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## Boundary Condition Effect on the Evaluation of Stress Triaxiality Fields

- Andrija Zaplatić<sup>a,b</sup>, Ana Vrgoč<sup>a,b</sup>, Zvonimir Tomičević<sup>a,\*</sup>, François Hild<sup>b</sup>
- <sup>4</sup> <sup>a</sup>University of Zagreb, Faculty of Mechanical Engineering and Naval Architecture 5 10002 Zagreb, Croatia
- <sup>b</sup>Université Paris-Saclay, CentraleSupélec, ENS Paris-Saclay, CNRS
- 7 LMPS Laboratoire de Mécanique Paris-Saclay, 91190 Gif-sur-Yvette, France

#### 8 Abstract

- 9 A general framework is presented for evaluating stress triaxiality fields using five
- different configurations of Dirichlet boundary conditions. The latter ones were
- measured via stereocorrelation for a simple shear test on a thin sample where
- buckling was mitigated with an anti-buckling fixture. Friction and material pa-
- rameters displayed negligible influence on the stress triaxiality fields. Accounting
- for the anti-buckling fixtures provided the most realistic stress triaxiality fields,
- but was computationally demanding. Prescribing all out-of-plane displacements,
- noisier but trustworthy stress triaxiality fields were also obtained by using much
- 17 less computational resources.
- 18 Keywords: Buckling, Dirichlet boundary conditions, inverse problem, simple
- 19 shear, stereocorrelation

#### 20 1. Introduction

- Thin sheets subjected to metal forming experience elastic springback after
- 22 their deformation stages. Therefore, it is important to accurately predict reversible

<sup>\*</sup>Corresponding author

deformations. Nowadays, the validity of forming processes is often controlled via

2 Finite Element (FE) analyses that depend on how trustworthy material properties

are. Furthermore, product optimization procedures are also governed numerically

4 via FE approaches, thereby improving product design and subsequent manufac-

turing stages to reduce material waste [1]. Experimental investigations need to be

6 carried out to determine the material response under simple or complex loading

regimes. For metal forming, shear is an especially important stress state [2, 3, 4].

8 However, pure shear stress states cannot be easily achieved experimentally for

sheets. As a result, mechanical tests considering simple shear are carried out on

thin sheets instead.

Material characterization during mechanical tests where complex loading regimes are employed call for advanced measurement methods. The development of digital imaging provided an opportunity for the emergence of full-field measurement techniques. Digital Image Correlation (DIC) [5, 6, 7, 8, 9, 10] stands out as the most widely employed full-field measurement method due to its versatility and straightforward use. Moreover, the development of global DIC [11, 12, 13, 14] formulated within an FE framework resulted in simple and seamless couplings between experiments and FE simulations. Robust identification methods were designed to utilize this opportunity for the calibration of material parameters.

The resulting output of global DIC is nodal displacements from which strains are calculated. Although displacement and strain fields are readily available with DIC, stress fields cannot be directly measured. The stress fields may be used to evaluate stress triaxiality fields (written as the ratio between hydrostatic and von Mises equivalent stresses). Stress triaxiality plays an important role in damage and

fracture mechanics for predicting the type of failure (i.e., ductile or brittle [15, 16,

2 17, 18, 19]). Combinations of DIC and X-ray diffraction (XRD) techniques may

be used to measure both total and elastic strain fields [20, 21, 22, 23, 23]. The

4 drawback is the required and expensive equipment, as well as the fact that the

number of measurement points for XRD is generally limited, and as such, this

method is not suited for industrial purposes.

The focus may then shift to analytical and numerical routes instead of experimental investigations to evaluate stress fields. In recent years, several approaches were proposed to assess stress and stress triaxiality fields from DIC measurements. Réthoré [24] developed the so-called Mechanical Image Correlation (MIC) 10 method for evaluating stress fields without assuming any constitutive law. A similar approach where no constitutive laws were defined was used by Dalémat et al. [25] where DIC was coupled with a Data Driven Identification algorithm (DDI) for evaluating stress fields. Musiał et al. [26] presented an original proposition for 14 evaluating stress fields from DIC data for uniaxial and simple shear tests by considering the measured displacement field gradient and a  $J_2$ -plasticity model. The DIC based stress fields gave more accurate results with respect to FE analyses since they accounted for all inaccuracies during experiments. Andrade et al. [27] 18 proposed a method to estimate the stress triaxiality fields from DIC strain fields for Von Mises' and Hill's models. Furthermore, Brosius et al. [28] developed a similar semi-analytical approach where the stress fields were determined from 21 DIC data. Lindner et al. [29] used Integrated DIC to evaluate stress triaxiality fields of a notched titanium alloy sample. It was concluded that even for thin samples, 3D meshes were required to analyze stress triaxiality fields. A similar 3D FE approach was used herein.

Abushawashi et al. [30] developed a novel method for constitutive modeling in plane strain conditions. Using DIC data, the authors determined equivalent stress and strain fields to run numerical simulations. From the numerical results, the stress triaxiality fields were evaluated since they display great influence on metal ductility [31, 32, 33]. Brünig et al. [34] also combined DIC data with numerical simulations to analyze a biaxial experiment on an H-specimen [35, 36, 37] covering a wide range of stress triaxialities and Lode parameters. Huang et al. [38] combined DIC results with computations to evaluate plastic strain and failure of Ti-6Al-4V alloys for specimens with different initial stress triaxialities. Wang et al. [39] coupled DIC data with FE runs to study Split Hopkinson Pressure Bar 10 experiments. It was shown that the failure strain decreased with increasing stress triaxiality or strain rate. Peng et al. [40] coupled DIC with FE analyses to charac-12 terize the stress state of flat metal specimen with inclined notches to analyze the influence of stress triaxiality and Lode angle on failure modes. Pham et al. [41] 14 developed a four-node quadrilateral plate element to analyze flexural and buckling responses of a functionally graded plate under different boundary conditions. 16

Advanced FE-DIC enables for straightforward couplings of measured data with numerical simulations in inverse problems aiming for material parameter calibration [42, 43, 44]. Finite Element Model Updating (FEMU) [45, 46, 47, 48] stands out as the most widely used algorithm for such purposes. With FEMU, the calculated displacement fields and resultant forces are compared to the measured quantities to determine the sensitivity matrices, *i.e.*, how the change in parameters affects them [49, 50, 51]. FEMU was employed for simple (*e.g.*, uniaxial [52]) and more complex (*e.g.*, biaxial [53]) mechanical tests. For identification purposes, the measured displacements were prescribed as Dirichlet boundary conditions on

the FE model. For thin samples, where plane stress states are expected, 2D DIC

measurements may be sufficient. However, this approach may be limited when

3D effects cannot be neglected. Réthoré et al. [54] proposed a framework where

4 the 3D displacement fields measured with stereocorrelation were used in an inte-

grated procedure. Wang et al. [55] also coupled measured 3D displacements with

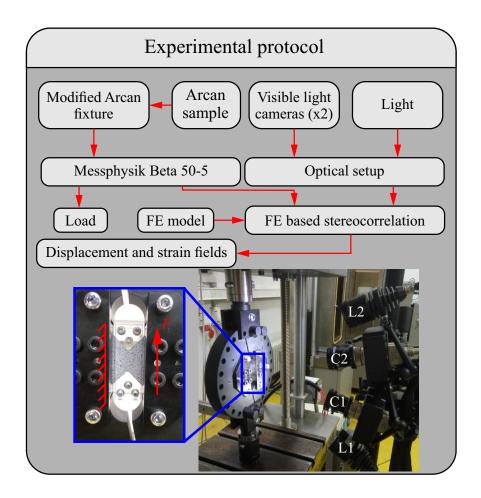
6 FEMU to describe plastic anisotropy in the so-called Erichsen bulge test.

