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## Effect of the grain elongation on the behaviour of granular materials in biaxial compression

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#### Abstract

In this paper we study the effect of the grain elongation on the shearing behaviour of dense granular materials by means of 2D numerical simulations of biaxial compression tests, using the *Contact Dynamics* method. The case of grains with hexagonal shapes (and four possible different elongations) is studied in comparison to the case of a sample with circular grains. For the studied shapes, samples with polygonal grains exhibit initial densities higher than the sample with discs, and the initial density decreases when the grain elongation increases. The friction angle at the residual state increases linearly with the particle elongation ratio. The cumulative rotations of discs are higher than those of polygons. Finally, in the case of elongated hexagons, the grains with highest rotations are located along thin bands because the shear bands are thinner and more persistent for these shapes. *To cite this article: C. Nouguier-Lehon, C. R. Mecanique ??? (2011).* 

#### Résumé

Influence de l'allongement des grains sur le comportement des matriaux granulaires au cours d'une compression biaxiale. Nous étudions dans cet article l'influence de l'allongement des grains sur le comportement de matériaux granulaires denses grâce à des simulations numériques 2D de l'essai de compression biaxiale par la méthode *Contact Dynamics*. Les grains sont de forme hexagonale (et de quatre élongations différentes) et leur comportement est comparé au cas des grains circulaires. Pour les formes étudiées, les échantillons de grains polygonaux sont initialement plus denses que l'échantillon de disques, et on observe une diminution de la densité initiale quand l'allongement des grains augmente. L'angle de frottement à l'état résiduel augmente linéairement avec l'allongement des particules. La rotation cumulée des disques est beaucoup plus importante que celle des polygones. Enfin, on peut remarquer que pour ces hexagones allongés, les grains qui tournent beaucoup sont situés le long de fines bandes car pour ces formes, les bandes de cisaillement sont plus fines et moins fluctuantes. *Pour citer cet article : C. Nouguier-Lehon, C. R. Mecanique ? ?? (2011).* 

Key words: Granular material; particle shape; biaxial test; rotations. Mots-clés : Matériau granulaire; forme des particules; essai biaxial; rotations.

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#### 1. Introduction

The discrete element method (DEM) has been widely used since the last thirty years to improve the understanding of physical phenomena controlling the behaviour of granular materials. It allows to access to the microstructural parameters such as contact forces between particles, that are difficult to experimentally measure. The majority of simulations were initially performed on samples of either discs in 2D or spheres in 3D (we can cite [1,2,3,4,5,6] among others). But, it is well known that the particle shape is a characteristic that has a great influence on the behaviour of such media [7,8,9,10]. Indeed, the possibility that grains are in contact through multiple contact points (due to roughness, angularity or nonconvexity of the particles) and the eventual grain elongation modify the behaviour of these materials. Several image analyses techniques and 3D surface reconstructions are nowadays available, that can be used in order to catch with remarkable precision the actual grain shape. However, the real shape of particles may be very complex and it is important to reproduce, in a rather simple way in numerical simulations, the main features of particle non-sphericity.

More recently, many numerical simulations were performed in order to study the effect of particle shape [11,12,13]. For instance, Mirgahsemi *et al.* [14] performed numerical simulations with samples composed of 500 regular polygons (from triangles and squares to polygons with 11 edges) showing that samples made of angular particles are denser than samples with rounded particles. Azéma *et al.* [15] showed that the existence of face-to-face contacts in a sample made of pentagonal particles leads to an higher anisotropy for the force transmission (with strong force chains essentially carried by face-to-face contacts). In previous works [16,17], we analysed the behaviour of samples composed of different grain shapes (circular, isotropic and anisotropic polygonal shapes). Our results clearly show the existence of a steady state of void ratio, of the shear strength and texture anisotropy, whatever the grain shape, as that has been found again by [18] from shear test simulations with samples of convex polygons. The effect of induced anisotropy was also studied by Alonso-Marroquín *et al.* [19] analysing the behaviour of polygons with adjusted shapes to model the behaviour of the marble.

