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OpenSpyrit: an Ecosystem for Reproducible Single-Pixel Hyperspectral Imaging

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Abstract: This paper describes OpenSpyrit, an open access and open source ecosystem for 8 reproducible research in hyperspectral single-pixel imaging, composed of SPAS (a Python 9 single-pixel acquisition software), SPYRIT (a Python single-pixel reconstruction toolkit) and 10 SPIHIM (a single-pixel hyperspectral image collection). The proposed OpenSpyrit ecosystem 11 responds to the need for reproducibility in single-pixel imaging, which is currently lacking 12 due to limited access to data and reconstruction algorithms. The SPIHIM collection currently 13 contains 140 hypercubes that are acquired using SPAS and reconstructed using SPYRIT. The 14 SPIHIM hypercubes are obtained by inverse Hadamard transformation of the raw data. They 15 have a size of $64 \times 64 \times 2048$ for a spectral resolution of 2.3 nm and a spatial resolution that is 16 comprised between 182.4 µm and 15.2 µm depending on the digital zoom. We also reconstruct 17 the hypercubes at a resolution of $128 \times 128 \times 2048$ using a data-driven reconstruction algorithm 18 available in SPYRIT, which leads to an increased spatial resolution. 19

21 1. Introduction

Spectral imaging is a major tool of modern science, with applications in astronomy, environmental 22 monitoring, food processing, agriculture, and biomedical imaging [1,2]. The pushbroom and 23 filter-based methods are scanning techniques that require multiple measurements to acquire a full 24 (x, y, λ) hypercube. Pushbroom methods acquire one (y, λ) slice at a time and require scanning 25 along the x-axis [3]. Filter-based setups acquire an (x, y) image for one spectral band, with the 26 full hypercube obtained from a sequence of measurements by rotating a filter wheel or monitoring 27 electronically tunable filters [4]. Both pushbroom and filter-based approaches suffer from low 28 optical throughput as only a small part of the hypercube is measured at a time. Moreover, the 29 spatial (i.e., for pushbroom) or spectral (i.e., for filters) resolutions are linear in proportion to the 30 number of measurements, and hence they are either slow or low resolution. These limitations 31 have led to computational snapshot methods that rely on algorithms that reconstruct a hypercube 32 from a few raw measurements [5]. Coded aperture snapshot spectral imagers and their different 33 variants exploit a diffractive element with a programmable mask, such that each raw measurement 34 gives access to an oblique projection of the hypercube [6]. Miniature ultra-spectral imaging uses 35 a liquid crystal phase retarder to multiplex the spectral domain [7]. The spectral DiffuserCam is 36 a multispectral filter array where the optics are replaced by a diffuser, such that each pixel on the 37 sensor can 'see' the whole field of view [8]. However, snapshot imagers suffer from an inherent 38 trade-off between the spatial and the spectral dimensions. 39

Hyperspectral single-pixel imaging is a generalization of single-pixel imaging whereby a reconstruction algorithm is used to recover high-spectral-resolution hypercubes from a set of spectra obtained using a set of spatial light patterns [9–14]. Compared to snapshot imagers, this approach requires more measurements; however, it leads to an excellent spectral resolution, as the spectral dimension is not multiplexed. Hyperspectral single-pixel imaging traces back to the concept of Hadamard spectroscopy [15] that introduced Hadamard-coded measurements to

obtain a signal-to-noise ratio boost known as Fellgett's effect [16]. This approach has received 46 renewed interest thanks to the advent of compressed sensing theory that allows the number of 47 measurements to be drastically reduced [17]. Interest has been further increased with the advent 48 of deep learning that enables fast reconstruction while outperforming handcrafted prior-based 49 methods [18]. The number of algorithms that exploit deep learning for single-pixel reconstruction 50 has continuously increased (see [19-25] to cite only a few relevant works). However, concerns 51 exist about a number of aspects of algorithms based on deep learning, such as the reliability 52 of the reconstruction, the dependence on training data, and the ease of interpretation of the 53 results. There is a need for reproducibility in single-pixel imaging, which is currently lacking 54 due to limited access to data and reconstruction algorithms. Data-driven algorithms are typically 55 difficult to compare due to the hyperparameters and stochastic nature of the training phase. 56 Another concern is the weak characterization of the performance of single-pixel imaging systems 57 (e.g., resolution, sensitivity, robustness to noise) compared to traditional ones (e.g., pushbroom). 58 Here, we propose the OpenSpyrit ecosystem for reproducible research in single-pixel imaging. 59 We have acquired a collection of hypercubes over 2,048 spectral channels using a single-pixel 60 imaging device whose spectral and spatial resolutions were characterized. Our imaging device 61 relies on a digital micromirror device (DMD) that displays a sequence of Hadamard patterns. It 62 acquires a spectrum for each pattern using a commercial spectrometer. While the hypercubes can 63 be recovered directly by inverse Hadamard transformation of the raw spectra, we also consider an 64 explainable reconstruction method based on deep learning [21]. Our datasets - SPIHIM [26] - are 65 made publicly available following FAIR (findability, accessibility, interoperability, reusability) 66 principles [27]. We share the raw data together with the Hadamard inverse transformed 67 hypercubes and the hypercubes reconstructed thanks to deep learning. Our reconstruction method 68 is implemented in the Python package SPYRIT [28], which allows the method to be retrained 69 from scratch or to evaluate the corresponding Pytorch models that we make available. Our 70 acquisition software is released via the SPAS package [29]. We believe the OpenSpyrit ecosystem 71 can considerably ease the training and/or benchmarking of hyperspectral single-pixel image 72 reconstruction algorithms. 73

