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RESEARCH ARTICLE

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Complete coverage path planning for wheeled agricultural robots

Danial Pour Arab^{1,2} | Matthias Spisser² | Caroline Essert¹

1 ICube, CNRS (UMR 7357), Université de Strasbourg, Illkirch, France

²T&S-Technology and Strategy Strasbourg, Schiltigheim, France

Correspondence

Caroline Essert, ICube, CNRS (UMR 7357), Université de Strasbourg, 300 Bd Sébastien Brant, 67400 Illkirch, France. Email: essert@unistra.fr

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Abstract

In the agricultural industry, an evolutionary effort has been made over the last two decades to achieve precise autonomous systems to perform typical in‐field tasks, including harvesting, mowing, and spraying. One of the main objectives of an autonomous system in agriculture is to improve the efficiency while reducing the environmental impact and cost. Due to the nature of these operations, complete coverage path planning (CCPP) approaches play an essential role to find an optimal path which covers the entire field while taking into account land topography, operation requirements, and robot characteristics. The aim of this paper is to propose a CCPP approach defining the optimal movements of mobile robots over an agricultural field. First, a method based on tree exploration is proposed to find all potential solutions satisfying some predefined constraints. Second, a similarity check and selection of optimal solutions method is proposed to eliminate similar solutions and find the best solutions. The optimization goals are to maximize the coverage area and to minimize overlaps, nonworking path length, and overall travel time. To explore a wide range of possible solutions, our approach is able to consider multiple entrances for the robot. For fields with a complex shape, different dividing lines to split them into simple polygons are also considered. Our approach also computes the headland zones and covers them automatically which leads to a high coverage rate of the field.

KEYWORDS

autonomous agriculture, complete coverage path planning, path planning, precision agriculture, route planning, vehicle routing problem, wheeled robots

1 | INTRODUCTION

compared with humans. This transformation touches every domain, including agriculture.

Robots are becoming more prevalent in our daily lives. Increasing the efficiency and reducing the costs makes them both popular and trendy in many industries. They can perform a wide range of specialized and often risky tasks with a remarkably high precision

On the one hand, a growing population necessitates more food and agricultural products (Marques et al., 2019), yet agriculture is also known for polluting the air and increasing mortality rates (Giannakis et al., 2019). An abuse of pesticides and herbicides also has a

All authors contributed equally.

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substantial impact on the environment, animals, plants, and humans, necessitating the development of some practical solutions (Meftaul et al., 2020). In this situation, the role of a precise autonomous system capable of optimizing the cost and efficiency of field operations is more important than ever.

The development of an autonomous system in agriculture is a complex process that requires the integration of several specialized and interrelated subsystems, among which path planning, path following, positioning system, and perception system. In this article, our main focus is the path planning subsystem. We refer readers to Vieira et al. (2021) for more information about path tracking and control laws for vehicles operating in soft soils, to Vieira et al. (2022) for positioning system for an autonomous agricultural robot, to Chen et al. (2021), Lin et al. (2021), and Tang et al. (2023) for perception systems, fruit detection, and positioning.

We focus in particular on the complete coverage path planning (CCPP). Contrary to point‐to‐point path planning, the aim of CCPP is not only to identify a path from an entry point to an exit point, but also to cover at best all the points in a workspace (Khan et al., 2017). CCPP is a fundamental challenge in robotics that has a wide range of applications, such as demining (Đakulovic & Petrovic, 2012), cleaning (Viet et al., 2013), or mapping and monitoring (Becker et al., 2022) to name a few. These applications demonstrate the versatility and significance of CCPP in various areas.

In agriculture, CCPP involves the generation of a path that optimally covers the surface of a field to perform specific operations, such as harvesting, seeding, and fertilizing. The constraints in terms of environment and machinery are very specific compared with other applications. A major concern is the need to avoid repeated passes to the same location. For instance, working a second time on already sown ground will destroy the first seeds, cost more seeds, compact the soil, and ultimately decrease the productivity of the field. Moreover, an agricultural robot often drags an implement to work the field. Its motion capacities are linked to the nature of this implement, and the freedom of movement of the robot differs when the implement is in contact with the ground or not. Turning the implement on or off cannot be done abruptly and requires the robot to go straight for a few meters to activate or deactivate the implement. All these constraints have an impact on the route to generate.

In general, the result of CCPP on a field is a set of back‐and‐forth trajectories connected by smooth and continuous half‐turns at areas along the edges of the field called headlands. The spacing between these trajectories depends on the width of the implement connected to the robot. This spacing is generally referred to as working width.

To perform CCPP on a field and to generate the best possible path, it is important to take into account the topographical and geometrical characteristics of the field, the robot features and capabilities, as well as those of its implements. The quality of CCPP outcome is generally ensured by satisfying and optimizing a set of constraints. These constraints can either be hard constraints, where the conditions must be satisfied, or soft constraints, which have some variable values that are optimized via a cost or reward function. In

general the main objectives of constraints for most of the operations is to maximize the productivity, minimize the cost and environmental damages, such as soil compaction and erosion.

However, constraints vary depending on the operation and the kind of machinery needed for that particular operation. For instance, in a seeding operation the implement is in contact with the ground when it is activated, therefore it can remain activated only in backand-forth trajectories or slight turns. During half-turns it must be deactivated and lifted to prevent machinery damages. This constraint, however, is completely irrelevant for pulverization where the implement is not in contact with the ground. In both cases, the distance traveled while the implement is activated is referred to as working path length, otherwise it is referred to as nonworking path length.

In addition to a wide range of constraints that may differ for each operation, the efficiency of some operations may depend on the result of other operations. For instance, the path for pulverization is predefined based on a tramline farming system which is usually done during tillage. Permanent parallel wheel tracks (tramlines) are created within the field area to eliminate soil compaction from the wheels within the cropped area Bochtis, Sørensen, Busato et al. (2010). In this paper, we propose a generic solution based on a novel CCPP approach for operations in which the implement is in contact with the ground when it is activated. The result of our approach is a sequence of moves that cover the field and the headlands at best.

The remainder of this paper is organized as follows: related works are described in Section 2. The objectives and main contributions of this paper are presented in Section 3. In Section 4, our novel approach is described in detail. The results of an experimental study on real fields of various shapes and sizes, as well as a comparison to ground truth, are reported in Section 5. A discussion follows, underlining the importance and effectiveness of the proposed approach. Finally, Section 6 brings this study to a conclusion and provides new perspectives toward future works.

2 | RELATED WORKS

To address this difficult problem and its numerous constraints, most of the time the CCPP problem is addressed in the literature as two distinct tasks. The first task is to generate a set of parallel back‐and‐ forth trajectories based on field data. The second task is to connect the parallel tracks to form an optimal sequence of trajectories connected by half‐turns, and allocate them to single or multiple robots. We refer to the first task as Coverage Path Planning (CPP), while the second part is mainly known as Vehicle Routing Problem (VRP), or in this particular application Agricultural Routing Problem (AVRP).

One common CPP approach is to generate trajectories parallel to the longest edge of the field, with a spacing equal to the working width, or to simply take a direction as input (Cariou et al., 2017; Hameed, 2017; Hameed et al., 2011; Jeon et al., 2021; Nilsson & Zhou, 2020; Zhou & Bochtis, 2015; Zuo et al., 2010). Extending this

approach, Hameed et al. (2010), Jensen et al. (2012), Plessen (2021), and Zhou et al. (2020) proposed to generate parallel trajectories along a curved reference line as well. After this step, the parallel trajectories are usually simply connected sequentially by half‐turns. Instead of choosing the longest boundary, Edwards et al. (2017) proposed to align the parallel trajectories to the boundary that minimized the number of necessary half‐turns. Cao et al. (2019a, 2019b) proposed an approach based on the rotating calipers algorithm (first proposed by O'Rourke et al., 1986) to determine a reference line that minimizes the number of half-turns. Mier et al. (2023) applied a brute force algorithm to find the optimal driving direction while trying discretized angles using a given step size.

Most studies, however, entirely ignored the coverage of headlands. Only the approaches proposed by Edwards et al. (2017), Jeon et al. (2021), and Nilsson and Zhou (2020) were able to cover the headlands automatically. To cover all corners of the field, Edwards et al. (2017) and Jeon et al. (2021) considered also reverse moves for trajectories inside the headlands. In case of a complex field, none of the approaches described in the literature can handle both headland coverage and field decomposition.

