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How chemical defects influence the charging of nanoporous carbon supercapacitors

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Ion desolvation and confinement are key physical processes in porous-carbon based supercapacitors undergoing charging and discharging cycles. We investigate electrolyte interactions between polarized porous carbon with subnanometer pore sizes and aqueous sodium chloride electrolyte using molecular dynamics. Inspired by recent first principles calculations, we developed a scheme accounting for chemical defects in electrodes where only the non-sp2 carbons species carry an extra negative charge (on the anode) and an extra positive charge (on the cathode) due to voltage polarization. This drives electrolyte species (ions and solvent molecules; water in this work) to adsorb at the electrode surface and in subnanometric pores upon polarization. First we observe an asymmetrical desolvation process of sodium and chloride ions at the external surface of the electrodes. The ionic distribution at the external surface of the electrodes is consistent with the Debye-Hückel electric potential equation and empirical trends observed for non-porous electrodes. In a second stage, we demonstrate that the nanoporosity of the electrodes is filled with ions and scarce water molecules and contributes to about 20% of the overall capacitance. A fraction of desolvated ions are irreversibly trapped in the core of electrodes during discharge. While maintaining the overall electroneutrality of the simulation cell, we found that anodes and cathodes do not carry the same amount of ions at all time steps leading to charge imbalance.

Ionic adsorption | Molecular dynamics | dehydration

derivation of the fundamental physical basis of electrochemical energy storage underlying modern electrochemistry devices like batteries and supercapacitors (1, 2). In particular, fundamental understanding of the ionic adsorption processes and confinement inside nanoporous carbon electrodes is essential for predicting and improving the capacitance (3) or deionisation efficiency of carbon-based devices (4, 5). Recent in situ X-ray (6) and neutron scattering (7) have shown that subnanometric pores of carbon electrodes enhance the ionic adsorption and its overall capacitance performance (8). In fact, if the pores are of the same size as electrolyte ions, high capacitances (leading to the term supercapacitor) have been observed that does not follow existing theories and empirical trends (9–12).

The term of electrical double layer (EDL) capacitor comes from the classical picture of non porous electrodes that accumulate oppositely charged ions at their vicinity upon voltage polarisation in a mean-field dielectric continuum description of the solvent populated with point charged ions at a given concentration. This picture although very popular obviously does not hold for porous electrodes with sub nanometric pores. In particular, the mean-field Gouy-Chapman-Stern description of a EDL fails in high molar concentrations and for pore

sizes smaller than a few nanometers (typically 4 nm for carbon substrates) (13, 14). EDL predictions usually rely on the Poisson-Boltzmann theory and modified versions such as Debye-Hückel (15, 16) and Donnan models (17). More recent approaches based on thermodynamics theory for heterogeneous ionic fluids allow to take into account ionic size hence ionic position correlations(18). Recently, this statistical physics description of an EDL theoretical prediction was extended to include time dependence and study the dynamics of the ionic charging process of a planar electrode (19).

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Presently, there is no theory capable of solving the electrostatics problem for ions confined in the nanopores of a disordered porous carbon material commonly used in electrochemical devices. Nowadays, atomistic simulation techniques implement statistical physics methods that are able of describing both the intrinsic textural disorder of a porous carbon materials at the nanoscale and the movement of electrolyte species (solvent molecules and ions) in their pores under operational functioning conditions of a supercapacitor device (i.e. under polarization) (20–23).

There are currently two main approaches to describe atomic systems under polarization, the constant voltage (CV) and the constant charge (CC) methods. (i) The CV approach assumes a perfectly conducting substrate hence accumulating/depleting charges only on the atoms at the pore and external surfaces with no regards to the intrinsically defective nature of porous

Significance Statement

Nanoporous carbon texture makes fundamental understanding of the electrochemical processes challenging. Based on DFT results, the proposed atomistic approach takes into account topological and chemical defects of the electrodes and attributing them a partial charge that depends on the applied voltage. Using a realistic carbon nanotexture, a model is developed to simulate the ionic charge both at the surface and in the subnanometric pores of the electrodes of a supercapacitor. Before entering the smallest pores, ions dehydrate at the external surface of the electrodes leading to an asymmetric adsorption behavior. Ions in subnanometric pores are mostly fully dehydrated. The simulated capacitance is in qualitative agreement with experiments. Part of these ions remain irreversibly trapped upon discharge.

