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# Including individual customer lifetime value and competing risks in tree-based lapse management strategies

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## Abstract

A retention strategy based on an enlightened lapse model is a powerful profitability lever for a life insurer. Some machine learning models are excellent at predicting lapse, but from the insurer's perspective, predicting which policyholder is likely to lapse is not enough to design a retention strategy. In our paper, we define a lapse management framework with an appropriate validation metric based on Customer Lifetime Value and profitability. We include the risk of death in the study through competing risks considerations in parametric and tree-based models and show that further individualization of the existing approaches leads to increased performance. We show that survival tree-based models outperform parametric approaches and that the actuarial literature can significantly benefit from them. Then, we compare, on real data, how this framework leads to increased predicted gains for a life insurer and discuss the benefits of our model in terms of commercial and strategic decision-making.

**Keywords** Machine Learning · Life insurance · Customer lifetime value · Lapse · Lapse management strategy · Competing risks · Tree-based models

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## 1 Introduction

In life insurance, “lapse risk” or “persistency risk” is the risk that the policyholder will cancel the contract at a time other than when the issuer expected when pricing the contract [41]. A life insurance policy can lapse if the policyholder stops paying the premiums required to keep the policy in force. This can happen if the policyholder becomes unable or unwilling to make the premium payments or if the policyholder chooses to surrender the policy for its cash value. When a policy lapses, the coverage and benefits the policy provides are no longer in effect, and the policyholder will not receive any payout if they pass away after the policy has lapsed. This risk is not considered an insurance risk because the payment to the policyholder “is not contingent on an uncertain future event that adversely affects the policyholder”. However, lapse management is still undoubtedly a primary concern for life insurers. Lapses may substantially affect a company’s solvency, its future profits and cash flows [9, 10] or its Asset and Liabilities Management (ALM) [21, 22, 24, 40]. The importance of measuring lapse and churn behaviours is global; it goes from yielding individual estimations of the Customer Lifetime Values (CLV) to being an estimator of a firm’s profitability [27, 28] or strength [2]. Therefore, this paper focuses on developing strategies to prevent lapses before they occur: for a life insurer, an enlightened and proactive lapse management strategy (LMS) is critical for successful monitoring and steering. This paper is about defining a framework for a life insurer to measure and optimise the future loss or profit to be expected when applying such an LMS.

Part of the literature on lapse management adopts an economic-centred point of view [15, 17, 38, 39, 42, 50, 54, 58, 60, 61, 63]; we refer the reader to the complete bibliometric analysis on this topic by [59] for a summarised view of all these references. This economic-centred research aims to determine lapse factors like interest rates, gross domestic product, or unemployment rates. They are driven by economic hypotheses such as the emergency fund hypothesis (lapsing is a way of constituting an emergency fund), the policy replacement hypothesis (lapsing will occur when one changes its policy) or the interest rate hypothesis (lapsing depends strongly on rate change and arbitrage).

On the other hand, a large part of the literature investigates the individual determinants of lapse with policyholder-centred approaches. Micro-oriented features such as policyholder’s personal information or the policy characteristics have shown to give valuable insights into lapse behavior [21, 34, 49, 56]. Curak et al. [16] as well as [25]’s works indicate that policyholders’ features such as age and the number of beneficiaries are significant lapse factors, whereas [60] dismissed those results. A recent work from [46] proposes a comparison of lapse management strategies based on an innovative evaluation metric derived from the Customer Lifetime Value (CLV). [33] investigates the benefits of incorporating spatial analysis in lapse modeling, and [3] shows with an approach based on random forests that microeconomic features such as the company’s commercial approach for instance—is determining in the lapse decision. In contrast, macroeconomic features only have a limited effect. This variety of results—sometimes

contradicting each other—demonstrates the active interest in this research problem.

This paper focuses on lapse management strategy and retention targeting and will contribute to the existing literature on the relationship between retention strategy and lapse prediction: as in [2] and [46], our goal is not only to model the lapse behavior but rather to select policyholders that are expected to generate future profit, if targeted by a retention strategy. This work shows that a well-chosen strategy, based on individualized CLV and directed towards a well-chosen target, increases the insurer's expected profitability. A critical concept that motivates many CLV-driven decisions is that customers should be judged as assets based on their future profitability for the insurer. Thus, since retention often serves as the basis for CLV models [19, 29, 45]—sometimes specifically designed for targeting tasks [62]—and since CLV considerations should drive retention management, it seems natural to extend the existing life insurance applications linking those topics together. We make decision-making a central concern of our work and suggest proactive lapse management tools allowing the insurer to undertake actions to prevent the causes of lapse; that is opposed to a reactive management approach where decisions are taken after lapses and aim at recapturing lost policyholders.

The goal of this paper is to create an individualized CLV model that will be used to enhance classical binary churn models. We will then have a model for lapse management strategy and retention targeting that we further improve with tree-based survival analysis and competing risks considerations. The global framework is directly inspired by [46]. We try in this paper to build from that existing work and extend it. We model an individual future CLV with a new survival approach for which the risks of death and lapse are treated as mutually exclusive competing risks. For this purpose, we introduce parametric approaches—Cox cause-specific and subdistribution models—as well as tree-based survival models—Random Survival Forest (RSF) and Gradient boosting survival analysis. We focus here on tree-based models as they are often considered state-of-the-art models [26]. Thus we introduce tree-based machine learning algorithms for binary prediction, including Classification and Regression Tree (CART), Random forests (RF), and Extreme Gradient Boosting (XGBoost) to lapse behavior modeling. CART and XGBoost [46, 49] were used in the literature for lapse modeling but have yet to be applied to predicting life insurance lapses in a competing risk setting. To our knowledge, while Random Survival Forest has been used for churn prediction recently [57], both RSF and Gradient boosting survival analysis have never been used for that purpose before in an actuarial context.

Our contribution to the actuarial literature is twofold. First, we detail a two-step lapse management modeling approach: we fit parametric and tree-based competing risk individual survival models to estimate individualized future CLVs that are part of an evaluation metric for tree-based lapse management models. Second, this work includes a business-oriented discussion of the results achieved by this framework, which is missing from existing similar approaches.

The results and discussions show that a CLV-based lapse management strategy very often outperforms a more classical binary classification approach, even with competing risks and individualized considerations. When the latter yields profitable

retention gain, the former can produce higher profits, up to more than 60%. If a loss-inducing retention strategy is considered, our methodology limits the loss considerably, often setting 0 as a floor limit or even turning it into a profit-inducing retention strategy. Sensitivity analysis explores the influence of conjectural and structural parameters.

The rest of this paper is structured as follows. We briefly outline the data used in our study in Sect. 2. In Sect. 3, we then introduce the binary classification models we selected and detail our study's methodology, describing the classical and CLV-based performance measures and discussing substantial parametrization improvements over existing approaches. Then, Sect. 4 details our two-step methodology, with the parametric and non-parametric modelings of individual survival predictions, in a competing risks framework and then their implementation in the tree-based classification approaches considered. Section 5 presents the real-life application we considered and the different results it produces. Those results are analyzed and discussed in Sect. 6 with commercial and strategic decision-making orientations. Eventually, Sect. 7 concludes this paper.

## 2 Data

We apply our framework to a real-world insurance portfolio. For privacy reasons, all the data, statistics, product names and perimeters presented in this paper have been either anonymized or modified. All analyses, discussions and conclusions remain unchanged.

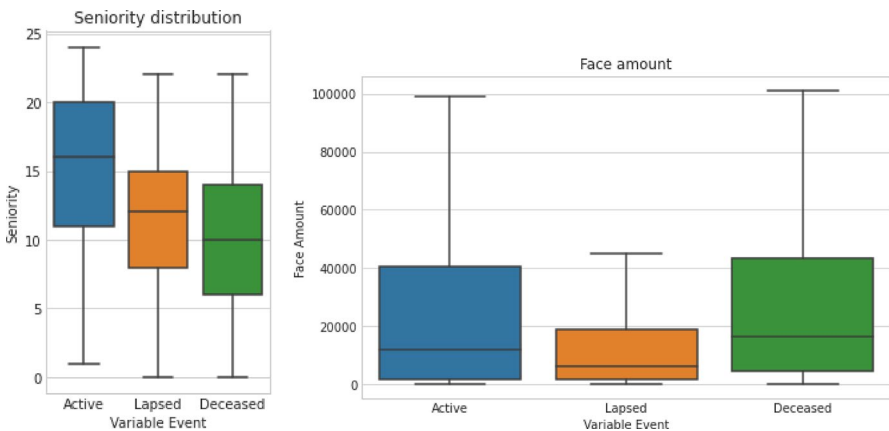
We illustrate our methodology with a life insurance portfolio from a French insurer contracted between 1997 and 2018. Each record in the data set represents a unique policy for a unique policyholder. In the following sections, we will often refer to a unique pair of policy and policyholder by the term "subject". The dataset contains 251,325 rows with 248,737 unique policies and 235,076 unique policyholders. It means that some policies are shared between several policyholders and that one individual can detain several insurance policies. The dataset contains 43 covariates described in Table 1.

The data set represents policies that are majority owned by men (57.4%) for a mean censored seniority time of 13.4 years. Three products are present in the dataset. Product one was chosen by 72% of policyholders, product 2 by 25% and product 3 by 3%.

Regarding their state, 61% of the policies are still active, 22% lapsed, and 17% ended after the PH's death. We chose here to present the distribution of the variable *SENIORITY* as it is the response variable in our survival models. Its modeling has a critical influence on CLV, thus, on our lapse management strategy framework. We also chose to show the distribution of the variable *TOTAL PREMIUM AMOUNT* representing the most recent observed face amount for every subject, as it is a known determinant of lapse behavior. We are aware that this covariate is a rather dynamic one as its value is updated at every payment, total or partial lapse, profit sharing, arbitration or even fees movements on a policy, and only considering its most recent value ignores a large part of the insights

**Table 1** Data set description

	Covariates (Numerical, Categorical, Date)	Description
ID	CDL.ID.PERSONNE	Policyholder (PH) unique ID
	CDL.ID.CONTRAT	Policy unique ID
PH-level information	CDL.DT.NAISSANCE	PH's birth date (main PH when several policyholders owns one policy)
	Age_souscription	PH's age at subscription
	Nb_Contrats	Number of different policies owned by the policyholder
	CDL.CD.SEXE	PH's gender (1=Female; 2=Male; other=Non precised)
	CDL.DESTINATAIRE.COURRIER	Anonymised PH's name
	CDL.NUM.ET.NOM.VOIE	Anonymised PH's address
	CDL.CD.POSTAL	Anonymised PH's postcode
Policy-level informations	CDL.COMMUNE	Anonymised PH's city of residence
	CDL.TOP.ASSURE	Binary: 1 if PH is the main PH on the policy, 0 otherwise
	CDL.TYPE.PRODUIT	Type of product ("Top-end product" or "Classical product")
	CDL.NOM.PRODUIT	Name of life insurance product ("Product 1", "Product 2" or "Product 3")
	CDL.PARTENAIRE	Name of the insurance distributor
	CDL.DATE.DEB.CONTRAT	Policy's start date
	CDL.DATE.FIN.CONTRAT	Policy's end date
	START_YEAR	Policy's start year
	END_YEAR	Policy's end year
	SENIORITY	Policy's seniority (final seniority if the policy is ended, current seniority otherwise)
External data	STATE	Policy's state ("Active", "Lapsed", or "Death" if the policy ended following PH's death)
	YEAR	Last year of observation
Policy's cumulated financial flows	DISCOUNT RATE	Discount rate corresponding to the last year of observation
	TOTAL_PREMIUM.AMOUNT	Total face amount of the policy
	TOTAL_EURO.PREMIUM.AMOUNT	Face amount of the policy in euros
	TOTAL_UC.PREMIUM.AMOUNT	Face amount of the policy in units of account
	ARBITRATION.EURO	Cumulated arbitration amount of the policy in euros
	ARBITRATION_UC	Cumulated arbitration amount of the policy in units of account
	FEES.EURO	Cumulated fees amount of the policy in euros
	FEES_UC	Cumulated fees amount of the policy in units of account
	OTHER.EURO	Cumulated other parts of the face amount of the policy in euros
	OTHER_UC	Cumulated other parts of the face amount of the policy in units of account
	PREMIUM.EURO	Cumulated payments amount of the policy in euros
	PREMIUM_UC	Cumulated payments amount of the policy in units of account
	PROFIT_SHARING.EURO	Cumulated profit sharing amount of the policy in euros
	PROFIT_SHARING_UC	Cumulated profit sharing amount of the policy in units of account
	CLAIM.EURO	Cumulated partial or total lapsed amount of the policy in euros
CLAIM_UC	Cumulated partial or total lapsed amount of the policy in units of account	
Covariates derived from financial flows	%TOTAL_UC.PREMIUM.AMOUNT	Percentage of the face amount in units of account
	%TOTAL_EURO.PREMIUM.AMOUNT	Percentage of the face amount in euros
	%CLAIM_UC	Percentage of the face amount in units of account that was lapsed
	%CLAIM_EURO	Percentage of the face amount in euros that was lapsed
Target covariate	%CLAIM	Percentage of the total face amount that was lapsed
	EVENT	Policy's state (0=Active, 1=Lapsed, 2 ended following PH's death)



**Fig. 1** Seniorities and face amounts distributions

it can provide. Without any better option, we can only use *TOTAL PREMIUM AMOUNT* as it is and defer any dynamic considerations for future work.

The seniorities and most recent face amount recorded before the potential end of the policy are distributed as in Fig. 1.

Without further analyzing the data, we can note several things. First, we can see that the mean censored seniority of 13.4 years is not equally distributed among our subjects. Active contracts tend to be older than lapsed ones, themselves older than policies that ended with the policyholder's death. That emphasizes the importance of several contributions, and the apparent difference in seniority regarding the cause of the policy's termination encourages a competing risks approach to analyze survival. Moreover, if we suspect lapse and death to be highly dependent on individual characteristics—such as the policyholder's age—this also supports an individualized survival analysis. Eventually, we can see that the last face amount observed is significantly lower for lapsed policies. It confirms our first intuitions and the face amount will be included in our model.

Among the covariates introduced in Table 1, several play a central part in our two-step modeling approach. First, the competing risks survival analysis step where *SENIORITY* will be the response variable, and all other covariates, including individual data and financial flows, are potential explanatory variables. The binary classification second step aims at predicting the *EVENT* outcome with minor transformations explained in Sect. 3 below. It is equivalent to using *STATE* as a target variable, as they are entirely similar. As a result, all covariates are not utilized and our predictions are solely based on the covariates underlined in Table 1 as they appeared to be of interest to insurers.

### 3 Framework

This section describes a modeling approach that follows [46]'s work. Our contributions place our work in a framework that differs from it by being only future-oriented, by a precise and individualized analysis of retention probabilities and by choosing a classification framework instead of regression. We chose to use a majority of their existing notations here.

Usual lapse management models based on classification aim to predict whether a policyholder will lapse. They may perform very well at that specific task, but it only reflects some aspects of this economic problem. Indeed, the literature is clear [2], and many policyholders may be predicted as “lapsers” but may not be profitable to the insurance company if targeted. In that case, keeping such policyholders would be irrational, and an efficient model should not predict them as targets. Targeting policyholders is an economic problem that requires an economic measure to assess. We propose to consider a measure based on the discounted expected profit of all the policies, in other words, the sum of all (CLVs). Optimizing a lapse, churn, or other prediction tasks with business-related measures is not new. However, to our knowledge, none of the existing approaches uses individualized future CLVs and models the profit of retention strategy by accounting for competing risks or using survival tree-based models.

