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Generic Approach for Hierarchical Modulation Performance Analysis: Application to DVB-SH

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Abstract—Broadcasting systems have to deal with channel diversity in order to offer the best rate to the users. Hierarchical modulation is a practical solution to provide several rates in function of the channel quality. Unfortunately the performance evaluation of such modulations requires time consuming simulations. We propose in this paper a novel approach based on the channel capacity to avoid these simulations. The method allows to study the performance in terms of spectrum efficiency of hierarchical and also classical modulations combined with error correcting codes. Our method will be applied to the DVB-SH standard which considers hierarchical modulation as an optional feature.

I. INTRODUCTION

In most broadcast applications, the receivers do not experience the same signal-to-noise ratio (SNR). For instance, in satellite communications the channel quality decreases with the presence of clouds in Ku or Ka band or with shadowing effects of the environment in lower bands.

The first solution for broadcasting is to design the system for the worst-case reception. However this solution does not take into account the variability of channel qualities. This holds a loss of spectrum efficiency for users with good reception. Then two other schemes have been proposed in [1] and [2] to improve the first one: time division multiplexing with variable coding and modulation, and superposition coding. Time division multiplexing consists in using a first couple modulation/coding rate during a fraction of time, and then using an other modulation/coding rate for the remaining time. All the population can receive the first part of the signal called the High Priority (HP) signal and only the receivers in good conditions receive the second one called the Low Priority (LP) signal.

Unlike time sharing, superposition coding sends information for all the receivers all the time and it was proved to achieve better rates than time sharing for the continuous Gaussian channel [2]. In superposition coding the available energy is shared to several service flows which are sent simultaneously and in the same band. Hierarchical modulation is a practical implementation of superposition coding. Figure 1 presents the principle of the hierarchical modulation using a non-uniform

16-QAM. The idea is to merge two different streams at the modulation step. The HP stream is used to select the quadrant, and the LP stream selects the position inside the quadrant. In good conditions receivers can decode both streams, unlike bad receivers which only locate the quadrant and then decode the HP stream as a QPSK constellation.

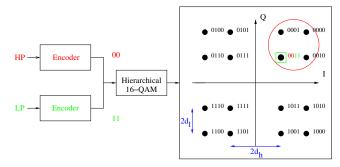


Fig. 1: Hierarchical Modulation using a non-uniform 16-QAM

In practical contexts, both schemes can be used combined with applications generating hierarchical flows, like H.264/SVC video [3], [4].

Satellite communications standards like DVB-S2 [5] and DVB-SH [6] consider hierarchical modulation as an optional feature. To our knowledge, the only way to estimate the performance of real code using hierarchical modulation is to run simulations. We propose here a new approach to evaluate the performance of such modulation. The method is based on the channel capacity and relies on the fact that the real code at coding rate \tilde{R} works as a theoretical ideal code at coding rate \tilde{R} . Our approach is applied to DVB-SH.

The paper presents our work as follows:

- In Section II we compute the capacity for any hierarchical modulation.
- We propose a method using the capacity to evaluate the performance of hierarchical modulations in terms of spectral efficiency and required E_s/N_0 for a targeted Bit Error Rate (BER) or Packet Error Rate (PER) in Section III.

Section IV concludes the paper by summarizing the results and presents the future work.

II. CAPACITY OF THE HIERARCHICAL MODULATION

In this section we introduce the channel capacity and compute it for any hierarchical modulation. Some results are given at the end of this section using the hierarchical 16-QAM.

A. Computation of the capacity

A channel can be considered as a system consisting of an input alphabet, an output alphabet and a transition matrix p(y|x). We define two random variables X, Y representing the input and output alphabets respectively. The mutual information between X and Y, noted I(X;Y), measures the amount of information conveyed by Y about X. For two discrete random variables X and Y, (1) gives the expression of the mutual information. It can be extended to continuous random

$$I(X;Y) = \sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x)p(y|x) \log_2 \left(\frac{p(y|x)}{p(y)}\right). \tag{1}$$

Using this notion, the channel capacity is then given by

$$C = \max_{p(x)} I(X;Y), \tag{2}$$

where the maximum is computed over all possible input distributions.

