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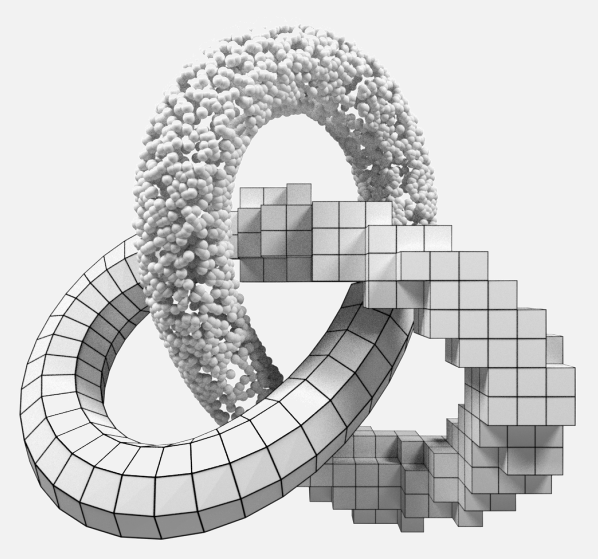
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Jerboa

Inference of geometric modeling operations

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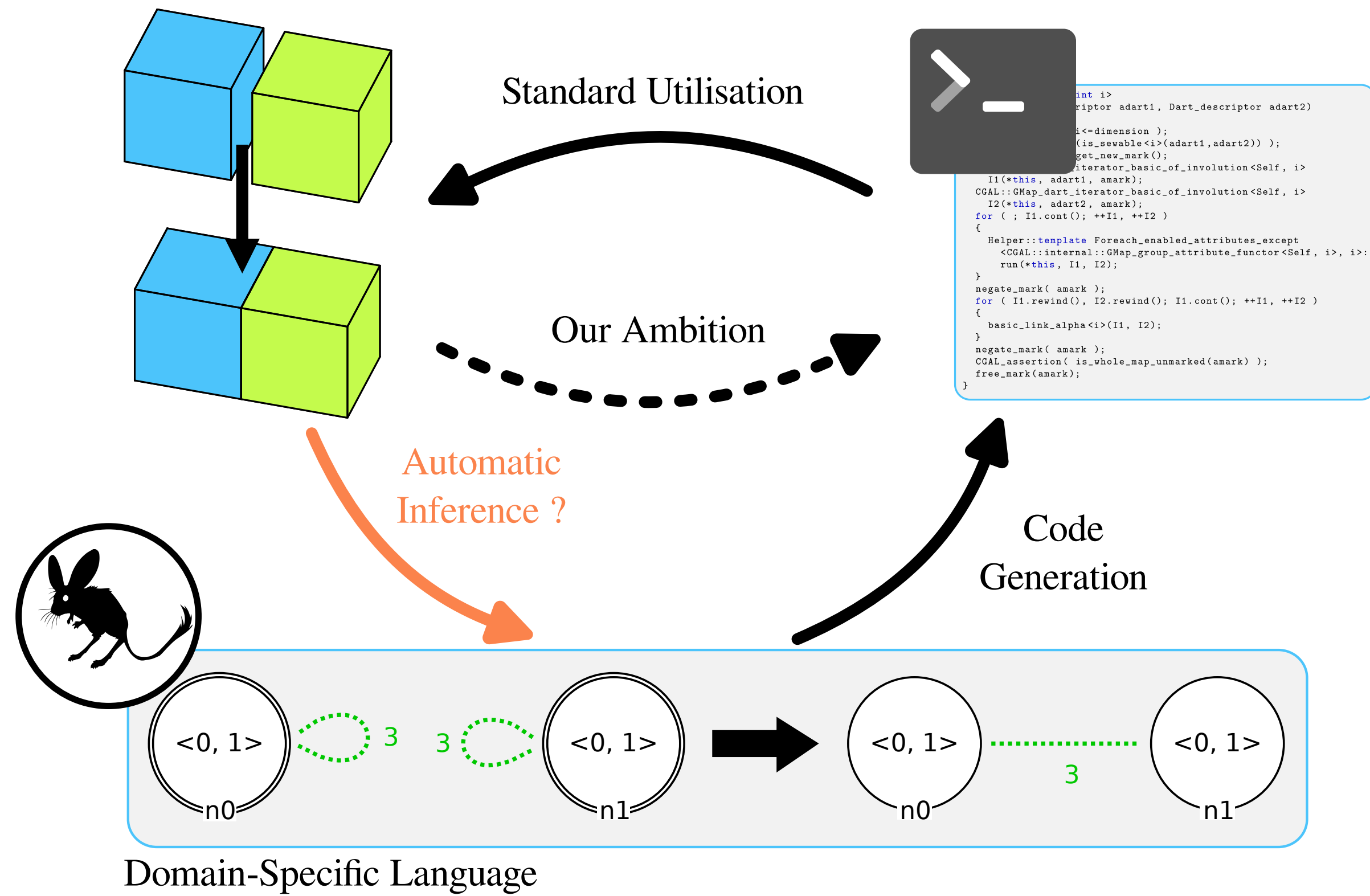
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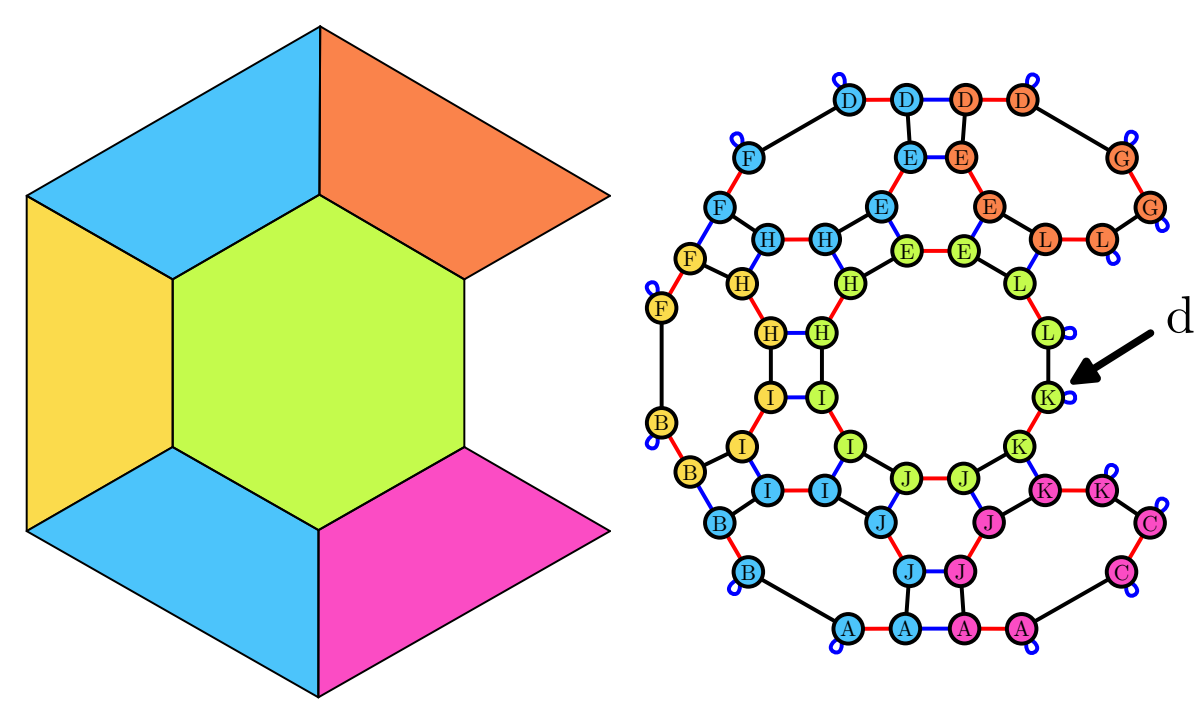
1. Problematic and motivating context

Conceiving an operation can be a difficult task even though it may be easily described from an example. We propose a new paradigm exploiting a **domain specific language** as a guideline to retrieve an operation from an object before and after modification.



2. Object representation: embedded generalized maps

Topology-based geometric modeling uses combinatorial structures to encode the decomposition of an object's topological cells (vertices, edges, faces ...) which is embedded in a geometric space to store additional informations.