74 2. Methods

The computational framework implemented in the OpenSpyrit ecosystem is depicted in Fig. 1. To acquire a 3D hypercube using a 2D sensor, we acquire multiple pixels at the same time by shaping the light with a DMD. After a sequence of spectra has been taken by using different DMD patterns, we feed the raw spectra into a deep reconstruction algorithm that recovers the hypercube.

80 2.1. Image formation model

Let $\hat{M} \in \mathbb{R}^{2K \times \Lambda}$ represent the raw measurements, where 2*K* is the number of DMD patterns and Λ the number of spectral channels provided by the spectrometer. Let $P \in \mathbb{R}^{2K \times N}$ be the matrix that contains the DMD patterns, where *N* is the number of (spatial) pixels in each pattern and $F \in \mathbb{R}^{N \times \Lambda}$ represents the 3D hypercube. We model the acquisition process as linear measurements corrupted by Poissonian-Gaussian noise [30]

$$\hat{\boldsymbol{M}} \sim g \,\mathcal{P}(\boldsymbol{PF}) + \mathcal{N}(\mu_{\text{dark}}, \sigma_{\text{dark}}^2),\tag{1}$$

where \mathcal{P} and \mathcal{N} are the Poisson and Gaussian distributions, g represents the system gain (in

⁸² counts/electron), μ_{dark} is the dark current (in counts), and σ_{dark} is the dark noise (in counts).

We choose P as Hadamard patterns, which maximizes the signal-to-noise ratio of the reconstructed hypercube with respect to the additive Gaussian noise [15]. To handle the negative values in P, the light patterns are split into positive and negative parts to be uploaded onto the



Fig. 1. Hyperspectral single-pixel imaging principle. The hypercube $F \in \mathbb{R}^{N \times \Lambda}$ is sent to a compact spectrophotometer via a digital micromirror device (DMD). A sequence of 2*K* light patterns $P \in \mathbb{R}^{2K \times N}$ is uploaded onto the DMD, leading to the measurement of the 2*K* raw spectra $\hat{M} \in \mathbb{R}^{2K \times \Lambda}$. A reconstruction method is then used to reconstruct the hypercube *F* from the raw spectra \hat{M} .

DMD [31]. In notations, we have

$$\boldsymbol{P} = \begin{bmatrix} \boldsymbol{P}_+ \\ \boldsymbol{P}_- \end{bmatrix},\tag{2}$$

where $P_+ \in \mathbb{R}^{K \times N}_+$ and $P_- \in \mathbb{R}^{K \times N}_+$ are the positive and negative parts of Hadamard patterns respectively, i.e., $P_+ - P_- = SH$, where $H \in \mathbb{R}^{N \times N}$ is the Walsh-Hadamard basis and $S \in \{0, 1\}^{K \times N}$ is a subsampling matrix that retains some of the rows of H. In the following, we denote the retained Hadamard patterns by $H_{\downarrow} = SH$. Different subsampling strategies (e.g., random, low frequency, high variance) have been investigated (see [32] for an overview).

We finally preprocess the raw measurements $\hat{M} = \begin{bmatrix} \hat{M}_+ \\ \hat{M}_- \end{bmatrix}$ to compensate for splitting

$$M = \hat{M}_{+} - \hat{M}_{-}, \tag{3}$$

where $\hat{M}_{+} \in \mathbb{R}^{K \times \Lambda}$ and $\hat{M}_{-} \in \mathbb{R}^{K \times \Lambda}$ correspond to the measurements obtained with the positive and negative patterns, respectively. Therefore, the preprocessed measurements M are Hadamard coefficients, in the sense that $\mathbb{E}(M) = H_{\downarrow}F$, where \mathbb{E} denotes the expectation. Note that the problem is separable across the spectral dimension, i.e., $\mathbb{E}(m_{\lambda}) = H_{\downarrow}f_{\lambda}$, $1 \le \lambda \le \Lambda$, where $m_{\lambda} \in \mathbb{R}^{K}$ and $f_{\lambda} \in \mathbb{R}^{N}$ are the λ -th column of M and P, respectively. Therefore, the spectral resolution of the hypercube is given directly by the spectral resolution of the spectrometer, while its spatial resolution depends only on the light patterns and our ability to recover f_{λ} from m_{λ} .

95 2.2. Image reconstruction

The hypercube can be reconstructed in the least squares sense as

$$\boldsymbol{F} = \frac{1}{N} \boldsymbol{H}_{\downarrow}^{\top} \boldsymbol{M}. \tag{4}$$

In the case K = N, the pseudo inverse $\frac{1}{N} \mathbf{H}_{\perp}^{\top}$ is the inverse of \mathbf{H} .