From the reviewed literature, it is concluded that very few studies combined DIC and FE simulations to assess stress triaxiality fields [56, 36, 57, 58]. One key question when coupling experimental and numerical tools is related to boundary conditions. Driving numerical simulations using DIC data for assessing stress 10 triaxiality fields is the goal of this work. To be consistent with the experiment, measured displacements are utilized to drive FE analyses. For that purpose, a 12 monotonic simple shear test was carried out with a Modified Arcan Fixture (MAF) on a 1 mm butterfly shaped specimen, which promoted uniform stress states in the 14 gauge area, made of C60 steel. To measure the surface kinematics, a stereovision setup was used to capture both in-plane and out-of-plane components. Since 16 thin samples subjected to simple shear loading are susceptible to buckling [59], 17 additional supports made of transparent Poly methyl methacrylate (PMMA) were 18 utilized to prevent sample buckling [60, 61, 59, 62]. The experimental setup analyzed herein was developed by Zaplatić et al. [63] where thin butterfly samples were subjected to simple shear. The friction coefficient between the PMMA plates 21 and the sample was calibrated numerically via FEMU. To study the effect of prescribed boundary conditions, five test cases were defined, which differed in the definition of the applied kinematics. For each test case, FEMU was carried out to determine the influence of boundary conditions on the calibrated material pa-

- rameters. In-depth analyses of the corresponding stress triaxiality fields were con-
- <sup>2</sup> ducted for each test case. Such experimental and numerical framework provides a
- unique approach for analyzing the influence of the prescribed Dirichlet boundary
- 4 conditions on stress triaxiality fields since the FE simulations were directly driven
- 5 by experimentally measured DIC data.

#### 6 2. Experimental protocol

- In this section, the entire experimental protocol involving the Modified Arcan
- 8 Fixture and stereovision system are presented. The stereocorrelation results are
- 9 then analyzed and discussed.
- The experiment presented herein was aimed at preventing buckling of thin sheet samples under simple shear loading. The mechanical test was carried out on 11 a Modified Arcan Fixture (Figure 1), which enables for three loading regimes, namely, shear, tensile and combinations thereof. The MAF employs butterfly 13 shaped samples with two V notches in the middle of the gauge section to pro-14 mote uniform strain distributions. The expected triaxiality levels in the gauge area (i.e., between the V notches) for the aforementioned loading regimes are 0, 16 0.33 and 0.66, respectively [63]. The 1-mm thick butterfly sample made of high carbon C60 steel was subjected to simple shear (Figure 1). The experiment was 18 performed on a uniaxial testing machine Messphysik Beta 50-5 in displacement control mode with a stroke rate of 1 mm/min. The standard force uncertainty  $\gamma_F$ of the load cell was equal to 10 N.



**Fig. 1:** Experimental workflow with the experimental and optical setup consisting of two vertically positioned visible light cameras (C1 and C2) and two light sources (L1 and L2). On the extracted detail, the Region Of Interest (for stereocorrelation purposes) is depicted on the butterfly sample with the positioned PMMA plates.

- Since a thin sample was subjected to simple shear, buckling was expected to
- occur. In order to mitigate shear buckling, an anti-buckling fixture was designed,
- which was composed of two 10-mm thick (PMMA) plates. The use of PMMA for
- 4 the material of the anti-buckling fixture was due to its transparency thus allow-
- 5 ing optical measurement methods to be used. Similar setups were employed to
- 6 minimize buckling and wrinkling of sub-millimeter thick sheets [60, 61, 59]. The

- dimensions of the two PMMA plates (i.e.,  $70 \times 25$  mm) were defined with respect
- to the observable area of the butterfly sample (Figure 1). The plates around both
- lateral surfaces were connected with a total of six M5 bolts, which were not tight-
- 4 ened to reduce the influence of the anti-buckling fixture on the stress triaxiality
- 5 fields. The material response in the Region Of Interest (ROI) was captured with
- 6 the stereovision system detailed in Table 1. A total of 900 images was acquired by
- each camera, where the first ten image pairs corresponded to the unloaded state.

Table 1: Hardware parameters of the stereo-system

Cameras	Dalsa Falcon 4M60
Definition	$2358 \times 1728$ pixels (B/W images)
Color filter	none
Gray Levels rendering	8 bits
Lens	Titanar 50 mm
Aperture	f/2.8
Field of view	3,996 mm <sup>2</sup>
Image scale	pprox 32 pixel/mm
Stereo-angle	25°
Stand-off distance	31.6 cm
Image acquisition rate	1 fps
Patterning technique	B/W paints
Pattern feature size	15 px

- The displacement and strain fields of the ROI were measured via FE-based
- stereocorrelation [64, 65, 66]. The employed software (EikoTwin DIC) consid-

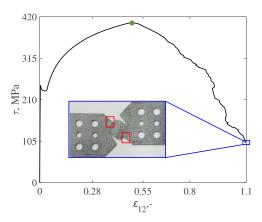
- ers a continuous description of the ROI discretized with triangular T3 finite ele-
- ments [67]. The aforementioned algorithm uses the known geometry of the sam-
- 3 ple and setup, as observed from the reference images, for calibration purposes.
- 4 Following the calibration step, shape corrections of the chosen ROI were per-
- 5 formed by running a second series of spatial registrations in which out-of-plane
- 6 corrections were allowed [65]. The stereocorrelation analysis parameters are re-
- ported in Table 2. The listed noise floor estimates were determined by calculating
- 8 the mean temporal standard deviations of each nodal displacement and element
- strains from the registration of the ten reference image pairs.

Table 2: Stereocorrelation analysis parameters

DIC software	EikoTwin DIC				
Image filtering	none				
Element length	1 mm				
Shape functions	linear (T3 elements)				
Mesh	see Figure 3				
Matching criterion	penalized sum of squared differences				
Regularization length	5 mm				
Displacement noise floor (x z y)	0.2 μm 0.1 μm 0.6 μm				
Strain $\varepsilon_{12}$ noise floor	$7 \times 10^{-5}$				

The global stress/strain response of the sample is shown in Figure 2. The engineering shear stress was calculated by dividing the measured force by the initial cross-sectional area  $S_0$  between the V notches (i.e.,  $21 \times 1$  mm). The strain levels were evaluated by averaging the measured strains within the virtual gauge located

- between the V notches of the DIC mesh (Figure 3(c)). The yield stress was ap-
- proximately equal to 248 MPa (for an offset strain of 0.4%). For the highest load
- level (i.e., 8.7 kN), the ultimate shear strength was equal to 417 MPa, and the cor-
- 4 responding shear strain 48.7%. From the deformed sample, two distinct symmet-
- 5 ric cracks were observed (Figure 2). The initial location of the cracks correlated
- 6 with tensile stress areas (i.e., with expected stress triaxiality of 0.33). Slight buck-
- 7 ling of the central region was also distinguished, especially where compressive
- 8 stress states were expected (depicted by green rectangles in Figure 2).



