

# Lattice strain development in an alpha titanium alloy studied using synchrotron and neutron diffraction

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| 1  | Lattice strain development in an alpha titanium alloy studied using synchrotron and  |
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| 2  | neutron diffraction  |
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| 14 |  |
| 15 | Abstract   |

16 Neutron and high-energy X-ray diffraction methods have been used to investigate deformation mechanisms (slip and twinning activities) during uniaxial tensile tests of Grade 1 17 commercially pure titanium (Ti- $\alpha$ ). These two diffraction techniques have provided valuable 18 19 and complementary information. The predictions made by an Elasto-Plastic Self-Consistent (EPSC) model, taking into account grain reorientation and stress relaxation induced by 20 twinning activity, have been compared with the experimental data. Results clearly 21 demonstrate that there is a good agreement between simulations and diffraction 22 measurements. The EPSC model enables accurate predictions of: (i) the lattice strains 23 developed in variously oriented {hk.l} grain families within the bulk material, (ii) the grain 24 reorientation induced by twinning activity and (iii) the macroscopic stress-strain response. 25

Two different textured products were studied in order to evaluate the influence of texture on the mesoscopic and macroscopic responses of  $Ti-\alpha$  alloy.

28 Keywords: titanium alloys, strain measurements, plasticity, modelling, anisotropy, diffraction

29 1. Introduction

Due to their high specific strength, good corrosion resistance and biocompatibility, titanium 30 and its alloys are of the utmost importance for aeronautic applications and are also widely 31 used in naval and biomedical industries [1–3]. Hexagonal Close Packed (HCP) metals present 32 a low crystalline symmetry as compared to cubic materials. They are then governed by a 33 heterogeneous plastic deformation, and the way it is accommodated is still not well 34 understood. At room temperature, it is well experimentally established that prismatic slip 35 36  $\{10.0\}(11.0)$  is the easiest deformation mode to be activated in HCP titanium. Pyramidal  $\langle c + a \rangle$  slip {10.1}(11.3), pyramidal  $\langle a \rangle$  slip {10.1}(11.0) and basal slip {00.2}(11.0) are 37 generally presented as secondary slip modes [4,5] that are more difficult to activate. In 38 particular,  $\{10.1\}(11.3)$  slip produces plastic deformation with a component out of the basal 39 plane (i.e. along the  $\vec{c}$ -axis). Deformation along  $\vec{c}$ -axis can also be accommodated by twinning 40 modes  $\{10.2\}(10,\overline{1})$  or  $\{11.2\}(11,\overline{3})$  that induce a reorientation of the crystal lattice [4,6,7]. 41 42 The relative activity of these multiple deformation mechanisms strongly depends on the chemical composition, grain size, morphological and crystallographic textures, straining 43 direction and strain rate. Understanding how the different deformation mechanisms operate 44 during plastic deformation of titanium alloys require thus further investigations. A deeper 45 knowledge of the mechanical behavior of HCP materials during plastic deformation calls for 46 the use of advanced techniques such as Time-Of-Flight (TOF) neutron or High Energy 47 synchrotron X-Ray Diffraction (HEXRD) enabling to monitor the evolution of internal elastic 48 strains. With a high spatial resolution, X-ray synchrotron radiation allows a very small gauge 49

50 volume (200  $\mu$ m × 200  $\mu$ m spot size for the present study) as compared to the neutron diffraction one (4 mm  $\times$  4 mm spot size for the present study), but offers fast rate data 51 52 acquisition (few seconds for synchrotron radiation and around 40 minutes for neutron diffraction in this work). This technique enables to measure online strain distributions and *in* 53 situ during a continuous mechanical loading. In contrast, for materials characterized by a 54 55 substantial creep behavior such as titanium alloys, the samples investigated by neutron techniques have to be unloaded once the desired macroscopic strain has been reached. 56 Analyses relate thus only to the residual lattice strains remaining after a given increment of 57 58 plastic deformation [8–10]. These two complementary non-destructive methods have been adopted in this work to measure the change in the {hk.l} d-spacing during tensile loadings in 59 order to characterize the internal elastic strains (or intergranular strains) distribution. 60 Experimental results can be explained and interpreted using a polycrystalline modeling 61 approach like the Elasto-Plastic Self-Consistent (EPSC) model [11–15]. 62 This 63 micromechanical modelling is a helpful technique to characterize the mechanical state of polycrystalline materials at the grain level and to understand the role played by plastic 64 anisotropy, slip-slip (and slip-twin) competitions in the macroscopic behavior. For example, 65 Warwick et al. [8] have examined a textured Grade 1 Commercially Pure titanium (CP Ti) by 66 coupling neutron diffraction to self-consistent modelling. A good agreement was found 67 between neutron diffraction and the simulated results. The authors found that twinning 68 produces a greater hardening than slip and that the residual lattice strains developed in the 69 {00.2} grains are higher than in other orientations for both tensile and compression straining. 70 71 A similar finding has been achieved by Gloaguen et al. [9], who analyzed the deformation mechanisms involved in the plasticity of Grade 2 CP Ti during compressive loadings. The 72 residual lattice strain of different {hk.l} orientations was tracked in both parallel and 73 74 transverse directions to the straining axis and the diffraction data were investigated to

highlight the role of tensile twin  $\{10.2\}$  in the  $\alpha$ -titanium alloy. Cho et al. [10] used a similar 75 methodology to characterize the intergranular residual strains accumulation in a near  $\alpha$ -76 titanium alloy and a Ti-834 alloy during tensile tests. It has been found that it was possible to 77 successfully reproduce the trends and magnitudes of the observed microstrains in both loading 78 and transverse directions. The plastic behavior of a two phase titanium alloy, Ti-6Al-4V, has 79 also been studied [16] thanks to this coupled approach. The X-ray synchrotron diffraction has 80 likewise been used with EPSC modelling by Stapleton et al. [17] to analyze the evolution of 81 internal lattice strains in a Ti-6Al-4V alloy during in situ tensile tests. A similar study has 82 been carried out in a near  $\beta$ -titanium alloy [18]. The main advantage of high energy X-rays is 83 the possibility to have short measurements during a continuous mechanical test. The number 84 85 of diffracting grains is nevertheless smaller as compared to neutron diffraction experiments due to the smaller gauge volume (respectively 200  $\mu$ m × 200  $\mu$ m × 2 mm and 4 mm × 4 mm × 86 4 mm). Therefore, the lattice strains determined with synchrotron X-ray radiation are less 87 representative due to a smaller number of crystallites contributing to the diffracting volume. 88 The comparison with a homogenization approach is then more problematic [14]. 89

The purpose of the work presented in this paper is to understand the internal strain 90 development of a commercially pure titanium under uniaxial tensile loadings. Experimental 91 92 observations are coupled with the predictions of the EPSC model in order to explain the plastic behavior of Ti- $\alpha$  and to identify the slip systems and twinning modes responsible for 93 the plastic activity within the material. One of the objectives of this study is to evaluate the 94 influence of crystallographic texture and twin activity on the mechanical response. An EPSC 95 model, taking into account grain reorientation and stress relaxation induced by twinning 96 97 activity, has been developed for this study. Two different textured samples (a unidirectional rolled plate and a forged bar) for the same alloy were studied in order to evaluate the 98 influence of texture on the mesoscopic and macroscopic responses of a Grade 1 CP Ti-α alloy. 99

100 A comparison between these two techniques and the experimental internal (X-ray) and 101 residual (neutron) strain values obtained with an EPSC model has been made to analyze the 102 potential difference.

