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Si plate radius influence on the photoacoustic signal processed by neural networks

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Abstract

The effect of the sample radius on the total photoacoustic signal processed by neural networks trained with undistorted and distorted signals is carefully analyzed for modulation frequencies from 20 Hz to 20 kHz. This is done for signals generated for a 400- μm -thick Si n-type plate, whose radius varies from 2 to 7 mm. It is found that the networks trained with both undistorted or distorted signals yield the best predictions for sample radii between 2 and 3 mm, which is close to the used microphone aperture radius of 1.5 mm. The network trained only with undistorted signals gives the best results for sample radii comparable to the microphone dimensions. The obtained results neural networks in the prediction of Si-plate radius indicate the experimental necessity to use samples with radii slightly over to microphone aperture.

Keywords: photoacoustic, semiconductors, artificial neural networks, thermal diffusion, thermal expansion, photothermal, inverse problem

1. Introduction

The photoacoustic effect is the effect of the sound appearance due to the illumination of a sample with an optical beam whose intensity is time-dependent [1-5]. Numerous non-destructive methods for the characterization and imaging of various solids, multilayer structures, microelectronic and photonic devices, soft matter, and biological tissues are based on this effect [6-21]. The use of neural networks in photoacoustics has become very popular recently, especially in imaging within biomedical applications [23-25]. Significant progress has been made, also, in photoacoustics of solids with different types of networks both in material characterization and in the development of experimental procedures [26-28]. Networks have proven to be a very effective tool for predicting the physical characteristics of solid samples [29-31]. Within the framework of multi-parameter fitting in photoacoustics, the networks most often predicted the values of the sample parameters such as thermal diffusion (D_T) and thermal expansion (α_T) together with the thickness of the sample (l) [32,33]. These parameters are important because they occur when calculating the temperature distributions of the sample and all components of the photoacoustic signal generated by the periodic illumination of the sample.

It has long been known that the geometric parameters of the sample are very important for the correct interpretation of the photoacoustic signal in the frequency domain [34-36]. If the circular plate shape samples are tested, one of such parameters is its radius R_s . It explicitly appears in the equation for calculating the thermoelastic and plasmaelastic components of the photoacoustic signal of a semiconductor, so that its influence on the shape of the total signal through these two components can be extremely significant [32,33]. In this paper, the analysis of the influence of the semiconductor sample radius changes on all components of the photoacoustic signal, thermodiffusion (TD), thermoelastic (TE), and plasmaelastic (PE), is presented, based on the theoretical model of a composite piston [1-3] that serves to form an appropriate base of photoacoustic signals for neural network training [26,27]. The tested sample is a Si n-type 400 μm thick wafer, classified as a plasma-thick sample – a sample with a thickness larger than the diffusion length of free carriers [32,33]. Plasma-thick semiconductor samples have a thermal response of known and characteristic patterns of behavior of the total signal and its components in the modulation frequencies ranging from 20 Hz to 20 kHz [33].

These patterns include domination of the TD component at lower, and the TE component at higher frequencies, while the PE component's influence on the total signal is negligible.

The basic idea of this paper is to determine which type of neural network gives better predictions in the case of a change in the radius of the sample: one that is trained by distorted signals, or by signals undistorted with instrumental deviations [37-39]. This analysis is very important because its results can give the possibility of working with distorted signals, which significantly simplifies and speeds up the process of characterization of the tested samples. Both types of network training signals were obtained theoretically, and the final verification of network efficiency was tested on experimental data. The conclusions of this analysis indicate, in experimental terms, the importance of the choice of sample radius about the dimensions of the microphone as a photoacoustic cell and signal detector. Also, based on the obtained network predictions a conclusion can be drawn on the justification of using approximations in the theoretical model of the composite piston, especially those related to the equality of microphone aperture and sample radii.

2. Theoretical introduction

The theoretical model of the composite piston presented in this paper is adapted to the experimental setup of an open photoacoustic cell [32,33,37,40]. It is assumed that a frequency-modulated light source of wavelength 660nm illuminates the Si n-type plate. Due to the photoacoustic effect of the absorbed modulated light and the sample interaction, a sound is recorded by an open photoacoustic cell in the transmission configuration (Figure 1). The photoacoustic signal detector is assumed to be an electret microphone (ECM 30B, JinInElectronicCo., Ltd.) with a radius of $R_0 = 4.9$ mm, and aperture radius of $r_0 = 1.5$ mm [33]. The sample is placed directly on the microphone with points of support that are slightly smaller but close to the radius of the sample R_s , so that the microphone at the same time can serve as a measuring cell of minimal volume $V_0 = \pi r_0^2 l_c$, where l_c is the distance from the microphone aperture to its membrane (length of OPC) (see Figure 1).

Figure 1. Simple ideal scheme of the transmission configuration of an open photoacoustic cell with an electret microphone and samples of different radii.

The measured signal in the transmission configuration and in the frequency range from 20Hz to 20 kHz is a sound signal that occurs due to the photoacoustic effect in the sample itself and is usually distorted by the influence of used instruments and the different types of noise. The signal thus measured is called the distorted signal $S_{\text{total}}(f)$. If a well-known signal correction procedure [33,37-39] is applied to such a signal, the so-called 'true' or undistorted signal $\delta p_{\text{total}}(f)$ can be obtained, generated from an illuminated sample. The theoretical model that fully describes the undistorted signals is based on the composite piston model [1-3]. This model explains that the total photoacoustics signal $\delta p_{\text{total}}(f)$ of a semiconductor is equal to the sum of its components; thermodiffusion $\delta p_{\text{TD}}(f)$, thermoelastic $\delta p_{\text{TE}}(f)$ and plasmaelastic $\delta p_{\text{PE}}(f)$ [33,40]:

$$\delta p_{\text{total}}(f) = \delta p_{\text{TD}}(f) + \delta p_{\text{TE}}(f) + \delta p_{\text{PE}}(f). \quad (1)$$

The thermodiffusion component can be written as follows [33,41]:

$$\delta p_{\text{TD}}(t) = \frac{\gamma p_0}{l_c} \frac{\mu_g}{\sqrt{2T_0}} T(l) e^{i\left(\omega t - \frac{\pi}{4}\right)}, \quad (2)$$

where $\omega = 2\pi f$, f is modulation frequency, γ is an adiabatic ratio, p_0 and T_0 are the ambient pressure and temperature, μ_g is the thermal diffusion length of the surrounding gas, $T_s(l)$ (see Appendix I) is the dynamic temperature component at the back sample surface, l is the sample thickness and l_c is the length of the cell (microphone).

Due to different temperature values on the illuminated and non-illuminated side of the silicon sample, its periodic bending and expansion occur. The effect of bending and spreading is most simply described by cylindrical (z, r) coordinates so that the thermoelastic component $\delta p_{\text{TE}}(f)$ of the photoacoustic signal can be written in the form [33,40]:

$$\delta p_{\text{TE}}(f) = \alpha_{\text{T}} \frac{3\pi p_0 \gamma R_s^4}{V_0 l^3} \int_{-l/2}^{l/2} z T(z) dz, \quad (3)$$

where $T(z)$ is the temperature distribution in the sample along the z -axes (see Appendix I), α_{T} is the coefficient of thermal expansion, V_0 is the microphone (cell) volume, and R_s is the sample radius. In most of the theoretical analyses, the $R_s \approx R_0$ approximation is taken to simplify the analysis, [32,33,37,39].

By modulated illumination of the sample with the light of proper wavelength, free carriers (electrons and holes) are generated, which leads to additional stress and periodic bending of the sample. The influence of photogenerated carriers on the bending of the sample is described by the plasmaelastic component $\delta p_{\text{PE}}(f)$ [33,40]:

$$\delta p_{\text{PE}}(f) = d_n \frac{p_0 \gamma}{V_0} \frac{3\pi R_s^4}{l^3} \int_{-l/2}^{l/2} z \delta n_p(z) dz, \quad (4)$$

where $\delta n_p(z)$ is the minority carrier density (see Appendix II), and d_n is the coefficient of electronic deformation. Analysing Eq.(3&4) one can see that $\delta p_{\text{TE}}(f)$ and $\delta p_{\text{PE}}(f)$ depends on R_s^4 , meaning that small changes in R_s leads to large changes in $\delta p_{\text{TE}}(f)$ and $\delta p_{\text{PE}}(f)$.

It must be bear in mind that during the measurement there are a lot of signal distortions due to the influence of the used instruments (microphones and accompanying electronics). These distortions have signal filtering characteristics and are described, in the low-frequency range, by the function of the first-order low-pass filter $H_e(f)$ in the form [37,39]:

$$H_e(f) = -\frac{\omega \tau_{c1}}{(1+i\omega \cdot \tau_{c1})} \cdot \frac{\omega \tau_{c2}}{(1+i\omega \cdot \tau_{c2})}, \quad (5)$$

where $\omega = 2\pi f$, f is the modulation frequency, $\tau_{c1} = (2\pi f_{c1})^{-1} = R_1 C_1$ and $\tau_{c2} = (2\pi f_{c2})^{-1} = R_2 C_2$ are the time constants and RC characteristics of the microphone and accompanying electronics (usually sound-card or lock-in).

In the high-frequency range, these distortions are described by the function of the second-order low-pass filter $H_a(f)$ in the form [37,39]:

$$H_a(f) = \frac{\omega_{c3}^2}{\omega_{c3}^2 + i\delta_{c3}\omega_{c3}\omega - \omega^2} + \frac{\omega_{c4}^2}{\omega_{c4}^2 + i\delta_{c4}\omega_{c4}\omega - \omega^2}, \quad (6)$$

where δ_k is the damping factor ($k = c3, c4$), ω_{c3} is the microphone cut-off frequency and ω_{c4} is the characteristic frequency which depends on the geometry of the microphone body.

The total measured signal $S_{\text{total}}(f)$ can be written as a product of $\delta p_{\text{total}}(f)$, $H_e(f)$ and $H_a(f)$ [33,37,39]:

$$S_{\text{total}}(f) = \delta p_{\text{total}}(f) H_e(f) H_a(f). \quad (7)$$

Characteristic parameters $H_e(f)$ and $H_a(f)$ can be obtained either from the microphone manual or by independent measurements [33,37,39]. By finding them, $H_e(f)$ and $H_a(f)$ can be removed from $S_{\text{total}}(f)$ in Eq. (7) so the required $\delta p_{\text{total}}(f)$ can be obtained [33,37], which is further described by the composite piston theory (Eqs.(1-4)).

3. Neural networks

Our motive for the study of neural networks is their use in the precise characterization of the properties of the tested materials. In the process of supervised learning by connecting the data of input neurons (values of photoacoustic signals), with the data of output neurons (radius), the weights are adjusted to the moment when the output becomes increasingly like the desired data values. In our work with networks so far, we have learned that for the sake of prediction, we need to present undistorted data to the trained network, data that are adapted to the theoretical model used to create the training base. This assumes that during the processing of experimental

results, we must also count on the signal correction procedure. If it turns out that signal correction is not required to determine some of the sample parameters (expected in the case of only R_s changes), this will mean significant time savings. Therefore, in this paper, we will try to train networks with distorted (NN1) and undistorted (NN2) photoacoustic signals with the desire to determine the radius of the investigated sample, as a very important experimental parameter. Our goal is to see if there are differences in the prediction of the radius of the sample of such formed networks and whether, based on that, we can speed up the process of processing experimental data.