**Fig. 2:** Macroscopic shear stress/strain response. The green point indicates time step 340 (*i.e.*, strain level of 44%). The analyses reported herein were carried out up to this point. On the deformed sample, the locations of buckling onset are highlighted by red rectangles, which corresponded to areas subjected to compression.

The carried out experiment with the anti-buckling fixture mostly resulted in negligible to small out-of-plane displacements. In Figure 3, out-of-plane displacement, residual and strain fields are reported for time step 340 before damage inception (Figure 2). The measured out-of-plane displacement field revealed a heterogeneous distribution, which indicated a tendency toward buckling. The area

- of increased displacements denoted by the blue rectangle corresponds to zones
- where negative triaxialities were expected (i.e., approximately -0.33, which in-
- <sup>3</sup> dicates compressive stresses). The same area is not highlighted in the correlation
- 4 residual map (Figure 3(b)), thus proving the trustworthiness of the measurements.
- 5 Increased residuals were visible in the central part of the ROI (highlighted by
- 6 the green rectangle). Due to the tendency toward buckling, minor wrinkling of
- 7 the central part of the ROI occurred, which led to changes in brightness (i.e.,
- 8 shadows). The strain map (Figure 3(c)) revealed that a single shear strain band
- developed between the V notches where the expected triaxiality was 0.

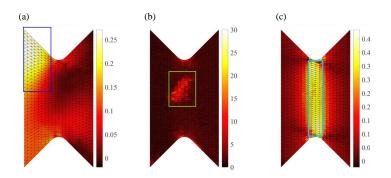


Fig. 3: (a) Out-of-plane Displacement (expressed in mm), (b) gray level residual (in % of the dynamic range of the reference images), and (c)  $\varepsilon_{12}$  strain fields for time step 340 (*i.e.*, before damage occurred). Positive displacements are oriented toward the reader. The blue box highlights localized increases in out-of-plane displacements where limited buckling initiated. The green box shows increased residuals where a slight change in brightness occurred. The cyan box depicts the location and size of the virtual strain gauge. Negligible out-of-plane displacements were measured and a uniform shear strain band developed.

#### 3. Numerical protocol

In this section, the entire numerical protocol is presented. First, the FE models of the sample and the PMMA plates is introduced. Second, the five analyzed test

- cases are defined. Last, the FEMU identification procedure is summarized. The
- numerical investigation presented herein dealt with the influence of the prescribed
- boundary conditions (BCs) on the predictions of the FE model, specifically the
- 4 stress triaxiality fields. To evaluate the latter ones, the material parameters were
- 5 calibrated via weighted Finite Element Model Updating (FEMU).
- In the present analyses, the numerical simulations were driven by *experimen*-
- 7 tally measured displacements prescribed as Dirichlet BCs. The goal was to ana-
- 8 lyze the influence of the BCs on the stress triaxiality fields. Yang et al. [68] in-
- 9 troduced bifurcation analyses in FE simulations to analyze wrinkling of the mod-
- ified Yoshida buckling test (YBT). Even though the numerical analyses closely
- followed the experiments, the BCs on the gripped part could not describe slip
- between the specimen and the grips in a straight forward manner. Using DIC
- measured data, there is no need to model the grips. Chen et al. [69] analyzed the
- influence of a disturbance force on buckling of YBT specimens. The simulation
- of thin sheet buckling was challenging, and imperfections had to be introduced
- in the numerical model. In the present study, the imperfections were included
- through the measured BCs. No geometrical imperfections were added [70]. All
- the reported simulations were performed with the implicit version of Abaqus [71],
- and no advanced tools (e.g., arc length method or explicit schemes) were needed.

#### 20 3.1. Test cases

- Five distinct test cases (Figure 4) were defined for which the influence of BCs
- was evaluated on the stress triaxiality fields and sample buckling modeling (Ta-
- ble 3). For each studied case, the FE model of the sample was discretized with
- 24 C3D8R elements.

**Table 3:** Test cases with their boundary conditions

Test case	Description
T1	Measured $U_x$ and $U_y$ displacements on stressed surfaces
	and $U_z$ displacements on the stressed edges of Surface 1 + PMMA plates ( $\mu=0.33$ ) (Figure 4(a) and (b) - R and Y)
T2	Measured $U_x$ and $U_y$ displacements on stressed surfaces
	and $\mathit{U}_z$ displacements on the stressed edges of Surface 1 + PMMA plates ( $\mu = 0.01$ )
Т3	Measured $U_x$ and $U_y$ displacements on stressed surfaces (Figure 4(b) - R)
T4	T3 and $U_z$ displacements on stressed edges (Figure 4(b) - R and Y)
T5	T3 and $U_z$ displacements on Surface 1 (Figure 4(b) - R, Y and B)

- In test case T1 (Figure 4(a)), the assembly of the butterfly sample and the
- 2 PMMA plates was modeled with defined interactions between the two parts. The
- 3 measured displacements were prescribed on the stressed surfaces of the sample
- 4 mesh as Dirichlet BCs. Out of plane (z) displacements were prescribed only along
- $_{5}$  the stressed edges of Surface 1 whose normal was along negative z. Conversely,
- $_{6}$  pure (i.e., 2D) DIC displacements x and y were extruded through the thickness
- of the mesh (i.e., along the z direction Figure 4(b) denoted in Red and Yellow
- 8 color).

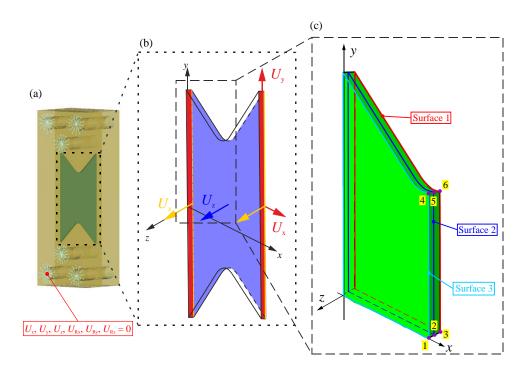


Fig. 4: (a) FE model with the PMMA plates. (b) Different sets of boundary conditions. Red (R) - in-plane displacements  $(U_x, U_y)$  on entire surfaces, yellow (Y) - out-of-plane displacements  $U_z$  on the edges and blue (B) - out-of-plane displacements  $U_z$  on the entire surface. (c) Detail of a quarter of the FE model where six points and three surfaces are defined, which are used for further analyses.

The second test case T2 was identical to T1 regarding the prescribed BCs and numerical model. However, the friction coefficient was set to  $\mu=0.01$  to probe the influence of negligible friction on the numerical model. For test case T3, only 2D displacements (*i.e.*, along x and y directions) were prescribed on the stressed surface (Figure 4(b) - denoted in Red color) as if they had been measured via 2D-DIC. This test case was not deemed eligible to simulate buckling as an idealized configuration was defined (*i.e.*, no imperfections in terms of out-of-plane displacements were introduced).

In test case T4, out-of-plane displacements were prescribed along the stressed edges of Surface 1, identical to T1 and T2, but the PMMA plates were not modeled (Figure 4(b) - denoted in Red and Yellow color). For the last test case (T5), the entire Surface 1 was further constrained with the measured out-of-plane-displacements (Figure 4(b) -denoted in Red, Yellow and Blue color). This choice was made due to the inaccurate description of buckling with case T4. To further probe the simulation validity regarding buckling, the out-of-plane displacements were prescribed on the entire surface. Each analysis performed herein was run for the first 340 time steps (*i.e.*, until the shear strain reached  $\varepsilon_{12} = 0.44$ , see Figure 2).