Generalized maps (Gmaps) [2] built as graphs:

- graph: incidence relations between the cells
- node attributes: geometric embedding values

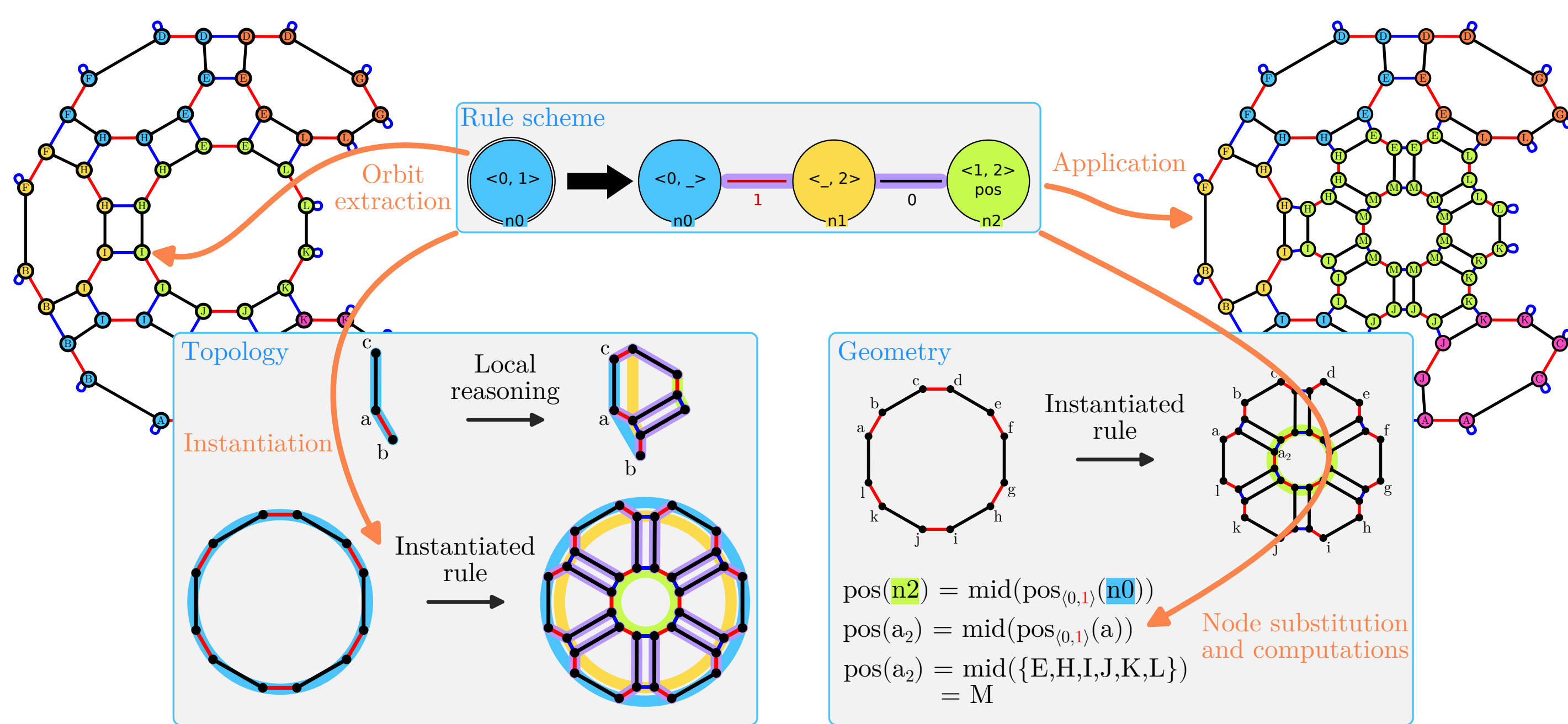
Orbits encode the object's topological cells as subgraphs:

- positions on vertices (orbits $\langle 1, 2 \rangle$).
- colors on faces (orbits $\langle 0, 1 \rangle$).

Color legend: 0, 1, 2.

