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# MASK SPOOFING IN FACE RECOGNITION AND COUNTERMEASURES

Neslihan Kose, Student Member, IEEE, Jean-Luc Dugelay, Fellow, IEEE Multimedia Department EURECOM Sophia-Antipolis France

#### Abstract

In this paper, initially, the impact of mask spoofing on face recognition is analyzed. For this purpose, one baseline technique is selected for both 2D and 3D face recognition. Next, novel countermeasures, which are based on the analysis of different shape, texture and reflectance characteristics of real faces and mask faces, are proposed to detect mask spoofing. In this paper, countermeasures are developed using both 2D data (texture images) and 3D data (3D scans) available in the mask database. The results show that each of the proposed countermeasures is successful in detecting mask spoofing, and the fusion of these countermeasures further improves the results compared to using a single countermeasure. Since there is no publicly available mask database, studies on mask spoofing are limited. This paper provides significant results by proposing novel countermeasures to protect face recognition systems against mask spoofing.

*Keywords:* spoofing, mask attacks, countermeasure, face recognition

*Email address:* neslihan.kose@eurecom.fr, jean-luc.dugelay@eurecom.fr (Neslihan Kose, *Student Member, IEEE*, Jean-Luc Dugelay, *Fellow, IEEE*)

#### 1 1. INTRODUCTION

In a spoofing attempt, a person tries to masquerade as another person and thereby, tries to gain access to recognition system. Face recognition is used in domains such as surveillance and access control. Since face data can be acquired easily in a contactless manner, spoofing is a real threat for face recognition systems.

The most common spoofing attacks are photograph and video attacks due to their convenience and low cost. Based on the observations that 2D face recognition (FR) systems are vulnerable to these attacks, researchers started to work on countermeasures to reduce their impact on recognition performances.

Proposed countermeasures against photo and video attacks are mainly 12 based on liveness detection, motion analysis and texture analysis. Counter-13 measures based on liveness detection examine movements such as eye blinking 14 [24] or lip movements [9]. In the literature, there are several countermeasures 15 based on motion analysis [4, 22]. These countermeasures rely on the fact that 16 the movement of a 2D plane is different compared to the movement of a 3D 17 object. In [4], under the assumption that the test region is a 2D plane, the 18 authors obtain a reference field from the actual optical flow field data. Then 19 the degree of differences between the two fields is used to distinguish between 20 a 3D face and a 2D photograph. In [22], a set of facial points are located auto-21 matically and their geometric invariants are used to detect attacks. The last 22

group is countermeasures based on texture analysis. In [3] and [19], images 23 are examined to find printing artifacts and blurring, respectively. In [14], dif-24 ferent contrast and texture characteristics of photographs and real faces are 25 analyzed to detect spoofing. Furthermore in [20, 21], micro-texture analysis 26 is proposed to detect 2D attacks. The study [7] includes brief information 27 about different types of 2D face countermeasures, which were developed for 28 a competition on countermeasures against 2D facial spoofing attacks. Six 29 teams participated to this competition. These teams are AMILAB, CASIA, 30 IDIAP, SIANI, UNICAMP and UOULU. All teams used one or multiple 31 clues obtained clearly from motion analysis, texture analysis and liveness 32 detection. The CASIA team presented a method with the combination of 33 motion and texture analysis techniques, and the method also allows switch-34 ing between detection schemes based on the scene context. The AMILAB 35 and the UNICAMP teams used all motion analysis, texture analysis and live-36 ness detection in deriving the detection scheme. IDIAP and UOULU used 37 texture analysis method and obtained zero percent Equal Error Rate (EER) 38 on development set and zero percent Half Total Error Rate (HTER) on test 39 set. This leads to the conclusion that, the attack videos in the database used 40 for this competition (i.e. PRINT-ATTACK Database [26]) mainly consist of 41 detectable texture patterns. 42

When 3D masks are introduced as attacks, some of the countermeasures proposed for the detection of 2D attacks are no longer applicable. The study of Kollreider et al. [13] shows that a face recognition system relying on eye <sup>46</sup> blinking and lip movements can be defeated by using photographic masks <sup>47</sup> wrapped over face with eyes and mouth regions cut out. Also, since motion <sup>48</sup> based countermeasures depend on different movements of 2D and 3D surfaces, <sup>49</sup> they are not applicable when masks are used instead of photos or videos. It <sup>50</sup> appears that the detection of 3D mask attacks is more challenging compared <sup>51</sup> to the detection of 2D facial attacks.

3D mask attacks to FR systems is a considerably new subject. The main 52 reason for the delay in mask spoofing studies is due to the unavailability of 53 public mask databases. To our knowledge, in the literature, there are two 54 countermeasure studies against 3D mask attacks [11, 29] excluding our stud-55 ies. These two studies are based on reflectance analysis. They utilize 2D data 56 (texture images) in their approach to detect 3D mask attacks. Kim et al. 57 [11] exploit the reflectance disparity based on albedo between real faces and 58 mask materials (silicon, latex or skinjell). The feature vector, which is used 59 in their approach for mask detection, consists of radiance measurements of 60 the forehead region under 850 and 685 nm illuminations. They report 97.78%61 accuracy for mask detection. In [11], the experiments are done directly on 62 the mask materials not on the real facial masks. Thus, it is not possible to 63 report spoofing performances of the masks used. The measurements are done 64 at exactly 30 cm and on the forehead region for mask detection. The require-65 ment for an exact distance and occlusion possibility in the forehead during 66 the measurements are the limitations of this method. In [29], multi-spectral 67 reflectance analysis is proposed. After measuring the albedo curves of facial 68

skin and mask materials with varying distances, two discriminative wave-69 lengths (850 and 1450 nm) are selected. Finally, a Support Vector Machine 70 (SVM) [8] classifier is used to discriminate between real and fake samples. 71 Experiments are conducted on a database of 20 masks from different materi-72 als (4 plastic, 6 silica gel, 4 paper pulp, 4 plaster and 2 sponge). The results 73 show that this method can achieve 89.18% accuracy. The superiorities of 74 [29] compared to [11] are the elimination of range limitation and the usage 75 of real facial masks. However, spoofing performances of the masks are still 76 not reported. In order to contribute to this compelling research problem and 77 fill the missing portions of the existing studies, we have proposed several 78 countermeasure techniques against 3D mask attacks in [15], [18] and [17]. 79