#### 103 **2.** Experimental methods

104 *2.1. Material* 

105 The investigated material is a Commercially Pure  $\alpha$ -titanium (denoted CP Ti- $\alpha$ ). Two 106 samples, produced by two different forming processes, are studied: a unidirectional rolled 107 plate and a forged bar. The samples are fully hexagonal compact phased at room temperature 108 and their chemical compositions are given in Table 1. The tensile specimens have different 109 geometries (see Fig. 1).



**Table 1:** Chemical composition data (wt.%) of the materials

| Specimen | С     | Ν      | 0     | Н      | Fe    | Ti      |
|----------|-------|--------|-------|--------|-------|---------|
| N-Sample | 0.07  | 0.008  | 0.12  | 0.0013 | -     | Balance |
| S-Sample | 0.012 | 0.0078 | 0.137 | 0.001  | 0.164 | Balance |

111

112 Cylindrical specimens (denoted below as N-sample) with 8 mm diameter and 42 mm gauge 113 length were cut along the extrusion direction (represented by the Longitudinal Direction: LD, 114 Fig. 1.a) for neutron diffraction experiments. This geometry was adopted in order to access to 115 a sufficiently large gauge volume. However, *in situ* synchrotron experiment specimens, 116 denoted as S-samples, have been machined along the Transverse Direction (TD) of the rolled 117 plate, as shown on Fig. 1.b. The sample thickness was small enough (2 mm) to enable 118 transmission measurements [19]. The metallographic characterization has revealed that the grains are generally equiaxed with an average grain size of 40 and 45 μm in S-samples and Nsamples, respectively.

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Fig. 1: Schematic view showing dimensions (in mm) of the samples used in a) neutron and b)
synchrotron experiments. LD: Longitudinal (loading) Direction, TD: Transverse Direction,

125

#### ND: Normal Direction

N-sample texture measurements were performed on the GEM beamline at the ISIS neutron spallation source (United Kingdom). Information about the instrument and the measurement technique can be found in [20,21]. Measurements of the initial texture (Fig. 2.a) have revealed that the samples have a strong asymmetric texture in the TD-ND plane, perpendicular to the loading axis (LD). This texture is consistent with the analyses made on extruded hexagonal polycrystalline samples found in literature [8,9,22].

The S-sample initial texture, shown in (Fig. 2.b), was measured using the neutron diffraction
on the 6T1 diffractometer from the French national Orpheus nuclear reactor (at Léon Brillouin
Laboratory, Saclay, Gif-sur-Yvette, France). As revealed in Fig. 2.b, basal poles are tilted +

30° away from the Normal Direction axis (corresponding to the plate normal direction)
toward the Transverse Direction. The observed texture is typical of rolled titanium plates
followed by recrystallization.



#### 138

**Fig. 2:** Initial crystallographic textures of the studied specimens a) N-sample and b) S-sample

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### 141 2.2. Neutron diffraction measurements

Tensile tests were performed at room temperature using the ENGIN-X neutron diffractometer (Fig. 3) at the ISIS spallation neutron source. The measurement steps were applied by a 50 kN Instron testing machine with a strain rate of  $10^{-5} s^{-1}$  up to 6 % of macroscopic strain. The specimen was subjected to a displacement controlled regime. The incident slits and radial collimators defined a scattering volume of  $4 \times 4 \times 4$  mm<sup>3</sup> with a counting time of 43 minutes per measurement. The macroscopic strain was determined using an extensometer that spanned the irradiated region. The sample was first deformed to the desired macroscopic strain and 149 then immediately unloaded, as shown in Fig. 4, to avoid any strain relaxation due to the creep







152 Fig. 3: Schematic top-view of the set-up used on the neutron diffraction instrument ENGIN-X

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Fig. 4: Measured macroscopic stress- strain curve obtained with ENGIN-X. The green points
indicate the macroscopic strain during neutron measurements after unloading, i.e. at zero
applied load.

Successive steps have been achieved at room temperature, in the plastic regime, studying the remaining residual strains resulting from a given increment of plastic deformation at zero

applied load. The schematic view of the ENGIN-X instrument (Fig. 3) shows a horizontal 160 loading axis positioned at 45° with respect to the incident beam. Two detector banks are set 161 up horizontally at  $\pm 90^{\circ}$  from the incident beam, enabling simultaneous measurements of 162 lattice strains from {hk.l} plane families with parallel (i.e. along the loading direction) and 163 perpendicular (i.e. along the transverse direction) directions, as regard to the loading applied 164 direction (Fig. 3). The Time-Of-Flight (TOF) technique enables to collect simultaneously an 165 entire diffraction pattern (the effective d-spacing range from 0.88 to 2.63 Å) on each detector 166 [23]. Single peak fitting was performed using the Open Genie code [24] with Gaussian 167 functions. The lattice strain  $\langle \varepsilon(hk, l, \varphi, \psi) \rangle_{V_d}$  of a grain group having a common {hk.l} plane-168 normal parallel to the diffraction vector  $\vec{Q}$  (defined by azimuthal and inclination angles, 169 respectively  $\varphi$  and  $\psi$ ) can be calculated by the following formula: 170

$$\langle \varepsilon(hk,l,\varphi,\psi) \rangle_{V_d} = ln\left(\frac{\langle d(hk,l,\varphi,\psi) \rangle_{V_d}}{d_0(hk,l)}\right) \qquad Eq. 1$$

The initial lattice parameter  $d_0(hk. l)$ , measured before deformation of the material, is used as the reference point for this calculation.  $\langle X \rangle_{V_d}$  (V<sub>d</sub>: diffracting volume,  $X = \varepsilon(hk. l, \varphi, \psi)$  or  $d(hk. l, \varphi, \psi)$ ) stands for the averaging over the diffracting grains for the considered {hk.1} reflection.  $\langle d(hk. l, \varphi, \psi) \rangle_{V_d}$  is the measured lattice spacing and resulting lattice strain values are given as micro-strain (denote  $\mu\varepsilon$ , i.e. units of 10<sup>-6</sup>). In the remainder of the paper, // and  $\perp$ symbols respectively refer to the lattice strain in the parallel and perpendicular directions to the stress axis (corresponding to the extrusion direction).

#### 178 2.3. Synchrotron X-ray measurements

179 ID15B beamline at the ESRF (the European Synchrotron Radiation Facility, Grenoble, 180 France) has been used to perform *in situ* tensile tests in a transmission mode, with a 181 monochromatic X-ray radiation of 87 keV ( $\lambda = 0.1425$  Å wavelength). The configuration of the experimental setup is shown in Fig. 5.a. The tests were performed on an Instron 8800 electrothermomechanical test machine with a maximum load capacity of 3 kN under a constant strain rate  $4.10^{-4}$  s<sup>-1</sup> up to 4 % macroscopic strain. The load was applied perpendicular to the rolling direction (Fig. 1.b). Fig. 6 shows the macroscopic curve obtained on ID15B beamline.



