

Optimizing the strength of the Bourdon effect by varying the triangle arrangement

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4	Optimizing the Strength of the Bourdon Effect by Varying the
5	Triangle Arrangement
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15	

16 Abstract

17

18 The Bourdon illusion refers to the perceived bentness of the straight collinear edges when two 19 right-angled triangles are placed apex to apex. We studied this illusion using a cancellation 20 method. In the first of three experiments, we manipulated the apex angle, with six different 21 angles ranging from 4 to 45 degrees. Results indicated that the Bourdon illusion is strongest 22 when the angle is around 12° . In the second experiment, we compared four scalene triangles 23 with a right-angled triangle. The angular shift was most salient when the shape corresponded 24 to a right-angled triangle. In the third experiment, the patterns were created by varying the 25 size of one right-angled triangle while holding the size of the second right-angled triangle 26 constant. Results indicated that the Bourdon illusion was strongest when both right-angled 27 triangles were of equal size. Our data suggest that the Bourdon illusion depends critically 28 upon the specific arrangement of shapes in the display.

29 Keywords: Bourdon illusion, angle perception, shape perception, geometrical illusion

31 **1. Introduction**

The Bourdon illusion occurs when two right-angled triangles are placed apex to apex so that the sides opposite the hypotenuse are collinear (ABC in Fig. 1a). Under these conditions, this perfectly straight edge appears to bend in the same direction as the opposite edges (DBE in Fig. 1a). This effect is stronger in subjective contours than in real contours (Walker & Shank, 1987; Walker & Shank, 1988a, 1988b; Wenderoth, Criss, & van der Zwan, 1990).

37 This illusion was originally but briefly described by Bourdon (1902) in a horizontal 38 version. To our knowledge, he did not systematically study this effect, probably because it 39 was negligible in the original version. In the first experimental investigation of the Bourdon 40 illusion, Rozvany and Day (1980) showed that its strength depends critically on the 41 orientation of the pattern, with results indicating that the illusion is strongest when the whole 42 pattern is tilted about 22.5° from a vertical axis passing through its center (see Fig. 1b), and is 43 far weaker when the whole pattern is either vertical, or at an angle of 45° from the vertical 44 axis. Similar results have been found for different mirrored orientations (Verstijnen & van 45 Leewen, 1998). Studies of the Bourdon illusion have typically examined the stimulus 46 configuration that produces it. For example, the strongest illusion is produced when the internal apical angles are equal to 12.5° (see Fig. 1b) (Rozvany & Day, 1980). It should be 47 48 noted that the Bourdon illusion also occurs in haptic mode, with similar parameters (Day, 49 1990). Other findings suggest that the illusory effect increases when a small gap is inserted between the apices of the two right-angled triangles (Day, Mitchell, & Stecher, 1990; 50 51 Wenderoth & O'Connor, 1987a, 1987b).

The Bourdon illusion has been observed with a solid figure like that shown in Figure 1a, but the bentness effect persists when the right-angled triangles are formed by lines (Rozvany & Day, 1980). Its strength increases as the thickness of the lines increases, until it is similar to that of a solid figure (Walker & Shank, 1988a). The illusion tends to disappear

when the right-angled triangles are replaced by outlines of triangles where the short sides (AD and CE in Fig. 1a) are missing, resulting in a nonsolid figure (Rozvany & Day, 1980; Wenderoth & O'Connor, 1987a). This is consistent with the fact that a solid right-angled triangle displayed against a white background is needed to create the full illusion.

60 The impact of triangle orientation on the Bourdon illusion has been extensively tested, 61 with most researchers showing that a specific oblique orientation creates the strongest 62 illusion, and a horizontal or vertical orientation the weakest one (Rozvany & Day, 1980; 63 Verstijnen & van Leewen, 1998; Wenderoth & O'Connor, 1987a). However, although the 64 right-angled triangle is known to be an important contributor to the illusion, the impact of 65 triangle shape has not yet been systematically explored. We therefore conducted three 66 experiments in which the Bourdon illusion was studied with different triangle shapes. The aim 67 of the first experiment was to directly test the strength of the Bourdon illusion as a function of 68 apical angles. When the internal apical angle β (see Fig. 1b) increased, the shape changed 69 from a scalene triangle to an isosceles triangle. This involved the use of a cancellation task, 70 and was a partial replication of earlier findings. In the second experiment, we investigated the 71 strength of the Bourdon illusion using different scalene triangles. Here, the apical angle β did 72 not change, whereas the angle γ (right angle in the original version; see Figs 1b and 3) varied 73 from an acute to an obtuse angle. In the third and final experiment, we studied how the 74 strength of the Bourdon illusion varied when the size of one right-angled triangle was 75 manipulated, but that of the other right-angled triangle was held constant (see Fig. 5).

