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A methodology to integrate reliability into the conceptual design of safety-critical multirotor unmanned aerial vehicles

Jonathan Liscouët^{a,*}, Félix Pollet^b, Joël Jézégou^b, Marc Budinger^c, Scott Delbecq^b, Jean-Marc Moschetta^b

^a Concordia University, 1455 De Maisonneuve Blvd., Montreal, QC H3G 1M8, Canada

^b ISAE-SUPAERO, Université de Toulouse, 10 Avenue Edouard Belin, 31400 Toulouse, France

^c ICA, Université de Toulouse, UPS, INSA, ISAE-SUPAERO, MINES-ALBI, CNRS, 3 rue Caroline Aigle, 31400 Toulouse, France

A B S T R A C T

This article introduces a new conceptual design methodology to evaluate and explore underactuated electric multirotor unmanned aerial vehicle (UAV) designs for safety-critical applications. A case study focusing on medical transport in an urban environment demonstrates the methodology's effectiveness. The current state of the art does not provide conceptual design methodologies that integrate reliability considerations for multirotor UAVs. The proposed methodology addresses this gap by developing systematic reliability calculation and introducing sizing based on failure cases. For this purpose, controllability and reliability analysis methods are developed and linked to an analytical sizing methodology. The controllability analysis is based on the available control authority index adapted for failure case assessment and reliability analysis. The link between the controllability analysis and the sizing methodology is achieved by introducing failure case sizing factors. The sizing relies on a modern analytical database-free methodology with multidisciplinary design optimization for design customization and computational efficiency. This methodology is developed with new design models to cover failure cases in forward flights. When applied to the case study, the methodology efficiently evaluates and compares five concepts and indicates that only two comply with both the safety and reliability requirements and mission specifications (payload and range). More specifically, the methodology shows the major impact of reliability considerations on the case study with sizing factors that almost double or triple the required rotor thrusts depending on the design. This methodology is applicable to challenging future multirotor UAV applications that require to demonstrate high safety levels and redundancies, such as urban air taxis, flying ambulances, and search and rescue and medical equipment transport.

Keywords:

Fault tolerance

Reliability

Controllability

Multidisciplinary design optimization (MDO)

Model-based design

Airworthiness regulations

1. Introduction

For the past two decades, multirotor unmanned aerial vehicles (UAVs), also known as drones, have been intensively developed. These vehicles, which operate without the involvement of human operators, can accomplish preassigned tasks that have the potential to change people's daily lives, such as functioning as urban air taxis, flying ambulances, and search and rescue and medical equipment transports. Such operations, which are beyond visual line of

sight (BVLOS) and usually over densely populated areas, are safety critical. Technical failure resulting in an uncontrollable UAV could be catastrophic if the vehicle collides with humans, aircraft, helicopters, or infrastructure, and the damage caused by accidents increases with the size, weight, and speed of the vehicle. Therefore, the design of such vehicles must be driven by safety considerations. Here, safety refers to flight control reliability because the safety of a UAV largely depends on this control in the event of failure.

Another primary challenge is energy efficiency, which is mainly driven by weight, specifically the maximum takeoff mass (MTOM). The weight challenge is highlighted for electric UAVs due to the low energy density of the batteries compared to conventional fossil fuel solutions. Hence, the emergence of multirotor UAVs for demanding safety-critical applications depends on the designers' ability to optimize designs for energy efficiency while also considering reliability.

* Corresponding author.

E-mail address: jonathan.liscouet@concordia.ca (J. Liscouët).

Nomenclature

Latin Symbols

A	State matrix
B	Control matrix
B_f	Control effectiveness matrix
C	Torque N m
C_i	Number of controllable failure cases of multiplicity i
C_P	Propeller power coefficient
C_T	Propeller thrust coefficient
C_d	Airframe drag coefficient
C_l	Airframe lift coefficient
D_f	Airframe drag N
D_{in}, D_{out}	Inner and outer diameters of the arms m
D_{pro}	Propeller diameter m
E	Energy J
F	Probability of failure
f	Rotor thrust vector
G	External disturbance vector
g	Gravity acceleration m/s^2
H	Failure matrix
h	Altitude m
J	Advance ratio
J_{OP}	Zero-Power Advance Ratio
J_{OT}	Zero-Thrust Advance Ratio
J_{axial}	Axial advance ratio
J_f	Matrix of inertia
K_i	Failure case sizing factor vector
K_{max}	Max. failure sizing factor vector
k	Max. number of simultaneous rotor failures considered in the design
k_M	Oversizing coefficient on the load mass
k_{ND}	Undersizing coefficient for the propeller speed
k_{esc}	Oversizing coefficient on the electronic speed controller power
k_{frame}	Ratio inner/outer diameter for the arms
k_{mb}	Sizing coefficient on the battery mass
k_{mot}	Oversizing coefficient on the motor torque
k_r	Number of necessary components of a k-out-of-n redundancy
$k_{speed\ mot}$	Oversizing coefficient on the motor speed
k_{thrust}	Thrust-to-weight ratio
k_{vb}	Oversizing coefficient for the battery voltage
L	Roll torque N m
L_{arm}	Arm length m
L_f	Airframe lift N
M	Pitch torque N m
m	Number of rotors
m_a	Multirotor total mass kg

m_{arms}	Arm mass kg
m_{body}	Body mass kg
N	Yaw torque Nm
N_{arms}	Number of arms
n_{pro}	Propeller rotational frequency m/s
n_r	Total number of components of a k-out-of-n redundancy
P	Power W
p	Roll rate rad/s
q	Pitch rate rad/s
R	Reliability
r	Yaw rate rad/s
S	Airframe area m^2
T	Control thrust N
t	Exposure time h
U	Voltage V
u_f	Control vector
v	Vehicle velocity m/s
v_∞	Free stream velocity m/s
x	State vector

Greek Symbols

α	Angle of attack rad
β	Propeller pitch-diameter ratio
δ	Incidence Thrust and Power correction factor
θ	Pitch rad
θ_{FP}	Flight path angle rad
λ	Failure rate h^{-1}
ρ_{air}	Air density kg/m^3
σ_{max}	Maximum allowable stress N/m^2
ψ	Yaw rad
ϕ	Roll rad

Attributes

'	Failure case
hov	Hover flight regime
cl	Climb flight regime
fwd	Forward flight regime
to	Takeoff regime
bat	Battery
esc	Electronic speed controller
frame	Frame
mot	Motor
pro	Propeller
mission	Mission
ref	Reference component
max	Maximum value

Accordingly, our objective is to develop a new conceptual design methodology with which to evaluate and explore designs for safety-critical applications. We focus on design evaluation and exploration to ascertain whether an aircraft can be built that meets performance and safety requirements [1]. It is essential to identify, evaluate, explore, and compare solutions to find the optimal concept for transition to the preliminary design, where no major design changes should occur [1]. The article's scope is the design of fully electric underactuated multirotor UAVs with fixed rotor thrust directions (i.e., no vectoring control or articulated rotor system). Nevertheless, the proposed methodology provides a framework for further adaptations to other classes of UAVs, such as fully actuated multirotors, fixed-wing and hybrid configurations, and alternate propulsion system technologies.

A core activity of the conceptual design is sizing, which aims to optimally size and specify the main components of the design to achieve the performance objectives. The published literature provides many empirical methodologies for sizing fixed-wing [2] and multirotor UAVs [3], [4]. These methods are derived from established fixed-wing aircraft and rotorcraft design methods [1], [5]. Alternative methods adopt an analytical approach to allow for greater customization of the designs being evaluated. Many of the analytical methods are built on component databases combined with an optimization problem [6–12]. The online tool *flyeval* [13–16] proposes a method for finding the optimal propulsion system using product data provided by the manufacturers. However, this method is limited by its focus on optimizing the component selection locally rather than optimizing this selection at the UAV

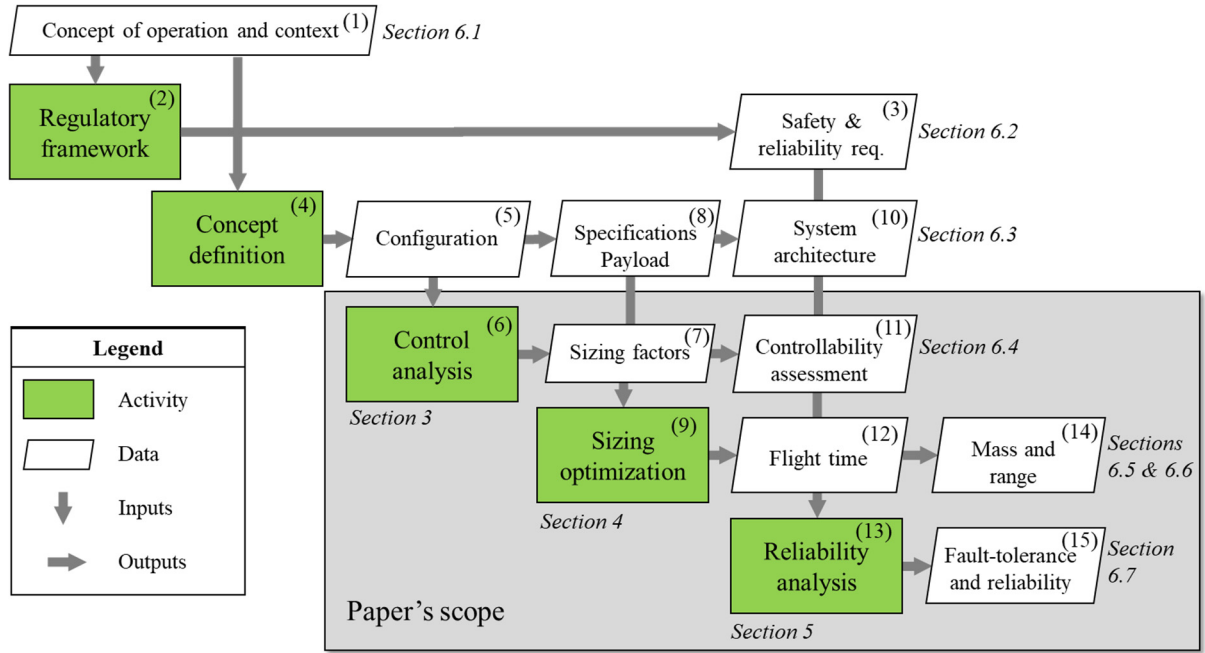


Fig. 1. Adapted extended design structure matrix diagram of the proposed conceptual design methodology.

level. Other authors address the optimization problem at the system scale with either an exhaustive search [10] or gradient-free algorithms [6], [8], [9], [11], [12]. In both cases, the process is time consuming. Alternatively, database-free methodologies introduce component estimation models [17–21] to streamline the sizing process for computation efficiency. However, none of these design methodologies integrate reliability considerations. Research on high reliability multirotor UAVs has focused on proposing specific fault-tolerant designs and control strategies [22–26] by evaluating the fault tolerance of given configurations [27], [28] or optimizing control to maximize operational reliability [29]. Hence, the current state of the art lacks effective conceptual design methodologies for multirotor UAVs that take reliability into account.