Figure 2. Representation of a single-layer neural network used for the analysis of distorted and undistorted photoacoustic signals that depend on the radius of silicon samples.

For the sake of simplicity, and based on the problem we want to solve, we decided that both networks used here have the simplest architecture, the so-called shallow networks: input layer, one hidden layer, and output layer [26,27]. The input layer was determined by the 144 neurons ($i = 72$ values of the photoacoustic signal amplitude A_i , and $i = 72$ values of photoacoustic signal phase φ_i characteristic), the hidden layer was determined by 10 neurons, and the output layer was determined by one neuron (the prediction of R_s , Figure 2). The choice of neural network architecture ensures good accuracy and optimal training time. Due to the better precision of the neural network, we adjusted the amplitudes by logarithmic normalization $20\log_{10}A_i$ to obtain the phase values range (A_i represents amplitudes normalized to unit pressure).

4. Results and discussion

4.1. Signal database formation

Due to the high sensitivity of these components to R_s changes in the total photoacoustic signal, we formed a `small` base of 26 undistorted $\delta p_{\text{total}}(f)$ and 26 distorted $S_{\text{total}}(f)$ theoretical photoacoustic signals obtained by Eqs.(1-7). As we said earlier, we assume that the sample is Si n-type plate, 400 μm thick. Bases are determined by amplitude-phase characteristics in the

frequency domain from 20 Hz to 20 kHz, changing the R_s from 2 mm to 7 mm in the steps of 0.2 mm. To simplify our considerations, we assumed that the excitation light intensity $I_0 = \text{const}$. The dependences of the a) amplitudes and b) phases of the $S_{\text{total}}(f)$ and $\delta p_{\text{total}}(f)$ signals on R_s in the frequency domain are clearly shown in Figures 3 and 4, respectively. The influence of the R_s is clearly expressed in both Figures at frequencies $f > 100$ Hz in the amplitudes (saddle shape) and in phases (distend areas). The black arrows indicate the directions of changes due to the R_s value increase. Unchanged amplitudes and phases in the low-frequency region ($f < 100$ Hz) indicate an area where the $S_{\text{total}}(f)$ and $\delta p_{\text{total}}(f)$ are insensitive to R_s changes.

Figure 3&4 clearly shows the instrumental influences as electronic filtering (Eq. (5)) at lower (H_e at $f < 100$ Hz) and acoustic filtering (Eq. (6)) at higher frequencies (H_a at $f > 5$ kHz) [33,37-39]. Electronic filters H_e reduce amplitudes (Figure 3&4.a) and raises phases (Figure 3&4.b) at low frequencies. Acoustic filters are characterized by resonant peaks in both amplitudes and phases. The parameters that define H_e and H_a are not dependent on R_s and are constant during its changes. Therefore, the reasons for changing $S_{\text{total}}(f)$ and $\delta p_{\text{total}}(f)$ by changing R_s are the same, and consist of the following: both signals are characterized with a saddle shape in amplitudes, which is more pronounced for $R_s = 2$ mm, while with an increasing radius the saddle shape slowly disappears and at $R_s = 7$ mm completely vanishes.

The insensitivity of the $S_{\text{total}}(f)$ and $\delta p_{\text{total}}(f)$ signals to R_s changes at lower frequencies allows one the possibility of, so-called, signal self-normalization that can contribute to the better performances of network training. On the other hand, the saddle shape of the $S_{\text{total}}(f)$ and $\delta p_{\text{total}}(f)$ signals is a typical pattern of plasma-thick silicon samples behavior in the frequency domain (strong TD and TE influence), allowing one to obtain better network parameter prediction. Both mentioned signal characteristics, insensitivity, and saddle shape are the reason why, in this paper, we decided to create a training base with distorted and undistorted signals of the plasma-thick samples, expecting efficient neural network optimization.

Figure 3. The bases of distorted PA signal $S_{\text{total}}(f)$: a) amplitudes, A , and b) phase, φ , from Si n-type as a function of simple radius R_s and modulation frequency, f .

Figure 4. The bases of undistorted PA signal $\delta p_{\text{total}}(f)$: a) amplitudes, A , and b) phase, φ , from Si n-type as a function of simple radius R_s and modulation frequency, f .

The question may be asked why the signals $S_{\text{total}}(f)$ and $\delta p_{\text{total}}(f)$ changes in amplitudes and phases due to R_s variations are most visible at $f > 100$ Hz. The explanation can be given by the theory based on the composite piston model (Eqs. (1-4)), in which the radius of the sample does not affect all components of the photoacoustic signal equally. Changes in R_s do not affect changes in the amplitude of $\delta p_{\text{TD}}(f)$ component at all (Figure 5.a), but they do change the amplitudes of $\delta p_{\text{TE}}(f)$ (Figure 6.a) and $\delta p_{\text{PE}}(f)$ components (Figure 7.a). In both $\delta p_{\text{TE}}(f)$ and $\delta p_{\text{PE}}(f)$ cases, the amplitudes increase with R_s . In all cases (Figures 5.b, 6.b & 7.b) phases do not change at all.

Figure 5. Thermodiffusion component $\delta p_{\text{TD}}(f)$ a) amplitudes A and b) phases φ as a function of simple radius R_s , and modulation frequency, f .

Figure 6. Thermoelastic component $\delta p_{\text{TE}}(f)$ a) amplitudes A and b) phases φ as a function of simple radius R_s , and modulation frequency, f .

Figure 7. Plasmaelastic component $\delta p_{\text{PE}}(f)$ a) amplitudes A and b) phases φ as a function of simple radius R_s , and modulation frequency, f .

To fully understand what presented signal component amplitude and phase changes mean, it is necessary to draw all the components and the total signal together, because not only the values of the components are important but also their mutual relationship, which is shown in Figure 8. This figure shows the amplitudes and phases of total signals and their components for $R_s = 2$ mm (solid lines) and $R_s = 7$ mm (dashed lines). The amplitude changes of the $\delta p_{\text{PE}}(f)$ component (blue) is smaller in absolute values compared to the changes in the $\delta p_{\text{TE}}(f)$ (green). This is the reason why $\delta p_{\text{PE}}(f)$ components do not affect the change in the total signal

$\delta p_{\text{total}}(f)$ (black). Therefore, only the mutual relationship between $\delta p_{\text{TD}}(f)$ (red) and $\delta p_{\text{TE}}(f)$ (green) amplitudes drives the $\delta p_{\text{total}}(f)$ behaviour in the frequency domain.

If $R_s = 2$ mm, the intersection of $\delta p_{\text{TD}}(f)$ and $\delta p_{\text{TE}}(f)$ is at $f \sim 2.4$ kHz, and therefore the $\delta p_{\text{total}}(f)$ (solid black) has a saddle shape at higher frequencies. When $R_s = 7$ mm, the intersection of $\delta p_{\text{TD}}(f)$ and $\delta p_{\text{TE}}(f)$ is at $f \sim 600$ Hz, and therefore $\delta p_{\text{total}}(f)$ (dashed black) is flattened (it has lost its saddle shape). Changes in the total signal for these and all other R_s values used to make the presented base will be visible in the range $f > 200$ Hz. The same conclusion was states for the distorted $S_{\text{total}}(f)$ signal, too. The analysis of the change of radius outside the range from 2 mm to 7 mm shows the loss of the influence of thermoelastic components on the total signal in the case of $R_s < 2$ mm, and their dominance in the total signal for $R_s > 7$ mm.

Figure 8. The tendency of changes in a) amplitudes A and b) phases φ of total photoacoustic signals $\delta p_{\text{total}}(f)$ (black lines) with its components: thermodiffusion $\delta p_{\text{TD}}(f)$ (red lines), thermoelastic $\delta p_{\text{TE}}(f)$ (green lines), and plasma elastic $\delta p_{\text{PE}}(f)$ (blue lines) for 400 μm .thick Si samples of radius $R_s = 2\text{mm}$ and $R_s = 7\text{mm}$.

The presented theoretical analysis of the total signal behavior by changing the radius of the sample shows that it makes sense to use both undistorted and distorted total signals to recognize R_s values because their amplitudes change significantly with changes in R_s only at higher modulation frequencies. The low-frequency range can be used as the total signal self-normalization range, due to the absence of any R_s influences on the total signal.

4.2. Network prediction results

The training results of NN1 neural networks trained by the base of distorted (Figure 3) and NN2 trained with the base of undistorted (Figure 4) signals are presented by the Mean Square Error (MSE) dependence of the number of Epochs in Figure 9. During network training, bases are divided into a training base, a testing base, and a validation base, based on which the generalized capabilities of networks are determined. To ensure the best performance of the

networks, the criterion of interrupting the MSE deviation of individual curves is activated. The NN1 network stopped its work in 3 epochs with the best validation performance of 0.014063 (Figure 9.a), while the NN2 network stopped its work in 4 Epochs, with the best validation performance of 0.0075805 (Figure 9.b).

a) b)

Figure 9. Network performance results: a) NN1 trained on distorted FA signals and b) NN2 trained on undistorted FA signals.

To evaluate the neural networks` NN1 and NN2`s ability to predict, we formed additional distorted and undistorted signal bases with values from 2.1 mm to 6.9 mm, formed using a step of 0.4 mm. These additional bases are used for network testing. In this way, we obtained 13 distorted +13 undistorted test signals evenly distributed throughout the range of R_s changes. The results of the neural network test on these signals are shown in Table I. The obtained relative errors are at the experimental measurements level of accuracy, which shows that for the network analysis of certain properties of samples, large photoacoustic signal databases are not necessary.

For the sake of clarity, the results in Table I are presented in Figure 10. It can be seen, based on the relative error percentage for NN1 and NN2, (Table I and Figure 10) that the prediction is good only in limited sample radius areas. A more accurate prediction of the NN1 (low % value of relative error) is for samples having $R_s \leq 3\text{mm}$ and samples with a radius larger than the microphone dimension ($R_s \geq 5\text{mm}$). A more precise prediction of the NN2 network ranges in a much wider range of radius values ($R_s \leq 4.5\text{mm}$), while higher values of R_s it give poorer predictions. The largest (%) relative errors are made by both NN1 and NN2 networks for the radius of the sample in the range (4.0-5.5) mm, ie. about a value equal to the radius of the microphone $R_0 = 4.9\text{ mm}$. These results lead to the conclusion that both networks give the best predictions when the value of R_s approaches the value of the microphone aperture radius ($r_0 = 1.5\text{ mm}$). This confirms the justification of the approximations $R_s = r_0$ taken here with the experimental configuration of the open cell. In general, the results show that for experimental work it is best to take samples whose dimensions are smaller than the dimensions of the microphone (R_0).

Table I: The results of NN1 and NN2 neural networks predictions of sample radius given in the table with relative (%) errors. Asterisk (*) denotes the predictions for experimentally measured PASs.