In the more complex case of concave fields, some authors have opted for a subdivision of the field into smaller convex subfields. Jin and Tang (2010) applied a decomposition method, identified a reference line for each resulting subfield, and generated trajectories parallel to the reference line. Finally an optimal sequence of subfields was determined. Oksanen and Visala (2009) and Oksanen et al. (2007) proposed a trapezoidal decomposition approach and a heuristic algorithm to select the best driving direction among 0°, 30°, 60°, 90°, 120°, and 150°. They applied a weighted average cost function to optimize some metrics: (1) operated area divided by total time, including turning time, (2) area of the subfield per remaining area, and (3) distance operated in the subfield.

Hameed (2014) applied a genetic algorithm to obtain the best possible reference line that minimizes the number of trajectories as well as the turning cost. Finally, They took the inclination of each trajectory into account to determine the optimal sequence of trajectories that minimizes fuel consumption. Dogru and Marques (2015a, 2015b) and Shen et al. (2020) applied a decomposition method considering inclination across the field, followed by a genetic algorithm to determine an optimal driving direction for each subfield as well as an optimal sequence of subfields that minimizes energy consumption. Hameed et al. (2016) also considered the inclination in their approach to find an optimal driving direction that simply minimizes the skips and/or overlaps. Jin and Tang (2011) proposed a decomposition method to classify the field into flat and slope areas, then a reference direction that leads to the minimum coverage cost (the weighted average of headland turning cost, soil erosion cost, and curved trajectory cost) was chosen from field edge segments and the slope contours.

Numerous studies have exclusively investigated AVRP, considering the parallel lines as a given input. Some of them focused only on one single robot. Bochtis et al. (2013) presented an approach based on the Clarke–Wright algorithm. Mier et al. (2023) and Plessen (2019, 2018) proposed a pattern-based routing algorithm. Considering one stationary service unit Jensen et al. (2015a, 2015b) proposed an approach based on the state–space search technique. Vahdanjoo et al. (2020) proposed an approach based on simulated annealing while considering several stationary service units. Evans et al. (2020) applied genetic algorithms to their approach while considering a mobile service unit.

Some other studies addressed multirobot AVRP. Burger et al. (2013) represented an approach based on mixed-integer linear programming. Seyyedhasani and Dvorak (2017, 2018a, 2018b) and Seyyedhasani et al. (2019) proposed a heuristic approach based on the Clarke–Wright algorithm and Tabu search. Cariou et al. (2020) proposed an approach to solve AVRP for a convoy of homogeneous robots. Conesa‐Muñoz et al. (2015, 2016a, 2016b) applied simulated annealing to their approach. Utamima et al. (2019a, 2019b) presented an evolutionary approach enhanced by a neighborhood search. Khajepour et al. (2020) applied an adaptive large neighborhood search in their approach. Conesa‐Muñoz et al. (2015, 2016a, 2016b), Khajepour et al. (2020), and Utamima et al. (2019a, 2019b) also considered one stationary service unit in their approaches. Jensen et al. (2012) represented an approach based on the Dijkstra algorithm while considering a mobile service unit cooperating with a primary service unit. Bochtis, Sørensen, and Vougioukas (2010) and Bochtis and Sørensen (2009, 2010) proposed an approach based on a breadth‐ first search algorithm modified by additional heuristics while considering one or two stationary service units or mobile service unit was.

All of these methods considered the two tasks as two separate problems. This can however have some limitations and possibly miss some interesting solutions. We think that browsing the solution space in one single exploration/generation step has the potential to find more exhaustively the interesting solutions. The approach we propose in this paper is based on this assumption, and includes many benefits that are highlighted in Section 3.

3 | MOTIVATIONS AND CONTRIBUTIONS

Performing a CCPP while respecting all constraints is a complex and difficult challenge. As previously mentioned, the novelty of the approach we propose is to generate the parallel tracks and the turns in one process, with the objective of allowing more possible alternatives.

Moreover, various simplifications of the problem and prior assumptions have been made in the literature. Most of these simplifications helped to find a feasible solution in a reasonable time for a category of fields, even if it may not be the most optimal. In this work, we aim at considering a maximal range of possible field shapes and configurations.

Using simplifications could also lead to a risk of oversimplification and ultimately to unfeasible solutions. For instance, assuming that a field can be accessed from all of its edges, which is not the case for most of the fields where crossing some edges may damage the robot or even the neighboring field, could lead to a solution that the farmer cannot apply in practice. A common solution to solve this problem was to consider an inner offset for a field polygon as headlands and doing the headland

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coverage manually. The automatic coverage of the headlands was only considered by Edwards et al. (2017), Jeon et al. (2021), and Nilsson and Zhou (2020). However Edwards et al. (2017) and Jeon et al. (2021) considered all field edges as accessible. Conversely, another simplification could be to consider as a possible entry or exit only one or two separate points, which would strongly limit the possible solutions. This is the approach followed by Nilsson and Zhou (2020), who considered only one point for both entering and exiting the field.

Other oversimplification for operations in which the implement is in contact with the ground while in use, include considering that tight turns can be made with the implement on, or considering that lowering and raising the implement could be done instantly. However in practice, it is not the case. Such simplifications would lead to an overestimation of the coverage rate.

The aim of our study is to provide a complete and realistic solution using a progressive CCPP approach for fields of various shapes and sizes, while avoiding oversimplification as much as possible to prevent inappropriate solutions. We aim at considering several possible entrances and authorizing the robot to finish its task anywhere on an accessible edge of the field, to increase the possibility of finding the optimum solution. We also propose an approach that can be parameterized and customized for different types of machinery and operations. Our approach is capable of dealing with both headland coverage and field decomposition.

This paper describes our approach that includes the following contributions in one single integrated system:

- automatic selection of best entry and exit points among an accessible edge of the field;
- one-step generation of tracks/turns optimizing coverage, overlaps, damage, and working time;
- all types of field shapes considered: convex or nonconvex with various dividing lines;
- output is several optimal alternative paths with a variety of properties;
- intelligent coverage of the headlands;
- geometry of the vehicle and the implement are taken into account:
	- offset between the vehicle and the implement,
	- minimum turning radius of the vehicle when the implement is off,
	- minimum turning radius of the vehicle when the implement is on and in touch with the ground;
- distance needed for activating/deactivating or lowering/raising the implement is taken into account;
- reverse moves are allowed for performing turns and half-turns;
- curved edges are taken into account.

4 | METHODOLOGY

Our approach consists of three steps: (1) preprocessing, (2) exploration, and (3) similarity check and selection of optimal solutions. The objective of the preprocessing step is to prepare the

field. Its inputs are the field polygon (i.e., a sequence of counterclockwise points), one or several dividing lines to decompose the field polygon if needed, the access segments, the working width, and the minimum turning radius of the robot. The output of this step is a set of entrances, a set of zones that might be used as headland and a set of turning spaces. Turning spaces are useful to take a trajectory within a headland and/or perform a turn from one headland to another.

Finding every potential solution and creating a solution space are the goals of the second step which is referred to as exploration algorithm. A solution found by the exploration algorithm is a path, that is, a sequence of trajectories that starts from an entrance, covers the field and the headlands at best, and ends on one of the access segments.

These two steps could be repeated several times if several entrances and/or dividing lines are provided. For simple fields for which no decomposition is required the number of explorations is the same as the number of entrances. For a complex case, that *d* alternative dividing lines are provided and *e* entrances are detected, our approach performs *d*∗e explorations. The approach performs also *e* more explorations while considering no dividing line. Since for some concave fields the ideal solution could be identified without decomposing the field. For instance, providing three possible entrances and three alternative dividing lines requires running the preprocessing step four times (one time with no dividing line plus the number of dividing lines) and executing the exploration algorithm 12 times in total (the product of four different preprocessing results and three entrances). Consequently, the final solution space is the union of 12 solution spaces obtained from the exploration algorithm.

Finally during the similarity check and selection of optimal solutions, the cost of each solution is computed. Then, similar solutions are extracted using a similarity function, and grouped into families of solutions. Only the lowest-cost solution is kept for each family. After removing similarity from the solution space, the best solutions with the lowest cost are selected. In the next sections, after giving a few definitions, we describe each of these steps in more detail.

4.1 | Definitions

Let us start by defining a few notions and notations. We define *w* as the width of the implement attached to the robot. Our approach exclusively considers operations in which the implement is in contact with the ground while in use. As a result, the implement is regarded as having two possible states: on and off. When on, the implement is completely in contact with the ground, and when off it is completely raised. The surface covered when the implement is in contact with the ground is called worked area or surface, and conversely the surface never in contact with the implement is called unworked area or surface.