R.D, K.I, and R.P. designed, wrote the manuscript, discussed and analyzed the results, R.D. and P.-L. V. performed the calculations

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carbons (see Fig. 1(a)). Applied to porous carbon materials, the CV approach thus assumes that all carbon atoms are in the sp2 hybridisation state, i.e. conducting electrons. The main assumption of the CV method is, therefore, the metallic approximation - the electrodes are considered ideal conductors with no localisation of electric charge except at the material boundaries in contact with the electrolyte. In recent simulation works(10), pore surfaces are treated as an extension of the external electrode surface. It is important to indicate that the charging process of substrate atoms is in the order of fs while ion diffusion occurs at the scale of ns (24, 25). Thus upon polarisation, the charges on the solid matrix species attract ions first. Once equilibrium is reached, thermal agitation of adsorbed ions can induce (in a constant voltage description) charge fluctuation on electrode atoms that in turn can redistribute ions in their vicinity. This is the main advantage of the CV approach; its main drawback is that it ignores charge localisation due to chemical heterogeneity. As a result, within the CV approach, ion docking is only observed at the external surfaces of the electrodes or in large nanopores; the subnanopores being found not to participate to the capacitance in sharp contract to experiment of activated carbon based super-capacitors (see Fig. 1(b))(3).

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(ii) The standard CC approach gives all substrate atoms the same fixed charge. The main drawback of the CC approach is that substrate charges are not allowed to fluctuate upon ion docking. Thus, this method only simulates the initial ion docking dynamics before charge self-regulation takes place. In the literature, it was reported that the CC approach may lead to an unphysical temperature increase(26). In the supplementary materials we give evidence that this issue might come from the configurational setup of the simulation cell with bouncing walls for ions in a rigid electrodes approximation. With a full periodic cell simulating a stack of immersed electrodes. using NVE simulation under polarization we found that the temperature was well tempered (after initial relaxation at 300K). However, this leads to unphysical ion docking deep in the electrodes regardless the pore size (see Fig. 1(b)). In sum, both the standard CC and CV methods fail for different reasons hence, are not able to reliably simulate the adsorption of ions in subnanoporous polarized electrodes (see Figs. 1(a, b)).

Therefore, we modified the CC method guided by experimental and theoretical results showing the key role of chemical defects and subnanopores in the building up of the capacitance(9, 27-34). With this method, there is no additional computational cost compared to classical MD-CC calculations. The local electrostatic field generated by the matrix defects (in the present work non sp2-carbon atoms and edge hydrogen species) drives ion adsorption on the electrode external surface as well as in the whole porosity including the subnanopores. Our electrodes are made of porous carbon texture that is found to be realistic for charcoal, activated carbon as well as for mature kerogen (35, 36). It was obtained using Hybrid reverse Monte Carlo(37) with a density around 1g/cc. Note that our activated carbon texture contains subnanometric pores of 0.5-0.9nm (see Fig. 1(d). This sharply contrasts from Carbide-Derived-Carbons (CDC) (38) previously used in supercapacitor simulations that only contains pores above

We propose a chemically driven charge localization model

(CDCL) that locates partial charges to defective species through the entire electrodes including species at the external or pore surface that are by nature defective. It takes advantage of both CC and CV methods while correcting their main drawbacks opening the path for modelling the adsorption of ions in subnanoporous defective electrodes including the role of doping of elements as such as N, S, F, etc.

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We demonstrate that using MD simulations with the COM-PASS force field (39, 40) at 300K, the CDCL approach unravels many subnanometric features underlying the physics of ion docking in the charged electrodes ranging from the differentiated desolvation mechanism of cations with respect to anions and their asymmetric adsorption/desorption mechanism inside the nanopores. The pore size distribution shows a maximum at 0.5-0.6 nm (Fig. 1(d)). Sodium and chloride ions can only dock as single bare ions (i.e. unsolvated) in those pores. The electrodes are separated by 30Å on both sides. The system is periodic in all directions and it is initially prepared with 6100 water molecules, 60 sodium and 60 chloride ions in the interelectrodes regions corresponding to a salt concentration of 0.67 mol/L (see Methods). As shown in Fig. 1(e), the texture of the electrode near the ions contains defects (incomplete rings or rings with 5 members). Fig.1(f) shows the ion density after polarization and we can observe ion docking inside the porous electrodes.