Fig. 5: a) Experimental setup showing S-sample positioning, b) example of image recorded
on the 2D detector with γ and β angle definitions

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The diffraction patterns (example presented in Fig. 5.b), have been recorded using a 2D 193 Pixium 4700 flat-panel detector [25], positioned in agreement with the targeted {hk.l} 194 195 diffracting planes and signal optimization. Each ring recorded with the 2D detector corresponds to a {hk.l} crystallographic family plane. Regarding high  $\alpha$ -Ti creep rates, high 196 speed data acquisition is mandatory for online measurements (2s counting time every 7s). 197 Considering the sample dimensions (1 mm  $\times$  2 mm) and the beam size (200  $\mu$ m  $\times$  200  $\mu$ m), 198 the irradiated volume is  $0.2 \times 0.2 \times 2 \text{ mm}^3$ . It has to be underlined that this latter volume is 199 much smaller than the gauge volume obtained in neutron diffraction experiments  $(4 \times 4 \times 4)$ 200 201 mm<sup>3</sup>). The recorded images were processed using the FIT2D pattern analysis software [26], which integrates the two-dimensional images (Fig. 5.b) into one-dimensional spectra 202 (intensity  $I(\gamma, hk.l)$  vs. scattering angle  $\langle 2\theta(hk.l) \rangle_{V_d}$ ). ( $\langle d(hk.l) \rangle_{V_d}$ ,  $I(\gamma, hk.l)$ ) couples have 203 204 been calculated integrating the 2D patterns over a given  $\pm \beta$  range for the two directions : longitudinal (i.e. LD, corresponding to the symmetrical azimuth angles  $\gamma = 90$  and  $270^{\circ}$ ) and 205 transverse (i.e. TD, corresponding to  $\gamma = 0$  and  $180^{\circ}$ ). The integration range over the ring 206 (defined by  $\pm \beta$ ) has to be reasonably large for a statistically representative behavior of the 207 material according to the considered orientation i.e. sufficient amount of the diffractive 208 209 crystallites contributing to the signal. In addition, the  $\beta$  value must be small enough to cover only crystallites oriented relatively to the considered direction. For these reasons and based on 210 [14,19] studies, the intensities of the diffraction rings were integrated, as a compromise, 211 212 within "cake shape" sectors defined by  $\beta \pm 10^{\circ}$ . Finally the arithmetic mean values of the dspacings  $\langle d(hk,l) \rangle_{V_d}$  were calculated from the averaging of the symmetrically equivalent  $\gamma$ 213 and  $\gamma + 180^{\circ}$  angles. 214

The  $\langle 2\theta(hk, l) \rangle_{V_d}$  positions of the diffraction peaks were determined using pseudo-Voigt function fitting [27–29]. The lattice spacing  $\langle d(hk, l) \rangle_{V_d}$  was then calculated from the peak positions using the Bragg's law [30].

218 2.4. Twinning activity in both N-sample and S-sample

Fig. 7.a shows the initial N-sample texture measured on the GEM beamline. The specimen has a strong asymmetric texture in the TD-ND plane with the majority of grains with their basal normal close to the transverse direction and perpendicular to the loading axis. After 6 % of macroscopic deformation, a reorientation of the {00.2} poles was observed (presented by a white framed area in Fig. 7.b). This can be associated with twinning deformation. Actually, the activation of compression twinning {11.2}(11. $\overline{3}$ ) produces a reorientation of the basal poles of approximatively 65° [6,31].



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Fig. 7: Experimental {10.0} and {00.2} pole figures of the a) as-received N-sample and b)
after the tensile loading up to 6 %. Pole figures (PFs) show the ND–LD plane, the center of
the poles being the TD.

Tensile loading along the longitudinal (or extrusion) direction, with the  $\vec{c}$ -axis close to the transverse direction (Fig. 7.a), reorients the  $\vec{c}$ -axis of the grains undergoing twinning deformation. The twinned area fraction can be quantitatively calculated focusing on the difference between {00.2} pole figures of both as-received and deformed samples. Based on the work of Brown et al. [32] and integrating over the white framed area in Fig. 7.a, the total twin volume fraction after 6 % applied macroscopic strain is about 13 %.

Contrary to the previous analysis, crystallographic texture of the S-sample could not be 236 measured in synchrotron experiments after the tensile test. Thus, analysis has focused on the 237 238 evolution of the intensity measured during *in situ* straining as shown in Fig. 8. Gharghouri et al. [33] were the first to show that severe intensity variations during plastic deformation can 239 be reliably attributed to twinning activity. Hence, Muránsky et al. [12], Brown et al. [32] and 240 Gharghouri et al. [33] highlighted a direct correlation between the intensity evolution of 241  $\{10.0\}$  and  $\{00.2\}$  diffraction peaks, measured with detectors placed at 90° from each other 242 and the tensile twinning  $\{10.2\}(10,\overline{1})$  that reorients the twin grains by 90° [31]. Our study 243 confirms findings of these authors: a dramatic increase in {10.0} intensity in the loading 244 245 direction (LD) is observed above around 365 MPa macroscopic stress (Fig. 8.a). At the same time, in the transverse direction (TD), the intensity of the  $\{10.0\}$ -orientated grains decreases, 246 while the {00.2} peak intensity increases significantly (Fig. 8.b). This reflects a change in the 247 grain volume fraction that diffracts in the TD and LD. Owing to the texture of the as-received 248 S-sample, the changes of  $\{00.2\}$  and  $\{10.0\}$  peak intensities in these two directions are due to 249 tensile twinning  $\{10.2\}(10, \overline{1})$  activity. 250

The evolution of the intensity of others reflections such as {10.1} in TD (Fig. 8.b) could naturally also be related to other twining mode activity but it is difficult to discern which one only in the light of the information given by present synchrotron X-ray diffraction experiments.



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Fig. 8: Evolution of the diffraction peak intensities (Miller indices indicated in the plot)
obtained from *in situ* synchrotron X-ray diffraction measurements in the a) loading (LD) and
transverse (TD) directions

## 259 3. Twinning scheme for Elasto-Plastic Self-Consistent model

The one-site EPSC approach applied in this work incorporate the single crystal plasticity model derived by the pioneering works of Kröner [34,35] and Hill [36]. It adopts a weighted population of grains approach which exploits the experimentally measured crystallographic

textures as inputs. Each grain is assumed to have the form of an ellipsoidal inclusion 263 embedded in a homogeneous effective medium with anisotropic properties representative of 264 the textured polycrystalline aggregate. The model has been extensively described in [9,15,37], 265 therefore only a brief description will be given here. More information concerning the 266 approach used can also be found in [38–41]. This model enables to incorporate the measured 267 experimental results as well as to determine the strain hardening parameters, the related 268 Critical Resolved Shear Stress (CRSS) and the mechanical strain/stress state at the 269 mesoscopic level, for the diffracting volume and during the mechanical tests. 270

271 The slip rate  $\dot{\gamma}^{g}$  on a slip system g is linked to the resolved shear stress rate  $\dot{\tau}^{g}$  [40,41] by:

where  $\tau^g$  is the resolved shear stress and  $\tau_c^g$ , the critical resolved shear stress.  $T^g$  is the deformation mechanisms management function and is expressed by:

$$T^{g} = \frac{1}{H^{gg}} \left( \frac{1}{2} (1 + tanh(\tau^{g})) \right) \left( \frac{1}{2} \left( 1 + tanh\left( k \left( \frac{\tau^{g}}{\tau_{c}^{g}} - 1 \right) \right) \right) \right) \left( \frac{1}{2} (1 + tanh(\dot{\tau}^{g})) \right) \qquad Eq. 3$$

where  $H^{gg}$  is the self-hardening coefficient and k, a numerical parameter. The hyperbolic tangent function was used because it enables the mechanical and hardening behaviors, observed in practice, to be reproduced [40,41].