R_s [mm]	NN1 R_s [mm]	rel % error, NN1	NN2 R_s [mm]	rel % error, NN2
2.1	2.1356	1.6933	2.1023	0.1086
2.5	2.4849	0.6048	2.5400	1.5996
2.9	2.9038	0.1319	2.8572	1.4745
3.3	3.2037	2.9183	2.8572	0.3332
3.7	3.8832	4.9527	3.7098	0.2650
4.1	4.1947	2.3089	4.1427	1.0416
4.5	4.7968	6.5967	4.5426	0.9470
4.9	4.8915	0.1740	4.5426	7.2936
5.3	5.3213	0.4014	5.1965	1.9530
5.7	5.6535	0.8155	5.6941	0.1028
6.1	6.0561	0.7190	6.1364	0.5964
6.5	6.4283	1.1034	6.1364	5.5942
6.9	6.8216	1.1358	6.8506	0.7156
4.54*	4.7976	5.6749	4.6644	2.7398
2.63*	2.6521	0.8315	2.6247	0.2014

To confirm the previous results, both networks presented the experimental results of distorted and undistorted signals of a sample that had a radius approximately equal to the microphone radius $R_s \approx R_0$, and with a sample radius close to the aperture radius $R_s \geq r_0$.

The results of network prediction in the case of the signal from Figure 11 (black for $R_s = 4.54$ mm and green for $R_s = 2.63$ mm) obtained using the open photoacoustic cell experimental set-up are shown in Table I with an asterisk (*), and in Figure 10 with dots (red for NN1, black for NN2). Based on the experimental results, it can be concluded that the prediction of the experimentally corrected photoacoustic signals by the NN2 network is more accurate. Therefore, it can be recommended that networks trained on undistorted signals (NN2) should be used in determining the R_s of the tested sample only with values smaller than the microphone radius R_0 .

Figure 10. Dependence of relative% error prediction of NN1 (red line) and NN2 (black line) networks on the sample radius for the tests of theoretical results and experimental verification (NN1 (red dot), NN2 (black dot)).

Figure 11. Experimental result of a) amplitude I b) phase of distorted (star) and undistorted (line) photoacoustic signal presented to the NN2 and NN1, respectively, for a sample of 400 μ m thick silicon n-type with a radius of $R_s = 4.54$ mm (black), and $R_s = 2.63$ mm (green).

Conclusion

We have shown that the radius of the sample R_s is a very important parameter that can lead to changes in the shape of the amplitude and phase of the total photoacoustic signal and its elastic components (plasma elastic and thermoelastic) in the frequency domain from 20 Hz to 20 kHz. The analysis includes the total signals with respect to the influence of measuring instruments (distorted signals) and those generated directly by the illuminated sample (undistorted signals). It was found that the largest changes in the total signal due to R_s changes occur in its thermoelastic component amplitude, bearing in mind that amplitude is proportional to R_s^4 . It means that total signal amplitude changes are expected to find only at modulation frequencies $f > 100$ Hz, while at lower frequencies the total signal amplitude remains the same, ie. it is not sensitive to R_s changes at all. As it is expected, changes in the PE component amplitude are found to not affect total signal behavior. It was also found that amplitudes of the signals that are distorted under the influence of measuring instruments have similar behavior due to R_s changes. It was determined that the radius of the sample does not affect the change of the thermodiffusion component and that the largest changes in the total undistorted and distorted signals are due to changes in the relationship between the thermodiffusion and thermoelastic components, which are noticeable in the modulation frequency domain of $f > 100$ Hz. The same relationship changes the phase of total signals in the entire frequency domain.

Numerical simulation created bases of distorted and undistorted signals depending on the sample radius in the range of changes from 2 mm to 7 mm with a change step of 0.2 mm, which were used for NN1 and NN2 network training, respectively. Through training, it has been shown that both networks achieve satisfactory accuracy after only a few epochs. This means that shallow networks can achieve acceptable performances even with databases created from a small amount of data. Undistorted and distorted signals, out of the base, having the same range of R_s but with a different step of its changes are presented to such trained networks due to the test.

Predictions of both NN1 and NN2 networks proved to be the best for small values of R_s in the range (2 - 3) mm, close to the dimensions of the microphone aperture ($r_0 = 1.5$ mm). This result indicates the justification of the theoretical approximation which assumes that $R_s = r_0$. In that case correction of the measured signal due to the instrumental influences is not necessary to

obtain correct network prediction, which means that the experimental data analysis procedure can be simplified.

When R_s values approach the microphone radius R_0 region, the NN2 network trained with undistorted signals gives better predictions. Both networks give poorer predictions for samples whose radii are larger than R_0 . This result leads to the conclusion that the samples used in open photoacoustic cell configuration, whose radii are not larger than the dimensions of the microphone should be used.

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Data Availability The data that support the findings of this study are available from the corresponding author upon reasonable request.

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Appendix I. Periodic temperature component in Si sample

Following the geometry of the problem presented in Figure 1, we are enabled to use the 1D diffusion equation to describe the temperature changes within the investigated Si sample along the heat propagation axis (z-axis) [8,32,33]:

$$\frac{d^2 T_s(z)}{dz^2} - \sigma^2 T_s(z) = -\frac{1}{k} \left[\frac{\varepsilon - \varepsilon_g}{\varepsilon} \beta I_0 \exp(-\beta z) - \frac{\varepsilon_g}{\tau} \delta n_p(z) \right]. \quad (\text{A1.1})$$

The solution $T_s(z)$ to the Eq.(3) can be given as a sum of thermalization $T_{\text{therm}}(z)$, bulk $T_{\text{br}}(x)$ and surface $T_{\text{sr}}(x)$ recombination components [8,32]

$$T_s(z) = T_{\text{therm}}(z) + T_{\text{br}}(z) + T_{\text{sr}}(z), \quad (\text{A1.2})$$

defined as

$$T_{\text{therm}}(z) = \frac{I_0}{k} \frac{\varepsilon - \varepsilon_g}{\varepsilon} \frac{\beta}{\beta^2 - \sigma^2} \left[b \frac{e^{\sigma(z-l)} + e^{-\sigma(z-l)} - e^{-\beta l} (e^{\sigma z} + e^{-\sigma z})}{e^{\sigma l} - e^{-\sigma l}} - e^{-\beta z} \right], \quad (\text{A1.3})$$

$$T_{\text{br}}(z) = \frac{\varepsilon_g B_1}{\tau k \sigma^2} \left\{ \frac{B_2 e^{\sigma z} + B_3 e^{-\sigma z}}{e^{\sigma l} - e^{-\sigma l}} - \frac{1}{c^2 - 1} \left[\frac{\delta n_p(z)}{B_1} + \frac{b^2 - c^2}{b^2 - 1} e^{-\beta z} \right] \right\}, \quad (\text{A1.4})$$

$$T_{\text{sr}}(z) = \frac{2\varepsilon_g}{k\sigma} \frac{s_1 \delta n_p(0) \cosh[\sigma(z-l)] + s_2 \delta n_p(l) \cosh(\sigma z)}{e^{\sigma l} - e^{-\sigma l}}, \quad (\text{A1.5})$$

where constants are

$$\begin{aligned} b &= \frac{\beta}{\sigma}, \quad c = \frac{1}{L\sigma}, \\ B_1 &= \frac{\beta I_0}{\varepsilon D_p (\beta^2 - L^{-2})} \\ B_2 &= B_4 e^{-\sigma l} + B_5, \\ B_3 &= B_4 e^{\sigma l} + B_5, \end{aligned}$$

and

$$\begin{aligned} B_4 &= -c \frac{\frac{1}{B_1} [\delta n_p(l) - \delta n_p(0) \cosh(l/L)] - \cosh(l/L) + e^{-\beta l}}{\sinh(l/L) \cdot (c^2 - 1)} - \frac{b}{b^2 - 1}, \\ B_5 &= c \frac{\frac{1}{B_1} [\delta n_p(l) \cosh(l/L) - \delta n_p(0)] - 1 + e^{-\beta l} \cosh(l/L)}{\sinh(l/L) \cdot (c^2 - 1)} + \frac{b e^{-\beta l}}{b^2 - 1}. \end{aligned}$$

Here, $\sigma = (1+i)/\mu$ being the complex heat diffusion coefficient, $\mu = \sqrt{D/\pi f}$ the thermal diffusion length of the semiconductor, β the semiconductor absorption coefficient, and D the thermal diffusivity. Also, $L = L_p / (1 + i2\pi f \tau_p)^{1/2}$ is the complex excess carriers diffusion length, $L_p = \sqrt{D_p \tau_p}$ the minority excess carrier diffusion length, i the complex unit, $\delta n_p(z)$ the photogenerated minority carriers (holes) dynamic density component, D_p the holes diffusion coefficient, τ_p the holes lifetime, and s_1 and s_2 are the surface recombination velocities at front and rear sample surfaces, respectively.

Total temperature and its components at the rear (nonilluminated) side of the sample ($z = l, e^{-\beta l} \rightarrow 0$) can be written as [8,32]:

$$T_s(l) = T_{\text{therm}}(l) + T_{\text{br}}(l) + T_{\text{sr}}(l), \quad (\text{A1.6})$$

where

$$T_{\text{therm}}(l) = \frac{I_0}{k\sigma} \frac{\varepsilon - \varepsilon_g}{\varepsilon} \frac{\beta^2}{\beta^2 - \sigma^2} \frac{1}{\sinh(\sigma l)}, \quad (\text{A1.7})$$

$$T_{\text{br}}(z) = \frac{\varepsilon_g}{\tau k \sigma^2} \frac{\beta I_0}{\varepsilon D_p (\beta^2 - L^{-2})} \left\{ \frac{B_2 e^{\sigma l} + B_3 e^{-\sigma l}}{2 \sinh(\sigma l)} - \frac{1}{c^2 - 1} \frac{\delta n_p(z)}{B_1} \right\}, \quad (\text{A1.8})$$

$$T_{\text{sr}}(l) = \frac{\varepsilon_g}{k\sigma} \frac{s_1 \delta n_p(0) + s_2 \delta n_p(l) \cosh(\sigma l)}{\sinh(\sigma l)}, \quad (\text{A1.9})$$

Appendix II. Periodic carrier densities in Si sample

Considering that the used Si membranes (Figure 1) are the low-level injection n -type semiconductors (minority carriers are used to explain carrier dynamics), the dynamic part of the 1D diffusion equation (important for sound wave generation) that explains carrier transport in membranes can be written in the form [8,32,33]:

$$\frac{d^2 \delta n_p(z)}{dz^2} - \frac{\delta n_p(z)}{L^2} = -\frac{\beta I_0}{\varepsilon D_p} e^{-\beta z}, \quad (\text{A2.1})$$

where $L = L_p / (1 + i2\pi f \tau_p)^{1/2}$ is the complex excess carriers diffusion length, $L_p = \sqrt{D_p \tau_p}$ is the excess carrier diffusion length, i is the complex unit, $\delta n_p(z)$ is the photogenerated minority (holes) dynamic density component, D_p is the holes diffusion coefficient, and τ_p is their lifetime. The solution $\delta n_p(z, f)$ of the Eq.(17) is given by [8,32,33]:

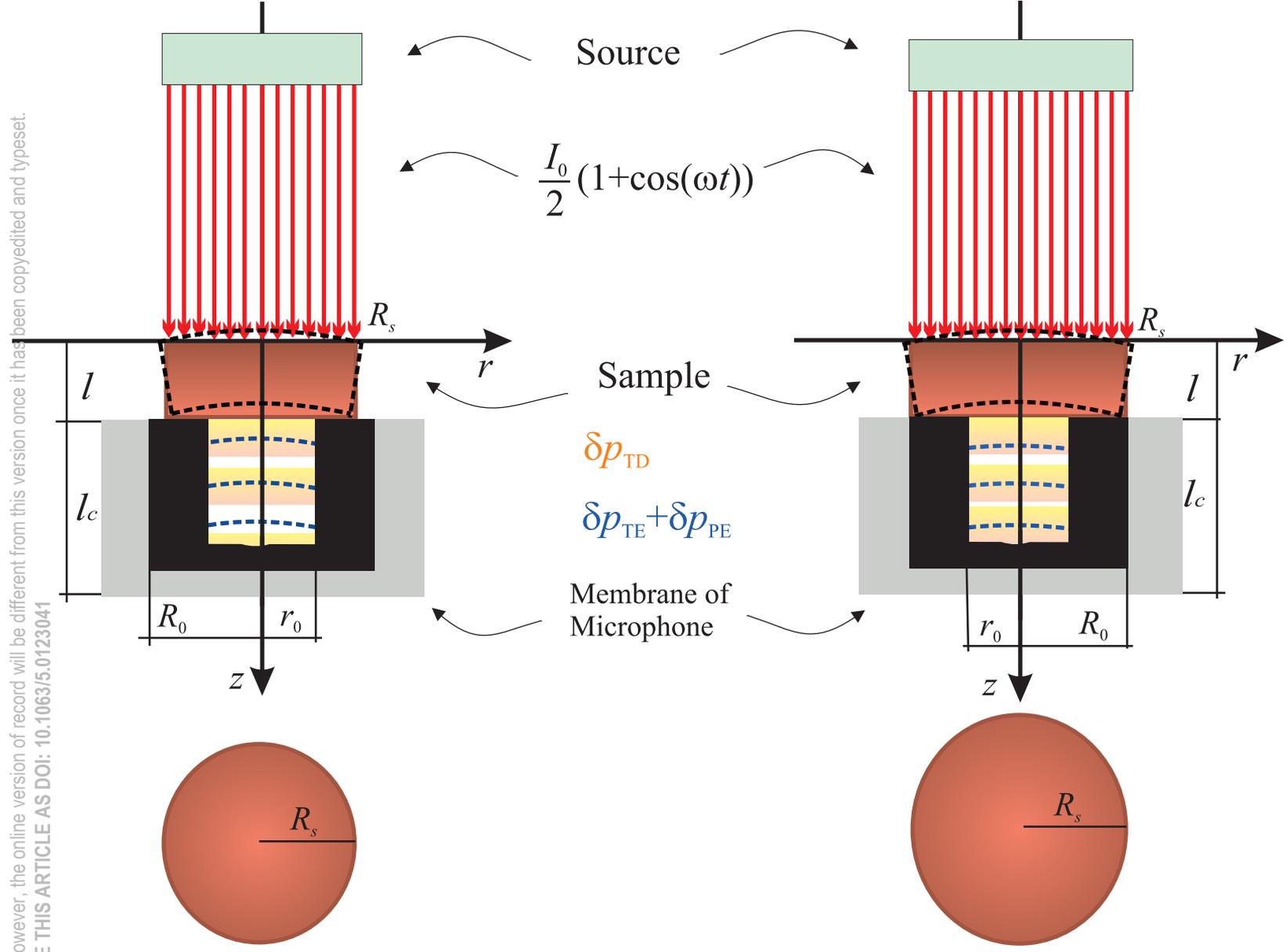
$$\delta n_p(z) = A_+ e^{z/L} + A_- e^{-z/L} - A e^{-\beta z}, \quad (\text{A2.2})$$

where $A = I_0 / (\varepsilon D_p \beta)$, and the integration constants A_{\pm} are defined by [8,32,33]:

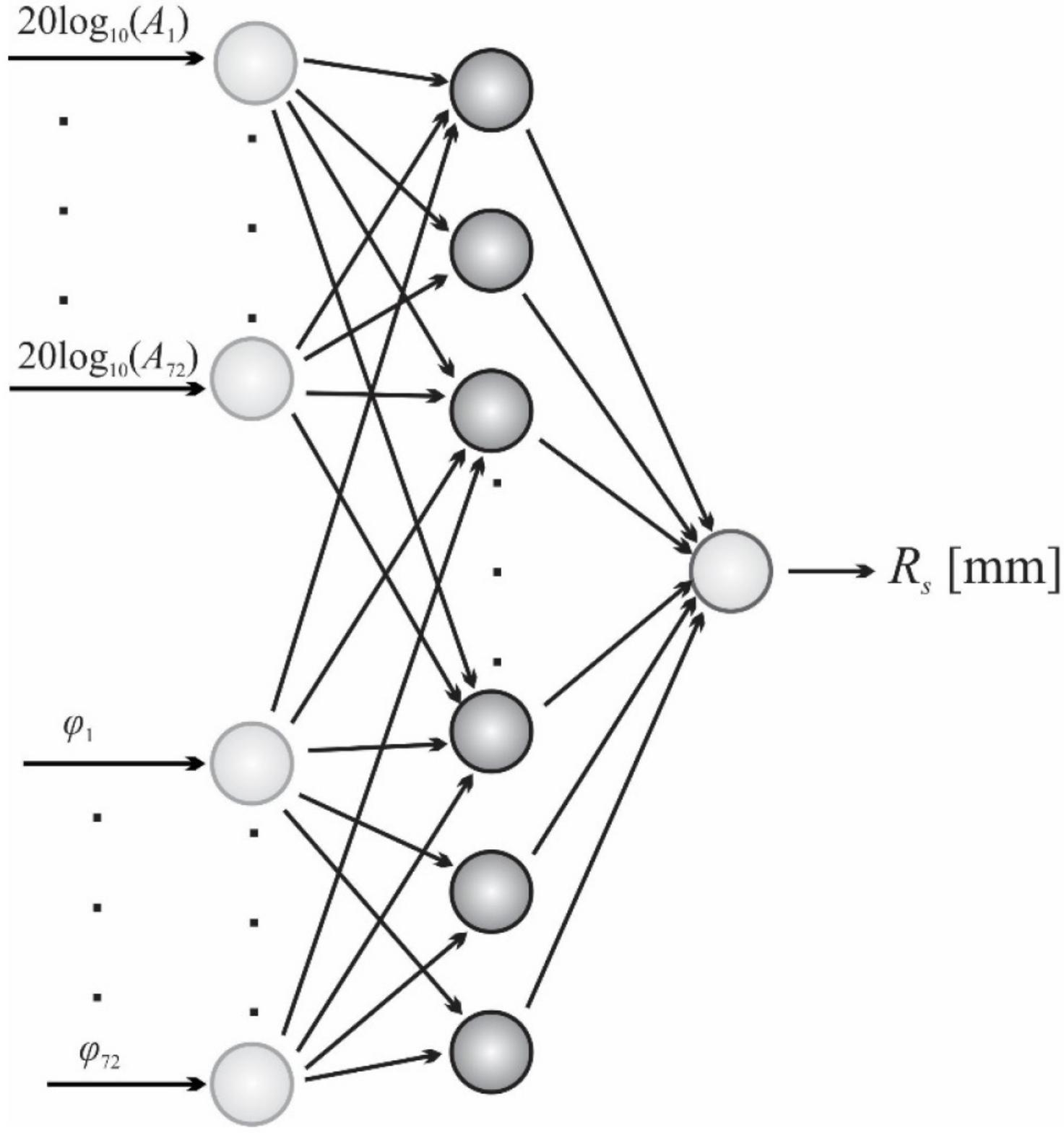
$$A_{\pm} = \frac{A}{v_D} \frac{v_{\beta} (v_D \pm s_2) e^{\mp l_2/L} - v_D (v_{\beta} - s_2) e^{-\beta l_2}}{(v_D + s_2) e^{l_2/L} - (v_D - s_2) e^{-l_2/L}}, \quad (\text{A2.3})$$

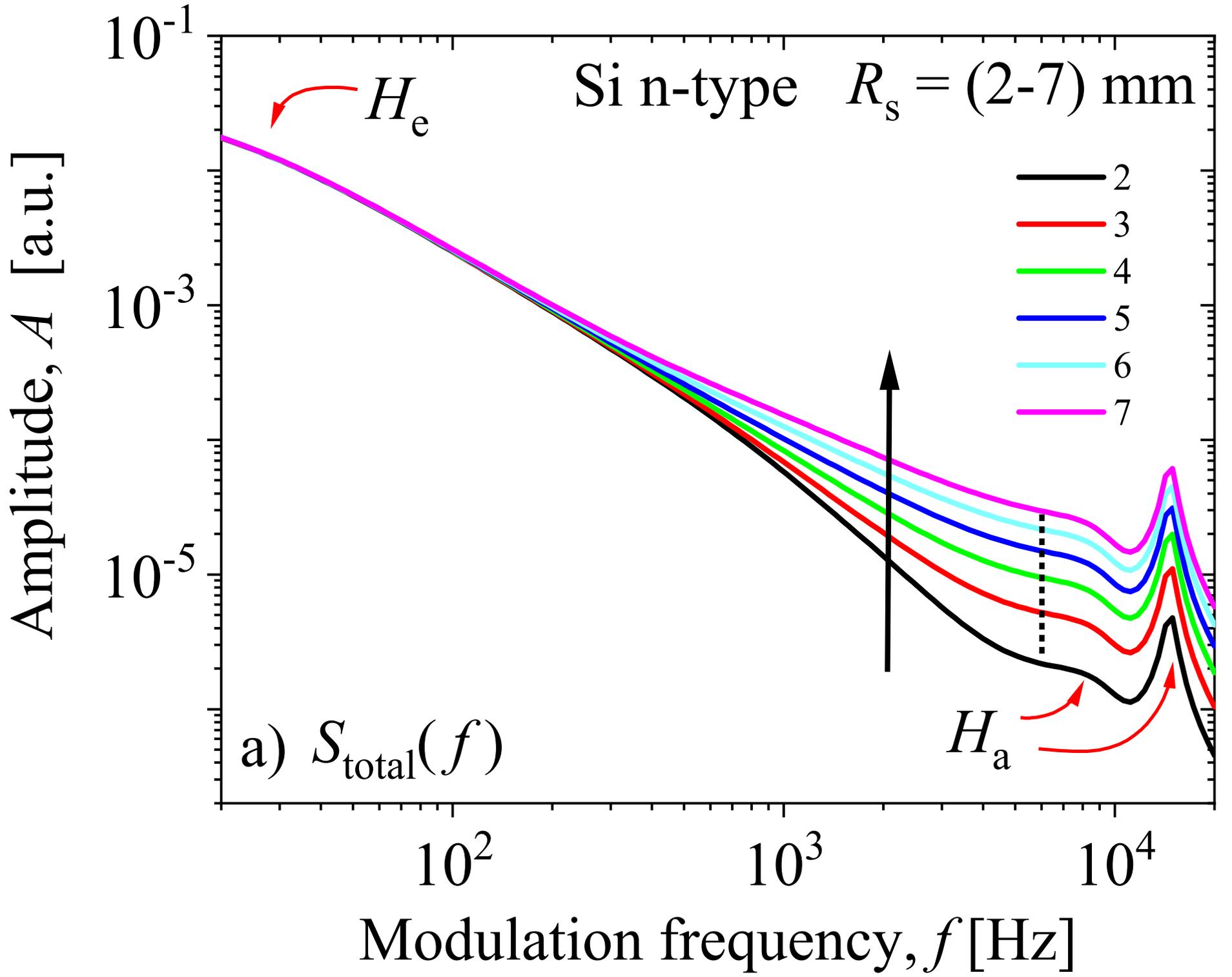
depending strongly on the relative ratio of the characteristic diffusion speeds $v_D = D_p / L$ and $v_{\beta} = \beta D_p$.