CLV is a well-studied subject in marketing and business economics and has also been modeled in an insurance context. For a given subject  $i$ , her future CLV at horizon  $T$  can be modeled as

$${}^FCLV_i(\mathbf{p}_i, \mathbf{F}_i, \mathbf{r}_i, \mathbf{d}, T) = \sum_{t=0}^T \frac{p_{i,t} F_{i,t} r_{i,t}}{(1 + d_{i,t})^t}, \tag{1}$$

with  $t$  in years,  $t = 0$  represents the last observation point for subject  $i$ . The quantity  $p_{i,t}$  is her profitability ratio as a proportion of  $F_{i,t}$ , representing her face amount observed at time  $t$ . The quantity  $r_{i,t}$  is the  $i$ -th subject’s probability of still being active at time  $t$ , and naturally,  $d_{i,t}$  is the discount rate at time  $t$ , for subject  $i$ . We argue that both the profitability ratio and the discount rate should be as individualized as possible—either at the product or policy level—as  ${}^FCLV_i$  reflects the individualized risk of policyholder  $i$  to the insurer. It is also worth mentioning that evaluating discount rates is well beyond the scope of this paper as it is complex and subject to significant judgment; for further details, we refer the astute reader to a variety of papers on the subject [4, 11, 51].

It is worth pointing out that  ${}^FCLV_i$  does not represent the global profit generated by subject  $i$  from her policy’s first year until time  $T$  as in [46]; it rather represents the future  $T$  years of profit.  ${}^FCLV_i$  is not to be compared with the Cash Surrender Value but rather with the Fair Market Value (FMV) of the outstanding liabilities. The only difference with the latter is that  ${}^FCLV_i$  is based on the insurer’s knowledge of its portfolio, thus computed with its own profitability and discount parameters rather than with market-consistent considerations. Whereas the portfolio market value would consist of financial instruments that replicate the insurance liability cash flows. In our framework, the life insurer is more interested in maximizing its own realistic profitability rather than a sum of individual market values.

We suggest a model for the insurer’s estimated profit—or loss—resulting from a lapse management strategy (LMS). In order to do that, we will compare the expected value of the portfolio before and after applying a given strategy. We are aware that there could be infinite ways to design a retention campaign: offering a punctual incentive, recurrent services or more profit sharing, for instance. Here, we define what we will consider an LMS.

**Definition 1** (*Lapse management strategy*) A  $T$ -years lapse management strategy is modeled by the offer of an incentive  $\delta_i$  to subject  $i$  if she is targeted. The incentive is expressed as a percentage of her face amount and should not exceed the profitability ratio  $p_{i,t}$ , at any time point  $t$ . Contacting the targeted policyholder has a fixed cost  $c$  and after contact, the incentive is accepted with probability  $\gamma_i$ . A targeted subject who accepts the incentive will be considered as an “acceptant” who will never lapse. In our dataset, any subject that has never been observed to lapse is considered as an “acceptant” and her probability of being active at year  $t \in [0, T]$  is denoted  $r_{i,t}^{\text{acceptant}}$ . Conversely, a subject who refuses the incentive and prefers to lapse will be



considered as a “lapse”. In our dataset, a subject is labeled as a lapse whenever she has been observed to lapse at year  $t = 0$ , and her probability of being active at year  $t$  is denoted  $r_{i,t}^{\text{lapse}}$ . A lapse management strategy is uniquely defined by the parameters  $(\mathbf{p}, \delta, \gamma, c, T)$ .

It is to be noted that even if the framework involves a time dimension, it is still a static approach: the insurer would run all analyses on its portfolio at one given time and apply an appropriate LMS immediately.

Even if this definition is already a simplification of any real-life insurance retention strategy, various constraints and the data and tools at the insurer’s disposal do not always allow to conduct such a study. In the following section, we consider a simplified version of this framework by assuming that  $p_{i,t}$ ,  $F_{i,t}$ , and  $d_{i,t}$  remain constant across time, and denoted  $p_i$ ,  $F_i$  and  $d_i$  hereafter, with  $F_i$  being the most recent face amount observed for subject  $i$ . Moreover, we set  $\gamma_i$  and  $\delta_i$  to be the same for all subjects and denoted as  $\gamma$  and  $\delta$  hereafter. The constraint that  $\delta < \min(p_i)$  detailed in Definition 1 still holds. Finally, the last observed state of subject  $i$  is denoted  $y_i$ , with  $y_i = 1$  if the policy is lapsed,  $y_i = 0$  otherwise.

With those considerations, we can then define the control portfolio’s future value as

$$\begin{aligned} {}^F CPV(\mathbf{p}, \delta, \gamma, c, T) &= \sum_{i=1}^n {}^F CLV_i(p_i, F_i, r_i^{\text{acceptant}}, d_i, T) \cdot \mathbf{1}(y_i = 0) \\ &+ \sum_{i=1}^n {}^F CLV_i(p_i, F_i, r_i^{\text{lapse}}, d_i, T) \cdot \mathbf{1}(y_i = 1). \end{aligned} \quad (2)$$

It represents the hypothetical value of the portfolio, considering that:

- every subject that did not lapse up to her last observation point— $y_i = 0$  at  $t = 0$ —has a vector of retention probabilities of  $r_i^{\text{acceptant}}$ ;
- every subject that has been observed to lapse— $y_i = 1$  at  $t = 0$ —has a vector of retention probabilities of  $r_i^{\text{lapse}}$

**Remark 1** It is important to note that this does not reflect the actual future value of the portfolio—as the future CLV of lapsers should be 0 - but rather its hypothetical expected future value given the nature (lapse or not) of every subject but not their actual states (actually lapsed or not). It represents this hypothetical future CLV of all subjects if no customer relationship management about lapses is carried out.

A classification algorithm would take the lapse indicator  $y_i$  as a target variable and yield predictions  $\hat{y}_i$ . Given a lapse management strategy and such a classification algorithm, we define the lapse managed portfolio future value by

$$\begin{aligned}
 {}^F LMPV(\mathbf{p}, \delta, \gamma, c, T) &= \sum_{i=1}^n {}^F CLV_i(p_i, F_i, \mathbf{r}_i^{\text{acceptant}}, d_i, T) \cdot \mathbf{1}(y_i = 0, \hat{y}_i = 0) \\
 &+ \sum_{i=1}^n {}^F CLV_i(p_i, F_i, \mathbf{r}_i^{\text{lapsers}}, d_i, T) \cdot \mathbf{1}(y_i = 1, \hat{y}_i = 0) \\
 &+ \sum_{i=1}^n {}^F CLV_i(p_i - \delta, F_i, \mathbf{r}_i^{\text{acceptant}}, d_i, T) \cdot \mathbf{1}(y_i = 0, \hat{y}_i = 1) \\
 &+ \gamma \cdot \sum_{i=1}^n {}^F CLV_i(p_i - \delta, F_i, \mathbf{r}_i^{\text{acceptant}}, d_i, T) \cdot \mathbf{1}(y_i = 1, \hat{y}_i = 1) \\
 &+ (1 - \gamma) \cdot \sum_{i=1}^n {}^F CLV_i(p_i, F_i, \mathbf{r}_i^{\text{lapsers}}, d_i, T) \cdot \mathbf{1}(y_i = 1, \hat{y}_i = 1) \\
 &- \sum_{i=1}^n c \cdot \mathbf{1}(\hat{y}_i = 1).
 \end{aligned} \tag{3}$$

Clearly, the sums appearing in the formulas above could be grouped to make them more concise. We chose not to do so for the sake of visualization: we can distinctly see each possible case in each summand.

Then, we define the economic metric of the algorithm as the retention gain, the future profit generated by the retention management strategy over  $T$  years as

$$RG(\mathbf{p}, \delta, \gamma, c, T) = {}^F LMPV(\mathbf{p}, \delta, \gamma, c, T) - {}^F CPV(\mathbf{p}, \delta, \gamma, c, T), \tag{4}$$

which can be simplified as

$$\begin{aligned}
 RG(\mathbf{p}, \delta, \gamma, c, T) &= \sum_{i=1}^n \left[ \gamma \left[ {}^F CLV_i(p_i - \delta, F_i, \mathbf{r}_i^{\text{acceptant}}, d_i, T) \right. \right. \\
 &\quad \left. \left. - {}^F CLV_i(p_i, F_i, \mathbf{r}_i^{\text{lapsers}}, d_i, T) \right] \cdot \mathbf{1}(y_i = 1, \hat{y}_i = 1) \right. \\
 &\quad \left. - {}^F CLV_i(\delta, F_i, \mathbf{r}_i^{\text{acceptant}}, d_i, T) \cdot \mathbf{1}(y_i = 0, \hat{y}_i = 1) \right] \\
 &\quad - \sum_{i=1}^n c \cdot \mathbf{1}(\hat{y}_i = 1).
 \end{aligned} \tag{5}$$

This evaluation metric can now be derived into an individual retention gain measure. More specifically, we define  $z_i$  as

$$z_i = \begin{cases} -{}^F CLV_i(\delta, F_i, \mathbf{r}_i^{\text{acceptant}}, d_i, T) - c & \text{if } y_i = 0 \\ \gamma \cdot \left[ {}^F CLV_i(p_i - \delta, F_i, \mathbf{r}_i^{\text{acceptant}}, d_i, T) \right. \\ \left. - {}^F CLV_i(p_i, F_i, \mathbf{r}_i^{\text{lapsers}}, d_i, T) \right] - c. & \text{if } y_i = 1 \end{cases} \tag{6}$$

That last equation can seem obscure at first glance. It simply assigns to each individual the expected profit or loss that would result from targeting her with a given lapse management strategy. A positive amount for subject  $i$  means that targeting her would generate profit, whereas a negative one would lead to a loss for the insurer. We can

take the example of a hypothetical scenario where  $p_i = 3\%$ ,  $\delta = 0.05\%$ ,  $\gamma = 10\%$  and  $c = 10$  euros. It would generate  $z_i$ s taking values from  $-234,614\text{€}$  to  $53,066\text{€}$  with a mean of  $-218\text{€}$  and a median of  $-55\text{€}$ . Different scenarios would result in very different distributions for the  $z_i$ 's.

Eventually, we define  $\tilde{y}_i$  as a binary target variable indicating for policyholder  $i$  if the individual expected retention gain resulting from a given retention strategy is a profit or a loss. More specifically, we define  $\tilde{y}_i$  as

$$\tilde{y}_i = \begin{cases} 1 & \text{if } z_i > 0 \\ 0 & \text{if } z_i \leq 0 \end{cases}. \quad (7)$$

**Remark 2** A subject in the dataset for which  $y_i = 0$  would produce  $\tilde{y}_i = 0$ , whereas one for which  $y_i = 1$  could produce  $\tilde{y}_i = 0$  or  $\tilde{y}_i = 1$ . In other words, it is never profitable for the insurer to offer an incentive to a subject that would not have lapsed. On the other hand, offering that same incentive to a lapser can be profitable. However, depending on the subject's features and the lapse management strategy parameters, it can also lead to a loss.

We can now include  $\tilde{y}_i$  as a new binary target variable in our models and directly consider  $RG$  as the global evaluation metric in the tree-based models we consider.

We can now compare two models: the classical one with  $y_i$  as a target variable and accuracy as the evaluation metric; and the CLV-augmented one with  $\tilde{y}_i$  as a target variable and  $RG$  as the evaluation metric.

Intuitively, the former tries to predict whether a policyholder will lapse and tune its parameters by minimizing the misclassification rate. On the other hand, the latter aims at predicting whether applying a given retention strategy to the  $i$ th individual will be profitable for the insurer and tune its parameters by maximizing the global expected retention gain.

## 4 Methodology

In Sect. 3, we described a business-oriented framework, augmenting lapse management strategy with an evaluation metric based on the future CLV of every subject. Evaluating this metric requires computing  $r^{\text{acceptant}}$  and  $r^{\text{lapsers}}$ , the matrices of size  $(n, T + 1)$  containing for every subject, survival probabilities that we detail below. This individual survival analysis differs from [46]'s work where  $r^{\text{lapsers}}$  is estimated globally and takes the same value for every policyholder regardless of their characteristics and where  $r^{\text{acceptant}} = 1$  for any subject and at any time, ignoring the fact that an "acceptant"'s policy can end with the policyholder's death.

Given this framework, we propose a two-step methodology: firstly, we detail how this survival analysis is carried out to model those retention parameters, and secondly, we explain how we use them for training tree-based classification models.

#### 4.1 Step 1: modeling $r^{\text{acceptant}}$ and $r^{\text{lapsr}}$

We recall that a given subject's policy can end with lapse or death, and the policy is considered active if competing events are yet to occur. Furthermore, while a lapsr's policy can end with lapse or death, whatever comes first, an acceptant one can only end with death.

$r^{\text{lapsr}}$  represents the probability that the policy of subject  $i$  is still active at time  $t$ , given that the subject is labeled as a lapsr—EVENT = 1—at  $t = 0$ . Predicting these overall conditional survival probabilities with competing risks can be achieved by creating a combined outcome: the policy ends with death or lapse, whichever comes first. To compute  $r^{\text{lapsr}}$  in practice, we recode the competing events as a combined event. This approach is compatible with any survival analysis method regarding statistical guarantees.

Conversely,  $r^{\text{acceptant}}$  represents the probability that the policy of subject  $i$  is still active at time  $t$ , given that the subject is not labeled as a lapsr—EVENT = 0 or 2—at  $t = 0$ . This estimation is more complex as we must dissociate the risks of lapse and death. These causes being mutually exclusive, a competing risks methodology is well-suited to estimate  $r^{\text{acceptant}}$  [43].

It is also important to note that here,  $r^{\text{lapsr}}$  is modeled on subjects that have lapsed in the past—they may have been offered an incentive in the past, this is unknown—and not on subjects that have been offered an incentive that they declined. Our framework makes the implicit hypothesis that both behaviors are alike. It is more intuitive for  $r^{\text{acceptant}}$  as a subject that has not lapsed in the past would have accepted any incentive if offered.

##### 4.1.1 Competing risks frameworks

We are aware that improvements of our model over [46]'s approach, require the analysis of both the risks of lapse and death, thus a competing risk setting. As detailed in Appendix A.1, several regression models exist to estimate the global hazard and the hazard of one risk in such settings: cause-specific and subdistribution models. They account for competing risks differently, obtaining different hazard functions and thus have distinct advantages, drawbacks and interpretations. These differences are discussed in [48], where the authors also considered a competing risk framework for lapse prediction.

After discussions detailed in Appendix A.1, the simplicity of a cause-specific approach and the fact that it can be adapted to any survival method, including tree-based ones, oriented our choice towards it. We then computed  $r^{\text{acceptant}}$  and  $r^{\text{lapsr}}$  with three different methods—Cox model, Random Survival Forest and Gradient Boosting Survival Model—and retained the best one. These methods are shortly described in the following sections.

### 4.1.2 Cox proportional hazard model

One of the most common survival models is the Cox proportional hazard (CPH) model [14]. It postulates that the hazard function can be modeled as the product of a time-dependent and a covariate-dependent functions. The hazard function at time  $t$  for subject  $i$  with covariate vector  $X_i$ , under Cox proportional hazard model can be expressed as

$$\underbrace{\lambda(t|X_i^1, X_i^2, \dots)}_{\text{hazard function}} = \lambda(t|X_i) = \underbrace{\lambda_0(t)}_{\text{baseline hazard}} \underbrace{e^{(X_i \cdot \beta_i)}}_{\text{partial hazard}}.$$

It is crucial to note that in this model, the hazard function is the product of the baseline hazard, which only varies with time, and the partial hazard, which only varies depending on the covariates. The parameters of this model are the  $\beta$ , and they can easily be estimated with a maximum likelihood approach. Their estimation can be carried out without having to model  $\lambda_0(t)$ —which is why CPH is considered semi-parametric.