In the present study, we analyse the effect of particles elongation, by performing 2D numerical simulations of biaxial compression test and using samples made of irregular hexagons with different aspect ratio. A sample of discs was also generated in order to compare with the behaviour of circular particles. First we present the numerical program and the specimen preparation. Then we analyse the effect of grain elongation on the initial state and on the global and local mechanical behaviour.

#### 2. Numerical procedures

#### 2.1. Numerical method

The programs used for these simulations are based on the *Contact Dynamics* (CD) method [20,21,22,23], i.e. a Discrete Element Method that allows to model granular assemblies as a collection of rigid or deformable bodies in contact with dry friction, without the introduction of elasticity at contacts (*cf. smooth DEM* [24]). In the CD method, the impenetrability condition and the friction law are treated by using the non smooth relations of Signorini and Coulomb, which link the relative velocity at the contact impulsion. To take the collisions into account, normal and tangential coefficients of restitution are introduced, respectively denoted  $e_N$  and  $e_T$ , with values between 0 and 1. Pure elastic shocks are considered for  $e_N = e_T = 1$ , while the entire energy vanishes during impact for  $e_N = e_T = 0$ . Finally,

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the equations of motion are discretised by an implicit algorithm, that allows to choose larger time steps than the smooth DEM. The CD method has been used in very various fields from Civil Engineering to Biomechanics: among others we can cite the modelling of the ballast behaviour [25] and of rock avalanches [26], the study of masonry structures [27], or the analyse of cytoskeleton structuration [28]. Comparisons between simulations performed with the CD method and smooth DEM showed that both numerical methods give similar results for quasistatic tests [29,30].

2.2. Shape characterization and sample generation



Figure 1. Construction of an irregular hexagonal shape with an elongation ratio  $\frac{b}{a}$ .

The particle elongation [31] can be defined as the ratio  $\frac{b}{a}$ , where *a* is the diameter of the smallest circle containing the particle and *b* is the diameter of the largest circle included in the particle (figure 1). So the elongation ratio  $\frac{b}{a}$  is the inverse of the aspect ratio, a parameter also used to characterize the particle elongation, that is defined as the ratio of the largest particle size to the smaller one. For a circular particle,  $\frac{b}{a} = 1$  and the higher the particle elongation the smaller the ratio  $\frac{b}{a}$ .

Starting from the same particle size distribution  $(d_{min} = 0.66 \text{ cm}, d_{max} = 2 \text{ cm}$  and a uniform distribution in particle surface fraction), the polygons are generated in order to obtain particles having, for a given diameter, the most elongated shape. To avoid the effect of particle roundness, all the polygonal shapes have six edges. The two first vertices are put diametrically opposed on the circle of a in diameter (points  $A_1$  and  $A_2$  in figure 1). Then, the four latest vertices will be on the lines tangent to the circle of b in diameter and parallel to this line  $A_1A_2$ . To avoid regular hexagons, these vertices are chosen in a random way between the two extremal cases which are on one hand the point located on the large circle (point  $P_1$  in figure 1) and on the other hand the point such as the small circle is the inscribed circle (point  $P_2$  in figure 1). In this work, we studied five different values of the elongation ratio:  $\frac{b}{a} = 1$  (circular particle); 0.8; 0.7; 0.6 and 0.5. The most elongated hexagons have thus their largest dimension twice the smallest one.