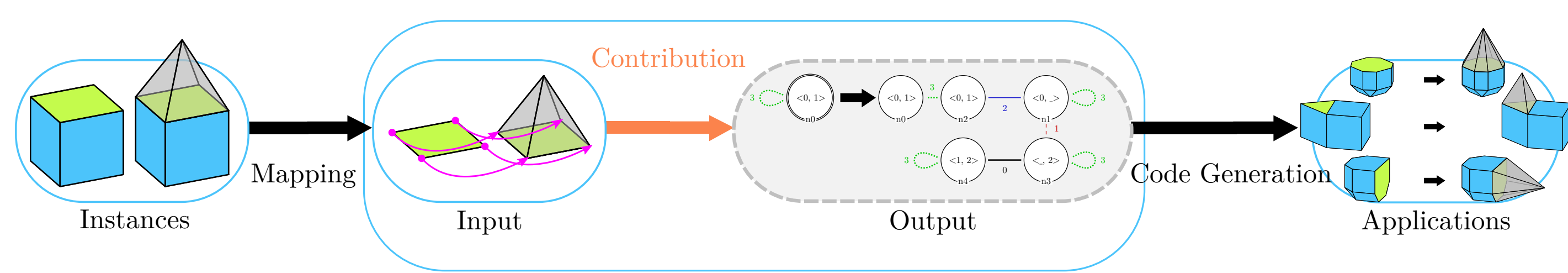
3. Modeling operations formalized as graph transformation [5, 1]

Graph transformation [3] extends rewriting to non-linear structures, allowing to formalize modifications of embedded Gmaps: a graph product extends rules to abstract over the underlying topology while algebraic data types and algebra morphisms describe geometric modifications.



4. Method and global workflow

General idea: reverse the instantiation and application process.