Here we consider the memoryless discrete input and continuous output Gaussian channel. The discrete inputs x_i are obtained using a modulation and belong to a set of discrete points $\chi \subset \mathbb{R}^2$ of size $|\chi| = M = 2^m$ called the constellation. Thus, each symbol of the constellation carries m bits. An explicit formula (3) for the capacity in this particular case is given in [8, Chapter 3].

$$C = \log_2(M) - \frac{1}{M} \sum_{i=1}^{M} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} p(\mathbf{y}|\mathbf{x}_i) \log_2\left(\frac{\sum_{j=1}^{M} p(\mathbf{y}|\mathbf{x}_j)}{p(\mathbf{y}|\mathbf{x}_i)}\right) d\mathbf{y}(3)$$

We are now interested to evaluate the capacity of a stream using a subset of all the bits. Reference [9] presents the case where each stream uses one bit. The idea is to modify the input random variable X by the input bits used in each stream. We define b_i as the value of the ith bit of the label of any constellation point x. Suppose the stream uses k bits among m in the positions $i_1, ..., i_k$. For any integer i, let $l_n(i)$ denote the nth bit in the binary representation of i such as $i = \sum_{n=1}^{+\infty} l_n(i) 2^{n-1}$. Then using (1) with the new input variable and continuous output, the capacity of the stream is

$$C = \frac{1}{2^k} \sum_{i=0}^{2^k - 1} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \underbrace{p(\mathbf{y}|b_{i_1} = l_1(i), \dots, b_{i_k} = l_k(i))}_{\text{sum over all possible k-uplets}}$$
$$\log_2 \left(\frac{p(\mathbf{y}|b_{i_1} = l_1(i), \dots, b_{i_k} = l_k(i))}{p(\mathbf{y})} \right) d\mathbf{y}, \quad (4)$$

where $p(\mathbf{y}) = \frac{1}{2^k} \sum_{i=0}^{2^k-1} p\left(\mathbf{y} | b_{i_1} = l_1(i), ..., b_{i_k} = l_k(i)\right)$. Let $L_n(\mathbf{x})$ denote the nth bit of the label of \mathbf{x} . We introduce

 χ_i the subset of χ defined as follows

$$\chi_i = \{ \mathbf{x} \in \chi | L_{i_1}(\mathbf{x}) = l_1(i), ..., L_{i_k}(\mathbf{x}) = l_k(i) \}.$$
 (5)

The set χ_i depends on i and the positions of the bits involved in the stream. Figure 2 shows an example of subsets for a 16-QAM with a particular mapping, where the stream uses bits in position 1 and 2 (in that case k = 2, $i_1 = 1$ and $i_2 = 2$).

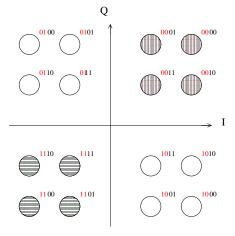


Fig. 2: Examples of χ_0 (vertical lines) and χ_3 (horizontal lines)

Then the conditional probability density function of y in (4) can be written

$$p(\mathbf{y}|b_{i_1} = l_1(i), ..., b_{i_k} = l_k(i)) = \sum_{\mathbf{x} \in \chi_i} p(\mathbf{y}|\mathbf{x})p(\mathbf{x}|\mathbf{x} \in \chi_i)$$
$$= \frac{1}{|\chi_i|} \sum_{\mathbf{x} \in \mathcal{X}} p(\mathbf{y}|\mathbf{x}), \qquad (6)$$

where $|\chi_i|=2^{m-k}$ for all i. Moreover, the transition distribution $p(\mathbf{y}|\mathbf{x})$ for a Gaussian channel is

$$p(\mathbf{y}|\mathbf{x}) = \frac{1}{\pi N_0} \exp\left(-\frac{\|\mathbf{y} - \mathbf{x}\|^2}{N_0}\right). \tag{7}$$