We also propose to reconstruct each λ -slice of the hypercube independently by using a datadriven algorithm. We consider the denoised completion network (DC-Net) [33] that computes the two steps

$$\bar{f}_{\lambda} = \mathcal{G}_{dc}(\boldsymbol{m}_{\lambda}), \quad \text{and}$$
 (5a)

$$f_{\lambda} = \mathcal{D}_{\theta}(f_{\lambda}), \tag{5b}$$

⁹⁷ where \mathcal{G}_{dc} represents the denoised completion step and \mathcal{D}_{θ} represents a neural network with ⁹⁸ parameters θ . The denoised completion network is given by $\mathcal{G}_{\theta} = \mathcal{D}_{\theta} \circ \mathcal{G}_{dc}$.

The operator \mathcal{G}_{dc} is chosen as the linear estimator achieving minimum mean squared error under Gaussian assumptions. It is given by

$$\mathcal{G}_{\rm dc}(\boldsymbol{m}) = \frac{1}{N} \boldsymbol{H}_{\downarrow}^{\top} \begin{bmatrix} \boldsymbol{I}_{M} \\ \boldsymbol{\Sigma}_{21} \boldsymbol{\Sigma}_{1}^{-1} \end{bmatrix} \boldsymbol{\Sigma}_{1} (\boldsymbol{\Sigma} + \boldsymbol{\Sigma}_{1})^{-1} \boldsymbol{m}, \qquad (6)$$

where $I_M \in \mathbb{R}^{M \times M}$ is the identity matrix, Σ_1 and Σ_{21} are blocks of the covariance matrix of Hf and Σ is the noise covariance, which can be estimated as detailed in [21]. While the denoised completion operator \mathcal{G}_{dc} is kept fixed during training, we optimize the parameters of the convolutional neural network in a supervised manner

$$\underset{\theta}{\operatorname{argmin}} \sum_{\ell} \| \boldsymbol{f}^{(\ell)} - \boldsymbol{\mathcal{G}}_{\theta}(\boldsymbol{m}^{(\ell)}) \|^2, \tag{7}$$

where $\{f^{(\ell)} \in \mathbb{R}^N\}_{1 \le \ell \le L}$ is an image database and $\{m^{(\ell)} \in \mathbb{R}^K\}_{1 \le \ell \le L}$ are the associated measurements computed according to Eq. (1) and Eq. (3).

101 2.3. SPAS: Single-Pixel Acquisition Software

SPAS [29] is an open source python package for single-pixel acquisition, which has been been 102 tested to control a DMD 4100 (0.7" XGA VIS, VIALUX) and an AvaSpec-ULS2048CL-EVO 103 spectrometer. It therefore requires the ALP4lib [34] package for DMD control and the MSL-104 Equipment [35] package for spectrometer control. SPAS provides simple functions for the 105 initialization of the DMD and spectrometer, for the upload of a sequence of patterns into the 106 DMD memory, and for the acquisition that is triggered by an external signal provided by the 107 DMD. Each pattern is displayed on the DMD during a given illumination time and the external 108 trigger is sent to the spectrometer for synchronization. During acquisition, the spectra are stored 109 in the spectrometer's internal memory and are transferred to the computer via a callback function, 110 which allows other tasks such as image reconstruction to be run in parallel. 111

SPAS also provides several functions for the visualization of the hypercubes (e.g., spectral
slicing, spectral binning, or RGB representation based on CIE color matching functions [36]),
in addition to the implementation of a simple interface to the more advanced reconstruction
functions of the SPYRIT package (see Section 2.5).

116 2.4. SPIHIM: Single-Pixel Hyperspectral Imaging data collection

SPIHIM [26] is a FAIR [27], open-access collection of hypercubes acquired using the principle of single-pixel imaging. The collection is stored in the PILoT warehouse managed by Girder, an open source web-based data management platform. Each acquisition is associated with a uniquely identified folder which contains the raw measurements (*_spectraldata.npz), the hypercube reconstructed by inverse Hadamard transformation (*_had_reco.npz), some metadata (*_metadata.json) and an overview folder with several spatial and spectral representations of the hypercube. The metadata provide information on the experimental



Fig. 2. Acquisition system. Light source (L), sample (S), telecentric lens (TL), digital micromirror device (DMD), bi-convex lens (CL), achromatic lens pair (LP), objective lens (OL), optical fiber (OF), spectrometer (SP), and instrumentation computer (PC). The green arrows indicate the communication workflow between the computer, the DMD, and the spectrometer. The blue arrows indicate the light path.

conditions as well as on the acquisition parameters. The collection currently contains 140
hypercubes acquired from 15 different objects: "Star Sector", "Cat", "PpIX", "Color checker",
"USAF", "Colored Star Sector", "No object", "Tomato slice", "Horse", "White spot", "Thorlabs
box", "Blob", "Tree leaf", "Lamb brain", "Apple". For further details about the objects, please
see Section 1A of Supplement 1. We also provide an exhaustive list and detailed description of
the acquisitions made from these objects (see Tables S1-S15 in Supplement 1).