For the first two test cases, the interaction between the sample and the PMMA plates needed to be defined. General contact was introduced with Coulomb fric-12 tion [72], where two different friction coefficients were considered. The plates were discretized with C3D4 tetrahedra. In the mechanical test, they were con-14 nected with six bolts that were not tightened. The numerical model was simplified to avoid modeling bolt pretension. The bolts were replaced by a combination of 16 kinematic couplings and connector elements (CONN3D2, type = beam). Kine-17 matic couplings were used to replace bolt heads on the surfaces around the holes 18 (depicted by cyan lines in Figure 4(a)), whereas the connector elements repre-19 sented the bolt shank and thread. Connector elements were used to link the master nodes of the kinematic coupling, thereby ensuring stiff connections between the 21 plates. To prevent rigid body motions of the plates, for a single master node, all displacements and rotations were disabled (red dot in Figure 4(a)). For all other master nodes, only out-of-plane displacements were disabled. Elastic properties (i.e., 3 GPa Young's modulus and 0.3 Poisson's ratio) were assigned to the PMMA plates.

#### 2 3.2. Parameter calibration

The extraction of stress triaxiality fields depends on material parameters. FEMU was employed as the identification procedure. To describe the nonlinear behavior, Armstrong-Frederick's kinematic hardening model [73] was selected. The sought parameters were the yield stress  $\sigma_y$ , hardening modulus C, and nonlinear coefficient c. FEMU minimizes differences between experimentally measured and numerically calculated quantities. The minimization procedure iteratively updates the sought parameters by calculating Hessian matrices based on sensitivity fields [49, 74] (i.e., changes of each considered quantity for a small variation of

the parameters). In the present cases, the differences between measured and computed displacement fields, as well as measured load and global reaction forces extracted from the numerical model were considered.

If the minimization procedure were to take into account only measured displacement fields (i.e., FEMU-U), the cost function would be formulated as the sum of squared differences between measured  $\{\mathbf{u}_m\}$  and computed  $\{\mathbf{u}_c\}$  nodal displacements

$$\chi_u^2(\{\mathbf{p}\}) = \frac{1}{\gamma_u^2 N_u} \|\{\mathbf{u}_m\} - \{\mathbf{u}_c\}\|_2^2,$$
 (1)

where  $\{\mathbf{p}\}$  is the column vector gathering all sought material parameters,  $\gamma_u$  the standard displacement uncertainty, and  $N_u$  the number of kinematic degrees of freedom [74]. When the only source of error is due to the measurement uncertainty,  $\chi_u$  tends to 1. Therefore, any deviation from 1 implies model errors.

FEMU may also be utilized to minimize the differences between the measured forces  $\{\mathbf{F}_m\}$  and calculated reaction forces  $\{\mathbf{F}_c\}$  (*i.e.*, FEMU-F) extracted from

the stressed edges of the FE model where Dirichlet BCs were prescribed

$$\chi_F^2(\{\mathbf{p}\}) = \frac{1}{\gamma_F^2 N_F} \|\{\mathbf{F}_m\} - \{\mathbf{F}_c\}\|_2^2,$$
 (2)

- where  $\gamma_F$  is the standard uncertainty of the load cell, and  $N_F$  the number of load
- з data.
- The identification procedure can be enhanced by combining the aforemen-
- 5 tioned cost functions

$$\chi_{tot}^2 = (1 - \omega)\chi_u^2 + \omega\chi_F^2,\tag{3}$$

- $_{6}$  where the factor  $\omega$  weighs the contribution of each individual cost function. In
- 7 this work,  $\omega$  was set to 0.5 to give equal weight to both cost functions.

#### 8 4. Numerical results

- In this section, the numerical results for each test case are presented and compared. First, FEMU was carried out to determine the optimal set of material parameters for each individual test case. For the identification procedure and further numerical analyses, the triangular T3 mesh used for stereocorrelation measurements (Figure 3) was converted into four-noded quadrilateral (Q4) elements. The 2D Q4 mesh was then extruded to construct the 3D mesh composed of linear brick elements with reduced integration (C3D8R).
- 16 4.1. FEMU identification results
- The calibrated material parameters, their initial value and converged cost functions are gathered in Table 4. The parameters calibrated for test case T1 were used as initial guess for the other cases. For each test case, the elastic parameters (*i.e.*,

- Young's modulus E and Poisson's ratio  $\nu$ ) were kept constant and set to 210 GPa
- 2 and 0.25, respectively.

**Table 4:** FEMU results for all test cases. The calibrated parameters of case T1 were used as initial guess for all other test cases. Values of  $\chi_U$ ,  $\chi_F$  and  $\chi_{tot}$  are displayed for initial and converged solutions. The standard parameter uncertainties  $(\pm)$  are also indicated.

Parameter	$\sigma_y$ , MPa	C, MPa	с	$\chi_U$		$\chi_F$		$\chi_{tot}$	
				Initial	Converged	Initial	Converged	Initial	Converged
T1	$360 \pm 15$	$3860 \pm 640$	$12 \pm 1.7$	60	59.6	40.4	9.3	51.2	42.6
T2	$380 \pm 9$	$3920 \pm 460$	$11 \pm 1.7$	59.4	59.5	43.9	10.5	52.5	42.7
Т3	$380 \pm 9$	$3920 \pm 460$	$11 \pm 1.7$	34	33	44.4	10.4	32	24.5
T4	$380 \pm 10$	$3910 \pm 510$	$11 \pm 2$	69	71	47	10.5	59	51
T5	$380 \pm 13$	$3890 \pm 660$	$11 \pm 2.4$	7.8	7	45.8	10.7	32.9	9

- The calibration procedure yielded parameters that provided good agreement
- 4 between the measured load and the global reaction forces. Each calibration re-
- sulted in lowered global residual  $\chi_{tot}$ . For case T1, the calibrated yield stress  $\sigma_y$
- and hardening coefficient C were the lowest, except for the nonlinear coefficient c,
- which was the highest of all test cases. Furthermore, the converged global residual
- 8  $\chi_{tot}$  and the force residual  $\chi_F$  were lower compared to test cases T2 and T4.
- The second test case T2 experienced an increase in yield stress  $\sigma_y$  by 6% and
- hardening coefficient C by 1%, whereas c was reduced by 7%. The global residual
- at convergence was only slightly higher than for T1. The displacement residuals
- for the initial parameters and at convergence displayed slightly lower values than
- their T1 counterpart. However, for T1 the force residuals were lower. Since fric-
- tion was negligible, higher values of  $\sigma_y$  and C were calibrated to compensate for
- the additional force due to friction [63].
- The third test case T3, where only in-plane measurements were prescribed,

yielded the second lowest global residual. This result was due to the lack of prescribed out-of-plane displacements that were affected by higher measurement uncertainties (Table 2). Furthermore, with this approach, buckling of the sample was not possible to simulate since no imperfections were considered. This observation highlights the significance of enriching the FE model with measured out-of-plane displacements for buckling simulation. Although only in-plane measurements were prescribed, it was decided to include out-of-plane displacements in the calculation of  $\chi_{tot}$ , which was significantly lower than for test cases T1 and T2. This observation shows that prescribing only in-plane measurements was not sufficient to describe any out-of-plane motion. This test case cannot be considered representative of the real experiment since it was idealized. The identified values of the sought parameters were essentially the same as for test case T2 since no friction was included in the numerical model.