1. Results and discussion

In view of the limitations identified for the CC and the CV method, we have chosen to develop the CDCL approach guided by the chemical attributes of the electrodes. Our electrodes are made of 70% sp2 carbon atoms i.e. having three carbon neighbors as immediate neighbors with a typical angle between consecutive carbon atoms around 120 degrees. The other 30% of carbon atoms can be considered as defects where charges are localised (an increase of partial charge for anode atoms, a decrease for cathode species) (41) (see DFT calculations in S.I.).

Upon polarization, DFT calculations show that excess charges in absolute value are localized on the defects or at their vicinity (30). Therefore, the CDCL scheme for the attribution of additional charges consists in applying a Δ_q value to the non-sp2 carbon atoms while attributing a null charge to sp2 carbon atoms. The sp2 character is hereafter determined based on the C-C-C angle between three consecutive carbon atoms (see S.I.). For the sake of simplicity, we assume the following linear formula for the excess charge estimate:

$$\begin{split} & \Delta_q = & \Delta_{q,max} * (|(\Theta - \Theta_{max})|/10) \forall \Theta \in [\Theta_{max} - 10, \Theta_{max} + 10] \\ & \Delta_q = & \Delta_{q,max} \forall \Theta \notin [\Theta_{max} - 10, \Theta_{max} + 10] \end{split}$$

where Θ_{max} is the value of the C-C-C angle in a perfect sp2 matrix (equal to 120 degrees) and $\Delta_{q,max}$ is the maximum excess charge (positive for the anode and negative for the cathode), which magnitude depends on the applied voltage. We calculated that a value of +/- $\Delta_{q,max}$ =0.0337 e gives an excess/deficit average charge on the anode/electrode of Δ_q equals +/- 0.02 e. In order to compare our results with results obtained with the CV method, we have calculated a conver-

sion factor by computing the average charge attributed to

the electrode atoms in the CV method. If we apply 1V, the

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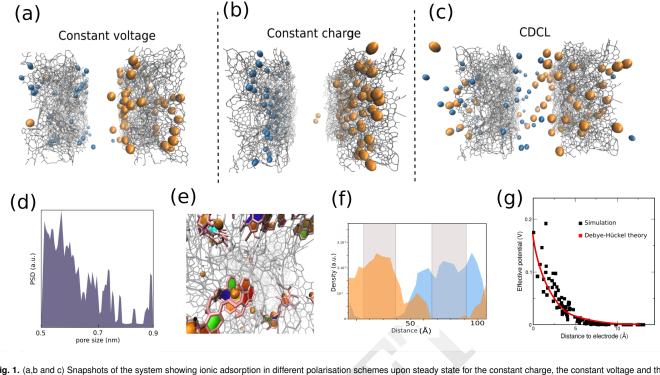


Fig. 1. (a,b and c) Snapshots of the system showing ionic adsorption in different polarisation schemes upon steady state for the constant charge, the constant voltage and the chemistry driven charge localisation schemes respectively. (d) Pore size distribution of the electrodes. (e) structure of the local structure of the porous carbon electrode near adsorption sites. Colored surfaces are guides for the eyes to emphasizing the texture of the pores near the docked-ions. (f) density of Na (in blue) and Cl (in orange) for $\Delta_q = 0.02$ e (1V) along the simulation cell axis, the two grey bands correspond to the electrodes position and thickness. (g) Calculation of the effective electrical potential acting on the ions in the solution for $\Delta_q = 0.02$ e (1V). Effective potential acting on the ions in the simulation cell (in black). Due to the roughness, the position of the surface has to be defined arbitrarily, which has been done using the position of the most forward carbon atom of the electrode. Fit obtained using the Debye-Hückel formula (in red). The charge distribution follows a Debye-Hückel law due to the screening of the solution.

average excess/deficit charge is +/-0.02 e per carbon atom on the anode/cathode respectively, which gives a voltage conversion factor of 0.02. In the CDCL approach, carbon defective species have a nominative charge that reflects their local chemical environment and is in absolute value proportional to the departure from the perfect sp2 state (equation 1) and the applied voltage.

Recent CV atomistic simulations of CDCs carbon-based porous structures have shown that solvated ions are adsorbed in pores above 1nm in size; no fully dehydrated ions have been observed implying that the subnanopores are still empty, in agreement with what we observe in our CV simulations(42). As demonstrated here below, it is important to note that the CDCL approach is the only method that is able to predict at the same time the adsorption of fully dehydrated ions inside the subnanopores (less than 1 nm, Fig. 1(c)), partially or fully hydrated ions on the external surface or in any other kind of larger pores. All confinement environments were experimentally found to contribute to the overall capacitance of EDL devices(2).