The hardening matrix  $H^{gr}$  is introduced to describe the CRSS rate evolution in a system g, as a function of the plastic slip (or twinning) on the other deformation systems r:

$$\dot{\tau}_c^g = \sum_r H^{gr} \dot{\gamma}^r$$
 Eq. 4

where  $\dot{\tau}_c^g$  is the CRSS rate. Due to a lack of relevant experimental data on latent hardening nature, especially in titanium alloys, the interactions between the different deformation modes are described by a simple law. In the present work, the hardening matrix is described by the following equation [39]:

$$H^{gr} = q.H^{gg}$$

 $H^{gg}$  is the self-hardening coefficient and  $H^{gr}$  corresponds to the latent hardening when g slip system is different from r. The q factor defines the degree of latent hardening.

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In the present study, twinning deformation is treated as a directional slip mechanism [42–44]. 286 It is characterized by the normal to the twinning plane  $n^t$  and the twinning direction  $m^t$ . 287 When a twinning system becomes active, a part of the parent grain is reoriented and stress 288 relaxation is introduced. In order to take into account these phenomena, different algorithms 289 have been proposed. Van Houtte [45] was the first to propose a "Monte Carlo" approach 290 291 consisting of randomly sampling and reorienting full grains. A scheme of such an approach 292 has been proposed by Tomé et al. [46]: reorienting the grain according to the most active twinning system, named Predominant Twin Reorientation (PTR) formulation. Lebensohn and 293 294 Tomé [47] have proposed another one called a Volume Fraction Transfer (VFT) formulation. The Euler space is partitioned in cells and, instead of keeping the grain volume fraction 295 constant while changing its orientation, as done in PTR, the volume fraction assigned to each 296 cell evolves with deformation. This last approach enables to predict the crystallographic 297 texture evolution but it has the disadvantage of losing the grain identity and it does not allow 298 299 to implement a realistic hardening scheme.

The scheme proposed in this paper, called Modified Predominant Twin Reorientation (MPTR), is based on Tomé et al. [46] and Clausen et al. [48] assumptions.

302 3.1 Modified Predominant Twin Reorientation (M-PTR)

The M-PTR scheme accounts for: (i) the stress relaxation associated with the twin formation and, (ii) the twinning fraction effect on texture evolution. At each imposed strain increment, the philosophy of the PTR scheme is adopted. The accumulated shear of each twin system in each grain is recorded and the Predominant Twin System (PTS) is identified as the one that involves the maximum volume fraction  $f_{cum}^t$  (Eq. 6):

$$f_{cum}^t = \sum \frac{\dot{\gamma}^t}{S^t}$$
 Eq. 6

Here,  $\dot{\gamma}^{t}$  represents the shear due to the twin system *t* and  $S^{t}$  is the characteristic twinning shear.

Once the predominant twin system is identified, the total fraction  $f_{cum}^{gr}$  accumulated in each grain is given by the sum over all  $N^t$  active twin systems:

$$f_{cum}^{gr} = \sum_{t=1}^{N^t} f_{cum}^t$$
 Eq. 7

In the EPSC model, a threshold fraction  $f_{limit}$  is introduced in Eq. 8. The idea behind this parameter is to take into account the twinning nucleation mechanism and the initial growth process in the parent grain. More information about these phenomena can be found in [49– 52]. When the volume fraction  $f_{cum}^{gr}$  in a parent grain reaches the threshold  $f_{limit}$ , that fulfills the following equation (Eq. 8), the PTS system is selected and the corresponding grain is fully reoriented.

$$f_{cum}^{gr} \ge f_{limit}$$
 Eq. 8

318  $f_{limit}$  is the model parameter that will be adjusted. Based on Tomé et al. [46], Tomé and 319 Lebensohn [53] and Wronski et al [54] studies, the threshold value  $f_{limit}$  is taken between 5 320 and 50 %. If  $\Omega^m$  is the parent grain orientation, the twin orientation (child)  $\Omega^{tw}$  will be 321 determined by the relation (Eq. 9) [55,56]:

$$\Omega^{tw} = R^{tw} \ \Omega^m$$
 Eq. 9

322 The lattice rotation tensor  $R^{tw}$  is given by:

$$R^{tw} = 2n^t \bigotimes n^t - I \qquad \qquad Eq. \ 10$$

323 where  $n^t$  is the twinning plane normal and I is the unit tensor.

324 Due to the fact that the twinning deformation is a secondary deformation mechanism in our 325 study (see section 2), the nucleated twin is treated as a new independent grain and the new 326 orientation is kept constant until the end of the simulation.

327 3.1.1 Twin variant selection criterion

Experimental studies have shown that each active twin system has six possible variants. 328 Therefore, it is important to define a criterion allowing for the selection of the most 329 330 appropriate twinning variant. Electron Backscatter Diffraction (EBSD) statistical analyses on zirconium [50] showed that {10.2} twinning variants with the highest Schmid factors were the 331 most active (about 56-60 % activation probability). Similar dependencies were observed for 332 {10.2} and {11.2} twinning systems during tensile or compressive loading of commercially 333 pure titanium in [54,57,58]. However, it has been noticed that variants with lower Schmid 334 factors may also contribute to plastic deformation. Thereby, it is clear that the selection 335 process is crucial since it affects the microstructure and the texture evolution of the sample. 336 For example, Wronski et al [54] have used a Visco-Plastic Self-Consistent (VPSC) model 337 with a simple Monte Carlo twin variant selection criterion to predict with accuracy the 338 crystallographic texture evolution in titanium during tensile and compression tests. On the 339 basis of these analyses and in order to provide a reasonable description of the selection 340 process, one variant is picked randomly among the three with the highest twin fractions. The 341 goal behind is to allow for the relatively less predominant variants to accommodate plastic 342 343 deformation.

344 3.1.2 Estimation of the stress relaxation

As mentioned previously, twinning activity induces not only the twinned zone reorientation but also a stress relaxation in the parent grain [48,59,60]. Stress relaxation has been implemented on the assumptions made in [48,59,60]. Elastic strain and stress, originally

present and developed in the new formed (child) grain are estimated by applying continuity 348 equations for tractions and displacements across the twin boundary. The stress and strain at 349 the grain level are assumed to be uniform in the present model and the elastic strains within 350 the plane of the child twin are supposed to be compatible to the matrix on the other side of the 351 twin boundary as described in [48]. Furthermore, stresses acting on the twining plane are also 352 assumed to be equal across the twin interface. When the newly child grain is created and 353 grown to an accumulated twin volume fraction  $f_{cum}^t$  (given in Eq. 6) of the parent grain, a 354 shear strain  $\gamma^t$  for the twin system *t* is calculated from the equation below: 355

$$\gamma^t = f_{cum}^t S^t \qquad \qquad Eq. 11$$

The plastic shear  $\gamma^t$  generates necessarily a back-stress between the parent and child grains in order to accommodate the plastic deformation. It is determined thanks to the Eq. 12 assuming that the imposed plastic shear is equal and opposite to the elastic shear:

$$\varepsilon^{II 0} = -R^t \gamma^t \qquad \qquad Eq. 12$$

Here,  $\varepsilon^{II\,0}$  represents the elastic back-strain and  $R^t$ , the Schmid tensor for the twin system *t*. According to Clausen et al. [48], parent crystal is assumed to be infinitely stiff in comparison with the newly formed twin. It is thus not accommodating any of the plastic shear, forcing the twin to develop an equal and opposite elastic strain. The back-stress is computed with the following relation (Eq. 12), using the twin elastic stiffness tensor:

$$\sigma^{II\,0} = c^t \,\varepsilon^{II\,0} \qquad \qquad Eq.\,13$$

In the formulation applied, the parent and the twin child single-crystal elastic coefficients are supposed to be the same. Then, the stress relaxation is introduced by correcting the current stress with the calculated back-stress  $\sigma^{II 0}$ . The sum is made over the twin systems *t* which become active in the current step [48,60]:

$$\sigma^{II} = \frac{\sigma^{II} + \sum_t \sigma^{II \ 0} f^t_{cum}}{1 - \sum_t f^t_{cum}} \qquad Eq. \ 14$$