The spoofing performances of the masks used and the countermeasure 80 which uses 3D data (3D scan) instead of 2D data (texture image) as input 81 to detect mask spoofing were first analyzed in our previous studies [16, 15], 82 respectively, using the mask database which was prepared within the context 83 of the European Union (EU) research project TABULA RASA [28]. The 84 mask database used in the present study and our previous studies [15, 16,85 18, 17] was created by MORPHO [23]. This database includes many high-86 quality mask samples. It consists of 3D masks of 16 real subjects. The scans 87 of subjects were acquired by a 3D scanner, and the masks were manufactured 88 using a 3D printer. In addition to texture images, it includes 3D scans for 89 both real and mask samples. Thanks to the nature of this database, we 90 were able to evaluate the impact of mask spoofing on both 2D and 3D face 91

<sup>92</sup> recognition, and to develop our countermeasures using both 2D and 3D data.

If a 3D mask is not able to spoof a recognition system, it is not a suc-93 cessful attack, and there is no need to develop a countermeasure against it. 94 Therefore, in [16], we analyzed how well the spoofing performances of the 95 masks used in our studies are. The results of this study show that the masks 96 used have very similar texture and especially 3D face shape characteristics to 97 their target faces. They are very successful to spoof face recognition systems. 98 To the best of our knowledge, spoofing performances of the masks used were 99 the first to be analyzed in this study. In [15], we proposed to apply micro-100 texture analysis on both texture and depth images, and obtained 88.12%101 and 86% accuracy, respectively, for the classification of mask and real faces. 102 The novelty of this work is that it was the first time 3D data was utilized 103 to discriminate mask and real samples. In our next study [18], which is the 104 continuation of [15], we studied fusing the information extracted from both 105 the texture and depth images, and obtained a higher classification accuracy 106 of 93.5%. In addition to the increase in performance, it was the first time the 107 performances of face recognition systems were analyzed with/without mask 108 attacks and with/without the proposed countermeasure integrated to the 109 recognition systems in [18]. By this way, it is possible to observe the positive 110 impact of countermeasure on recognition performances in presence of mask 111 attacks. Finally, in [17], we proposed a countermeasure based on reflectance 112 analysis using the texture images in the same database. We obtained 94%113 classification accuracy in [17], which was the best score we had obtained so 114

115 far.

In this paper, after showing the impact of attacks on the selected recog-116 nition systems; we provide an overview on our spoofing detection approaches 117 which were introduced in the studies [15], [18] and [17]. We extend the 118 works explained in these studies with some improvements, additional analy-119 sis, comparisons of performances of diverse countermeasures using the same 120 protocol, and with a detailed analysis of the fusion scenarios. Additionally, a 121 novel countermeasure is proposed in the present paper. In [15], micro-texture 122 analysis is applied on texture images, whereas in this paper, we apply micro-123 texture analysis on reflectance components of texture images as a new coun-124 termeasure. We observe that higher accuracy is obtained using reflectance 125 component instead of texture image (original image) itself. This proves that 126 reflectance image provides more appropriate information than original im-127 age to discriminate mask and real samples. In the present study, we obtain 128 98.99% classification accuracy, which is the best accuracy that have been re-129 ported in the literature for mask spoofing detection up to now. Also, in the 130 present paper, we integrate the countermeasure with the best performance 131 to the selected 3D FR system in order to show the positive impact of the 132 countermeasure on the system under mask attacks, directly. 133

The paper is organized as follows: Section 2 gives brief information on the mask database which is used in this study. Section 3 presents the selected 2D and 3D FR systems, and then evaluates the impact of mask spoofing on these systems. Section 4 gives brief information about the techniques that were used to develop the proposed countermeasures. Section 5 explains each of
the proposed countermeasures. Section 6 shows the experiments and results
of all the proposed countermeasures together with the fusion scenarios for
comparison purposes. Finally, conclusions are provided in Section 7.

#### 142 2. THE MASK DATABASE

A mask used for 3D face spoofing purposes has to show very similar 143 3D shape characteristics to the target face to be considered as a successful 144 attack. The mask database used in this study was prepared to fulfill this 145 objective. Initially, scans of the subjects in the mask database were taken 146 by a 3D scanner which uses a structured light technology in order to obtain 147 similar face shape characteristics to the target person. Then the 3D model 148 (3D mesh) of each subject was sent to a 3D printer and the masks were 149 manufactured by Sculpteo 3D Printing [27]. The material used for the masks 150 is polychrome mineral powder, which is a 3D printing standard. 151

The mask database is 2D+3D. For the sake of clarity, the database of real faces in 2D and 3D will be referred as DB-r2 and DB-r3, while the database of mask attacks will be referred as DB-m2 and DB-m3 in the rest of this paper.

In the mask database, 20 subjects appear in total. The masks were manufactured for 16 of these subjects. For DB-r, an average of 10 scans of each subject were acquired. For DB-m, an average of 10 scans of each subject wearing either his/her own mask or masks of the other subjects that



Figure 1: Example from the mask database which is created by [23]. From left to right (upper row) The real face, the cropped texture image, the 3D scan after preprocessing, the cropped depth map estimated from the raw 3D scan (lower row) same images for the corresponding mask attack.

appear in the same database were acquired. Finally, 200 real face acquisitions
from 20 subjects and 198 mask acquisitions from 16 masks are used for the
evaluations of this study. Figure 1 shows one example from this database for
a real face access and the corresponding mask attack access.