The granular sample is contained inside a box with rigid walls and the grains are perfectly rigid in these numerical simulations. Since each sample is made of grains with different shapes, we used a sample creation leading to the densest state (maximal relative density). First, a sample of non contacting discs is generated with the particle size distribution chosen and they are then replaced by hexagons so that a = 2r. The hexagons are set with a random orientation, a random velocity and normal and tangential coefficients of restitution equal to 1 in order to have chocks without energy dissipation. The gravity and the coefficients of friction  $\mu_g$  between grains and  $\mu_w$  between walls and particles are set to zero. The sample is isotropically compressed with the same constant velocity applied to the top and the right walls. To avoid a looser area in the center of sample, this displacement is regularly stopped so that the particles are evenly distributed inside the box, before pursuing the compression until a state of isotropic stress is reached. Five different samples with 4995 grains are generated: four of them are made of hexagons and the last one is made of discs. The figure 2 shows zoom in samples for every assemblies generated with the polygonal shapes. This generation procedure allows to obtain homogeneous samples in respect with the density and to avoid a preferential direction of contact normal (figure 3), that would happen if the particles were deposit in the gravity field, especially in that case of elongated particles [17,32]. Moreover, it was also verified that the orientation of particles was randomly distributed: figure 4 shows the polar distributions of the hexagons largest axis orientations.



Figure 2. Zoom in the assemblies made of elongated hexagons at the initial state.



Figure 3. Polar distributions of normal vector orientation in the initial configuration for every elongation ratio.



Figure 4. Polar distributions of hexagon orientations in the initial configuration for every elongation ratio.

#### 3. Results

#### 3.1. Analysis of initial states



Figure 5. Initial void ratio  $e_0$  as a function of the elongation ratio  $\frac{b}{a}$ .

Figure 5 shows the effect of grain elongation on the initial void ratio  $e_0$ . We can note that, for the studied shapes, the sample made of discs  $(\frac{b}{a} = 1)$  is the loosest sample, which is consistent with previous numerical studies about the effect of particle angularity [14,15]. When the particle shape slightly deviates from the circular shape  $(\frac{b}{a} = 0.8)$ , the initial void ratio decreases to reach a minimum for  $\frac{b}{a} = 0.7$ , which corresponds to an aspect ratio  $\frac{a}{b} \approx 1.5$ . It is the same result as [33,34,35] who obtained, experimentally and numerically, the densest packing for ellipsoids with an aspect ratio equal to 1.5. For lower elongation ratio, the initial void ratio increases. The angularity of polygons allows first to reach a denser initial state, but the particle elongation reduces this ability and for very elongated particles, a larger initial void ratio is expected, as observed by [32,33,34].

We can also remark in figures 3 and 4 that the samples made of hexagons with  $\frac{b}{a} = 0.8$  and  $\frac{b}{a} = 0.7$  present distributions of contact directions and particle orientations with more fluctuations, in spite of the isotropic procedure used to generate the samples. This is because these hexagons are almost regular and only very slightly elongated. So, during the sample preparation, they arrange themselves with face-to-face contacts having almost all the same orientation. As a consequence, these samples also exhibit a more variable orientation distribution. It would be interesting to generate samples containing more particles and to test the repeatability of specimen creation in order to see whether a preferential direction emerges.

#### 3.2. Mechanical behaviour in biaxial compression

The biaxial compression tests are performed for a constant confining stress  $\sigma_0 = 10$  kPa by applying a constant horizontal velocity  $V_1$  onto the right wall. To avoid dynamics effects, the velocity  $V_1$  is chosen such as the inertia parameter I defined from [36] is small enough:  $I = \dot{\varepsilon} \sqrt{\frac{m}{\sigma_0}} \leq 10^{-3}$ . The coefficients of friction are set to 0.5 between particles and kept to zero between walls and particles. For these quasistatic simulations, the contact network slowly evolves, so the restitution coefficients are decreased to  $e_N = 0.2$  and  $e_T = 0.1$ . Figures 6 and 7 show the stress-strain curves and the volumetric behaviour of samples during the biaxial compression. Since the samples are dense, the evolution of  $\frac{q}{p} = \frac{\sigma_1 - \sigma_2}{\sigma_1 + \sigma_2}$  as a function



Figure 6. Evolution of  $\frac{q}{p} = \frac{\sigma_1 - \sigma_2}{\sigma_1 + \sigma_2}$  as a function of the axial strain  $\varepsilon_1$  for the sample of discs and 3 samples of elongated particles.