Using (6) and (7) in (4), we finally obtain the capacity for one stream (8). The capacity is an increasing function of E_s/N_0 and its value is less or equal to k the number of bits used in the stream. The positivity of the capacity results of its mathematical definition [7].

$$C = k - \frac{1}{2^{k}\pi} \sum_{i=0}^{2^{k}-1} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \left(\frac{1}{|\chi_{i}|} \sum_{\mathbf{x} \in \chi_{i}} \exp\left(\left\| \mathbf{u} - \frac{\mathbf{x}}{\sqrt{N_{0}}} \right\|^{2} \right) \right)$$
$$\log_{2} \left(1 + \frac{\sum_{\mathbf{x} \in \chi \setminus \chi_{i}} \exp\left(\left\| \mathbf{u} - \frac{\mathbf{x}}{\sqrt{N_{0}}} \right\|^{2} \right)}{\sum_{\mathbf{x} \in \chi_{i}} \exp\left(\left\| \mathbf{u} - \frac{\mathbf{x}}{\sqrt{N_{0}}} \right\|^{2} \right)} \right) d\mathbf{u}$$
(8)

We begin with few definitions before applying (8) to the hierarchical 16-QAM considered in DVB-SH.

Hierarchical modulations merge several streams in a same symbol. They often use non-uniform constellation. Non-uniform constellations are opposed to uniform constellations where the symbols are uniformly distributed. The constellation parameter is defined to describe non-uniform constellations. Figure 1 illustrates a non-uniform 16-QAM. The constellation parameter α is defined by $\alpha = d_h/d_l$ where $2d_h$ is the minimum distance between two constellation points carrying different HP bits and $2d_l$ is the minimum distance between any constellation points. Thus α verifies $\alpha \geq 1$ where $\alpha = 1$ corresponds to the uniform 16-QAM. The DVB-SH standard [10] recommends two values for α : 2 and 4.

Back to the hierarchical modulation capacity, we suppose the HP stream uses the bits in position 1 and 2. The LP stream involves the remaining bits, i.e., bits 3 and 4. Figures 3 and 4 present the 16-QAM capacity for the two values of α defined in the DVB-SH guidelines [10].

When α grows, the constellation points in each quadrant become farer to the I and Q axes. Thus it is easier to decode the good quadrant and the capacity for the HP stream increases. However in the same quadrant, the points gets closer and the capacity for the LP stream decreases as it is harder to decode which symbol was sent. Concerning the HP stream capacity, it increases with α but nevertheless it is limited by the QPSK capacity as the same energy is used for 16 points instead of 4.

To conclude, we can observe that the global hierarchical modulation capacity (i.e. HP+LP) is always less than the 16-QAM capacity for any value of $\alpha>1$. This result has been proved in [9] where the different streams use one bit. We can also note that the best total capacity is achieved when the constellation is close to the uniform constellation, but on the other hand performances for the HP stream are decreased.

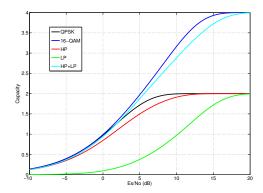


Fig. 3: 16-QAM Hierarchical Modulation Capacity - $\alpha = 2$

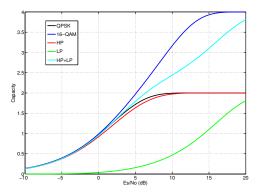


Fig. 4: 16-QAM Hierarchical Modulation Capacity - $\alpha = 4$

III. PERFORMANCE EVALUATION FOR HIERARCHICAL MODULATIONS

We present in this part a method to get easily the spectrum efficiency and the required E_s/N_0 for a given targeted BER/PER for any modulation and coding rate without computing extensive simulations. In [11] a fast coding/decoding performance evaluation method based on the mutual information computation is proposed and applied to time varying channel for QPSK modulation with very good prediction precision. The method developped hererafter based on channel capacity computation makes it possible to predict the performances of a coding scheme combined with any modulation and especially any hierarchical modulation.

