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Ferroelectric phase transitions in epitaxial antiferroelectric PbZrO₃ thin films

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Abstract

The archetypical antiferroelectric, PbZrO₃, is currently attracting a lot of interest but no consensus can be clearly established on the nature of his ground state as well as on the influence of external stimuli over its physical properties. Here, the antiferroelectric state of 45-nm-thick epitaxial thin films of PbZrO₃ is established by observing the characteristic structural periodicity of antiparallel dipoles at the atomic scale, combined with clear double hysteresis of the polarization-electric field response related to antiferroelectric–to–ferroelectric phase transitions. Surprisingly, while the antiferroelectric state is identified as the ground state, temperature-dependent measurements show that a transition to a ferroelectric-like state appears in a large temperature window (100 K). Atomistic simulations further confirm the existence, and provides the origin, of such ferroelectric state in the films. Electric-fieldinduced ferroelectric transitions are also detected by the divergence of the piezoresponse force microscopy response. Using this technique, we further reveal the signature of a ferroelectric ground state for 4-nm-thick PbZrO₃ films. Compared to bulk crystals, these results suggest a more complex competition between ferroelectric and antiferroelectric phases in epitaxial thin films of PbZrO₃.

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Introduction

From their first description by Kittel in 1951,¹ the definition of antiferroelectrics has aroused numerous debates, even up to date.^{2,3} It is generally admitted that two main features need to be gathered to establish a material as antiferroelectric: on the one hand, an antipolar crystal organization and, on the other hand, the existence of a polar phase close in energy and reachable by application of an electric field.^{2,4} This latter feature is paramount for key applications involving antiferroelectricity. Indeed, the peculiar shape of the double hysteresis of polarization vs. electric field results from the volatile transition from an antiferroelectric (AFE) to a ferroelectric (FE) state and propels antiferroelectrics towards high-energy storage capacitors,⁵ high-strain actuators,⁶ electrocaloric^{7,8} and photovoltaic⁹ devices. Controlling the stability of the AFE state with respect to the FE one in thin films appears then as the cornerstone for the future integration of such materials into devices.

Among antiferroelectric materials, perovskite lead zirconate, PbZrO₃, is probably the most studied. In its bulk form, PbZrO₃ undergoes a first-order phase transition from an antiferroelectric phase with a *Pbam* orthorhombic symmetry to a paraelectric phase with a cubic symmetry at a critical temperature of 505 K.¹⁰ This phase transition, which nature is still unclear,^{11,12} is accompanied by a divergence of the dielectric susceptibility, as commonly observed for ferroelectric to paraelectric phase transitions.^{1,10} Moreover, several reports mentioned the existence of an intermediate ferroelectric phase with a rhombohedral symmetry, detected in a small temperature interval (495-505 K).¹³⁻¹⁸ In thick PbZrO₃ films (900 nm) fabricated by sol-gel methods, this intermediate ferroelectric phase has also been revealed and its temperature stability could be expanded by an external electric field.¹⁹ Besides, in epitaxial PbZrO₃ thin films, the room-temperature stabilization of a pure antiferroelectric phase turned out to be more controversial, with earlier reports on either purely ferroelectric films²⁰ or mixed antiferroelectric–ferroelectric films.²¹ In turn, it was theoretically established that epitaxial strain would affect the competition between the AFE and FE phases.²² Note that Pb-based thin films have been investigated by first-principle techniques for over twenty years.^{22–27} Furthermore, calculations without strain showed that surface effects promote the stabilization of a FE phase below

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a critical thickness of 7 nm.²⁶ Experimentally, a thickness-driven phase transition was detected in epitaxial PbZrO₃ thin films^{28,29} or superlattices,³⁰ with critical thicknesses ranging from 8 to 22 nm. However, tunnel transport measurements suggested an antiferroelectric state down to 4 nm PbZrO₃ thickness.³¹ Moreover, tuning lead stoichiometry in 50-nm-thick epitaxial thin films of PbZrO₃ was demonstrated to turn the room-temperature ground state from antiferroelectric to ferroelectric thanks to the incorporation of Pb_{Zr} antisite defects.³²

Here, combining structural and polarization measurements, we report the room-temperature stabilization of pure antiferroelectric epitaxial thin films of PbZrO₃ with thicknesses under 50 nm. We observe a ferroelectric-like state in ultrathin films of 4 nm. Next, we investigate the temperature dependence of the antiferroelectric properties of 45-nm films and reveal a transition to a ferroelectric-like state over a large temperature window (100 K), whose polar configuration is revealed at the atomic scale using scanning transmission electron microscopy. Such surprising polar state is also further evidenced by first-principle-based simulations, which point out the role of epitaxial strain for its emergence in the thin films.