Figure 1 about here

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81 2. Experiment 1

82 2.1. Observers

We recruited 19 psychology undergraduates (age range: 18-25 years) from Rennes University as our observers. All had normal or corrected-to-normal visual acuity, and were naïve to the purpose of the experiment. Like the two subsequent experiments, Experiment 1 was conducted in accordance with the principles of the Declaration of Helsinki.

87

88 2.2. Apparatus

89 A PC was used to display the stimuli on a 22 in. CRT monitor (NEC MultiSync FP2141SB) 90 driven by a ViSaGe graphic board with a color resolution of 14 bits per gun (Cambridge 91 Research Systems, Rochester, United Kingdom). The experimental software was written to 92 generate the stimuli, control the stimulus presentation, and collect responses in MATLAB 7.9 (MathWorks, http://mathworks.com), using the CRS Toolbox extensions. The monitor was 93 94 calibrated using an OptiCal photometer with the calibration routines of Cambridge Research 95 Systems. Observers viewed the screen from a distance of 80 cm, with their head stabilized by 96 a chin rest. Both eyes were used for viewing. Participants used a Cedrus response box (RB-97 530) to record their responses. The experiment was performed in a dark room.

98

99 2.3. Stimuli

100 Observers viewed two right-angled triangles connected by their apices, similar to those shown 101 in Figure 1a. All the figures were dark (x = 0.30, y = 0.45; Y = 1.03 cd/m²), displayed against 102 a neutral gray background (x = 0.29, y = 0.32; Y = 60.32 cd/m²).

In accordance with previous studies (Rozvany & Day, 1980; Verstijnen & van
 Leeuwen, 1998), the figures were oriented at an angle of 22.5° from the vertical axis (see

105 angle α in Figs 1b and 1c), to maximize the Bourdon illusion. The stimuli were displayed in 106 the center of the screen. Each triangle had an AB/BC length of approximately 6.4°.

107 There were six values of angle β : 4°, 8°, 12°, 23°, 34° and 45° (see Fig. 1b). It should 108 be noted that the 12° angle formed a right-angled triangle similar to those used in previous 109 studies (Rozvany & Day, 1980; Verstijnen & van Leeuwen, 1998), whereas the 45° angle 110 formed an isosceles triangle.

111

112 2.4. Procedure

113 Prior to the experiment, observers familiarized themselves with the screen for 3 minutes. They 114 were then asked to simultaneously adjust two edges (AB and BC in Figure 1) in a series of 115 increments until they appeared collinear (cancellation task), by pressing the appropriate 116 buttons on a response box. The method was as follows: we determined a line (see the dashed 117 line in Fig. 1b) that ran perpendicular to the AC line and passed through point B (y = 0.404, 118 x+167.03). Participants could simultaneously adjust the edges (AB and BC) in small 119 increments (approximately 0.5 arcmin) in both directions defined by the dashed line. At the 120 beginning of each trial, the initial position of the apex coordinates (point B in Fig. 1) was 121 randomly picked from the line within the range of -5° to 5° .

122 This sequence was repeated until the observer deemed that the adjustment was 123 satisfactory and pressed the central button on the response box. There was then a 1-s pause 124 before a new trial started. Each observer completed 10 trials in each angle β condition, 125 making a total of 60 trials, presented in random order. There was an initial practice block of 126 three trials. The experimental session only started when the observers felt at ease with the 127 task, otherwise they went through another practice session.

128

130 2.5. Results

131 Illusion strength was measured as the difference in degrees (angular error) between the 132 apparent (mean cancellation adjustment) and actual collinearity of the two edges. If the 133 cancellation adjustment was identical to the coordinates of the AC line, then the angular error 134 would be zero. This would mean that observers did not compensate for the illusory effect. 135 However, if the value of the cancellation adjustment differed from the coordinates of the AC 136 line, the angular error would be greater than or less than zero. This would mean that observers 137 compensated for the illusory effect by moving the stimulus edges in the opposite direction. It 138 should be noted that a positive value corresponded to an adjustment toward the top lefthand 139 corner, and a negative value to an adjustment toward the bottom righthand corner. The mean 140 angular errors for the six values of angle β are plotted in Figure 2.