First, we investigate the adsorption of ions on the external surface of the electrodes. The excess charge imposed additional Coulombic forces on the ions of the system. The effective voltage acting on the ions has been computed by extracting the Coulombic forces on the ions with and without electric field at the initial time of the simulation. The charge distribution, in Fig. 1(g), shows that ions close to the external surface of the electrodes are the ones experiencing larger attraction forces due

to the applied voltage compared to ions in bulk electrolyte away from the electrode surface. Since it is related to a Coulombic term, the force experienced by the ions is proportional to Δ_q (see equation 1). The evolution of the effective potential is characteristic of electrolyte solution and screening effect. Using the Debye-Hückel formula(43), we can compare the Debye length obtained from the simulation and that for a solution with a uniform ion distribution for an ionic concentration of 0.67 mol.L⁻¹ (corresponding to the salt concentration in the inter-electrode void), with a dielectric constant of 80(44). The agreement between the simulation and the Debye-Hückel expression for the electric potential at the external surface of the anode is remarkably good and gives a Debye length around 0.2-0.3 nm in quantitative agreement with Debye length obtained for this electrolyte type and concentration(44).

The number of effective ions adsorbed on and in both porous electrodes is related to the capacitance of the system. The capacitance has been calculated and is reported on Fig 2(a) for each simulation with different Δ_q (the estimation of voltage is given from the aforementioned conversion). There is a threshold at low voltage above which ions are being adsorbed on the external surface of the electrodes (approximately Δ_q =0.0025 e corresponding to 0.125 V). For larger polarization voltages, the amount of ions incorporated in the electrodes increases quasi-linearly until it reached the maximum, hence, the capacitance exhibits a peak shown in Fig. 2(a) in agreement with the recent theoretical and simulation work of Verkholyak et al.(45). Note that at voltages above about 1.8V, we consider

that the simulation is probably unrealistic since we do not consider water splitting that happens at these voltages (46). The capacitance is in agreement with the typical measured capacitance of activated carbons (around 100 F/g with a specific surface area at around 500 m²/g for our carbon texture) (47). The maximum capacitance we find, of about $20\mu\text{F/cm}^2$ is in agreement with experimental values (2, 9, 10). Comparing the results obtained with the CV and the CDCL on figure 2(a), we can estimate that the contribution of the subnanopores to the capacitance is about 20%, meaning that the supercapacitor made of subnanoporous electrodes remains mostly a standard EDL device with respect to aqueous electrolytes.

Due to the ionic docking in the subnanometric pores, the capacitance estimated from the CDCL method is larger than that the one obtained with the CV method (dots, see Fig. 2(a)). There is a positive correlation between the capacitance and the specific surface area as measured with BET experiments (48). In fact the large value of the specific surface area reflects both the amount of subnanopores and chemical defects on the carbon backbone. Chloride and sodium contribute differently to the capacitance (orange and blue dashed lines, see Figs. 2(a)). The adsorption sites are different due to the ionic size, as shown by the radial distribution function in Fig 2(b). This leads to an asymmetric loading and charge unbalanced electrodes, which is a direct consequence of the ion docking into the subnanometric pores (while the simulation cell overall charge remains neutral at all times in the simulation). The capacitance being the sum of the charges divided to the voltage, the peak can be explained with the less and less efficient ion docking upon voltage increase, this will be discussed hereafter.

In more detail, Figs. 3(a) and (b) show the number of adsorbed ions on the surface, inside the subnanopores of the electrodes during polarization simulations and the total ionic loading during charge and discharge simulations with $\Delta_q = 0.01e$ (see S.I. video). At the voltage corresponding to the maximum capacitance, the total adsorption is larger for Cl⁻ than Na⁺. Comparing Figs. 3(a) and (b), one can see that Na⁺ is mostly adsorbed at the external surface whereas Cl⁻ is equally adsorbed inside and at the external surface of the electrodes. We observe that half of the sodium ions are adsorbed; the rest remains in the solution in-between the electrodes. Similarly, 2/3 of the chloride ions are adsorbed and 1/3 remain in the electrolyte solution.