Results and discussion

Structural characterizations. In its bulk antiferroelectric phase, PbZrO₃ crystallizes with an orthorhombic symmetry with a = 5.882 Å, b = 11.783 Å and c = 8.228 Å.³³ In the following, we use the subscripts 'o' and 'pc' to define the orthorhombic and pseudo-cubic symmetries, respectively. PbZrO₃ thin films were grown by pulsed laser deposition on orthorhombic GdScO₃(110)_o single crystal substrates using a KrF excimer laser. A lead-enriched Pb_{1.1}ZrO₃ home-made ceramic target was used for pulsed laser deposition (Supplementary Material). To enable electric-field measurements, we resorted to pseudo-cubic Ba_{0.5}Sr_{0.5}RuO₃ thin films as bottom oxide electrodes. Figure 1a shows a typical 2 θ - ω X-ray diffraction scan of a typical PbZrO₃ (45 nm) / Ba_{0.5}Sr_{0.5}RuO₃ (38 nm) bilayer grown on GdScO₃(110)_o.

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The films do not show any peaks of parasitic phases and display two peaks at 43.95° and 43.57°, corresponding to the (004)_o and (240)_o planes of the orthorhombic crystal symmetry, respectively. These two possible (001)_o and (120)_o epitaxial orientations for PbZrO₃, with the corresponding [001]_o and [210]_o growth directions, (sketches in Figure 1b) have been reported in the literature.^{21,34} The c parameter, inferred from the position of the (004)_o peak, is estimated to 8.23±0.01 Å, which is in good agreement with the bulk orthorhombic value.³³ In order to investigate the in-plane epitaxial strain, reciprocal space mappings were performed around the (240)_o and (33-2)_o planes of the GdScO₃ substrate (Figure 1c-d). While the bottom electrode of Ba_{0.5}Sr_{0.5}RuO₃ appears fully strained on GdScO₃, the in-plane reciprocal lattice of PbZrO₃ strongly deviates from that of the substrate.

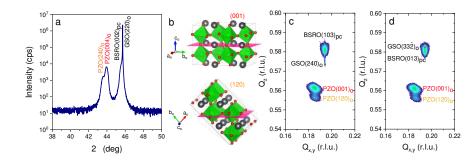


FIG. 1. Structural characterizations of a 45-nm-thick PbZrO₃ film grown on Ba_{0.5}Sr_{0.5}RuO₃-buffered GdScO₃ (110)_o. (a) 2θ-ω X-ray diffraction scan showing two peaks related to different orientations of PbZrO₃. (b) Sketch of the two possible epitaxial orientations of PbZrO₃. The pink planes represent (001)_o and (120)_o basal planes, oriented perpendicular to the growth direction. (c-d) Reciprocal space maps of (240)_o (c) and (33-2)_o (d) peaks of GdScO₃. PZO, BSRO and GSO stand for PbZrO₃, Ba_{0.5}Sr_{0.5}RuO₃ and GdScO₃, respectively. As there are four in-plane variants for the PbZrO₃, the peak indices have not been marked in (c) and (d) but replaced by the film orientation they are referred to instead (see Supplementary Material).

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To complete the structural analysis of these samples, we used high-angle annular dark field scanning transmission electron microscopy (HAADF-STEM) cross section analysis along two zone axes of the GdScO₃(110)_o substrate (Figure 2). Over these large scale (> 500 nm) specimens, the PbZrO₃ film appears well crystallized and continuous. Using image filtering with selected area electron diffraction (SAED), we were able to identify four variants of the PbZrO₃(120)_o domains with 90° in-plane rotations (Figure 2c), with domain sizes varying typically between 10 nm and 50 nm. From the reciprocal space maps, a residual average in-plane strain of -0.05% for (001)_o and +0.13% for (120)_o is estimated in the PbZrO₃ thin film, with respect to the bulk value (Supplementary Material). The larger signal of the spots associated to the (001)_o orientation, with respect to the spots of the (120)_o orientation, suggests the predominance of (001)_o-oriented PbZrO₃ in this film. Although the distribution of these two possible orientations varies from one sample to another with similar thicknesses, a majority of (001)_o domains is often detected for PbZrO₃ on GdScO₃.

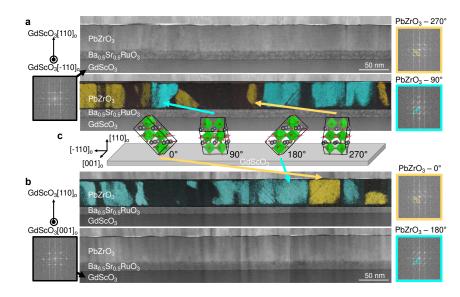


FIG. 2. Room-temperature statistical distribution of the antiferroelectric domains in $PbZrO_3(120)_{\circ}$ along the (a) [1-10]_o and (b) [001]_o zone axes of the GdScO₃(110)_o substrate (see the respective GdScO₃