The proposed methodology addresses this gap by developing systematic reliability calculation and introducing sizing based on failure cases. For this purpose, controllability and reliability analysis methods are developed and linked to an analytical sizing methodology. The controllability analysis is based on the authority control index (ACAI) adapted for failure case assessment and reliability analysis. The link between the controllability analysis and the sizing methodology is achieved by introducing failure case sizing factors. The sizing relies on a modern analytical database-free methodology with multidisciplinary design optimization (MDO) for design customization and computational efficiency. This methodology, previously introduced by the authors [17], [18], [30], is further advanced to include the failure cases in the sizing process and ensure that the UAV will have sufficient control authority. In particular, the sizing optimization problems presented [18], [30] are reformulated to address non-nominal flight regimes, and the design models introduced in [17] are further advanced to include new design parameters to explore the effects of technological innovations on UAV performance. The effectiveness of the new methodology is validated and demonstrated with a case study on a new multirotor UAV for medical transport (e.g., organ transplants) in an urban environment.

Section 2 introduces the overall methodology. Section 3 describes how the control analysis provides a controllability assessment and sizing factors for reliability analysis, which includes failure cases in the sizing. Section 4 focuses on the sizing. It introduces the new design models and describes the optimization

problem with the sizing. Section 5 describes how generalized reliability calculations process the controllability assessment to systematically evaluate the reliability. Section 6 introduces the case study and discusses the design exploration, sizing, and reliability results. Finally, Section 7 concludes the article.

2. Proposed methodology

Fig. 1 represents the proposed methodology in the form of an adapted eXtended Design Structure Matrix (XDSM) diagram [31], [32]. The diagram shows a methodology divided into five main steps: analysis of the regulatory framework, concept definition, control analysis, sizing optimization, and reliability analysis. This paper focuses on control analysis, sizing optimization, and reliability analysis.

A concept of operation (1) describes the operational employment, environment, and attributes of a proposed system from the user's viewpoint [33]. An example of information contained in a concept of operation that is essential for the proposed design methodology is provided in the case presented in Section 6.1. As shown in Fig. 1, the regulatory framework analysis (2) of the concept of operation identifies the safety and reliability requirements (3) that apply to the design. The concept definition (4) provides candidate designs. The outputs of the regulatory framework analysis and concept definition are illustrated in the case study in sections 6.2 and 6.3. The concept configuration (5) initiates the control analysis (6) based on controllability and control allocation analyses. The control analysis is developed in Section 3. The proposed methodology introduces sizing factors (7), which are factors applied to the rotor thrust specification to include the failure cases in the sizing process and thus ensure consistency between the controllability assessment and operational performance. Together with the sizing factors, the mission and concept specifications (8) are used to converge to an optimal sizing (9) for the mission, thus, minimizing weight or maximizing range and ensuring that the operation is within each component's technological constraints. The sizing methodology developed in Section 4 is highly multidisciplinary. The system architecture (10) from the concept definition, the controllability assessment (11) from the control analysis, and the flight time (12) from the sizing optimization then permit a

reliability analysis (13) of the concept. The reliability analysis is developed in Section 5. Finally, the results of the sizing optimization (14) and reliability analysis (15) can be used to explore and compare different concepts or technologies, negotiate performance with mission specifications, and provide valuable insights into the design to select the optimal one. This final step is illustrated with the case study in Section 6.

3. Control analysis

The safety and reliability assessment aims to automatically evaluate the safety and reliability of the specified design concepts. The safety of operation depends primarily on the capability of the flight control system to ensure controllability under adverse conditions, such as in cases of a rotor failure. Therefore, a methodology is presented that formalizes and systematizes the association of a modern controllability assessment approach with reliability calculations and control allocation. The methodology is applied to assess each concept's safety and reliability and provide sizing factors for the controllable failure cases to be used in the sizing process for a consistent design.

3.1. Controllability analysis

The controllability analysis aims to differentiate the potentially controllable from the uncontrollable failure cases. The first challenge results from the difficulty of applying classical controllability theory to the multirotors, while the second challenge results from the lack of design information inherent to the conceptual design phase.

Some studies of fault-tolerant control of quadcopters have proposed emergency landing procedures to avoid a catastrophic condition from a single rotor failure [23–25], [34], [35]. The incorporation of such a procedure would represent a significant improvement in the reliability of quadcopters. However, these procedures do not maintain the yaw control. Here, similar to the case study discussed by Saad and Liscouët [36], a failure can occur in cruise flight, and the control scheme must completely stop the speeding vehicle and engage a hover mode before performing a controlled descent. This procedure requires sufficient control of all control axes. For this reason, the present analysis assumes that catastrophic failure can be avoided only if the UAV maintains full or degraded control over all control axes.

3.1.1. Underactuated multirotor dynamics model

The underactuated multirotor UAVs with fixed rotor thrust directions are approximated with the following dynamics model linearized for a hover flight condition for simplicity [27], [37–39]:

$$\dot{x} = Ax + B(u_f - G), \quad (3.1)$$

where $x = [h \ \phi \ \theta \ \psi \ v_h \ p \ q \ r]^T \in \mathbb{R}^8$ is the state vector with h as the altitude [m]; ϕ , θ , and ψ are the roll [rad], pitch [rad], and yaw [rad] angles; v_h is the vertical velocity [m/s]; and p , q , and r are the roll, pitch, and yaw rates [rad/s]. In addition, $A = \begin{bmatrix} 0_{4 \times 4} & I_4 \\ 0 & 0 \end{bmatrix} \in \mathbb{R}^{8 \times 8}$ represents the state matrix; $B = \begin{bmatrix} 0 \\ J_f^{-1} \end{bmatrix} \in \mathbb{R}^{8 \times 4}$ represents the control matrix with J_f as the vehicle's matrix of inertia; $u_f = [T \ L \ M \ N]^T \in \mathbb{R}^4$ represents the system total thrust/torque with T as the lift force [N] and L , M , and N as the roll, pitch, and yaw moments [N·m]; and $G \in \mathbb{R}^4$ represents the external disturbance vector.

For simplicity, the vehicle's center of gravity is assumed to be fixed and aligned with the vehicle's geometrical center. This hypothesis reduces the external disturbance vector to the vehicle's weight [27]:

$$G = [m_a g \ 0 \ 0 \ 0]^T \in \mathbb{R}^4, \quad (3.2)$$

where m_a is the vehicle mass [kg], and g is the gravity acceleration [m/s²].

3.1.2. Available control authority index

In the classical controllability theory introduced by Kalman, assessing the controllability of a control system involves the well-known rank test of the controllability matrix. However, as noted in previous work [27], [39, Ch. 10], [40], the classical theory requires the origin point to be an interior point of the achievable control constraint set, which is not always the case with rotor failures. In the same way, the classical controllability analysis method requires the control allocation to be defined [39, Sec. 10.4.2], which can be an issue under rotor failures since, by definition, an operational control allocation cannot be defined for uncontrollable cases. Therefore, as an alternative, the ACAI introduced by Du et al. [27] is used in this study to evaluate the minimum control authority remaining after a failure. This subsection synthesizes the calculation of the ACAI before adapting it to failure cases in Section 3.1.3.

The main component of the control authority is the previously defined system's total thrust/torque u_f , which results from the rotor thrust vector f as follows [27]:

$$u_f = B_f f, \quad (3.3)$$

where $B_f \in \mathbb{R}^{4 \times m}$ is the control effectiveness matrix reflecting the configuration and geometry of the vehicle's design, and $f \in \mathbb{R}^m$ is the rotor thrust vector with m as the number of rotors.

Each rotor provides a purely positive and limited thrust, leading to the following rotor thrust vector constraint set:

$$\mathcal{F} = \{f \mid f = [f_1, \dots, f_m]^T, 0 \leq f_i \leq f_{\max,i}\}, \quad (3.4)$$

where f_i is the thrust of i -th rotor and $f_{\max,i}$ is the maximum thrust [N] of the i -th rotor.

Eq. (3.3) and (3.4) provide the system's total thrust/torque constraint set [27]:

$$\Omega = \{u_f \mid u_f = B_f f, f \in \mathcal{F}\} \quad (3.5)$$

The ACAI is a measure of the maximum control thrust/torque that can be produced in all directions (T , L , M , and N) after considering the effect of external disturbance. More specifically, it is the radius of the largest enclosed four-dimensional sphere centered at G in the attainable total thrust/torque constraint set Ω [27]:

$$\rho(G, \partial\Omega) \triangleq \begin{cases} \min \{\|G - u_f\| : G \in \Omega, u_f \in \partial\Omega\} \\ -\min \{\|G - u_f\| : G \in \Omega^c, u_f \in \partial\Omega\}, \end{cases} \quad (3.6)$$

where $\partial\Omega$ is the boundary of Ω and Ω^c is the complementary set of Ω . Detailed information on the computation of the ACAI is provided by Du et al. [27].