While the implement is in the off state, it is possible to perform tight or half‐turns respecting *γoff* as the minimum turning radius of the POUR ARAB ET AL. $\begin{bmatrix} 5 \end{bmatrix}$

robot. As the implement is elevated, the corresponding curved surface will not be worked. When the implement is on, to avoid damaging it during turns, only slight turns respecting a minimum turning radius of *γon* are authorized. In this case, the corresponding surface will be worked.

However, the robot cannot change state abruptly from on to off or vice versa. It must be done gradually while the robot moves straight. Therefore the transition state is defined as a third state when changing from on to off and conversely. The straight trajectories in the transition state have a constant length of e_t , and are referred to as transition trajectories. ℓ*^t* represents the distance required on the straight trajectory before or after performing a tight turn, where the surface will not be worked either. We refer to these unworked portions of straight trajectories as gaps. They are represented in Figure 1 with crossed out red segments. Therefore, each tight turn causes two gaps in the trajectory.

4.2 | Preprocessing: Definition of headlands and turning spaces

After acquiring the raw input data, and converting from the geographic coordinate system to the Cartesian coordinate system, three preprocessing operations are performed: the generation of entrances, the generation of headlands, and the generation of turning spaces. Both operations are detailed below.

4.2.1 | Entrances

Entrances are the locations where the robot can enter the field. Each entrance also contains the direction or heading of the robot at the corresponding location. Given the field polygon and the access segments, our approach determines the entrances on each corner of an access segment where its distance from the adjacent edge of the field polygon is *w*∕2. Its direction is the same as the direction of the adjacent edge. Once all candidate entrances are determined, an expert must validate them or discard the entrances that seem irrelevant. Figure 5 represents the selected entrances for a subset of the evaluation data set.

4.2.2 | Headlands

A headland is a space adjacent to the boundary of the field that can be used to perform half‐turns. When half‐turns are performed in a headland, this space is not worked, and two gaps are also caused before and after it along the trajectories. Then, this space must be worked separately after the rest of the field is finished. Our method starts by defining these headlands, and anticipating how they can be covered.

To be able to define these surfaces, for each boundary of the field a headland area is generated that contains:

• one outer border that corresponds to the field boundary;

FIGURE 1 Preprocessing result for *p* = 2. The field polygon is represented by blue points and black and green solid segments. (a) Preprocessing result for a field and (b) a close-up on a preprocessing result. [Color figure can be viewed at wileyonlinelibrary.com]

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- one inner border that is generated parallel to the outer border inside the field at a distance of *p* ∗w, where *p* is either given as an input, or deduced from *w* and *γoff*;
- *p* inner trajectories that are generated between the outer and inner borders and parallel to them, at a distance of *w*∕2 from the borders and *w* from each other;
- one gap-covering trajectory generated inside the field at a distance of *w*∕2 from the inner border and parallel to it.

These geometric elements are illustrated in Figure 1 for $p = 2$. If a dividing line is provided, another type of headland is also defined: it is fully included within the field polygon with two inner borders, *p* inner trajectories, and two gap‐covering trajectories centered around the dividing line, and it has no outer border. This is illustrated in Figure 1 where the dividing line is represented in brown.

Therefore the inner trajectories are mainly useful for covering the unworked surfaces caused by the half‐turns and the gap‐covering trajectories are used to cover the unworked surfaces caused by gaps.

4.2.3 | Turning spaces

The third preprocessing operation is the computation of turning spaces. A turning space is defined at an angle between two adjacent headlands, and ensures a safe and feasible turn to or between inner or gap‐covering trajectories of a headland or switch between subfields, if a dividing line is provided. It is delimited by two turning lines parallel to the angle bisector.

As illustrated in Figures 2a,c, for two adjacent headlands first their angle bisector is computed (black dashed line). Finally the two turning lines (blue solid lines) are computed parallel to the angle

bisector with a spacing of *l*/2 where $l = \max(\sqrt{2} (p*w), 2(\ell_0 + \gamma_{off}))$, where ℓ _o is the length of the offset between the robot and the implement. Before a tight turn, there is a straight gap trajectory. Consequently the robot is ℓ*^o* meters ahead of the implement when the gap trajectory is performed. Therefore, ℓ*^o* must be taken into account while computing turning spaces to provide the robot enough space to turn.

The intersection between turning lines and the inner/gapcovering trajectories will be used as candidate start/end point for turns from one headland to another. Therefore, regardless of the angle between two headlands, turning spaces can ensure a proper space for turns to travel to inner and or gap‐covering trajectories of adjacent headlands.

Let us note that not all of the headlands and turning spaces generated during the preprocessing step will necessarily be used. The exploration algorithm will decide which ones will be used. Section 4.4 provides more detail on how turning spaces are used to make turns and half‐turns inside a headland.

4.3 Trajectory types and metrics

To facilitate understanding of the proposed approach, it is essential to introduce some useful concepts and metrics. To cover the field, the robot performs a series of long straight lines and turns to change directions. When performing straight lines, the implement is always on.

Dubins trajectories (Dubins, 1957) and Reeds–Shepp curves (Reeds & Shepp, 1990) are employed to generate continuous and smooth turns. Taking as input a minimum turning radius, the starting and destination coordinates, and the direction of the robot at these

FIGURE 2 Trajectory (a, c) and tree (b) representations of turns inside the turning spaces. (b) The tree representation of trajectories of (c). [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

coordinates, both methods compute the shortest curve from the starting point to the destination point, with the difference that the Reeds–Shepp method also considers reverse moves while all turns generated by the Dubins method contain only forward moves.

Therefore a turn generated by the Reeds–Shepp method is optimal in terms of trajectory length, but in terms of travel time a turn generated by the Dubins method may be better, as a reverse move requires the robot to stop, change the direction and accelerate to reach again its target speed. Moreover, the Dubins method may be used with the implement on during a slight turn when the radius is wide. It is not the case with the Reeds–Shepp method which always needs to have the implement off as a reverse move is needed. Consequently, in our approach turns with no reverse moves are preferred. However if performing a turn with no reverse moves is not possible, then a turn with reverse moves is also examined. Lastly, between straight lines with implement on and turns with implement off, a short and straight transition trajectory is needed to change the state of the implement.

Taking into account these considerations, six different feasible combinations of trajectories and implement states were defined as follows:

- STRAIGHT ON: straight trajectory while the implement is on.
- DUBINS_ON: turn computed via Dubins method in which the implement is on.
- DUBINS_OFF: turn computed via Dubins method in which the implement is off.
- REEDS OFF: turn computed via Reeds–Shepp method in which the implement is off.
- GAP_OFF_ON: transition trajectory of length ℓ*^t* during which the implement is transitioning from off to on.
- GAP ON OFF: transition trajectory of length l_t during which the implement is transitioning from on to off.

A few rules apply when defining a sequence of trajectories of the above types. As a first rule, a GAP_OFF_ON trajectory must always be followed by a STRAIGHT_ON trajectory, where both trajectories have the same direction. The second rule is that a STRAIGHT_ON trajectory only can be followed by a DUBINS_ON or a GAP_ON_OFF trajectory. Consequently the third rule says that a GAP_ON_OFF trajectory can be either used for exiting the field or it must be followed by a DUBINS_OFF or a REEDS_OFF trajectory. According to the fourth rule, a DUBINS_OFF or a REEDS_OFF trajectory can be either used for exiting the field or it must be followed by a GAP_OFF_ON trajectory. We refer to these rules as the trajectory sequence rules. Let us note that a trajectory used for exiting the field must end up on an access segment.

A path is a sequence of *k* trajectories with a variety of these five types. Therefore, a trajectory Λ_i with a length of ℓ_i where $\{i \in \mathbb{N} \mid i \leq k\}$ is represented as $((P_i, ∅_i), (P'_i, ∅'_i), Γ_i)$ where $(P_i, ∅_i)$ represents its start point and direction, (P[']_{*i*}, ϑ [']_{*i*} represents its destination point and direction, and Γ*ⁱ* precise its trajectory type. Assuming that the directions of the robot and its implement are the same, *Pi* and *P*′*ⁱ*

represent the location of the implement. It is relatively straightforward to compute the location of the robot on the path when the distance between the implement and the robot is known.

A DUBINS_ON trajectory can only be used to travel from one headland to another using a slight turn. The angle between these two headlands must be between *π* − *α* and *π* + *α* where *α* = arcsin $\left(\frac{l}{2 * γ_{on}}\right)$ and *l* is the spacing between the turning lines.

Finally, we define the four following metrics that are used to check the suitability of the candidate solutions in our approach.