In order to perform the numerical simulations, the model parameters must be identified to describe simultaneously the macroscopic stress-train curve and the lattice strains measured on the various {hk.1} reflections. The single crystal elastic constants used in these simulations are shown in Table 2.

| 373 |  |
|-----|--|
|-----|--|

Table 2: The single crystal elastic constants (GPa) used in M-PTR model

| Reference | <i>c</i> <sub>11</sub> | <i>c</i> <sub>12</sub> | <i>c</i> <sub>13</sub> | <i>c</i> <sub>33</sub> | <i>c</i> <sub>44</sub> | <i>c</i> <sub>66</sub> |  |
|-----------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|--|
| [61]      | 162.4                  | 92                     | 69                     | 180.4                  | 46.7                   | 35.2                   |  |

374

Experimental PFs were used to generate the Orientation Distribution Function (ODF). A set 375 376 of 2000 grain orientations weighted by the measured volume fraction has been selected from the experimental ODF. The choice of this number is the result of a preliminary study that 377 allows us to determine the sufficient numbers of grains which describe correctly the 378 experimental data (i.e. neutron or synchrotron measurements) [9,11]. On the basis of 379 experimental observations in [4,7,62,63], the deformation systems considered in the 380 381 simulations are: prismatic slip (denoted P(a)), basal (B(a)), pyramidal ( $\Pi_1(a)$ ), first-order pyramidal ( $\Pi_1(c + a)$ ) and {11.2} twinning (ctw-{11.2}) for neutron data simulations and, 382 prismatic slip (P(a)), basal (B(a)), pyramidal ( $\Pi_1(a)$ ), first-order pyramidal ( $\Pi_1(c + a)$ ), 383 {10.2} twinning (ttw-{10.2}) and {11.2} twinning (ctw-{11.2}) for X-ray synchrotron data 384 simulations. In the two cases, the optimal value assigned to the parameter k (see Eq. 3) is 20. 385 This is to ensure the stability and numerical convergence of the simulations [40,41]. 386

As previously pointed out, owing to a lack of relevant data on the nature of latent hardening in HCP titanium alloys and to be more consistent with the theoretical and experimental information currently available, a simple and empirical law in Eq. 5 is applied to describe the interactions between different deformation modes. The q parameter (see Eq. 5), which determines the degree of latent hardening has been adjusted to provide the best accordance between the experimental and predicted results (set to a value of 1.3 for the simulations). Concerning the twinning activity, the threshold fraction  $f_{limit}$  is set to 25 % what leads to a good description of the material behavior.

Due to the easy activation of prismatic deformation mode P(a), its CRSS value  $\tau^{P(a)}$  is 395 directly related to the macroscopic yield strength and the elastic-plastic transition during 396 tensile tests. The self-hardening coefficient  $H^{P(a)}$  was determined by fitting experimental 397 macroscopic stress-strain curves at the plasticity activity outset. These parameters are then 398 adjusted comparing neutron and synchrotron diffraction measurements. About basal  $(B\langle a \rangle)$ , 399 pyramidal  $(\Pi_1(a))$ , first-order pyramidal  $(\Pi_1(c+a))$ ,  $\{10.2\}$  twinning (ttw- $\{10.2\}$ ) and 400 {11.2} twinning (ctw-{11.2}), there is less consensus on their relative role on the overall 401 behavior. These deformation mechanisms activation sequence can be found in the literature 402 and may differ from one type of alloy to another and / or from one author to another [64-68]. 403 The main goal here is to identify a set of parameters able to explain the results obtained at 404 both the macroscopic scale and diffracting volume level. Several numerical simulations are 405 performed to determine the right set of parameters, in a first step, to successively favor in turn 406 407 one or several mechanisms. Fig. 9.a shows an example of comparison of the simulated results for {20.1} reflection with different activation sequence combinations (denoted COMB1, 408 COMB2, COMB3 and COMB4) and the measured residual lattice strain in neutron 409 410 diffraction. A qualitative analysis shows that only COMB2 sequence reproduces correctly the behavior of {20.1} grain groups. This illustrates clearly the influence of the choice of the 411 412 number of deformation modes and their hierarchy on the mechanical behavior at the diffracting volume level, even if all these combinations describe the observed macroscopic 413 behavior (Fig. 9.b). 414



416 Fig. 9: a) Residual experimental (symbols) and predicted (lines) lattice strain evolution of 417 {20.1} grains in loading direction versus applied stress and b) Experimental and simulated 418 macroscopic stress-strain curves during neutron diffraction experiments. COMB1:  $P\langle a \rangle$  -419  $B\langle a \rangle - \Pi_1 \langle a \rangle - \Pi_1 \langle c + a \rangle - ctw$ -{11.2}, COMB2:  $P\langle a \rangle - \Pi_1 \langle a \rangle - B\langle a \rangle - \Pi_1 \langle c + a \rangle -$ 420 ctw-{11.2}, COMB3:  $P\langle a \rangle - B\langle a \rangle - \Pi_1 \langle c + a \rangle - ctw$ -{11.2} and COMB4:  $P\langle a \rangle - \Pi_1 \langle a \rangle -$ 

421 
$$\Pi_1(c + a) - ctw{11.2}$$

In order to obtain the final material parameters from neutron strain measurements, a least squares method is used, in a second step, to optimize the parameters by minimizing a function  $e^2$  defined as the sum of squares between deviations of the experimental and simulated quantities, over all p grain groups:

$$e^{2} = \sum_{i=1}^{p} \left( \frac{\langle \varepsilon(hk.\,l,\varphi,\psi) \rangle_{V_{d\,meas}}^{i} - \langle \varepsilon(hk.\,l,\varphi,\psi) \rangle_{V_{d\,simul}}^{i}}{u(\langle \varepsilon(hk.\,l,\varphi,\psi) \rangle_{V_{d\,meas}}^{i})} \right)^{2} \qquad Eq. 15$$

426

427 where  $\langle \varepsilon(hk, l, \varphi, \psi) \rangle_{V_{d meas}}^{i}$  is the measured value,  $\langle \varepsilon(hk, l, \varphi, \psi) \rangle_{V_{d simul}}^{i}$  the simulated 428 value, and  $u(\langle \varepsilon(hk, l, \varphi, \psi) \rangle_{V_{d meas}}^{i})$  the uncertainties of the measured lattice strains.

The final set of values that gives the optimum agreement between the measured and simulatedresults are summarized in Table 3.