As demonstrated by Du et al. [27], a configuration is potentially controllable in all directions only if

$$\text{rank } C(A, B) = 8 \text{ and } \rho(G, \partial\Omega) > 0, \quad (3.7)$$

where $C(A, B)$ is the system controllability matrix, and the previous condition verifies that it is full rank.

3.1.3. Available control authority index for failure cases

The proposed methodology is based on assessing the controllability of each possible failure case. Each failure case whose ACAI is verified (3.6) will be considered potentially controllable. Accordingly, this subsection introduces a new approach to calculating the

ACAI for failure cases. The first step is to define the full set of failure cases to be considered with a systematic combination of one to k rotor failure(s). Limiting the number of failed rotors to a maximum value k is a practical design rule to prevent overdesigning for cases that are extremely improbable. It assumes that the UAV flight control system will not adapt or reconfigure for more than k rotor failures. Hence, any combination of more than k rotor failures will lead to loss of control. The total number of failure cases to be assessed, j , is given by

$$j = \sum_{i=1}^k \frac{m!}{i!(m-i)!}, \quad (3.8)$$

where m is the total number of rotors and $k \in [1, \dots, m-1]$ is the maximum number of simultaneous rotor failures to be considered in the design.

The second step is to define a failure matrix for each possible failure case as follows:

$$H_j = \text{diag}(\eta_1, \dots, \eta_m), \quad (3.9)$$

where H_j is the failure matrix of the j -th failure case and the parameters $\eta_i \in \{0, 1\}$, $i = 1, \dots, m$ represent available ($\eta_i = 1$) and failed ($\eta_i = 0$) rotors.

The third step is to define the control effectiveness matrix from the failure matrix for each failure case:

$$B'_{f,j} = B_f H_j, \quad (3.10)$$

where $B'_{f,j}$ is the control effectiveness matrix reflecting the effect of the j -th failure case.

Then, the fourth step is to define the system total thrust/torque constraint set for each failure case as follows:

$$\Omega'_j = \{u'_{f,j} \mid u'_{f,j} = B'_{f,j} f, f \in \mathcal{F}\}, \quad (3.11)$$

where Ω'_j is the remaining system total thrust/torque constraint in the j -th failure case.

Finally, the ACAI can be calculated for each failure case as the following:

$$\rho'_j(G, \partial\Omega') \triangleq \begin{cases} \min \left\{ \|G - u'_{f,j}\| : G \in \Omega'_j, u'_{f,j} \in \partial\Omega'_j \right\} \\ -\min \left\{ \|G - u'_{f,j}\| : G \in \Omega'^c_j, u'_{f,j} \in \partial\Omega'_j \right\}, \end{cases} \quad (3.12)$$

where $\rho'_j(G, \partial\Omega')$ is the ACAI for the j -th failure case, $\partial\Omega'_j$ is the boundary of Ω'_j , and Ω'^c_j is the complementary set of Ω'_j .

The result of the controllability analysis represents the controllability assessment of all the failure cases and the counts of controllable cases for each failure case of multiplicity i , C_i . For no-failure $i = 0$ (and $C_0 = 1$), single failures $i = 1$, double failures $i = 2$, and so on, with $i = [0, \dots, k]$. This result enables the reliability calculation developed in Section 5. Additionally, the identification of each controllable case enables the assessment of sizing factors for the failure cases as per Section 3.2.

3.1.4. Lack of design information

A major challenge of the proposed approach based on the ACAI stems from the inherent lack of design information in the conceptual design phase. The proposed controllability analysis requires a wholly defined aircraft dynamics model in Eq. (3.1). Defining the design configuration and geometry, meaning the number of rotors and their orientations and positions relative to the geometrical center, is not sufficient to complete the aircraft dynamics

model. Further design information is required, such as the vehicle mass and inertia matrix, maximum rotor thrusts, and the reactive torque-to-thrust coefficient of the rotors.

At the conceptual design level, the thrusts and torques required to transition from one flight phase to another are neglected to focus on the thrusts and torques required to maintain controllability in a stabilized phase. In addition, prior to sizing, the design hypothesis related to sizing should not restrict performance or affect the controllability assessment. Therefore, non-restrictive generic design values are defined according to these hypotheses to compensate for the missing design information. Alternatively, empirical data can be used. For example, the thrust-to-weight and reactive torque-to-thrust ratios can be based on off-the-shelf design data trends.

3.2. Failure case sizing factor

The failure case sizing aims to include the failure cases in the sizing process to ensure that the UAV will have sufficient control authority following any failure assessed as controllable. To this end, this section introduces failure case sizing factors linking the controllability assessment to the sizing process.

The sizing methodology presented in Section 4 requires an estimate of the power demand for each rotor in each failure case. Accordingly, the failure case sizing factor is defined as the rotor thrust vector ratio of a failure case to the normal operation. In this way, the power demand of each rotor in a failure case can be directly scaled from the power demand in the normal operation. The failure case sizing factors are calculated as follows:

$$K_j = f'_j \oslash f, K_j \in \mathbb{R}^m, \quad (3.13)$$

where K_j is the failure case sizing factor vector of the j -th failure case, f'_j is the rotor thrust vector of the j -th failure case, f is the rotor thrust vector of the normal operation, and \oslash represents the Hadamard or element-wise division.

The rotor thrust vector results from the system total thrust/torque using the control allocation matrix for both the normal and failure cases, and the control allocation matrix is defined using the pseudoinverse approach as follows:

$$\begin{cases} f = P u_f, & \text{with } P = B_f^T (B_f B_f^T)^{-1} \\ & \in \mathbb{R}^{m \times 4} \text{ for normal operation} \\ f'_j = P'_j u'_{f,j}, & \text{with } P'_j = B'^T_{f,j} (B'_{f,j} B'^T_{f,j})^{-1} \\ & \in \mathbb{R}^{m \times 4} \text{ for the } j\text{-th failure case,} \end{cases} \quad (3.14)$$

where u_f is the system total thrust/torque of the sizing maneuver in normal operation, and $u'_{f,j}$ is the required system total thrust/torque of the j -th failure case.

Eq. (3.13) and (3.14) lead to the following failure sizing factor calculation for each failure case:

$$K_j = (P'_j u'_{f,j}) \oslash (P u_f) \quad (3.15)$$

The required system total thrust/torque can generally be alleviated in cases of failure depending on the probability of occurrence. However, it is assumed here that the control authority must be fully preserved in all directions (T, L, M and N) for all the failure cases assessed as controllable; hence, $u'_f = u_f$. The maximum sizing factors obtained for each rotor for all the failure cases provide the maximum sizing factor vector, K_{\max} :

$$K_{\max} = [\max(k_{1,1}, \dots, k_{1,j}), \dots, \max(k_{m,1}, \dots, k_{m,j})] \in \mathbb{R}^m, \quad (3.16)$$

where $k_{i,l}$ is the l -th component of the i -th sizing factor vector K_i .

Applying K_{max} to the maximum rotor thrusts resulting from the calculation of the normal operation performance covers the failure cases in the sizing process (cf. Section 4).

In some cases, the control allocation can include negative values for the rotor thrust. A rotor thrust is unidirectional, and a negative allocation must be avoided. In these cases, reallocation is automatically performed after deactivating the negatively allocated motor. This simple method permits negative values resulting from the pseudoinverse reallocation to be avoided. Future work should incorporate more advanced control allocation methods to avoid the need for this reallocation procedure.

4. Sizing

This section focuses on the sizing of the selected concepts and their performance evaluation using MDO. Low-order models optimizing the computation time accurately represent flight physics and estimate the characteristics of the main UAV components.

4.1. Sizing methodology

The sizing of a multirotor is essentially an inverse process within the conceptual design. The goal is to deduce the characteristics of the components from UAV performance specifications using design models. These models are combined to produce a sizing process, which is implemented into an optimization problem framework. The effect of key design drivers on performance is assessed with a design of experiments approach. Many specialized fields are involved in this process, including aerodynamics, flight physics, propulsion, and weights, due to the multidisciplinary nature of the flying vehicles.

The proposed sizing methodology is based on the database-free methodology introduced by the authors in [18], [30]. The novelty of this methodology lies in the use of low-order estimation models based on scaling laws, similarity laws, or regressions to scale reference components with their operational constraints [17]. This approach provides a computationally efficient solution to sizing. In this study, additional design models are implemented to account for the failures that occur in forward flight. The optimization problem is reformulated to ensure that the optimally sized design remains controllable after the loss of one or two rotors.

4.1.1. Design models

The sizing methodology involves three categories of design models [41]: estimation, simulation, and evaluation models. The estimation models return the characteristics of the sized components. The simulation and evaluation models calculate the quantities driving the sizing of components and their performance. This subsection introduces low-order design models to enable sizing UAVs for missions with multiple flight regimes. Specifically, we introduce flight dynamics models to simulate the flight regimes and estimation models for the power transmission components of the propulsion system and airframe.

Vehicle simulation model – In the context of inverse simulation for sizing, the vehicle simulation model outputs the individual propeller's thrusts and mechanical powers from the specified flight regimes, taking the relevant aerodynamic effects into account. The flight regimes include takeoff, climb, hover, forward flight (i.e., cruise), and descent. In addition, this study considers the failures that occur in forward flight, as discussed in Section 3. Typically, the failure cases determine the maximum propeller thrusts and energy required to complete the mission.

In hovering, the control thrust T_{hov} [N] generated by the propulsion must equal the weight of the UAV. In the absence of

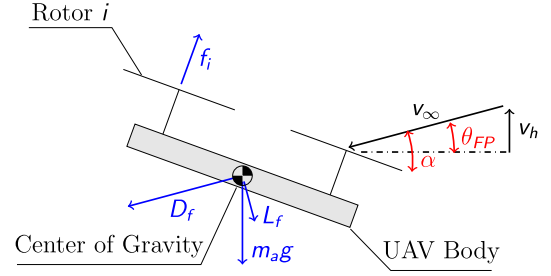


Fig. 2. Side view of a quadcopter in climbing forward flight, adapted from [30].

relative wind, there is no additional force acting on the drone, and the control thrust is expressed as

$$T_{hov} = m_a g \quad (4.1)$$

An additional aerodynamic force resulting from the airframe drag D_f [N] must be accounted for in axial flight (i.e., climb) as follows:

$$T_{cl} = m_a g + D_f = m_a g + \frac{1}{2} \rho_{air} C_d S_{top} v_h^2, \quad (4.2)$$

where C_d is the airframe drag coefficient [-], ρ_{air} is the air density [kg/m³], S_{top} is the top surface of the drone [m²], and v_h the vertical velocity [m/s].