Even though the identification procedure converged, the global residual was 14 the highest of all proposed FE modeling strategies for test case T4. Both displacement and force residuals for the first iteration and at convergence were greater than 16 those for T1 and T2. Furthermore, the displacement residual experienced a slight 17 increase at convergence due to higher out-of-plane displacements (i.e., buckling, 18 which could not be accurately described). It was concluded that 3D measurements prescribed as Dirichlet BCs were sufficient to simulate buckling. However, due to the complexity of the material behavior, buckling for case T4 was not fully 21 controlled (i.e., restricted by the PMMA plates). The deviation of the calculated out-of-plane displacements from the measured counterparts resulted in increased displacement residual  $\chi_U$ . The initial and converged force residuals  $\chi_F$  also displayed higher values than the previous test cases, except for T2 where the same level was reached.

For the final test case T5, the measured out-of-plane displacements were prescribed over the entire Surface 1 to drive the numerical simulation toward limited buckling with Dirichlet BCs. The calculation of  $\chi_U$  considered only stereocorrelation measurements. The lowest  $\chi_{tot}$  was reached with this approach since out-ofplane displacements were accounted for and controlled. This last case resulted in approximately eight times lower displacement residuals than for T1. By constraining the entire Surface 1, buckling could be triggered with stereocorrelation data. The drawback of this approach is the introduction of additional measurement uncertainties in the prescribed out-of-plane displacements (Table 2). An additional 10 cost function regarding the reaction forces extracted from the constrained surface was defined in the FEMU algorithm. The goal was to minimize these reaction 12 forces to be as close as possible to zero. The identification procedure yielded the highest value of  $\sigma_y$  compared to all other test cases, which increased by approx-14 imately 7%, whereas C changed only slightly from its initial value (i.e., 0.7%). The nonlinear coefficient c experienced the highest relative change (ca. 8%). The standard uncertainty of the calibrated parameters was also calculated to 17 determine the influence of the prescribed Dirichlet BCs. For the yield stress  $\sigma_y$ , the highest uncertainty was reached for test cases T1 and T5, i.e., the more complex 19 cases. The parameter uncertainties for the other three cases were similar. For test cases T1 and T5, the highest uncertainty for C was also observed, whereas 21 for T2 and T3 they were similar. The highest uncertainty for c was obtained for case T5. From these results, it was concluded that the prescribed BCs had an influence on the calibrated material parameters. The most complex test cases T1 and T5 yielded the highest parameter uncertainties. For case T1, the cause was friction, whereas for T5 it was due to the prescribed out-of-plane displacement on

the entire measurement surface.

14

To illustrate the effect of friction, a unique set of material parameters was 3 selected (i.e., those of case T1, see Table 4) and computations were run with the five BCs. From each simulation, the reaction forces were extracted and are displayed in Figure 5(a). All test cases yielded lower reaction forces compared to T1. This trend was explained by the fact that all of them were frictionless (i.e., for case T2 friction was approximately zero and for the other three it was not modeled). The influence of friction cannot be deemed negligible, which is further supported by the calibrated material parameters (Table 2). For the last four test cases, friction was neglected, and the FEMU procedure yielded higher values for  $\sigma_y$  and C compared to T1 to compensate for the absence of friction. This effect 12 was especially apparent for the first two test cases T1 and T2 where the same numerical model was employed.

Cases T1 and T2 were very close in terms of numerical model. Their reaction 15 force differences were the lowest of all the reported differences (Figure 5(b)), 16 which was further substantiated by the lowest mean. The highest differences were 17 observed between cases T1 and T4. Overall, the root mean square differences were about 33 times the standard force uncertainty  $\gamma_F$ . These results highlight the consequence of not including friction in the identification procedure.

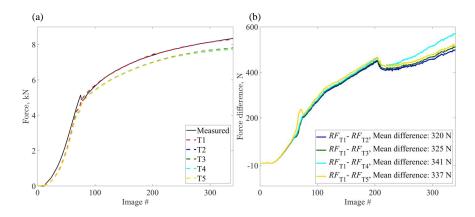
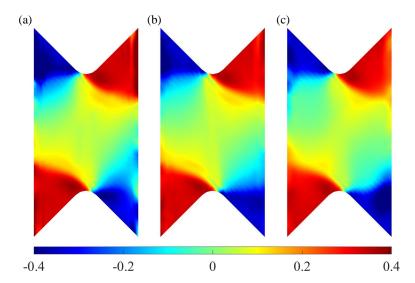


Fig. 5: (a) Comparison of global reaction forces extracted from the FE models for the material parameters calibrated for case T1. (b) Differences in global reaction forces with respect to T1. The mean reaction force differences were on average  $33\times$  higher than the standard force uncertainty  $\gamma_F$  (i.e.,  $\chi_F \approx 33$ ). These results show the consequence of not including friction in the identification procedure (i.e., lower reaction forces since the material parameters were not properly calibrated in the absence of friction).

#### 4.2. Stress triaxiality fields

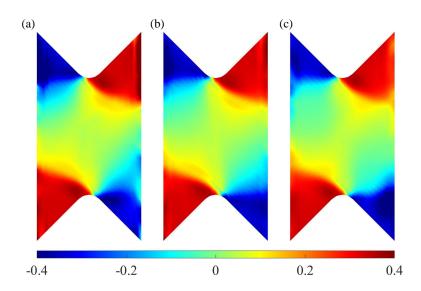
In the following, the influence of different BC prescriptions on stress triaxiality fields is studied, both surface-wise and node-wise (Figure 4(c)). Three surfaces were chosen to evaluate them, namely, the back Surface 1, middle Surface 2 and front Surface 3. Moreover, in total six nodes were chosen for the evaluation of the corresponding triaxialities. The three nodes in the middle (*i.e.*, nodes 1, 2 and 3) of the FE model were chosen to asses the stress state in the gauge area (*i.e.*, between the V notches) since the butterfly sample was designed to promote uniform stress states in the gauge region. The sample was subjected to simple shear, thus uniform shear stress states were expected (*i.e.*, the stress triaxiality should vanish). Furthermore, three points were chosen in the root of the V notch (*i.e.*, nodes 4, 5 and 6) to evaluate the stress state in that area. All test cases

- displayed similar distributions of stress triaxialities on the chosen sample planes
- <sup>2</sup> (Figures 6-10). The locations of the initiated cracks in the sample (see inset of
- Figure 2) coincided with the areas of positive stress triaxialities (i.e.,  $\approx 0.33$ )
- 4 where tensile stresses occurred.
- From the stress triaxiality fields shown in Figure 6 for test case T1, identical
- 6 distributions are observed on all three surfaces. The stress triaxiality fields were
- <sup>7</sup> generally divided into three main parts, namely, areas with positive (red) tensile,
- 8 negative (blue) compressive, and approximately zero (green) shear parts. Small
- 9 fluctuations in terms of increased stress triaxiality values occurred on the edges of
- the surfaces. This effect was attributed to the prescribed BCs, which introduced
- additional random fluctuations due to measurement uncertainties. Furthermore,
- no severe wrinkling was caused by sample buckling since it was prevented with
- 13 this numerical model.