A. Principle

- 1) Ideal code: Before applying the approach to a real code, we begin with an example using theoretical ideal codes achieving the channel capacity. The normalized capacity for a modulation is defined by $\overline{C}_{mod} = \frac{1}{m} C_{mod}$ where C_{mod} is the modulation's capacity and m denotes the number of bits per symbol. The \overline{C}_{mod} function has some properties:
 - It is an increasing function of E_s/N_0 .
 - It verifies $0 \le C_{mod} \le 1$.
 - It is equivalent to the notion of coding rate when using ideal codes.

Given a modulation and a coding rate, if we want to know at which E_s/N_0 the code is able to decode, we just need to inverse the normalized capacity function for that coding rate. Figure 5 illustrates this example using a QPSK.

2) Real code: Let us now consider an actual waveform based on a real code. We can consider that the real code at a coding rate R works as an ideal code with rate \tilde{R} where $\tilde{R} \geq R$. Determining \tilde{R} requires a performance curve (BER or PER vs E_s/N_0) for one actual reference modulation and coding scheme with code rate R. The performance curve allows to estimate the behaviour of the code. We illustrate our method with an example. We would like to study the hierarchical modulation using an non-uniform 16-QAM ($\alpha=2$) in the DVB-SH standard at a target BER of 10^{-5} . We use the 2/9 and 1/5-turbo codes for the HP and LP streams respectively. To

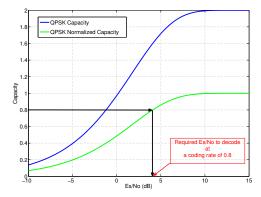


Fig. 5: Decoding threshold for a coding rate of 0.8

determine \tilde{R} and the decoding thresholds, the method works as follow:

1) Use the performance curve of the reference modulation with rate R to get the operating point $(E_s/N_0)_{ref}$ corresponding to the desired performance. In the DVB-SH guidelines [10, Table 7.5], we read:

For the coding rate 2/9,
$$BER_{QPSK}(-3.4dB) = 10^{-5}$$

For the coding rate 1/5, $BER_{QPSK}(-3.9dB) = 10^{-5}$

2) Compute the normalized capacity for the reference modulation which corresponds to \tilde{R} :

For the HP stream,
$$\tilde{R} = \overline{C}_{\text{QPSK}} (-3.4 \text{dB}) \approx 0.27$$

For the LP stream, $\tilde{R} = \overline{C}_{\text{OPSK}} (-3.9 \text{dB}) \approx 0.25$

3) For the studied modulation, compute E_s/N_0 such as the normalized capacity at this SNR equals \tilde{R} :

$$\begin{array}{lcl} \left(E_s/N_0\right)_{HP} & = & \overline{C}_{{\rm HP},\alpha=2}^{-1} \left(\tilde{R}=0.27\right) = -2.7 {\rm dB} \\ \\ \left(E_s/N_0\right)_{LP} & = & \overline{C}_{{\rm LP},\alpha=2}^{-1} \left(\tilde{R}=0.25\right) = 6.2 {\rm dB} \end{array}$$

The DVB-SH guidelines provide the decoding thresholds for the HP and LP streams [10, Figure 7.40]. Less the 0.3dB due to the pilots, we read -2.6dB and 6.2dB for the HP and LP streams respectively.

4) Finally the points $((E_s/N_0)_{HP}, R_{HP} \times m)$ and $((E_s/N_0)_{LP}, R_{LP} \times m)$ are plotted on the spectrum efficiency curve (e.g., Figure 7 and 8).

These steps are repeated for all the coding rates. Our method makes two assumptions. First of all, it approximates the information rate by $R \times m$. This approximation is justified by the fact that the targeted performance (BER = 10^{-5}) is very small and thus only hardly impact the useful information rate.

The second assumption is to suppose as in [11] that the performance of the decoding only depends on the normalized capacity and not on the modulation as for ideal codes. To validate this second assumption, Figure 6 presents the normalized capacity in function of the coding rate for various modulations using the data of DVB-SH [10, Table 7.5]. We can

remark that for a given coding rate, the normalized capacities for each modulation are closed. We will see that the small difference between the normalized capacities does not have a great impact on our results. Moreover, Figure 6 also shows the DVB-SH codes are closed to the Shannon limit (continuous line).