In the mask database, DB-r and DB-m are partitioned in train and test 164 sets. 8 subjects out of 16 subjects whose masks are manufactured, and 2 165 subjects out of 4 subjects whose masks are not manufactured are selected 166 for DB-r. The samples of the selected subjects are assigned to the test set of 167 DB-r, while the rest is used for the train set of DB-r. For DB-m, the mask 168 attack accesses to the corresponding identities in the test set of DB-r are 169 involved in the test set of DB-m, while the rest is used for the train set of 170 DB-m. There is no overlap between the train and test sets, which makes the 171 spoofing detection more challenging. Finally, there are 100 samples in each 172 of the client (real accesses) test and train sets, and 99 samples in each of the 173

<sup>174</sup> impostor (mask attack accesses) test and train sets.

## 175 3. IMPACT ANALYSIS OF MASK SPOOFING ON FACE RECOG 176 NITION

In this section, initially, we explain the pre-processing applied for the selected 3D and 2D FR techniques. Next, we give the details about these recognition techniques. Finally, we evaluate the impact of spoofing mask attacks on both 3D and 2D face recognition.

#### <sup>181</sup> 3.1. Pre-Processing for the Selected Face Recognition Systems

The pre-processing for the selected 3D FR system is based on the method 182 given in [10]. In order to crop the face region, the tip of the nose is detected. 183 and the facial surface is cropped by a sphere with radius 80 mm, centered 10 184 mm away from the nose tip in +z direction. Note that the face looks towards 185 +z direction. Next, the spikes are removed by thresholding, and then a hole 186 filling procedure is applied. Finally, a bilateral smoothing filter is used to 187 remove white noise while preserving edges. These pre-processed 3D scans 188 (only shape, without texture) are used as input for 3D face recognition. 189

For 2D face recognition, the texture images in the mask database are cropped as shown in Figure 1, and resized into 64 × 64 images. In this study, we aim to show first how vulnerable the systems are to spoofing mask attacks by evaluating the performances of the selected systems with/without attacks, and then how a countermeasure improves the performance in presence of mask attacks by evaluating the performances of these systems with/without countermeasure. For micro-texture analysis applied inside the proposed countermeasures, which is explained in Section 4, images are resized into  $64 \times 64$  as proposed in [20]. Thus, although this resizing parameter may reduce the baseline performance in 2D, since our aim in this study is not to report high baseline performance, we preferred to use the same images as input for both the 2D baseline evaluation and proposed countermeasures.

Figure 1 shows an example for the texture images and 3D scans which are used in 2D and 3D evaluations, respectively.

#### <sup>204</sup> 3.2. Selected Face Recognition Systems

The 3D FR system selected as baseline for this study is introduced in [10]. 205 It is also selected as baseline system in TABULA RASA project [28]. It uses 206 the pre-processed 3D mesh of the face as input. Three landmark points are 207 previously annotated at the nose tip and outer eye corners for each sample 208 in the database. Initially, a linear transformation is computed in a least 209 squares sense (LSS), based on two sets of landmarks (landmarks of generic 210 model and subject's face). Least squares means that the overall solution 211 minimizes the sum of the squares of the errors made in the results of every 212 single equation. The best fit in the LSS here is calculated by minimizing 213 the squared distance between the point sets of generic model and subject's 214 face. For this purpose, the obtained transformation that includes rotation, 215 translation and isotropic scaling is applied onto the generic model, aligning it 216

with the subject's face. Next, the alignment is further improved by Iterative 217 Closest Point (ICP) method [5]. Afterwards, 140 previously selected points 218 on the generic model are coupled with the closest vertices on the face under 219 analysis, and Thin Plate Spline (TPS) [6] warping is applied on the generic 220 model resulting in warping parameters (WP) of size  $140 \times 3$ . WPs that 221 represent the deviations from the common structure are given to the classifier 222 for recognition. Finally, the distance between two face models is computed 223 by taking the median of cosine distances between the corresponding feature 224 vectors (WP), and recognition rates are computed. Figure 2 shows the feature 225 extraction scheme on a sample model using this method, which is named WP. 226



Figure 2: The feature extraction scheme and an illustration on a sample model: (a) The subject's face with and without texture (b) generic model before and after alignment (c) generic model after warping with and without texture. This figure is taken from [10].

For 2D face recognition, Local Binary Patterns (LBP) [1] is selected as 227 baseline. The success of LBP in face description is due to the discriminative 228 power, computational simplicity of the operator, and its robustness to mono-229 tonic gray scale changes caused by, for example, illumination variations. The 230 use of histograms as features also makes the LBP approach robust to face 231 misalignment and pose variations to some extent. For 2D FR, we use the 232 operator  $LBP^{u2}_{8,2}$  on  $8 \times 8$  blocks. The similarity between each image pair is 233 computed with chi-square distance metric. Performances are evaluated using 234 the similarity scores between image pairs. 235

#### 236 3.2.1. Evaluation on 2D and 3D Face Recognition

In this part, the evaluations are done for 2 modes. The first mode is 237 the baseline mode: a standard biometric system with no spoofing and no 238 countermeasure. The baseline performance is evaluated using DB-r. Perfor-239 mance is evaluated by verification all vs. all. Access from every identity in 240 DB-r is tested against all other models in DB-r. The performance is mea-241 sured by observing the rate of users rejected when authenticating against 242 their own template (False Rejection Rate - FRR) and by the rate of users 243 accepted when authenticating against someone else's template (False Accep-244 tance Rate - FAR). The second mode is the evaluation of FR systems under 245 mask attacks (baseline under attacks in Figure 3). Both DB-r and DB-m 246 are used. When spoofing attacks are applied, performance is expected to 247 degrade. In this mode, the FAR corresponds to the rate of attacks that are 248

accepted by the system when spoofed. The FRR corresponds to the rate of 249 real-access attempts that are incorrectly dismissed by the system as attacks. 250 For the evaluations regarding 2D and 3D FR systems here, only test set 251 is used. Train set is used for classifier training inside the proposed counter-252 measures. Figure 3 shows the behavior of the 3D and 2D baseline systems 253 with/without attacks. All results are presented in terms of detection error 254 trade-of (DET) profiles which illustrate the behavior of a system as the de-255 cision threshold is changed, i.e. how the false rejection rate varies according 256 to the false acceptance rate. 257



Figure 3: The DET Curves of the 3D and 2D face baseline biometric system with/without mask attacks, respectively.

