

Programmable frequency-bin quantum states in a nano-engineered silicon device

Marco Clementi, Federico Andrea Sabattoli, Houssein El Dirani, Laurene Youssef, Massimo Borghi, Linda Gianini, Noemi Tagliavacche, Nicola Bergamasco, Camille Petit-Etienne, Erwine Pargon, et al.

▶ To cite this version:

Marco Clementi, Federico Andrea Sabattoli, Houssein El Dirani, Laurene Youssef, Massimo Borghi, et al.. Programmable frequency-bin quantum states in a nano-engineered silicon device. Nature Communications, 2023, 14 (1), pp.176. 10.1038/s41467-022-35773-6. hal-03997028

HAL Id: hal-03997028 https://hal.science/hal-03997028v1

Submitted on 20 Feb 2023 $\,$

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Programmable frequency-bin quantum states in a nano-engineered silicon device

1

2

3	Marco Clementi ^{1,2*†} , Federico Andrea Sabattoli ^{1,3†} , Houssein
4	El Dirani ^{4,5} , Laurene Youssef ^{6,7} , Linda Gianini ^{8,9} , Massimo
5	Borghi ¹ , Noemi Tagliavacche ¹ , Nicola Bergamasco ¹ , Camille
6	Petit-Etienne ⁶ Erwine Pargon ⁶ I E Sine ¹⁰ Marco
-	Liscidini ¹ Corrado Sciancalenore ^{4,11} Matteo Galli ^{1*}
1	and Danielo Rejenti ⁹
8	and Damele Dajom
9	¹ Dipartimento di Fisica, Università di Pavia, Via Agostino Bassi
10	6, 27100 Pavia, Italy.
11	² Current address: Photonic Systems Laboratory (PHOSL), École
12	Polytechnique Fédérale de Lausanne, 1015 Lausanne, Switzerland.
13	³ Current address: Advanced Fiber Resources Milan S.r.L., Via
14	Federico Fellini 4, 20097 San Donato Milanese (MI), Italy.
15	⁴ Univ. Grenoble Alpes, CEA-Leti, 38054 Grenoble, France.
16	⁵ Current address: LIGENTEC SA, 224 Bd John Kennedy, 91100
17	Corbeil-Essonnes, France.
18	⁶ Univ. Grenoble Alpes, CNRS, LTM, 38000 Grenoble, France.
19	⁷ Current address: ENSIL-ENSCI, Centre Européen de la
20	Céramique (IRCER), 12 Rue Atlantis, 87068 Limoges, France.
21	⁸ CEA-LETI, Optics and Photonics Department (DOPT), 17 Rue
22	des Martyrs, 38054 Grenoble, France.
23	⁹ Dipartimento di Ingegneria Industriale e dell'Informazione,
24	Università di Pavia, Via Adolfo Ferrata 5, 27100 Pavia, Italy.
25	¹⁰ Department of Physics, University of Toronto, 60 St. George
26	Street, Toronto, ON, M5S 1A7, Canada.
27	¹¹ Current address: SOITEC SA, Parc technologique des
28	Fontaines, Chemin des Franques, 38190 Bernin, France.
29	*Corresponding author(s). E-mail(s): marco.clementi@epfl.ch;
30	$\mathrm{matteo.galli}@\mathrm{unipv.it};$
31	[†] These authors contributed equally to this work.

Abstract

Photonic qubits should be compatible with easy on-chip manipulation 33 and noise-tolerant transmission over optical networks to find practical 34 use across the whole spectrum of quantum technologies. Furthermore, 35 the source of qubits should grant programmable control over the emit-36 ted state and high brilliance, in order to provide quantum algorithms 37 with resilience to losses. However, encoding schemes demonstrated so 38 far only combine at most two of the aforementioned properties, restrict-30 ing the full potential of photonic quantum technologies. In this work, 40 we finally overcome this hurdle by demonstrating a programmable sil-41 icon nano-photonic chip capable of generating frequency-bin entangled 42 photons, a type of qubit encoding compatible with long-range trans-43 mission over optical links. Our device emits quantum states that can 11 be manipulated using existing telecommunication components, includ-45 ing active devices that can be integrated in silicon photonic technology. 46 Remarkably, our design also overcomes the state-of-art trade-off between 47 brightness and operation bandwidth. As a powerful demonstration, we 48 programmed our chip to generate the four computational basis states, 49 and the four maximally-entangled Bell states, of a two-qubit system. 50 For each state we perform quantum state tomography, confirming high 51 brightness, fidelity, and purity. Such a device combines all the key prop-52 erties of on-chip quantum state reconfigurability and dense integration. 53

⁵⁴ 1 Introduction

Photons serve as excellent carriers of quantum information. They have long 55 coherence times at room temperature, and are the inescapable choice for 56 broadcasting quantum information over long distances, either in free space or 57 through the optical fiber network. Quantum state initialization is a particu-58 larly important task for photonic qubits, since adjusting entanglement after 59 emission is nontrivial. Initialization strategies depend on the degree of freedom 60 used to encode quantum information, and the most common choice for quan-61 tum communication over optical channels is time-bin encoding [1]. Here the 62 two qubit levels consist of the photon being in one of two time windows, gener-63 ally separated by a few nanoseconds. Time-bin encoding is extremely resilient 64 to phase fluctuations resulting from thermal noise in optical fibers, with qubits 65 maintaining their coherence even over hundreds of kilometers [2, 3]. However, 66 the control of the state in which time-bin-entangled photons are generated is 67 challenging, and impractical in emerging nano-photonic platforms. For on-chip 68 manipulation of qubit states, dual-rail encoding, in which the two states of a 69 qubit correspond to the photon propagating in one of two optical waveguides, 70 is a superior strategy [4, 5], and is thus a common choice for quantum com-71 puting and quantum simulation in integrated platforms. Yet this approach is 72 not easily compatible with long-distance transmission links using either optical 73 fibers or free space channels. 74

32

Recently frequency-bin encoding has been proposed, and experimentally 75 demonstrated, as an appealing strategy that can combine the best character-76 istics of time-bin and dual-rail encodings [6-11]. In this approach, quantum 77 information is encoded by the photon being in a superposition of different 78 frequency bands. Frequency bins can be manipulated by means of phase modu-79 lators, and are resistant to phase noise in long-distance propagation. Pioneering 80 studies have investigated the generation and manipulation of frequency-bin-81 entangled photons in integrated resonators. They have considered quantum 82 state tomography of entangled photon pairs [12], qudit encoding [13], and 83 multi-photon entangled states [14]. The experimental results have all been 84 achievable thanks to the recent development of high-Q integrated resonators 85 in the silicon nitride and silicon oxynitride platforms. 86