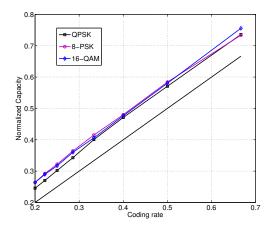


Fig. 6: DVB-SH: normalized capacities

B. Application to DVB-SH

In our study, we use the guidelines of DVB-SH [10, Table 7.5] to get the reference curves and the operating points at a target BER of 10^{-5} . These data correspond to a static receiver. The guidelines also provide all the reference numerical results for the hierarchical modulation [10, Figure 7.40] where 0.3dB need to be removed due to the pilots. Thus it allows to evaluate the efficiency of our method.

The method described earlier is now applied to plot the spectrum efficiency curves as a function of required E_s/N_0 (target BER = 10^{-5}). Figures 7 and 8 present the results for $\alpha=2$ and $\alpha=4$ respectively. The reference results from the guidelines correspond to the standard curves. The results show a good precision and it does not require computing extensive simulations. Moreover, our work consolidates the fact that the capacity is a good metric to evaluate performance.

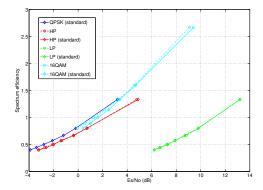


Fig. 7: DVB-SH spectrum efficiency, $\alpha = 2$, BER = 10^{-5}

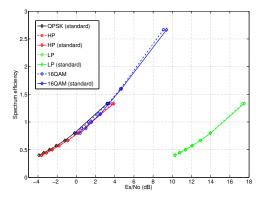


Fig. 8: DVB-SH spectrum efficiency, $\alpha = 4$, BER = 10^{-5}

C. DVB-SH: Additional Results

We apply hereafter the method to compute the required E_s/N_0 in function of α or the coding rate.

Figures 9 and 10 present how the required E_s/N_0 varies with α . For the LP stream, the required E_s/N_0 is an increasing function of α , unlike the one for the HP stream who decreases. In fact the required E_s/N_0 for the HP stream tends to the required SNR of the QPSK modulation. These results are obvious when we look the modification of the constellation with α . When α increases, the points in one quadrant become closer and the constellation is similar to a OPSK. It explains why the LP stream is harder to decode and requires a better SNR.

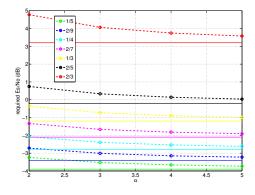


Fig. 9: Required E_s/N_0 function of α , HP Stream, BER = 10^{-5}

The last point concerns the variation of the required E_s/N_0 with the coding rate. It is presented on Figure 11 for $\alpha =$ 2. Obviously, if there is less redundancy, the SNR has to be higher to decode.

All these results are helpful during the dimensioning of a broadcast system. If the operator knows the SNR distribution of the receivers, it is possible to optimize the choice of the constellation parameter or the coding rate for each stream.

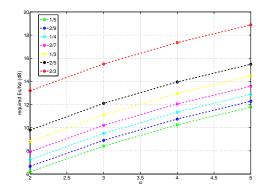


Fig. 10: Required E_s/N_0 function of α , LP Stream, BER =

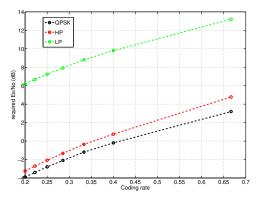


Fig. 11: Required E_s/N_0 function of the coding rate, $\alpha=2$

IV. CONCLUSION

In this paper, we introduce a general method allowing to analyse the performance of hierarchical modulations. This method relies on the channel capacity which has been computed for any kind of constellation. It has been applied to DVB-SH in order to obtain the spectrum efficiency. The comparisons with reference simulation results show the good reliability of the method.

Future work will improve the comparison between hierarchical modulation and time sharing. We also plan to take into account the mobility in the context of DVB-SH. Finally we will apply our method to DVB-S2 and other standards including hierarchical modulation to complete the study.

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