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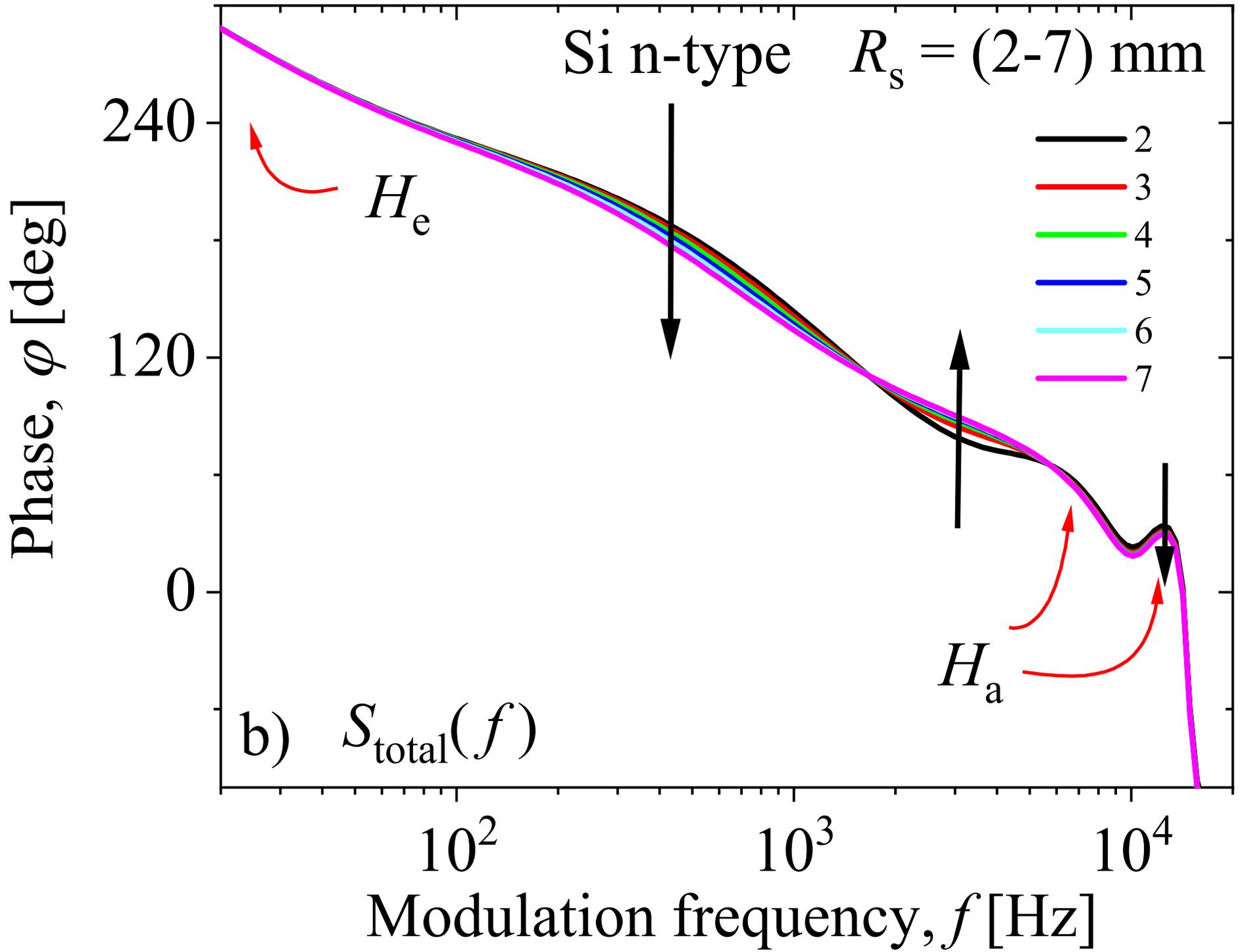


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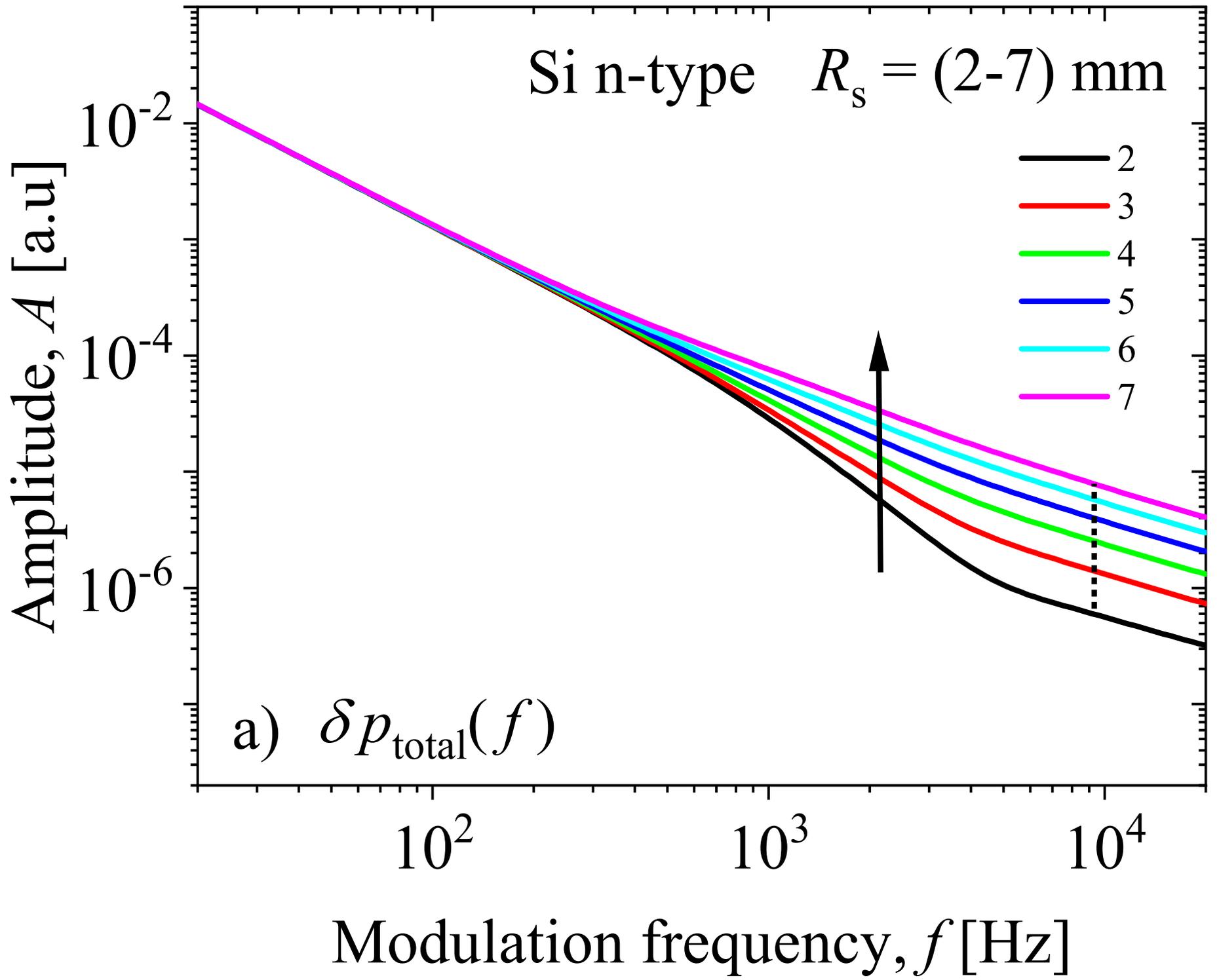