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of the four variants of these antiferroelectric domains visible in our films. Antiferroelectric signatures. To establish the antiferroelectric nature of the PbZrO₃ thin films, we investigated the polar displacements and oxygen octahedral tilts at the atomic scale. Cross-sectional images were captured by annular bright field scanning transmission electron microscopy (ABF-STEM). As shown in Figure 1, the PbZrO₃ thin films adopt two orientations, $(001)_0$ and $(120)_0$. In the crosssection view of the $(001)_o$ -oriented domains, the Pb atoms are periodically displaced within the film plane, meaning their displacements cannot be resolved due to the overlapping of the displaced atoms in the columns. For the (120)_o orientation, however, these antipolar Pb displacements can be detected when the zone axis is parallel to the c axis. The ABF-STEM image in Figure 3a of a PbZrO₃ thin film with (120)_o preferential orientation shows a region with two crystallographic domains. On the magnification of the first domain, highlighted in green, and the corresponding simulation (Figure 3b), the displacements of the Pb atoms adopt the typical up-up-down-down antipolar pattern (see large grey dots and arrows), as expected for bulk $PbZrO_{3}(120)_{o}$ along the $[001]_{o}$ zone axis (Figure 3d).^{4,35} In the second domain (Figure 3c), highlighted in blue, the staggered atomic displacements along the [2-10]. zone axis (Figure 3e) prevent any conclusions on the polarity of this domain. Nevertheless, in this magnified ABF-STEM image we can observe elongated columns at the oxygen positions (red dots), which appear as single spots in the first domain (Figure 3b), indicating anti-phase tilting of the oxygen octahedra. The twinned domains observed along the $[001]_o$ and the $[2-10]_o$ zone axes are thus 90° oriented domains. Overall, the presence of these twinned nanodomains brings complementary information on the structure of PbZrO₃ thin films.

FFTs on the left panels). HAADF-STEM images are displayed for both zone axes and duplicated with

highlighted PbZrO₃ domains (yellow and blue), as deduced from PbZrO₃ FFTs (right panels). (c) Sketch



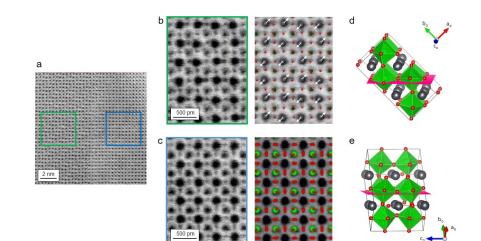


FIG. 3. Atomic scale antiferroelectric features in PbZrO₃. (a) Cross-sectional ABF-STEM image of a PbZrO₃ thin film showing two domains with different atomic arrangements. (b-c) Magnifications of the two domains delimited by the green (b) and blue (c) squares. The left panels display the raw image and the right panels are overlapped by the simulations of the matching atomic arrangement corresponding to [001]_o (top) and [2-10]_o (bottom) zone axes, respectively. The white arrows are guides for the eye to underline the antiparallel Pb atom displacements along the [100]_o direction. (d-e) Sketches of the PbZrO₃ crystals with the zone axis parallel (d) or perpendicular (e) to the c-axis. In both cases, the (120)_o plane is indicated in pink.

Indeed, the specific arrangement of the oxygen atoms, as visible in the blue domain (Figure 3c), stems from the R mode describing the antiphase rotations of the oxygen octahedra ($a^-a^-c^0$ tilting system).³⁶ Furthermore, the staggered polarization observed in the green domain (Figure 3b) is a result of the Σ mode. By definition, the two aforementioned modes, which are required to describe the antipolar structure associated to the *Pbam* symmetry of PbZrO₃,¹¹ tend to signify that our PbZrO₃ thin films fulfill the structural requirement for an antiferroelectric state. However, these features are not sufficient to certify their antiferroelectric character. Indeed, the reversible transition from an antipolar to a ACCEPTED MANUSCRIPT **Applied Physics Reviews** Publishing

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To assess the electrical properties, capacitors were fabricated on the PbZrO₃/Ba_{0.5}Sr_{0.5}RuO₃//GdScO₃ sample by a combination of optical lithography and lift-off of sputtered Pt top circular electrodes, with diameters varying from 5 to 120 μ m. A typical displacement current vs. voltage curve of a 30 μ m diameter Pt/PbZrO₃/Ba_{0.5}Sr_{0.5}RuO₃ capacitor is shown in Figure 4a. Four clear and sharp switching peaks are observed through this 45-nm-thick PbZrO₃ film. The peaks at \pm 2.3 V (equivalent to electric fields of 0.5 MV.cm⁻¹) correspond to the transition to the ferroelectric phase and the peaks at \pm 0.4 V (0.09 MV.cm⁻¹) to the switching to the antipolar phase. The associated polarization vs. electric field loop (Figure 4b) exhibits a well-defined double hysteresis, as expected for antiferroelectrics.³⁷ These electric-field induced ferroelectric phase transitions were further visualized using piezoresponse force microscopy (PFM) through the Pt top electrode of the capacitors (Supplementary Material). While no signal is recorded in the AFE phase, imaging under a dc electric field gives rise to a homogeneous vertical piezoresponse that is switchable by the voltage polarity (Figure 4c, top). Furthermore, the lateral piezoresponse under dc electric field reveals the formation of in-plane domains with submicron sizes (Figure 4c, bottom). As soon as the dc electric field is released, both the vertical and lateral piezoresponses vanish, attesting for a reversible transition to the AFE state. In the electrical measurements as well, we did not detect any contribution from a mixed ferroelectric phase at remanence²¹ and the measured remnant polarization of 2.3 µC.cm⁻² may only result from the constant parasitic capacitive contribution vs. voltage (Figure 4a). One remarkable feature of these polarization loops is the very low leakage current at such low film thickness. No significant variations of the polarization loops were observed for capacitor sizes ranging from 5 to 120 μm diameter. In this epitaxial stack, the quality of the interface between the Ba_{0.5}Sr_{0.5}RuO₃ bottom electrode and the GdScO₃ substrate seems critical to obtain such homogeneous electrical properties. Even though we have reached these high-quality epitaxial films, leakage currents hinder the electrical detection of the AFE-FE transition for films thinner than 45 nm.

ferroelectric state by applying an external electric field is required to conclude on the antiferroelectric

nature of a material.