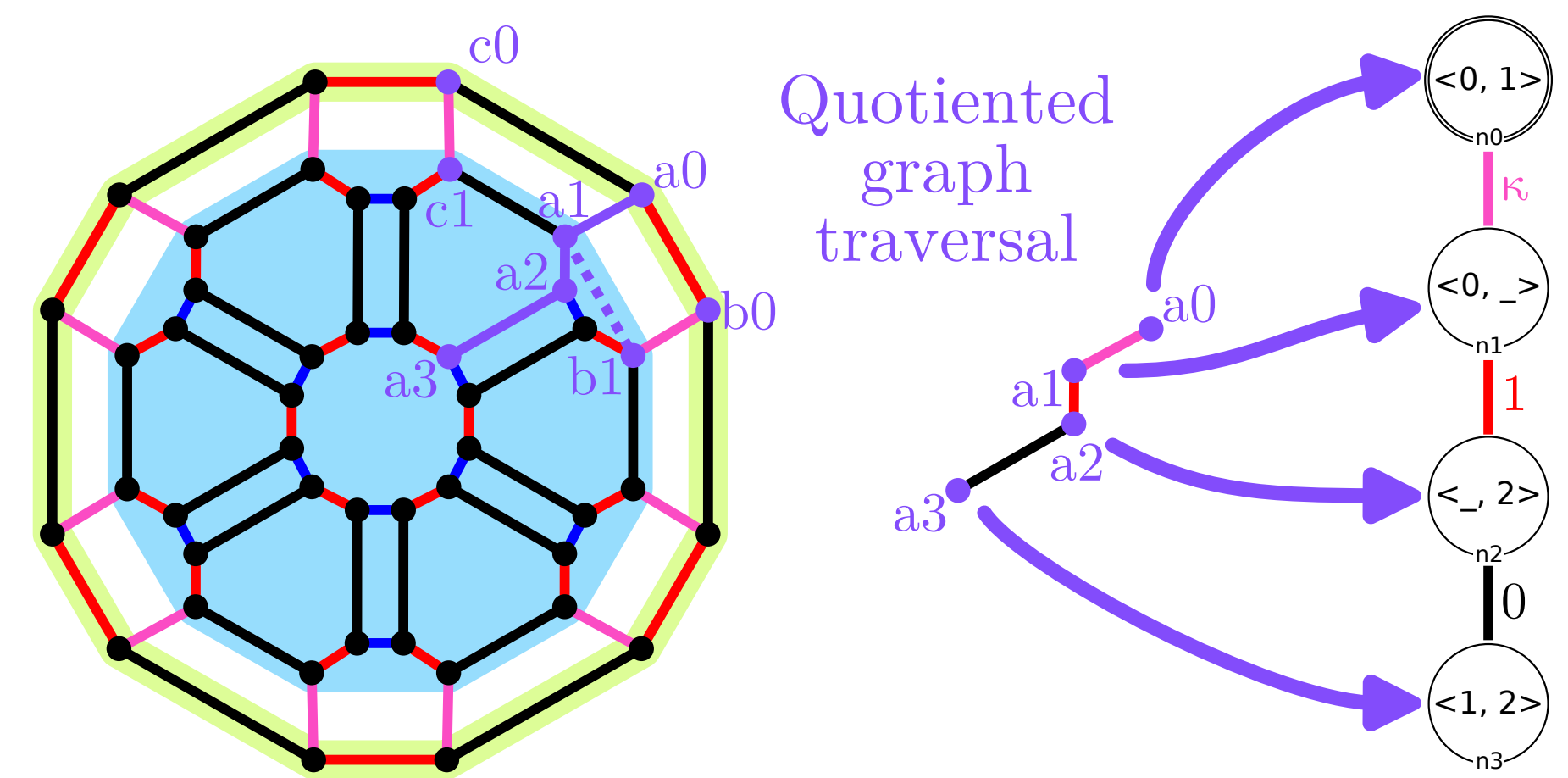


5. Topological folding algorithm [4]

Input: two partial Gmaps with preservation relation (arcs κ), an orbit type $\langle o \rangle$ and a dart a .

Output: a graph \mathcal{S} encoding the rule on $\langle o \rangle$, given that the operation is applied to a .

General idea: quotiented graph traversal algorithm iteratively folding nodes and arcs.



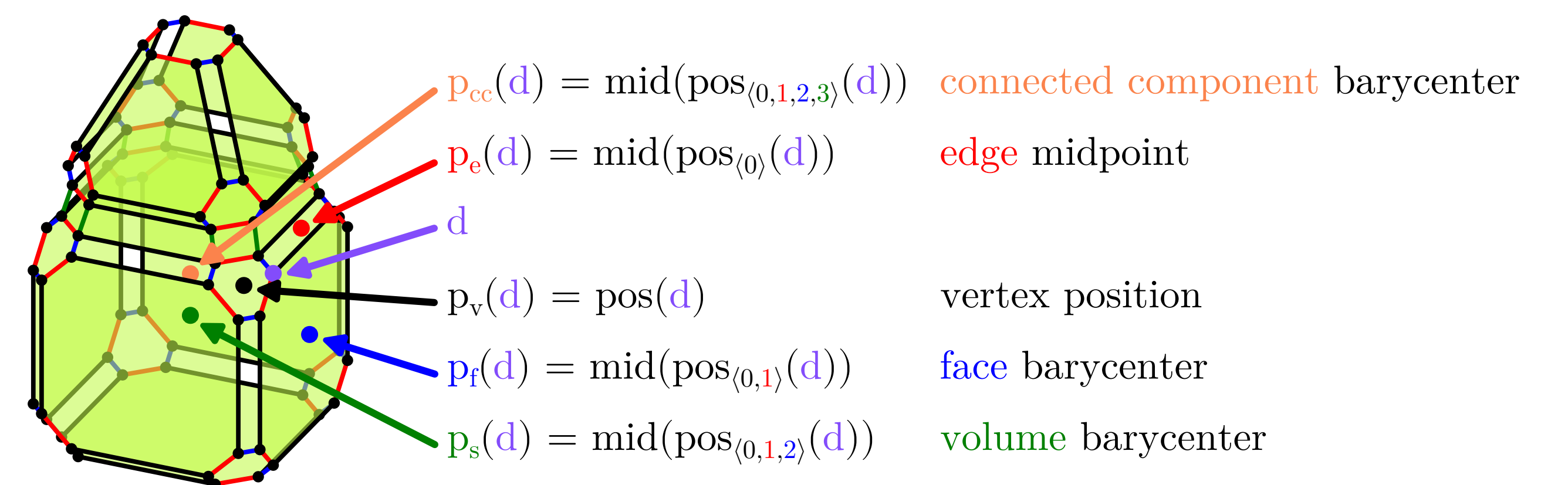
Color legend: 0, 1, 2, κ . Before instance in blue, after instance in green.