We use Python and lifelines [18] to implement it. We specify a spline estimation for the baseline hazard function. We select the covariates and model parameters using AIC [1] and use the concordance index [31] to compare CPH to other models. The concordance index—or Harrel’s c-index or simply c-index—is a metric to evaluate the predictions made by a survival model. It can be interpreted as a generalization of the area under a receiver operating characteristic (ROC) curve [30]—or AUC—in a survival setting with censored data.

### 4.1.3 Random survival forest

Survival trees have been extensively studied for a long time, and a complete review of such existing methods up to 2011 can be found in [5]. The most important thing to understand is that a survival tree can be created by modifying the splitting criterion of a regular tree. Most survival tree algorithms are designed with a split function that aims to maximize the separation of the resulting child nodes in terms of survival profiles. This separation between nodes is estimated by maximizing the log-rank statistic [44, 47]. Each terminal node of a survival tree contains a survival profile from which we can derive the survival and cumulative hazard function.

An RSF is the counterpart of a random forest (see Appendix A.2.2) for such survival trees. It has been developed in [36] and extended for competing risks a few years after [37]. A prediction with RSF for a given subject is made by getting his/her survival profile in each tree in the forest. His/her corresponding survival and cumulative hazard function are estimated in each tree with Kaplan–Meier and Nelson–Aalen estimators, respectively. Eventually, the aggregation of those single-tree estimates constitutes the RSF’s prediction.

We use Python and `sksurv` [53] to implement RSF, and we tune and evaluate our model using the concordance index.

**Remark 3** `Sksurv` allows us to use RSF with a cause-specific consideration of the competing risks. To this day, `sksurv` does not have a subdistribution competing risks model, whereas its R implementation `randomForestSRC` does [35].

Moreover, a severe limitation of that approach is that predictions can only be made at time points observed in the training set. Concretely, this prevents us from using RSF to extrapolate survival and hazard functions to unobserved time points.

#### 4.1.4 Gradient boosting survival model

In the same way Random Forest has a survival counterpart, this is also true for Gradient Boosting approaches. An essential distinction between classical boosting algorithms (see Appendix A.2.3) and Gradient Boosting Survival Model (GBSM) lies in its loss function. The loss function that we use with GBSM is the partial likelihood loss of a CPH model, and the optimization in such a model is achieved by maximizing a slightly modified log-partial likelihood function,

$$\arg \min_f \sum_{i=1}^n \delta_i \left[ f(X_i) - \log \left( \sum_{j \in g_i} e^{f(X_j)} \right) \right],$$

where  $\delta_i$  is the event indicator and  $f(X_i)$  is GBSM's prediction for the  $i$ -th subject, with a covariate vector  $X_i$ .  $g_i$  is the tree leaf including subject  $i$ .

Similarly to RSF, we use Python and `sksurv` [53] to implement GBSM. We tune and evaluate our model using the concordance index. Remark 3 also applies here.

#### 4.1.5 Final modeling choice

Our analysis shows that, based on concordance index, RSF and GBSM both outperformed a semiparametric Cox model in our study case. Regarding interpretability, we note that the feature importance analysis is very similar between the three models. All the details about the final concordance index scores, covariates importance and various plot for further analysis are available in Appendix A.2.

In the following sections, we decide to retain **GBSM** for the modeling of  $r^{\text{acceptant}}$  and  $r^{\text{lapsr}}$  as it has the best concordance index.

**Remark 4** As this study aims to be business-oriented and favor real-life decision-making, it is crucial to note that the computation times for fitting these different models are very different and could potentially be a huge constraint for real operational deployment. Specific computation times differ greatly depending on various factors, such as the number of subjects or features considered, the computation power or parallelization ability at disposal, for instance. However, we can still give here an order of magnitude for those differences. If the tuning and fitting process

**Table 2** Insightful LMS

Scenarios	$p$	$\delta$	$\gamma$	$c$	$d$	$T$
A-1	2.50%	0.04%	25%	10	1.50%	5
A-5	2.50%	0.04%	5%	10	1.50%	5
A-25	5.00%	0.10%	25%	10	1.50%	5
B-6	2.50%	0.08%	10%	10	1.50%	20
B-27	5.00%	0.20%	20%	100	1.50%	5

for CPH can last a few tens of seconds, it lasts hours for RSF and tens of hours for GBSM.

## 4.2 Step 2: classification tasks

Our work focuses on lapse management with tree-based models. It aims to answer the question: which policyholders would be worth targeting with a lapse management strategy to maximize the expected T-year profit for the insurer? We will consider a single tree built with Breiman's CART algorithm, Random Forest, XGBoost, and RE-EM trees. The following sections detail how those different approaches work. Those models will be compared on two different classification tasks; and tuned with two different evaluation metrics, a statistical metric and a business-related one.

**On  $y_i$**  First, we will use a classical lapse prediction framework to model the policyholder's behavior. Each policyholder will be labeled as a lapsers or a non-lapsers with a binary outcome  $y_i$ . Our first batch of models will be trained with  $y_i$  as a response variable and produce predictions  $\hat{y}_i$ . Accuracy( $y, \hat{y}$ ), which is undoubtedly the most intuitive performance measure for binary classification, is defined as the proportion of correctly predicted observations over all observations. It is widely used for churn analysis and appears to be a satisfying performance measure for relatively balanced outcomes—22% of all observed subjects being lapsers—in binary classification problems. We will use it as an evaluation metric in a 10-fold cross-validation step for tuning our models.

We know that more advanced evaluation metrics are available for binary classification, including the recall, the  $F_\beta$  score family [13], the AUC under the ROC or under the Precision-Recall curve, the Brier Score [8] and lift curve. They are standard evaluation metrics in classification and provide valuable insights into the model's performance, they are also frequently used in the applied binary classification literature, especially in the presence of a significant imbalance in the data [32]. However, in this paper, the mildness of the imbalance of  $y_i$  and our will to compare a customer-centered framework to representative real-world practices encourages us to use accuracy as a comparison. One of the goals of this article is to demonstrate that some of the current practices in real-world applications, based on statistical metrics such as accuracy can be significantly improved by considering a profit-driven target variable and evaluation metric. We are aware that accuracy may not be an optimal choice of evaluation metric for binary prediction in general and churn or

lapse analysis specifically, but it seems representative of what practitioners use (see Table 2 from [20] for example), as it is suggested in [46]. We do not aim at comparing our framework against the best existing methods but rather against the most representative. Nevertheless, the numerical results of Table 3 have also been obtained with recall, F1-score, and AUC for tuning and cross-validation and some are available in Appendix A.4: the conclusions obtained with such measures are similar to those obtained with accuracy. Thus, in this article and as in [46], we will only select, evaluate and discuss the models in the light of accuracy.

**On  $\tilde{y}_i$**  Secondly, we will use the CLV-Augmented lapse prediction framework, detailed in Sect. 3. Each policyholder will be labeled as a targeted lapses or a non-targeted policyholder with the binary outcome  $\tilde{y}_i$  and prediction for that outcome are denoted  $\hat{\tilde{y}}_i$ .

**Remark 5** Note that whenever  $y_i = 0$ , we also have  $\tilde{y}_i = 0$ . In other words, if subject  $i$  does not intend to lapse, it is never worth proposing her an incentive: the subject will accept it with probability 1 and would not have lapsed.

On the other hand, when  $y_i = 1$ , it corresponds to either  $\tilde{y}_i = 1$  or  $\tilde{y}_i = 0$ . In other words, if subject  $i$  is labeled as a lapses, it does not necessarily mean it is worth targeting her. From the insurer's point of view, some policies are better off lapsed.  $\tilde{y}$  can be seen as a more detailed version of  $y_i$  as it carries not only behavioral information regarding lapse but also a profitability one.

We thus train a second batch of models with  $\tilde{y}_i$  as a response variable. We use  $RG$  as an evaluation metric in a 10-fold cross-validation step for tuning these models.

*Summary of our methodology:* First, we train a CART, RF and XGBoost models with  $y_i$  as a binary target variable and accuracy as a tuning evaluation metric.

Then we train them with  $\tilde{y}_i$  as a binary target variable and  $RG$  as a tuning evaluation metric.

Finally, we train and test all six models on different random samples of our dataset and keep track of the model's classification performance on all of them and for various retention strategies for comparison's sake.

The sections below briefly introduce the tree-based model we selected before displaying how they performed in various lapse management scenarios.

#### 4.2.1 CART

CART (*Classification And Regression Trees*) is an algorithm developed by [7] that consists of recursively partitioning the covariate space. It is a widespread, intuitive and flexible algorithm that handles regression and classification problems.

#### 4.2.2 Random forest

A natural idea to correct CART's instability and enhance its prediction accuracy is the aggregation of a significant number of single trees, each grown on different subsamples of the dataset. A random forest (RF by [6]) is a tree-based bagging



**Table 3** Means of the results obtained on considered LMS

No.	Time (s)	Model	% Target diff (% of 1's)	Accuracy		Retention gain		RG/target		Improvement
				$\gamma_i$	$\bar{\gamma}_i$	$\gamma_i$	$\bar{\gamma}_i$	$\gamma_i$	$\bar{\gamma}_i$	
A-1	4949	CART	62.6% (8.2%)	92.3%	85.3%	114,661	219,655	4.48	38.20	91.6%
		RF		92.9%	85.4%	232,314	287,884	9.82	56.65	23.90%
		XGB		93.4%	85.8%	243,365	324,952	9.61	54.64	33.50%
A-5	4753	CART	86.7% (2.9%)	92.3%	83.6%	-514,477	-112,372	-20.08	-86.48	78.20%
		RF		92.9%	83.4%	-323,544	-3937	-13.65	-28.28	98.80%
		XGB		93.4%	83.3%	-383,004	0	-15.14	0	100.00%
A-25	5379	CART	31.0% (15.2%)	92.3%	89.2%	4,160,423	3,882,623	162.44	241.06	-6.70%
		RF		92.9%	89.5%	4,018,432	3,666,219	169.65	249.54	-8.80%
		XGB		93.4%	90.0%	4,455,108	4,410,629	176.09	267.87	-1.00%
B-6	5906	CART	36.6% (13.9%)	92.3%	88.8%	705,721	922,490	27.69	60.21	30.70%
		RF		92.9%	88.9%	1,352,182	1,269,349	57.11	97.63	-6.10%
		XGB		93.4%	89.6%	1,342,882	1,428,722	53.09	96.76	6.40%
B-27	4811	CART	73.9% (5.7%)	92.3%	84.3%	-694,436	751,404	-27.16	226.99	208.20%
		RF		92.9%	84.4%	-13,512	1,018,369	-0.51	356.48	7637.00%
		XGB		93.4%	84.7%	-38,050	1,253,252	-1.55	345.94	3393.70%

procedure where each tree is grown on randomly drawn observations and contains splits considering only randomly drawn covariates.

### 4.2.3 XGBoost

Other tree-based approaches have been designed to reduce the instability of a single-tree model. Model boosting is an adaptive technique, first developed by Freund et Shapire [23], that does not rely on the aggregation of independent weaker models but rather on the aggregation of weak models built sequentially, one after the other. XGBoost [12] is a widespread and performant tree-boosting model that relies on a gradient-boosting step and provides a very optimized parallelized procedure. It is considered a state-of-the-art library for various prediction problems.

The interested reader can find more detailed explanations about CART, RF and XGBoost mechanisms in the aforementioned references. For these modeling approaches, we used Python and sklearn [52].

## 5 Real-life application

Based on the real life-insurance dataset at our disposal (described in Sect. 2), we use the survival model we selected and estimate  $r^{\text{acceptant}}$  and  $r^{\text{lapses}}$  for every individual. This allows us to compute the individual CLVs, RGs,  $z_i$ 's and  $\tilde{y}_i$ . We have already defined what a strategy is (see Definition 1), and we can thus apply our classification methodology to various retention strategies.

### 5.1 Considered lapse management strategies

The strategies considered are based on several criteria. First, we selected realistic strategy parameters and time horizons based on actual retention campaigns led by life insurers. Moreover, we chose to present strategies that illustrate the exhaustive list of conclusions and discussions that are carried out in the next section. Finally, we also incorporated strategies that are “obviously bad” in the sense that such strategies would necessarily lead to a loss for the insurer. Such extreme scenarios will supplement our discussions. In any case, we consider  $p_i$  and  $d_i$  to be constant in our application, as both those parameters were not estimated at the individual level by the life insurer that provided with the dataset.

Results related to the 64 considered LMS are given in Appendix A.5. Our analysis showed that all considered LMS results can be split into five categories depending on how applying our framework impacted their expected retention gain over a naïve targeting. We have realistic profitable strategies that are improved by our framework, but also highly loss-inducing, moderate loss-inducing, highly profitable and unrealistically highly profitable strategies. We refer to the LMS displayed in Table 2 as representative strategies as they all belong to one of those categories. Numerical results regarding the most representative strategies can be found in Sect. 5.2 and related comments on how to read these tables are given in Sect. 5.3.

## 5.2 Numerical results

See Table 3.

## 5.3 Comments

Several terms in the two previous tables need to be explained. “% target diff” represents how different  $y$  and  $\tilde{y}$  are. It is the percentage of subjects for which  $y_i = 1$  and  $\tilde{y}_i = 0$ : in other words, the proportion of lapsers not worth targeting with a given strategy. The quantity “% of 1’s” represents the proportion of ones in  $\tilde{y}$  the target variable. It is to be compared with the 22% of ones in  $y$ : the proposed framework’s imbalance increases with “% target diff”.

Then the table shows the 10-fold cross-validated mean accuracies, retention gains and  $RG/target$  with two methodologies: the columns denoted  $y_i$  represent the metrics obtained by a model with  $y_i$  as a response variable and accuracy as an evaluation metric, and the columns denoted  $\tilde{y}_i$  represent the metric obtained by a model with  $\tilde{y}_i$  as a response variable and  $RG$  as an evaluation metric.

$RG/target$  represents the achieved retention gain for every targeted individual, for  $y_i$ , it is  $RG / \sum_i \hat{y}_i$ , for  $\tilde{y}_i$  it is  $RG / \sum_i \hat{\tilde{y}}_i$ . Eventually, “Improvement” represents the percentage of improvement between the  $RG$  obtained with a classification on  $y_i$  and the gain obtained with a classification on  $\tilde{y}_i$ . As the reported financial information was distorted for confidentiality reasons (see Sect. 2), relative measures such as “Improvement” are certainly more informative than absolute ones such as  $RG$ .

Some LMS are worth focusing on. For every strategy, we display its 10-fold cross-validated results: 10% of the dataset acting as an out-of-sample validation set at every fold. Every model is tuned by cross-validation within every fold. The boxplots below summarize some typical key results illustrated by several strategies. Those results will be discussed in Sect. 6.