The control thrust must maintain both vertical and horizontal equilibriums when the multirotor is in steady forward flight (i.e., cruise). For simplicity, it is assumed that the center of gravity is fixed and aligned with the geometrical center of the UAV, which avoids external pitch, roll, or yaw torques in this flight phase. Additionally, the normal force of the propellers resulting from asymmetric conditions is omitted according to Y. Leng [21], who showed that this force is of a second order of magnitude compared to the axial force. Fig. 2 illustrates the simplified model, where v_∞ is the free stream velocity [m/s], v_h the vertical velocity [m/s], θ_{FP} is the flight path angle of the drone [rad] equal to 0 in level flight, f_i [N] is the thrust of the i -th propeller, and L_f is the aerodynamic downward force [N]. The angle of attack α [rad] is considered identical for each rotor.

Solving the equilibrium of forces for the angle of attack α [rad] and the total thrust T_{fwd} [N] produces

$$\alpha = \theta_{FP} + \tan^{-1} \frac{D_f \cos \theta_{FP} - L_f \sin \theta_{FP}}{m_a g + D_f \sin \theta_{FP} + L_f \cos \theta_{FP}} \quad (4.3)$$

$$T_{fwd} = \sqrt{(m_a g + D_f \sin \theta_{FP} + L_f \cos \theta_{FP})^2 + (D_f \cos \theta_{FP} - L_f \sin \theta_{FP})^2} \quad (4.4)$$

Transient and non-nominal flight regimes can be expressed relative to the regular scenarios presented above. A thrust-to-weight ratio k_{thrust} [-] is introduced to express the takeoff thrust T_{to} [N] as follows:

$$T_{to} = k_{thrust} m_a g \quad (4.5)$$

The individual propulsive forces of the m propellers are obtained by distributing the control thrust equally for each regime except for the failure case in forward flight, as in the following:

$$f = \frac{T}{m} K_{max} \in \mathbb{R}_+^m, \quad (4.6)$$

where K_{max} is a unity vector for the nominal hover, climb, forward, and takeoff regimes and is defined as per Section 3.2 for the failure cases.

Propeller simulation model – The propeller simulation model provides the aerodynamic efforts for each flight regime, taking into account the propeller geometry. The propulsive force f [N] and mechanical power p [W] of a propeller are expressed as a function of its thrust and power coefficients, C_T [-] and C_P [-], respectively:

$$f = C_T \rho_{air} n_{pro}^2 D_{pro}^4 \quad (4.7)$$

$$p = C_P \rho_{air} n_{pro}^3 D_{pro}^5 \quad (4.8)$$

where n_{pro} is the rotational frequency of the propeller [Hz] and D_{pro} is its diameter [m].

In [17], Budinger et al. applied dimensional analysis and Buckingham's theorem [42], [43] to derive an expression of the power and thrust coefficients in axial flight (i.e., $\alpha = \frac{\pi}{2}$) as a function of the propeller's pitch-diameter ratio β [-] and axial advance ratio J_{axial} [-]. A third-order polynomial regression was then applied to off-the-shelf propeller datasheets from APC [44] to express the power and thrust coefficients in axial flight as follows:

$$\begin{aligned} C_{T, axial}(\beta, J_{axial}) = & 0.02791 - 0.06543 J_{axial} + 0.11867 \beta \\ & + 0.27334 \beta^2 - 0.28852 \beta^3 + 0.02104 J_{axial}^3 \\ & - 0.23504 J_{axial}^2 + 0.18677 \beta J_{axial}^2 \end{aligned} \quad (4.9)$$

$$\begin{aligned} C_{P, axial}(\beta, J_{axial}) = & 0.01813 - 0.06218 \beta + 0.00343 J_{axial} \\ & + 0.35712 \beta^2 - 0.23774 \beta^3 \\ & + 0.07549 \beta J_{axial} - 0.1235 J_{axial}^2 \end{aligned} \quad (4.10)$$

This regression model, which is only valid in axial flight, can be extended to nonaxisymmetric conditions using an analytical correction term, as proposed by Y. Leng [21]. For a given blade geometry (i.e., a fixed pitch-diameter ratio β), the extended regression model is [30]

$$C_{T,P}(\alpha, J) = \eta_{T,P}(\alpha) C_{T,P,axial}(J_{axial}) \quad (4.11)$$

with

$$\eta_{T,P}(\alpha) = 1 + \frac{(J \cos \alpha)^2}{2(\pi \bar{r})^2 \left(1 - \frac{J \sin \alpha}{J_{0T,P}}\right)} \delta(\alpha), \quad (4.12)$$

where $J = \frac{v_{\infty}}{n_{pro} D_{pro}}$ is the advance ratio [-], $J_{axial} = \frac{v_{\infty}}{n_{pro} D_{pro}} \sin \alpha$ is the axial advance ratio [-], and J_{0T} and J_{0P} represent two axial advance ratios when the thrust and power coefficients reach 0. These ratios are obtained from Eq. (4.9), (4.10). In Eq. (4.12), \bar{r} is the position of the representative section of the blade expressed as a percentage of the radius. Here, \bar{r} is assumed to be equal to 75%. Additionally, $\delta(\alpha)$ is a corrective factor for consistency within helicopter analysis.

Fuselage aerodynamics simulation model – The aerodynamic efforts acting on a multirotor are not restricted to propeller forces. The fuselage aerodynamic simulation model outputs the aerodynamic loads on the fuselage from the specified flight regimes. When in motion, the airframe and the payload are subject to drag force and lift force proportional to the square of the relative airspeeds:

$$D_f = \frac{1}{2} C_d \rho_{air} v_{\infty}^2 S_{ref} \quad (4.13)$$

$$L_f = \frac{1}{2} C_l \rho_{air} v_{\infty}^2 S_{ref}, \quad (4.14)$$

where the effective area S_{ref} [m²] is the projected surface facing the relative airflow. The drag coefficient C_d [-] and lift coefficient C_l [-] depend on many parameters such as the body shape, airflow

direction, and surface aspect. Baker et al. [45] provide the following typical drag coefficients for a Reynolds number of 10^4 : 1.05 for a cube shape, 0.47 for a sphere, and 0.04 for a streamlined body.

In addition, the lift of a multirotor acts mostly as a downward force, as depicted in Fig. 2. This force is due to the necessary inclination of the drone in forward flight. However, the fairing of a multirotor can be optimized to minimize drag and provide positive lift in forward flight, as in the Endurance quadcopter by Hitec [46], [47]. Due to the high-level uncertainty involved in determining the multirotor's positive lift in the conceptual phase and utilizing a conservative approach, this lift is ignored in this study. A fixed value $C_d = 0.5$ for the drag coefficient is adopted, which is equivalent to approximating the fuselage as an ideal rounded cylinder.

Estimation models for the power transmission of the propulsion system – The functional parameters and characteristics of the key components of the electric propulsion system are estimated with similarity models developed by Budinger et al. [17]. Specifically, we reuse the motor, electronic speed controller (ESC), and battery estimation models. Unlike the previous propeller simulation model, these estimation models are based on scaling laws rather than data regressions. The scaling laws are obtained using dimensional analysis and Buckingham's theorem and have the advantage of requiring only one reference per component for scaling.

Airframe estimation model – The airframe estimation model provides the UAV space envelope and airframe mass and ensures geometrical and structural integrity. The arms of the geometry model consider the rotor diameter and the number of arms as inputs. Their length L_{arm} (m) is calculated so that the propellers do not collide with each other while minimizing their volume:

$$L_{arm} = \frac{\frac{D_{pro}}{2}}{\sin\left(\frac{\pi}{N_{arms}}\right)}, \quad (4.15)$$

where N_{arms} is the number of arms [-] of the multirotor and D_{pro} is the propeller diameter [m].

The inner diameter D_{in} [m] and outer diameter D_{out} [m] of the rods are then estimated using a stress calculation based on the maximum applied load provided by the vehicle simulation model. The airframe body is considered rigid in comparison to the arms, hence, the problem has to be reduced to cantilever beams. Consequently, the Euler-Bernoulli beam theory applied to a circular hollow section gives the following expression for the outer diameter:

$$D_{out} = \sqrt[3]{\frac{32 f_{max} L_{arm}}{\pi \sigma_{max} (1 - k_{frame}^4)}}, \quad (4.16)$$

where f_{max} [N] is the maximum load applied at the arms' extremities and σ_{max} [N/m²] is the maximum allowable stress of the arm material. The standardized coefficient k_{frame} , inner to outer diameter ratio [-], is defined as a design variable to avoid an under-constrained equation.

Finally, the arms' mass is computed through the geometry and material density, and the body's mass is derived from the arms' mass using a scaling law as follows:

$$m_{body} = m_{body,ref} \frac{m_{arms}}{m_{arms,ref}} \quad (4.17)$$

4.1.2. Sizing optimization

As a result of the high number of disciplines involved in the sizing, we adopt an MDO approach. The resolution of an MDO problem can be computationally expensive due to the high number of variables involved. This study applies the efficient sizing

Table 1
Optimization parameters.