Worked area: The worked area is the first of the key metrics in this approach. This metric is only computed for STRAIGHT_ON and DUBINS_ON. For all the other types of trajectories, the worked area is zero. For a trajectory Λ*i*, if Γ*ⁱ* is STRAIGHT_ON, then the worked area is given by *w*∗ℓ*i*. If Γ*ⁱ* is DUBINS_ON, the curve between *Pi* and *P*′*ⁱ* is first sampled to a set of points with a spacing of 0.5m between two consecutive points. Then for each pair of consecutive samples and having the direction at each sample, the two lateral ends of the implement is computed and a trapezoid is constructed. Finally the worked area is computed as the sum of areas of all trapezoids.

Overlap area: This metric, that measures the overlap area of two trajectories, is only computed for two trajectories of types STRAIGHT_ON, two DUBINS_ON, or one STRAIGHT_ON and one DUBINS ON. Otherwise it is equal to zero. Once the worked areas of the two trajectories are computed, the overlap area is deduced by calculating their intersection.

Damage: This Boolean metric verifies whether the robot is crossing a trajectory that was previously worked (types STRAIGHT_- ON or DUBINS ON), with a new trajectory while its implement is off (DUBINS_OFF, REEDS_OFF, GAP_OFF_ON, or GAP_ON_OFF). This avoids to unnecessarily damage the previously worked zones with the wheels of the robot without working it again.

Inside: The last metric, named inside, is also Boolean. For a trajectory Λ*ⁱ* if the robot and its implement remain inside the metric is true, otherwise it is false.

4.4 | Exploration algorithm

The overall concept of the exploration algorithm is to take as input the result of the preprocessing, the access segments, a set of hard constraints, *γ*_{on}, *γ*_{off}, *ℓ*_t, and the coverage threshold, to progressively build a tree of nodes representing possible sequences of trajectories (locations, directions, and trajectory types) satisfying the hard constraints. The following sections detail the notion of node, the hard constraints, and the method used to build the tree.

4.4.1 | Nodes

Each node of the tree represents a possible candidate for the next step of the trajectory. It contains a flag representing one of the five possible trajectory types, and a corresponding destination point and direction. A set of parent and child nodes N_p and N_c are represented,

respectively, by $(P_p, θ_p, Γ_p)$ and $(P_c, θ_c, Γ_c)$. Consequently, a trajectory $Λ_c$ from N_p to N_c is represented as $((P_p, \vartheta_p), (P_c, \vartheta_c), \Gamma_c)$.

The root of the tree is a specific node containing the entrance location and direction, and a default trajectory type with the implement off. A leaf node is a specific node containing an exit point located on an access segment, a direction, and a trajectory type with the implement off.

A solution is a path represented by a branch of the tree, that is, a sequence of trajectories from the root to a leaf node.

4.4.2 | Hard constraints

The hard constraints are Boolean constraints that must be satisfied by a solution to be valid. We defined five hard constraints, most of them linked to one of the previously defined metrics: inside constraint, limited overlap constraint global overlap constraint, local loop constraint, damage constraint, switch constraint, and minimum working distance constraint. A node $N_c = (P_c, \vartheta_c, \Gamma_c)$ can be added to the tree as a child of *N_p* = (P_p , ϑ_p , Γ_p) only if the candidate trajectory Λ_c ((P_p , ϑ_p), (P_c , ϑ_c), Γ_c) satisfies all the hard constraints.

Inside constraint: According to the inside constraint, the inside metric of Λ*^c* must be true.

Damage constraint: The damage constraint ensures that the damage metric of Λ*^c* over trajectories constructed for all ancestor nodes of N_p remains false.

Limited overlap constraint: This constraint forbids overlaps in the center of the field, that is, outside the headlands and the gapcovering trajectories.

Global overlap constraint: The global overlap constraint limits the overall overlap, within authorized zones, to a certain threshold. When adding a new node, the overlap between Λ*^c* and all its ancestors is computed, and added to a cumulative sum. When the cumulative overlap exceeds a global overlap threshold Δ*global* over the surface of the field, the branch is discarded. If a dividing line is provided, this metric is applied on each subfield separately.

Local loop constraint: At a more local level, to avoid undesirable local loops, when adding a new node the overlap between Λ*^c* and the ancestors is computed. If an overlap is found that exceeds Δ*local*, which is a percentage of the area of Λ*^c* named local loop threshold, then the branch is discarded. An exception is made to the local loop constraint when the objective in terms of coverage rate is satisfied, to let the robot reach an access segment to exit the field.

Switch constraint: In case a dividing line is provided, this constraint ensures that a switch between subfields is authorized: it is if the worked area since the last switch is more than a threshold Δ*switch* called switch threshold, or if the objective in terms of coverage rate is already satisfied for the current subfield.

The minimum working distance constraint: Ensures that the sum of the lengths of consecutive trajectories of type STRAIGHT_ON or DUBINS_ON is not lower than a threshold Δ_{min_dist} named minimum working distance threshold. The main reason behind this constraint is that it is inconvenient and expensive to activate the implementation over a short distance. Therefore, after a trajectory of type STRAIGHT_ON or DUBINS_ON, only another STRAIGHT_ON or DUBINS_ON trajectory is authorized if the minimum working distance constraint is not respected yet.

4.4.3 | Construction of the tree and its trajectories

The construction of the tree and its trajectories can be detailed at two different levels: the initialization that defines how the initial trajectories are created, and the node generation and exploration that describes how back‐and‐forth trajectories are created and added to the tree. In this section we also describe how and in which conditions a turning space is used for the generation of turns that lead the robot to an inner or gap‐covering trajectory of a headland.

Initialization: The first step consists of initializing the tree by adding an entrance $N_0 = (P_0, \vartheta_0, \Gamma_0)$ to the tree and generating the first branches of the tree. As illustrated in Figure 3, three options can be followed to start working:

- go straight and start working immediately: in this case, the first trajectory will be of type GAP_OFF_ON to point *N*1. After this, the next trajectory will have to be of type STRAIGHT_ON.
- cross the headland to point *N*² with implement off. After this, the next trajectory has to be of type GAP_OFF_ON then STRAIGHT_ON.
- turn immediately in the headland to points *N*₃ or *N*₄. After this, the next trajectory has to be of type GAP OFF ON then STRAIGHT_ON.

After being validated by the hard constraints, these nodes are added to the tree as children of N_0 and further exploration is conducted on each leaf of the tree. In Figure 3 gap-covering trajectories are not illustrated because gap‐covering trajectories are mostly for covering the unworked areas caused by transition trajectories, therefore they are not used for initialization.

Node generation and exploration: After initializing the tree, a depth‐first exploration is performed. In general for each unvisited leaf of the tree, new nodes are generated respecting the trajectory sequence rules. The nodes that satisfy the hard constraints are added to the tree as the new children of the leaf. One of these children is then selected for further node generation and exploration. If all of the generated nodes for a leaf violate at least one hard constraint, the leaf is removed from the tree and the exploration continues on its siblings.

For each unvisited node $N_p = (P_p, \vartheta_p, \Gamma_p)$, a ray r_p that starts from P_p with the direction \mathcal{O}_p is generated. The intersection of r_p with inner borders of all headlands and all turning spaces is then calculated. The intersection of r_p with a headland inner border leads to the generation of a cycle of traversals and half‐turns while an intersection with a turning space leads to a headland switch. In case that the field polygon is divided into subpolygons by a dividing line, only the inner borders and turning spaces that are inside the same subpolygon as *Pp*

FIGURE 3 Trajectory and tree representation of the initialization. The entrance and root of the tree N_0 are represented by a red triangle. *N*₁, *N*₂, *N*₃, and *N*₄ are the first nodes that might be added to the tree as children of *N*₀. Orange dashed lines represent trajectories from *N*₀ toward its children. [Color figure can be viewed at wileyonlinelibrary.com]

FIGURE 4 Trajectory and tree representation of a cycle of traversal and half-turn. *N_n* is the selected leaf for which the node generation is conducted. The purple point represents an exit node. For readability purposes, turning spaces, inner, and gap-covering trajectories of headlands are not represented in this figure. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

are considered for intersection computation with *rp*. This is useful for limiting the unnecessary switches between subpolygons.

Cycles of traversals and half‐turns: A cycle of traversal and half-turn is a sequence of trajectories of types: GAP_OFF_ON, STRAIGHT_ON, GAP_ON_OFF, and DUBINS_OFF. They can be made either in the main part of the field or within a headland along the boundary of the field.