Despite all this progress, there are obstacles that must be overcome in order 87 to exploit the full advantage of photonic integration. In frequency-bin encod-88 ing today, the generation of photon pairs occurs via spontaneous four-wave 89 mixing in a single ring resonator, with the desired state obtained *outside* the ۵n chip, by means of electro-optical modulators and/or pulse shapers. And since 91 commercial modulators have limited bandwidth, the frequency span separat-92 ing the photons cannot exceed a few tens of gigahertz, which sets a limit to 93 the maximum free spectral range of the resonator. Finally, because sponta-94 neous four-wave mixing efficiency scales quadratically with the resonator free 95 spectral range [15], there is also a significant trade-off between the generation 96 rate and the number of accessible frequency bins. 97

In this work, we show that these limitations can be overcome by utilizing 98 the flexibility of light manipulation in a nano-photonic platform and the dense 99 optical integration possible in silicon photonics. Our approach is based on 100 constructing the desired state by direct, on-chip control of the interference of 101 biphoton amplitudes¹ generated in multiple ring resonators that are coherently 102 pumped. States can thus be constructed "piece-by-piece" in a programmable 103 way, by selecting the relative phase of each source. In addition, since the fre-104 quency bin spacing is no longer related to the ring radius, one can work with 105 very high-finesse resonators, reaching megahertz generation rates. These two 106 breakthroughs, namely high emission rates in combination with high values of 107 the free spectral range, together with output state control using on-chip com-108 ponents, are only possible using multiple rings: they would not be feasible were 109 the frequency bins encoded on the azimuthal modes of a single resonator. 110

We demonstrate that with the very same device one can generate all superpositions of the $|00\rangle$ and $|11\rangle$ states or, in another configuration with different frequency bin spacing, all superpositions of the $|01\rangle$ and $|10\rangle$ states. One needs only to drive the on-chip phase shifter and set the pump configuration appropriately. This means that all four fully-separable states of the computational basis and all four maximally-entangled Bell states $(|\Phi^{\pm}\rangle = (|00\rangle \pm |11\rangle)/\sqrt{2}$ and $|\Psi^{\pm}\rangle = (|01\rangle \pm |10\rangle)/\sqrt{2}$ are accessible. Our high generation rate allows

¹See Supplementary Information for a detailed discussion.

us to perform quantum state tomography of all these states, reaching fidelities
up to 97.5% with purities close to 100%.

¹²⁰ 2 Device characterization and principle of ¹²¹ operation

The device is schematically represented in Fig. 1a. The structure is operated by 122 exploiting the fundamental transverse electric (TE) mode of a silicon waveg-123 uide, with a $600 \times 220 \,\mathrm{nm}^2$ cross section, buried in silica. Two silicon ring 124 resonators (Ring A and Ring B) in all-pass configuration act as sources of 125 photon pairs. Their radii are some 30 µm to ensure high generation rates, and 126 they are not commensurate so that the two free spectral ranges are different: 127 $FSR_A = 377.2 \text{ GHz}$ and $FSR_B = 373.4 \text{ GHz}$, respectively. The two rings are 128 critically coupled to a bus waveguide and their resonance lines can be tuned 129 independently by means of resistive heaters. The device also contains a tun-130 able Mach-Zehnder interferometer (MZI), whose outputs are connected to the 131 input of two tunable add-drop filters that allow one to control the field inten-132 sity and relative phase with which Ring A and Ring B are pumped in the 133 spontaneous four-wave mixing experiment [16]. 134

Linear transmission measurements through the bus waveguide are shown 135 in Figs. 1b-g. In a first configuration (Figs. 1b-d), which we will later refer 136 to as " Φ ", two resonances of Ring A and Ring B are spectrally aligned to be 137 later used for pumping, thus only one transmission dip is observed at 194 THz 138 (1545 nm) in Fig. 1c. Since Ring A and Ring B have different free spectral 139 ranges, the other resonances are not aligned, and one observes double dips, 140 with spacing $\Delta(m) = |m| (\text{FSR}_{\text{A}} - \text{FSR}_{\text{B}})$, with m being the azimuthal order 141 with respect to the pump resonance. In Figs. 1b and d we plot the transmission 142 double dip corresponding to m = -5 and m = +5, named "idler" and "signal", 143 respectively. For both the signal and idler bands the resonances of Ring A 144 and Ring B are separated by $\Delta = 19 \,\text{GHz}$. Later, the two frequencies will 145 be used to encode the two states of the qubits, with signal and idler pairs of 146 frequencies representing the two qubits. For this reason, in Figs. 1b and d, 147 we name $|0\rangle_{si}$ the two frequency bins closer to the pump, and $|1\rangle_{si}$ the two 148 bins further away from the pump, in line with previous works on frequency-149 bin entanglement [6]. Our device can also operate in a different configuration, 150 which we will refer as " Ψ ". Here Ring A and Ring B are thermally tuned so that 151 the resonances corresponding to the states $|0\rangle_i$ and $|1\rangle_s$ belong to Ring B and 152 those corresponding to $|0\rangle_{\rm s}$ and $|1\rangle_{\rm i}$ belong to Ring A (see Fig. 1e-g). As can be 153 seen from all panels in Figs. 1b-g, the resonances of the two generating rings 154 have quality factors $Q \approx 150,000$ (Full width at half maximum $\Gamma \approx 1.3 \,\mathrm{GHz}$), 155 which guarantee well-separated frequency bins and high generation rates. 156

The basic principle of operation of the device is the following: (i) Ring A and Ring B are set in the proper configuration (e.g., Φ) by controlling the thermal tuners; (ii) The pump power is coherently distributed between the two rings with the required relative phase and amplitude set either through the MZI or directly through the bus waveguide; (iii) Photon pairs are collected in the bus waveguide, with the desired state resulting from a coherent superposition of the two-photon states that would be generated by each ring separately.