130 2.5. SPYRIT: Single-Pixel Reconstruction Toolkit

SPYRIT is a Python package for single-pixel image reconstruction [28] that relies on PyTorch [37] 131 and can be easily installed using the pip package management system. It implements the forward 132 model of Eq. (1), the preprocessing step of Eq. (3), and the reconstruction step of Eq. (5) 133 via classes that inherit from nn.module. This allows the full pipeline to be seen from an 134 image acquisition to its reconstruction as a neural network, in addition to full exploitation of 135 PyTorch functionalities (e.g., data loaders, network architectures, loss functions, optimizers, etc.). 136 The source code of the SPYRIT package is available on GitHub and benefits from continuous 137 integration with automated release of Python packages, dedicated benchmarks for regression 138 testing, and integrated documentation. The software is licensed under LGPL-3.0: it can be be 139 used and modified be anyone for private, public or commercial use. The SPYRIT package is 140 complemented by a companion Github repository¹ that contains script examples that rely on 141 SPYRIT. In particular, the scripts that generate the figures displayed in this manuscript and 142 Supplement 1 are available in /2022_OE_spyrit2/. 143

144 3. Experiments

145 3.1. Experimental setup

Our setup is composed of an illumination arm, a DMD, and a light collection arm as depicted
 in Fig. 2. The illumination arm is composed of a white LED lamp (Thorlabs LIUCWHA) and
 a bi-telecentric lens system (Edmund Optics TECHSPEC® Large Format Telecentric 62902,

¹https://github.com/openspyrit/spyrit-examples

magnification 0.9x) that forms the image of the object in the active plane of a DMD (ViALUX 149 GmbH DLP V-700, 1024 x 768 micromirrors, 13.7 µm pitch). The DMD is made of a matrix 150 of microscopic mirrors that can be individually tilted to either +24° (ON state) or -24° (OFF 151 state) according to spatial light patterns. The light collection arm, placed at $+24^{\circ}$ with respect 152 to the illumination arm, holds a 35 mm focal length bi-convex lens, a MAP104040-B Matched 153 Achromatic Lens Pair (both focal lengths are 40 mm), and an objective lens (x20, NA = 0.35) 154 that focuses light at the entrance of an optical fiber (1500 μ m core diameter, NA = 0.39, FT1500 155 UMT) connected to a compact spectrometer (Avantes AvaSpec-ULS2048CL-EVO, $\Lambda = 2048$ 156 spectral channels, 515–750 nm, entrance slit of 200 µm, 1200 lines/mm grating). The setup, 157 which is supported by a cage system, is lightweight and transportable. The setup depicted in 158 Fig. 2 is referred to as version v1.1 in the SPIHIM collection. The variants v1.2, v1.3 and v1.3.1 159 differ with respect to the optical elements in the illuminate and collection arms of the setup. 160 Additional details are provided in the SPIHIM collection [26]. 161

The integration time of the spectrometer is chosen as equal to the illumination time. A dead 162 time of 44 μ s, referred to as dark phase, is necessary for the DMD to tilt its micromirrors 163 according to the next pattern. Another dead time of 356 µs is necessary for the spectrometer to 164 flush its buffer and prepare a new acquisition. This leads to an acquisition time per pattern equal 165 to the spectrometer integration time plus the longest dead time. The total time for the acquisition 166 of a hypercube is $T = 2K(\Delta t + \delta t)$, where Δt represents the integration time and δt represents 167 the dead time. While the integration time can be chosen by the user, the dead time is imposed 168 by the device. Note that the dead time of the spectrometer is much longer that the smallest 169 illumination time allowed by the DMD which cannot be operated at its maximum frequency 170 $(22 \text{ kHz corresponding to } 45 \,\mu\text{s})$. Our acquisitions are typically made with an integration time 171 of 1 ms. Therefore, the fully sampled acquisition of an image of $N = 64 \times 64$ pixels requires 172 2K = 2N = 8,192 patterns × 1.4 ms ≈ 11.5 s. 173

174 3.2. Experimental data for setup characterization

For the purpose of reproducibility, we characterize the spatial and spectral resolution of the 175 setup. To do so, we consider five objects from the SPIHIM collection. To determine the spatial 176 resolution, we consider the Star Sector resolution target (Thorlabs, R1L1S2P, see top row of 177 Fig. 4) and the USAF resolution target (Edmund, USAF 1951 38256, see bottom row of Fig. 4). 178 Both samples are illuminated in transmission using a cold white LED array light source (Thorlabs, 179 LIUCWHA). To determine the spectral resolution, we consider the light spots of a Mercury-Argon 180 calibration lamp (Ocean Optics HG-1 with characteristic peaks at 546, 577, 579, 697, 707, 727, 181 and 738 nm). As a more realistic reference image, we consider the image of a cat taken from the 182 STL-10 [38] test set. The cat image is printed on a plastic sheet on which we superimpose a linear 183 variable filter (Ocean Optics, LVF-HL, see Fig. 3). Finally, we consider an image of a tomato 184 slice (see Fig. 7) to evaluate the capacity of the neural network to reconstruct the hypercube 185 as a function of the acceleration rate. A tomato slice has smooth optical contrast compared to 186 calibration targets that have high symmetry and sharp edges where reconstruction can fail for an 187 undersampled acquisition. Details about these acquisitions can be found in Supplement 1 (see 188 Tables S1, S2, S5, S7 and S8). 189