As illustrated in Figure 4 , ray r_p hits the vertical headland's inner border on the right, called the destination inner border, at the position of N_{c3} . As a result, trajectories from N_p to N_{c3} with two intermediate nodes N_{c1} and N_c 3 are straight trajectories of types GAP_OFF_ON, STRAIGHT_ON, and GAP_ON_OFF, respectively. To complete the cycle the possible turns from *Nc*³ are calculated. The positions of *Nc*⁴ and *Nc*⁵ are determined by computing the intersection of rays r_r and r_l with the destination inner border. These two rays are parallel to r_p with a spacing of w. The direction at N_{c4} and N_{c5} is the opposite direction of ϑ_p . In the particular case where we are close to a neighbor headland and the trajectory is oblique to it, point *N_{c6}* is also computed as the intersection of rays r_r or r_l and the inner

border of the neighbor headland. This allows for more options for the algorithm in terms of satisfaction of the various overlap and damage constraints.

Note that in exceptional cases where the typical cycle does not satisfy the hard constraints, type REEDS_OFF is also examined for the last trajectory.

Headland switch: The process of traveling from one headland to an adjacent headland via a turning space is referred to as headland switch. It is used to cover the headlands that were not worked due to the half‐turns. It is also useful for going from one subfield to another, if a dividing line was provided to decompose the field polygon. Figure 2a,c illustrates a trajectory representation of different possibilities of headland switch and Figure 2b demonstrates a tree representation of Figure 2c.

As illustrated in Figures $2a$,c, the position of N_{c3} is the intersection of r_p and a turning space referred to as selected turning space. Subfigure a illustrates the intersection of r_p with a turning line. Subfigure c represents a complex case in which all possible ways to switch from the right headland to two possible neighbor headlands are shown. In general complex cases happen only around a dividing

line. A headland switch is also a sequence of GAP_OFF_ON, STRAIGHT_ON, GAP_ON_OFF, and DUBINS_OFF trajectories. The first three trajectories (trajectories from N_p to N_{c3}) that are straight trajectories of types GAP_OFF_ON, STRAIGHT_ON, and GAP_ON_OFF, are used to arrive at the selected turning space. Afterwards, all possible turns from N_{c3} to other headlands at destination nodes (N_{c4}, ..., N_{c10}) are determined by computing the intersection of the inner and gap‐covering trajectories of the target headlands with the corresponding turning spaces. The direction of a destination node corresponds to the direction of the target inner or gap‐covering trajectory. Their trajectory type is set to DUBINS_OFF, therefore turns are generated by the Dubins method. If they do not satisfy the hard constraints, their trajectory type is modified to REEDS_OFF and a turn generation with the Reeds–Shepp method is also examined.

The number of nodes generated to switch from one headland to another depends on the number of inner and gap‐covering trajectories of the target headland. It also depends on whether an inner or gap-covering trajectory of the target headland intersects with an access segment or not.

Exiting the field: During the cycles of traversals and half‐turns, if ray r_p intersects with an access segment (green solid line segment), a sequence of trajectories of type GAP_OFF_ON, STRAIGHT_ON, and GAP_ON_OFF (illustrated by $N_p \rightarrow N_{c1} \rightarrow N_{c7} \rightarrow N_{c8}$ in Figure 4) is also generated to examine the possibility of exiting the field.

Another way of exiting the field is when working the headlands. If the current direction crosses a turning space, and this turning space is adjacent to an access segment, then the possibility of turning to exit the field with a node of type DUBINS_OFF is examined. This situation is illustrated in Figure $2c$ with the sequence of nodes $N_p \rightarrow N_{c1} \rightarrow N_{c2} \rightarrow N_{c3} \rightarrow N_{c11}$.

In these two cases, a leaf node is generated to finish the branch. Then the sum of the worked areas of all the trajectories in the branch is computed. The branch is kept only if this sum is greater or equal to a predefined coverage threshold Δ*cov*. We say that a branch satisfying this criterion and the hard constraints are valid. The output of the exploration algorithm is a set of valid solutions (tree of valid branches) that is referred to as the solution space.

4.5 | Similarity check and selection of optimal solutions

Once the solution space is generated, it is usually wide and browsing all the solutions would be a tedious task for the user. To present to the user only a few of the most relevant solutions, we first define a cost function based on the metrics, then we explain how we group the solutions into families based on a similarity criterion and select the optimal solution of each family.

To compute and compare the solutions found by the exploration method, we propose a cost function to minimize, built as a weighted average of four soft constraints: (1) *Scov*, maximizing the coverage

rate; (2) S_{ovl} , minimizing the overlaps; (3) S_{nwd} , minimizing the nonworking distance; and (4) *Sotm*, minimizing the operation time.

Maximizing the coverage rate: The first soft constraint S_{cov} is calculated as follows:

$$
S_{cov} = 1 - \frac{C_i - C_{min}}{C_{max} - C_{min}}, \qquad (1)
$$

where *Ci* is the area covered by solution *i*, and *Cmin* and *Cmax* are, respectively, the minimum and the maximum worked area over the entire solution space. Therefore minimizing S_{cov} leads to maximizing the coverage rate.

Minimizing the overlaps: The second soft constraint *Sovl* is calculated as follows:

$$
S_{\text{ovl}} = \frac{O_i - O_{\text{min}}}{O_{\text{max}} - O_{\text{min}}},\tag{2}
$$

where *Oi* is the overlap area of solution *i*, and *Omin* and *Omax* are, respectively, the minimum and the maximum overlap area over the entire solution space.

Minimizing the operation time: The total time required to travel all trajectories of solution *i*, denoted *Ti*, is computed as follows:

$$
T_i = \frac{L_i^{on}}{V_{on}} + \frac{L_i^{off}}{V_{off}} + \frac{L_i^{gap}}{V_{gap}},
$$
\n(3)

where L_i^{on} is the length of all STRAIGHT_ON and DUBINS_ON trajectories, L_i^{off} is the length of all DUBINS_OFF and REEDS_OFF trajectories, and L_i^{gap} is the length of all GAP OFF ON and GAP ON OFF trajectories and for solution *i*. V_{on} , V_{off} , and V_{gap} are, respectively, the average speed of the robot when its implementation is in on, off, and transition modes. Therefore, the fourth constraint *Sotm* is defined as follows:

$$
S_{otm} = \frac{T_i - T_{min}}{T_{max} - T_{min}},
$$
\n(4)

where *Tmin* and *Tmax* are, respectively, the minimum and the maximum traveled time over solutions of the solution space.

Minimizing the nonworking distance: The third constraint *Snwd* is the sum of the lengths of all trajectories when the implement is not on, that is, all DUBINS_OFF, REEDS_OFF, GAP_OFF_ON, and GAP_ON_OFF trajectories. It is calculated as follows:

$$
S_{nwd} = \frac{L_1^{nw} - L_{min}^{nw}}{L_{max}^{nw} - L_{min}^{nw}},
$$
\n(5)

where $L_i^{nw} = L_i^{off} + L_i^{gap}$, and L_{min}^{nw} and L_{max}^{nw} are, respectively, defined in a similar fashion as the minimum and the maximum nonworking distances over the entire solution space.

Final cost function: The final cost function *f* is defined as follows:

$$
f = \frac{(S_{cov} * W_{cov}) + (S_{ov1} * W_{ov1}) + (S_{otm} * W_{otm}) + (S_{nwd} * W_{nwd})}{W_{cov} + W_{ov1} + W_{otm} + W_{nwd}},
$$
(6)

where W_{cov} , W_{ovl} , W_{atm} , and W_{nwd} are weights given as input for the corresponding cost functions.

The generated solution space may contain several very similar solutions where their differences could be only one turn or two. To eliminate suboptimal solutions while still preserving a variety of propositions, they are grouped into families of solutions based on a similarity criterion, and only the solution with the lowest cost within each family is kept. The similarity criterion is based on the general direction of the solutions, which corresponds to the main direction of the back‐and‐forth trajectories, that is, the ones most frequently used inside the field polygon. If the field polygon is divided into subpolygons, the general direction is computed for each subpolygon. Therefore, two solutions are considered similar, and belonging to the same family, if they have the same general direction(s). After applying the similarity criterion and keeping only one optimal trajectory per family, the best solution of each family is presented to the user, and the most optimal solution among them is highlighted. The number of families is limited to the number of possible general directions, which corresponds to the number of borders of the field.

5 | RESULTS AND DISCUSSION

5.1 | Experiment

This approach was implemented in a program written in C++ that includes a GUI to set the input variables and visualize the generated solutions. To accelerate the computations, all the processes can run in parallel thanks to an implementation using OpenMP (n.d.). The program was run on an Intel Xeon W‐2135 CPU @ 3.70 GHz× 12 with 32 GB RAM.