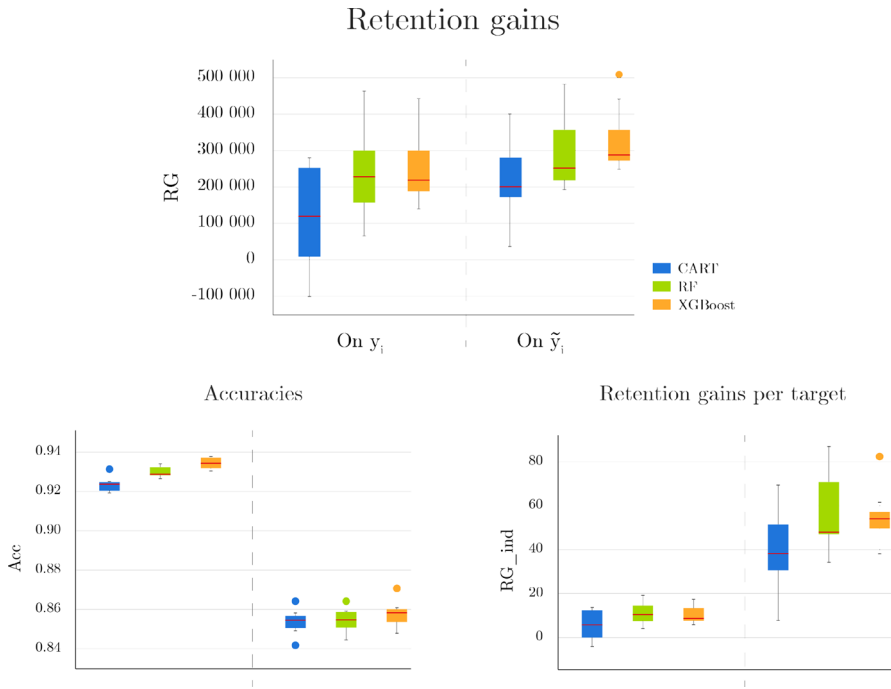
**Remark 6** With considerable computation power and great parallelization, the results for all strategies—see other strategies in Appendix A.5—were obtained with a wall time of less than 4 days and a CPU time of more than 100 days.

## 6 Discussion

### 6.1 General statements

As expected and shown in the actuarial literature, RF and XGBoost perform globally better than CART regarding mean accuracy and  $RG$ . It is true for all LMS considered in Table 10. Globally, XGBoost is more consistent and is the best model in most scenarios, both with and without the CLV-based measure. It is only outperformed by RF in strategies no A-7, A-11, A-14, A-29, B-7, B-14 and B-31.

As expected, by design, the vast majority of strategies, including all the realistic ones, show that a classification on  $\tilde{y}_i$  produces a targeting that yields better  $RG$



**Fig. 2** Strategy no A-1: (Positive result on  $y_i$  and an improved result on  $\hat{y}_i$ )

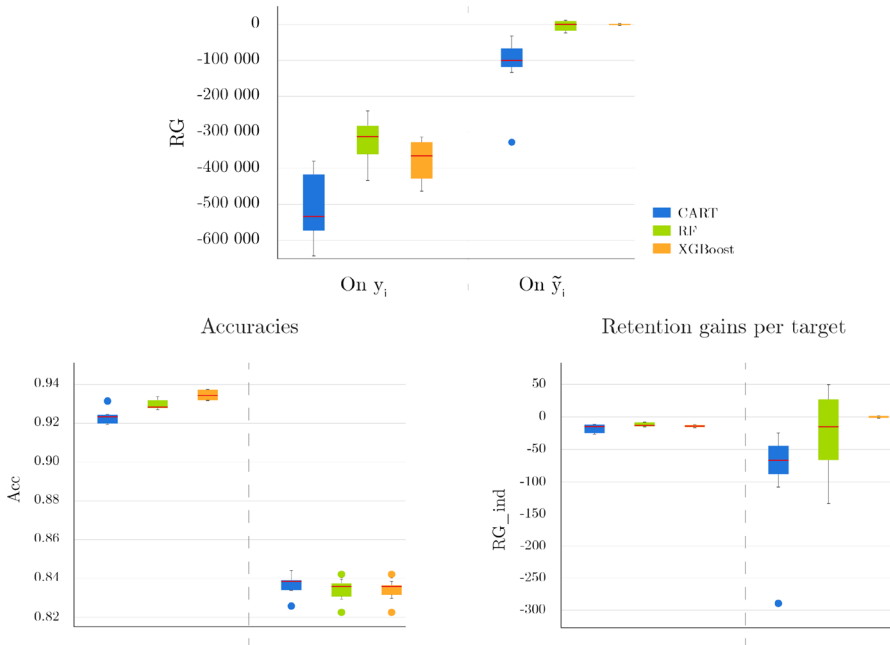
than a classification on  $y_i$ . Conversely, a classification on  $y_i$  produces a targeting that delivers better accuracies regarding whether a policyholder will churn than a classification on  $\hat{y}_i$ . These results were expected because of the models' respective objectives. Even if it is not surprising, it once again shows that for an insurer, lapse prediction and lapse management strategy are two very different prediction problems, often treated as similar ones.

Our CLV-augmented model shows different behavior depending on the strategy considered. As highlighted by Fig. 2, a model on  $y_i$  is greatly improved by our framework regarding RG and RG/target. Conversely, its accuracy in lapse prediction is not optimal.

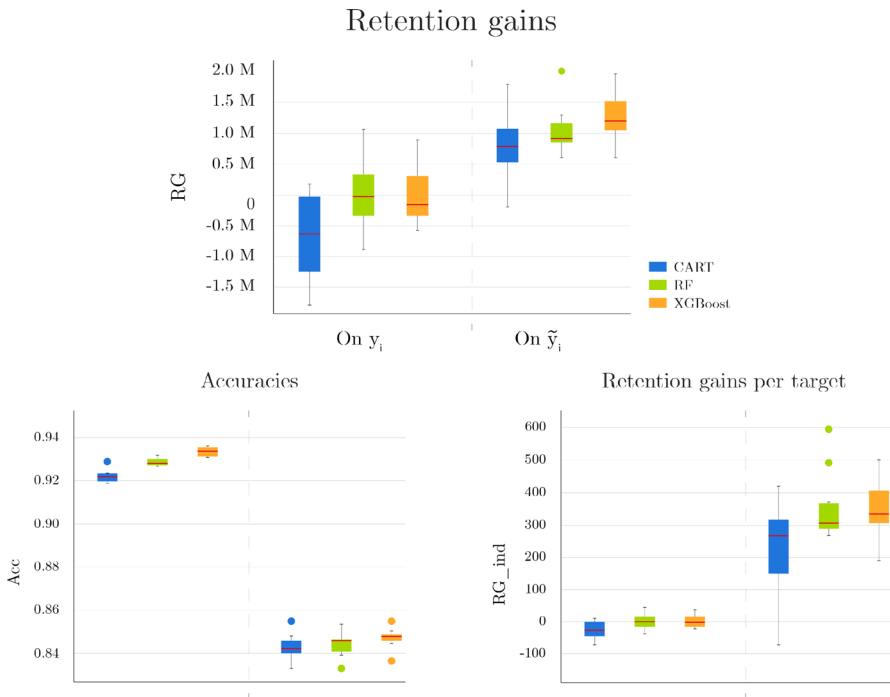
An attractive property of our framework can be observed in Fig. 3: it yields loss-limiting targeting. When the LMS considered is too aggressive, it will usually prefer to predict that an LMS should not be applied at all ( $\forall i, \hat{y}_i = 0$ ), thus generating a RG around 0€. This is made evident in some extreme strategies (LMS no A-5, A-15, B-11, B-13 and B-16) and explains the presence of 0's in Table 3.

On less extreme strategies, it shows to yield substantial improvement when classification on  $y_i$  gives negative RG. That observation confirms what was already pointed out by [46]: it can even turn a negative RG into a positive one [see LMS no A-8, B-8, B-12, B-23 and B-27 (Fig. 4)].

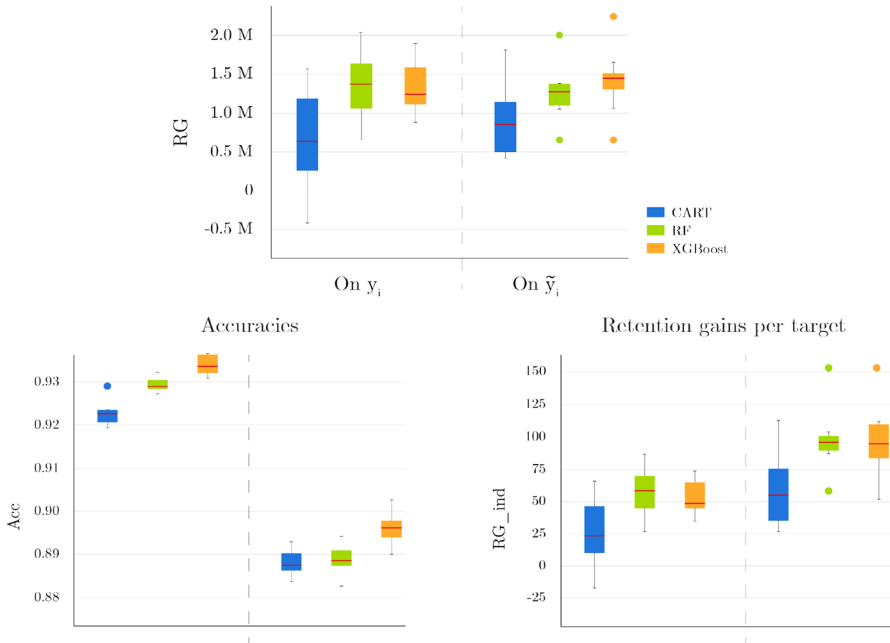
Our framework also improves a strategy where a classification on  $y_i$  gives high RG. However, the improvement decreases as the difference between the total number



**Fig. 3** Strategy no A-5: (Very negative result on  $y_i$  and a loss-limiting result on  $\tilde{y}_i$ )



**Fig. 4** Strategy no B-27: (Negative result on  $y_i$  and positive one on  $\tilde{y}_i$ )



**Fig. 5** Strategy no B-6: (High positive result on  $y_i$  slightly improved with  $\hat{y}_i$ )

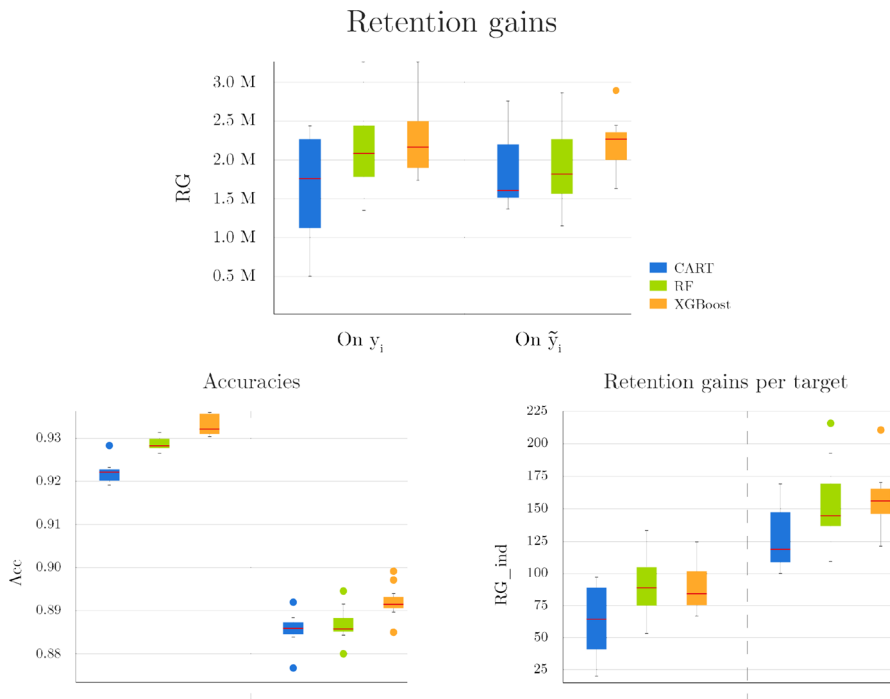
of lapsers and the number of lapsers that would be profitable if retained is sizeable. An example of that is shown in Fig. 5.

Finally, we can generate LMS for which our framework does not improve the expected RG. It is the case in LMS no A-13, A-18 or A-27 (see e.g. Fig. 6). In LMS no A-13, we can see that the mean of the RG is not improved, but the median is. In all those cases, the RG per target produced by the CLV-augmented model is greatly improved, indicating that a CLV-augmented strategy prefers to target fewer policyholders but only those who would generate high future profits. This last observation explains why a CLV-augmented LMS generates higher RGs when the cost of contact  $c$  is considerable. Indeed, the more costly a contact is, the more precise and specific a targeting strategy should be.

Generally, we can collate the results of various LMS—excluding LMS no B-27 that has a very high improvement ratio—to obtain a mean performance of our framework.

The average observed RG improvement of a CLV-augmented framework over the classical lapse one is 57,9%.<sup>1</sup> If we weigh these results by the expected RGs, the average improvement is still 31.7%. As a comparative result, it is reported in Sect. 6.2 of Loisel et al.’s work [46] that they obtain improvements over that same classical framework between 18% and 26%, depending on the considered strategies. This emphasizes that by extending their work, we seem to improve on their results. Obviously, as we were not able to compare our results on the same data

<sup>1</sup> Using XGBoost.



**Fig. 6** Strategy no A-25: (Results on  $y_i$  better than results on  $\tilde{y}_i$ )

and strategies, and because our definitions of *RG* differ, such a conclusion is to be treated cautiously.

## 6.2 Marketing decision making

We already pointed out that the improvement of a lapse management strategy including CLV grows with the proportion of lapsers with a negative CLV (see Appendix A.3). Models resulting from our framework do not consider them as good targets. In fact, there is a Pearson correlation coefficient of 77% between *RG* improvement and the proportion of target differences among the LMS detailed in Table 10. Of course, as the improvement ratio has no clear interpretation in some cases, this analysis should be carried out in more depth, separating the cases where both *RG*—with and without the inclusion of CLV—are positive from the cases where one of them is negative. By doing so, we observe that the Pearson correlation coefficient for LMS yielding positive *RG* regardless of the inclusion of CLV is even higher: 83%.

In terms of targeting, it seems crucial to understand what differentiates a subject for which  $y_i = 1$  and  $\tilde{y}_i = 0$  from the others. An investigation of such policyholder profiles can be carried out for every lapse management strategy. We take the example of LMS no A-1, where 62.6% of policyholders were in that case (see Sect. 5.2). With that strategy, the profile of non-targeted lapsers indicates that

- 57.2% of them are men, similar to the entire dataset,
- 76.4% of them contracted product no 1 whereas 72% of all policyholders chose it,
- the mean seniority of their policy is 10.4 years compared to the 13.4 years for the complete dataset,
- the mean face amount of such policies is 12,156, whereas the average face amount for all considered policies is 40,263.

In that strategy, our framework indicates that marketing efforts on low seniority policyholders with low face amount policies are inefficient. Of course, this conclusion is only valid for the considered LMS; however, our framework allows us to conduct such analysis for any LMS and interpret the results at an individualized level.

### 6.3 Management rules decision making

Sensitivity analysis of those results can highly benefit management rules decision-making. This framework serves as a tool that compares future hypothetical lapse management strategies in order to choose the best one—among realistic scenarios. It can also be used to tune a given strategy by answering questions like:

- For which incentive  $\delta$  the retention strategy becomes profitable ?
- For which acceptance probability  $\gamma$  the retention strategy becomes profitable ?
- With a given budget, what is the optimal list of policies that should be targeted?
- At which horizon  $T$ , the retention strategy become profitable ? In other words, when can the insurer expect a return on investment?

Answering these questions constitutes a 1-parameter sensitivity analysis. In our framework, six parameters influence the expected retention gain ( $p, \delta, \gamma, c, d, T$ ).