**Fig. 6:** Stress triaxiality fields for time step 340 (test case T1), for the front surface (a), the midthickness surface (b) and back surface (c). Almost identical fields are observed for the three analyzed surfaces.

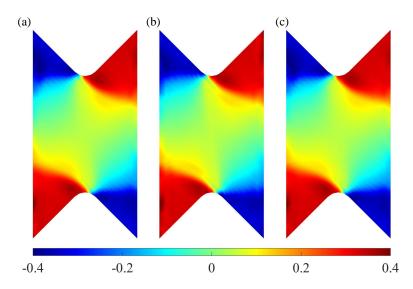
- Test case T2 (Figure 7) displayed identical triaxiality distributions as T1 since
- the numerical model was the same, except for the value of the friction coefficient.
- 3 As in the previous case, increased stress triaxiality levels were observed on the
- 4 boundaries of the FE model where Dirichlet BCs were prescribed. The stress
- 5 triaxiality in the middle of the gauge area was also close to zero. From the stress
- 6 triaxiality fields, it was concluded that the influence of friction remained very
- 7 limited.



**Fig. 7:** Stress triaxiality fields for time step 340 (test case T2), for the front surface (a), the midthickness surface (b) and back surface (c). Almost identical fields are observed for the three analyzed surfaces.

Test case T3 differed from other ones as it was the only configuration where no out-of-plane displacements were prescribed to the FE model. No buckling developed in the numerical simulations since they were idealized (*i.e.*, there were no imperfections in terms of out-of-plane displacement). All three surfaces displayed identical stress triaxiality distributions. The stress triaxiality levels in the middle of the gauge area were close to zero (*i.e.*, a shear stress state developed). Similar

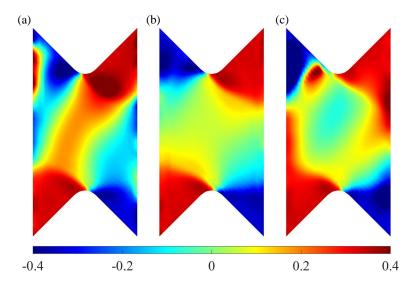
- distributions of stress triaxialities were observed compared to cases T1 and T2,
- 2 and the constrained edges of the FE model displayed lower fluctuations since no
- 3 out-of-plane displacements were prescribed.



**Fig. 8:** Stress triaxiality fields for time step 340 (test case T3), for the front surface (a), the midthickness surface (b) and back surface (c). Almost identical fields are observed for the three analyzed surfaces.

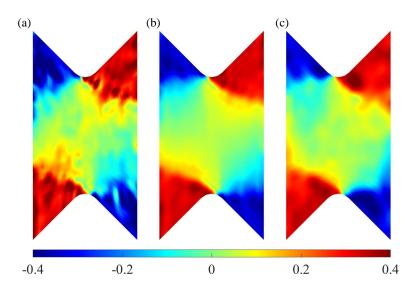
For test case T4, the fluctuations in the stress triaxiality fields on Surfaces 1 and 3 (Figure 9) were more marked. The middle Surface 2 was similar to the previous test cases and no significant fluctuations occurred. However, Surface 1 suffered from more important variations in the stress triaxiality field in the middle of the gauge section, where zero levels were expected. This effect was attributed to buckling, which was triggered by introducing out-of-plane displacements in the Dirichlet BCs. Even though buckling developed, it was not severe. Its influence on the stress triaxiality fields was not negligible since additional stresses were induced. From the stress triaxiality fields, the effect of limited buckling was seen. The gauge area on Surface 1 was subjected to tensile stresses, whereas the same

- area on Surface 3 was compressed. From this observation, it was concluded that
- <sup>2</sup> buckling was oriented away from the reader.



**Fig. 9:** Stress triaxiality fields for time step 340 (test case T4), for the front (a) and back (c) surfaces where the influence of buckling is more pronounced than for the mid-thickness surface (b).

- Since the entire Surface 1 was constrained by the prescribed out-of-plane dis-
- 4 placements, test case T5 was the most sensitive to measurement uncertainties.
- 5 Triaxiality fluctuations were observed on all three surfaces in Figure 10, and as
- 6 expected, Surface 1 was most affected. The stress triaxiality distribution on all
- 7 three surfaces was still close to the previous cases. For test case T4, where buck-
- 8 ling was also simulated, similar distributions of stress triaxialities in the gauge
- 9 region were distinguished. The stress triaxiality values for the red areas ranged
- from 0.3 to approximately 0.5, which was similar to the levels obtained for cases
- 11 T1 and T2. In the gauge area, they were higher than for T1. This trend was at-
- tributed to buckling inception since out-of-plane displacements were prescribed
- on Surface 1.



**Fig. 10:** Stress triaxiality fields for time step 340 (test case T5). For the front surface (a), the influence of the measurement uncertainties is more important than for the back surface (c); for the mid-thickness surface (b) it is minimal.

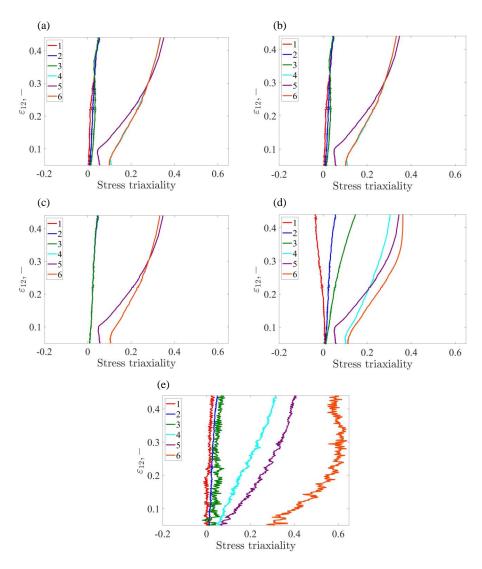
The stress triaxiality history for the six chosen nodes (Figure 4(c)) is plotted against the average shear strain calculated from the virtual gauge (Figure 3(c)) 2 and reported in Figure 11. From the analysis of the stress triaxiality fields, it 3 was concluded that the gauge area was subjected to predominantly shear stresses (i.e., with stress triaxiality approximately equal to zero). The middle nodes 1, 2 and 3 (Figure 3(a)) for case T1 (Figure 11(a)) displayed small deviations through 6 the thickness in the middle of the sample with an increase of the mean shear 7 strain. However, the mean values for time step 300 were equal to 0.03 for all three nodes (Table 5). The second set of nodes (i.e., 4, 5 and 6) experienced notable 9 fluctuations. However, their levels all converged toward 0.33 (i.e., tensile stress state) for the final time step.

