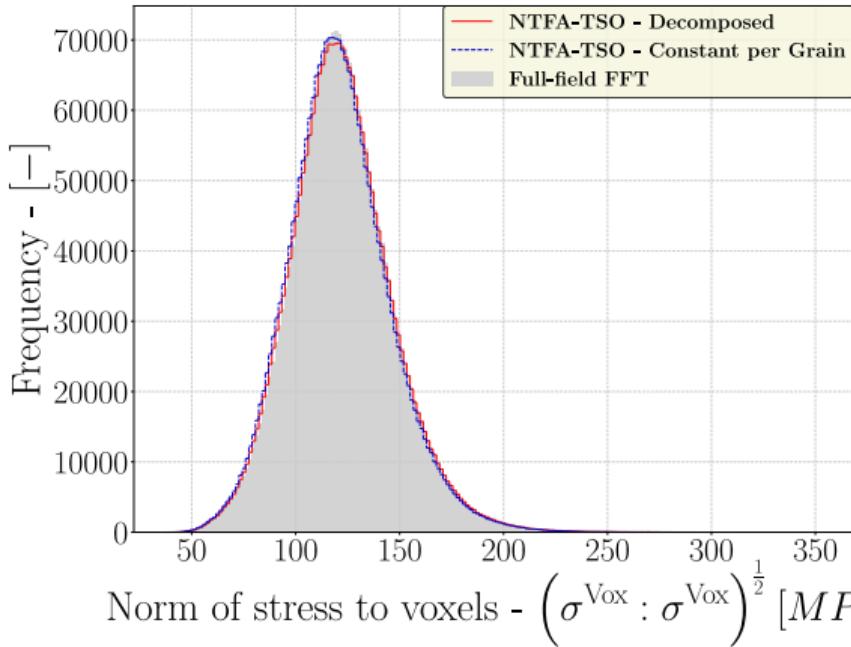
Local fields

Uniaxial Compressive Strain Test: Macroscopic Comparison between Experimental Results, Full-Field FFT and NTFA-TSO Model



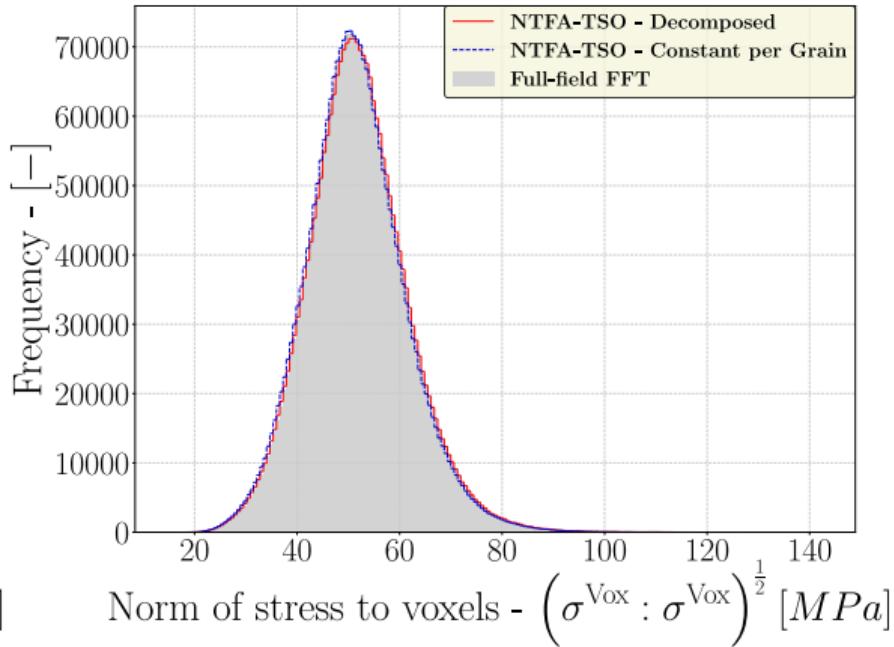
Uniaxial Compressive Strain Test: Local Comparison between Full-Field FFT and NTFA-TSO Model

$$\bar{\varepsilon}_{33} = 20 [\%], T = 1700 [{}^{\circ}\text{C}], \dot{\varepsilon} = 10^{-1} [\text{s}]^{-1}$$



Results

$$\bar{\varepsilon}_{33} = 7 [\%], T = 1500 [{}^{\circ}\text{C}], \dot{\varepsilon} = 10^{-6} [\text{s}]^{-1}$$



Local fields

Conclusion

Mechanical problem

- ◊ Behaviour law \Leftarrow from experimental results
- ◊ Aim: to recover asymptotic behaviour

Inverse calibration

- ◊ Behaviour law parameters impacted by the loading conditions
- ◊ Iterative calibration process using Levenberg Marquardt algorithm

Model reduction: NTFA-TSO

- ◊ NTFA: 2 different decompositions studied
- ◊ Reduced-variable evolution laws \Leftarrow effective-dissipation-potential linearisation

Results

- ◊ **[Macroscopic scale]** Good agreement between:
 - Experimental results
 - FFT results
 - NTFA-TSO model
- ◊ **[Local scale]** Almost no error margin between:
 - FFT results
 - NTFA-TSO model

Perspectives

Objectives:

- ◊ To adapt the **NTFA-TSO model** to **all loading conditions** (RIA)
- ◊ To keep a **low number of internal variables**

Method: definition of reference loading conditions

- ◊ Temperature: $T_0 \in [|1000, 2600|] [^\circ C]$ with $T_{\text{Pas}} = 50 [^\circ C]$
- ◊ Macroscopic strain rate: $\dot{\varepsilon}_0 = 10^{-1} [s]^{-1}$

Future work:

- ◊ [A] Focus on temperature loading conditions
 - **1D Lagrange interpolation functions on modes: $\mu_{\text{vp}}(T_0)$**
- ◊ [B] Focus on macroscopic strain rate loading conditions
 - **Same modes at $(T_0, \dot{\varepsilon}_0)$ and $(T, \dot{\varepsilon})$: $\mu_{\text{vp}}(T, \dot{\varepsilon})$**
 - Function: $T_0 = g_{|\dot{\varepsilon}_0}(T, \dot{\varepsilon})$
 - Macroscopic strain rate domain: $\dot{\varepsilon} \in [10^{-6}, 10^{-1}] [s]^{-1}$
- ◊ [C] Developing a tri-axial loading NTFA-TSO model