6. Retrieving geometric expressions: linear hypothesis

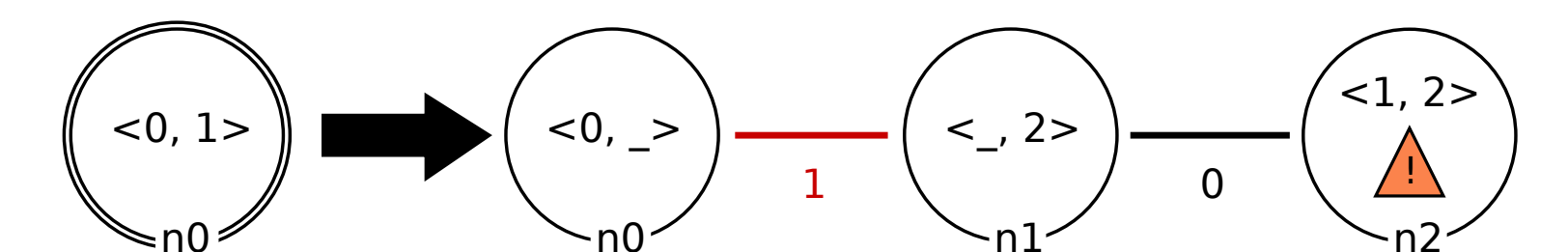
The output of the topological folding algorithm lacks expressions for the geometric computation.

Problem: Rules abstract topological cells meaning darts will share the same expression.

Solution: Values of interest that exploit the topology to express computations independently from the actual structure.



Triangulation operation:



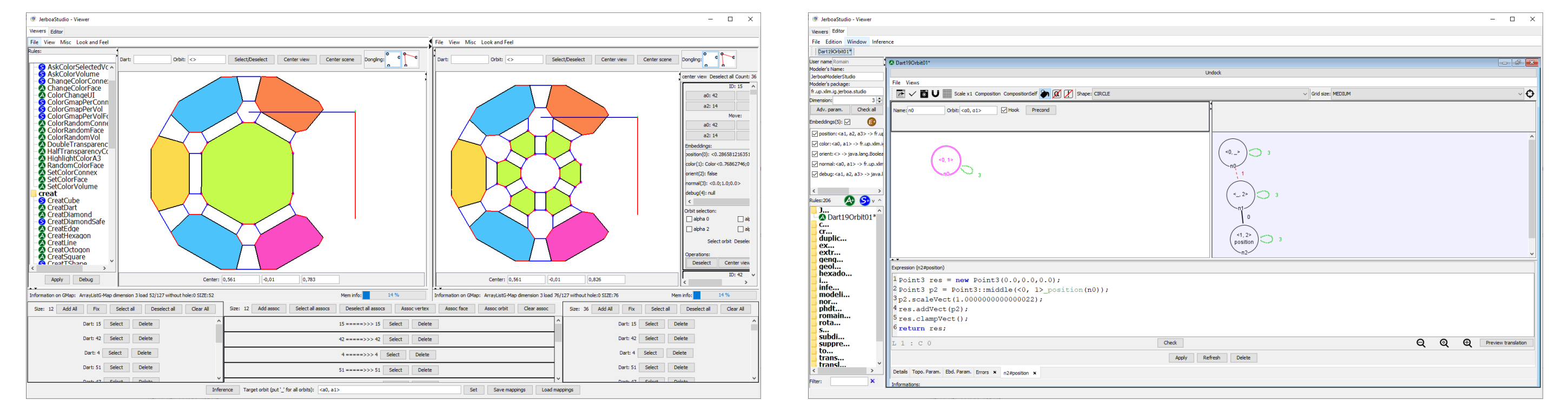
We obtain the following equation, which we solve as a constraint satisfaction problem.

$$\text{pos}(n_2) = \underbrace{w_v p_v(n_0)}_{\text{vertex}} + \underbrace{w_e p_e(n_0)}_{\text{edge}} + \underbrace{w_f p_f(n_0)}_{\text{face}} + \underbrace{w_s p_s(n_0)}_{\text{volume}} + \underbrace{w_{cc} p_{cc}(n_0)}_{\text{cc}} + t$$

Solution found: $w_f = 1.0$ with all other variables being zero.