Fig. 3(c) shows the number of adsorbed ions (i) on the surface, (ii) inside the nanopores and (iii) in total for different polarizations. Cl⁻ ions are partially adsorbed on the surface and inside the electrode nanopores following a monotonous increase until Δ_q =0.01e (0.5V) and then it reaches a plateau. Na⁺ is adsorbed in larger quantity than Cl⁻ at voltages larger than Δ_q =0.01e (0.5V). Interestingly, as the voltage increases, we observe a transition from an external surface adsorption only (from Δ_q =0.0025e to Δ_q =0.01e) to a dual inside-pore docking/surface adsorption for the sodium ions above Δ_q =0.01e (0.5V). This is due to the fact that surface adsorption involves hydrated ions whereas inside-pore docking involves bare ions. Low voltages do not provide enough energy to loosen the hydration shell of Na⁺ leading to external surface adsorption of hydrated ions (2).

The process of ion adsorption in nanopores is accompanied with a change in the solvation shell of the ions. In bulk water, sodium ions have a first solvation shell made of approximately 6

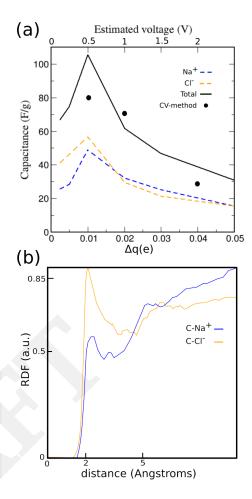


Fig. 2. (a) Capacitance due to sodium and chloride ions adsorbed inside and onto the electrodes at steady state with a maximum additional charge Δ_q (the added/subtracted charge is maximal on defective (non-sp2) sites). Note that the carbon atoms at the vicinity of the pores are not necessarily the non-sp2 carbons. The x-axis represents the excess of charge on each carbon atom of the positive electrode with respect to Δ_q . The dots correspond to the calculated value with the CV method. The simulated capacitance value is in the ball park of experimental values (100 F/g) for supercapacitors based on porous carbons with specific surface area around 500 m²/g (which is the value of our simulated porous carbon) (b) Radial distribution functions for C-Na and C-Cl distances at steady state for $\Delta_q =$ 0.01e.

water molecules (49), which is also observed in our simulations before charging the electrodes. An ion and its first layer hydration shell are of about 0.7 nm in diameter and, therefore, can only access the largest pores in our system.

Fig. 3(d) shows the evolution of the hydration shells of the adsorbed Na⁺ and Cl⁻ ions together with the total number of adsorbed ions at Δ_q =0.01e (0.5V). The adsorbed Na⁺ ions are surrounded on average by 4-5 water molecules, whereas the Cl⁻ ions carry 2-3 water molecules. All adsorbed ions have lost either partially or totally their hydration shell, when adsorbed on the surface of the electrodes, or their whole hydration shell when entering the subnanopores. Fig. 3(e) shows the hydration number of Cl⁻ ions before adsorption and after adsorption inside the nanopores. The hydration shell becomes loose at the surface and then the ions can enter either bare or with at most one water molecule in the subnanopores. Note that we observed the formation of anion-cation ionic pairs only in the solution outside of the electrodes.

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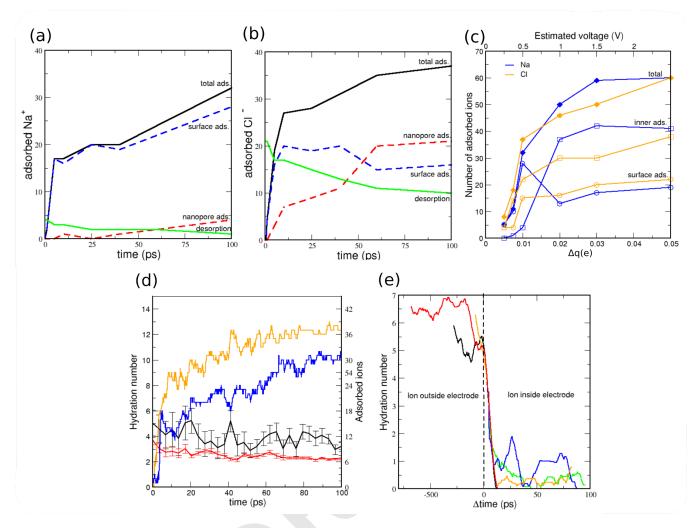