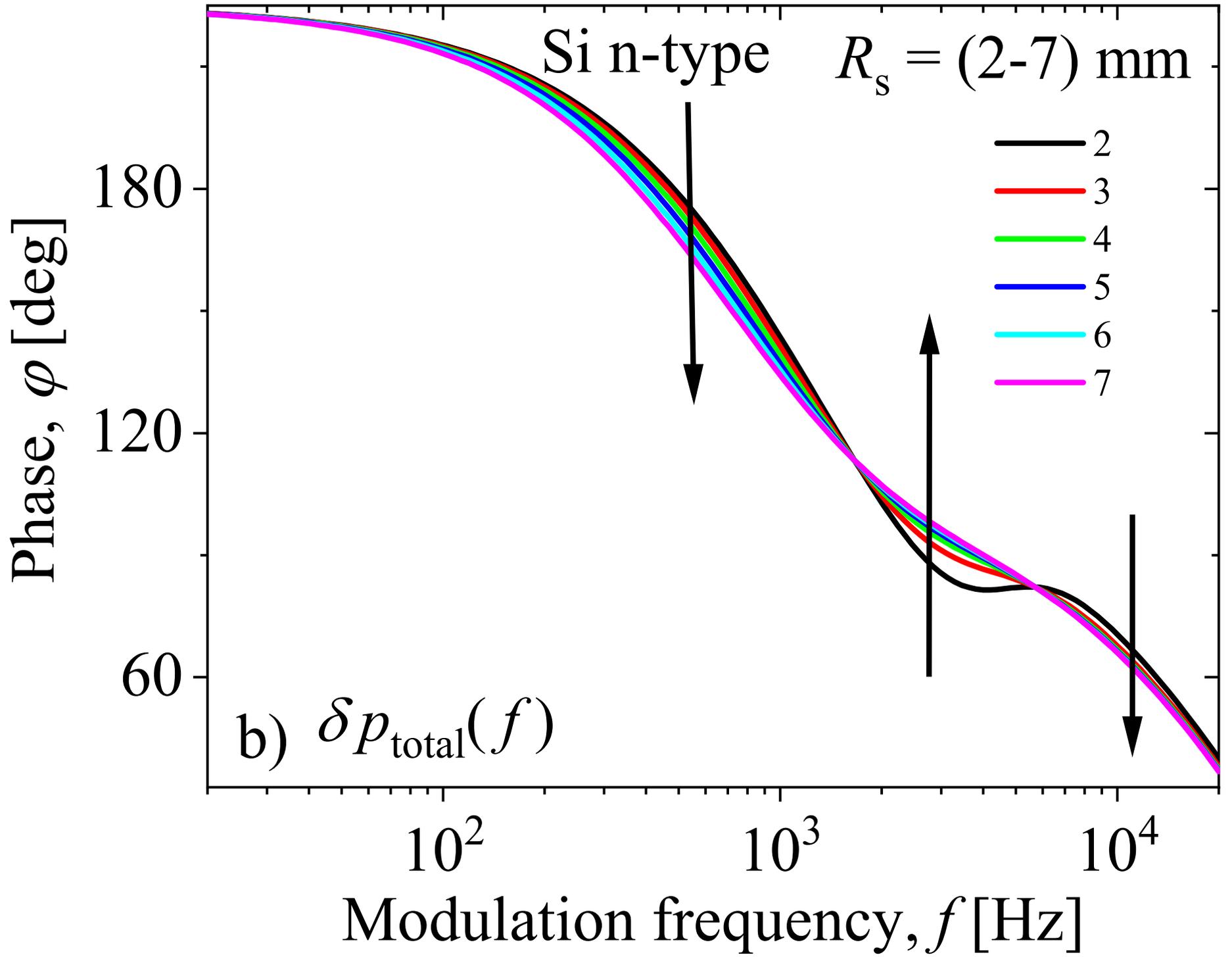
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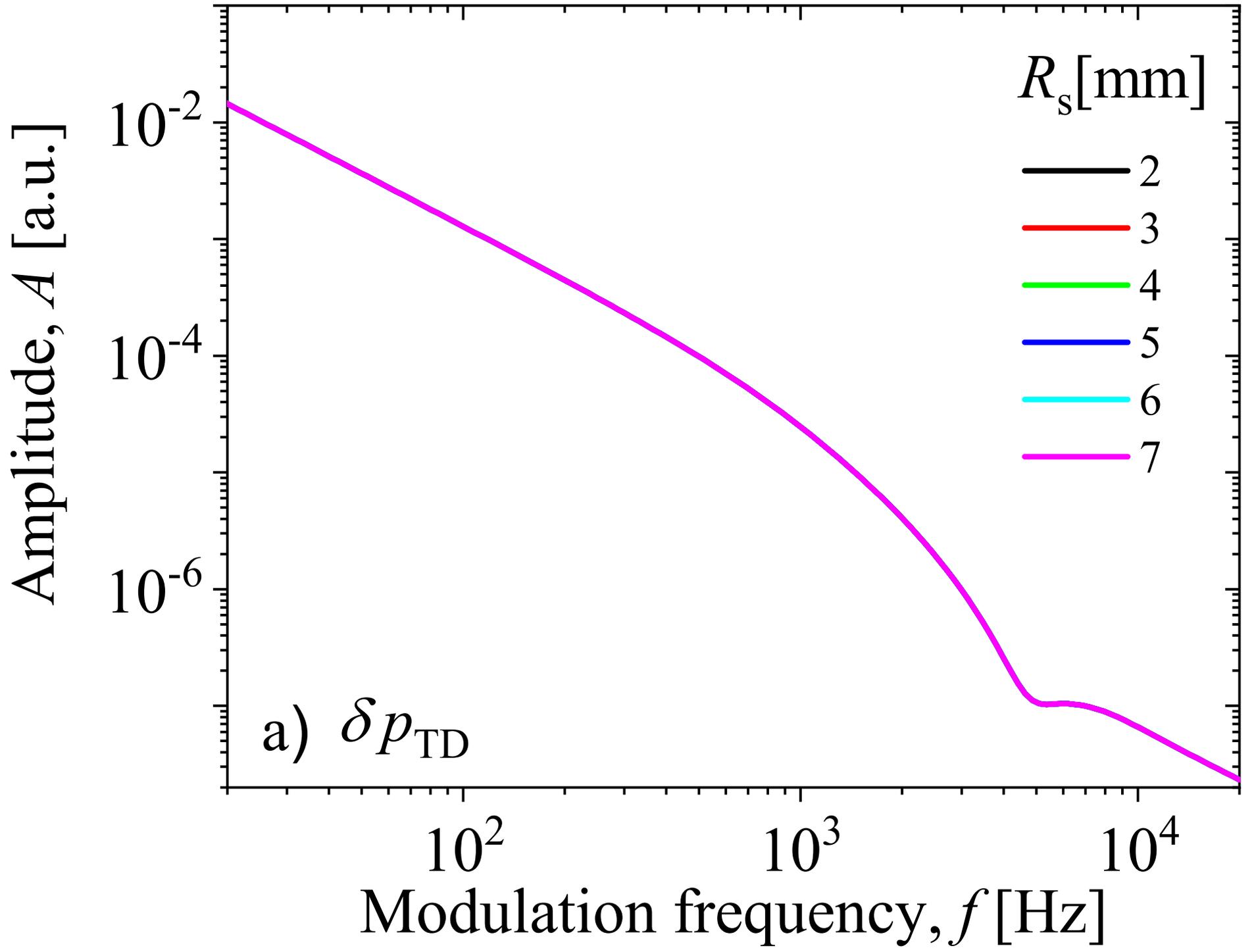
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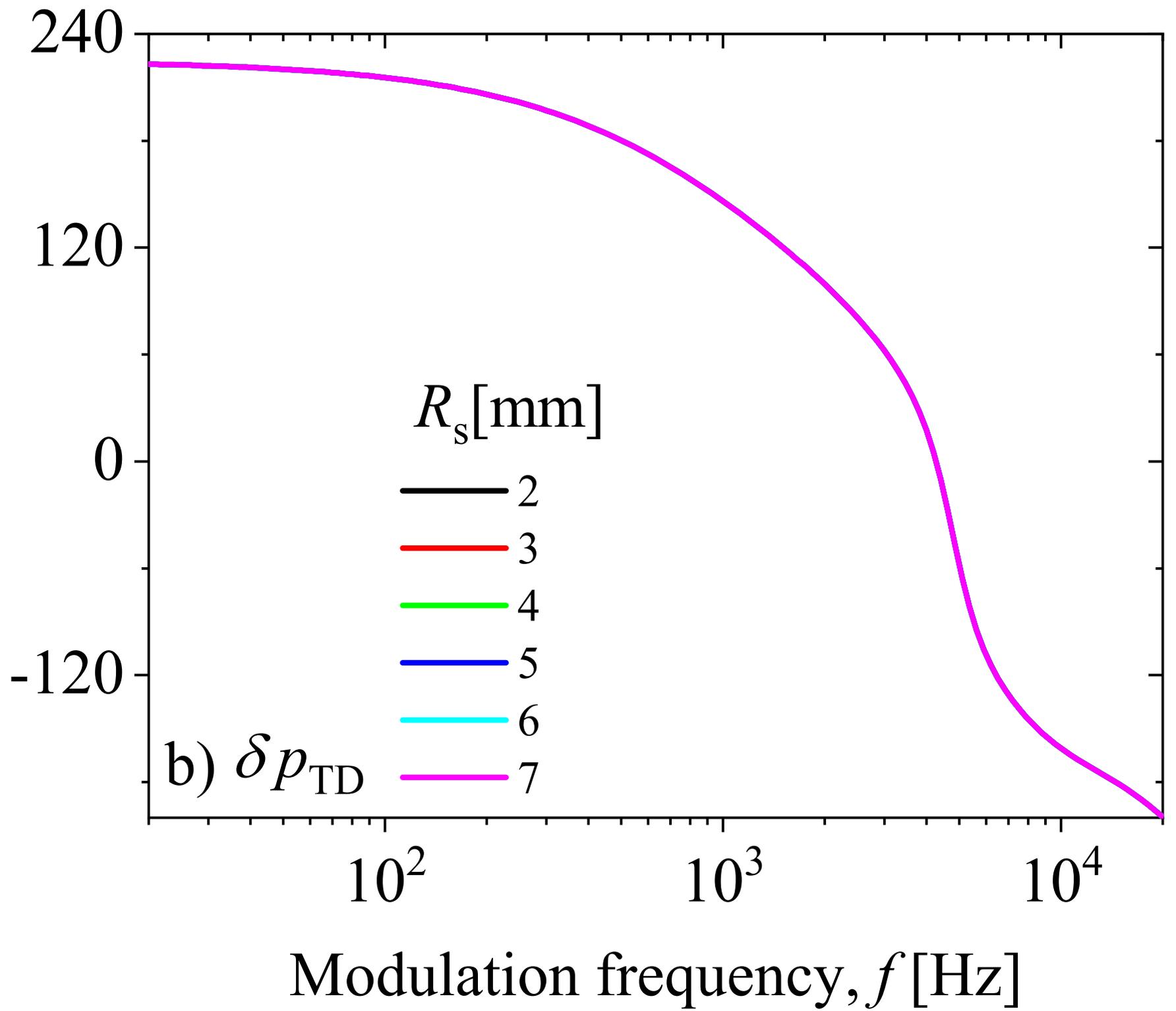