	Parameter	Description
Design variables	k_M	Oversizing coefficient on the load mass
	k_{mot}	Oversizing coefficient on the motor torque
	$k_{speed\ mot}$	Oversizing coefficient on the motor speed
	k_{vb}	Oversizing coefficient for the battery voltage
	k_{ND}	Undersizing coefficient for the propeller speed
	k_{frame}	Ratio inner/outer diameter for the arms
	k_{mb}	Sizing coefficient on the battery mass
	k_{esc}	Oversizing coefficient on the ESC power
	β	Angle pitch/diameter for the propeller
	J_j	Advance ratios
	v_∞	Cruise speed
Constraints	$C_{mot,max} \geq C_{mot,j}$	Motor torque constraints
	$U_{bat} \geq U_{mot,j}$	Battery voltage constraints
	$P_{bat,max} \geq \sum_{i=1}^m P_{mot,i,j}$	Battery power constraints
	$U_{esc} \geq U_{bat}$	ESC voltage constraint
	$P_{esc,max} \geq P_{esc,j}$	ESC power constraints
	$0 \leq v_j - J_j n_{pro,j} D_{pro} \leq 0.05$	Propeller operational speeds constraints
	$n_{pro,max} D_{pro} \geq n_{pro,j} D_{pro}$	Propeller maximum speed constraint
	$E_{bat} \geq E_{mission}$	Mission energy constraint
Objective functions	$MTOM$	Maximum takeoff mass
	$range$	Maximum range

Note: Subscript j refers to the flight regimes introduced in Section 4.1.1.

methodology for multirotors proposed by Delbecq et al. [18] to reduce the complexity and computation time of the problem. This methodology is described in the following:

1. Define a system of algebraic equations based on design models subject to inequality constraints. Design models are discussed in Section 4.1.1.
2. Reduce the number of inequality constraints with a monotonicity analysis. The first monotonicity principle introduced by Papalambros and Wilde in [48] enables the identification of the set of inequalities that can be turned into equalities by studying the variations of the objective and constraint functions for each design variable. The reduction of inequality constraints reduces the complexity and computational cost of a problem.
3. Apply a monolithic normalized variable hybrid (NVH) architecture [49] to the MDO problem. Here, the architecture defines the formulation of the optimization problem and how the different models are coupled [50]. The NVH architecture introduces standardized coefficients to replace the initial design variables and consistency constraints to preserve consistency between the coupling variable inputs and outputs at the optimal solution. This approach solves any multidisciplinary couplings and singularities such as algebraic loops and under- and over-constrained sets of equations.
4. Sequence the sizing equations and expressions explicitly for integration into an optimal sizing code.

The resulting optimization problem is formulated as follows:

$$\begin{aligned}
 &\underset{x}{\text{minimize}} && f(x) \\
 &\text{subject to} && g_j(x) \leq 0, j = 1, \dots, p \\
 &&& x \in X \subseteq \mathbb{R}^n \\
 &&& X = \{(x_i) \in \mathbb{R}^n : 0 \leq x_i \leq \infty\},
 \end{aligned}$$

where

- $f(x)$ is the objective function. For UAV, mass minimization and range maximization are among the most common objectives [8], [11], [12], [18], [51].

- x is the design variable vector that represents a design alternative. Design variables can be continuous (e.g., propeller pitch to diameter ratio), discrete (e.g., number of arms), or Boolean (e.g., deciding whether or not to implement a gear-train). In this study, only continuous design variables are considered. In particular, normalized sizing coefficients k_{mass} , k_{pro} , k_{mot} , k_{esc} , k_{bat} , and k_{frame} are introduced as per the NVH architecture.
- $(g_j)_j$ is the set of inequality constraints ensuring the solution's feasibility. Requirement constraints ensure compliance with the performance requirements. Compatibility constraints ensure compatible components are combined. For example, they ensure electrical compatibility between the ESCs, motors, and battery packs that are essential for a valid design. A constraint on the motor torque (i.e., the sizing factor) ensures the sizing of the propulsion system for the failure cases. A consistency constraint on the MTOM ensures that the estimated MTOM for the vehicle simulation model converges with the actual MTOM calculated from the mass of the components.

The optimization parameters are summarized in Table 1. Fig. 3 provides a visual summary of the resulting MDO architecture for the optimal multirotor design problem with an XDSD diagram [31]. The variables C_j on the left-hand side represent the constraints. An optimizer iterates over a sizing procedure to converge on the best feasible solution. The sizing procedure consists of a feed-forward computational sequence to derive the characteristics of the drone given a set of design variables and specifications. The thin black arrows in Fig. 3 represent the process connections.

The concept is sized with a sequential and inverse approach that begins with the required UAV performance requirements, followed by the sizing of each component, before the verification of the resulting design performance and finally an iteration. More specifically, the flight dynamics model translates the UAV performance into a propeller performance requirement based on an initial MTOM guess. The propeller estimation model sizes the propeller and returns its specification from the performance requirements. The specification parameterizes the inverse simulation model of the propeller, which transforms the propeller performance requirement into the electric motor performance requirement. This cycle is repeated until all the components are sized as per the sizing wave process introduced by Liscouët et al. in [52].

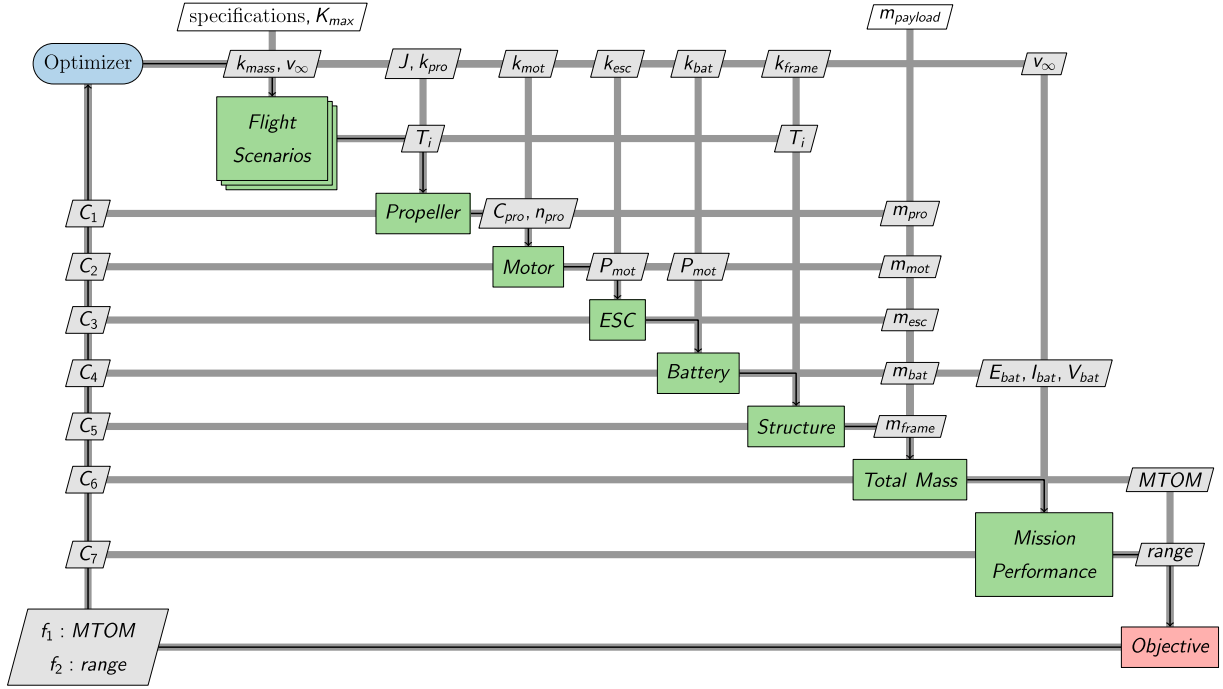


Fig. 3. Extended design structure matrix diagram of the proposed multirotor UAV sizing optimization.

The actual mass of the UAV can then be computed and compared to the initial guess for consistency. The battery specifications are used to compute the actual range as a function of the flight velocity. These computations of the mass and range provide objective functions for optimization.

The sizing optimization was implemented into FAST-OAD, which is a framework for rapid overall aircraft design [53]. It takes advantage of the OpenMDAO environment to offer efficient analysis and optimization capabilities [54]. The gradient-based optimization algorithm SLSQP [55] was chosen as the solver.

5. Reliability analysis

The reliability analysis formalizes and systematizes the link between the controllability and reliability evaluations. For a systematic approach to architecting, the design is divided into the propulsor configuration and the power and control subsystem. The propulsor configuration is characterized by the number of propulsors and their geometrical arrangement, including rotation direction. In this study, we define a propulsor subsystem as the assembly of an ESC, electric motor, and propeller. The power and control subsystem includes the batteries, autopilot, and inertial measurement units (IMUs).

5.1. Reliability analysis hypothesis

The reliability analysis evaluates the reliability of the following function: the provision of full or degraded control of all control axes. The computation is based on independent and random failures, leading to constant failure rates and the convenient exponential distribution. The probability of failure is expressed as follows:

$$F(t) = 1 - e^{-\lambda t}, \quad (5.1)$$

where λ is the failure rate [h^{-1}] and t is the exposure time [h].

The exposure time corresponds to the maximum flight time between two charges and is enforced by the assumption of a built-in test procedure confirming the functionality of each component at

Table 2

Failure rates for high-end transport category aircraft quality.

Component	Failure rate (per hour)
Battery	10^{-6}
Inertial measurement unit (IMU)	$3 \cdot 10^{-6}$
Flight controller	$5 \cdot 10^{-5}$
Electronic speed controller	$1 \cdot 10^{-5}$
Electric motor	10^{-6}
Propeller	10^{-8}

power-up. The flight time is a design optimization variable and results from the sizing described in Section 4.

The failure rates summarized in Table 2 are in the orders of magnitude of modern high-end transport category aircraft equipment. This assumption is likely to be overly optimistic for several applications. Therefore, it will be interesting to evaluate the impact of derating these failure rates. Accordingly, Table 8 shows the reliability of conventional and redundant design for failure rates ranging from the toy industry (x1,000 derating) to high-end transport category aircrafts (no derating).