Irrespective of the imaging configuration, all the patterns of a 64×64 Hadamard basis are 190 acquired, resulting in a total of K = N = 4,096 Hadamard patterns split into 8,192 positive and 191 negative patterns. We also consider accelerated acquisitions for which K < 4,096 patterns are 192 acquired. The fully sampled datasets can be downsampled *a posteriori* to simulate an accelerated 193 acquisition with different acceleration factors. Typically, the 64×64 Hadamard patterns are 194 resized to fill the largest square region possible on the DMD, which corresponds to 768×768 195 micromirrors. In this case, each pixel of the Hadamard patterns corresponds to an area of 12×12 196 micromirrors. However, it is also possible to display the patterns on smaller fields of view, acting 197

Zoom Pixel size (µm)	×1 182.4	×2 91.2	×3 60.8	×4 45.6	×6 30.4	×12 15.2
STL-10 cat	1	n.a.	n.a.	n.a.	n.a.	n.a.
Star Sector	1	4	9	16	36	144
USAF	1	4	9	16	36	144
Mercury-Argon lamp	17.4	n.a.	n.a.	n.a.	n.a.	n.a.
Tomato slice	1	4	n.a.	n.a.	36	144

Table 1. Integration times for the different zooms and samples. Times are given in ms/pattern; 'n.a.' indicates that a dataset is not available. The corresponding images are available in Supplement 1 (see Tables S1, S2, S5, S7 and S8). Click on the integration times to access the raw data via a unique identifier.

as a hardware zoom that is independent of the optical components of the acquisition setup. We 198 consider six DMD-based hardware zooms: $\times 1$, $\times 2$, $\times 3$, $\times 4$, $\times 6$, and $\times 12$, which correspond 199 to patterns with a pixel size of 12, 6, 4, 3, 2, and 1 micromirrors, respectively. The higher the 200 zoom factor, the lower the photon counts. To obtain measurements with similar signal-to-noise 201 ratios, we chose the integration time depending on the zoom, as indicated in Table 1. For the $\times 1$ 202 zoom, we set the integration time to 1 ms/pattern for the STL-10 cat and 17.4 ms/pattern for the 203 Mercury-Argon calibration lamp. For the Star Sector and USAF targets that we image at zooms 204 $\times 1$, $\times 2$, $\times 3$, $\times 4$, $\times 6$, and $\times 12$, we choose integration times of 1, 4, 9, 16, 36, and 144 ms/pattern, 205 respectively. For the tomato slice, we choose 4 ms/pattern for $\times 2$ zoom and 144 ms/pattern for 206 ×12 zoom. 207

208 3.3. Training of the DC-Net

We train a DC-Net using SPYRIT [28] for a number of measurements of 4096, 2048, 1024, 209 and 512. In particular, we consider the L = 100,000 images that correspond to the 'test' 210 subset of the ImageNet dataset [39]. The original images are randomly cropped to 128×128 211 and are normalized between -1 and 1. The image domain denoiser \mathcal{D}_{θ} is a U-Net with three 212 downsampling steps separated by a max pooling operation and three upsampling steps separated 213 by transposed convolutions. The number of filters in the contracting path is increased from 16 to 214 32, then to 64. Each layer is separated by a ReLU and batch normalization layer. Our U-Net has 215 a total of 499,985 learnable parameters. We solve Eq. (7) using the ADAM optimizer [40], with 216 an initial learning rate of 10^{-3} , which is halved every 10 epochs, for a maximum of 30 epochs. 217 The training phase took about 300 minutes on a NVIDIA GeForce RTX 2080 Ti graphic card in 218 the case of K = 512. The DC-Nets trained for the four number of measurements are available in 219 the /soft/model/ folder of SPIHIM. They can be easily loaded and run using SPYRIT (see 220 Section 2 of Supplement 1 for a comprehensive overview of the hypercubes reconstructed for 221 different numbers of measurements). 222

223 4. Results

4.1. An acquisition example

To show the spatial and spectral capabilities of our hyperspectral camera, we first consider the STL-10 cat image with a linear variable filter in front of it. The integration time was set at 1 ms/pattern leading to a total acquisition time of 11.5 s. Figure 3 shows the obtained hypercube to which we apply spectral binning to facilitate its display. We compute seven bins within the



Fig. 3. STL-10 cat hypercube acquisition with a linear variable filter. The full hypercube is binned spectrally for display (seven bins in the range 544–670 nm, bin widths ~19 nm, central wavelengths: 553.7, 572.6, 591.1, 609.3, 627.1, 644.5, and 661.5 nm). The colorbars show intensities in counts/pixel. The image on the bottom right is an RGB representation of the full hypercube. Acquisition: K = N = 4,096 patterns, ×1 zoom, integration time of 1 ms/pattern; reconstruction by means of Eq. (4) with N = 4,096.