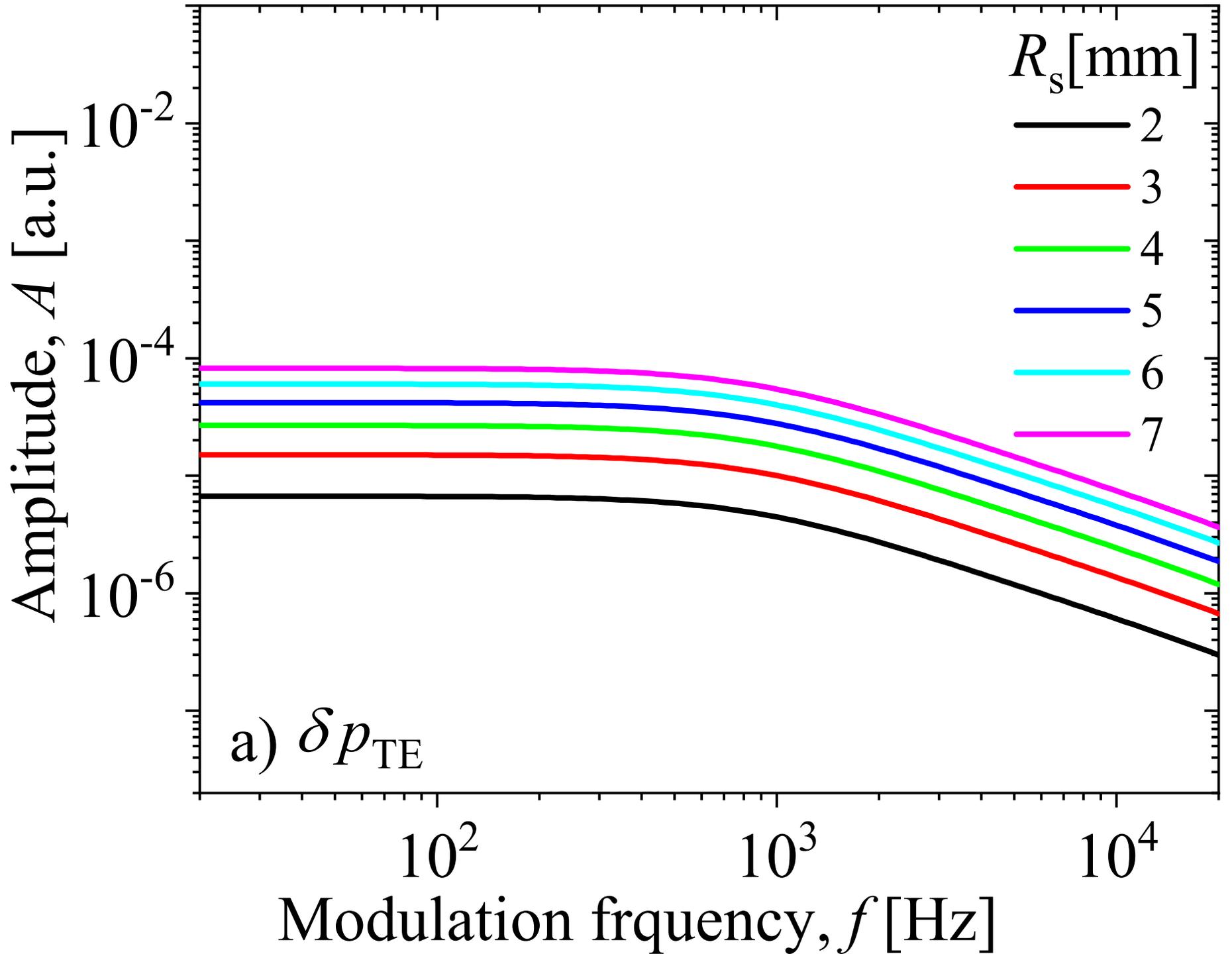
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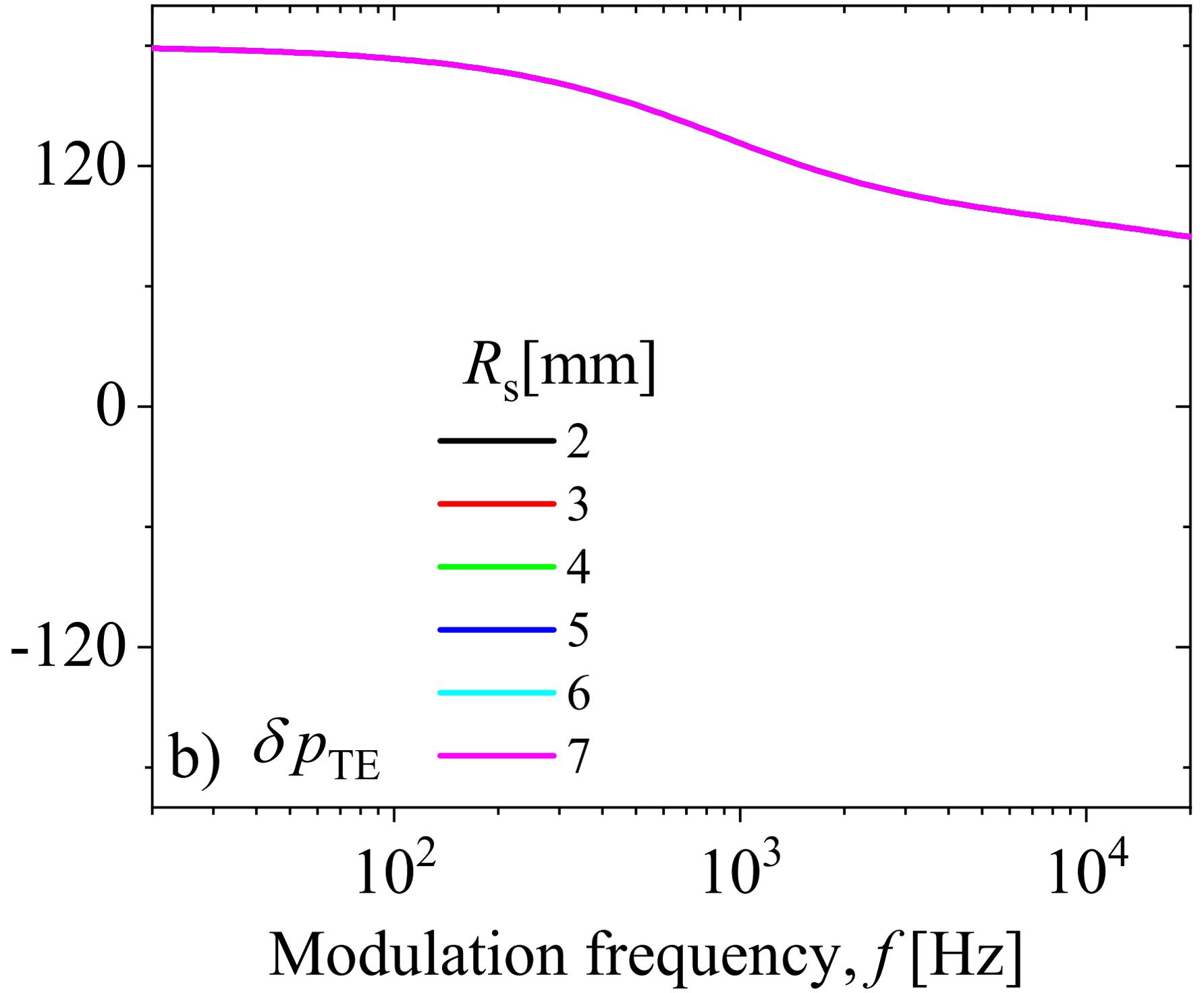
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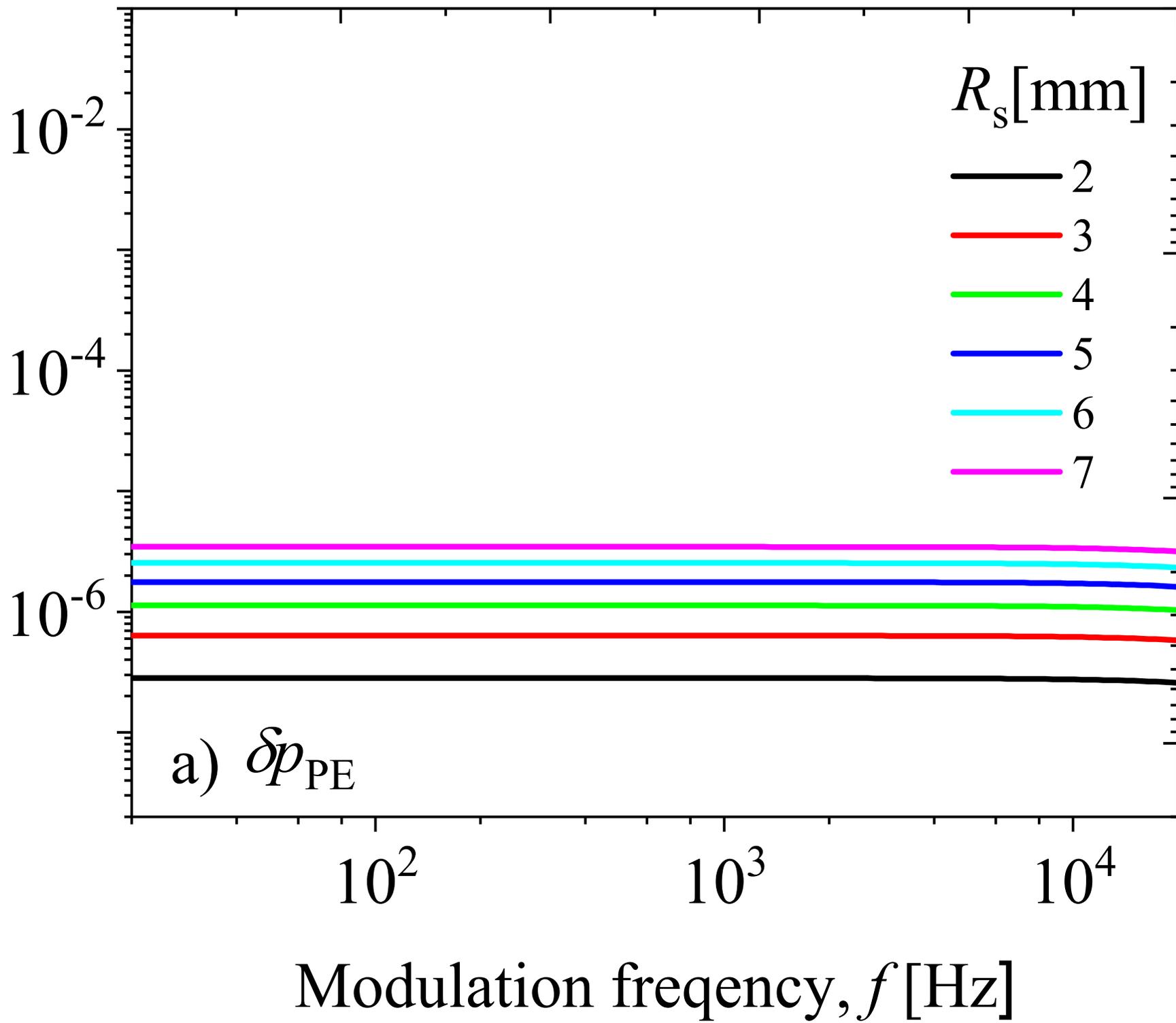
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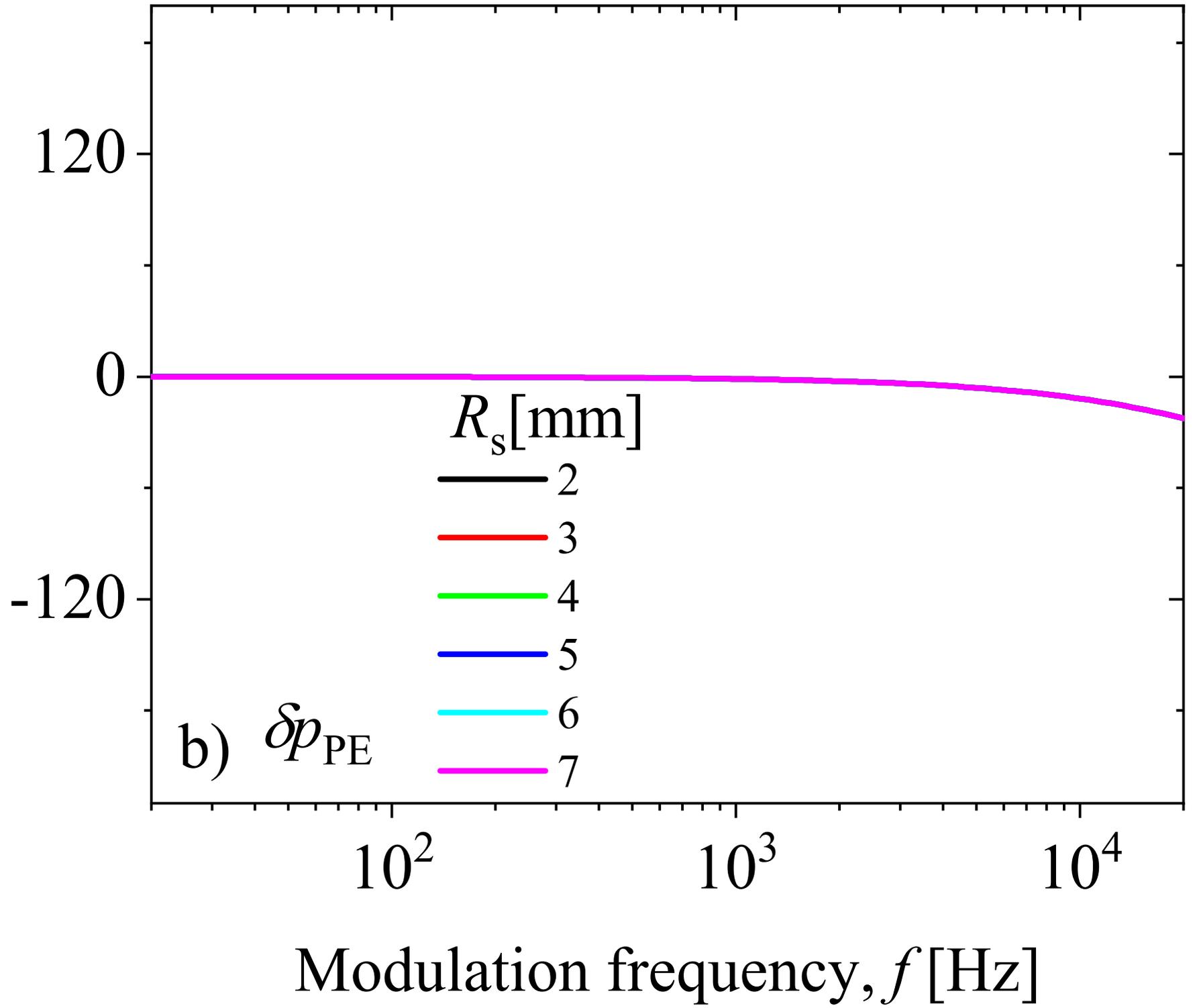
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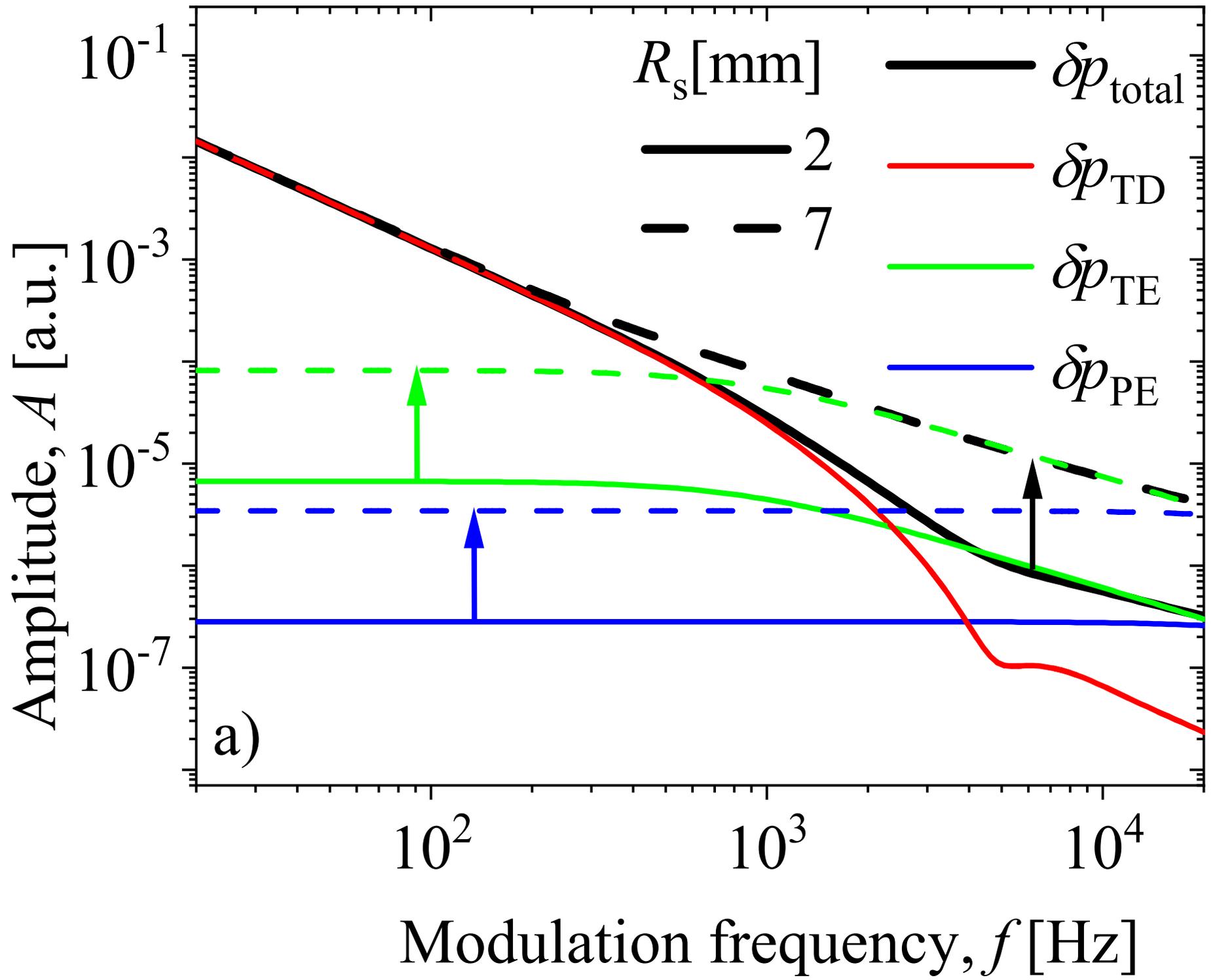