¹⁶⁴ 3 Results

161

162

163

¹⁶⁵ Spontaneous four-wave mixing

The photon generation efficiency through spontaneous four-wave mixing 166 (SFWM) was assessed for the two rings by setting the device in configuration 167 Ψ , which is convenient to pump each ring individually through the bus waveg-168 uide. The two resonators were pumped with an external tunable laser, and the 169 chip output was separated in the signal (194.7–197.2 THz), pump (192.2–194.7 170 THz), and idler (189.7–192.2 THz) bands by means of a telecom-grade coarse 171 wavelength division multiplexer (see Fig. S1 in the Supplementary Informa-172 tion). The generated signal and idler photons were then narrowband filtered 173 using tunable fiber Bragg gratings with an 8 GHz stop-band, and routed to 174 a pair of superconductive single-photon detectors. The overall insertion losses 175 from the bus waveguide to the detectors are 6 dB and 7 dB for signal and 176 idler channels, respectively. The results of the experiment are summarized in 177 Fig. 2. The two rings exhibit similar generation efficiency $\eta = R/P_{wg}^2$, with 178 $\eta_{\rm A} = 57.6 \pm 2.1 \, {\rm Hz}/\mu {\rm W}^2$ for Ring A and $\eta_{\rm B} = 62.4 \pm 1.7 \, {\rm Hz}/\mu {\rm W}^2$ for Ring B 179 [15]. The internal pair generation rate R can exceed 2 MHz for both ring res-180 onators (Fig. 2a). A high coincidence-to-accidental ratio (CAR) exceeding 10^2 181 was obtained for any value of the input power, a necessary condition to ensure 182 a high purity of the generated state (Fig. 2b). 183

We now turn to the spectral properties of the generated photon pairs and the demonstration of entanglement. We set our device to operate in the Φ configuration, which will later be used to generate the maximally entangled state

$$|\Phi(\theta)\rangle = \frac{|00\rangle + e^{i\theta} |11\rangle}{\sqrt{2}},\tag{1}$$

188

where $|00\rangle = |0\rangle_{s} |0\rangle_{i}, |11\rangle = |1\rangle_{s} |1\rangle_{i}$, and the phase θ can be adjusted by acting 189 on the thermoelectric phase shifter after the interferometer (see Supplementary 190 Information); $\theta = 0$ and $\theta = \pi$ correspond to the well-known Bell states $|\Phi^+\rangle$ 191 and $|\Phi^{-}\rangle$, respectively. The corresponding SFWM spectrum of the signal and 192 idler bands is shown in Fig. 3 a and b (upper panels); the device was electrically 193 tuned to set $\theta = 0$, with the pump power split equally between Rings A and 194 B by means of the MZI. Here we focus on the azimuthal order $m = \pm 5$, with 195 the generated frequency bins clearly distinguishable in the marginal signal and 196 idler spectra. 197

¹⁹⁸ Two-photon interference

¹⁹⁹ In order to demonstrate entanglement, the demultiplexed signal and idler ²⁰⁰ photons were routed (see Fig. S1 in the *Supplementary Information*) to

two intensity electro-optic modulators (EOMs), coherently driven at $f_{\rm m} =$ 201 9.5 GHz, which corresponds to half the frequency bin separation of the 202 selected azimuthal order $m = \pm 5$. The modulators operate at the mini-203 mum transmission point (i.e. at bias voltage V_{π}) to achieve double-sideband 204 suppressed-carrier amplitude modulation. The amplitude of the modulating 205 RF signal was chosen to maximize the transferred power from the carrier to 206 the first-order sidebands, with a modulation efficiency of around $-4.8 \,\mathrm{dB}$, cor-207 responding to a modulation index $\beta \approx 1.7$. These losses can be reduced by 208 integrating the modulators on chip. Furthermore, our approach allows the use 209 of frequency bin spacings potentially much lower than the frequency cut-off of 210 the modulators. This will allow the use of complex wavelength shifting modu-211 lation techniques [17, 18] to avoid the generation of double sidebands and the 212 consequent 3 dB in added losses. 213

The resulting spectrum is shown in the lower panels of Fig. 3a and b, in 214 which one can clearly recognize three peaks. Indeed, given the chosen mod-215 ulated frequency, the central one results from the overlap of the down- and 216 upper-converted original bins. From a quantum optics point of view, this oper-217 ation achieves quantum interference of the original frequency bins [12] in a 218 similar fashion to what can be done with time bins in a Franson interferometer 219 [19, 20]. Here the achievable visibility of quantum interference depends on the 220 correct superposition of the spectra of the modes encoding the two frequency 221 bins for the signal and idler photons respectively, as outlined in Fig. 4a. 222

For coincidence counting, the modulated signal and idler photons were 223 filtered using narrowband fiber Bragg gratings to select only the central line at 224 the output of the corresponding modulator, and routed to the single-photon 225 detectors. The results of this experiment are shown in Figs. 4b and c as a 226 function of the modulation frequency. The rapid oscillation of the correlation 227 is due to the different phase acquired by the photons during their propagation 228 from the device to the EOMs. If the resonances share the same Q factor and 229 coupling efficiency, the coincidence rate is proportional to the cross-correlation 230 function (see Supplementary Information) 231

$$G_{\rm s,i}^{(2)}(f_{\rm m}) = 1 + \frac{\Gamma^2}{\left(f_{\rm m} - \Delta/2\right)^2 + \Gamma^2} \cos\left(4\pi \left(f_{\rm m} - \Delta/2\right) \delta T + 2\varphi_{\rm s} - 2\varphi_{\rm i} - \theta\right),\tag{2}$$

where $\delta T = t_i - t_s$ is the difference between the idler and signal arrival times 232 at the EOMs, and $\varphi_{s(i)}$ is the signal (idler) modulator driving phase. Fig. 4b 233 shows good agreement between the experimental results and curve described 234 by Eq. (2) for $\varphi_{\rm s} - \varphi_{\rm i} = \theta/2$ and $\delta T = 8.5 \,\mathrm{ns}$, which corresponds to the $\sim 2 \,\mathrm{m}$ 235 path difference between the idler and signal EOMs in our setup (see Supple-236 mentary Information). The curve visibility obtained from a least-square fit of 237 the model is $V = 98.7 \pm 1.2\%$. The two-photon correlation reaches its maximum 238 value $G_{s,i}^{(2)}(f_m) \approx 2$ when $f_m = \Delta/2$, as shown other work on frequency-bin 239 entanglement [12]. Thanks to the high brightness of the source, coincidence 240 counts on the detectors remain well above the noise level even with the added 241

 $_{242}$ losses from the modulators, with a CAR level > 50 and detected coincidence $_{243}$ rate > 2 kHz, thus implying an interference pattern with a high visibility.

With these results in hand, we set $f_{\rm m} = \Delta/2$ and varied $\varphi_{\rm s}$ to perform a Bell-like experiment. The corresponding quantum interference curves are reported in *Supplementary Information*.