544-670 nm range with a bin width of ~19 nm (central wavelengths: 553.7, 572.6, 591.1, 609.3, 627.1, 644.5, and 661.5 nm). We also provide an RGB representation as recommended by the

²³¹ CIE [36]. Details about this acquisition can be found in Supplement 1 (see Table S2).

Each bin displays a different bandpass window that is selected by the linear filter. As expected, the bandpass window translates diagonally within the field of view, from the top left corner to the bottom right corner, as the central wavelength increases. This is also visible on the RGB representation that displays the color palette starting with the green color in the top left corner to the red color in the bottom right corner. The STL-10 cat is visible in the background.

237 4.2. Spatial resolution and DMD-based zoom

We evaluate the spatial resolution of our system by imaging two calibrated resolution targets: the 238 Star Sector and the USAF target. The Star Sector is composed of 36 black bars distributed around 239 360° . The USAF target is composed of bar groups with decreasing bar spacing and length. In 240 Fig. 4, we display the images obtained for both targets at four different zooms ($\times 1, \times 3, \times 6$, and 241 \times 12), after summation in the 550–590 nm range. The integration time was set at 1, 9, 36, and 242 144 ms/pattern respectively leading to a total acquisition time of 11.5, 77.0, 298.2, and 1,183.0 s 243 respectively. Details about these acquisitions can be found in Supplement 1 (see Tables S1 and 244 S5). 245

For both targets, we first establish the spatial resolution in pixels. Then, we convert it to line 246 pairs per millimeter (lp/mm) to account for the optical magnification. For the Star Sector, we 247 determine the system resolution as the smallest radius of a circular profile for which consecutive 248 black bars appear to touch. For the USAF, we determine the system resolution as the smallest 249 distinguishable bar group vertically and horizontally [41]. We also report the theoretical spatial 250 resolution computed as $1/(2\Delta x)$, where Δx is the image pixel size in millimeters. The image 251 pixel size depends linearly on the zoom, given the DMD pixel size and the telecentric lens 252 magnification. We obtain 182.4, 91.2, 60.8, 45.6, 30.4, and 15.2 μ m for $\times 1$, $\times 2$, $\times 3$, $\times 4$, $\times 6$, and 253 $\times 12$ zooms, respectively (see Table 1). 254

In Fig. 5, we plot the spatial resolution as a function of the zoom, considering six different



Fig. 4. Resolution targets acquired with different zooms. Top row: Star Sector; bottom row: USAF. Zoom increases from left to right: $\times 1$, $\times 3$, $\times 6$, and $\times 12$; K = N = 4,096 patterns; the integration time increases with the zoom: 1, 9, 36, and 144 ms/pattern, from left to right. All hypercubes are reconstructed using Eq. (4). The displayed images are obtained by summing the hypercubes in the 550-590 nm range.

zooms that correspond to six independent acquisitions. We observe that spatial resolutions
 obtained from both the USAF and Star Sector targets are in good agreement with theoretical
 values computed from the pixel size only. This indicates that our system is limited only by the
 pixel size and that the DMD-based hardware zoom is not associated with undesirable blur.

260 4.3. Spectral resolution at different locations

We evaluate the spectral resolution by imaging a Mercury-Argon calibration lamp positioned in the object plane. We place the lamp at three different positions to create light spots at different locations in the field of view and acquire a hypercube for each spot. Figure 6 shows the superposition of the three lamp spots (2K = 8,192 patterns per acquisition, integration time $\Delta t =$ 17.4 ms/pattern). Details about this acquisition can be found in Supplement 1 (see Table S7).

For all three acquisitions we observe a central bright spot corresponding to the position of the 266 light source (Fig. 6(a)). For each spot, we sum the contributions of all pixels in the respective red 267 rectangles, obtaining the spectra indicated in Fig. 6(b). For the three acquisitions, we recover a 268 spectrum that consists of the emission lines of mercury ($\lambda < 650$ nm) and argon ($\lambda > 650$ nm). 269 In the following, we consider the peaks at 546, 697, 707, 727, and 738 nm. We measure the full 270 width at half maximum of all peaks, for all spot locations, and obtain spectral resolutions between 271 2.15 nm and 2.30 nm. These spectral resolutions are in excellent agreement with the theoretical 272 spectral resolution of the spectrometer that is 2.3 nm, confirming that the spectral resolution of 273 our device is directly given by the spectral resolution of the spectrometer. We observe no spectral 274 degradation that originates from components before the spectrometer (e.g., DMD or focusing 275 optics). Note that the peak at 578 nm results from the observation of the mercury emission 276 doublet at 577 and 579 nm, which cannot be resolved. We also find that the amplitude of the 277 different peaks, except the doublet, are the same for the three spot locations, which indicates that 278 the spectral response of our system is spatially invariant. 279



Fig. 5. Spatial resolution as a function of the zoom. The red line is the theoretical resolution calculated from the pixel size; the green dots represent the resolution measured from the USAF target; the black stars represent the resolution measured from the Star Sector target. The spatial resolution is given in line pairs/millimeters (lp/mm) and evaluated from the images displayed in Fig. 4.