Fig. 3. (a) Evolution of the number of sodium ions in the electrode during the loading, adsorbed in the pore network (blue) or on the surface of the electrode (red) while imposing a voltage corresponding to a Δ_q =0.01e (0.5V) (total in black) and during unloading (in green) for Δ_q =0. To determine the adsorption, a cutoff of 4.0 Å and 5.0 Å have been used for Na-C and CI-C distances respectively, corresponding to the first minimum in the radial distribution functions. (b) Evolution of the number of chloride ions in the electrode. (c) Number of (blue) sodium ions and (orange) chloride ions adsorbed (diamond) in total, (squares) inside the electrodes, (circles) at the surface. (d) Evolution of the hydration number during the adsorption around Na (black) and CI (red) ions and number of ions adsorbed inside the electrodes at Δ_q =0.01e (0.5V). Error bars correspond to the standard deviation. Evolution of the quantity of adsorbed Na (blue) and CI(orange). (e) Hydration number of several ions versus Δ time (each color corresponds to a different Na⁺ ion), where Δ time is the time difference to the moment where the ion enters into the electrode. The values reported are the running average over 100 steps.

Focusing now on the role of water in porous electrodes at full saturation, we observed that in polarized electrodes that few water molecules adsorb in the pores of the electrodes (50). The ratio for the amount of water inside the electrode is less than 15%. The carbon structure is rather hydrophobic as indicated by radial distribution functions (shown in S.I.), the shortest C-water distance being about 3.5 $\rm \mathring{A}$.

Corrected for the effective accessible pore volume, the subnanopores are just large enough to accommodate one bare ion (diameter for sodium and chloride equal 0.1nm and 0.18nm respectively) in agreement with the conclusions of Simon and Gogotsi(2). While the electrodes are being charged, the density of water inside the electrodes slightly increases. This indicates that the adsorption of ions into the carbon electrodes make the structure less hydrophobic in a similar fashion as the clay interlayer void is hydrophilic only because the presence of cations compensating the overall clay layer negative charge. The clay basal planes per se are rather hydrophobic

as they carry no OH surface groups immediately in contact with adsorbed water; the ions act as water pump inside a polarized porous carbons or in-between clay layers charged through isomorphic substitutions (51).

In summary, chloride and sodium ions in water are behaving differently upon working conditions of a supercapacitor (52). Chloride species appear to be more mobile than sodium ions that are likely to get trapped in their tighter hydration cage (53). It also makes chlorides adsorbing faster and at lower voltage inside the carbon nanopores (see Figs. 3(a) and (b)).

Regarding the desorption process, the ions that are adsorbed deep in the core of the electrode will more likely remain trapped upon discharge. At voltage set back to zero, about 10% of the formerly docked Na⁺ ions (about 3% of the total number of cations) and 30% of the adsorbed Cl⁻ (about 10% of the total number of anions) are still trapped inside the electrodes (after 1 ns of unloading, 2 Na⁺ and 6 Cl⁻ are inside the electrodes, see S.I.). Note that desorption, which is

simulated under a null voltage, takes place over a longer time than ion docking (see Figs. 3(a and b)). The trapped ions may not participate to the current unloading cycle but they could move to a nearby pore during the cycling and become again available for storage. The trapped ions upon depolarization is compatible with the hysteretic behavior observed in the supercapacitor I-V characteristic curve. More specifically, the ions that are being desorbed at zero voltage are only the ions that have an easy path to exit the porous material. Other ions, that are in small pores or in tortuous porous network, are not easily extracted from the media. Being smaller ion, Na⁺ is often trapped more deeply in the porous network at larger voltages. Three adsorption/desorption cycles has been performed in this work and we have observed that after the first cycle, the amount of ions irreversibly docked inside the electrode nanoporosity remains constant.

2. Conclusion

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We propose a new approach to describe the charge and discharge process in subnanoporous carbon made electrodes, in a supercapacitor setting, that we call chemically driven charge localisation model (CDCL). Despite its mean-field character, the CDCL approach is an improvement of the current standard methods to simulate charged devices at the atomic scale, namely the constant charge and the constant voltage methods that are ineffective to correctly describe ionic docking in subnanopores. Informed from DFT calculations, the CDCL method consists in localising charges on defective non-sp2 carbon sites, including chemical or topological defects. By contrast to the standard methods, this allows simulating both adsorption on the electrodes external surfaces and in-subnanopore docking.