#### <sup>258</sup> Figure 3 shows that:

• Although the mask attacks are successful to spoof both 2D and 3D FR systems, the 3D FR system is more vulnerable to mask attacks compared to the 2D FR system (area between red and blue curves is <sup>262</sup> much more for 3D compared to 2D FR system).

- Equal Error Rate (EER) at the baseline mode increases from 1.8% to 25.1% for 3D and from 4.7% to 9.9% for 2D FR system under attacks.
  3D shape characteristics of a real face and corresponding mask attack are more similar compared to their texture characteristics. Hence, analysis on texture may reveal more information to detect mask attacks compared to analysis on 3D shape characteristic.
- Robustness against mask spoofing is observed to be both method and modality dependent as also concluded in [16].
- FR systems are vulnerable to spoofing mask attacks hence, countermeasures are necessary to reduce their impact on face recognition.

For the baseline mode evaluations, we used the test set of DB-r, which 273 contains 100 real samples from 10 subjects. In this study, we also report 274 the baseline performances of the selected systems on the Face Recognition 275 Grand Challenge Database (FRGC) v1.0 [25] database in order to check 276 if the selected systems still provide satisfactory baseline performances with 277 more number of subjects. The scans of the subjects in the mask database 278 were acquired with a high quality laser scanner (technology of MORPHO). 279 The FRGC database was also prepared using the high quality laser scanner 280 Minolta. Therefore, the scan quality in the FRGC is quite similar to the scan 281 quality in our mask database. Furthermore, FRGC v1.0 includes 943 samples 282

from 275 subjects and more challenging compared to the DB-r of the mask database. Table 1 shows the EER, verification rate at 0.001 FAR and rank-1 identification rates computed with the selected systems using both the mask database (the DB-r of the mask database) and the FRGC database.

3D and 2D baseline systems using the Mask Database (MD) and the FRGC Database. Techniques WP LBP (MD) (FRGC) (MD) (FRGC) EER (%) 1.79 2.41 4.68 2.96

Table 1: EER, Verification Rate at 0.001 FAR and Rank-1 Identification Rate (IR) for the

	$\overline{VR}$ at 0.0	001 FAR (%)	91.33	3 87.70	90.89	90.03	
	IR (%)		100	94.01	98.89	9 94.50	
							=
1	Table 1 shows	that slightly	better	performan	nces are o	obtained in	terms
1			• • • • •		. 1	1 /	.1

of 287 identification and verification using the mask database compared to the ones 288 obtained using the FRGC. For each FR technique, EER computed for the two 289 databases are quite similar. Although there is a high increase in the number 290 of subjects/samples when the FRGC is used for the evaluation, the perfor-291 mances of the selected baseline systems on the FRGC are still satisfactory, 292 even quite similar to the results obtained using the mask database. These 293 results show that the selected systems provide significant performances hence 294 they are appropriate for this study, and the number of subjects/samples in 295 the mask database is sufficient enough to obtain consistent results in this 296 study. 297

## 4. TECHNIQUES USED INSIDE THE PROPOSED COUNTER MEASURES

Mask attack is a 3D attack that can be used to spoof both 2D and 3D 300 FR systems. Most of the existing 3D scanners do not provide only 3D scan, 301 they also capture texture image. Figure 1 shows an example for the two 302 outputs of a scanner. Thus, when there is only one camera for 2D and one 303 scanner for 3D FR system, a countermeasure which uses texture images as 304 input can be used to protect both 2D and 3D FR systems if texture images 305 are provided as default output of a scanner. In the present study, we propose 306 four countermeasures against 3D mask attacks, which use either the depth 307 maps or texture images as input (Figure 5). 308

In this section, we first explain the pre-processing applied for the proposed countermeasures. Then, we give a detailed information about the techniques that were used to develop the proposed countermeasures.

#### 312 4.1. Pre-Processing for the Countermeasures

There are slight alignment differences between faces in the mask database. For the countermeasures, initially, all 3D faces in DB-r3 and DB-m3 are aligned to a generic face using LSS alignment, which makes the alignment of all faces identical.

In this study, we want to benefit from the information that the mask surface is smoother than the real face surface to detect mask attacks. Therefore, the depth maps are estimated from the raw aligned 3D scans. Next, 2D cropping is applied to extract face region from both the texture images and depth maps. Then all images are resized into  $64 \times 64$  grayscale image.

In our previous studies [15, 17], we used normalized images. We notice 322 that normalization has a positive impact in performances when the counter-323 measure is applied on depth maps, whereas it reduces performances slightly 324 when applied on texture images. In the present paper, we did not apply nor-325 malization, and we improved our cropping code compared to the ones used 326 in our previous studies. The final version of the texture images and depth 327 maps used for the proposed countermeasures are shown in the second and 328 fourth columns of Figure 1, respectively. 329

#### 330 4.2. The Variational Retinex Algorithm

In the present paper, the image is decomposed into reflectance and illumination components using the variational retinex algorithm explained in the studies [2, 12].

In this subsection, we first give information about minimizing energy functions. Then, we explain the variational retinex algorithm [2, 12].

#### 336 4.2.1. Minimizing Energy Functions

The concept of minimizing the energy of a given system is used in image processing. Minimizing energy functions often includes solving partial differential equations, more specifically, Euler-Lagrange differential equations.

In the Euler-Lagrange problem, we usually have a continuous real-valued function y = f(x) with continuous derivative y' = df/dx. Considering x, y, y and y' as three independent variables, a new function g(x, y, y') is defined. Using this function, the energy function is defined as:  $E = \int g(x, y, y') dx$ . The energy function E has a minimal value if Euler-Lagrange equation:

$$\frac{\partial g}{\partial y} - \frac{\partial}{\partial x} \left( \frac{\partial g}{\partial y'} \right) = 0 \tag{1}$$

is satisfied. The left hand side of this equation is denoted as  $\nabla E$ . Here f is introduced as a function of one independent variable x, the same concept is applied when f is a function of n independent variables:  $x1, x2, \ldots, xn$ . In particular, when u = f(x, y), function of two independent variables x and y, Euler- Lagrange equation becomes:

$$\nabla E = \frac{\partial g}{\partial u} - \frac{\partial}{\partial x} \left( \frac{\partial g}{\partial u_x} \right) - \frac{\partial}{\partial y} \left( \frac{\partial g}{\partial u_y} \right) = 0 \tag{2}$$

The variational retinex algorithm is developed by defining and minimizing an energy function.