141 The angular error increased as the angle β increased until the latter was equal to 12°, 142 beyond which the angular error decreased. The greatest adjustment (1.83°) was therefore 143 made when the angle β was 12°. Smaller adjustments (0.17° and 1.12°) were required for 144 angle β of 4° and 8°. Results were relatively symmetrical on both sides of the 12° angle. Thus, 145 the adjustments were around 1.03° when the angle β was 23°, and 0.05° for angle β of 34°. 146 When the angle β was 45°, the angular error was -0.23°.

147 This pattern was confirmed by a repeated-measures analysis of variance (ANOVA). 148 An analysis of angular error for angle β (4° × 8° × 12° × 23° × 34° × 45°) yielded a significant effect, F(5, 940) = 113.261, p < .001, $\eta_{G}^{2} = 0.306$, $\eta_{P}^{2} = 0.377$. Post hoc t tests with 149 150 Holm-Bonferroni correction for multiple comparisons are presented in Table I. Results 151 indicated significant differences between the angle β of 12° and the other five conditions 152 (Holm-Bonferroni correction, p < 0.001 for 5 tests). Interestingly, no significant differences 153 were found between angles 4° and 34° (Holm-Bonferroni correction, p > 0.5) or between angles 8° compared to an angle β of 23° (Holm-Bonferroni correction, p > 0.5). These 154

155	comparisons also revealed significant differences between all other conditions (Holm-
156	Bonferroni correction, $p < .02$ for 8 tests). We concluded that the Bourdon illusion is strongest
157	when the angle β is around 12°.
158	
159	Figure 2 about here
160	
161	Table I about here
162	
163	3. Experiment 2
164	3.1. Observers
165	We recruited 20 different psychology undergraduates aged 18-25 years as observers
166	for the second experiment. All had normal visual acuity, and all were naïve to the purpose of
167	the experiment. This second experiment was conducted in accordance with the Declaration of
168	Helsinki.
169	
170	3.2. Apparatus
171	The same apparatus was used as in Experiment 1.
172	
173	3.3. Stimuli
174	Figures were made up of two right-angled triangles connected by their apices. These triangles
175	were displayed in black (x = 0.30, y = 0.45; Y = 1.03 cd/m ²) against a neutral gray
176	background (x = 0.29, y = 0.32; Y = 60.32 cd/m ²). The ABD/CBE apex angle was
177	systematically 12.5° (see angle β in Fig. 1), and the vertical orientation of the figure was 22.5°
178	(angle α in Fig. 1). These values had produced the strongest illusions in previous studies
179	(Rozvany & Day, 1980; Verstijnen & van Leeuwen, 1998). In the present experiment, the

180 triangles were displayed with five different angle γ values, ranging from 4° to 135° in steps of 181 22.5° (see Fig. 1b). Figure 3 shows the stimuli used in this experiment. It should be noted that 182 in one condition, there was an angle of 90°, corresponding to a right-angled triangle (type of 183 triangle used in the first experiment).

- 184
- 185

Figure 3 about here

186

187 3.4. Procedure

The procedure was identical to that used in Experiment 1. There were a few minutes of dark adaptation prior to the experiment, and practice trials preceded the data collection. Each observer performed 10 trials in each γ angle condition, making a total of 50 trials, presented in random order each time.

192

193 *3.5. Results*

We calculated the mean angular error for each condition (see Fig 4) as the difference between the mean cancellation adjustment made by each observer and the coordinates of the AC line (see Fig. 1b). The results of the cancellation task showed that the strength of the illusion was modulated by the γ angle value. The angular error increased as the γ angle increased up to a value of 90°. Corresponding mean angular errors were 0.889° (angle $\gamma = 45°$), 1.487 degrees (angle $\gamma = 67.5°$) and 2.696 degrees (angle $\gamma = 90°$). Beyond 90°, the angular error decreased from 1.947° (angle $\gamma = 112.5°$) to 1.209° (angle $\gamma = 135°$).