431**Table 3:** Optimized set of CRSS and hardening coefficients (MPa) obtained with the model.432In blue, CRSS normalized values with respect to  $CRSS^{P(a)}$ , determined with the EPSC model433and neutron diffraction results.

|   | Neutron diffraction |                            | Synchrotron | liffraction     |  |
|---|---------------------|----------------------------|-------------|-----------------|--|
| _   | CRSS                | $\mathrm{H}^{\mathrm{gg}}$ | CRSS        | H <sup>gg</sup> |  |
| P(a)  | 115 (1)             | 120                        | 110 (1)     | 100             |  |
| B(a)  | 150 (1.30)          | 180                        | 150 (1.36)  | 150             |  |
| $\Pi_1\langle a\rangle$                         | 130 (1.13)          | 140                        | 120 (1.09)  | 120             |  |
| $\Pi_1 \langle \mathbf{c} + \mathbf{a} \rangle$ | 240 (2.09)          | 250                        | 180 (1.64)  | 200             |  |
| ttw-{10.2}                                      | -                   | -                          | 190 (1.73)  | 250             |  |
| ctw-{11.2}                                      | 250 (2.17)          | 300                        | 220 (2)     | 300             |  |

#### 434 4. Model results and discussion

Before starting the simulations, residual stresses were quantified in the as-received N-sampleand S-sample.

437 Lattice parameters a = 2.9509 Å and c = 4.6844 Å of the N-sample were found from a 438 Rietveld refinement [10] of the initial entire diffraction ring for measurements along the LD. 439 From these, the ideal d-spacing  $\langle d_0^{Rietveld}(hk,l) \rangle_{V_d}$  for all peaks {hk.l} can be calculated 440 from:

$$\frac{1}{\langle d_0^{Rietveld}(hk,l) \rangle_{V_d}} = \frac{4h^2 + hk + k^2}{3a^2} + \frac{l^2}{c^2}$$
 Eq. 16

441 The difference between the predicted  $\langle d_0^{Rietveld}(hk,l) \rangle_{V_d}$  and measured d-spacing 442  $\langle d(hk,l,\varphi,\psi) \rangle_{V_d}$  by neutron diffraction is assumed to be due to initial residual lattice strain 443  $\varepsilon_{hk,l}^{res} \left( \varepsilon_{hk,l}^{res} = \frac{\langle d_0^{Rietveld}(hk,l) \rangle_{V_d}}{\langle d(hk,l,\varphi,\psi) \rangle_{V_d}} - 1 \right)$  in the extrusion direction (see Table 4).

445

Table 4: Initial residual lattice strains in N-sample in the extrusion direction (LD)

| {hk.l}                                       | <b>{10.0}</b> | <b>{00.2}</b> | <b>{10.1}</b> | <b>{10.2}</b> |
|--|---------------|---------------|---------------|---------------|
| $\epsilon_{hk.l}^{res}$ (×10 <sup>-6</sup> ) | 91 ± 38       | $22 \pm 50$   | $-57 \pm 40$  | $-62 \pm 46$  |
| {hk.l}                                       | <b>{11.0}</b> | {10.3}        | {11.2}        | {20.1}        |
| $\epsilon_{hk.l}^{res}$ (×10 <sup>-6</sup> ) | $-40 \pm 38$  | $64 \pm 48$   | $-55 \pm 42$  | -116 ± 39     |

446

447 Similar order of magnitude is also found along TD. This indicates that the maximum 448 deviation is equivalent to a strain of  $120 \times 10^{-6}$ , and thus corresponds to initial residual 449 stresses below 10 MPa.

The as-received cold rolled sheet used in this study has already been studied in previous work [15]. Analysis of the residual stress obtained from  $\{30.2\}$  and  $\{21.3\}$  reflections have then shown values between  $-10 \pm 35$  MPa and  $+12 \pm 24$  MPa along the rolling direction. The stress values along the TD are also in the same order of magnitude. Eventually, the two samples N and S display rather low residual stress values and latter do not play, *a priori*, a significant role on the elastoplastic behavior. For this reason, initial residual strains / stresses in the asreceived material were not accounted for in the model.

457 4. 1 Neutron diffraction results

The EPSC model developed in the section 3 is used here to simulate the mechanical behavior of the CP Ti- $\alpha$  alloy. Experimental and predicted macroscopic responses of the N-sample under uniaxial tensile test along the extrusion direction (or LD) is shown Fig. 10.a.

The plastic slope predicted by the model is in good agreement with that measured up to 5 %
macroscopic strain. The calculated value of the Young's modulus of 107 GPa is close to the

463 experimental one equal  $102 \pm 1$  GPa. This is consistent with the values commonly found in 464 the literature [69].



466 Fig. 10: Experimental and simulated macroscopic stress–strain curves in a) neutron and b)
467 synchrotron diffraction experiments

Fig. 11 shows the predicted relative activity of each deformation mode considered in the simulation. The experimental macroscopic yield stress is about 280 MPa corresponding to 0.29 % total strain. The adjusted CRSS values are consistent with the EBSD analyses of Barkia et al. [67] with the following order:  $P(a) - \Pi_1(a) - B(a) - \Pi_1(c + a) - ctw$ -{11.2}.

472



473

474 **Fig. 11**: Relative contribution of each deformation mode to the total plastic deformation as a

475

function of deformation during neutron diffraction experiments

The main deformation mode is prismatic slip. For example, at 3 % macroscopic total strain, the proportions of activated systems are: 39 % for prismatic slip, 13 % for basal slip, 25 % for pyramidal (a) slip, 18 % for pyramidal (c + a) and 3.5 % for {11.2} twinning.

This activation sequence (Fig. 11) will influences the behavior of the polycrystal at the local 479 level (i.e. at the diffracting volume level). Then, it is interesting to see its impact on the 480 different mechanical states of {hk.l} grain families. To illustrate this, the evolution of residual 481 intergranular strains is shown in Fig. 12 for both longitudinal (loading direction) and 482 transversal directions. When a polycrystalline aggregate is subjected to a tensile test in the 483 elastic region, the lattice strains develop linearly with the load up to the micro-yielding point. 484 485 There is a significant difference in the elastic response for each {hk.l} grain family due to the elastic anisotropy and the range of possible crystallographic orientations. Slip activity is 486 initiated in plasticity regime in some grains similarly orientated. One can notice the 487 accommodation of the imposed plastic deformation and these grains undergo less loads. 488

489 The neutron experiments results shown in Fig. 12 clearly highlight an anisotropic mechanical490 behavior of {hk.l} groups of grains.

According to the simulations, plasticity initiation begins with the yielding of  $\{10.0\}_{//}$  grains at 260 MPa (corresponding to 0.24 % of total strain). Theses grains are favorably oriented for prismatic slip P(a), the lowest-CRSS mechanism, correlated with a favorable Schmid factor (i.e. 0.5) for these orientations [4,6,67]. Indeed, the grains that activate the prismatic slip first and most easily are those which have their lattice crystalline  $\vec{c}$ -axis perpendicular to the loading direction. These grains undergo plastic deformation below the macroscopic yield stress (R<sub>E</sub> = 280 MPa). It should be recalled that the outset of microplasticity does not cause the macroscopic yield because slip activity is initiated in a small number of grains. As the applied stress increases,  $\{20.1\}_{//}$  orientation begins to shed load at 300 MPa. This can be explained by the activation of pyramidal slip  $\Pi_1(a)$ . The  $\{10.1\}_{//}$  and  $\{10.2\}_{//}$  orientated grains yield at 330 MPa, reflecting the high activity of the basal slip (~ 45 % of activity proportion).





Fig. 12: Residual experimental (symbols) and predicted (lines) lattice strain evolution in both
 (a) longitudinal and (b) transversal directions versus applied stress during neutron diffraction
 experiments.