#### 352 4.2.2. The Variational Retinex Algorithm

An image can be considered as a two dimensional function S(x, y), where (x, y) denotes a pixel on the image. The value of the function S = S(x, y)represents the intensity of the light at the pixel (x, y). As stated in [2], the intensity S may be characterized by two components which are;

• the amount of source illumination falling on the object, the illumination component L(x, y). • the amount of illumination reflected by the object, the reflectance component R(x, y).

S(x, y) is computed using the illumination and reflectance components as shown in Eq. (3).

$$S(x,y) = L(x,y) \times R(x,y)$$
(3)

In [2], it is stated that if images are assumed to be composed of illumination and reflectance components, generating the retinex effect means being able to separate one component from another. A first step taken by most algorithms in such sort of problems is the conversion to the logarithmic domain by s = log(S), l = log(L), and r = log(R). In the logarithmic domain the relation between these three images becomes: s = l + r.

In [12], Kimmel et al. make the following assumptions:

#### 1. The logarithmic illumination l varies spatially smoothly.

2. The logarithmic reflectance r consists of constant or smooth parts and discontinuous jump parts.

373 3. *l* is greater than or equal to the logarithmic intensity  $s \ (l \ge s)$ .

4. l is close to s (i.e. l does not deviate far away from s).

Based on the assumptions listed above, in the studies [2, 12], the energy function is defined as follows:

$$E(l) = \int (|\nabla l|^2 + \alpha (l-s)^2 + \beta |\nabla (l-s)|^2) dx dy$$
 (4)

where  $\alpha$  and  $\beta$  are positive constants. Since S is the given image, s here is constant. In this equation;

• The first penalty term 
$$(|\nabla l|^2)$$
 forces spatial smoothness on  $l$ .

- The second penalty term  $(l s)^2$  forces a proximity between l and s. The difference between these images is exactly r, which means that the norm of r should be small. Simultaneously, it forces the solution l to be  $l \ge s$ . In [12], it is stated that in practice this term should be weak enough not to attract l down too much towards s. This is why the parameter  $\alpha$  should be very small.
- The third term forces r to be spatially smooth. In [12], it is stated that the parameter  $\beta$  should be a very small value to preserve the discontinuous jumps of r. Note that spatially smooth r contradicts spatially smooth l since r + l = s. However in practice adding this penalty term kicks in mainly on sharp edges and handles situations where the illumination is not smooth (as well as cases of direct light sources and specularities).
- <sup>393</sup> The integrand of this energy function is:

$$g(l, l_x, l_y) = |\nabla l|^2 + \alpha (l - s)^2 + \beta |\nabla (l - s)|^2$$
  
=  $(l_x^2 + l_y^2) + \alpha (l - s)^2 + \beta ((l_x - s_x)^2 + (l_y - s_y)^2)$  (5)

<sup>394</sup> Euler-Lagrange equation becomes:

$$\nabla E = \frac{\partial g}{\partial l} - \frac{\partial}{\partial x} \left( \frac{\partial g}{\partial l_x} \right) - \frac{\partial g}{\partial y} \left( \frac{\partial g}{\partial l_y} \right)$$
  
=  $2\alpha(l-s) - \frac{\partial}{\partial x} \left( 2l_x + 2\beta(l_x - s_x) \right) - \frac{\partial}{\partial y} \left( 2l_y + 2\beta(l_y - s_y) \right)$   
=  $2\alpha(l-s) - 2l_{xx} - 2\beta(l_{xx} - s_{xx}) - 2l_{yy} - 2\beta(l_{yy} - s_{yy})$   
=  $2 \left[ \alpha(l-s) - \Delta l - \beta \Delta(l-s) \right]$   
=  $0$  (6)

which means  $\alpha(l-s) - \Delta l - \beta \Delta(l-s) = 0$ . In [2], to solve this equation, the idea of the steepest descent is applied with an auxiliary variable t:

$$\frac{dl}{dt} = -\nabla E = \Delta l + \beta \Delta (l-s) - \alpha (l-s)$$
(7)

To find a local minimum of a function using steepest descent, one takes steps proportional to the negative of the gradient of the function at the current point. In our evaluation, l is computed via steepest descent as follows:

$$l_n = l_{n-1} - dt \cdot \nabla E \tag{8}$$

Finally, projecting onto the constraint  $l \ge s$  is done by  $l_n = max(l_n, s)$ .

In our experiments, the values 0.0001 and 0.1 are used for  $\alpha$  and  $\beta$ , respectively, as suggested in [2, 12]. The initial value of l ( $l_0$ ) is taken as s. The step size dt and the total number of iterations are selected as 0.05 and 5000, respectively. After the iterations, optimum l is obtained, and r is computed from r = s - l. Finally, the reflectance and illumination components are evaluated from  $R = e^r$  and  $L = e^l$ , respectively.



Figure 4: Example from the mask database which is created by [23] (a) The real face with texture, the reflectance image and the illumination image of the real face (b) Same images associated with the mask of the same person.

Figure 4 shows an example from the mask database for a real face and corresponding mask attack. First column shows the original images, second column and third column show the reflectance and illumination images, respectively, which are computed using the variational retinex algorithm.

#### 411 4.3. Micro-Texture Analysis Technique

The micro-texture analysis, which was first proposed in [20] to detect 2D face attacks, is used to detect 3D mask attacks here. In [20], it is applied on texture images, whereas in this paper, we apply this technique not only on texture images but also on depth maps estimated from 3D scans and on reflectance components of texture images.