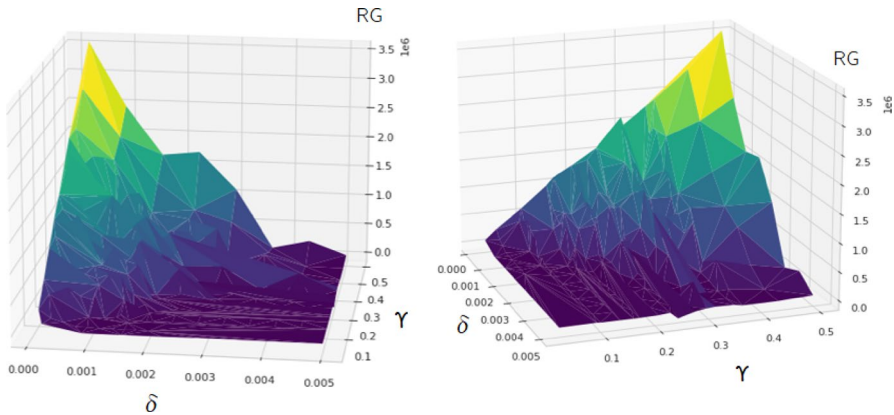
We can argue that among them are three structural parameters that are insurer's dependent and not linked to the external state of the world:  $\delta$ ,  $\gamma$  and  $c$ . Among them, the contact cost  $c$  is more or less fixed and can not be easily changed by the insurer. Conversely,  $\delta$  and  $\gamma$  are to be chosen by the insurer. Moreover, they also are correlated with management and commercial efficiency—an efficient campaign impacts the final  $\gamma$ —and correlated together: the higher the incentive  $\delta$ , the higher the probability of acceptance  $\gamma$ .

By fixing all other parameters and trying various combinations of  $\delta$  and  $\gamma$  we obtain the following 3D surfaces.

This surface is not surprising and indicates that the higher the acceptance rate and the lower the incentive, the higher the retention gain. The surface gradient can give powerful insights regarding the most efficient commercial efforts to make: is it better for the insurer to propose lower incentives and manage to conserve the same acceptance probability or to put commercial effort into improving the acceptance probability for the same proposed incentive? This surface directly addresses this question.

**Remark 7** Of course, the interdependency of those parameters should make some part of this surface unrealistic from a management decision-making point of view.





**Fig. 7** 3d plot  $(\delta, \gamma, RG)$

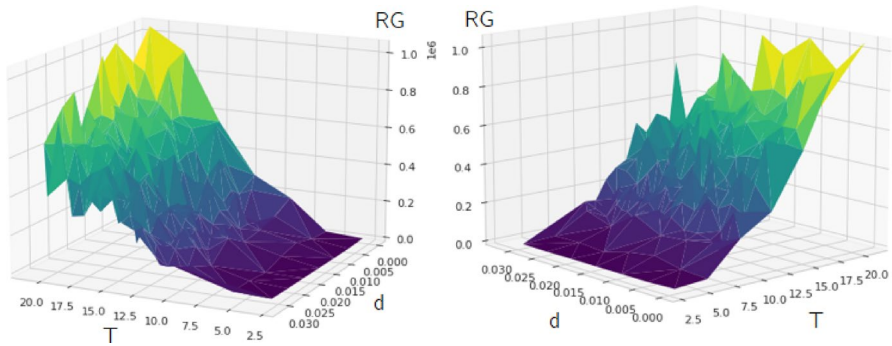
The insurer should consider such dependencies when designing a lapse management strategy.

Among the six parameters are also three conjectural parameters that depend on the external state of the world: the insurer's profitability  $p$  (that depends on competition, macroeconomic considerations or regulation), the discount rate  $d$  and the time horizon  $T$  (that can be driven by the insurer's vision but also by regulation: the ORSA time horizon with the strategic and the long-term business planning time horizon should be both considered). Among them, we chose to fix  $p$  and let  $d$  and  $T$  vary. Moreover,  $p$  and  $T$  are obviously interdependent and considered through the management's prospective view of the conjecture's evolution. A given interest rate scenario should represent a curve on the following surface.

This surface is less smooth than the one displayed in Fig. 7 and seems to indicate a more unstable relationship between RG and the conjectural parameters. An explanation of that behavior can be that those surface points are generated by running our framework on a random subsample of our dataset, for computation time considerations. Generating the same surface with more policyholders is likely to give a smoother behavior (Fig. 8).

**Remark 8** Of course, the interdependency of  $T$  and  $d$  should make some part of this surface unrealistic from an actuarial point of view. Actuarial rate projections would give precise plausible scenarios on this surface. Such considerations should be taken into account by the insurer when designing a lapse management strategy.

**Remark 9** The insurer can also use our framework to measure the retention gain to be expected at different time horizons obtained by existing retention campaigns. In that case, the insurer would have to neutralize the effect of the existing LMS in order to estimate the control portfolio's future value. We leave this remark as future work for applied risk management research.



**Fig. 8** 3d plot ( $d$ ,  $T$ ,  $RG$ )

## 7 Conclusion and perspectives

The work carried out in this paper shows that including CLV in lapse management strategy can largely benefit an insurer's decision-making ability regarding lapse management strategy. We showed that survival tree-based models can outperform parametric approaches in such actuarial contexts. Then, our comparison of tree-based models on different lapse management strategies indicated that our CLV-based framework leads to increased predicted gains for any realistic scenario and acts as a loss-limiting targeting approach, regardless of the retention strategy. Moreover, the global results obtained in Sect. 6.1 show that our approach significantly improves on existing ones. Eventually, the discussion section highlighted the fact that our model can give insights to the life insurer regarding commercial and strategic decision-making.

The framework and methodologies described in this paper suffer some limitations. For instance, following one single fixed strategy for every policyholder is arguably unrealistic. We could imagine an extension of our models to individualized lapse management strategies that would vary between subjects and could also be adjusted with time. In the application, we also considered constant parameters  $p$  and  $\delta$ : a limiting assumption whose impact could be studied. There is also room for improvement regarding the correlations of LMS parameters: the value of the incentive and the acceptance probability are evidently interdependent parameters for an insurance company, and this interdependency could be considered.

This paper defines a practical management tool for life insurers as those models can measure the  $RG$  and improve real strategies used in existing retention campaigns. Finally, our vision of CLV, and by extension, our whole methodology design could be improved by using longitudinal data that would yield time-dynamic results. We leave those two last observations for future work.

A real-life comparison between an actual retention strategy targeting and both the naïve and CLV-improved methodologies could be insightful for the insurer.

## A Appendix

### A.1 Competing risk framework

There are several regression models to estimate the global hazard and the hazard of one risk in settings where competing risks are present: modeling the cause-specific hazard and the subdistribution hazard function. They account for competing risks differently, obtaining different hazard functions and thus distinct advantages, drawbacks, and interpretations. Here, we will introduce those approaches' theoretical and practical implications and justify which one we will use in our modeling approaches.

In cause-specific regression, each cause-specific hazard is estimated separately, in our case, the cause-specific hazards of lapse and death, by considering all subjects that experienced the competing event as censored. Here,  $t$  is the traditional time variable of a survival model, with  $t = 0$  being the beginning of a policy. It is not to be confused with the use of  $t$  in Sects. 3 and 4. We remind that  $J_T = 0$  corresponds to an active subject that did not experience lapse  $J_T = 1$  or death  $J_T = 2$ . The cause-specific hazard rates regarding the  $j$ th risk ( $j \in [1, \dots, J]$ ) are defined as

$$\lambda_{T,j}(t) = \lim_{dt \rightarrow 0} \frac{P(t \leq T < t + dt, J_T = j \mid T \geq t)}{dt}.$$

We can recover the global hazard rate as  $\lambda_{T,1}(t) + \dots + \lambda_{T,J}(t) = \lambda_T(t)$ , and derive the global survival distribution of  $T$  as

$$\begin{aligned} P(T > t) &= 1 - F_T(t) = S_T(t) \\ &= \exp\left(-\int_0^t (\lambda_{T,1}(s) + \dots + \lambda_{T,J}(s)) ds\right). \end{aligned}$$

This approach aims at analysing the cause-specific “distribution” function:  $F_{T,j}(t) = P(T \leq t, J_T = j)$ . In practice, it is called the Cumulative Incidence Function (*CIF*) for cause  $j$  and not a distribution function since  $F_{T,j}(t) \rightarrow P(J_T = j) \neq 1$  as  $t \rightarrow +\infty$ . By analogy with the classical survival framework, the *CIF* can be characterised as  $F_{T,j}(t) = \int_0^t f_{T,j}(s) ds$ ,<sup>2</sup> where  $f_{T,j}$  is the improper<sup>3</sup> density function for cause  $j$ . It follows that

$$f_{T,j}(s) = \lim_{dt \rightarrow 0} \frac{P(t \leq T < t + dt, J_T = j)}{dt} = \lambda_{T,j}(t) S_T(t).$$

The equation above is self-explanatory: the probability of experiencing cause  $j$  at time  $t$  is simply the product of surviving the previous time periods by the cause-specific hazard at time  $t$ . We finally obtain the *CIF* for cause  $j$  as

$$F_{T,j}(t) = \int_0^t \lambda_{T,j}(s) \exp\left(-\int_0^s \lambda_T(u) du\right) ds.$$

<sup>2</sup> We suppose that  $T$  has a continuous distribution.

<sup>3</sup> Because derived from the *CIF*, an improper cumulative distribution function.

There are several advantages to that approach. First of all, cause-specific hazard models can be easily fit with any classical implementation of CPH by simply considering as censored any subject that experienced the competing event. Then the *CIF* is clearly interpretable and summable  $P(T \leq t) = F_{T,1}(s) + \dots + F_{T,J}(s)$ <sup>4</sup>. On the other hand, the *CIF* estimation of one given cause depends on all other causes: it implies that the study of a specific cause requires estimating the global hazard rate, and interpreting the effects of covariates on this cause is difficult. Indeed, part of the effects on a specific cause comes from the competing causes, but in our setting, we are only interested in the prediction of the survival probabilities, not their interpretation as such.

We have introduced it at the beginning of this section; another approach is often considered to analyze competing risks and derive a cause-specific *CIF*. This other approach called the subdistribution hazard function of Fine and Gray regression, works by considering a new competing risk process  $\tau$ . Without loss of generality, let's consider death as our cause of interest,

$$\tau = T \times \mathbb{1}_{J_T=2} + \infty \times \mathbb{1}_{J_T \neq 2}.$$

It has the same as  $T$  regarding the risk of death,  $P(\tau \leq t) = F_{T,2}(t)$  and a mass point at infinity  $1 - F_{T,2}(\infty)$ , probability to observe other causes ( $J_T \neq 2$ ) or not to observe any failure. In other words, if the previous approach considered every subject that experienced competing events as censored, this approach considers a new and artificial at-risk population. This last consideration is made clear when deriving the hazard rate of  $\tau$ ,

$$\lambda_\tau(t) = \lim_{dt \rightarrow 0} \frac{P(t \leq T < t + dt, J_T = 2 \mid \{T \geq t\} \cup \{T \leq t, J_T \neq 2\})}{dt}.$$

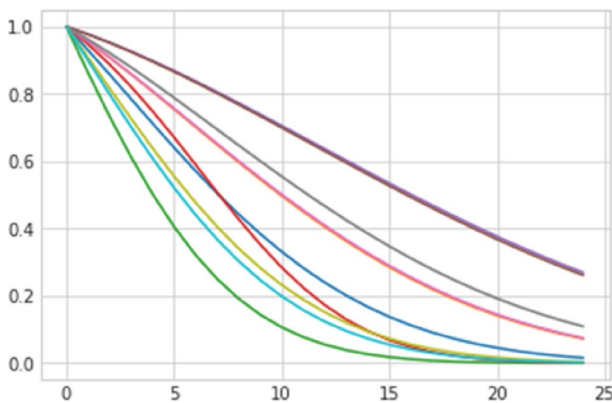
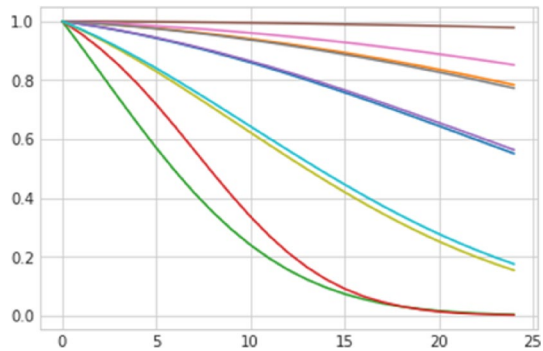
Finally, we obtain the *CIF* for the risk of death as

$$F_{T,2}(t) = 1 - \exp\left(-\int_0^t \lambda_\tau(s) ds\right).$$

This subdistribution approach resolves the most important drawback to cause-specific regression, as the coefficients resulting from it do have a direct relationship with the cumulative incidence: estimating the *CIF* for a specific cause does not depend on the other causes, which makes the interpretation of *CIF* easier. The subdistribution hazard models can be fit in R by using the `crr` function in the `cmprsk` package or using the `timereg` package. Still, to our knowledge, there is no implementation of a Fine and Gray model in `Lifelines` or, more generally, Python. We can also note that these two approaches are linked, [55] and the link between  $\lambda_\tau(t)$  and  $\lambda_{T,j}(t)$  is given by

<sup>4</sup> unlike to the function  $1 - \exp\left(-\int_0^t \lambda_{T,j}(u) du\right)$ .

**Fig. 9** 10 policyholders' survival curve for  $r^{acceptant}$  with Cox model



**Fig. 10** 10 policyholders' survival curve for  $r^{lapses}$

$$\lambda_{\tau}(t) = r_j(t)\lambda_{T,j}(t), \text{ with } r_j(t) = \frac{P(J_T = 0)}{\sum_{p \neq j}^J P(J_T = p)}.$$

In other words, if the probability of any competing risk is low, the two approaches give very close results.

## A. 2 Survival analysis results

The quantity  $r_{i,t}^{lapses}$  represents the probability that the policy of subject  $i$  is still active at time  $t$ , given that it was active at its last observed time. Predicting the overall conditional survival with the competing risks, in that case, can be achieved by creating a combined outcome. The policy ends with death or lapse, whichever comes first, and to compute  $r^{lapses}$ , we recode the competing events as a combined event. In terms of statistical guarantees, this approach is compatible with any survival analysis method.