507 One can notice the linear deviation of the hardest  $\{11.2\}_{//}$  grains (Fig. 12) with a change in 508 relative activity between prismatic P(a) and basal B(a) slips (Fig. 11). Other orientations such

as  $\{10.3\}_{//}$  and  $\{00.2\}_{//}$  yield only at 355 MPa with the activation of the pyramidal mode 509  $\Pi_1(c + a)$  or {11.2} twinning deformation. These {hk.l}// grains have the  $\vec{c}$ -axis nearly 510 aligned along the LD and they are poorly orientated for the soft  $\langle a \rangle$  slip mechanism to be 511 activated. In the LD, the largest compressive residual strains are observed for  $\{10.1\}_{//}$  and 512  $\{20.1\}_{//}$  grains (~ -620 µɛ and ~ -399 µɛ at 5 % of total strain, respectively). Similar 513 behaviors can be seen along  $\{10.0\}_{//}$ ,  $\{10.2\}_{//}$  and  $\{11.0\}_{//}$  orientations, although the lattice 514 strains are relatively smaller: ~ -246  $\mu\epsilon$ , ~ -312  $\mu\epsilon$  and ~ -183  $\mu\epsilon$ , respectively. These 515 behaviors are well captured by the model except for  $\{10.2\}_{//}$  orientation where a shift of 335 516 517 με can be noticed between the experimental and simulated results. As shown in Fig. 12.a, the  $\{00.2\}_{//}$  grain orientation develops significant tensile residual lattice strains (~ 760 µE) during 518 the first 1 % of total strain. This indicates that the load is redistributed towards the plastically 519 harder grains like the  $\{00.2\}_{//}$  ones after the initiation of plasticity. This phenomenon is 520 521 expected since all these grains are poorly orientated for the soft (a) slip mechanisms. A similar behavior is observed for the  $\{10.3\}_{//}$  grains orientation relatively close to the  $\{00.2\}_{//}$ 522 one, although the experimental lattice strains are relatively smaller: 570 µE. This set of grains 523 is also unfavorable to (a) slips. Their residual strain evolution is well described by the 524 numerical simulations. 525

In the TD (Fig. 12.b), the model predicts the evolution of intergranular strains in the majority of the {hk.1} orientations studied even if some discrepancies are observed. All {hk.1} $_{\perp}$  grains present an opposite behavior to that observed in the longitudinal direction, highlighting the Poisson effect. The residual lattice strains evolution of {11.0} $_{\perp}$  reflection is under-predicted. A large gap of 450 µε is observed between the experimental and simulated results, beyond 2.3 % of total strain. For {20.1} $_{\perp}$  grains, the model captures the tensile state, although the state is underestimated by ~ 250 µε at 3 % of total strain. Nevertheless, for the majority of 533 orientations, in particular:  $\{10.0\}_{\perp}$ ,  $\{00.2\}_{\perp}$ ,  $\{10.1\}_{\perp}$ ,  $\{10.2\}_{\perp}$ ,  $\{10.3\}_{\perp}$  and  $\{11.2\}_{\perp}$ , the predictions are fairly accurate with the exception of the  $\{11.0\}_{\perp}$  reflection. Therefore, one can 534 only to conclude that the difference could not be attributed to a lack of description of the 535 hardening. In our opinion, this difference could be explained by the presence of 536 heterogeneities in the set of grains participating to this orientation or by the reverse plasticity 537 when the material is subjected to reverse loading. The differences between model calculations 538 and measurements are more pronounced than in the {hk.l}// grains. Similar observation has 539 been made in previous studies [13,48]. 540

#### 541 4.2 Synchrotron diffraction results

In contrast to neutron diffraction experiments, in situ synchrotron measurements have been 542 performed during a continuous tensile test. Fig. 10.b shows the experimental and predicted 543 544 bulk response. The simulated results describe with accuracy the elastic and plastic slopes up to 4 % macroscopic strain. The calculated Young's modulus of 107 GPa is very close to the 545 546 experimental one of  $109 \pm 2$  GPa. These values are consistent with those found in the neutron 547 diffraction analysis. This proves that the model parameters allow to describe the elastic behavior of the material, suggesting that the elastic constants used in the modeling are quite 548 reasonable with a well-described crystallographic texture. The yield stress is 240 MPa with 549 the prismatic slip P(a) as the main deformation mode (Fig. 13). 550



551

Fig. 13: Relative activities of the different active deformation modes for uniaxial tensile
loading during synchrotron diffraction experiments

Its initial CRSS value (110 MPa, see Table 3) is consistent with that found for N-sample and more generally with  $\alpha$ -titanium [64–68].

Concerning the prediction of lattice strain evolution, only the results obtained in the 556 longitudinal direction were retained. Indeed, for a given {hk.l}// reflection, all diffracting 557 grains have the same orientation of the  $\vec{c}$ -axis with respect to the tensile direction. They have 558 more-or-less the same deformation history and the Schmid factors for each deformation 559 system are the same for these grains. The grains which participate in the  $\{hk.l\}_{\perp}$  reflection 560 have a wide range of crystallographic orientations with respect to the loading axis. In other 561 562 words, a rotation of a grain around an axis perpendicular to the loading direction highly 563 changes the stiffness in the tensile direction and, consequently, the strain and stress state in the grain. The lattice strain of the diffracting grains, for the considered {hk.l} reflection, shows 564 large variation. 565

The mechanical response in the TD is very sensitive to the texture and the elastic strain measured is thus the average over a set of diffracting grains with different strain history. Many authors have already pointed out this problem [11,13,70,71]. This can explain the more pronounced discrepancies noticed between calculations and measurements in the direction perpendicular to the tensile axis in the section 4. 1. Moreover, the number of diffracting grains in X-ray synchrotron experiments is weak as compared to neutron diffraction experiments due to the reduced gauge volume. Therefore, the lattice strains determined with synchrotron X-ray radiation are less representative of the polycrystal due to a smaller number of crystallites contributing to the diffracting volume.

575 The comparison with the homogenization approach is then more problematic especially in the TD. In the LD, this problem remains present but, for a given  $\{\mathbf{hk}, \mathbf{l}\}_{//}$  reflection, all the grains 576 have an identical lattice plane normal in a direction parallel to the tensile axis with a very 577 similar mechanical state for these grains in plasticity. The range of lattice strains for all grains 578 579 in the diffracting volume along the longitudinal direction is lower than the range of the strains for the transverse direction within a given {hk.l} family. This compensates somehow the lack 580 of statistics met with the gauge volume. Therefore, the focus is made on the internal strain 581 evolution in the LD. The lattice strain evolution is reasonably predicted along LD (Fig. 14). In 582 the elastic regime, a linear evolution is observed whose slope depends on the grain family due 583 to the elastic anisotropy, each group of grains shows a more or less stiff behavior. 584





Fig. 14: Experimental (symbols) and predicted (lines) lattice strain evolution along LD for
tensile test during synchrotron diffraction experiments

For example,  $\{10.0\}_{//}$  grains family, which exhibit the most compliant behavior with the lowest elasticity modulus  $E_{hk.l}$  (Table 5), accumulate the largest elastic lattice strains as compared to those met for  $\{1.01\}_{//}$  and  $\{10.2\}_{//}$  reflections. The elastic modulus  $E_{hk.l}$  are very well predicted by the model.