This finding was supported by a repeated-measures ANOVA. Results revealed a significant effect of the γ angle value ($45^{\circ} \times 67.5^{\circ} \times 90^{\circ} \times 112.5^{\circ} \times 135^{\circ}$), F(4, 792) = 68.519, p</br>
203 <.001; $\eta^{2}_{G} = 0.084$, $\eta^{2}_{p} = 0.257$. A post hoc paired *t* test (with Holm-Bonferroni correction)

204 revealed a significant difference between all γ angle conditions, these multiple comparisons

205	are shown in Table II. We concluded that the Bourdon illusion is strongest when γ angle is
206	equal to 90° (i.e., corresponding to a right-angled triangle).
207	
208	Figure 4 about here
209	
210	Table II about here
211	
212	4. Experiment 3
213	4.1. Observers
214	We recruited 19 different psychology undergraduates aged 19-25 years as observers. All had
215	normal or corrected-to-normal vision and were naïve to the purpose of the experiment. This
216	third experiment was conducted in accordance with the Declaration of Helsinki.
217	
218	4.2. Apparatus
219	The apparatus was identical to that used in Experiment 1.
220	
221	4.3. Stimuli
222	Figures were composed of two right-angled triangles connected by their apices. These
223	triangles were displayed in black (x = 0.30, y = 0.45; Y = 1.03 cd/m ²) against a neutral gray
224	background (x = 0.29, y = 0.32; Y = 60.32 cd/m ²). The apex angle was systematically 12.5°
225	(see angle β in Fig. 1), and the vertical orientation of the figure was 22.5° (angle α in Fig. 1).
226	These values had produced the strongest illusions in previous studies (Rozvany & Day, 1980;
227	Verstijnen & van Leeuwen, 1998).
228	Figure 5 shows the stimuli used in this experiment. The patterns were created by
229	varying the size of one right-angled triangle while holding the size of the second right-angled

230	triangle constant. Each of the two right-angled triangles was displayed in four versions of
231	varying size. For the triangle that varied in size, the AB (or BC) lengths corresponded to the
232	distance of A (or C) from the central apex (see Fig. 1b) and were approximately 8.6°, 6.4°,
233	4.2° and 2.1° , while the AD (or CE) lengths (see Fig. 1b) were 2.4° , 1.8° , 1.2° and 0.6° . For
234	the triangle that stayed the same size, the AB (or BC) length was approximately 8.6° and the
235	AD (or CE) length was around 2.4°. It should be noted that in one condition, the two right-
236	angled triangles were the same size. There were seven different conditions.
237	
238	Figure 5 about here
239	
240	4.4. Procedure
241	The procedure was identical to that used in the two previous experiments. There were 3
242	minutes of screen adaptation prior to testing. Each observer performed 10 trials in each
243	condition, making a total of 70 trials. Practice trials preceded the data collection. The order of
244	the trials was randomized for each observer.
245	
246	4.5. Results
247	For each observer, the strength of the illusion was measured as the angular error, obtained by
248	computing the difference between the cancellation adjustment and the coordinates of the AC
249	line (see Figure 1b). Mean angular errors for all seven conditions are shown in Figure 6. The

angular error increased as the distance of C from the central apex increased: gradually at first (angular error of 1.572° at 2.1°), then levelling off ($1.884^{\circ}-1.845^{\circ}$ between 4.2° and 6.4°), before rising steeply (2.674° at 8.6°). The angular error decreased as the distance of A from the central apex decreased: steeply at first (angular error of 2.674° at 8.6°), then levelling off ($1.443^{\circ}-1.263^{\circ}$ between 4.2° and 6.4°), before gradually decreasing (0.754° at 2.1°).