This LBP based micro-texture analysis technique emphasizes the micro-417 texture differences in the feature space. It aims at learning the differences 418 between real and fake face, and designs a feature space which emphasizes 419 those differences. The original LBP forms labels for the image pixels by 420 thresholding the  $3 \times 3$  neighborhood of each pixel with the center value and 421 considering the result as a binary number. The LBP operator has been 422 extended to use neighborhoods of different sizes.  $LBP_{P,R}$  is computed such 423 that for a given central pixel in an image, a pattern number is computed by 424 comparing its value with those of its neighbors. In Eq. (9),  $g_c$  is the gray 425 value of the central pixel,  $g_p$  is the value of its neighbors, P is the number of 426 neighbors around a circle of radius R.  $LBP_{P,R}$  calculation is shown in Eq. 427 (9) and (10): 428

$$LBP_{P,R} = \sum_{p=0}^{P-1} s(g_p - g_c)2^p$$
(9)

429

$$s(x) = \begin{cases} 1, & x \ge 0\\ 0, & x < 0 \end{cases}$$
(10)

Uniform patterns are verified to be the fundamental patterns of local image texture. A local binary pattern is called uniform if the binary pattern contains at most two bitwise transitions from 0 to 1 or vice versa when the bit pattern is traversed circularly. The notation is  $LBP_{P,R}^{u2}$ . u2 stands for using only uniform patterns and labeling all remaining patterns with a single 435 label.

In [20], authors claim that micro-texture details that are needed to dis-436 criminate a real face from face print can best be detected using combination 437 of different LBP operators. Thus, they derive an enhanced facial repre-438 sentation using multi-scale LBP operators. Their proposed representation 439 computes LBP features from  $3 \times 3$  overlapping regions to capture the spatial 440 information and enhances the holistic description by including global LBP 441 histograms computed over the whole image. This is done as follows: the face 442 is cropped and resized into a  $64\times 64$  pixel image. Then,  $LBP^{u2}_{8,1}$  operator is 443 applied on the face image and the resulting LBP image is divided into  $3 \times 3$ 444 overlapping regions (with an overlapping size of 14 pixels). The local 59-bin 445 histograms from each region are computed and collected into a single 531-bin 446 histogram. Then, two other histograms are computed from the whole face 447 image using  $LBP^{u2}_{8,2}$  and  $LBP^{u2}_{16,2}$  operators, yielding 59-bin and 243-bin his-448 tograms that are added to the 531-bin histogram previously computed. In 449 [20], the length of the final enhanced feature histogram is reported as 833 450 (i.e. 531 + 59 + 243). 451

#### 452 4.4. Classification Technique

Mask face detection is a two-class classification problem. Since SVM [8] are proven to be a powerful tool for discriminating two classes of data, we adopted an SVM classifier for this purpose. SVM finds the maximum margin hyper-plane to separate the training data in feature space and a decision for  $_{457}$  a new test data x is classified. In our experiments, we adopted linear kernel  $_{458}$  since our feature vectors are high-dimensional and are hence likely to be  $_{459}$  linear separable.

#### 460 5. THE PROPOSED COUNTERMEASURES

Four countermeasures are proposed in this study to discriminate mask and real samples. Three of them use the 2D data (texture images), and the remaining one uses the 3D data (depth maps estimated from the raw 3D scans) available in the mask database as input.



Figure 5: The flowchart of the proposed countermeasures.

The flowchart of the countermeasures proposed in this paper are shown in Figure 5. In this figure, the micro-texture analysis (explained in Subsection 467 4.3) applied on texture images is called CM1, applied on reflectance images is called CM2, applied on depth maps is called CM4, and finally the countermeasure for which the pixel intensity values on reflectance images are used
directly by the classifier is called CM3 (CM denotes countermeasure).

CM1 and CM4 are first introduced in our study [15], and CM3 is first 471 introduced in our study [17]. In the present paper, we provide an overview on 472 our spoofing detection approaches introduced in the studies [15, 17]. We ex-473 tend the works explained in these studies with some improvements (e.g. bet-474 ter cropping, usage of non-normalized images instead of normalized images), 475 additional analysis, comparisons of performances of diverse countermeasures 476 using the same protocol, and with a detailed analysis of the fusion scenarios. 477 Also, CM2 is first introduced in the present paper. It is a new counter-478 measure providing very satisfactory accuracy to classify mask and real faces. 479 The results of CM2 show that reflectance component of an image provides 480 more appropriate information than original image itself for mask detection. 481 From the fusion results, we also observed that it provides complementary 482 information on mask detection. 483

#### 484 5.1. CM1: Micro-Texture Analysis on Texture Images

Captured image from mask may visually look very similar to the image captured from live face (e.g. the texture images in the first column of Figure 4). A close look at the differences between faces in DB-r2 and DB-m2 reveals that their surface properties are different. For mask manufacturing 3D printers are used, hence they may contain printing quality defects that can be detected with micro-texture patterns. For CM1, micro-texture analysis is applied on texture images, and the feature histogram of length 833 is
obtained. Finally, linear SVM classifier is applied to detect mask and real
faces.

#### 494 5.2. CM2: Micro-Texture Analysis on Reflectance Images

For CM2, initially, the illumination and reflectance components (Figure 495 5) of the texture images are obtained using the variational retinex algorithm 496 introduced in Subsection 4.2. Then, micro-texture analysis is applied on 497 reflectance components of texture images rather than texture images itself. 498 The reason of this analysis on reflectance images is that a close look at the 499 differences between the reflectance images of the real and mask faces reveals 500 that the texture characteristics on their reflectance components are also dif-501 ferent. The feature vectors of length 833, which are obtained by applying 502 micro-texture analysis on reflectance images, are used as input by linear SVM 503 classifier. This feature vector gives information from the reflectance image 504 in the image texture level. 505

#### 506 5.3. CM3: Pixel Intensity Analysis on Reflectance Images

<sup>507</sup> Our observations on the reflectance components of mask and real faces <sup>508</sup> reveal that reflectance characteristics of mask and real face samples are dif-<sup>509</sup> ferent especially at some specific regions of the face (eyelashes, eyebrows and <sup>510</sup> moustache). Based on these observations, in this study, we use the intensity values on reflectance component of each image as input for linear SVM classifier. Since the intensity values on reflectance images are between 0 and 1  $(R(x, y) \in [0, 1])$ , we stretched it to the interval [0, 255] by multiplying Rwith 255. The reflectance component, which is in the size of 64 × 64 pixel image, is reshaped as [1 4096] (64 × 64 = 4096). The resultant vector is the feature vector providing information in the pixel intensity level. Finally, linear SVM classifier is applied to detect real and mask faces.