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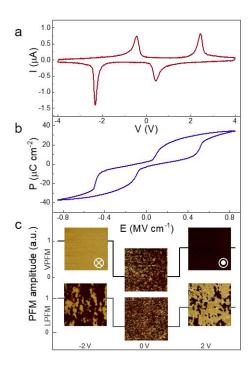


FIG. 4. Electric-field induced ferroelectric phase transitions at room temperature. (a) Current versus voltage loop (I-V) and (b) the corresponding P-E loop. The experiments were performed at 2 kHz. (c) Vertical (top) and lateral (bottom) $3\times3 \mu m^2$ PFM phase images recorded under -2 V, 0 V, and +2 V, corresponding to the FE with downward polarization, the AFE, and the FE with upward polarization, respectively. The lateral PFM phase shows domains in the FE state. The normalized PFM amplitudes plotted in the different configurations (continuous lines) exhibit non-zero signals in the FE state and noise levels in the AFE state (see Supplementary Figure 1). VPFM and LPFM stand for vertical and lateral PFM, respectively.

In this section, we use PFM as a powerful tool to complete polarization vs electric field loops. The piezoresponse was recently reported to be proportional to the dielectric susceptibility of antiferroelectric thin films, which diverges at the AFE-FE and FE-AFE transitions.³⁸ Therefore, by

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applying an external electric field, a sharp increase in the piezoresponse is expected at the critical fields observed in the displacement current vs. electric field loops (Figure 5a). We note that, although the I-E loop shown in Figure 4a and Figure 5a are measured on different samples, they display similar properties, underlying the reproducibility of these antiferroelectric devices. An AC voltage of 2 V peak to peak is superimposed to a series of square pulses with incremental amplitudes (right panel of Figure 5b), between the bottom electrode and the PFM probe in contact with the top Pt electrode. Unlike ferroelectrics, antiferroelectrics are not piezoelectric. The PFM signal is thus recorded only in the ON state of the square pulses. Four peaks are detected in the piezoresponse (left panel of Figure 5b), similarly to the I-E loop (Figure 5a). Nevertheless, a shift of the AFE-FE and FE-AFE fields is observed. The AFE-FE transition in the positive bias occurs at 0.46 MV.cm⁻¹ on the I-E against 0.29 MV.cm⁻¹ with PFM. Similarly, the FE-AFE transition is detected around 0.1 MV.cm⁻¹ on the I-E against 0.2 MV.cm⁻¹ with PFM. While the I-E loop is acquired at 100 Hz in a dynamic regime, the piezoresponse measurement is performed in a quasi-static regime bouncing back and forth between the ON and OFF states of the rectangular waveform. Therefore, the dynamics might not be fully comparable. The PFM set up was then improved so that the experimental conditions are closer to the I-E loop measurements (right panel of Figure 5c). A triangular waveform is applied with a superimposed AC of 0.3 V peak to peak, oscillating at the PFM resonance frequency in order to amplify the collected signal. This process allows the whole loop to be acquired at 100 Hz, as displayed in Figure 5c. Although the matching is not perfect, the four PFM peaks, corresponding to the phase transitions, approach the ones observed for the I-E loop, bridging both detection methods. It should be note that intrinsic transition field deviations might persist as the I-E loop is collected over the whole capacitor (30 µm diameter) and thus considered as a global measurement. On contrary, the electromechanical response is restricted to the contact area of the PFM probe (few tens of nanometers in diameter). The AC voltage amplitude might also contribute to the shift of the coercive fields. As one may expect, we observed a non-zero piezoresponse for the FE phase and a zero piezoresponse in the AFE phase (Figure 5b-c), in agreement with PFM images with and without electric field (Figure 4c). Despite all the above-mentioned different

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measurement conditions, this dynamic PFM technique proves to be of main interest to probe the polar state of ultrathin films, when leakage currents impede the standard electrical approach. Consequently, PbZrO₃ thin films of 24 nm and 4 nm were investigated by such dynamic PFM loops. While the 24-nm-thick film exhibits two additional negative peaks (around 0.2 MV.cm⁻¹) in its piezoresponse, suggesting a mixed AFE-FE phase (Figure 5d), the 4-nm-thick film displays a butterfly-like shape, mimicking the behavior of ferroelectrics (Figure 5e). Even though piezoresponse properties suggest a polar ferroelectric-like state for 4-nm-thick films, further experiments are still needed. Nevertheless, this observation corroborates the predictions²² and experimental observations²⁸⁻³⁰ of a ferroelectric phase transition below a certain thickness in epitaxial PbZrO₃. The stability of the ferroelectric and antiferroelectric phases thus seems to be affected by the so-called size effect.