255	A repeated-measures ANOVA assessed significant differences in illusion strength
256	across conditions, $F(6, 1128) = 53.940$, $p < .001$; $\eta_{G}^{2} = 0.162$, $\eta_{p}^{2} = 0.223$. A Holm-Bonferroni
257	post hoc test revealed significant differences between the condition where A and C were the
258	same distance from the central apex and all other conditions as shown in Table III
259	(Holm-Bonferroni correction, all $ps < .001$). Comparisons between the conditions where the
260	distance of C (or A) from the central apex was either 4.2° or 6.4° were not significant. All
261	other comparisons were significant (Holm-Bonferroni correction, all $ps < .05$). We conclude
262	that the Bourdon illusion is strongest when the two triangles are of equal size.
263	
264	Figure 6 about here
265	
266	Table III about here
267	
267 268	5. Discussion
	5. Discussion Summary of Results
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268 269 270 271 272	Summary of Results Our experiments were designed to test the effect of shape arrangement on the strength of the Bourdon illusion. A cancellation method was used for quantification. In this task, observers simultaneously adjusted two sides (AB and BC in Fig. 1) until they appeared straight. Results
268 269 270 271 272 273	Summary of Results Our experiments were designed to test the effect of shape arrangement on the strength of the Bourdon illusion. A cancellation method was used for quantification. In this task, observers simultaneously adjusted two sides (AB and BC in Fig. 1) until they appeared straight. Results demonstrated that triangle shape plays a critical role in inducing the illusion. In Experiment 1,
268 269 270 271 272 273 274	Summary of Results Our experiments were designed to test the effect of shape arrangement on the strength of the Bourdon illusion. A cancellation method was used for quantification. In this task, observers simultaneously adjusted two sides (AB and BC in Fig. 1) until they appeared straight. Results demonstrated that triangle shape plays a critical role in inducing the illusion. In Experiment 1, the strongest Bourdon illusion occurred when the internal apical angle (β) was around 12°.
 268 269 270 271 272 273 274 275 	Summary of Results Our experiments were designed to test the effect of shape arrangement on the strength of the Bourdon illusion. A cancellation method was used for quantification. In this task, observers simultaneously adjusted two sides (AB and BC in Fig. 1) until they appeared straight. Results demonstrated that triangle shape plays a critical role in inducing the illusion. In Experiment 1, the strongest Bourdon illusion occurred when the internal apical angle (β) was around 12°. The second experiment showed that the illusion was stronger for right-angled triangles, and

illusion, and suggest that the right-angled triangle is the predominant figural determinant forcancellation adjustments.

281

282 Comparison with Previous Studies

283 The first experiment indicated that the greatest angular error was for an internal apical angle 284 of 12°, consistent with previous findings (Rozvany & Day, 1980). In our first experiment, this 285 angular error was 1.83°, and in the two subsequent experiments where the value of angle β 286 was held constant at 12.5°, the maximum angular errors were 2.696° and 2.674°. These values 287 are similar to those found in previous studies when authors used similar displays to create the 288 Bourdon illusion (3-4° in Rozvany & Day, 1980; 2-4° in Verstijnen & van Leeuwen, 1998; 289 3.75° in Walker & Shank, 1987; 1-2° in Wenderoth, O'Connor, & Johnson, 1986; 2° in Wenderoth & O'Connor, 1987b). We interpret these results to mean that an angle β of 12.5° 290 291 contributes to a robust Bourdon illusion.

292 There is nonetheless considerable variability between studies. One possible 293 explanation is that there are differences in the methods adopted to collect the data and in the 294 apparatuses used. Verstijnen and van Leeuwen (1998) reported three different tasks in which 295 the Bourdon illusion was studied in different orientations while the inner apical angle was 296 held constant at 12.5°. Results showed that the strength of the Bourdon illusion varied 297 according to the task. When the pattern had an orientation of 22.5°, authors found a mean 298 angular error of around 2-3° for a multiple-choice task and a construction task, and 3-4° for an 299 adjustment procedure. In the present study, we used a cancellation task that had not 300 previously been administered, which may explain why our results differed.

301 In the first experiment, results indicated that the Bourdon illusion was stronger when 302 scalene triangles were used rather than isosceles triangles (e.g., angle β equal to 45°). These 303 data were consistent with previous studies using an angle discrimination task, in which 304 performances on angles forming an isosceles triangle were more precise than those forming a 305 scalene triangle (Kennedy et al., 2006, 2008). Increasing angle β may conceivably have 306 reduced the strength of the illusion because the salience of the apical angle increased. When 307 the apical angles were well discriminated, observers correctly dissociated the collinear (AB 308 and BC in Fig. 1) edges from the hypotenuse (BE and BD in Fig. 1). Consequently, the use of 309 isosceles triangles reduces an even cancels the Bourdon illusion.