²⁴⁷ Quantum state tomography

Finally, we show that our device can be operated to generate, directly on 248 chip, frequency bin photon pairs with a controllable output state. For each 249 of the explored configurations we performed quantum state tomography. First 250 we kept the device in configuration Φ , in which Ring A and Ring B generate 251 photon pairs in the state $|0\rangle_{s,i}$ and $|1\rangle_{s,i}$, respectively. Thus, the two states of 252 the computational basis $|00\rangle = |0\rangle_{\rm s} |0\rangle_{\rm i}$ and $|11\rangle = |1\rangle_{\rm s} |1\rangle_{\rm i}$ can be generated by 253 selectively pumping only the appropriate resonator, as shown in Fig. 5a and 254 b. The states were characterised via quantum state tomography [12, 21, 22], 255 as detailed in the *Methods* section. In both cases the states are accurately 256 reproduced, with fidelity and purity exceeding 90%. 257

In a second experiment, the MZI was operated to split the pump power so 258 that the probabilities of generating a photon pair in Ring A and in Ring B are 259 equal. If the pump power is sufficiently low that the probability of emitting 260 two photon pairs is negligible, then the generated frequency bins are in the 261 state $|\Phi(\theta)\rangle$ described by Eq. (1), where the phase factor θ is controlled by the 262 phase shifter after the MZI. By setting $\theta = 0$ or π , we were able to generate 263 the two Bell states $|\Phi^+\rangle$ and $|\Phi^-\rangle$, respectively (see Fig. 5c and d). The real 264 and imaginary parts of the density matrix are shown in Fig. 5g, h, k, and 265 1. As expected, we found non-zero off-diagonal terms in the real part of the 266 density matrix, which indicate entanglement. In these cases as well the device 267 is capable of outputting the desired with purity and fidelity exceeding 90%. 268 The entanglement of formation, a figure of merit to quantify the entanglement 269 of the generated pairs [23], was extracted from the measured density matrices, 270 yielding values >80% for the two Bell states, in contrast with values <20% for 271 the two separable states $|00\rangle$ and $|11\rangle$. 272

Our device can also operate in the Ψ configuration, with the ring resonances arranged as shown in Fig. 1e-g. In this case one is able to generate also the two remaining computational basis states $|01\rangle$, $|10\rangle$ and the two remaining Bell states $|\Psi^+\rangle$ and $|\Psi^-\rangle$. Note that in this configuration, the pump resonances for the two ring resonators are not aligned (Fig. 1f).

When generating the two separable states, either Ring A (to generate $|01\rangle$) 278 or Ring B (to generate $|10\rangle$) was pumped through the bus waveguide by simply 279 tuning the pump to the corresponding resonance (see Figs. 6a and b). To 280 generate the two Bell states, the pump pulse spectrum (which is tuned to 281 be in the middle of the two resonances) is shaped using an external EOM 282 operated at the frequency corresponding to half the difference between the 283 two pump resonances $(f_{\rm m,p} = \Delta_{\rm p}/2 = 19 \,{\rm GHz})$ (see Figs. 6c and d and the 284 *Methods* section). The pumping ratio and the phase between the two rings were 285

8

adjusted by tailoring the modulation to obtain an equal probability amplitude of generating a single photon pair for the states $|01\rangle$ and $|10\rangle$ respectively, while still keeping the probability of double pair generation negligible. The relative phase of the superposition can be controlled by adjusting the EOM driving phase to select either $|\Psi^+\rangle$ or $|\Psi^-\rangle$.

The four generated state were characterized via quantum state tomography 291 as in the previous case. However, we stress that here two different values of 292 bin spacing for the signal ($\Delta_s = 19 \,\text{GHz}$) and idler ($\Delta_i = 3\Delta_s = 57 \,\text{GHz}$) 293 qubits were used. While this does not constitute a problem for the generation 294 of entanglement, as the Hilbert space of the two qubits is built from the tensor 295 product of Hilbert spaces of two qubits with different values for Δ_s and Δ_i , 296 it offered us the opportunity to demonstrate, for the first time, frequency bin 297 tomography for uneven spacing. This is done by operating the signal and idler 298 EOMs (see Fig. S1 of the Supplementary Information) at different frequencies 299 equal to half the frequency spacing of the corresponding resonances. 300

The experimental results are shown in Figs. 6e-l. All four states were pre-301 pared with fidelity close to or exceeding 90%, and purity between 85% and 302 100%. The entanglement of formation is below 5% for the separable states 303 $|01\rangle$ and $|10\rangle$, while above 80% for the Bell states $|\Psi^+\rangle$ and $|\Psi^-\rangle$, as expected. 304 The reconstructed density matrices show increased noise with respect to those 305 reported in Fig. 5, because the modulation efficiency of our idler modulator 306 was significantly reduced at such a high frequency, resulting in additional losses 307 lowering the count rate on the detectors (see the *Methods* section). 308

³⁰⁹ Scalability to higher-dimensional states

Our approach can be generalized to frequency bin qudits by scaling the num-310 ber of coherently excited rings. We give a proof of principle demonstration of 311 this capability by using a different device hosting d = 4 rings and add-drop 312 filters. The four sources, $j = 0, \ldots, d - 1$, have radii $R_j = R_0 + j\delta R$, where 313 $R_0 = 30 \,\mu\text{m}$ and $\delta R = 0.1 \,\mu\text{m}$, which leads to a bin spacing of approximately 314 9 GHz at 7 FSR from the pump. The spectral response of the device at the 315 output of the bus waveguide, indicated in Fig. 7a, shows the four equidis-316 tant bins (A, B, C, D) associated with the signal and with the idler photons, 317 and the overlapping resonances of the rings at the pump frequency. As in 318 the case of qubits, we used an MZI tree to split the pump into four paths, 319 each feeding a different add-drop ring filter that is used to control the field 320 intensity at the photon pair sources. We focused on the capability to gener-321 ate the four computational basis states and the two-dimensional Bell states 322 formed by adjacent frequency bins pairs. First, the add-drop filters are tuned 323 on resonance one at a time. This selects the computational basis state that 324 is generated. We characterized those states by performing a Z-basis correla-325 tion measurement, i.e., by projecting the signal and the idler photon on the 326 Z-basis $\{|j\rangle_{s} |m\rangle_{i}\}, j(m) = A, B, C, D$ in order to measure the uniformity and 327 the cross-talk between the four frequency bins. From the correlation matrices, 328 shown in Fig. 7b-e, it was possible to measure the ratio of the coincidence 329