**Table 5:** Mean nodal stress triaxiality for each test case in the plastic regime (*i.e.*, from time step 100 to 340)

Node	1	2	3	4	5	6
T1	0.01	0.02	0.03	0.20	0.19	0.20
T2	0.01	0.02	0.03	0.20	0.19	0.20
Т3	0.02	0.02	0.02	0.20	0.19	0.20
T4	-0.01	0.02	0.06	0.20	0.20	0.25
T5	0.01	0.02	0.04	0.20	0.25	0.50

- Test case T2 was essentially identical to T1 with regards to nodal stress tri-
- 2 axiality history, thereby indicating negligible influence of friction on the stress
- triaxiality (Figure 11(b)). Furthermore, similarities were also observed for the
- 4 mean levels (Table 5); for cases T1, T2 and T3, they were identical. Test case
- 5 T3, where only in-plane displacements were prescribed on the stressed edges, did
- 6 not exhibit any buckling, which was further illustrated by the indistinguishable
- stress triaxiality histories for nodes 1, 2 and 3 and 4 and 6 (Figure 11(c)). Node 5
- 8 displayed an identical history as cases T1 and T2.
- Test case T4, where the FE model was enriched with out-of-plane displace-
- ments, exhibited more pronounced buckling compared to the first two cases (Fig-
- ure 11(d)). Therefore, the previously commented trend for nodes 1,2 and 3 was no
- longer observed. A divergence of nodal stress triaxialities occurred (Figure 11(d)).
- This phenomenon was attributed to buckling since Surface 3 (Node 1) was sub-
- jected to compression and Surface 1 (Point 3) to tension according to the stress
- triaxiality fields (Figure 9). The middle point 2 displayed the same response as in

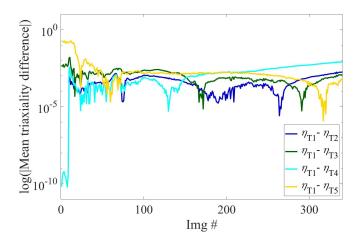
- previous test cases. Nodes 4 and 6 also experienced higher divergence compared
- 2 to the other test cases. Nodes 2 and 5 located on the middle plane (i.e., Surface
- 2) did not exhibit any dependence on buckling as the levels and histories were
- 4 equivalent to case T1.



**Fig. 11:** Nodal stress triaxiality history vs. mean shear strain (in the optical gauge) for test cases T1 (a), T2 (b), T3 (c), T4 (d) and T5 (e). For the middle nodes 1,2 and 3, the trend is similar for all cases, except T4 where buckling developed. For nodes 4, 5 and 6 the trend is similar for each test case.

cases were of similar order of magnitude.

The introduction of measured out-of-plane displacements on Surface 1 resulted in noisier stress triaxialities (Figure 11(e)). Although all nodes were affected, nodes 3 and 6 suffered the most since they were located on the constrained surface, thus displaying higher sensitivity to measurement uncertainties. The influence of the latter ones was also observed from the mean values of all nodes as they showed slight deviations from the previous test cases, especially for node 6, which was two times higher than for the other cases (Table 5). Figure 12 reports the mean stress triaxiality differences for Surface 2 with respect to test case T1 since for the chosen plane all cases displayed similar results. The mean stress triaxiality differences for test cases T2 and T4 showed similar 10 trends. For the first one hundred images (in elasticity) the differences were insignificant, whereas in the plastic regime they were several orders of magnitude 12 larger. Conversely, test cases T3 and T5 exhibited much larger differences than T2 and T4 in elasticity. However, T3 did not display any distinct change in the 14 difference levels, whereas T5 showed a gradual decrease of the differences with increased load levels. This trend was attributed to a better description of sample buckling, thus better simulating the complex stress states in the material. Al-17 though additional measurement uncertainties were introduced in test case T5, no severe anomalies were observed. In plasticity, the mean differences for all test



**Fig. 12:** Comparison of mean stress triaxiality differences for Surface 2 between all test cases with respect to T1. Highest differences are reported in elasticity, whereas for plasticity the differences are of similar orders of magnitude. Slightly higher differences are observed between test cases T1 and T4 thereby confirming that for the stress triaxiality fields it is necessary to use a 3D model.

#### 5. Discussion

- In this section, the influence of the calibrated parameters on the stress triax-
- 3 iality fields is studied for each test case. The converged solution for the stress
- 4 triaxiality fields was subtracted to that for which a single parameter was changed
- 5 by 1%. The standard differences per image are displayed for all three surfaces to
- 6 study the influence of the considered parameter through the sample thickness.
- By observing the standard sensitivity to the yield stress  $\sigma_y$  (Figure 13), a sud-
- 8 den increase to stress triaxiality differences occurred in the early stages of yielding
- 9 as seen on the force curve. This trend was similar in all test cases. For cases T1
- and T5, the increase was more pronounced than for the other ones. In the middle
- of the sample (i.e., Surface 2) the highest difference was observed for T1, whereas
- on Surface 3 it was for cases T5 and T1. This trend was attributed to the complex-

- 1 ity of the numerical models. After the initial stages of yielding, the calculated
- 2 differences were lower and stable until the end of the numerical analysis.

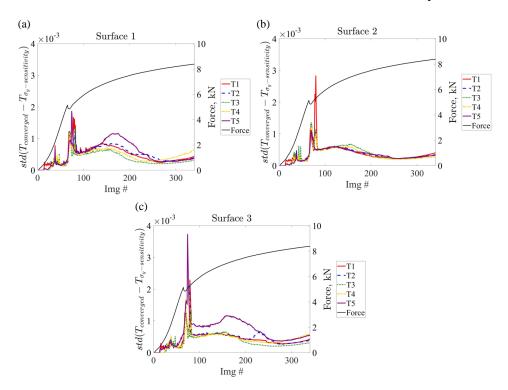


Fig. 13: Standard sensitivity of stress triaxiality fields to  $\sigma_y$  for each test case for (a) Surface 1, (b) Surface 2 and (c) Surface 3. A sudden increase in standard sensitivity occurred in the early stages of yielding for each test case. These changes are negligible since they were two orders of magnitude lower than the actual stress triaxiality levels.

- The standard sensitivity of the stress triaxiality fields to parameter C (Fig-
- 4 ure 14) was the highest in the early stages of hardening. In elasticity and early
- 5 plasticity, they were negligible and after yielding they began to rise. After the
- 6 maximum point, the values decreased and remained low until the end of the nu-
- merical simulations. For case T5, the highest level was reached for Surfaces 1
- 8 and 3. For Surface 2, all test cases displayed similar values. However, for Sur-
- 9 faces 1 and 3, T4 was an outlier since toward the end of the simulation the stress

triaxiality differences did not follow the same trend as the other test cases.

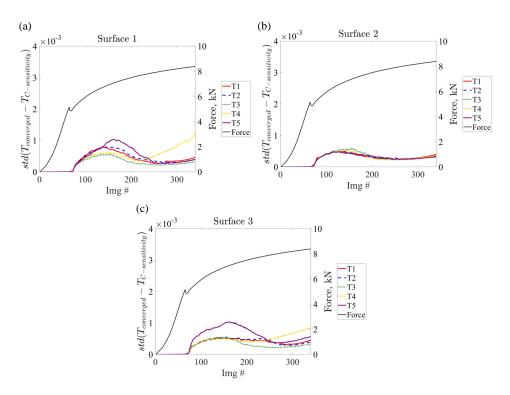


Fig. 14: Standard sensitivity of stress triaxiality fields to parameter C for each test case for (a) Surface 1, (b) Surface 2 and (c) Surface 3. The standard sensitivities were higher in early plasticity. Such changes are negligible since they are approximately three orders of magnitude lower than the actual stress triaxiality levels.

- For all test cases, the change in parameter c (see Figure 15) displayed an influ-
- ence on the stress triaxiality differences at the very end of the numerical simula-
- tions (i.e., when approaching the ultimate load). In elasticity and early plasticity,
- 5 the differences were negligible. During the early stages of hardening the influ-
- 6 ence was more noticeable. Yet, it was still limited in comparison to later stages.
- 7 On Surface 1, case T4 displayed much higher values than the other ones due to
- 8 buckling initiation.