7. JerboaStudio

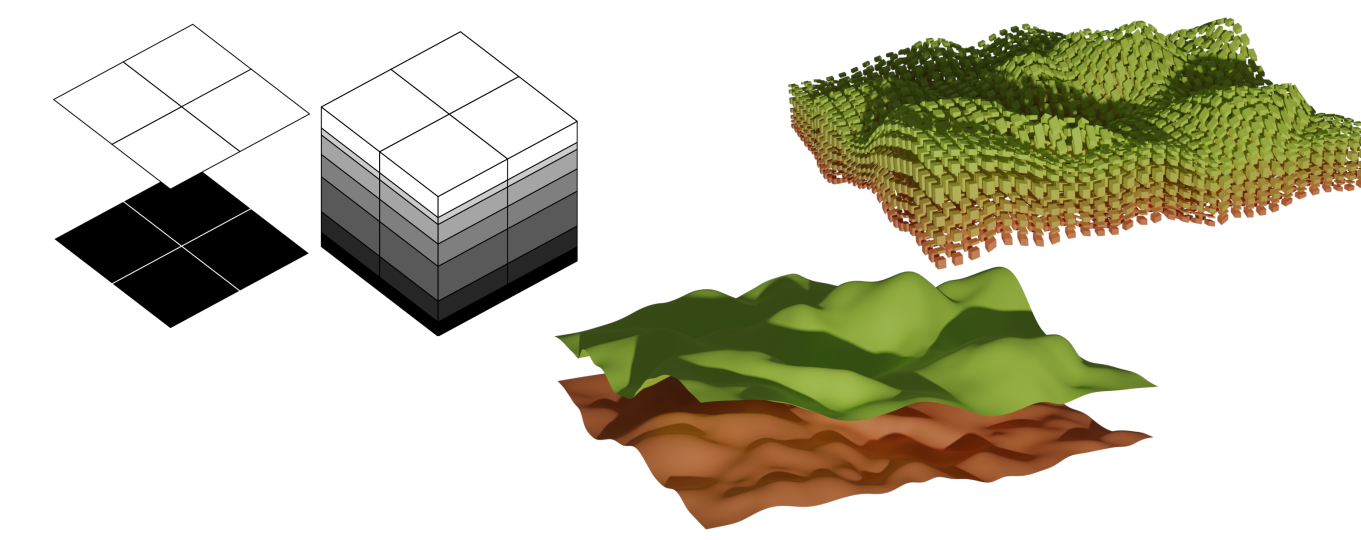
The **viewer** tab (left) contains both instances used for the inference while the **editor** tab (right) allows visualizing (and modifying) the inferred operations.