counts n_{jj} in the frequency-correlated basis $|j\rangle_{s} |m\rangle_{i}$ to that in the uncorrelated 330 basis $\sum_{j\neq m} n_{jm}$, and it is about two orders of magnitude. We could compen-331 sate for the slightly different amplitude of the different basis states by acting 332 on the MZI tree at the input. Second, the add-drop filters associated with the 333 adjacent frequency bin pairs A-B, B-C and C-D are tuned on resonance one at 334 a time, thus generating the Bell states $|\Phi\rangle_{AB}$, $|\Phi\rangle_{BC}$ and $|\Phi\rangle_{CD}$. The visibil-335 ity of quantum interference is assessed by mixing the corresponding frequency 336 bins with the electro-optic modulator. Unlike in the qubit experiment, here we 337 choose a modulation frequency that matches the spectral separation between 338 the bins. We used phase modulators configured to create first order sidebands 339 of amplitude equal to that of the baseband, and recorded the coincidences in 340 signal/idler bins B,C and D. The resulting Bell curves, shown in Fig. 7f, have 341 visibilities $V_{AB} = 0.831(5)$, $V_{BC} = 0.884(6)$ and $V_{CD} = 0.81(1)$, indicating the 342 presence of entanglement between the bin-pairs in all cases. It is worth not-343 ing that, as in the two-dimensional case, the relative phase between the three 344 Bell curves in Fig. 7f could be adjusted using on-chip phase shifters in order 345 to realize maximally entangled high-dimensional Bell states. 346

347 4 Conclusions

We demonstrated that a rich variety of separable and maximally entangled states, including any linear superposition of $\{|00\rangle, |11\rangle\}$ or $\{|01\rangle, |10\rangle\}$, can be generated using frequency-bin encoding in a single programmable nano-photonic device, fabricated with existing silicon photonic technologies compatible with multi-project wafer runs. This guarantees that these devices can be available for widespread use in applications, ranging from quantum communication to quantum computing.

Our approach constitutes a new paradigm for the integration of frequency-355 bin devices that goes well-beyond a miniaturization of bulk strategies. Indeed, 356 unlike previous implementations, the states are all generated inside the device, 357 without relying on off-chip manipulation of a single initial state. Controlla-358 bility of the generated state was shown to be readily accessible on-chip, via 359 electrical control of thermo-optic actuators in one configuration (Φ), and by 360 tailoring the pump spectral properties in another (Ψ) . In a future version of 361 the device the use of more than two rings for the definition of the state will 362 allow the two configurations to have the same frequency spacing for the qubits. 363 As a result, the device will be capable of generating all four Bell states with 364 the same physical characteristics, as recently demonstrated using an external 365 periodically-poled lithium niobate crystal [24]; it will also be used to explore 366 more of the Hilbert space of the two qubits. 367

Since in our approach the frequency bin spacing is only limited by the resonator linewidth, the requirements for the electro-optic modulators are greatly relaxed with respect to previous implementations. Indeed, as demonstrated in this work, the frequency bin separation is compatible with existing silicon integrated modulators [25]. Thus, one can foresee a future evolution of our device that will involve modulators integrated on-chip. This will further increase its suitability for practical applications, such as quantum key distribution and quantum communications in general. In addition, the ability to independently choose the bin spacing Δ for both qubits, as shown in Figs. 1b-g, demonstrates an additional flexibility in choosing the basis for frequency-bin encoding that can be exploited for the engineering of the source.

The approach demonstrated here is scalable, for one can design and implement devices with more than two generating rings by taking advantage of silicon dense integration, opening the possibility of using frequency qudits instead of simple qubits. As demonstrated in a number of theoretical proposals, such an ability will be of pivotal importance for multiple applications in quantum communication, sensing, and computing algorithms [26].

Finally, our approach allowed us to overcome the trade-off between the fre-385 quency bin spacing and the generation rate that characterized previous work. 386 This was instrumental in achieving a comprehensive assessment of the proper-387 ties of the generated states, which could be performed using only telecom-grade 388 fiber components – with the sole exception of single-photon detection – with 389 an overall low loss $(< 4 \,\mathrm{dB})$ ensured by the all-fiber technology. The accuracy 390 and the precision that have been achieved in our measurements are state-of-391 the-art for frequency-bin encoding, even considering results obtained with bulk 392 sources. well-beyond any other reported so far on frequency-bin encoding. All 393 these results will usher in the use of frequency bin qubits as a practical choice 394 for photonic qubits, capable of combining easy manipulation and robustness 395 for long haul transmission. 396

397 Acknowledgements

This work has been supported by Ministero dell'Istruzione, dell'Università 398 е della Ricerca (Dipartimenti di Eccellenza Program (2018 - 2022)399 (F11I18000680001)). The device has been designed using the open source 400 Nazca designTM framework. Useful support in the analysis of experimental 401 data was provided by P. G. Kwiat through free access to online tutorials and 402 software (http://research.physics.illinois.edu/QI/Photonics/Tomography/). 403

$_{404}$ Methods

The device was fabricated at CEA-Leti (Grenoble), on Sample fabrication. 405 a 200-mm Silicon-on-Insulator (SOI) substrate with a 220-nm-thick top device 406 layer of crystalline silicon on 2-um-thick SiO₂ buried oxide. The patterning 407 process of the silicon photonics devices and circuits combines deep ultravi-408 olet (DUV) lithography with 120-nm resolution, inductively coupled plasma 409 etching (realized in collaboration with LTM - Laboratoire des Technologies 410 de la Microélectronique) and O_2 plasma resist stripping. Hydrogen anneal-411 ing was performed in order to strongly reduce etching-induced waveguide 412 sidewalls roughness [27]. After high-density plasma, low-temperature oxide 413 (HDP-LTO) encapsulation - resulting in a 1125-nm-thick SiO2 layer - 110 nm 414

of titanium nitride (TiN) were deposited and patterned to create the ther-415 mal phase shifters, while an aluminium copper layer (AlCu) was used for the 416 electrical pad definition. Finally, a deep etch combining two different steps 417 - $C_4F_8/O_2/CO/Ar$ plasma running through the whole thickness of both sil-418 ica upper cladding and buried oxide, followed by a Bosch deep reactive ion 419 etching (DRIE) step to remove 150 µm of the 725-µm-thick Si substrate - was 420 implemented to separate the sub-dice, thus ensuring high-quality optical-grade 421 lateral facets for chip-to-fiber edge coupling. 422