Figure 7. Evolution of  $\varepsilon_V$  as a function of the axial strain  $\varepsilon_1$  for the sample of discs and 3 samples of elongated particles.

of the axial strain  $\varepsilon_1$  exhibits a peak followed by a softening leading to a residual state. The behaviour of the discs sample is different from the behaviour of hexagons samples: the shear resistance and the dilatancy are greater for the samples made of non-circular particles. Angularity and particle elongation allow a better mobilization of friction at contacts and restrict grain rotation, as it will be shown in the following section.

The effect of elongation on the value of the internal friction angles at peak  $\Phi^{peak}$  and at the residual state  $\Phi^*$  is shown in figure 8, where  $\sin \Phi = \frac{\sigma_1 - \sigma_2^2}{\sigma_1 + \sigma_2^2}$ . The sample made of hexagons with  $\frac{b}{a} = 0.7$  exhibits the larger  $\Phi^{peak}$  value, that can be connected with the fact that it is also the densest sample. Then  $\Phi^{peak}$  decreases with  $\frac{b}{a}$ . We observe a linear increase of the internal friction angle at the residual state  $\Phi^*$  in the range of the particle elongation examined here. The same result was observe by Ng [35] for samples made of ellipsoids with similar aspect ratios. In our study, the procedure chosen to generate the hexagons does not allow to model particles with  $\frac{b}{a}$  greater than 0.8. So we can not predict the evolution of  $\Phi^*$  and  $\Phi^{peak}$  for samples composed of particles whose shape gradually approaches a circular one. On the other hand, it would be interesting to simulate samples with more elongated particles ( $\frac{b}{a} < 0.5$ ) to check whether the linear increase of  $\Phi^*$  is confirmed or whether there is a value of  $\frac{b}{a}$  from which it no longer increases.



Figure 8. Effect of the elongation ratio  $\frac{b}{a}$  on the friction angle at peak  $\Phi^{peak}$  and at the residual state  $\Phi^*$ .

#### 4. Discussion

A lot of results found in the previous section can be explained by the particle angularity allowing them to exhibit face-to-face contacts. At the initial state, the samples made of polygonal particles are denser because this angular shape is able to better fill up the voids than the circular one. But beyond the elongation ratio  $\frac{b}{a} = 0.7$  these face-to-face contacts are less and less possible (there are 15% of face-to-face contacts in the sample with  $\frac{b}{a} = 0.8$ , whereas there are only 10% in the sample with  $\frac{b}{a} = 0.5$ ) because the prevailing mechanism is the volume exclusion while it is negligible for a small deviation from the circular shape [37]. So, the initial void ratio increases for the samples made of the most elongated hexagons.

This ability for the angular particles to have face-to-face contacts also restricts the grain rotation during the biaxial compression. For the sample of discs, 77% of grains have a cumulative rotation (from the initial state to  $\varepsilon_1 = 20\%$ ) greater than  $\pm 15^\circ$ , while less than 50% of hexagons rotate more than  $15^\circ$  in absolute value for the same axial strain  $\varepsilon_1$ , whatever their elongation ratio. Moreover, these large rotations are not distributed in the same way for the discs than for the polygons: large rotations are uniformly distributed inside the sample of discs (figure 9) but are located along thin bands for the samples of hexagons (figure 10). This phenomenon is linked with the width and persistence of shear bands, which is not the same in samples of discs and samples of polygons. They are more spread in the case of circular particles and are very volatile. In figure 11 the large cumulative rotation of discs is shown for strain increments of 5%. One can see that zones where the cumulative rotation is large move depending on the strain amplitude. On the contrary for samples made of angular grains, shear bands are thinner [38] and they change very little during the deformation, as shown in figure 12. This is consistent with the result obtained by [2], [39] and [40] which performed numerical simulations on samples of discs but by introducing some rolling resistance at contact points in order to reproduce a high gradient of particle rotation along the shear band, as it is found in actual sand. Finally, we can note that for these hexagonal particles, the rotations have the same direction inside a given shear band (anticlockwise or clockwise), this confirms the importance of sliding contacts (increasing the mobilization of friction) for these elongated shapes.