In the following sections of this appendix,  $r_{i,t}^{acceptant}$  indicates the probability of survival for subject  $i$  at time  $t$  given that it will not lapse. In other words, it is the survival probability regarding only the risk of death. As detailed in Sect. 4.1.1, this

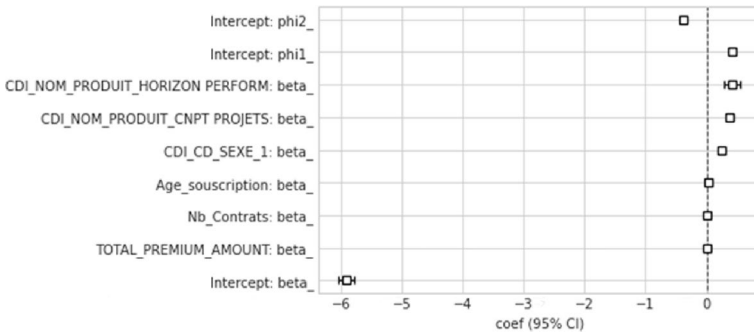


Fig. 11 Coefficient plot for  $r^{lapser}$

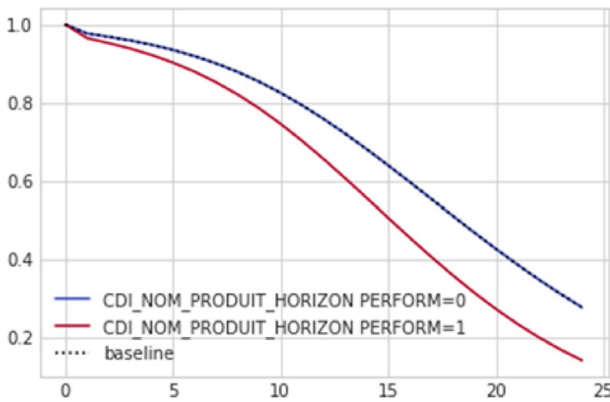


Fig. 12  $r^{lapser}$  trajectories for different products

corresponds to the cause-specific survival probability for death. It is to be noted that the density from which we derive our survival probabilities is improper as it derives itself from the *CIF*, which is not a proper distribution function.<sup>5</sup> Therefore, any conclusion about those probabilities should be drawn with care. Similarly to  $r^{lapser}$ , covariates selection and tuning are performed by minimizing AIC.

All graphs representing survival curves below are plotted with the same axis. The x-axes are the time in years, the y-axes represent the survival probability.

### A.2.1 Cox-model

We first decide to estimate survival with a Cox Proportional hazard model with a spline baseline hazard from the Python library Lifelines. Covariate selection and tuning are performed by minimizing AIC.

Here is what  $r^{acceptant}$ , the vector of cause-specific probabilities, looks like, and we can compare it to  $r^{lapser}$  on some subjects (Figs. 9, 10).

<sup>5</sup> as it does not tend to 1 as  $t$  goes to  $+\infty$

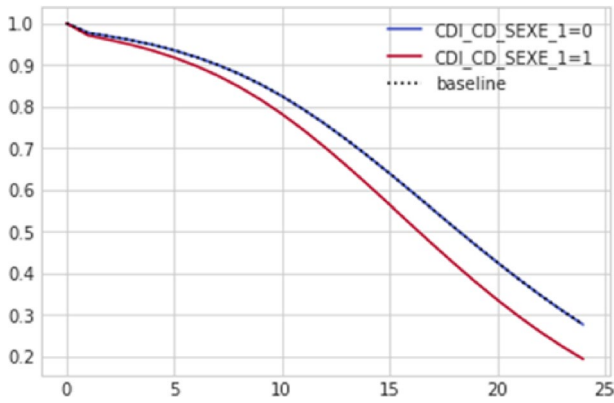


Fig. 13  $p^{lapse}$  trajectories by gender

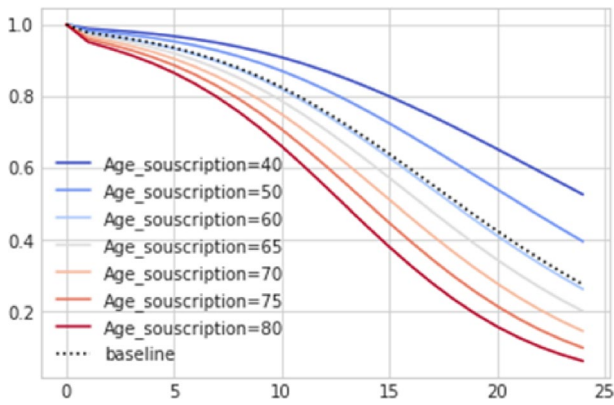


Fig. 14  $p^{lapse}$  trajectories for different ages

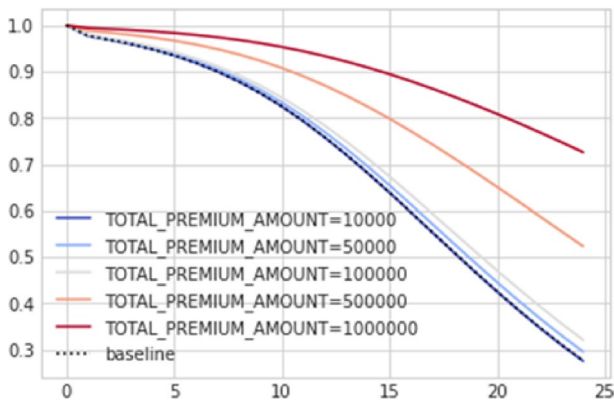


Fig. 15  $p^{lapse}$  trajectories for different face amounts

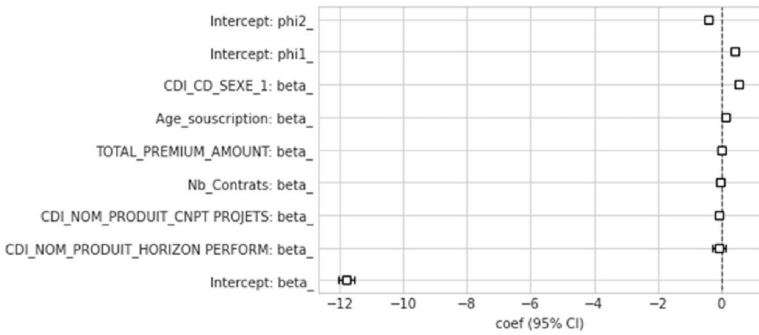


Fig. 16 Coefficient plot for  $r^{acceptant}$

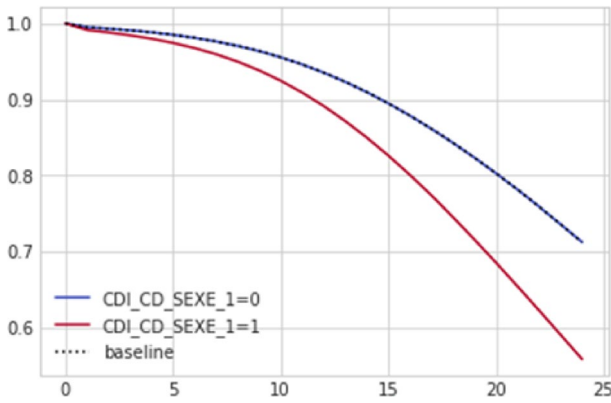
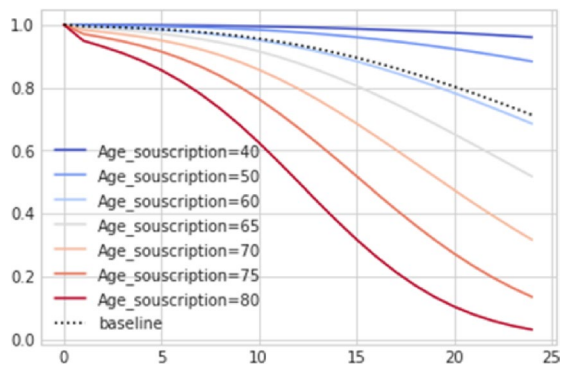


Fig. 17  $r^{acceptant}$  trajectories by gender

Fig. 18  $r^{acceptant}$  trajectories for different ages



The effect of various covariates on the survival outcome can be found below (Figs. 11, 12, 13, 14, 15, 16, 17, 18, 19).



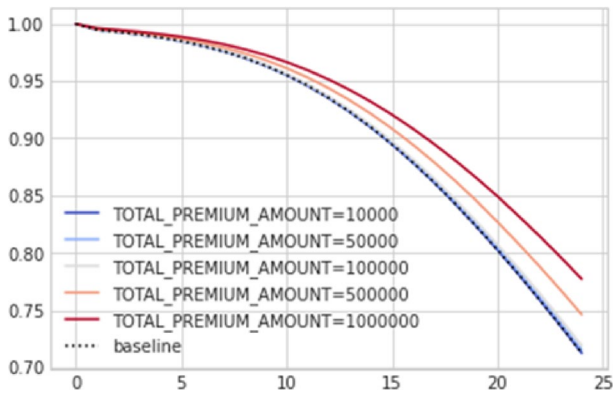


Fig. 19  $r^{acceptant}$  trajectories for different face amounts

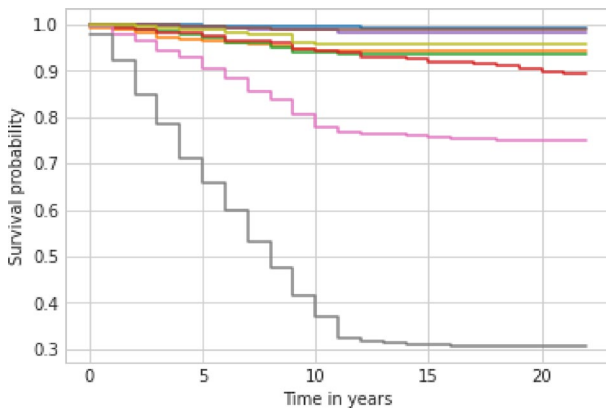


Fig. 20 10 policyholders' survival curve for  $r^{acceptant}$  with RSF

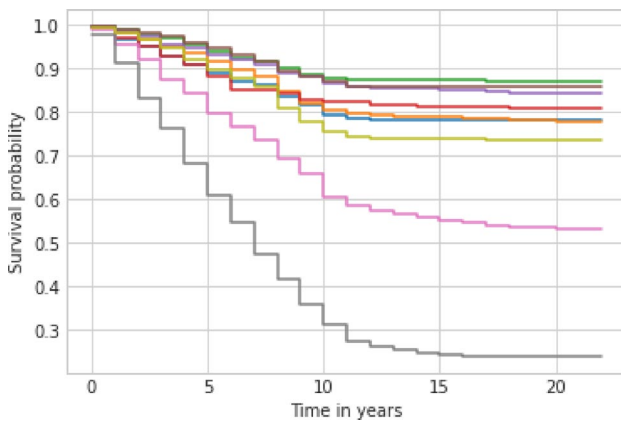


Fig. 21 10 policyholders' survival curve for  $r^{lapses}$  with RSF

### A.2.2 RSF

We obtain better results than Cox in terms of concordance index at the cost of very high computation time for one training with one set of parameters—5 days without parallelisation, 4 h with—compared to a few seconds for cox model (Tables 4, 5).

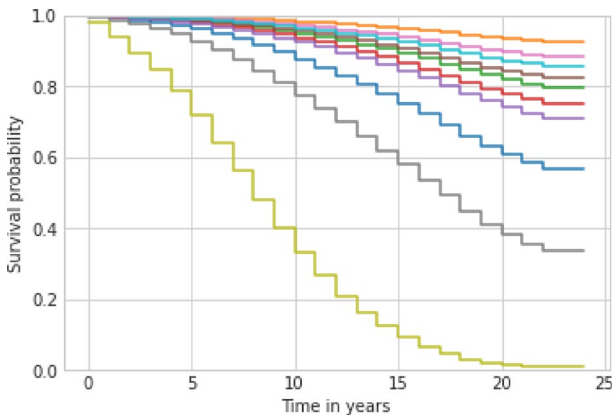
Some of the results we obtain are displayed below (Figs. 20, 21).

**Table 4** Covariates importance for  $r^{acceptant}$  with RSF

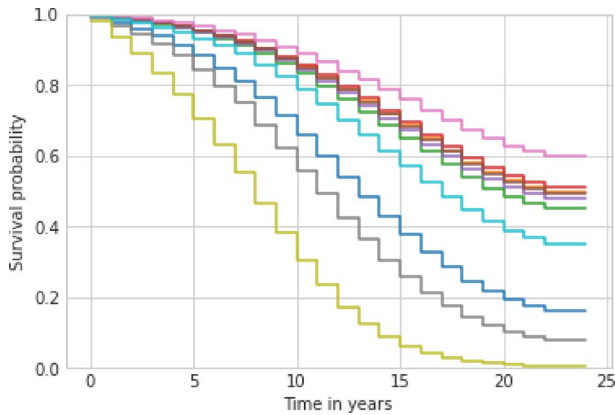
Weight	Feature
$0.3148 \pm 0.0064$	Age_souscription
$0.0100 \pm 0.0008$	CDI_CD_SEXE_1
$0.0091 \pm 0.0014$	PRODUIT_2
$0.0077 \pm 0.0006$	TOTAL_PRE-MIUM_AMOUNT
$0.0013 \pm 0.0004$	Nb_Contrats
$0.0010 \pm 0.0003$	PRODUIT_3

**Table 5** Covariates importance for  $r^{lapse}$  with RSF

Weight	Feature
$0.1838 \pm 0.0045$	Age_souscription
$0.0415 \pm 0.0018$	TOTAL_PRE-MIUM_AMOUNT
$0.0083 \pm 0.0011$	CDI_CD_SEXE_1
$0.0026 \pm 0.0013$	PRODUIT_2
$0.0022 \pm 0.0006$	PRODUIT_3
$0.0020 \pm 0.0006$	Nb_Contrats



**Fig. 22** 10 policyholders’ survival curve for  $r^{acceptant}$  with GBSM



**Fig. 23** 10 policyholders' survival curve for  $r^{lapses}$  with GBSM

### A.2.3 XGSB

We obtain better results than Cox and slightly better results than RSF in terms of concordance index at the cost of even higher computation time for one training with one set of parameters—10 h with great parallelisation—compared to a few seconds for Cox model (Tables 6, 7).

Some of the results we obtain are displayed below (Figs. 22, 23).

**Table 6** Covariates importance for  $r^{acceptant}$  with GBSM

Weight	Feature
$0.3274 \pm 0.0071$	Age_souscription
$0.0104 \pm 0.0006$	TOTAL_PRE-MIUM_AMOUNT
$0.0100 \pm 0.0008$	CDI_CD_SEXE_1
$0.0025 \pm 0.0005$	PRODUIT_2
$0.0005 \pm 0.0001$	Nb_Contrats
$0.0000 \pm 0.0001$	PRODUIT_3

**Table 7** Covariates importance for  $r^{lapses}$  with GBSM

Weight	Feature
$0.1872 \pm 0.0039$	Age_souscription
$0.0438 \pm 0.0020$	TOTAL_PRE-MIUM_AMOUNT
$0.0134 \pm 0.0014$	PRODUIT_2
$0.0076 \pm 0.0009$	CDI_CD_SEXE_1
$0.0051 \pm 0.0006$	PRODUIT_3
$0.0011 \pm 0.0004$	Nb_Contrats

### A.2.4 Final survival model

The final concordance index scores are displayed below (Table 8):

**Table 8** Survival models comparison

	Concordance index	
	$\mu_{lapse}$	$\mu_{acceptant}$
Cox model	69.5%	80.7%
RSF	71.6%	83.7%
GBSM	73.0%	84.1%

### A.3 Other results

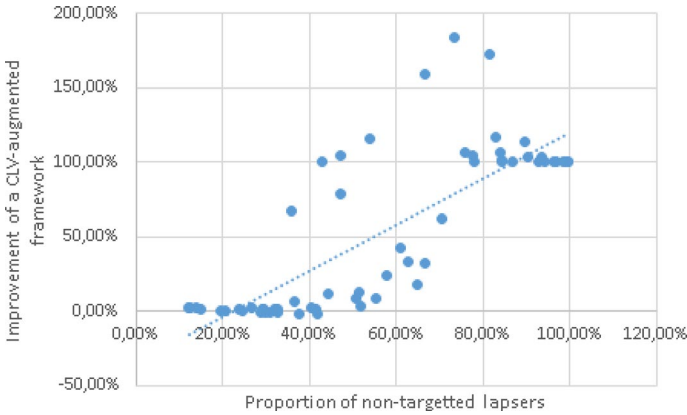
#### A.4 Considering various statistical metrics

The table below contains the results of the "LMS listed in Table 3, evaluated on accuracy, recall, F1-score and AUC. For every metric, it displays the results of a classification over  $y_i$  tuned and cross-validated with each of the metrics—respectively  $\mu_{accuracy}^{y_i}$ ,  $\mu_{recall}^{y_i}$ ,  $\mu_{F1-score}^{y_i}$  and  $\mu_{AUC}^{y_i}$ —or over  $\tilde{y}_i$  which is always tuned and cross-validated with *RG* (Table 9, Fig. 24).