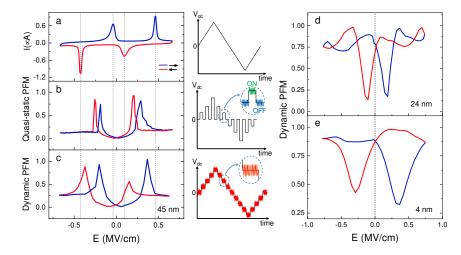
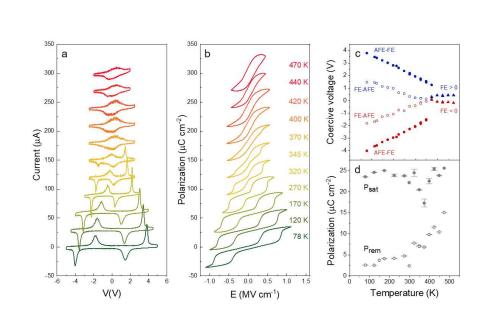


FIG. 5. Electric-field induced antiferroelectric-ferroelectric transitions probed by piezoresponse force microscopy. (a) I-E loop of a 45-nm-thick film collected at 100 Hz. (b) Piezoresponse detected in quasi-static regime on the same sample. (c) Piezoresponse detected in a dynamic regime at 100 Hz. The right panels in (a-c) are sketches of the applied voltage waveforms. From top to bottom: a simple triangular waveform, a series of rectangular waveforms superimposed with an AC voltage (only the ON states are

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recorded), and a triangular waveform superimposed with an AC voltage. (d-e) Dynamic electromechanical measurements of two PbZrO₃ ultrathin films of 24 nm (d) and 4 nm (e). The blue and red curves in (a-e) account for the voltage scanning directions, as sketched in (a).

Temperature-induced phase transition. After evaluating the stability of the antiferroelectric phase of these epitaxial PbZrO₃ thin films when their thickness decreases, we now turn to the influence of temperature. Bulk PbZrO₃ undergoes a temperature-driven phase transition from an antiferroelectric state to a paraelectric state at 505 K.¹⁰ However, several reports indicated the existence of an intermediate phase just below the critical temperature.^{13,15} Dielectric, Raman spectroscopy, and pyroelectric measurements suggest its ferroelectric nature with a corresponding rhombohedral R3c structure.^{14,18,19} Surprisingly, the research to date has no reported such temperature-induced phase transition in PbZrO₃ films thinner than 900 nm. Hence, investigating the polar state of this intermediate phase in epitaxial thin films is of importance to establish their phase diagram.

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equivalent for negative bias. The triangles are the coercive voltages of the ferroelectric-like phase. (d) Temperature evolutions of the remnant polarization (P_{rem}) in solid symbols and of the saturation polarization (P_{sat}) in open symbols. Electrical measurements are performed from 78 K up to 470 K on the 45-nm-thick PbZrO₃ film with a Linkam[®] set up. The current loops and associated double hysteresis loops are depicted in (Figure 6ab). Four displacement current peaks can be clearly observed at 78 K (Figure 6a), giving rise to the characteristic double hysteresis loop (Figure 6b). As the temperature increases, these peaks shift to lower voltages and the coercive fields follow a linear evolution in temperature until 370 K (Figure 6c). At 400 K, the four peaks can no longer be detected and only two displacement current peaks are observed, suggesting a destabilization of the antiferroelectricity upon heating and the onset of a ferroelectric-like behavior with the corresponding FE-like P-E loop. Concomitantly with this apparent phase transition, the evolution of the saturation polarization (Psat) shows a singularity around 370 K, while a non-vanishing remnant polarization (Prem) starts increasing around this temperature (Figure 6d). Hence, the $PbZrO_3$ thin film seems to undergo a transition from an antiferroelectric to a ferroelectric-like state at 370-400 K. For temperatures higher than 470 K, the application of the electric field induces some significant leakage contributions accompanied by irreversible changes, preventing the detection of the paraelectric phase transition. This described linear decrease of the coercive fields with temperature was previously reported for 1000 nm thick films, ranging from 333 K to 473 K. 39 In

FIG. 6. Electric-field induced phase transitions with increasing temperature. (a-b) I-V and P-E loops of a 45-nm thick $PbZrO_3$ film acquired at several temperatures ranging from 78 K to 470 K at 1 kHz. The I-V and P-E loops are vertically shifted. (c) Evolution of the coercive voltages as a function of temperature.