#### 518 5.4. CM4: Micro-Texture Analysis on Depth Maps

The 3D shape of high quality mask is also very similar to the 3D shape 519 of corresponding real face (e.g. the 3D scans in the second column of Figure 520 1). Our analysis on DB-r3 and DB-m3 show that the mask scan is smoother 521 than the real face scan. Especially the parts of the face with facial hair are 522 quite different. Since there is no real facial hair (e.g. mustache, eyebrow) on 523 the masks, the 3D scan of mask is smoother in these parts compared to the 524 real face scan. When high quality scanners are used for acquisition, although 525 there is a decrease in the number of holes, it is still possible to observe some 526 holes on the scan especially at the parts of the face with facial hair. Thus, in 527 our study, micro-texture analysis is also applied on the depth maps which are 528 estimated from the raw 3D scans, and the other feature histogram of length 529 833 is obtained. Finally, linear SVM classifier is applied to detect real and 530 mask faces. 531

#### 532 6. EXPERIMENTS AND RESULTS

In this section, we first show the stand-alone classification performances of the proposed countermeasures together with the fusion scenarios. Then, we integrate the countermeasure providing the best performance to the selected 3D FR system in order to observe the improvement in the recognition performance of the system in presence of mask attacks.

#### 538 6.1. Stand-Alone Classification Performances of the Countermeasures

In the present study, we apply the proposed countermeasures (CM1, CM2, CM3, CM4) using the same database with the same train-test sets, hence an exact comparison between these countermeasures is possible. Train set is used for classifier training. This classifier is subject to two kind of errors:

- FLR (False Living Rate), that represents the percentage of fake data misclassified as real. (similar to FAR)
- FFR (False Fake Rate), which computes the percentage of real data assigned to the fake class. (similar to FRR)

The lower these two errors, the better the performance of the countermeasures. In this section, we first evaluate the performances of the single countermeasures, and then evaluate the performances for the fusion scenarios. The Region of Convergence (ROC) curves in Figure 6 shows the standalone classification performances of the four countermeasures together with the fusion based countermeasure providing the best performance in Table 3.



Figure 6: The Classification Performances of the Countermeasures.

Area Under Curve (AUC), EER and best accuracy results using CM1, CM2, CM3, and CM4 are shown in Table 2.

Countermeasures	AUC	$\operatorname{EER}(\%)$	Accuracy(%)
CM1	0.956	9.04	91.46
CM2	0.980	5.02	95.98
CM3	0.984	9.04	93.47
CM4	0.919	18.59	82.91

Table 2: AUC, EER and Accuracy Results Using the Four Countermeasures

Table 2 and Figure 6 show that;

• The best performances in terms of EER and accuracy are obtained using CM2, and the best performance in terms of AUC is obtained using CM3. • The best performances are obtained with the countermeasures based on reflectance analysis (CM2 and CM3) compared to the performances obtained with CM1 and CM4. This shows that reflectance characteristics of the real and mask faces in the mask database provide more appropriate information than their texture and smoothness characteristics.

- CM4, which is based on smoothness analysis, provides worse results compared to the other countermeasures. However, the performance of CM4 can be still considered as satisfactory.
- 2D data (texture images) provide more information than 3D data (depth maps) to detect mask spoofing.

After evaluating the performances of the single countermeasures, we analyze the performances for the fusion scenarios.

For feature level fusion, the feature histograms computed from different 572 types of images (texture, reflectance and depth) are concatenated and the 573 classifier is applied on the resultant feature histogram. In Table 3, the fea-574 ture level fusion of 2 countermeasures, 3 countermeasures and finally all the 575 4 countermeasures are reported for which the length of the final feature his-576 tograms are 1666, 2499 and 3332, respectively. Once the enhanced histogram 577 is computed, a linear SVM classifier is used to determine whether the image 578 corresponds to a live face or not. 579

For score level fusion, linear SVM classifier is applied using the features computed from each type of images (texture, reflectance and depth) separately, and then Z-score normalization is applied for each score group. Finally, the weighted score level fusion is used for combining the outputs of the individual SVMs to determine whether the image corresponds to a live face or not.

AUC, EER and best accuracy results are shown in Table 3 for the fusion scenarios.

Countermeasures	Featur	e Level	Fusion	Score Level Fusion		
Involved in Fusion	AUC	EER	Acc.	AUC	EER	Acc.
		(%)	(%)		(%)	(%)
CM1, CM2	0.994	3.01	97.49	0.988	3.01	97.49
CM1, CM3	0.985	9.04	93.97	0.993	5.02	96.48
CM1, CM4	0.972	9.04	92.96	0.976	8.04	94.47
CM2, CM3	0.984	9.04	93.47	0.993	5.02	96.48
CM2, CM4	0.994	3.01	97.49	0.992	4.02	96.98
CM3, CM4	0.986	8.04	92.96	0.994	5.02	95.98
CM1, CM2, CM3	0.985	9.04	93.47	0.998	2.01	98.99
CM1, CM2, CM4	0.998	2.01	97.99	0.993	5.02	96.48
CM1, CM3, CM4	0.987	8.04	93.47	0.997	2.01	97.99
CM2, CM3, CM4	0.986	8.04	93.47	0.997	2.00	98.49
CM1, CM2, CM3, CM4	0.987	8.04	93.47	0.997	2.01	98.49

Table 3: AUC, EER and Accuracy Results for the Fusion Scenarios of the Proposed Countermeasures

<sup>588</sup> From the reported results in Table 3, we can remark the followings:

Both score and feature level fusion of the countermeasures improve the
 performance compared to using single countermeasure. For instance,
 CM4 provides a detection accuracy of 82.9% whereas when CM4 and

<sup>592</sup> CM1 are fused, the accuracy is improved to 92.96% for feature and <sup>593</sup> 94.47% for score level fusion. This proves that when both the texture <sup>594</sup> images and depth maps are provided by 3D scanners, more robust <sup>595</sup> countermeasures can be obtained by fusion.