**Table 5:** Measured and predicted elastic modulus  $E_{hk,l}$  (GPa) for different reflections {hk. l}//

| {10.0} | {10.1} | {10.2} | {11.0} |
|--------|--------|--------|--------|
|        |        |        |        |

| Experimental | $93 \pm 0.8$  | $103.2 \pm 1$ | $104.2 \pm 1.8$ | $97.8 \pm 1.4$ |
|--------------|---------------|---------------|-----------------|----------------|
| Model        | 92.2          | 102.5         | 105.8           | 98.6           |
|              | {10.3}        | {11.2}        | <b>{20.1}</b>   | -              |
| Experimental | $113.6 \pm 2$ | $104 \pm 1$   | $100 \pm 1.4$   | _              |
| Model        | 112.3         | 103.8         | 101.6           | _              |

593

In general, the simulations exhibit a reasonable agreement with the experiment in terms of 594 both trends and magnitudes. The relative activities of the deformation modes are plotted in 595 Fig. 13. The  $\{10.0\}_{//}$  and  $\{11.0\}_{//}$  grain families yield first at 240 MPa. Such micro-yielding 596 is correctly reproduced by the model, and it is clear that this first inflection is induced by the 597 activation of prismatic slip P(a). At 260 MPa, the  $\{20.1\}_{//}$  and  $\{10.1\}_{//}$  grain families begins 598 to shed load due to the activation of pyramid slip  $\Pi_1(a)$ . A third inflection taking place at 306 599 MPa is observed for the  $\{10.2\}_{//}$  and  $\{11.2\}_{//}$  orientations. This inflection is a result of the 600 activity of basal slip B(a). A significant load partitioning takes place later in {10.3}// grains, 601 and is associated with the noteworthy activity of pyramidal  $\Pi_1(c + a)$ . This slip mode 602 becomes very quickly the major slip system governing the material plasticity until 4 % of the 603 604 total strain (Fig. 13).

The effect of crystallographic texture difference between N- and S-samples is clearly visible in the evolution of relative activities of the different active deformation systems. In the Nsample, the majority of the grains have the  $\vec{c}$ -axis nearly perpendicular to the loading axis and they are favorably oriented for the prismatic slip P(a) while in the S-sample, the rolling texture induces the significant activity of pyramidal  $\Pi_1$ (c + a) (see Fig. 11 and Fig. 13). At ~ 365 MPa, the lattice strain relief in the {10.0}// grains is caused by the {10.2} tensile twinning inducing a stress relaxation. This observation has been made in previous works [71– 612 73], and is well captured by the simulations. It is noted that {11.2} compressive twinning
613 during the deformation is almost negligible, which is consistent with the initial
614 crystallographic texture of the S-sample (Fig. 7).

615 For diffraction measurements, the residual strains usually show poorer agreement between measurements and simulation results than the in situ strains measured under a mechanical 616 617 load. This can be explained by the fact that the model does not take into account slip activity [70] or twinning-detwinning [74] one during unloading (i.e the reverse plasticity, when the 618 material is subjected to reverse loading, is not predicted by the model). The experimental 619 macroscopic stress-strain curves show actually a slight reverse plasticity during the unloads, 620 especially for large macroscopic strain values (see Fig. 10), for stress values close to zero. 621 Some discrepancies between the model predictions and the measurements could therefore be 622 623 expected. Despites this limitation, residual strain evolution is well described by the numerical simulations for the majority of {hk.l} orientations along the LD and TD (see Fig. 12). The 624 observed discrepancies ( $\{10.2\}_{//}, \{11.0\}_{\perp}$  for example) between the model predictions and the 625 measurements could be partially explained by this lack of description. On the other hand, the 626 627 main limitation of synchrotron is the small gauge volume resulting in a limited number of 628 diffracting grains for a given reflection and an exacerbated sensitivity of the results to spatial heterogeneities. The comparison with a homogenization approach becomes then more 629 630 problematic. In our study, in order to overcome this problem, only longitudinal strains have been analyzed and intensity of each diffraction ring has been integrated within "cake shape" 631 sectors defined by  $\beta \pm 10^{\circ}$ . The arithmetic mean values of the d-spacings were subsequently 632 calculated from the averaging of the symmetrically equivalent  $\gamma$  and  $\gamma$  + 180° angles (see 633 section 2.3). Moreover, the ratios between the CRSS of the different deformation modes with 634 respect to the one of the P(a) family are in agreement with the ranges identified with neutron 635 diffraction. These results are in accordance with those obtained, for example, by Barkia et al. 636

[67] by TEM (slip trace analysis) or Amouzou et al. [68] with an EVPSC model. The same
activation sequence combination has been used for these two experiments. Therefore, we can
deduce that the longitudinal lattice strains determined with synchrotron X-ray radiation are
representative due to a sufficient number of crystallites contributing to the diffracting volume
for the LD.

642 Nevertheless, due to the crystallographic texture, the activity rates for the different643 deformation modes are not the same according to the samples of this study.

#### 644 5. Conclusion

In this work, the evolution of lattice strains and texture under mechanical loading in  $\alpha$ -Ti alloy has been examined using two different techniques: neutron and X-ray synchrotron diffractions. These results have been compared with the prediction of EPSC model and the elastoplastic deformation has been studied at the different scales. The major conclusions are summarized as below:

> An extended EPSC model taking into account twin domain reorientation and 650 associated stress relaxation has been developed. On the basis of this study, the relative 651 652 activity of slip and twinning deformation modes occurring in the samples have been determined and analyzed. By tuning the hardening coefficient and the initial CRSS, it 653 is shown that the model predictions, in terms of lattice strain evolution (8 and 7 654 different reflections for neutron and synchrotron diffraction, respectively) and 655 macroscopic stress-strain curves are in good agreement with the experimental data. 656 The lattice strain relief caused by the twinning is well captured by the simulations. 657

Our work highlights the strong crystallographic texture effect onto the deformations
 mechanisms activation sequence of N- and S-samples. In the N-sample, the majority
 of the grains have the c-axis nearly perpendicular to the loading axis and they are

favorably oriented for the prismatic slip P(a) (and for the tensile twinning  $\{10.2\}(10,\overline{1})$ ) while in the S-sample, the rolling texture induces the significant activity of pyramidal  $\Pi_1(c + a)$ .

> X-ray synchrotron source offers fast rates of data acquisition (few seconds for X-rays 664 and about 40 minutes for neutron diffraction in this work) enabling real time and in 665 situ strain distribution measurements during continuous mechanical loading. Despite a 666 667 small irradiated volume for X-rays, the inflections of {hk.l} orientations due to the slip or twinning deformation modes are relatively well reproduced by the model. This 668 669 agreement is only obtained in the LD with intensity of each diffraction ring has been integrated within "cake shape" sectors defined by  $\beta \pm 10^{\circ}$ . The arithmetic mean values 670 of the d-spacings were calculated from the averaging of the symmetrically equivalent  $\gamma$ 671 and  $\gamma + 180^{\circ}$  angles. 672

The advantage of neutron diffraction techniques is notably related to a substantial and
representative scattering volume of 4 × 4 × 4 mm<sup>3</sup>. Despite the fact that the model
does not take into account slip activity or twinning-detwinning one during unloading,
residual strain evolution is well described by the numerical simulations for the
majority of {hk.l} orientations along LD and TD.

Free comparison between the extended EPSC model with *in situ* or *post mortem* characterization give the same trends: the  $\langle a \rangle$  slip on prismatic planes is the easiest deformation mechanism. Pyramidal  $\langle a \rangle$  slip is the second easiest and basal  $\langle a \rangle$  slip the third.  $\langle c + a \rangle$  slip is regarded as more difficult than  $\langle a \rangle$  slip mechanisms which result in twinning to accommodate strain along the  $\vec{c}$ - axis.

683

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