The blue circles correspond to the coercive voltages of the transition from an AFE to a FE state (solid circle) and its associated back-switching (open circle) for positive voltages. The red dots are their

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To gain microscopic insights into the temperature-induced ferroelectric phase transition, we performed in-situ STEM investigations on a similar 45-nm-PbZrO₃ thin film as a function of temperature. HAADF-STEM images of the same region of PbZrO₃ were taken at five different temperatures while heating from 300 K to 570 K (Figure 7a-e). From the raw images, the displacements of the Pb atoms were estimated by comparing their positions to the barycenter of the four surrounding Zr atoms. The maps of the resulting dipoles are displayed in the bottom panels of Figure 7a-e. The background color scale represents the angular modulation of the dipoles while the vector lengths are proportional to the displacement amplitudes. At 300 K, the dipoles arrange periodically in the form of antiparallel stripes aligned along the $(011)_{pc}$ direction (corresponding to the $(100)_o$ axis) in which each stripe contains two parallel dipole lines (Figure 7a). The 4x unit-cell periodicity, associated with the antipolar arrangement in this orthorhombic structure is confirmed by the $%{011}_{pc}$ superlattice reflections in the electron diffraction pattern (Supplementary Figure 2). It appears that the dipoles are not fully compensated (upward dipoles have a larger amplitude than downward dipoles), in line with recent reports in which the quasi-antiferroelectric state of PbZrO₃ displays an amplitude modulation mode or ferrielectric behavior.^{29,40,41} Interestingly, this non-compensation can also contribute to the remnant polarization (2.3 µC.cm⁻²) we observed in the polarization vs. electric field loop of Figure 4. Note that other contributions such as polar antiphase boundaries,³⁵ interface compressive strains⁴² or localized abundant Pb defects³² cannot also be completely excluded. The antipolar arrangement remains at 420 K (Figure 7b) and 470 K (Figure 7c) with a gradual decrease of the Pb displacement magnitude when approaching 470 K (see polar plots in the HAADF images). The angle values exhibit two clear populations at 300 K (Figure 7a), and a more dispersive distribution upon heating up to 470 K (Figure 7b-c). At 520 K, a sudden reorganization occurs with mostly parallel displacements pointing in the plane of the film, characterized by an angular modulation close to 0° (Figure 7d). This pseudo-cubic (010)_{pc} direction of the dipoles is not consistent with the commonly accepted rhombohedral

the case of these 45-nm-thick PbZrO₃ films, the onset of ferroelectricity at a lower temperature (370-

400 K) could be related to the reduced film thickness.

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ferroelectric phase of PbZrO₃. Instead, it could indicate that this ferroelectric-like phase belongs to a tetragonal-like symmetry.^{21,29} On the electron diffraction pattern (Supplementary Figure 2), the typical superlattice reflections of the orthorhombic phase vanish at 520 K. The ferroelectric-like state observed at 520 K disappears at 570 K to make way for a disordered, paraelectric-like, state where the magnitude of the displacement is in the noise range (Figure 7e). To summarize, the polar plots of the Pb displacements highlight these phase transitions as follows: first, a clear distribution in between two opposite orientations at 300 K, then a single polar population at 520 K, and finally an isotropic disordered phase at 570 K (insets of Figure 7a-e). When cooling the specimen down to 300 K, dipoles rearrange in the form of antiparallel stripes, as observed for the initial state (not presented herein).

Overall, the local displacement maps from the STEM measurements (Figure 7) corroborate the electrical measurements (Figure 6), suggesting a temperature-induced phase transition to an intermediate ferroelectric-like phase. We note that the critical temperatures for the ferroelectric phase transition do not perfectly coincide. In the electrical measurements, the ferroelectric-like state appears around 370-400 K while it shows up at 480-520 K in the STEM measurements. A lowering of the AFE-FE transition temperature by 135 K was previously observed in 900 nm-thick PbZrO₃ films when an external DC electric field of 0.265 MV.cm⁻¹ was applied.¹⁹ Thus, the shift of 115±35 K between electrical measurements and static STEM observations could be ascribed to the electric-field-induced stabilization of the ferroelectric phase in our PbZrO₃ films. Indeed, since the free energies of the antiferroelectric and ferroelectric phases are very close, the high electric field required during electrical measurements to switch the dipoles can favor a ferroelectric transition at a lower critical temperature.

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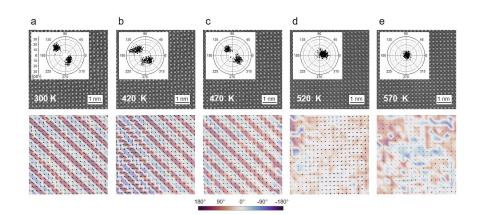


FIG. 7. Temperature-induced phase transition inferred from scanning transmission electron microscopy. (a-e) HAADF-STEM images of the same $PbZrO_3$ domain measured at 300 K (a), 420 K (b), 470 K (c), 520 K (d) and 570 K (e). Insets on the HAADF images display polar plots showing the angle and magnitude distribution of the Pb displacements from their central positions. The bottom panels represent the angle (color scale) and magnitude (vector lengths) modulations of the Pb displacements.