- For feature level fusion, the best performances are obtained by the 596 fusion of CM1, CM2 and CM4. In this part, we observed that when 597 we concatenate the same type of features (micro-texture features of 598 length 833 for each of CM1, CM2 and CM4), we observe a significant 599 increase in the performance. In CM3, the features are pixel intensity 600 values (features of length 4096). Therefore, when we apply feature level 601 fusion using CM3 with the other countermeasures, the positive impact 602 of CM3 in the performances was not observable as shown in Table 3. 603
- For score level fusion, the best performances are obtained by the fusion of CM1, CM2 and CM3. All these countermeasures (CM1, CM2 and CM3) uses texture images as input (reflectance image is computed from texture image). This proves that 2D data provides very beneficial information for mask spoofing detection.

• CM3 increases the performances when it is used in score level fusion, whereas the impact of it in feature level fusion is not remarkable.

Although CM1, CM2 and CM3 provide very satisfactory results alone,
 the score level fusion of these countermeasures provides the best performance compared to all other scenarios in Table 2 and 3. Therefore, in

- Figure 6, the ROC curve of this fusion based countermeasure is shown as the best one.
- Since existing 3D scanners provide both 3D scan and corresponding
   texture image, more robust countermeasures can be developed by fusion
   of these two type of outputs (2D and 3D data).

#### 619 6.2. Integration of the Countermeasure to Face Recognition Systems

In this subsection, we integrate the countermeasure with the best performance (fusion of CM1, CM2 and CM3) to the 3D FR system selected as baseline.

The evaluations are done for 4 modes. The first two modes are the base-623 line mode and the mode under attacks, which are explained in Subsection 624 3.3. The third mode illustrates performance when the countermeasure is 625 applied against the attacks, that results in an improved performance with 626 respect to the second mode. For the samples which are detected as attack 627 by the countermeasure, a least similarity score, which is zero in this test, 628 is assigned to those samples in verification tests. Last mode evaluates the 629 performance of the baseline system together with the countermeasure in the 630 normal operation mode of system, i.e., without attacks. The inclusion of the 631 countermeasure may degrade the baseline performance when not confronted 632 to attack (e.g. the countermeasure may consider as fake some real users.). 633

For evaluations, we fix 3 different evaluation points at FFR = 1%, 5%, and 10% (FFR and FLR were defined in the previous subsection). Once fixed, we incorporate the countermeasure as a first step into the baseline biometric systems oriented to discard fake data, and generate the performance
evaluations for the 4 modes explained above.

Figure 7 shows the behavior of the 3D face baseline system with/without attacks and with/without the countermeasure. The three figures represent the overall system performance under spoofing attacks when three different operating points (FFR = 1%, 5%, and 10%) are used for adjusting the countermeasure.

It is clear from Figure 7 that the 3D FR system is vulnerable to mask 644 attacks (more area between blue and red curves indicates more vulnerability 645 to the attacks). Performance enhancement is obtained almost all regions of 646 DET plots in Figure 7 when the countermeasure is introduced in presence of 647 mask attacks (black curve compared to red curve). If we take an operating 648 point where FFR = 1%, then FRR of the 3D FR system under attacks 649 drops from around 65% to around 50% at FAR = 2%. For both of the two 650 other plots (at FFR = 5% and 10%), the introduction of the countermeasure 651 lowers FRR from around 65% to 4% and 7%, respectively, at FAR = 2%. 652 The performance of the countermeasure is observed to be better at FFR =653 5% compared to the cases at FFR = 1% and 10%. Finally, the inclusion 654 of the countermeasure improves the results of 3D FR system under attacks, 655 whereas it degrades baseline performances of the system when not confronted 656 to attack (pink curve compared to blue curve). 657





Figure 7: The DET Curves of the 3D face baseline biometric system when integrating the countermeasure.

#### **558** 7. CONCLUSIONS

In this study, a 2D+3D mask attack database is used to evaluate the performances of the proposed countermeasures for the protection of face recognition systems against mask attacks.

The novelty of this study is that it is still one of the few studies that proposes countermeasures against 3D mask attacks. The analysis are done on depth maps, texture images and reflectance components of texture images, and 4 different countermeasures are proposed. Three of the proposed countermeasures use 2D data (texture images), and the remaining one uses 3D data (depth images) as input. These countermeasures can be used to protect

both 2D and 3D FR systems against mask attacks. The results of this study 668 show that analysis on reflectance images provide the best results compared 669 to analysis on texture and depth images. All of the 4 countermeasures pro-670 vide satisfactory information hence can be used as independent sources to 671 discriminate masks from real faces. However with the fusion of these coun-672 termeasures, we observe a significant improvement in the performances. For 673 instance, in this paper, a classification accuracy of 99% (almost perfect ac-674 curacy) is achieved for real face vs. mask face by fusing the information 675 extracted from the reflectance images and texture images. 676

Up to now, we have analyzed several characteristics of real and mask 677 faces, and obtained almost perfect results on this mask database. The lim-678 itation of our study is that we were able to test the performances of the 679 proposed countermeasures using the masks made from one type of material, 680 which is polychrome mineral powder. When masks made from different ma-681 terials are used, we may obtain different performance accuracy. Our future 682 works are first to test the performances of the proposed countermeasures us-683 ing masks made from different materials in order to observe if we can still 684 obtain satisfactory results, and then to propose new countermeasures for 685 more challenging mask databases with higher number of subjects as soon as 686 available. 687

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