A collection of 30 fields from the real world were chosen to evaluate the proposed approach. These fields range in area from 1.83 to 13.20 ha. Twenty fields have a simple shape for which no field decomposition was required, while 10 fields have a complex shape for which at least two different dividing lines were provided to try different field decompositions. To extract the data of these fields, the annotation tool of Géoportail (n.d.) was used. At least one access segment and two entrances were considered for each field.

The algorithm was run on each field with the variety of given dividing lines and entrances. For each field, we obtained several families of solutions, one best path for each family, one of them being the most optimal solution overall. All the best paths were compared with the ground truth, by visually comparing the results with the reference satellite image of the field, where the tracks are visible. Among the best solutions, the one found as having the best visual similarity with the reference satellite image is referred to as the most similar solution. The general directions of back-and-forth moves as well as how a field is divided into subfields were used as the similarity criterion. We assumed the path was chosen by the farmer who is an expert and is completely familiar with the field. Although it was relatively straightforward to delineate the headlands and the general directions of back‐and‐forth moves from the satellite images, determining the parameters of the vehicle and the implement, or the maximum coverage rate and overlap from these images only was

almost impossible. These parameters were guessed at best, as average settings, and similar for all fields. The parameters of our approach are given in Table 1.

To avoid weighing down this section, we give information about the complete data set and detailed results as appendices, and present here the average results and illustration on a subset of fields to highlight some interesting properties. The appendices contain for each field of the complete data set, a link to its data in the online application of Géoportail (n.d.), the coordinates of a point inside the field, figures illustrating the shape, entrances and access segments (see Section A.1). The numerical results as well as illustrations are, respectively, provided in Sections A.2 and A.3.

5.2 | Analysis of the results

The average results of the evaluation are summarized in Table 2. According to these statistics, for simple fields our approach was able to achieve a coverage rate of 98.69% while limiting the overlap to 3.00% on average. For complex fields the average coverage rate was 98.23% while the average overlap was limited to 3.09%. This accomplishment is mainly due to the capability of our approach to cover the headlands and deal with curved edges.

For 85% of simple fields, the most optimal solutions and the solution most similar to the satellite images were the same. For the other 15% of cases, the most similar solution was found by our 12 | **I**A/II EV

approach, but not considered as being the most optimal according to the predefined criteria.

For complex fields, 70% of the most optimal solutions were identical to the most similar to the satellite images. In 10% of the cases, the most similar solution was also found by our approach, but not considered as being the most optimal. For the remaining 20%, no similar solution was found. We identified two possible reasons. First, as previously mentioned, we guessed the parameters at best. Perhaps the different values we imposed for the thresholds and the vehicle parameters were not the ones used by the farmer. Adjusting them, for instance, decreasing the coverage threshold Δ*cov* and/or increasing the global overlap threshold Δ*global*, may lead to more solutions and consequently increase the possibility of finding the most similar solution. Second, some constraints or preferences may be considered by the farmer that was not applied in our approach. For instance, the farmer may have used visual clues to help working the land which may have had an influence on the choice of the trajectories, while we did not consider this as a useful factor for a robot.

As previously mentioned, the total number of explorations for a field depends on the number of selected entrances and the number of provided dividing lines. Therefore, for each field several explorations were performed. Consequently, in Table 2, single exploration time contains the average and standard deviation over all explorations performed on all simple and complex fields.

In the following, we illustrate the results on a sample of six fields extracted from the data set: four simple and two complex fields. The name of each sample corresponds to its original name in the data set provided in the appendices. The shapes and input data of the six fields are shown in Figure 5. Each field is represented by a set of counterclockwise ordered points. For the complex fields, respectively, two and three dividing lines are provided and shown in brown. Table 3 contains a link to the data of these fields in the web application of Géoportail (n.d.) as well as the coordinates of a point inside the field.

Figure 6 illustrates the results obtained on the six fields, and Table 4 summarizes the numerical results. As illustrated in the figure, our approach not only successfully covered unworked areas caused by half‐turns and gaps, but also intelligently selected the headlands to perform half-turns. Figure 6f illustrates the capacity of our approach to deal with curved trajectories within headlands.

For complex fields, our approach was not only capable of finding the most optimal solution but also determined which dividing line leads to a better field decomposition. The results generated for the complex fields are represented in Figure $6j$, I, m.

The generation of the solution space for Fields C4 and C2 took almost 47 and 10 min, respectively. Indeed for these fields, respectively, 9 and 12 successive explorations had to be performed to take into account all the combinations of entries and dividing lines.

TABLE 2 Numerical results of the evaluation.

FIGURE 5 Sample of six fields from the data set. A field polygon is represented by green and black line segments where green segments are accessible edges of the field. Dividing lines are represented in brown. Entrances are represented by red arrows. (a) Field S6—2.24 ha, (b) Field S7—4. 58 ha, (c) Field S8—4.22 ha, (d) Field S9—2.55 ha, (e) Field C4—6.25 ha, and (f) Field C2—2.21 ha. [Color figure can be viewed at wileyonlinelibrary.com]

TABLE 3 Links to the sample fields from the data set in Géoportail (n.d.) and coordinates of a point inside the field.

Field	S6		S8	S9	C4	
Link	bit.lv/3WGTfER	bit.lv/3DP8vaG	bit.lv/3NLmOJf	bit.lv/3EeTvUo	bit.lv/3E3I8OK	bit.ly/3zZK1dg
Lon/Lat	7.4311°/48.8245°	2.4845°/50.3106°	7.5924°/48.831°	7.4641°/48.8146°	3.1021°/48.2449°	2.7067°/50.3336°

Abbreviations: Lat, latitude; Lon, longitude.

FIGURE 6 Obtained results on six fields from the data set and their reference satellite image. Black arrows indicate where the robot enters and exits. (a) S6-most optimal solution, (b) S6-most similar solution, (c) S6-satellite image, (d) S7-most optimal and similar solution, (e) S7satellite image, (f) S8—most optimal and similar solution, (g) S8—satellite image, (h) S9—most optimal and similar solution, (i) S9—satellite image, (j) C4—most optimal solution, (k) C4—satellite image, (l) C2—most optimal solution, (m) C2—most similar solution, and (n) C2—satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

FIGURE 6 Continued

TABLE 4 Numerical results of six fields from the data set.

Note: S_{cov}, S_{ovl}, S_{nwd}, S_{otm}, and f are computed by Equations (1), (2), (5), (4), and (6), respectively. The most optimal and most similar solutions are the same for Fields S7, S8, S9, and C4.

Computing in a preliminary step a smart polygon decomposition adapted to the agricultural use case, that considers not only the geometry of the field but also for instance the inclination, could avoid unnecessary explorations and speed up the process for complex fields.

As illustrated in Figure $6j,k,l$, after covering the main part and some parts of the headlands of the first subfield, the path goes to the second subfield and covers it entirely. Finally it comes again in the first subfield and covers its remaining headlands and exits the field. This kind of solution cannot be found in classic approaches that consist of two sequential steps (CPP and AVRP). This highlights the interest of our one‐step approach. The following sections highlight some other interesting properties of the approach.

5.2.1 | Interest of grouping solutions into families

Figure 7 illustrates the most optimal solution from three different families for Field S6. Table 5 summarizes the numerical results for each solution. As can be observed, the difference between the results for these families is rather small. However, as illustrated in Figure 7 the solutions look completely different in terms of their general direction. Two of them have similar entry and exit, while the first one

uses a different exit. This illustrates the interest of clustering the results into different families to identify and present a variety of good solutions to the farmer.

5.2.2 | Benefit of multiple entrances

Table 6 summarizes the numerical result for each entrance of Field S9 separately. The most optimal solution was through *E*1. Considering *E*² as the entrance, our approach was also capable to find some acceptable results. However they were not as good as the one found while considering E_1 . That means, taking into account more entrances enhances the probability of finding a better result. However it also increases the exploration time. In this specific case, taking E_1 into account in addition to E_2 increased the coverage rate by 0.71% and nearly doubled the exploration time.

5.2.3 | Impact of field accessibility

Figure 8 illustrates the most optimal solutions for two scenarios on Field S7: in the first one the field is only accessible from its upper

FIGURE 7 Most optimal solution for different families for Field S6. Black arrows indicate where the robot enters and exits. (a) S6-first family, (b) S6—second family, and (c) S6—third family. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

Note: S_{cov} , S_{ovl} , S_{nwd} , S_{otm} , and f are computed by Equations (1), (2), (5), (4), and (6), respectively.