Linear spectroscopy. The experimental apparatus is schematically repre-423 sented in Fig. S1 of the Supplementary Information. The linear characteriza-424 tion of the sample shown in Fig. 1 was realized by scanning the wavelength 425 of a tunable laser (Santec TSL-710), with its polarization controlled by a 426 fiber polarization controller (PC). Light was coupled to the sample at the 427 input of the bus waveguide and collected at the output using a pair of lensed 428 fibers (nominal mode field diameter: $3 \mu m$), with an insertion loss lower than 429 3 dB/facet. The output signal was detected by an amplified InGaAs photodi-430 ode and recorded in real time by an oscilloscope. The resonance configuration 431 was adjusted by addressing each ring resonator's phase shifter with electric 432 probes driven by multi-channel power supply. 433

Nonlinear characterization. The SFWM efficiency for each resonator was 434 assessed through power-scaling experiments (Fig. 2). The flux of generated 435 idler and signal photons was measured by varying the pump power coupled 436 to each microring, while keeping the resonances in place by acting on the 437 thermo-electric phase shifters. The tunable laser source spectrum was filtered 438 by a band-pass (BP) filter in order to reduce the amount of spurious photons 439 at signal and idler frequencies coming from the launching part of the setup, 440 mainly associated with amplified spontaneous emission of the laser diode and 441 Raman fluorescence from the fibers. The collected signal and idler photons 442 were first separated using a coarse wavelength division multiplexer (CWDM), 443 with 2.5 THz (20 nm) nominal channel separation and measured inter-channel 444 crosstalk $< -80 \, \text{dB}$. The frequency bins of interest were then narrowband 445 filtered (3 dB-bandwidth: 8 GHz) by a pair of tunable fiber Bragg gratings 446 (FBG): besides selecting the frequency bins with high accuracy, this procedure 447 also suppresses any spurious broadband photon falling outside the bandwidth 448 of the input bandpass filter and not eliminated by the CWDM. 449

The resulting signal and idler photons were routed, using circulators, towards two superconductive single-photon detectors (SSPDs), where timecorrelated single photon counting (TCSPC) was performed with a precision of about 35 ps, mainly determined by the detectors jitter. A coincidence window of $\tau_c = 380$ ps was chosen by selecting the average full-width at half-maximum (FWHM) of the histogram peak. Accidental counts were estimated from the background level; note that this value is not subtracted from the number of coincidences counted, but was used only to estimate the coincidence-to-accidental ratio, according to the formula:

$$CAR = \frac{total \ counts \ in \ coinc. \ window - accidental \ counts \ window - accidental \ win$$

Quantum state tomography. Two-photon interferometry and tomography 450 of the generated quantum states were performed by including a pair of inten-451 sity EOMs (iXblue MX-LN) at the signal and idler demultiplexer outputs, 452 coherently driven by a multi-channel RF generator (AnaPico APMS20G). The 453 sidebands of interest were selected by tuning the central stop-band wavelength 454 of the FBGs. The tomography of each quantum state involved 16 individual 455 measurements, each performed in an acquisition time of 15 s. For each measure-456 ment, each FBG was tuned to one of the three sideband frequencies obtained 457 from the modulation of the signal (idler) bins, and the EOM's relative phase 458 was adjusted appropriately. Estimation of the density matrices was performed 459 via maximum-likelihood technique [21, 22]. For the generation of states in the 460 $\{|01\rangle, |10\rangle\}$ basis (Ψ configuration), we added a phase EOM at the input of 461 the setup, coherently driven by the same RF source used for tomography, and 462 we entered the chip at the bus waveguide. The two generation rings were then 463 pumped by the first-order sidebands, while their relative phase was fixed by 464 the phase of the modulation. 465

Measurement of qudits. For the Z-basis correlation measurement, a total 466 set of different projectors (for each photon) is used for each basis state. The 467 projector $|j\rangle_{\rm s} |m\rangle_{\rm i}$ is implemented by setting the signal(idler) FBG to reflect 468 only the frequency bin j(m). For those combinations carrying negligible counts 469 (corresponding to frequency uncorrelated bins), the central frequency of the 470 two FBGs cannot be determined by simply maximizing the coincidence rate or 471 the flux of singles in each bin. To circumvent this, we coupled a secondary laser 472 beam in the counter-propagating direction with respect to that of the pump, 473 and recorded the back reflected light from the sample. The spectra of the latter 474 are monitored after being transmitted by the FBGs, and simultaneously reveal 475 the spectral location of the stop band of the FBG and the four resonance 476 frequencies of the rings. In this way, the stop band can be overlapped with the 477 desired frequency bin with high precision. 478

479 **References**

- [1] Marcikic, I., de Riedmatten, H., Tittel, W., Scarani, V., Zbinden, H.,
 Gisin, N.: Time-bin entangled qubits for quantum communication created
 by femtosecond pulses. Phys. Rev. A 66, 062308 (2002). https://doi.org/
 10.1103/PhysRevA.66.062308
- [2] Marcikic, I., de Riedmatten, H., Tittel, W., Zbinden, H., Legré, M.,
 Gisin, N.: Distribution of time-bin entangled qubits over 50 km of optical fiber. Phys. Rev. Lett. 93, 180502 (2004). https://doi.org/10.1103/
 PhysRevLett.93.180502