It is to be noted that regardless of the evaluation metric used for tuning and validation purposes, the objective function used with XGB to generate those results is always the log-loss function. Using the area under the ROC curve or the area under the Precision-Recall curve as an objective function in this boosting algorithm would surely yield better results when trained on  $y_i$  and even better on the more unbalanced  $\tilde{y}_i$ . As stated in Sect. 4.2, this analysis is not within the scope of our article.

**Table 9** Results of representative LMS with various statistical metrics

No	Model	Recall			FI-score			AUC			Retention gain			RG/target				
		$\frac{accuracy}{Y_i}$	$\frac{recall}{Y_i}$	$\frac{\tilde{Y}_i}{Y_i}$	$\frac{FI-score}{Y_i}$	$\frac{\tilde{Y}_i}{Y_i}$	$\frac{AUC}{Y_i}$	$\frac{accuracy}{Y_i}$	$\frac{recall}{Y_i}$	$\frac{\tilde{Y}_i}{Y_i}$	$\frac{FI-score}{Y_i}$	$\frac{\tilde{Y}_i}{Y_i}$	$\frac{AUC}{Y_i}$	$\frac{accuracy}{Y_i}$	$\frac{recall}{Y_i}$	$\frac{\tilde{Y}_i}{Y_i}$		
A-1	CART	92.3%	75.7%	18.0%	76.4%	28.9%	85.6%	58.4%	114.661	128.251	135.085	128.251	219.655	4.48	5.13	5.46	5.13	38.20
	RF	92.9%	74.7%	14.7%	77.7%	24.9%	85.6%	57.0%	232.314	203.821	203.821	203.821	287.884	9.82	8.66	8.66	8.66	56.65
	XGB	93.4%	79.6%	18.5%	80.0%	30.1%	87.8%	58.8%	243.365	261.553	266.198	266.198	324.952	9.61	10.25	10.55	10.55	54.64
A-5	CART	92.3%	76.8%	2.5%	76.7%	4.8%	86.0%	51.1%	-514.477	-497.277	-494.414	-497.277	-112.372	-20.08	-19.28	-19.21	-19.28	-86.48
	RF	92.9%	74.9%	0.6%	77.9%	1.3%	85.7%	50.3%	-323.544	-323.543	-325.110	-323.543	-3937	-13.65	-13.64	-13.72	-13.64	-28.28
	XGB	93.4%	79.8%	0.4%	80.0%	0.7%	87.9%	50.2%	-383.004	-379.736	-379.736	-379.736	0	-15.14	-14.88	-14.88	-14.88	0
A-25	CART	92.3%	76.2%	50.2%	76.7%	60.1%	85.8%	73.6%	4.160.423	4.322.030	4.267.310	4.322.030	3.882.623	162.44	170.53	251.34	251.34	241.06
	RF	92.9%	75.3%	47.5%	78.0%	60.3%	85.8%	72.7%	4.018.432	3.687.705	3.687.705	3.687.705	3.666.219	169.65	154.49	154.49	154.49	249.54
	XGB	93.4%	80.1%	51.2%	80.1%	63.0%	88.0%	74.4%	4.455.108	4.633.404	4.578.684	4.633.404	4.410.629	176.09	179.36	180.16	179.36	267.87



**Fig. 24** Correlation between the proportion of non-targetted lapsers and the improvement of a CLV-augmented LMS.(Taking the results of XGBoost and excluding LMS n°B-27 that has a very high improvement ratio.)

### A.5 Complewete LMS numerical results

See Table 10.

**Table 10** More LMS

LMS	$p$	$\delta$	$\gamma$	$c$	$d$	$T$	LMS	$p$	$\delta$	$\gamma$	$c$	$d$	$T$
A-1	2.50%	0.04%	25%	10	1.50%	5	B-1	2.50%	0.08%	20%	10	1.50%	5
A-2	2.50%	0.04%	25%	10	1.50%	20	B-2	2.50%	0.08%	20%	10	1.50%	20
A-3	2.50%	0.04%	25%	100	1.50%	5	B-3	2.50%	0.08%	20%	100	1.50%	5
A-4	2.50%	0.04%	25%	100	1.50%	20	B-4	2.50%	0.08%	20%	100	1.50%	20
A-5	2.50%	0.04%	5%	10	1.50%	5	B-5	2.50%	0.08%	10%	10	1.50%	5
A-6	2.50%	0.04%	5%	10	1.50%	20	B-6	2.50%	0.08%	10%	10	1.50%	20
A-7	2.50%	0.04%	5%	100	1.50%	5	B-7	2.50%	0.08%	10%	100	1.50%	5
A-8	2.50%	0.04%	5%	100	1.50%	20	B-8	2.50%	0.08%	10%	100	1.50%	20
A-9	2.50%	0.10%	25%	10	1.50%	5	B-9	2.50%	0.20%	20%	10	1.50%	5
A-10	2.50%	0.10%	25%	10	1.50%	20	B-10	2.50%	0.20%	20%	10	1.50%	20
A-11	2.50%	0.10%	25%	100	1.50%	5	B-11	2.50%	0.20%	20%	100	1.50%	5
A-12	2.50%	0.10%	25%	100	1.50%	20	B-12	2.50%	0.20%	20%	100	1.50%	20
A-13	2.50%	0.10%	5%	10	1.50%	5	B-13	2.50%	0.20%	10%	10	1.50%	5
A-14	2.50%	0.10%	5%	10	1.50%	20	B-14	2.50%	0.20%	10%	10	1.50%	20
A-15	2.50%	0.10%	5%	100	1.50%	5	B-15	2.50%	0.20%	10%	100	1.50%	5
A-16	2.50%	0.10%	5%	100	1.50%	20	B-16	2.50%	0.20%	10%	100	1.50%	20
A-17	5.00%	0.04%	25%	10	1.50%	5	B-17	5.00%	0.08%	20%	10	1.50%	5
A-18	5.00%	0.04%	25%	10	1.50%	20	B-18	5.00%	0.08%	20%	10	1.50%	20
A-19	5.00%	0.04%	25%	100	1.50%	5	B-19	5.00%	0.08%	20%	100	1.50%	5
A-20	5.00%	0.04%	25%	100	1.50%	20	B-20	5.00%	0.08%	20%	100	1.50%	20

LMS	$p$	$\delta$	$\gamma$	$c$	$d$	$T$	LMS	$p$	$\delta$	$\gamma$	$c$	$d$	$T$
A-21	5.00%	0.04%	5%	10	1.50%	5	B-21	5.00%	0.08%	10%	10	1.50%	5
A-22	5.00%	0.04%	5%	10	1.50%	20	B-22	5.00%	0.08%	10%	10	1.50%	20
A-23	5.00%	0.04%	5%	100	1.50%	5	B-23	5.00%	0.08%	10%	100	1.50%	5
A-24	5.00%	0.04%	5%	100	1.50%	20	B-24	5.00%	0.08%	10%	100	1.50%	20
A-25	5.00%	0.10%	25%	10	1.50%	5	B-25	5.00%	0.20%	20%	10	1.50%	5
A-26	5.00%	0.10%	25%	10	1.50%	20	B-26	5.00%	0.20%	20%	10	1.50%	20
A-27	5.00%	0.10%	25%	100	1.50%	5	B-27	5.00%	0.20%	20%	100	1.50%	5
A-28	5.00%	0.10%	25%	100	1.50%	20	B-28	5.00%	0.20%	20%	100	1.50%	20
A-29	5.00%	0.10%	5%	10	1.50%	5	B-29	5.00%	0.20%	10%	10	1.50%	5
A-30	5.00%	0.10%	5%	10	1.50%	20	B-30	5.00%	0.20%	10%	10	1.50%	20
A-31	5.00%	0.10%	5%	100	1.50%	5	B-31	5.00%	0.20%	10%	100	1.50%	5
A-32	5.00%	0.10%	5%	100	1.50%	20	B-32	5.00%	0.20%	10%	100	1.50%	20

No	Time (s)	Model	% Target diff	Accuracy		Retention gain		RG/target		Improvement <sup>a</sup>
				$y_i$	$\tilde{y}_i$	$y_i$	$\tilde{y}_i$	$y_i$	$\tilde{y}_i$	
A-1	4949	CART	62.58%	92.3%	85.3%	114,661	219,655	4.48	38.20	91.57%
		RF		92.9%	85.4%	232,314	287,884	9.82	56.65	23.92%
		XGB		93.4%	85.8%	243,365	324,952	9.61	54.64	33.52%
A-2	6111	CART	26.66%	92.3%	89.8%	7,092,097	6,142,119	277.00	353.83	-13.39%
		RF		92.9%	90.2%	6,596,374	5,696,455	278.47	351.02	-13.64%
		XGB		93.4%	90.9%	7,308,721	7,432,688	288.92	404.84	1.70%
A-3	4603	CART	93.50%	92.3%	83.3%	-2,187,622	-8224	-85.52	-31.09	99.62%
		RF		92.9%	83.4%	-1,900,265	45,483	-80.18	194.35	102.39%
		XGB		93.4%	83.5%	-2,032,650	77,481	-80.39	174.44	103.81%
A-4	5555	CART	55.37%	92.3%	86.5%	4,789,814	5,117,844	187.00	577.74	6.85%
		RF		92.9%	86.4%	4,463,796	4,255,175	188.47	566.05	-4.67%
		XGB		93.4%	86.8%	5,032,706	5,433,366	198.92	610.26	7.96%
A-5	4753	CART	86.72%	92.3%	83.6%	-514,477	-112,372	-20.08	-86.48	78.16%
		RF		92.9%	83.4%	-323,544	-3937	-13.65	-28.28	98.78%
		XGB		93.4%	83.3%	-383,004	0	-15.14	0	100.00%
A-6	5803	CART	44.27%	92.3%	87.9%	335,810	517,224	13.17	39.91	54.02%
		RF		92.9%	87.9%	655,350	661,021	27.68	61.13	0.87%
		XGB		93.4%	88.6%	654,219	729,493	25.86	58.22	11.51%
A-7	4241	CART	99.09%	92.3%	83.3%	-2,816,759	-10,205	-110.08	-384.04	99.64%
		RF		92.9%	83.3%	-2,456,122	1013	-103.65	66.30	100.04%
		XGB		93.4%	83.3%	-2,659,020	243	-105.14	15.92	100.01%
A-8	5164	CART	82.78%	92.3%	84.0%	-1,966,473	-46,323	-76.83	-22.31	97.64%
		RF		92.9%	84.0%	-1,477,229	253,885	-62.32	149.67	117.19%
		XGB		93.4%	84.1%	-1,621,796	273,243	-64.14	117.83	116.85%

No	Time (s)	Model	% Target diff	Accuracy		Retention gain		RG/target		Improvement <sup>a</sup>
				$y_i$	$\bar{y}_i$	$y_i$	$\bar{y}_i$	$y_i$	$\bar{y}_i$	
A-9	4781	CART	77.60%	92.3%	83.7%	-825,372	-161,100	-32.19	-127.87	80.48%
		RF		92.9%	83.4%	-384,736	8,596	-16.22	32.12	102.23%
		XGB		93.4%	83.6%	-498,263	22,337	-19.70	35.47	104.48%
A-10	6075	CART	29.10%	92.3%	89.7%	4,614,513	4,483,831	180.36	266.33	-2.83%
		RF		92.9%	89.9%	4,973,929	4,328,724	210.01	280.90	-12.97%
		XGB		93.4%	90.7%	5,354,770	5,368,917	211.69	301.57	0.26%
A-11	4506	CART	96.56%	92.3%	83.2%	-3,127,655	-118,886	-122.19	-2230.39	96.20%
		RF		92.9%	83.3%	-2,517,315	1340	-106.22	87.71	100.05%
		XGB		93.4%	83.3%	-2,774,278	736	-109.70	52.00	100.03%
A-12	5534	CART	57.93%	92.3%	86.2%	2,312,231	3,310,314	90.36	412.71	43.17%
		RF		92.9%	86.1%	2,841,351	3,129,652	120.01	465.74	10.15%
		XGB		93.4%	86.6%	3,078,755	3,825,920	121.69	475.53	24.27%
A-13	4640	CART	92.91%	92.3%	83.3%	-1,201,626	-163,056	-46.87	-1838.44	86.43%
		RF		92.9%	83.3%	-717,620	-5339	-30.28	-354.24	99.26%
		XGB		93.4%	83.3%	-875,378	508	-34.60	16.26	100.06%
A-14	5739	CART	47.12%	92.3%	87.3%	-1,476,651	-831,019	-57.49	-77.99	43.72%
		RF		92.9%	86.0%	-380,683	126,532	-16.03	21.14	133.24%
		XGB		93.4%	85.5%	-644,389	29,382	-25.47	7.10	104.56%
A-15	4216	CART	99.61%	92.3%	83.3%	-3,503,908	-97,263	-136.87	-2354.34	97.22%
		RF		92.9%	83.3%	-2,850,198	0	-120.28	0	100.00%
		XGB		93.4%	83.3%	-3,151,393	0	-124.60	0	100.00%
A-16	5096	CART	84.46%	92.3%	83.8%	-3,778,933	-734,773	-147.49	-418.58	80.56%
		RF		92.9%	83.5%	-2,513,261	8914	-106.03	20.13	100.35%
		XGB		93.4%	83.6%	-2,920,405	34,492	-115.47	45.75	101.18%
No	Time (s)	Model	% Target diff	Accuracy		Retention gain		RG/target		Improvement <sup>a</sup>
				$y_i$	$\bar{y}_i$	$y_i$	$\bar{y}_i$	$y_i$	$\bar{y}_i$	
A-17	5390	CART	28.74%	92.3%	89.5%	5,100,456	4,899,479	199.11	279.88	-3.94%
		RF		92.9%	89.8%	4,635,482	4,226,648	195.69	276.06	-8.82%
		XGB		93.4%	90.2%	5,196,736	5,138,253	205.40	299.27	-1.13%
A-18	6452	CART	12.12%	92.3%	91.3%	52,090,240	47,706,070	2034.15	2170.64	-8.42%
		RF		92.9%	91.9%	46,171,160	42,049,900	1949.05	2082.36	-8.93%
		XGB		93.4%	92.5%	51,629,950	52,606,740	2040.95	2339.70	1.89%
A-19	4913	CART	64.89%	92.3%	85.2%	2,798,173	3,182,143	109.11	481.60	13.72%
		RF		92.9%	85.2%	2,502,903	2,743,070	105.69	554.76	9.60%
		XGB		93.4%	85.6%	2,920,720	3,438,303	115.40	576.64	17.72%