310 Our second experiment showed that scalene triangles did not produce the same effect, 311 indicating that the angle y values influenced the strength of the Bourdon illusion. These 312 results suggest that angles β and γ interact to create the illusion. Right angles are easily 313 perceptible, whereas acute angles tend to be overestimated, and obtuse angles underestimated 314 (Chen & Levi, 1996; Nundy et al., 2000). Thus, the use of a right angle does not change the 315 perception of angle β , and maximizes the illusion. By contrast, the perception of angle β is 316 modulated by acute or obtuse angles. The illusion is therefore weaker, consistent with our 317 psychophysical results.

318 Our data indicated that the strongest Bourdon illusion occurred when the triangles 319 were of equal size (Exp. 3). This result suggests that increasing the visibility of the 320 symmetrical display increases the illusion. These data are consistent with those reported in 321 previous studies showing that an unbalanced pattern decreases the strength of many visual 322 illusions. For instance, changes at the intersection between oblique and parallel lines on one 323 side of the Poggendorff illusion reduce the misalignment phenomenon (Day, 1988). Similarly, 324 the strength of the Zöllner illusion decreases when the inner or outer parts of the oblique lines 325 are removed (Oyama, 1975).

326

327 Previous Explanations for the Bourdon Illusion

Various explanations for the Bourdon illusion have been put forward. Walker and Shank (1987, 1988a) developed a model based on interactions between orientation-selective neurons. For these authors, there are no interactions when two lines have very different orientations. By contrast, when two lines have similar orientations, they mutually induce a specific neural distribution. This results in a peak of firing from the summation of lateral inhibition from the edges with the neural excitation from the solid figure, resulting in a mutual attraction effect.

334 According to another explanation put forward by Wenderoth, O'Connor, and Johnson 335 (1986) (see also Wenderoth, 1991), every stimulus is processed along three separate neural 336 channels coding orientation, position, and collinearity. These authors postulated that the illusion arises from conflicting signals between these channels. Under normal circumstances, 337 338 the neural signals are not in conflict, but this is not the case with the Bourdon edges (lines AB 339 and BC in Fig. 1a) and so a neural compromise occurs. The Bourdon illusion involves a 340 failure to dissociate the orientation of the collinear edges (e.g., AB and BC in Fig. 1) from the 341 orientations and positions of the hypotenuse edges (e.g., BD and BE in Fig. 1). This failure 342 results in the collinear edges being attracted in the direction induced by the hypotenuse edges.

Finally, Day (1989, 1990) suggested that multiple cues define a visual pattern. When these cues are in conflict, the perception is a compromise between them. In the Bourdon illusion, the collinear edges have one specific orientation, and each hypotenuse edge has a different one. The compromise between these orientations results in the collinear edges being perceived to follow the direction of the hypotenuse edges.

According to these models, the collinear and hypotenuse edges combine to explain the Bourdon illusion, albeit via different mechanisms. However, they fail to consider other figural parameters. Our data suggest that the use of right-angled triangles generates a stronger illusion, and thus increases the angular error (Exp. 2). Furthermore, our angular error analysis 352 showed that the strongest illusion occurred when the right-angled triangles were of equal size353 (Exp. 3).

The present study suggests that the Bourdon illusion arises from a combination of configural processing. It is constructed by integrating multiple sources of information, including the object's geometric properties. Thus, models such as those described above should be extended to take the different figural parameters into account.

358

359 Role of Inhibitory Processes

The Bourdon illusion can be classified as an illusion of orientation, whose effects are associated with misalignment or nonparallelism (Day, 2010; Hamburger et al., 2017). This type of illusion has different stimulus properties, but the oblique factor is a common condition (Day, 2010).

Rozvany and Day (1980) noted that the Bourdon illusion is stronger when the figures are oblique, rather than vertical or horizontal, as is the case of the Zöllner (Parlangeli & Roncato, 1995; White, 1975), Poggendorff (Day & Dickinson, 1976; Weintraub et al., 1980), and tilt (Clifford, 2014; Clifford, Wenderoth & Spehar, 2000) illusions. These illusions are weaker when the figures are vertical or horizontal. These illusions and the Bourdon illusion may conceivably share common mechanisms.