- [3] Inagaki, T., Matsuda, N., Tadanaga, O., Asobe, M., Takesue, H.:
 Entanglement distribution over 300 km of fiber. Opt. Express 21(20),
 23241–23249 (2013). https://doi.org/10.1364/OE.21.023241
- [4] Kok, P., Munro, W.J., Nemoto, K., Ralph, T.C., Dowling, J.P., Milburn,
 G.J.: Linear optical quantum computing with photonic qubits. Rev. Mod.
 Phys. 79, 135–174 (2007). https://doi.org/10.1103/RevModPhys.79.135
- ⁴⁹⁴ [5] Silverstone, J.W., Santagati, R., Bonneau, D., Strain, M.J., Sorel, M.,
 ⁴⁹⁵ O'Brien, J.L., Thompson, M.G.: Qubit entanglement between ring⁴⁹⁶ resonator photon-pair sources on a silicon chip. Nature Communications
 ⁴⁹⁷ **6**, 7948 (2015). https://doi.org/10.1038/ncomms8948
- ⁴⁹⁸ [6] Olislager, L., Cussey, J., Nguyen, A.T., Emplit, P., Massar, S., Merolla,
 ⁴⁹⁹ J.-M., Huy, K.P.: Frequency-bin entangled photons. Physical Review A
 ⁵⁰⁰ 82(1) (2010). https://doi.org/10.1103/physreva.82.013804
- [7] Kaneda, F., Suzuki, H., Shimizu, R., Edamatsu, K.: Direct generation
 of frequency-bin entangled photons via two-period quasi-phase-matched
 parametric downconversion. Optics Express 27(2), 1416 (2019). https:
 //doi.org/10.1364/oe.27.001416
- [8] Rieländer, D., Lenhard, A., Farìas, O.J., Máttar, A., Cavalcanti, D.,
 Mazzera, M., Acín, A., de Riedmatten, H.: Frequency-bin entanglement
 of ultra-narrow band non-degenerate photon pairs. Quantum Science
 and Technology 3(1), 014007 (2017). https://doi.org/10.1088/2058-9565/
 aa97b6
- [9] Lukens, J.M., Lougovski, P.: Frequency-encoded photonic qubits for scalable quantum information processing. Optica 4(1), 8–16 (2017). https: //doi.org/10.1364/OPTICA.4.000008
- [10] Lu, H.-H., Lukens, J.M., Peters, N.A., Williams, B.P., Weiner, A.M.,
 Lougovski, P.: Quantum interference and correlation control of frequency bin qubits. Optica 5(11), 1455–1460 (2018). https://doi.org/10.1364/
 OPTICA.5.001455
- [11] Silverstone, J.W., Bonneau, D., Ohira, K., Suzuki, N., Yoshida, H., Iizuka,
 N., Ezaki, M., Natarajan, C.M., Tanner, M.G., Hadfield, R.H., Zwiller,
 V., Marshall, G.D., Rarity, J.G., O'Brien, J.L., Thompson, M.G.: Onchip quantum interference between silicon photon-pair sources. Nature
 Photonics 8, 104–108 (2014). https://doi.org/10.1038/nphoton.2013.339
- Imany, P., Jaramillo-Villegas, J.A., Odele, O.D., Han, K., Leaird, D.E.,
 Lukens, J.M., Lougovski, P., Qi, M., Weiner, A.M.: 50-GHz-spaced comb
 of high-dimensional frequency-bin entangled photons from an on-chip silicon nitride microresonator. Optics Express 26(2), 1825 (2018). https:

⁵²⁶ //doi.org/10.1364/oe.26.001825

- [13] Kues, M., Reimer, C., Roztocki, P., Cortés, L.R., Sciara, S., Wetzel,
 B., Zhang, Y., Cino, A., Chu, S.T., Little, B.E., Moss, D.J., Caspani,
 L., Azaña, J., Morandotti, R.: On-chip generation of high-dimensional
 entangled quantum states and their coherent control 546(7660), 622–626
 (2017). https://doi.org/10.1038/nature22986
- [14] Reimer, C., Kues, M., Roztocki, P., Wetzel, B., Grazioso, F., Little, B.E.,
 Chu, S.T., Johnston, T., Bromberg, Y., Caspani, L., Moss, D.J., Morandotti, R.: Generation of multiphoton entangled quantum states by means
 of integrated frequency combs. Science 351(6278), 1176–1180 (2016).
 https://doi.org/10.1126/science.aad8532
- Azzini, S., Grassani, D., Galli, M., Andreani, L.C., Sorel, M., Strain,
 M.J., Helt, L., Sipe, J., Liscidini, M., Bajoni, D.: From classical four-wave
 mixing to parametric fluorescence in silicon microring resonators. Optics
 letters 37(18), 3807–3809 (2012)
- [16] Liscidini, M., Sipe, J.E.: Scalable and efficient source of entangled frequency bins. Optics Letters 44(11), 2625 (2019). https://doi.org/10.1364/
 ol.44.002625
- [17] Riaziat, M.L., Virshup, G.F., Eckstein, J.N.: Optical wavelength shifting
 by traveling-wave electrooptic modulation. IEEE Photonics Technology
 Letters 5(9), 1002–1005 (1993). https://doi.org/10.1109/68.257172
- [18] Kittlaus, E.A., Jones, W.M., Rakich, P.T., Otterstrom, N.T., Muller, R.E., Rais-Zadeh, M.: Electrically driven acousto-optics and broadband non-reciprocity in silicon photonics. Nature Photonics 15, 43–52 (2021). https://doi.org/10.1038/s41566-020-00711-9
- [19] Franson, J.D.: Bell inequality for position and time. Physical review letters
 62(19), 2205 (1989)
- ⁵⁵³ [20] Grassani, D., Azzini, S., Liscidini, M., Galli, M., Strain, M.J., Sorel, M.,
 ⁵⁵⁴ Sipe, J.E., Bajoni, D.: Micrometer-scale integrated silicon source of time ⁵⁵⁵ energy entangled photons. Optica 2(2), 88–94 (2015). https://doi.org/10.
 ⁵⁵⁶ 1364/OPTICA.2.000088
- ⁵⁵⁷ [21] James, D.F.V., Kwiat, P.G., Munro, W.J., White, A.G.: Measurement of qubits. Phys. Rev. A 64, 052312 (2001). https://doi.org/10.1103/ PhysRevA.64.052312
- [22] Takesue, H., Noguchi, Y.: Implementation of quantum state tomography
 for time-bin entangled photon pairs. Optics Express 17(13), 10976 (2009).
 https://doi.org/10.1364/OE.17.010976

- ⁵⁶³ [23] Wootters, W.K.: Entanglement of formation of an arbitrary state of two
 ⁵⁶⁴ qubits. Phys. Rev. Lett. 80, 2245–2248 (1998). https://doi.org/10.1103/
 ⁵⁶⁵ PhysRevLett.80.2245
- Seshadri, S., Lu, H.-H., Leaird, D.E., Weiner, A.M., Lukens, J.M.: Com plete frequency-bin Bell basis synthesizer. arXiv (2022). https://doi.org/
 10.48550/ARXIV.2205.06141
- ⁵⁶⁹ [25] Streshinsky, M., Ding, R., Liu, Y., Novack, A., Galland, C., Lim, A.E.-J.,
 ⁵⁷⁰ Lo, P.G.-Q., Baehr-Jones, T., Hochberg, M.: The road to affordable, large⁵⁷¹ scale silicon photonics. Opt. Photon. News 24(9), 32–39 (2013). https:
 ⁵⁷² //doi.org/10.1364/OPN.24.9.000032
- ⁵⁷³ [26] Wang, Y., Hu, Z., Sanders, B.C., Kais, S.: Qudits and high-dimensional
 quantum computing. Frontiers in Physics 8, 479 (2020). https://doi.org/
 ⁵⁷⁵ 10.3389/fphy.2020.589504
- ⁵⁷⁶ [27] Bellegarde, C., Pargon, E., Sciancalepore, C., Petit-Etienne, C., Hugues,
 ⁵⁷⁷ V., Robin-Brosse, D., Hartmann, J.-M., Lyan, P.: Improvement of sidewall
 ⁵⁷⁸ roughness of submicron soi waveguides by hydrogen plasma and annealing.
 ⁵⁷⁹ IEEE Photonics Technology Letters **30**(7), 591–594 (2018). https://doi.
 ⁵⁸⁰ org/10.1109/LPT.2018.2791631