No	Time (s)	Model	% Target diff	Accuracy		Retention gain		RG/target		Improvement <sup>a</sup>
				$y_i$	$\bar{y}_i$	$y_i$	$\bar{y}_i$	$y_i$	$\bar{y}_i$	
A-20	6160	CART	29.03%	92.3%	89.6%	49,787,960	45,366,730	1944.15	2616.32	-8.88%
		RF		92.9%	90.0%	44,038,580	39,947,830	1859.05	2547.89	-9.29%
		XGB		93.4%	90.6%	49,353,940	49,789,670	1950.95	2796.17	0.88%
A-21	5079	CART	51.69%	92.3%	86.8%	482,682	544,887	18.85	53.99	12.89%
		RF		92.9%	86.8%	557,090	554,195	23.52	65.17	-0.52%
		XGB		93.4%	87.1%	607,670	624,556	24.01	64.79	2.78%
A-22	6199	CART	23.94%	92.3%	90.2%	9,335,438	8,527,444	364.60	454.78	-8.66%
		RF		92.9%	90.6%	8,570,307	7,931,029	361.80	460.42	-7.46%
		XGB		93.4%	91.2%	9,518,466	9,581,934	376.27	501.56	0.67%
A-23	4601	CART	89.51%	92.3%	83.6%	-1,819,600	135,305	-71.15	121.80	107.44%
		RF		92.9%	83.5%	-1,575,489	159,620	-66.48	215.65	110.13%
		XGB		93.4%	83.7%	-1,668,346	228,226	-65.99	208.69	113.68%
A-24	5650	CART	50.83%	92.3%	87.0%	7,033,156	7,124,100	274.60	680.08	1.29%
		RF		92.9%	87.0%	6,437,729	6,364,477	271.80	711.89	-1.14%
		XGB		93.4%	87.4%	7,242,450	7,840,770	286.27	771.71	8.26%
A-25	5379	CART	30.97%	92.3%	89.2%	4,160,423	3,882,623	162.44	241.06	-6.68%
		RF		92.9%	89.5%	4,018,432	3,666,219	169.65	249.54	-8.76%
		XGB		93.4%	90.0%	4,455,108	4,410,629	176.09	267.87	-1.00%
A-26	6410	CART	12.52%	92.3%	91.3%	49,612,660	45,948,690	1937.51	2083.30	-7.39%
		RF		92.9%	91.9%	44,548,720	40,814,960	1880.59	2029.68	-8.38%
		XGB		93.4%	92.5%	49,676,000	50,549,740	1963.72	2260.20	1.76%
A-27	4887	CART	66.67%	92.3%	85.1%	1,858,140	2,575,538	72.44	442.86	38.61%
		RF		92.9%	85.0%	1,885,853	2,387,018	79.65	531.25	26.57%
		XGB		93.4%	85.4%	2,179,093	2,879,880	86.09	544.35	32.16%
A-28	6047	CART	29.42%	92.3%	89.4%	47,310,370	43,168,880	1847.51	2519.41	-8.75%
		RF		92.9%	89.9%	42,416,140	38,573,620	1790.59	2504.61	-9.06%
		XGB		93.4%	90.5%	47,399,990	47,812,830	1873.72	2721.63	0.87%
A-29	5070	CART	53.79%	92.3%	86.5%	-204,467	-5098	-7.95	-1.66	97.51%
		RF		92.9%	86.1%	163,014	273,435	6.90	40.30	67.74%
		XGB		93.4%	86.8%	115,297	248,982	4.55	28.64	115.95%
A-30	6179	CART	24.36%	92.3%	90.3%	7,522,978	7,058,487	293.94	382.06	-6.17%
		RF		92.9%	90.6%	7,534,275	7,068,293	318.08	411.80	-6.18%
		XGB		93.4%	91.2%	8,219,857	8,265,167	324.94	442.88	0.55%
A-31	4627	CART	90.18%	92.3%	83.6%	-2,506 749	-139,983	-97.95	-121.44	94.42%
		RF		92.9%	83.5%	-1,969,564	73,101	-83.10	111.49	103.71%
		XGB		93.4%	83.6%	-2,160,719	76,641	-85.45	93.28	103.55%
A-32	5679	CART	51.25%	92.3%	86.8%	5,220,695	5,811,833	203.94	583.55	11.32%
		RF		92.9%	86.9%	5,401,696	5,269,505	228.08	605.69	-2.45%
		XGB		93.4%	87.4%	5,943,841	6,682,230	234.94	670.03	12.42%

No	Time (s)	Model	% Target diff	Accuracy		Retention gain		RG/target		Improvement <sup>a</sup>
				$y_i$	$\bar{y}_i$	$y_i$	$\bar{y}_i$	$y_i$	$\bar{y}_i$	
B-1	4778	CART	75.89%	92.3%	84.0%	-627,165	-148,913	-24.46	-65.19	76.26%
		RF		92.9%	83.7%	-280,855	11,973	-11.84	9.57	104.26%
		XGB		93.4%	84.1%	-366,103	25,099	-14.47	12.30	106.86%
B-2	6074	CART	29.70%	92.3%	89.7%	3,862,156	3,397,247	150.95	203.11	-12.04%
		RF		92.9%	89.9%	4,127,224	3,550,730	174.26	230.67	-13.97%
		XGB		93.4%	90.6%	4,451,686	4,408,819	175.99	250.17	-0.96%
B-3	4528	CART	96.60%	92.3%	83.2%	-2,929,448	-85,465	-114.46	-1482.06	97.08%
		RF		92.9%	83.3%	-2,413,433	3724	-101.84	-108.33	100.15%
		XGB		93.4%	83.3%	-2,642,119	9092	-104.47	93.79	100.34%
B-4	5476	CART	60.93%	92.3%	85.9%	1,559,874	2,471,262	60.95	329.63	58.43%
		RF		92.9%	85.8%	1,994,645	2,517,111	84.26	422.45	26.19%
		XGB		93.4%	86.3%	2,175,670	3,089,897	85.99	422.77	42.02%
B-5	4708	CART	84.33%	92.3%	83.4%	-857,439	-159,856	-33.45	-218.16	81.36%
		RF		92.9%	83.3%	-484,459	40	-20.44	7.23	100.01%
		XGB		93.4%	83.3%	-596,203	897	-23.57	46.96	100.15%
B-6	5906	CART	36.63%	92.3%	88.8%	705,721	922,490	27.69	60.21	30.72%
		RF		92.9%	88.9%	1,352,182	1,269,349	57.11	97.63	-6.13%
		XGB		93.4%	89.6%	1,342,882	1,428,722	53.09	96.76	6.39%
B-7	4400	CART	98.49%	92.3%	83.2%	-3,159,722	-39,633	-123.45	-1230.61	98.75%
		RF		92.9%	83.3%	-2,617,037	1024	-110.44	0.56	100.04%
		XGB		93.4%	83.3%	-2,872,219	295	-113.57	19.31	100.01%
B-8	5278	CART	73.18%	92.3%	84.6%	-1,596,562	169,852	-62.31	41.78	110.64%
		RF		92.9%	84.6%	-780,396	637,625	-32.89	194.52	181.71%
		XGB		93.4%	85.0%	-933,133	780,845	-36.91	188.79	183.68%
B-9	4601	CART	94.12%	92.3%	83.3%	-2,380,789	-113,444	-92.86	-840.25	95.24%
		RF		92.9%	83.3%	-1,403,468	317	-59.21	7.96	100.02%
		XGB		93.4%	83.3%	-1,724,731	3980	-68.17	149.44	100.23%
B-10	5947	CART	35.98%	92.3%	89.0%	-760,449	429,196	-29.35	29.80	156.44%
		RF		92.9%	88.5%	1,175,540	1,354,131	49.71	118.11	15.19%
		XGB		93.4%	89.8%	871,455	1,456,080	34.48	96.25	67.09%
B-11	4229	CART	99.16%	92.3%	83.3%	-4,683,072	-48,985	-182.86	-1186.22	98.95%
		RF		92.9%	83.3%	-3,536,046	0	-149.21	0	100.00%
		XGB		93.4%	83.3%	-4,000,747	0	-158.17	0	100.00%
B-12	5391	CART	66.76%	92.3%	85.0%	-3,062,732	-388,289	-119.35	-80.44	87.32%
		RF		92.9%	84.7%	-957,039	710,688	-40.29	220.55	174.26%
		XGB		93.4%	85.3%	-1,404,561	834,198	-55.52	163.88	159.39%
B-13	4493	CART	96.30%	92.3%	83.3%	-2,358,179	-159,922	-91.98	-2793.13	93.22%
		RF		92.9%	83.3%	-1,384,098	0	-58.40	0	100.00%
		XGB		93.4%	83.3%	-1,705,577	0	-67.42	0	100.00%

No	Time (s)	Model	% Target diff	Accuracy		Retention gain		RG/target		Improve- ment <sup>a</sup>
				$y_i$	$\tilde{y}_i$	$y_i$	$\tilde{y}_i$	$y_i$	$\tilde{y}_i$	
B-14	5851	CART	42.98%	92.3%	87.8%	-3,251,762	-1,761,821	-126.63	-143.20	45.82%
		RF		92.9%	86.4%	-1,013,089	79,273	-42.69	11.90	107.82%
		XGB		93.4%	83.3%	-1,582,006	4396	-62.52	287.68	100.28%
B-15	4040	CART	99.67%	92.3%	83.3%	-4,660,462	-38,969	-181.98	-2075.03	99.16%
		RF		92.9%	83.3%	-3,516,676	0	-148.40	0	100.00%
		XGB		93.4%	83.3%	-3,981,592	161	-157.42	10.53	100.00%
B-16	5182	CART	77.97%	92.3%	84.2%	-5,554,044	-1,491,522	-216.63	-549.23	73.15%
		RF		92.9%	83.6%	-3,145,668	52,475	-132.69	84.54	101.67%
		XGB		93.4%	83.3%	-3,858,022	0	-152.52	0	100.00%
No	Time (s)	Model	% Target diff	Accuracy		Retention gain		RG/target		Improve- ment <sup>a</sup>
				$y_i$	$\tilde{y}_i$	$y_i$	$\tilde{y}_i$	$y_i$	$\tilde{y}_i$	
B-17	5324	CART	32.66%	92.3%	88.9%	3,361,471	3,037,200	131.25	191.31	-9.65%
		RF		92.9%	89.3%	3,241,680	2,911,023	136.86	204.43	-10.20%
		XGB		93.4%	89.6%	3,596,593	3,546,671	142.15	222.04	-1.39%
B-18	6411	CART	13.83%	92.3%	91.1%	39,860,670	37,695,680	1556.66	1778.71	-5.43%
		RF		92.9%	91.7%	35,787,050	32,345,100	1510.72	1654.32	-9.62%
		XGB		93.4%	92.0%	39,908,670	40,886,810	1577.61	1848.71	2.45%
B-19	4853	CART	70.34%	92.3%	84.7%	1,059,189	1,813,631	41.25	392.14	71.23%
		RF		92.9%	84.8%	1,109,101	1,808,616	46.86	474.33	63.07%
		XGB		93.4%	85.0%	1,320,578	2,141,271	52.15	482.34	62.15%
B-20	5973	CART	31.76%	92.3%	89.2%	37,558,390	34,068,550	1466.66	2125.97	-9.29%
		RF		92.9%	89.4%	33,654,470	30,032,580	1420.72	2072.47	-10.76%
		XGB		93.4%	90.1%	37,632,650	38,008,480	1487.61	2277.17	1.00%
B-21	5228	CART	41.79%	92.3%	87.7%	1,136,879	1,179,837	44.40	92.50	3.78%
		RF		92.9%	88.1%	1,276,808	1,188,256	53.91	104.81	-6.94%
		XGB		93.4%	88.7%	1,385,145	1,356,864	54.74	104.76	-2.04%
B-22	6296	CART	19.52%	92.3%	90.7%	18,704,980	17,177,190	730.55	852.81	-8.17%
		RF		92.9%	91.1%	17,182,100	15,732,340	725.34	859.29	-8.44%
		XGB		93.4%	91.5%	19,071,370	19,050,020	753.90	939.00	-0.11%
B-23	4746	CART	81.36%	92.3%	84.1%	-1,165,404	458,223	-45.60	172.83	139.32%
		RF		92.9%	84.0%	-855,770	525,335	-36.09	288.55	161.39%
		XGB		93.4%	84.1%	-890,871	645,445	-35.26	310.86	172.45%
B-24	5845	CART	40.47%	92.3%	88.2%	16,402,700	15,013,310	640.55	1093.43	-8.47%
		RF		92.9%	88.4%	15,049,520	13,423,040	635.34	1122.81	-10.81%
		XGB		93.4%	88.9%	16,795,360	17,144,260	663.90	1247.50	2.08%
B-25	5274	CART	37.42%	92.3%	88.6%	1,607,847	1,839,864	62.84	126.33	14.43%
		RF		92.9%	88.7%	2,119,067	1,923,982	89.49	152.71	-9.21%
		XGB		93.4%	89.2%	2,237,965	2,194,469	88.45	155.54	-1.94%
B-26	6425	CART	14.83%	92.3%	91.1%	35,238,060	32,690,970	1376.37	1558.26	-7.23%
		RF		92.9%	91.6%	32,835,370	29,986,540	1386.17	1543.12	-8.68%
		XGB		93.4%	92.0%	36,328,440	36,803,630	1436.10	1688.53	1.31%

No	Time (s)	Model	% Target diff	Accuracy		Retention gain		RG/target		Improvement <sup>a</sup>
				$y_i$	$\tilde{y}_i$	$y_i$	$\tilde{y}_i$	$y_i$	$\tilde{y}_i$	
B-27	4811	CART	73.92%	92.3%	84.3%	-694,436	751,404	-27.16	226.99	208.20%
		RF		92.9%	84.4%	-13,512	1,018,369	-0.51	356.48	7636.98%
		XGB		93.4%	84.7%	-38,050	1,253,252	-1.55	345.94	3393.68%
B-28	5995	CART	32.61%	92.3%	89.1%	32,935,780	29,342,930	1286.37	1847.71	-10.91%
		RF		92.9%	89.4%	30,702,790	27,725,620	1296.17	1933.38	-9.70%
		XGB		93.4%	90.0%	34,052,420	34,390,060	1346.10	2094.90	0.99%
B-29	5143	CART	47.03%	92.3%	87.3%	-363,861	55,985	-14.12	3.38	115.39%
		RF		92.9%	87.4%	377,170	488,284	15.95	49.62	29.46%
		XGB		93.4%	88.0%	275,772	491,567	10.89	44.89	78.25%
B-30	6243	CART	20.47%	92.3%	90.7%	14,747,500	13,838,380	576.23	690.22	-6.16%
		RF		92.9%	91.1%	14,816,830	13,378,460	625.54	743.34	-9.71%
		XGB		93.4%	91.5%	16,146,490	16,169,440	638.30	814.80	0.14%
B-31	4730	CART	83.83%	92.3%	83.7%	-2,666,144	-487,716	-104.12	-267.75	81.71%
		RF		92.9%	83.7%	-1,755,409	139,545	-74.05	102.66	107.95%
		XGB		93.4%	83.7%	-2,000,244	134,199	-79.11	130.13	106.71%
B-32	5865	CART	41.41%	92.3%	88.0%	12,445,210	11,693,070	486.23	884.49	-6.04%
		RF		92.9%	88.3%	12,684,250	11,381,260	535.54	971.28	-10.27%
		XGB		93.4%	88.8%	13,870,470	14,101,470	548.30	1048.38	1.67%

<sup>a</sup> In order to account for negative retention gains, the improvement is computed with an absolute value for the denominator. This leads to a rather unintuitive improvement measure whenever one of the models yields negative RG and the other positive RG

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**Data availability** For privacy reasons, all the data, statistics, product names and perimeters presented in this paper have been either anonymized or modified. All analyses, discussions and conclusions remain unchanged.

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