Fig. 6. Spectral resolution at different spatial locations in the field of view. (a) Image of a three-spot of the Mercury-Argon calibration lamp. (b) Spectra of each of the light spots indicated in (a). Integration time: 17.4 ms/pattern. The image in (a) is obtained by summing the hypercube along the spectral dimension. The spectra in (b) are obtained by summing all pixels within the red rectangles displayed in (a). These results confirm that the spectral resolution of our device is directly given by the spectral resolution of the spectral response of our system is spatially invariant.

280 4.4. Reconstructions for different values of K and N

We evaluate our ability to reconstruct images from different amounts of measurements considering 281 three samples: the Star Sector target, the USAF target, and a tomato slice. We consider the Star 282 Sector and USAF targets imaged using $\times 12$ zoom, whereas for the tomato slice, both the $\times 2$ and 283 $\times 12$ zooms were considered. Details about these acquisitions can be found in Supplement 1 284 (see Tables S1, S5 and S8). For each sample, we consider K = 4,096 measurements, K = 1.024285 measurements, and K = 512 measurements. The case K = 4,096 measurements corresponds to a 286 full basis scan with 64×64 Hadamard patterns. The cases K = 1.024 and K = 512 measurements are obtained by subsampling the full basis scan acquisition. We retain the patterns that lead to 288 the measurements with the highest energy (i.e., we chose S such that $\mathbb{E}(||SHf||_2^2)$ is maximal). 289 as suggested in [42]. We reconstruct the hypercubes in the least square sense using Eq. (4) (see 290 first column of Fig. 7) as well as with the data driven DC-Net given by Eq. (5) (see second, 291 third, and fourth columns of Fig. 7). All reconstructed images are obtained by keeping a single 292 spectral channel at $\lambda = 579$ nm. The Hadamard matrices are constructed such that the set of 293 patterns at a given resolution is included in the set of patterns at higher resolutions. For instance, 294 a full basis scan at resolution 64 (i.e., K = 4,096 measurements taken from patterns of size 295 $N = 64 \times 64$) is equivalent to an acquisition at resolution 128 (i.e., K = 16, 384 measurements 296 taken from patterns of size $N = 128 \times 128$) undersampled by a factor of four. To illustrate this, we 297 reconstruct the USAF target at resolution 64 (see second row of Fig. 7) and at resolution 128 (see 298 third row of Fig. 7). More hypercubes reconstructed at resolution 128 can be found in Section 2 299 of Supplement 1 where we consider fifteen different objects and four different spectral channels. 300 The least-squares reconstruction is independent of the choice for N and depends on K only, 301 which can be seen by comparing the first image of the second row and the first image of the third 302 row. On the other hand, the reconstruction quality of the data-driven algorithm depends on the 303 size of the images considered during the training phase. Training the DC-Net with 128×128 304 images rather than with 64×64 images improves the quality of the reconstruction significantly. 305 This can be observed by comparing the images of the second row of Fig. 7 to those of the third 306 row of Fig. 7. In particular, the bars of the elements 5 and 6 of the group 4 can be resolved in the 307 deep reconstruction, but not in the least-squares reconstruction (see the red rectangles in Fig. 7). 308 This improvement is observed even if no such piecewise-constant binary images are present in the 309 ImageNet database used for training. As expected, lowering the number of measurements leads 310 to a loss of spatial resolution, which can be evaluated from the reconstructions of the resolution 311 targets (see second, third, and fourth rows of Fig. 7). The lower the number of measurements, the 312 higher the loss. For the Star Sector, the degradation of the spatial resolution appears as a blurred 313 region in the center of the target, where high spatial frequency structures are present. We also 314 observe this effect in the tomato slice images (see fifth and sixth row of Fig. 7). However, as 315 fewer high frequencies are present, the degradation appears more limited. 316

317 5. Discussion

Images collected by hardware-driven commercial systems are relatively abundant. Among 318 the main hyperspectral databases, the AVIRIS collection (e.g., see the NASA website [43]) 319 contains thousands of hypercubes over 214 spectral channels taken from airborne platforms. 320 The BGU ICVL collection [44] currently contains 201 hypercubes over 519 spectral channels 321 corresponding to indoor and outdoor scenes taken from the ground. Very few databases offer 322 hypercubes with more than a thousand spectral bands. In contrast to existing datasets, our 323 computational device provides access to 2,048 spectral channels. Our imaging system natively 324 acquires a $64 \times 64 \times 2048$ hypercube with a spectral resolution of 2.3 nm, while the spatial 325 resolution can be adjusted between 182 µm and 15 µm using a DMD-based hardware zoom that 326 can achieve a $\times 12$ magnification with no modification of the optical components. The setup 327 characterization demonstrates that the spectral resolution is not affected by the micromirror matrix 328