Atomistic simulations based on a first-principle-based effective Hamiltonian scheme provide additional qualitative insight into these temperature-induced phase transitions (see Supplementary Material)²⁷. In the case of bulk PbZrO₃, this effective Hamiltonian predicts the following structural phases when heating the system from 0 K (Figure 8, top): (1) Phase I (0 – 650 K), which is simply the known *Pbam* ground state of PbZrO₃, and that is characterized by three main types of order parameter: an antiphase octahedral tilting about the (011)_{pc} axis ((100)_o), along with antiparallel cation displacements along the (011)_{pc} ((100)_o) and a complex tilting about the (100)_{pc} axis ((001)_o) that are both associated with the Σ point of the cubic first Brillouin zone; (2) Phase II (of *Pbam symmetry too*, 650 – 1300 K), which is deduced from Phase I via the annihilation of the antiphase octahedral tilting about (011)_{pc}, and ``only'' possesses Σ -related cation motions along (011)_{pc} and oxygen octahedral tilting about (100)_{pc}; (3) Phase III (>1300 K), which is the paraelectric state with cubic P*m-3m* symmetry, and for which all order parameters have vanished. Note that, in Phase II, we numerically found that the lattice parameters are

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all close to each other, which may give the impression that this phase is cubic and which thus may explain why it has been overlooked so far (another reason may be that such Phase II exists only on a small local scale in the samples). Effective Hamiltonians are known to qualitatively describe phase transitions' sequence but can provide quantitatively incorrect transition temperatures, as it is the case here for bulk PbZrO₃.⁴³

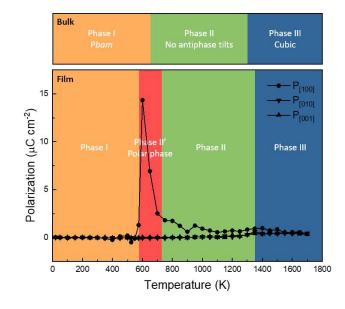


FIG. 8. Computed phase diagram of PbZrO₃ using atomistic simulations. Calculated structural phases of PbZrO₃ as a function of temperature for bulk (top) and an epitaxial film with fixed in-plane parameters in the $(001)_{pc}$ plane (bottom). The computed polarizations vs. temperature along the inplane $(100)_{pc}$, $(010)_{pc}$ and out-of-plane $(001)_{pc}$ directions are displayed for the film case (Supplementary Material).

Let us now turn our attention to the case of PbZrO₃ films for which we mimic epitaxy with biaxial strain by imposing fixed in-plane lattice constants of about 4.165 Å in the (001)_{pc} plane ((120)_o plane), in 18

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about 150 K, which is rather similar to our measurements providing a 100 K window. **Conclusions** Our work demonstrates direct evidence for antiferroelectric behavior in 45-nm-thick epitaxial PbZrO₃ films. The system is found to exhibit a typical double hysteresis loop resulting from the antiferroelectric to ferroelectric electric-field induced transitions as well as the visualizations of an antipolar order at the atomic scale. Reducing the film thickness results in the destabilization of the antiferroelectric state, as revealed by dynamic piezoresponse force microscopy. Finally, we observe a transition to a ferroelectric-like state roughly above 400 K with a wide temperature stability range through temperature-dependent measurements. We observe the transition to a ferroelectric-like state roughly above 400 K with a wide temperature stability range. Atomistic simulations predict that such polar state with Pmc2₁ orthorhombic symmetry arises from epitaxial conditions. Furthermore, the polar displacements associated to this phase suggest a polarization along pseudo-cubic <100>_{pc} directions.

agreement with the experimental values of our PbZrO3 films. Starting from 0 K and increasing the

temperature provides the following structural phases (Figure 8, bottom): (i) Phase I (*Pbam*, 0 – 575 K) as in bulk; (ii) Phase II' ($Pmc2_1$, 575 – 725 K) that looks like bulk Phase II but with the important difference that a ferroelectric polarization now additionally appears along the (100)_{pc} direction in agreement with the polar shifts observed in Figure 7d, with a maximum computed value of about 15 μ C.cm⁻² in good agreement with the experimental values (Figure 6); (iii) bulk-like Phase II (*Pbam*, 725 – 1350 K); (iv) Phase III' (paraelectric, >1350 K), similar to Phase III of bulk but with a P4/mmm

The predicted existence of the novel *polar* Phase II' in epitaxial thin films and not in the bulk indicates that strain is instrumental to make the ferroelectric polarization we observe along a $(100)_{pc}$ direction

to emerge in the films. It is also interesting to realize that this polar phase (i) is predicted to occur at a lower temperature than the Phase I to Phase II bulk transition, in agreement with our experimental demonstrations of a polar phase below the bulk critical temperature; and (ii) has a predicted range of

symmetry because of epitaxial conditions.

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Figures showing PFM imaging through capacitors under or without electric field (Supplementary Figure 1) and electron diffraction patterns from STEM as a function of temperature (Supplementary Figure 2).

Competing interests

Supplementary Material

Acknowledgements

The authors declare no competing interests.

The Supplementary Material contains a description of the methods as well as two Supplementary

These results open questions on the nature of this electric-field and temperature induced ferroelectric

phase in such epitaxial PbZrO₃ thin films. In order to exploit the functional properties of this prototypical antiferroelectric, further theoretical investigations are required to shed light on the

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complex interplay between structure, electric field and temperature.