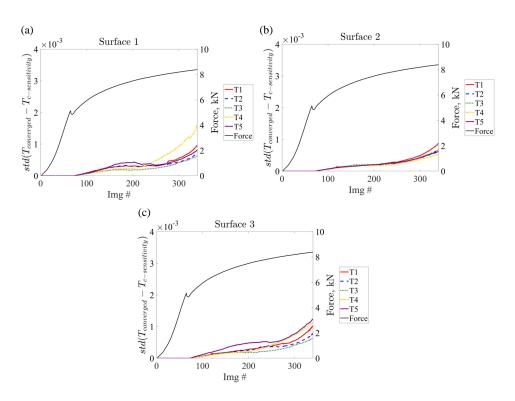


Fig. 15: Standard sensitivity of stress triaxiality fields to parameter c for each test case for (a) Surface 1, (b) Surface 2 and (c) Surface 3. The standard sensitivities are more pronounced at the very end of the numerical simulations. These changes are negligible (three orders of magnitude lower) compared to the actual triaxiality levels.

- From Figures 13-15 it was concluded that the change in triaxiality fields re-
- mained very limited as the standard variations were of the order of  $10^{-3}$ . These
- 3 differences were ten times lower than the parameter changes. It is worth noting
- 4 that for Surface 2, for each parameter, the stress triaxiality differences were mini-
- 5 mal and the curves for each test case were in good agreement. For the yield stress
- $\sigma_y$ , the differences were higher in amplitude than for the hardening parameters C
- and c for each test case and surface.
- Table 6 gathers the mean sensitivities calculated from image 150 until the end
- of the analysis for each surface and test case observed in Figures 13-15. For Sur-

- faces 1 and 3, larger fluctuations were observed, where T5 displayed the highest
- sensitivity to material parameter changes. Conversely, for Surface 2, the change
- 3 of material parameters induced similar influences on the stress triaxiality changes
- 4 for each test case. These values were two orders of magnitude lower than the
- 5 parameter change (1%).

6

Table 6: Mean standard sensitivities to parameter changes for the three considered surfaces

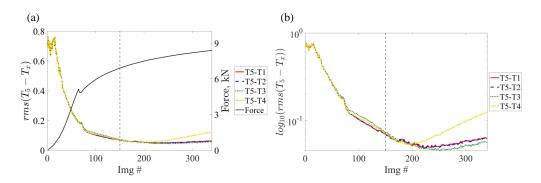
	$\overline{std(\sigma_y)} \times 10^{-4}$			$\overline{std(C)} \times 10^{-4}$			$std(c) \times 10^{-4}$		
	S1	S2	<b>S3</b>	S1	<b>S2</b>	<b>S3</b>	S1	S2	<b>S3</b>
T1	3.9	3.1	4.4	4.2	3.1	4.2	4.3	3.5	4.2
T2	4.3	3.2	4.9	4.1	3.1	4.5	3.7	3.1	3.7
Т3	3.1	3.4	3.1	3	3.2	3	2.9	3.1	2.9
T4	4.2	2.9	4.4	5.4	3	6.2	4.7	2.7	5.8
Т5	6.7	3.2	5.8	6.2	3	5.3	6.1	3	4.4

as reference and the stress triaxiality fields were subtracted to each previous test case only for Surface 1. This choice was made as measured out-of-plane displace-

Last, the comparison between all test cases is analyzed. Test case T5 was taken

- 9 ments were prescribed on the aforementioned surface. Root mean square (RMS)
- differences were calculated and are displayed in Figure 16. It was observed that in
- elasticity, the RMS differences were about eight times higher than in the hardening
- stages of the sample (Figure 16(a)). In the semi-logarithmic plot (Figure 16(b))
- this trend becomes clearer. In elasticity, each type of BC had a strong influence on
- the stress triaxiality levels and distributions. As plasticity set in, the displacement
- levels became higher. Therefore, when comparing these computations, the results

in elasticity were discarded.



**Fig. 16:** Root mean square differences in stress triaxiality fields with respect to test case T5 for Surface 1. (a) RMS difference vs. image number. (b) Semi-logarithmic plot of the previous differences. The dashed vertical line depicts the beginning of the computations reported in Table 7. The highest differences are for case T4 where buckling developed whereas for other cases they remained of same order of magnitude.

- In Table 7, the mean values of the RMS differences are gathered from image
- 3 150 until the final one. It was observed that the lowest value was for T3. Since
- 4 T1 and T2 were similar, except for the consideration of friction, the mean differ-
- 5 ences were close. The highest difference was for case T4, where significant and
- 6 unphysical buckling occurred. Although there was a visible influence of different
- <sup>7</sup> BCs, they remained low.

Table 7: Mean RMS differences in stress triaxiality fields with respect to T5 for Surface 1

Case	$\overline{RMS}$
T5-T1	0.0561
T5-T2	0.0563
T5-T3	0.0528
T5-T4	0.0768

## 6. Conclusions and outlook

- In this study, an extensive analysis was carried out to evaluate the effect of
- 3 different Dirichlet BCs on the evaluation stress triaxiality fields. The prescribed
- displacements were measured via FE-based stereocorrelation for a simple shear
- 5 test on a 1 mm thick sample. To evaluate stress triaxiality fields, the constitutive
- equation and its parameters had to be identified. Armstrong-Frederick's kinematic
- <sup>7</sup> hardening model was selected and calibrated via weighted FEMU.
- First, the five investigated cases led to different sets of material parameters.
- 9 Yet, negligible influence was evidenced on the stress triaxiality fields. A very fine
- calibration of the material response was thus not required in the studied test.
- Second, when modeling the anti-buckling fixture, the friction coefficient was
- considered as an additional parameter to be calibrated. Compared to the predic-
- tions with a very small value, the stress triaxiality fields were very close even
- though the calibrated material responses were different. Such simulations were
- 5 very costly, therefore three other cases were also investigated.
- Third, by prescribing only in-plane displacements measured on the stressed
- surfaces of the FE model, limited wrinkling was not accounted for. Interestingly,
- the stress triaxiality fields were close to the previous estimates and constituted a
- 19 first estimate if wrinkling had been fully prevented.
- Fourth, by also considering the out-of-plane displacements on the stressed
- edges of the sample, buckling was observed in the simulations. The resulting de-
- 22 formed shape was not consistent with the measured one. Different stress triaxiality
- 23 fields were observed and it was concluded that they were not physical.
- Fifth, prescribing all out-of-plane displacements as BCs on the sample surface,

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- limited buckling was accurately simulated. The drawback was the inclusion of ad-
- ditional measurement uncertainties through such BCs. As a result, the stress triax-
- 3 iality fields were more fluctuating, yet close to the levels observed when modeling
- the anti-buckling fixture. This case provided, by construction, accurate deformed
- 5 shapes in a less computationally demanding manner than the first one.
- The framework presented herein is not limited to the specific experiment
- 7 where simple shear was applied to an Arcan sample. The procedure is generic
- 8 and may also be applied to simpler or more complex experimental investigations
- 9 and for other materials.

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- perform the stereocorrelation analysis reported herein.

# 15 Compliance with Ethical Standards

The authors have no conflict of interest to declare.

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