Fig. 7. Image reconstructions for different samples, number of measurements, and reconstruction methods. First row: subsampling masks for $N = 128 \times 128$; second and third rows: USAF ×12 zoom; fourth row: Star Sector ×12 zoom; fifth row: tomato slice ×2 zoom; sixth row: tomato slice ×12 zoom. First column: K = 4,096 measurements, least-squares reconstruction; second column: K = 4,096 measurements, denoised completion network (DC-Net) reconstruction; third column: K = 1,024 measurements, DC-Net reconstruction; fourth column: K = 512 measurements, DC-Net reconstruction. The least-squares reconstructions are obtained using Eq. (4), while the DC-Net reconstructions are given by Eq. (5). We have set $N = 128 \times 128$ in all rows, except in the second where $N = 64 \times 64$. All images correspond to the spectral channel $\lambda = 579$ nm.

of the DMD and is equal to that of the commercial spectrometer, while the spatial resolution is approximately driven by the minimal group of micromirrors. As for the optical zoom, the higher the magnification, the lower the photon flux. To account for this effect, the images at higher zooms have been acquired for a longer duration (see Fig. 4), with a scaling factor equivalent to the zoom squared. Our system maintains a high spectral resolution for a lower price than currently available hyperspectral cameras with the same spectral resolution.

The shortest integration time that we consider is 1 ms/pattern, leading to a total acquisition 335 time of 11.5 s. As the spectrometer imposes a dead time δt of 356 µs during which no signal is 336 acquired, this represents a waste of $356/(356 + 1000) \approx 26\%$ of the total acquisition time. To 337 reduce the total acquisition time, it is possible to reduce the number of patterns 2K uploaded onto 338 the DMD. The total acquisition time of the accelerated acquisition depends directly on the number 339 of patterns (e.g., $11.5/2 \approx 5.75$ s considering only half of the patterns). This acceleration comes 340 at the cost of a spatial resolution reduction, as illustrated in Fig. 7. The acceptable acceleration 341 factor depends on the frequency content of the scene. While a 2-fold acceleration may be already 342 excessive for sharp or highly structured objects, an acceleration up to 8-fold may be acceptable 343 for smoother objects. In this study, we chose a subsampling strategy based on energy criteria; 344 however, any other subsampling strategy can be evaluated by subsampling a full acquisition a 345 posteriori. The determination of the best subset of patterns remains an open problem and the 346 subject of active research. To ease such studies, we provide several examples for reading and 347 reodering the SPIHIM measurements according to a given subsampling pattern as done in Fig. 7. 348 For the sake of generality, we have chosen to provide reconstructions where no assumptions 349 are made on the spectral content of the hypercube. Therefore, our algorithm reconstructs each 350 λ -slice of the hypercube independently using a DC-Net. We have chosen this approach for its 351 robustness to noise deviation, as underlined in [21]. However, many other data-driven approaches 352 can be considered, including approaches that exploit the spatio-spectral redundancy to jointly 353 reconstruct several λ -slices (e.g., [45]). The OpenSpyrit ecosystem could serve as a basis for a 354 more systematic comparison of the performance of these algorithms. Alternatively to the splitting 355 strategy given by Eq. (2), the patterns can be shifted to positive values. While the comparison of 356 shifting and splitting have been addressed in [31] for wavelet patterns, the question of handling 357 the negative values of Hadamard patterns remains open. The SPIHIM collection allows studies 358 to be conducted with both approaches. Indeed, shifted Hadamard patterns $\frac{1}{2}(SH+1)$ coincide 359 with the positive part of Hadamard patterns P^+ . Therefore, the SPIHIM collection includes 360 the measurements from shifted Hadamard patterns that are obtained by retaining every second 361 spectrum.

363 6. Conclusion

We propose OpenSpyrit, an ecosystem for reproducible research in hyperspectral single-pixel 364 imaging. In particular, we introduce SPAS (a Python acquisition package), SPYRIT (a Python 365 reconstruction package) and SPIHIM (a data collection), to respond to the need for reproducibility 366 and open access in single-pixel imaging. The SPIHIM collection currently contains 140 367 hypercubes that are natively $64 \times 64 \times 2048$ in size with a spectral resolution of 2.3 nm and a 368 spatial resolution that can be adjusted between 182.4 µm and 15.2 µm using a digital zoom. It also contains the hypercubes reconstructed at resolution of $128 \times 128 \times 2048$ by a data-driven 370 reconstruction algorithm. The SPIHIM dataset can be exploited for spectral imaging studies 371 in general, but also for more specific studies. In particular, the OpenSpyrit ecosystem should 372 provide a benchmark for single-pixel reconstruction algorithms. In the future, the data collection 373 is expected to continue growing and, in a similar manner, the SPYRIT package should integrate 374 novel reconstruction algorithms. 375

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- 383 **Disclosures.** The authors declare that they have no conflicts of interest.
- **Data availability.** Data underlying the results presented in this paper are available in the SPIHIM collection of the PILoT warehouse [26].
- 386 Supplemental document. See Supplement 1 for supporting content.

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