5.2. Power and control subsystem reliability

The reliability calculation for the generic propulsion system architectures is based on the classical reliability block diagram (RBD) methodology [56]. The reliability of components in series and parallel is obtained as follows [56]:

$$\text{For } n \text{ components in series, } R_s(t) = \prod_{i=1}^n R_i(t) \quad (5.2)$$

$$\text{For } n \text{ components in parallel, } R_p(t) = 1 - \prod_{i=1}^n (1 - R_i(t)), \quad (5.3)$$

where $R_i(t)$ is the reliability of the i -th component.

Information technologies can rely on more sophisticated redundancies, such as a majority voting redundancy [56]. For example, a flight control computer receiving air data from three independent

flight sensor sources can protect against a flight sensor failure by comparing the data from the three sources and isolating the divergent one. In this case, the reliability is obtained using a k -out-of- n redundancy calculation as follows [56]:

$$R_{k_r/n_r}(t) = \sum_{i=k_r}^{n_r} \frac{n_r!}{i!(n_r-i)!} R^i (1-R)^{n_r-i}, \quad (5.4)$$

where $R_{k_r/n_r}(t)$ is the reliability of a k_r -out-of- n_r redundancy, $R(t)$ is the reliability of the identical components of the redundancy, n_r is the total number of components, and k_r is the minimum number of components necessary for the function.

5.3. Propulsor configuration subsystem reliability

A reliability calculation for a propulsor configuration based on controllability analysis and Boolean algebra was previously presented in [28], [36]. In this study, this approach is formalized and systematized toward automatization.

The reliability is calculated from the union of the probabilities of each controllable case, including the failure-free case. Finally, the controllable cases are expressed as mutually exclusive so that the reliability is a systematic sum of their probabilities as formalized below:

$$R_{PC}(t) = \sum_{i=0}^k C_i \cdot R_{pr}(t)^{m-i} \cdot (1 - R_{pr}(t))^i, \quad (5.5)$$

where $R_{PC}(t)$ is the reliability of the propulsor configuration, $R_{pr}(t)$ is the reliability of a propulsor, and C_i is the number of controllable cases of the failure cases of multiplicity i . The C_i are provided by the control analysis as per Section 3.1.3.

The reliability of a propulsor is the product of the speed controller, motor, and propeller reliabilities. Finally, the overall reliability $R_{sys}(t)$ is obtained by combining the power and control subsystem and propulsor configuration reliabilities as two sub-assemblies in series using Eq. (5.2). The overall reliability is normalized by the flight duration, t , for comparison with the regulation requirements provided as average probabilities per flight hours (cf. Section 6.2):

$$R_{sys}(t) = \frac{R_{EC}(t) \cdot R_{PC}(t)}{t}, \quad (5.6)$$

where $R_{EC}(t)$ is the reliability of the power and control subsystem.

6. Case study

This section presents a case study that illustrates the application of the developed methodology and tool. The choice of application and mission profile emphasizes the sizing and safety challenges, while the analysis of the applicable regulation provides the safety and reliability requirements. The selected concepts represent different levels of safety to illustrate the impact of safety considerations on the design and performance.

6.1. Concept of operation and context

The case study targets a safety-critical application with a demanding operation performance (payload and range) to emphasize the challenge of performing conceptual design sizing while also considering safety and reliability.

The transportation of organs for transplant by drones within large cities is the selected case study. As illustrated in Fig. 4, transporting organs involves a significant payload of up to 20 kg, including an organ in an icebox (15 kg) and the fuselage around it

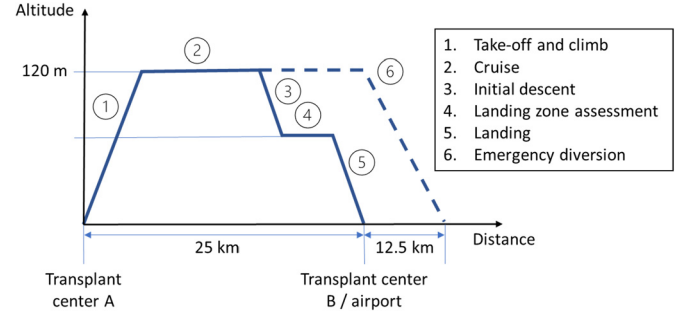


Fig. 4. Profile of the case study mission.

(5 kg), over a considerable distance of 25 km. An emergency diversion site is assumed to exist midway along the route. The descent and landing phases are estimated to take 30 seconds. In addition, flying BVLOS over densely populated areas involves major safety and reliability concerns. This type of safety-critical application represents a promising use for drone technology, which could reduce the time and cost associated with an essential health service and thus make it more accessible.

6.2. Regulatory framework analysis

The safety and reliability requirements are based on an analysis of the unmanned aerial system (UAS) regulations. The European Union Aviation Safety Agency (EASA) UAS regulatory framework is considered to provide certification specific to UASs owing to its comprehensive approach. We consider Regulation (EU) 2019/947 [57] and Regulation (EU) 2019/945 [58] and the proposed means for compliance with the Special Condition "Light-UAS.2510-Equipment, Systems, and Installation (High Risk)" [59], which define the applicable safety requirements for the operation, design, and manufacturing of UASs. These regulations detail the high-level safety objectives established in EASA basic regulation (EU) 2018/1139 [60].

Determining the safety objectives is based upon the following key characteristics of the case study's concept of operation: BVLOS operation of a light multirotor UAV over a densely populated urban area or over assemblies of people as per the EASA definition; a class D airspace; no passenger transport but cargo containing a human organ; and an altitude equal to or less than 120 m. These characteristics generate the following safety and reliability requirements:

- 1) The equipment and systems, including lift-thrust units and their command, must be designed such that a catastrophic failure condition does not result from a single failure.
- 2) The design must ensure compliance with the relationship between failure conditions and probabilities as provided in Table 3.
- 3) The failure to respect the following UAV design constraints would lead to more stringent allowable probabilities than provided in Table 3: the maximum dimension shall be below 3 m, and MTOM shall be below 200 kg (corresponding to a 400 m² worst crash area).

6.3. Concept definition

The case study focuses on a underactuated multirotor UAV with idealized configurations and identical, evenly distributed, coplanar, and perfectly aligned rotors for simplicity.

The concepts shown in Fig. 5 represent different fault tolerance levels to illustrate the impact of reliability considerations on the conceptual design. For design consistency, three generic

Table 3

Reliability requirements - Relationship between the classification of failure conditions and their probabilities of occurrence.

Classification of failure condition	Allowable qualitative probability	Allowable quantitative probability (average probability per flight hour)
No safety effect	None	None
Minor	Probable	$< 1.10^{-2}$
Major	Remote	$< 1.10^{-3}$
Hazardous	Extremely remote	$< 1.10^{-5}$
Catastrophic	Extremely improbable	$< 1.10^{-7}$

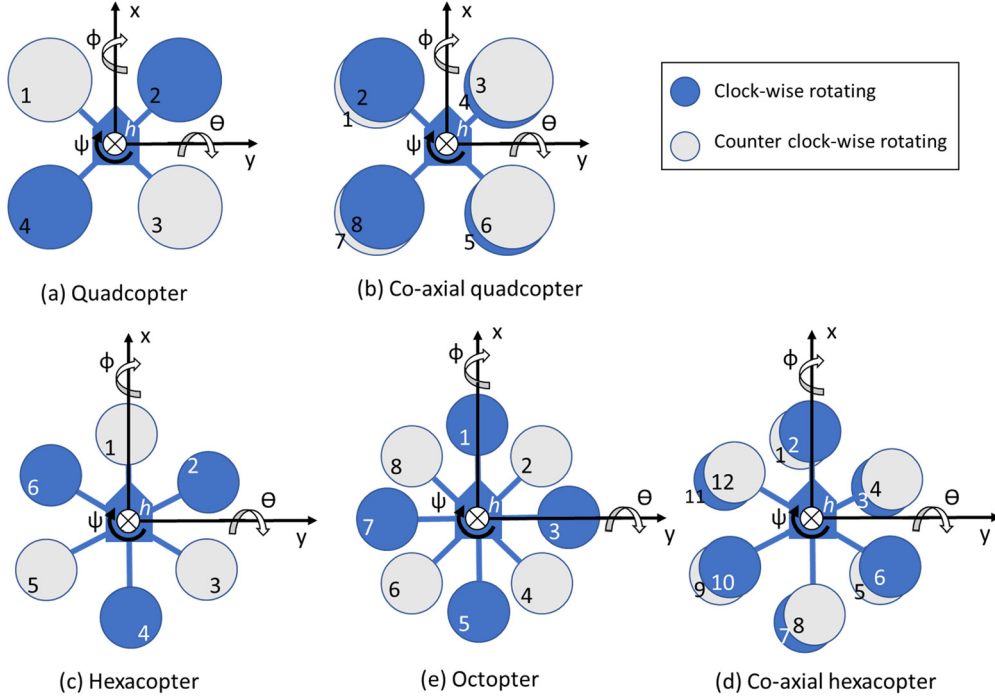


Fig. 5. Case study UAV configuration concepts. (For interpretation of the colors in the figure(s), the reader is referred to the web version of this article.)

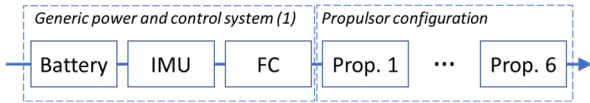


Fig. 6. Hexacopter reliability block diagram (fault-intolerant architecture).

power and control subsystem architectures were established and matched to the propulsor configurations based on the fault tolerance level. The hexacopter RBD in Fig. 6 illustrates the generic fault-intolerant power and control system architecture, which does not incorporate redundancy. The coaxial quadcopter RBD in Fig. 7 illustrates the single fault-tolerant architecture, which incorporates battery redundancy and majority voting based on three pairs of IMUs and flight controllers to survive single failures. The coaxial hexacopter RBD in Fig. 8 illustrates the double fault-tolerant architecture, which incorporates triple battery redundancy and majority voting based on four pairs of IMUs and flight controllers to survive double failures.