One classic explanation is that these illusions stem from neural inhibitory processes (Gillam, 2017; Westheimer, 2008). It is well known that any given orientation is coded by neurons sensitive to a range of orientations. The illusion is attributed to the fact that a bias is introduced by lateral inhibition between neighboring orientation channels (Blakemore, Carpenter, & Georgeson, 1970; Blakemore & Tobin, 1972; Carpenter & Blakemore, 1973).

Lateral inhibition was also a central aspect of Walker and Shank (1987, 1988a)'s
theory explaining the Bourdon illusion. However, Wenderoth et al. (1990) noted that this

377 explanation holds good not only for a two-triangle display such as that in the original Bourdon 378 figure, but also for a single-triangle display. The role of lateral inhibition has also been 379 disputed in other phenomena. For example, Gillam (2017) discussed the role of lateral 380 inhibition because the illusion persists when the original lines are replaced by subjective 381 contours. It is still present when the parallel lines are replaced by empty interspaces in the 382 Zöllner illusion (Earle & Maskell, 1995) or by dots in the Wundt-Hering illusion (Coren, 383 1970). This has also been observed for other figures using subjective contours, such as the 384 Poggendorff (Gregory, 1972; Tibber et al., 2008) and Bourdon (Walker & Shank, 1987, 385 1988a, 1988b) illusions, indicating that physical angles and lateral inhibition processes are not 386 necessary because the illusion persists.

387 Nonetheless, Seymour et al. (2018) confirmed the inhibition of cortical responses, by 388 performing functional neuroimaging of area V1 of the human visual cortex during the 389 perception of the tilt illusion. Results showed that participants who exhibited strong neural 390 suppression perceived a stronger illusory effect. This could be the result of lateral inhibition, 391 but feedback projections from extrastriate cortical areas may also be involved. This is a 392 relevant idea, in view of studies suggesting that feedback signals play an important role in the 393 perception of Kanisza shapes (Kok & de Lange, 2014; Kok et al., 2016). Feedback projections 394 have been ignored in previous theories, even though they are just as numerous as feedforward 395 projections in the visual cortex (Markov et al., 2014).

The present study shows that figural parameters modulate the Bourdon illusion. Taken together, our data support the hypothesis that the mechanisms underlying the distortions in contour perception involve multiple levels of processing. It would be interesting for future research to clarify the role of feedforward, feedback and lateral processes in orientation illusions.

402 Data availability

403 Materials created and used for this study were described in the manuscript. The data obtained

404 during this study were reported in the manuscript along with figures and tables. Any

405 additional information, materials, and datasets are available from the corresponding author.

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506 Figure Legends

507	Fig. 1:	Example of the Bourdon illusion. (a) The edges AB and BC are collinear, but
508		appear to bend in the same direction as the chevron formed by the arms of the angle
509		DBE. (b) Here, α refers to the orientation of the long axis of the figure relative to
510		the vertical axis, β refers to the internal apical angles of the figure, and γ
511		corresponds to the right angles. In our study, angle α was systematically equal to
512		22.5°. In the first experiment, apex angle β values ranged from 4° to 45°. In the
513		second experiment, we manipulated the angle γ so that its values ranged from 45° to
514		135°. The dashed line indicates the direction of possible adjustments to edges AB
515		and BC.
516		
517	Fig. 2:	Mean cancellation adjustments in degrees as a function of the internal apical angle
518		β (Experiment 1). The dashed line indicates the expected response when AB and
519		BC are collinear. Error bars are +/- 1 SEM.
520		
521	Fig. 3:	Stimulus figures used in Experiment 2. Here, five different angle γ values were
522		used: 45° (a), 67.5° (b), 90° (c), 112.5° (d) and 135° (e).
523		
524	Fig. 4:	Cancellation adjustments plotted as a function of angle γ values (Experiment 2).
525		Error bars are +/- 1 SEM.
526		
527	Fig. 5:	Stimuli used in Experiment 3. (a-c) In three patterns, the right-angled triangle at the
528		top was smaller than the right-angled triangle at the bottom. (d) Classic Bourdon
529		figure in which the two right-angled triangles are of equal size. (e-g) In three

530	patterns, the right-angled triangle at the bottom was smaller than the right-angled
531	triangle at the top.

533	Fig. 6:	Mean adjustments made to cancel the Bourdon illusion as a function of the distance
534		of A (bottom triangle) or C (top triangle) from the central apex (Experiment 3).
535		Error bars are +/- 1 SEM.
536		