TABLE 6 Numerical results on Field S9 for each of its entrances.

		Exploration				Similarity check and selection of optimal solutions				
Field	Entrance	Solutions	Time (s)	$S_{\text{cov}} * W_{\text{cov}}$	$S_{ovl} * W_{ovl}$	$S_{nwd} * W_{nwd}$	$S_{\text{otm}} * W_{\text{otm}}$		Coverage (%)	Overlap (%)
S9	Ľ۱.	168	39.79	0.000	0.099	0.073	0.085	0.256	97.77	4.87
S ₉	È۵	18	35.69	0.558	0.022	0.000	0.000	0.580	97.06	3.09

FIGURE 8 Most optimal solutions for Field S7 while considering it is only accessible from its upper edge (a) or from all its edges (b). Black arrows indicate where the robot enters and exits. (a) S7—one accessible edge and (b) S7—all edges are accessible. [Color figure can be viewed at wileyonlinelibrary.com]

TABLE 7 Comparison of results over Field S7 while considering it is accessible only by its upper edge (real-world scenario) and all its edges.

		Exploration			Similarity check and selection of optimal solutions		
Field	Accessible edges	Solutions	time (s)	time (s)	Coverage (%)	Overlap (%)	
	1 Edge	2511	22.32	0.07	98.58	1.80	
S7	All edges	10.137	35.4729	0.30	98.61	0.88	

FIGURE 9 Most optimal solutions for Field S7 when *γoff* was set to 2m. Black arrows indicate where the robot enters and exits. [Color figure can be viewed at wileyonlinelibrary.com]

edge, which corresponds to the real‐world scenario, and in the second one it is accessible from all its edges, which is an oversimplification. Table 7 summarizes the numerical results for each scenario. With the second scenario, we obtained a better solution according to the defined criteria. However, in the real world this solution would not be feasible, as the robot would exit to the neighbor's field at the bottom. Therefore, an inaccurate description of the accessibility of a field may lead to an unfeasible result. In some cases, it may damage the robot or the neighbor's field.

5.2.4 | Forward and reverse half-turns

To demonstrate our method's ability to perform half‐turns other than U-turns, one last test was performed on Field S7 where all parameters remained the same except *γoff* that was set to 2m. As

illustrated in Figure 9, our approach chose to perform half‐turns using reverse moves on the left side of the field, while in the right side no reverse moves were required. Table 8 summarizes the numerical results of this test.

5.2.5 | Discussion on comparative results

In this kind of study it is difficult, if not impossible, to compare our approach to previous approaches from the literature due to the very different nature of the approaches, the variety of constraints taken into account or not, and the lack of standardized data set. To emphasize this challenge, in this section we present an attempt to compare our approach with an open‐source algorithm named Fields2Cover (F2C) and proposed by Mier et al. (2023). The inputs of F2C are the field polygon, the width of headlands (*p* ∗w), the minimum turning radius of the robot (*γoff*), and one single objective function to choose among three suggestions: minimizing the total path length, minimizing the number of half-turns in headlands and maximizing the coverage rate. In this comparison, minimizing the number of half‐turns in headlands was chosen as the objective function. Let us note that our algorithm accounts for these three constraints simultaneously, under different names. Let us also note that F2C does not cover the headlands themselves. We ran F2C on six fields (S6, S7, S8, S9, C2, and C4) and extracted the computation times, number of half‐turns, coverage, and overlap.

An example of visual comparison between the results of our approach and F2C is provided in Figure 10. As for numerical results,

TABLE 8 Numerical results of Field S7 while *γoff* was set to 2m.

	Exploration				Similarity check and selection of optimal solutions						
Field	Total	Solutions	Time (s)		Time (s) $S_{cov} * W_{cov}$	$S_{ovl} * W_{ovl}$	$S_{nwd} * W_{nwd}$	$S_{\text{otm}} * W_{\text{otm}}$		Coverage (%)	Overlap (%)
		135	7.70	0.02	0.002	0.062	0.059	0.065	0.187	98.46	2.96

Note: S_{cov} , S_{ovl} , S_{nwd} , S_{otm} , and f are computed by Equations (1), (2), (5), (4), and (6), respectively.

FIGURE 10 Result obtained on Field S6 from the data set using our approach and F2C. (a) S6-our approach and (b) S6-F2C. [Color figure can be viewed at wileyonlinelibrary.com]

our approach outperformed F2C in terms of coverage rate by over 12.42% on average. On the contrary, F2C performed better in terms of overlap area, with on average 3.23% overlap for our methods against 0% for F2C. The computational time of F2C was also extremely low in comparison to our approach, with an average of 1.52*s* for F2C against 624.6*s* for ours. It also slightly outperformed our approach in terms of the number of half‐turns (1.5 less half‐turns on average).

However, these figures have to be counterbalanced by the fact that F2C does not provide any headland coverage, as can be seen in the example of Figure 10. Most of our overlaps and many extra turns are due to headland coverage, while no headland coverage means no overlaps, fewer turns, and ultimately less computational time. Similarly, our method accounting for headland naturally provides a better coverage. Our method also aligned the main direction of work with one of the borders of the field. It was not the case with F2C, which may also explain in part the lower coverage by F2C. Additionally, the solution proposed by F2C will anyway require to cover an additional circular headland which will in the end increase the overlaps. Our method already includes the headland coverage which is not fully circular and requires less work. Finally, the F2C method did not take into account the transition states of the implementation. In the example of Figure 10b, when using an implement in contact with the ground, the upper trajectory is too short and could not be achieved in practice due to the minimal trajectory length necessary to activate and deactivate the implement. This would cause again a loss of coverage. These examples demonstrate the difficulty to compare the various approaches.

This is why in this study we preferred to visually compare our results to a ground truth made of satellite images. However, this choice also has some limitations, mostly due to the variety of the machinery, and the difference between the preferences and habits of

a human operator and the constraints applicable to a robot. Nevertheless, we could demonstrate in this paper that our approach can provide complete optimal paths, including headlands, comparable to the current practice, applicable to a large number of configurations and use cases, completely parameterizable, and still in a reasonable time.

6 | CONCLUSION AND PERSPECTIVES

In this paper, a novel CCPP approach based on tree exploration was proposed to generate an optimal path that starts from an entrance location, covers the field and the headlands and ends on one of the accessible edges of the field. To accomplish this task, first, one or several explorations were conducted while considering multiple entrances and hard constraints. If some dividing lines were also provided, a combination of entrances and dividing lines were considered in the exploration. The result of this exploration was a solution space containing all possible solutions. Finally a similarity check and selection of optimal solutions were applied to extract a variety of most optimal paths without redundancies, by minimizing a weighted average cost function of the soft constraints. The goal of this approach was to maximize the worked area while minimizing the overlaps, the nonworking path length, and the traveled time.

This study revealed that considering multiple entrances could lead to better solutions. It was also shown that considering multiple dividing lines for fields with a complex shape increased the probability of finding a better solution. It also showed how critical it was to consider the actual accessibility of the field.

Currently, our approach is able to take dividing lines as input to decompose complex field polygons into simpler subpolygons. It tries multiple dividing lines to find the one that leads to the optimal path.

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However, this process could be expensive in terms of computation time. One of our perspectives is to develop an intelligent field decomposition method that can determine whether a field needs to be decomposed, and if so, propose dividing lines while taking into account both the shape and the inclination of the field.

The output of our algorithm, a generated path, is meant to be sent to an autonomous agricultural robot to be executed. Such a robot needs other subsystems to achieve the task, such as accurate positioning, motion control, and perception system using sensors. Our group has recently developed an autonomous robot integrating such features Vieira et al. (2021, 2022). One of our perspectives is to test and validate the whole integrated system including our approach, by conducting field experiments in the near future.

Due to the varied nature of the previous approaches, the variety of field operations and constraints taken into consideration, and lack of standardized data set, it could be difficult to compare an agricultural CCPP approach with previous approaches. It could be even more difficult if the output or implementation of previous approaches is not publicly available. Therefore, in further studies, we are going to provide a data set containing all information to evaluate both 2D and 3D CCPP methods, as well as a general data structure for saving the output of a CCPP approach, to facilitate a more accurate comparison and evaluation of different approaches.

There is a variety of agricultural machinery, depending on the type of operations or the nature and geometry of the field, with different parameters and requirements. A thorough statistical analysis of the effect of each physical parameter is something that is beyond the scope of this paper, but that would be interesting to study in the future, with perhaps the potential to bring suggestions for the design of future machinery.