Applied to a realistic texture of nanoporous carbon, we could unravel the fundamental processes underlying the capacitive effect of a subnanoporous carbon-based supercapacitor device in operation. We show in particular that subnanometric pores constitute about 20% of the capacitance of such a device using a standard aqueous electrolyte. The simulated value of the capacitance of about 100 F/g (or 20 μ F/cm²) is in good agreement with the experimental values measured on activated carbon based supercapacitors. In more details, we show that the docking of ions in pores is preceded by an assymetrical desolvation at the vicinity of the external pore surface. The ion adsorption density profile on the electrodes external surfaces is in agreement with the Debye-Hückel theory with a Debye length of 0.2-0.3nm. The desolvation process is actually different for sodium and for chloride ions as the hydration shell of sodium is tighter than that of chloride. Once ions are desolvated, they can access nanopores; subnanopores being mostly populated with bare ions in agreement with in situ X-rays experiments (6). Due to the difference in their ionic size, the docking mechanism of sodium and chloride ions, leads to an unbalanced electrode charging. Upon discharge, we found that a significant amount of ions (10% of the cations and 30% of the anions) remains trapped in the subnanopores due to the pore network tortuosity right after the first charge that is compatible with the typical I-V curve of supercapacitors.

The current CDCL method allows exploring how doping with elements such as N, S, etc. influence the ion adsorption and the in-pore docking (54). Furthermore, the current CDCL method could be coupled with a constant voltage approach in

order to take into account the variation of the substrate defects charge upon ionic thermal movement. This will allow studying the ageing of the electrodes texture upon charge-discharge cycling.

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3. Methods

A super-capacitor composed by porous carbon layers (of 22Å thickness), separated with a water solution containing electrolytes, has been simulated with a fully atomistic approach. The electrodes has been generated using a liquid quench MD method (55) using the reactive force field ReaxFF (56) to obtain a micro-porous carbon containing hydrogen (0.3 H/C). The charges due to defects in the carbon structure are compensated by H atoms. This structure has been relaxed at 293 K and 1 atm, then, cut in half in order to add a phase of bulk of water replacing the other half. The cut leads to unstable atoms at the interface due to broken bonds. Thus, we performed a relaxation with an MD run at a higher temperature (1500 K) to force water molecules to react with the unstable carbon atoms, stabilize the structure and diffuse within the structure. Then, we have duplicated the system one time toward the orthogonal direction of the cut surface. Each electrode contains 5440 atoms. has a connected pore network and a density of 1.45 g.cm⁻³.

In order to study the charge of the capacitor with ions we have built a model in which pure water solution has been enriched with 60 Na⁺ and 60 Cl⁻ ions. We have investigated the adsorption of the ions in the porous carbon structure that has been described previously. Since ReaxFF is not well suited for simulating systems with electric fields, the potential used for the charge and discharge simulations is the COMPASS potential (39, 40) to describe the electrodes-water interactions and the SPC/E (57) potential to describe water molecule interactions which is well-known for it's good description of polar liquids. The interactions cutoff has been set to 12Å. In this work, considering the complexity of the electrodes and therefore of finding a relevant force field to simulate the motion of the atoms of the electrodes, the electrodes were kept rigid. This is an approximation that could slightly influence the quantity of ions that can be adsorbed (in a flexible system, one can imagine that the pores will slightly adapt to the presence of ions). In further studies, the use of reactive force fields such as ReaxFF should be considered in order to assess the stability of the structure and the durability of the pore network due to the ion adsorption. Since such a reactive potential relies on the calculation of charges at each step of the dynamics, the CDCL method should be implemented as a post-calculation to add the charge excess/deficit after the electronegativity equalization method algorithm.

Ewald summation has been used for the long range interactions. The PPPM scheme, which is well suited for large systems (in this work over 30 000 atoms), as implemented in LAMMPS has been used with a threshold on the forces of 10⁻⁴. Periodic boundary conditions have been imposed to the simulation cell. The electrodes are symmetrical and the simulation cell is electroneutral.

For the dynamics, we have used a time step of 0.2 fs, in agreement with the frequency of the O-H stretching modes in water. The system has been thermostated using Nosé-Hoover thermostats. Before adding the electric field, the system has been equilibrated during 300ps at 300K. As discussed in S.I., we have not observed any increase of temperature under electric field contrarily to the results published in a recent work by Merlet et al. (26) the authors attribute to a macroscopic dipole moment, which is an artifact of the simulation.

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