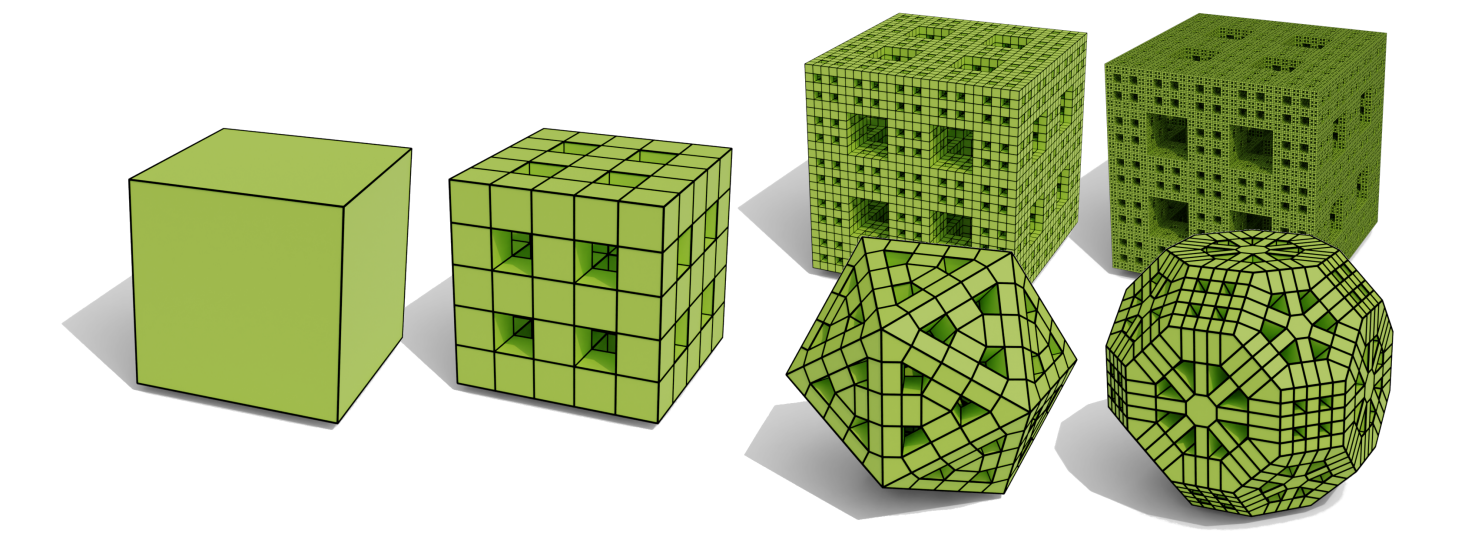
8. Results and conclusion

Main results: proof of correctness for topological folding algorithm [4], but some operations cannot be expressed directly in the language; retrieve computations with any embedding in a vectorial space by many cases remains out of the linear hypothesis.

Application to layering:



Menger (2, 2, 2) sponge [6]:



[1] A. Arnould, H. Belhaouari, T. Bellet, P. L. Gall, and R. Pascual. Preserving consistency in geometric modeling with graph transformations. *MSCS*, 2022.

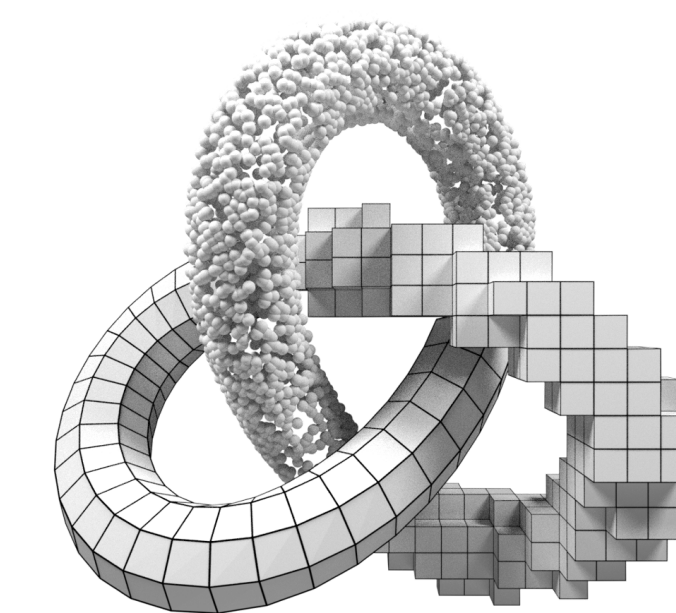
[2] G. Damiand and P. Lienhardt. *Combinatorial Maps: Efficient Data Structures for Computer Graphics and Image Processing*. CRC Press, 2014.

[3] R. Heckel and G. Taentzer. *Graph Transformation for Software Engineers*. Springer, 2020.

[4] R. Pascual, H. Belhaouari, A. Arnould, and P. Le Gall. Inferring topological operations on generalized maps: Application to subdivision schemes. *GVC*, 2022.

[5] R. Pascual, P. Le Gall, A. Arnould, and H. Belhaouari. Topological consistency preservation with graph transformation schemes. *SCP*, 2022.

[6] L. Richaume, E. Andres, G. Largeteau-Skapin, and R. Zrour. Unfolding Level 1 Menger Polycubes of Arbitrary Size With Help of Outer Faces. In *DGCI*, 2019.



GTMG : Groupe de Travail Modélisation Géométrique

La présentation de ces travaux a été primée lors des journées du GT en Mars 2022.