Fig. 1 Device layout and transmission spectra. a. Schematic of the device, in which a Mach Zehnder Interferometer (MZI) is used to route optical pumping power to the two generating rings (Ring A and Ring B) via two add-drop filters (F). The pump relative phase for the two rings is controlled by a thermo-electric phase shifter. b-d. Linear characterization of the sample through the bus waveguide, with the device operated in configuration Φ . A detail of the transmission spectrum around the idler (panel b, m = -5), pump (panel c, m = 0), and signal (panel d, m = +5) bands shows resonances belonging to both ring resonators, identified by labels A and B respectively. In this configuration, Ring B is associated to the $|0\rangle_{s,i}$ frequency bins for both signal and idler, e-g. Same as panels b-d, respectively, but with the device set in configuration Ψ . Here, Ring A corresponds to the $|0\rangle_s$ resonance for the signal and $|1\rangle_i$ resonance for the idler, Ring B corresponds to the $|1\rangle_s$ resonance for the signal and $|0\rangle_i$ resonance for the idler.



Fig. 2 Spontaneous four-wave mixing. Generation of pairs through spontaneous fourwave mixing using the two rings of the device. The two sets of resonances are shifted such that all the resonances are separated (configuration Ψ). A tunable laser is tuned on resonance with either Ring A or Ring B, and the related signal and idler photons are detected. Similar coincidence rates (panel **a**) are observed, proving that the two rings have similar generation efficiencies. Inset shows an example histogram of the photon arrival time delays. Panel **b** shows the calculated CAR, which exhibits the typical reduction for the higher values of the input power due to the generation of higher-order photon states.



Fig. 3 Effect of modulation on spontaneous four-wave mixing spectra. Normalized spontaneous four-wave mixing spectra for the **a**. idler and **b**. signal channels after demultiplexing both in the absence (upper panels) and presence (lower panels) of modulation. The bin pair order m with respect to the pump resonances is marked, while spontaneous four-wave mixing generated in the add-drop filter rings is marked as F. Note that, despite the different out-coupling efficiency for each resonance and the limited resolution of the spectrometer, it is still possible to observe the expected symmetry in the intensity of the generated bins, and how the bin spacing increases with the azimuthal order m. Lower panels show the effect of the double-sideband suppressed-carrier modulation on the signal and idler spectra, where only the first-order sidebands are preserved. The spectra shown here are associated with generation of the state described by Eq. (1), where we chose $\theta = \pi$ (Bell state $|\Phi^-\rangle$). Analogous spectra are attainable for any of the device configurations discussed in this work.



Fig. 4 Frequency mixing and two-photon interference. a. Schematic of the effect of modulation on the generated idler (red) and signal (blue) frequency bins. The frequency mixing produces maps each of the signal and idler states in a superposition of three frequency components: the outermost ones are reminiscent of the probability amplitude proportional to $|0\rangle_{s,i}$ or $|1\rangle_{s,i}$, while the "central" bin results in a superposition of the two. Each frequencyshifted bin also acquires a phase $\pm \varphi_{s,i}$ due to the modulation. The superposition of the generated bins is regulated by the modulation frequency, and the overlap is ideally maximized when $f_m = \Delta/2$, when perfect indistinguishability of the generated bins is achieved. b. Two-photon correlation $G_{1,2}^{(2)}$ of the frequency-mixed bins as a function of the detuning $f_m - \Delta/2$. The experimental points (black dots) were obtained by counting coincidences between frequency-mixed bins ad varying modulation frequency, while keeping fixed the modulation phase, and normalizing. Error bars (light gray) were estimated assuming Poissonian statistics. Blue curve represents the best-fit of the curve according with Eq. (2), showing good agreement (panel c) with theoretical predictions.



Fig. 5 Quantum state tomography in the $\{|00\rangle, |11\rangle\}$ basis (Φ configuration). Columns from left to right refer respectively to states: $|00\rangle$, $|11\rangle$, $|\Phi^+\rangle$, and $|\Phi^-\rangle$. a-d. Device pumping scheme for each of the generated state. The path covered by the pump laser is highlighted in red. The generation rings A and B are selectively addressed by acting on the tunable MZI, while the relative phase of the pump is varied through a thermal phase shifter. e-h. Real and g-l. imaginary part of the reconstructed density matrices for each of the generated states, estimated through the maximum-likelihood method. F, P and EF indicate respectively fidelity, purity and entanglement of formation of each reconstructed state.



Fig. 6 Quantum state tomography in the $\{|01\rangle, |10\rangle\}$ basis (Ψ configuration). Columns from left to right refer respectively to states: $|01\rangle, |10\rangle, |\Psi^+\rangle$, and $|\Psi^-\rangle$. a-d. Device pumping scheme. The bus waveguide is used as input for the pump, whereas the generation rings' resonances are addressed by spectral shaping (modulation) of the pump, performed before coupling to the chip. The relative generation phase between rings A and B is tuned by adjusting the phase of the input modulator driver. e-l. Reconstructed density matrices for each of the generated states (see caption of Fig. 5 for details).



Fig. 7 Higher-dimensional states (qudits). a. Normalized transmission spectrum of the device used for the generation of higher-dimensional states. The device layout is analogous to the one shown if Fig. 1a, but four generation rings (labeled A, B, C, D) are involved. Panels from left to right show respectively the idler, pump, and signal resonances associated to the correspondent four rings involved. **b-e.** Correlation matrices showing coincidence counts for each pair of resonators while pumping respectively rings A, B, C, D. **f.** Bell-type quantum interference measurements performed on the generated states $|\Phi\rangle_{AB}$ (orange dots), $|\Phi\rangle_{BC}$ (green dots) and $|\Phi\rangle_{CD}$ (blue dots).