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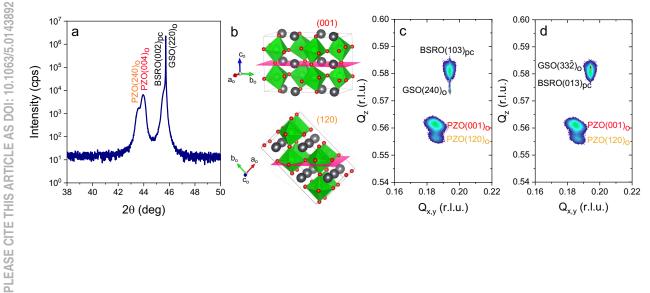
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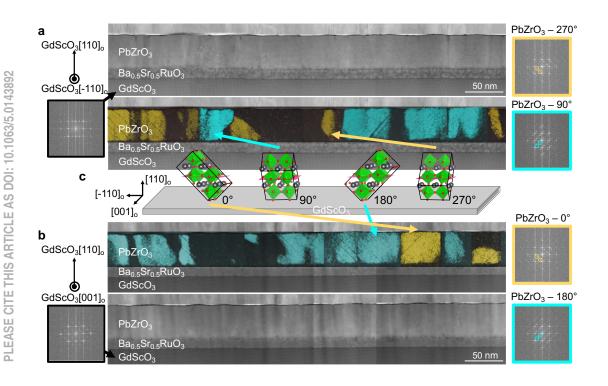
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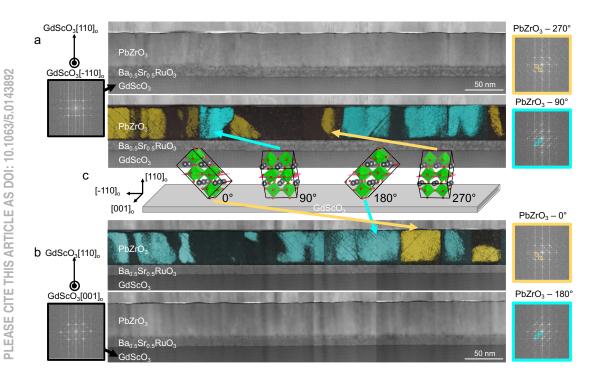








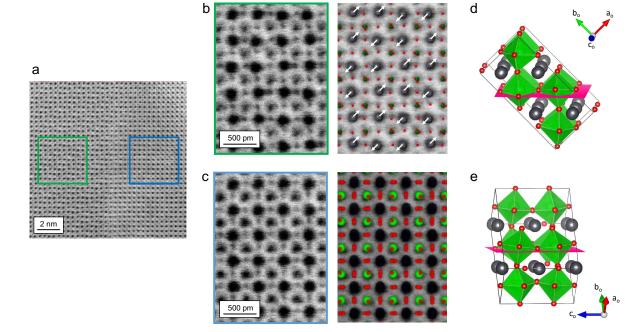






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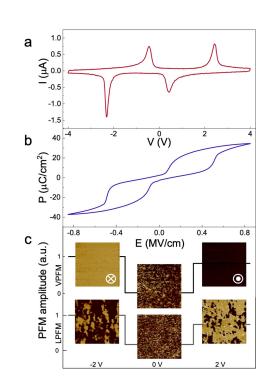
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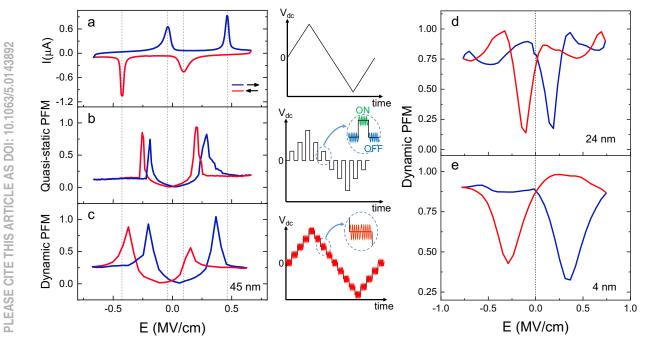


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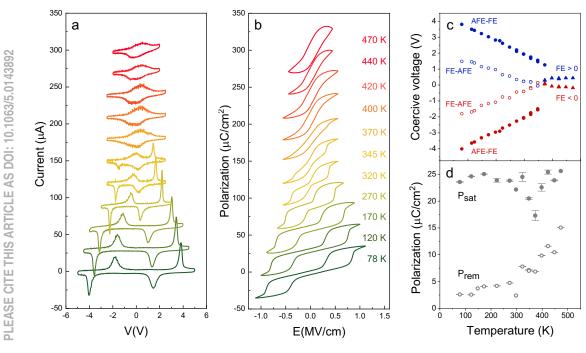
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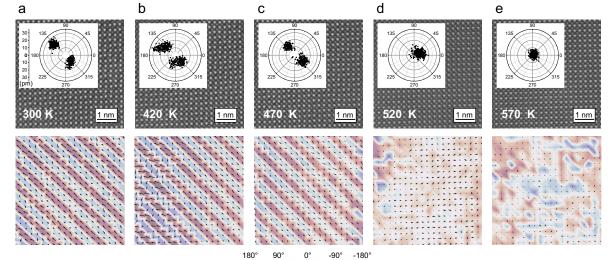






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