Currently, the proposed approach does not account for inclinations and obstacles. Most often, modern robots include sensors to avoid moving obstacles, that could also be used to deal with static obstacles. However, this could cause some unwanted unworked areas and overlaps. As a result, our another perspective is to consider the static obstacles inside a field beforehand, to avoid them with a more optimal route. One another perspective is to consider the inclination and the elevation across the field to correct overlaps and skips caused by the projection of a 3D surface to a 2D plane. This information could also be integrated as a new soft constraint to minimize the soil erosion and/or the energy consumption. Other perspectives include considering one or several mobile service units on the accessible edges of the field, and extension to a multirobot approach.

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DATA AVAILABILITY STATEMENT

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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APPENDIX A

A.1 | Data set

See Figures A1 and A2.

FIGURE A1 Representation of simple fields. A field polygon is represented by green and black line segments where green segments are accessible edges of the field. Entrances are represented by red arrows. (a) Field S1—3.34 ha, (b) Field S2—5.09 ha, (c) Field S3—7.23 ha, (d) Field S4—8.23 ha, (e) Field S5—4.39 ha, (f) Field S6—2.24 ha, (g) Field S7—4.58 ha, (h) Field S8—4.22 ha, (i) Field S9—2.55 ha, (j) Field S10—3.87 ha, (k) Field S11—7.85 ha, (l) Field S12—1.89 ha, (m) Field S13—5.81 ha, (n) Field S14—1.95 ha, (o) Field S15—13.20 ha, (p) Field S16—3.59 ha, (q) Field S17—3.44 ha, (r) Field S18—1.83 ha, (s) Field S19—7.68 ha, and (t) Field S20—4.34 ha. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

FIGURE A2 Representation of complex fields. A field polygon is represented by green and black line segments where green segments are accessible edges of the field. Dividing lines are represented in brown. Entrances are represented by red arrows. (a) Field C1—3.09 ha, (b) Field C2—2.21 ha, (c) Field C3—4.50 ha, (d) Field C4—6.18 ha, (e) Field C5—6.25 ha, (f) Field C6—10.41 ha, (g) Field C7—3.80 ha, (h) Field C8—3.58 ha, (i) Field C9-2.69 ha, and (j) Field C10-4.15 ha. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

See Tables A1 and A2.

TABLE A1 Links to simple fields data and coordinates of a point inside the field.

Field	S ₁	S ₂	S ₃	S4	S ₅
Link	bit.ly/3FYtuKu	bit.ly/3WGAyRI	bit.ly/3zX1vqJ	bit.ly/3DJL0Pl	bit.ly/3htb8H3
Lon/Lat	7.435°/48.7732°	7.474°/48.7825°	2.9205°/49.8115°	1.6713°/47.9864°	3.3216°/50.6623°
Field	S ₆	S7	S ₈	S9	S ₁₀
Link	bit.ly/3WGTfER	bit.ly/3DP8vqG	bit.ly/3NLmQJf	bit.ly/3EeTvUo	bit.ly/3UOyTrv
Lon/Lat	7.4311°/48.8245°	2.4845°/50.3106°	7.5924°/48.831°	7.4641°/48.8146°	1.3491°/48.012°
Field	S ₁₁	S ₁₂	S ₁₃	S14	S ₁₅
Link	bit.ly/3zW7v30	bit.ly/3UMC6I3	bit.ly/3TjkOkA	bit.ly/3UAmdo0	bit.ly/3GpidXZ
Lon/Lat	$3.4701^{\circ}/46.652^{\circ}$	7.5742°/48.8071°	$3.578^{\circ}/46.7016^{\circ}$	7.4269°/48.8194°	3.5611°/46.6875°
Field	S16	S17	S18	S19	S ₂₀
Link	bit.ly/3tcGhRN	bit.ly/3zW26sE	bit.ly/3Trsqlq	bit.ly/3DWHgKJ	bit.ly/3NN8pnT
Lon/Lat	2.5127°/48.2645°	2.6443°/48.2546°	7.9196°/48.9513°	2.1269°/46.8124°	1.5874°/47.1346°

Abbreviations: Lat, latitude; Lon, longitude.

TABLE A2 Links to complex fields data and coordinates of a point inside the field.

Abbreviations: Lat, latitude; Lon, longitude.

A.2 | Numerical results

See Tables A3 and A4.

TABLE A4 Numerical results obtained for simple fields.

A.3 | Illustrative results A.3.1 | Field S1 See Figure A3.

FIGURE A3 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color

Gap trajectory
Turns and half tu STRAIGHT_ON Worked area
Overlap area

figure can be viewed at wileyonlinelibrary.com]

See Figure A4. (a)

A.3.2 | Field S2

FIGURE A4 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

A.3.3 | Field S3 See Figure A5.

FIGURE A5 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

A.3.4 | Field S4 See Figure A6. (a) (b)

Gap trajectory	
Turns and half turns A	
STRAIGHT_ON	
Norked area	
Overlap area	

FIGURE A6 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

A.3.5 | Field S5

See Figure A7.

A.3.6 | Field S6 See Figure A8.

FIGURE A8 Black arrows indicate where the robot enters and exits. (a) Most optimal result, (b) most similar result, and (c) satellite image. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

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A.3.7 | Field S 7 See Figure A9 .

FIGURE A9 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

 (b) (a) \mathcal{H}

A.3.8 | Field S8

See Figure A10.

FIGURE A10 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) Satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

A.3.9 | Field S9

See Figure A11.

Gap trajectory Turns and half turns	
STRAIGHT_ON	
Worked area	
Overlap area	

FIGURE A11 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) Satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

A.3.10 | Field S10 See Figure A12.

 (b)

FIGURE A12 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) Satellite image. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

A.3.11 | Field S11

See Figure A13.

Gap trajectory	
Turns and half turns	
STRAIGHT_ON	
Worked area	
Overlap area	

FIGURE A13 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at wileyonlinelibrary.com] FIGURE A14 Black arrows indicate where the robot enters and

A.3.12 | Field S12 See Figure A14.

(a)

Gap trajectory Turns and half turns	
STRAIGHT_ON	
Worked area	
Overlap area	

exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

A.3.13 | Field S13 See Figure A15. (a)

Gap trajectory	
Turns and half turns	
STRAIGHT_ON	
Worked area	
Overlap area	

FIGURE A15 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

A.3.14 | Field S14 See Figure A16.

 (b)

FIGURE A16 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

A.3.15 | Field S15

See Figure A17.

Gap trajectory	
Turns and half turns	
STRAIGHT_ON	
Worked area	
Overlap area	

FIGURE A17 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

A.3.16 | Field S16

FIGURE A18 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

Gap trajectory	
Turns and half turns	
STRAIGHT_ON	
Worked area	
Overlap area	

FIGURE A19 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

FIGURE A20 Black arrows indicate where the robot enters and exits. (a) Most optimal result, (b) most similar result, and (c) satellite image. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

A.3.19 | Field S19 See Figure A21.

A.3.20 | Field S20 See Figure A22.

FIGURE A22 Black arrows indicate where the robot enters and

exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

FIGURE A21 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

A.3.21 | Field C1

See Figure A23.

FIGURE A23 Black arrows indicate where the robot enters and exits. (a) Most optimal result and (b) satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

FIGURE A24 Black arrows indicate where the robot enters and exits. (a) Most optimal result, (b) most similar result, and (c) satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

 (c)

A.3.23 | Field C3

See Figure A25.

A.3.24 | Field C4

Gap trajectory Turns and half turn: STRAIGHT_ON Worked area Overlap area

FIGURE A25 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color

figure can be viewed at wileyonlinelibrary.com]

FIGURE A26 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

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A.3.25 | Field C 5 See Figure A27 .

FIGURE A27 Black arrows indicate where the robot enters and exits. (a) Most optimal result and (b) satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

A.3.26 | Field C6

See Figure A28.

FIGURE A28 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

A.3.27 | Field C7 See Figure A29. (a)

 (b)

Turns and half turns

FIGURE A29 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

A.3.28 | Field C8 See Figure A30.

 (a) (b)

> Gap trajectory
Turns and half t œ Turns and nair to
STRAIGHT_ON
Worked area
Overlap area

FIGURE A30 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at wileyonlinelibrary.com]

A.3.29 | Field C9 See Figure A31.

 (b)

FIGURE A31 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at [wileyonlinelibrary.com\]](http://wileyonlinelibrary.com)

A.3.30 | Field C10 See Figure A32.

FIGURE A32 Black arrows indicate where the robot enters and exits. (a) Most optimal and similar result and (b) satellite image. [Color figure can be viewed at wileyonlinelibrary.com]