6.4. Control analysis results

The controllability analysis (cf. Section 3.1) indicates that the quadcopter and hexacopter configurations cannot maintain control of all the control axes after any single failure. As shown in Table 4, the coaxial quadcopter can ensure control of all the control axes for any single failure but loses control for some double failure cases. The coaxial hexacopter and octocopter can maintain control

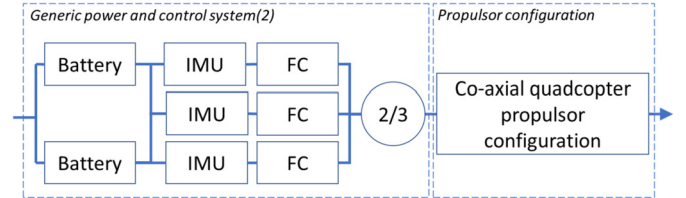


Fig. 7. Coaxial quadcopter propulsion system reliability block diagram (single fault-tolerant architecture).

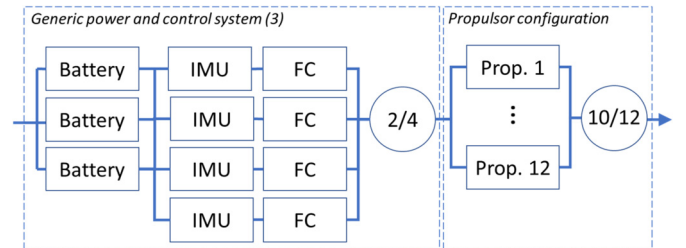


Fig. 8. Coaxial hexacopter propulsion system reliability block diagram (double fault-tolerant architecture).

of all the control axes after all single and double failures. The controllability analysis does not extend to triple failures (i.e., $k = 2$) because the probability of combining more than two failures is too remote for sound design consideration.

Table 4

Results of the controllability assessment of the coaxial quadcopter.

	Controllable cases	Uncontrollable cases
Single rotor failures	R1, R2, R3, R4, R5, R6, R7, R8 ($C_1 = 8$)	None
Double rotor failures	R1&R4, R1&R5, R1&R6, R1&R8, R2&R3, R2&R5, R2&R6, R2&R7, R3&R5, R3&R7, R3&R8, R4&R6, R4&R7, R4&R8, R5&R7, R6&R8 ($C_2 = 16$)	R1&R2, R1&R3, R1&R7, R2&R4, R2&R8, R3&R4, R3&R6, R4&R5, R5&R6, R5&R8, R6&R7, R7&R8

Note: R_i represents the failure of the i -th rotor; $R_i \& R_l$ represent the simultaneous failures of the i -th and l -th rotors.

Table 5Failure case sizing factors K_{max} obtained for the fault-tolerant configurations.

Configuration	K_{max}
Coaxial quadcopter	200%
Coaxial hexacopter	186%
Octocopter	283%

Table 6

Baseline mission specifications.

Parameters	Values
Payload [kg]	20
Max. thrust-to-weight ratio k_{thrust} [-]	1.6*
Climb height [m]	122
Climb speed [m/s]	3.0
Cruise distance [m]	25,000
Descent and hover duration [min]	0.5
Emergency diversion [m]	12,500 (cruise distance / 2)

* Similar to the DJI Agras T20 max thrust-weight ratio of 1.7 [61].

Table 5 presents the maximum failure sizing factors obtained for the fault-tolerant configurations as per Section 3.2, which are all driven by double failure cases. Here, the scaling factors are reduced to single scalars applicable to all the rotors owing to the symmetry of the idealized case study designs.

In some octocopter double failures, the control allocation strategy automatically disables a third rotor to avoid negative control allocation, as per Section 3.2, thereby explaining the compelling failure sizing factor of the octocopter's double failures. Further work on implementing a more advanced control allocation method should evaluate whether this impact can be reduced.

6.5. Design exploration

The design exploration studies the different fault-tolerant configurations presented in Section 6.4. The coaxial quadcopter, coaxial hexacopter, and simple octocopter concepts are optimized for the baseline mission described in Section 6.1. Emphasis is placed on evaluating the effect of the failure cases on the sizing. The baseline mission specifications are summarized in Table 6. The objective of the optimization problem is to minimize the MTOM.

The design exploration focuses on the variation in the components' characteristics as a function of mission requirements to understand how the specifications affect the design. For this purpose, we investigate the variations of the MTOM as a function of the specified range and payload, with all the other mission specifications remaining constant. Technological innovations such as new battery technologies provide an opportunity to further improve UAV performance. For this reason, it is pertinent to study the impact of a variation in the battery energy density and specific power on the UAV performance. For this purpose, three different cell types are used as references for the scaling laws of the battery estimation model as summarized in Table 7.

6.6. Sizing results

6.6.1. Concept comparison for the baseline mission

The mass breakdowns obtained for the coaxial quadcopter, coaxial hexacopter, and simple octocopter concepts are presented in Fig. 9. A high-power, high-energy li-ion battery is used for the comparison (i.e., Battery 1 in Table 7).

No feasible solution was found for the octocopter with the baseline mission. A downgraded mission with an emergency rerouting of 2.5 km instead of 12.5 km was applied to this concept for comparison. Still, the octocopter design did not converge with failure case sizing. Remarkably, the octocopter sized without failure case considerations is much heavier than its competitors.

The coaxial quadcopter and coaxial hexacopter exhibit comparable weights; the main difference lies in the structural mass supporting the rotors. The consideration of failure cases in the sizing mainly induced an increase in the motor mass, such as a 73% increase for the coaxial hexacopter. The other components were barely impacted.

Based on these results and the controllability analysis presented in Section 6.4, the coaxial hexacopter appears to be the most appropriate concept for the safety-critical application. Consequently, the following sensitivity studies focus on the coaxial hexacopter.

6.6.2. Effect of payload requirement

As shown in Fig. 10, the UAV mass increases exponentially with the payload. An increase in the payload mass implies more propulsive power and more energy being required to complete a mission, thus, resulting in an exponential increase in the total weight. In this regard, the battery cell type has a significant impact on the performance. A higher energy density reduces the battery weight for the benefit of the payload. However, this gain is constrained by the electrical power that the selected battery can provide, which explains why the potential of the ultra-high-energy battery (Battery 3 in Table 7) is limited despite a higher energy density. Indeed, this cell type has low specific power.

6.6.3. Effect of range requirement

Fig. 11 shows the evolution of takeoff weight as a function of range. The weight of the battery and subsequently the mass of the other components increases as more energy is required to increase the achievable range. Consequently, a higher energy density for the batteries has a positive impact on performance. Remarkably, a higher threshold (~ 45 kg) constrains the optimal mass of the UAV in the case of the ultra-high-energy, low-power battery (Battery 3 in Table 7). Thus, a decrease in the range requirement below 20 km does not allow further mass reduction. The critical constraint is no longer the quantity of energy required to conduct the mission but rather the power required for take off. The low specific power of the ultra-high-energy battery reaches its limits here. A similar trend can be observed for the other cell types but at a much lower threshold value (below 5 km).

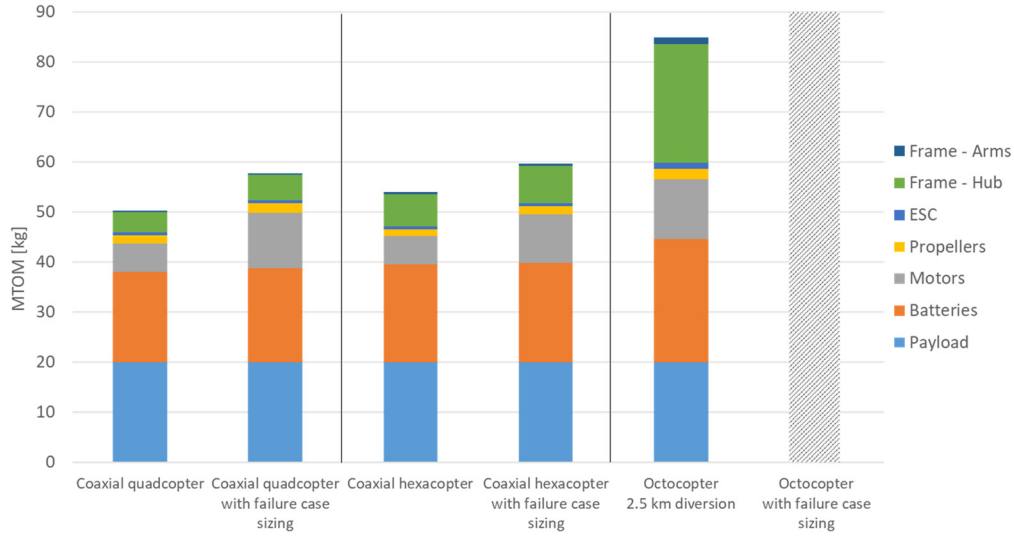
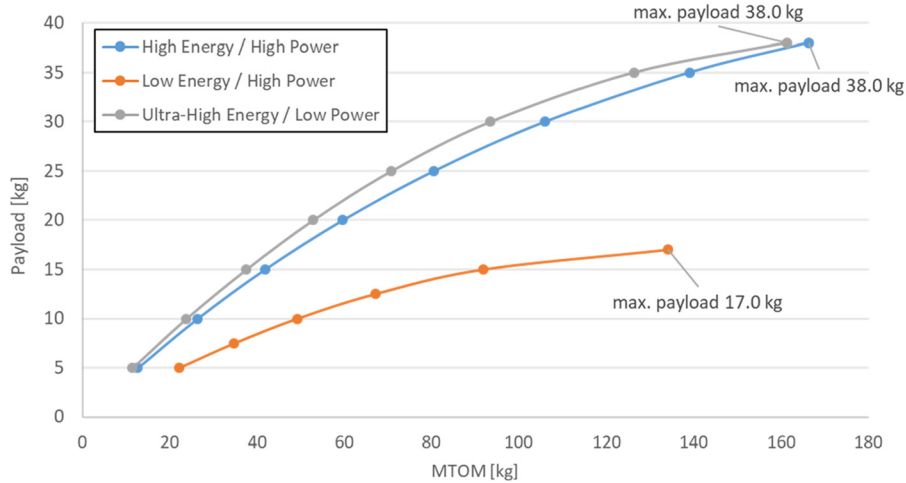
6.7. Reliability analysis results

The reliability of the concepts shown in Fig. 5 is modeled with RBDs. Fig. 6 illustrates the RBD of the hexacopter. The simple quad-

Table 7

Reference batteries for scaling laws.