Figure 9. (a) Cumulative rotation of discs from initial state to  $\varepsilon_1 = 20\%$ . The discs which rotate more than 15° anticlockwise are filled in black and respectively in white if it is a clockwise rotation. (b) Relative displacement of discs from initial state to  $\varepsilon_1 = 20\%$  showing the location of zones associated to large displacements.



Figure 10. (a) Cumulative rotation of hexagons with  $\frac{b}{a} = 0.5$  from initial state to  $\varepsilon_1 = 20\%$ . The grains which rotate more than 15° anticlockwise are filled in black and respectively in white if it is a clockwise rotation. (b) Deformation after  $\varepsilon_1 = 20\%$  of an initial regular grid imprint on the sample of hexagons with  $\frac{b}{a} = 0.5$  at the initial state, showing the location of the most distorted zones. (c) Relative displacement of hexagons with  $\frac{b}{a} = 0.5$  from initial state to  $\varepsilon_1 = 20\%$  showing the location of zones associated to large displacements. The cases of hexagons with  $\frac{b}{a} > 0.5$  are similar.

#### 5. Conclusions and perspectives

Numerical simulations of biaxial compression were performed on samples composed of either hexagons or discs in order to analyse the effect of particle angularity and elongation. The mechanical response of these samples was analysed in particular in comparison to that of a sample of circular particles. Our results show that particle shape modify the global and local behaviours of these granular materials.



Figure 11. Cumulative rotation of discs (a) from initial state to  $\varepsilon_1 = 5\%$  and (b) from  $\varepsilon_1 = 5\%$  to  $\varepsilon_1 = 10\%$ . The grains which rotate more than 5° anticlockwise are filled in black and respectively in white if it is a clockwise rotation.

- For the range of  $\frac{b}{a}$  ratio studied and for the same initial confining pressure, the samples made of angular particles are denser than the sample made of circular particles, but the particle elongation reduces this ability and density of samples with hexagons decreases with their elongation.
- Samples made of angular particles exhibit larger shear strength and dilatancy due to the face-to-face contacts that restrict rotations and the friction angle at the residual state is found to linearly increase with the particle elongation, for the range of  $\frac{b}{a}$  ratio studied.
- The large rotations are distributed inside the whole sample of discs whereas they are located inside thin bands for the samples made of angular grains, because the shear bands are thinner and more persistent in these media.

Therefore, DEM simulations using only circular or spherical particles seem too restrictive. If the introduction of rolling resistance is an attractive solution [39,40], the difficulty of this strategy lies in choosing the value of such a parameter. Taking into account the non-circular shape of the particles (angularity and elongation) allow to introduce into the numerical model only parameters whose physical origin is clear.

Further analyses are presently under way in order to correlate these results with the evolution of some local parameters (coordination number, anisotropy of contact forces) and to clarify the effect of particle elongation. Comparisons with the results obtained for samples made of some other shapes (octagons [41], clumps made of overlapping discs [42,43], rectangles with rounded caps [37]...) are also in progress, in order to extend this analysis and to generalize the effect of the grain shape on the mechanical behaviour of granular materials.

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Figure 12. Cumulative rotation of hexagons with  $\frac{b}{a} = 0.2$  (a) from initial state to  $\varepsilon_1 = 5\%$  (b) from  $\varepsilon_1 = 5\%$  to  $\varepsilon_1 = 10\%$  (c) from  $\varepsilon_1 = 10\%$  to  $\varepsilon_1 = 15\%$  and (d) from  $\varepsilon_1 = 51\%$  to  $\varepsilon_1 = 20\%$ . The grains which rotate more than 5° anticlockwise are filled in black and respectively in white if it is a clockwise rotation.

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