	Battery 1 [62]	Battery 2 [63]	Battery 3 [64]
Battery chemistry	Lithium-ion NCA	Lithium-ion Polymer	Lithium-ion NMC
Cell type	High Energy/High Power Molicel INR-21700-P42A	Low Energy/High Power ProLite X TP3400-4SPX25	Ultra-High Energy/Low Power Kokam SLPB080085270
Energy density [Wh/kg]	224	155	249
Specific power [kW/kg]	2.4	3.9	0.5
Nominal voltage [V]	43.2	14.8	3.7
Capacity [Ah]	42.0	3.4	26.0
Max current [A]	450	170	104
Weight [kg]	8.100	0.326	0.387

**Fig. 9.** Mass breakdown results from the preliminary design.**Fig. 10.** Payload effect on maximum takeoff mass for three different battery cell types and a fixed range.

copter's RBD, which is not shown, differs from the hexacopter's RBD only in the number of propulsors. Fig. 7 shows the RBD of the coaxial quadcopter, and Fig. 8 illustrates the RBD of the coaxial hexacopter. The simple octocopter's RBD, which is not shown, differs from the latter only in the number of propulsors.

The reliabilities are summarized in Table 8. For clarity, the probability of failure $F(t)$ rather than the reliability $R(t)$ is shown. The probabilities of failure and reliabilities are complementary, $R(t) = 1 - F(t)$. The results in Table 8 show that the simple quadcopter and hexacopter concepts fail to satisfy the reliability requirements defined in Section 6.2; specifically, a catastrophic failure condition must not result from a single failure and must be extremely im-

probable (i.e., probability of occurrence less than 10^{-7} per flight hour). The coaxial quadcopter is fault tolerant and thus complies with the single failure requirement, but, in the best case scenario, it only marginally passes the probability of occurrence requirement. Given the approximations of the reliability analysis in the conceptual phase, its marginality makes this solution a high risk in terms of development. The simple octocopter and the coaxial hexacopter are double fault tolerant and have promising reliabilities, but they require high-caliber equipment to achieve high reliability levels.

Table 8 also shows that increasing the number of propulsors and hence the redundancy tends to increase the fault tolerance

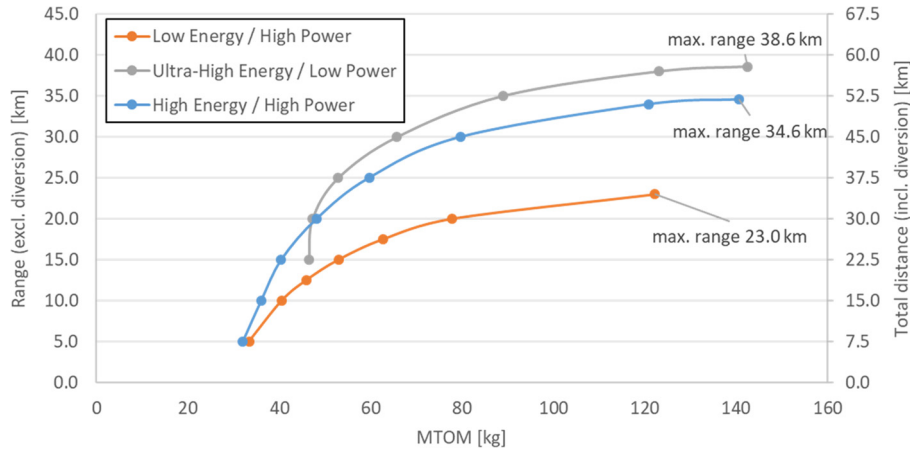


Fig. 11. Range effect on maximum takeoff mass for three different battery cell types.

Table 8

Safety and reliability assessment results.

Characteristics/concepts	Simple quadcopter (4 rotors)	Simple hexacopter (6 rotors)	Coaxial quadcopter (8 rotors)	Simple Octocopter (8 rotors)	Coaxial hexacopter (12 rotors)
Fault tolerance*	0 failures	0 failures	1 failure	2 failures	2 failures
Flight time (min)	19.9	17.7	22.3	14.2**	21.7
Failure rate derating	Probability of failure per flight hour				
x1 (transport aircraft)	$1.14 \cdot 10^{-4}$	$1.44 \cdot 10^{-4}$	$4.14 \cdot 10^{-9}$	$4.36 \cdot 10^{-14}$	$1.75 \cdot 10^{-13}$
x10	$1.14 \cdot 10^{-3}$	$1.44 \cdot 10^{-3}$	$4.14 \cdot 10^{-7}$	$4.40 \cdot 10^{-11}$	$1.75 \cdot 10^{-10}$
x100	$1.14 \cdot 10^{-2}$	$1.44 \cdot 10^{-2}$	$4.13 \cdot 10^{-5}$	$4.38 \cdot 10^{-8}$	$1.74 \cdot 10^{-7}$
x1,000 (toy industry)	$1.12 \cdot 10^{-1}$	$1.41 \cdot 10^{-1}$	$4.02 \cdot 10^{-3}$	$4.28 \cdot 10^{-5}$	$1.68 \cdot 10^{-4}$

Note: The designs that are potentially compliant with the safety and reliability requirements are highlighted in green.

* Fault tolerance of 0 means that certain single failures can have a catastrophic effect; fault tolerance of 1 means that no single failure can have a catastrophic effect, but certain double failures can; and fault tolerance of 2 means that no double failure can have a catastrophic effect.

** No failure case sizing (i.e., K_{max} is a unity vector) and a mission including a 2.5 km diversion instead of 12.5 km.

and reliability. However, adding more propulsors also decreases the reliability by increasing the part count (more parts means potentially more faults). For example, the simple hexacopter has more propulsors than the quadcopter but lower reliability because the additional propulsors do not provide fault tolerance and add to the total part count. In the same way, the simple octocopter has fewer propulsors but is more reliable than the coaxial hexacopter because both concepts are limited to double fault tolerance by design choice, but the simple octocopter has a lower part count.

6.8. Intermediate conclusion of the case study

The analysis of the EASA regulations has shown that the UAV must satisfy demanding reliability and safety requirements. The reliability analysis has shown that among the considered concepts, only the single octocopter, coaxial hexacopter, and coaxial quadcopter can satisfy these requirements. Still, these designs require high-caliber equipment equivalent to transport aircraft category products, and the significant oversizing factors from the failure cases impact the MTOM. The octocopter sizing does not converge for the baseline mission and requires the alleviation of the diversion requirement and no sizing for failure. All the other concepts are within the MTOM limits defined by the regulations for light UAVs, but they cannot carry a payload heavier than 38 kg for 25 km. Alternatively, in the most optimistic case, it is possible to reach a range of 39 km with a payload of 20 kg. In addition to the configuration, the type of battery cell appears to be a critical design decision impacting UAV performance. The coaxial hexacopter with ultra-high-energy low-power battery cells appears to be the best compromise with regard to mass and reliability. Future work should investigate the integration of battery cell specifications in

terms of specific power and energy density in the sizing optimization and eventually consider combining different battery cell types to achieve higher performance.

7. Conclusion

This paper introduces a new design methodology for the conceptual design of multirotor UAVs. The novel contributions lie in including safety and reliability considerations and enabling the exploration of an effective design. The current state of the art does not provide conceptual design methodologies that integrate reliability considerations for multirotor UAVs. The proposed methodology addresses this gap by developing a systematic reliability calculation and introducing sizing based on failure cases. For this purpose, controllability and reliability analysis methods are developed and linked to an analytical sizing methodology. The controllability analysis is based on the ACAI adapted for failure case assessment and reliability analysis. The controllability analysis and the sizing methodology are linked by introducing failure case sizing factors. The sizing relies on a modern analytical database-free methodology with MDO for design customization and computational efficiency. This methodology is advanced with new design models to cover failure cases in forward flights. A case study, which focused on medical transport in an urban environment, demonstrated the methodology's effectiveness. The case study first analyzed new UAV standards and regulations to establish a framework for certification and define the safety and reliability requirements. This first step also provides a relevant example of how to apply such new regulations to safety-critical urban applications. The methodology then efficiently evaluated and compared five concepts and

clearly indicated that only two comply with both the safety and reliability requirements and the mission specifications (payload and range). More specifically, the methodology showed the major impact of reliability considerations on the case study designs, with sizing factors ranging from 186% to 283% for the required rotor thrusts depending on the design concept. The methodology also provided valuable insights into the effect of critical design decisions, such as mission specifications and the choice of battery cell types. Hence, the new design methodology provides a novel means to effectively evaluate and explore underactuated multirotor design alternatives and also supports optimal decision making within the conceptual design.

Future work needs to address the current limitations of the proposed methodology. The controllability analysis focuses on the control authority remaining in a stabilized flight phase, such as forward flight. The analysis should be extended to include inertial effects in the oversizing factors to address flight phase transitions. Future work should also focus on integrating the propulsor configuration and control system reliability calculation to allow a systematic concept definition and design exploration. Finally, we profiled the methodology for underactuated multirotor concepts. Other concepts, such as fully actuated multirotor, fixed-wing, and hybrid multirotor fixed-wing concepts, are expected to be more adaptable for certain applications such as long-range missions. Therefore, new dynamics and design models should be developed to further adapt and advance the proposed methodology for these other concepts. In this way, UAV designers will have an effective way of evaluating and comparing a large variety of designs to select the optimal solution for reliability and energy efficiency in the conceptual design phase. Thus, the proposed methodology will contribute to the emergence of UAVs for challenging safety-critical applications.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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