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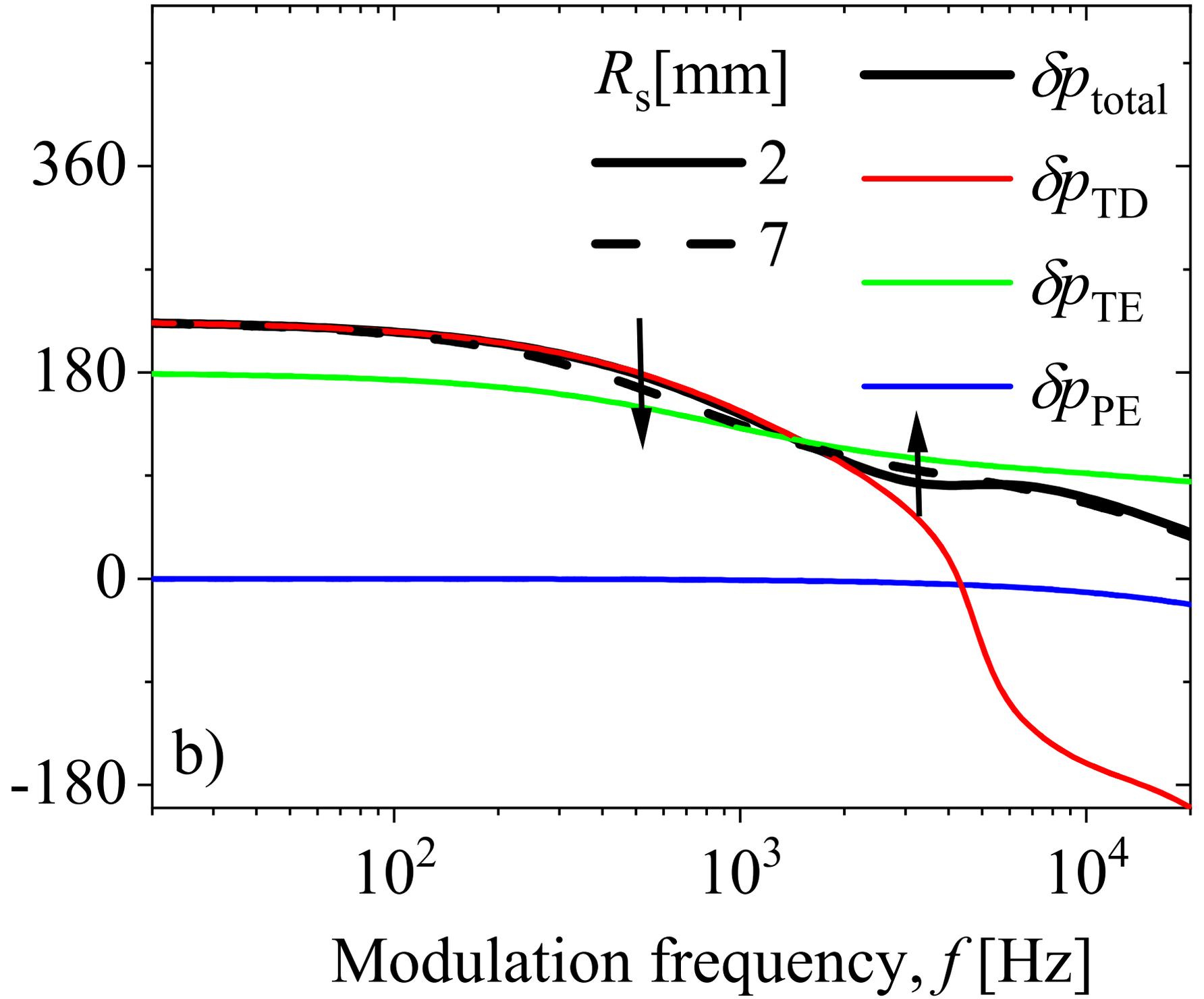
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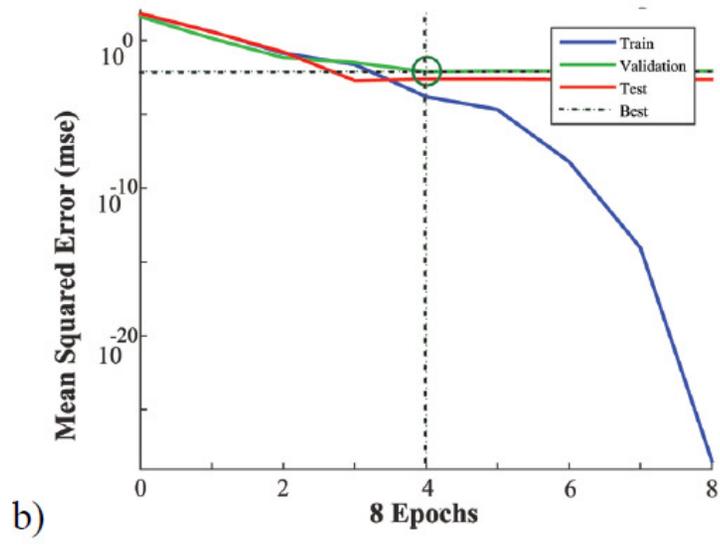
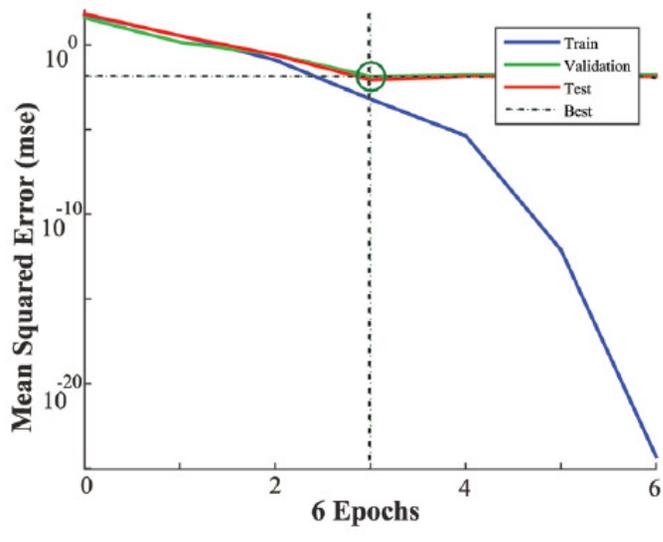
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Phase, φ [deg]

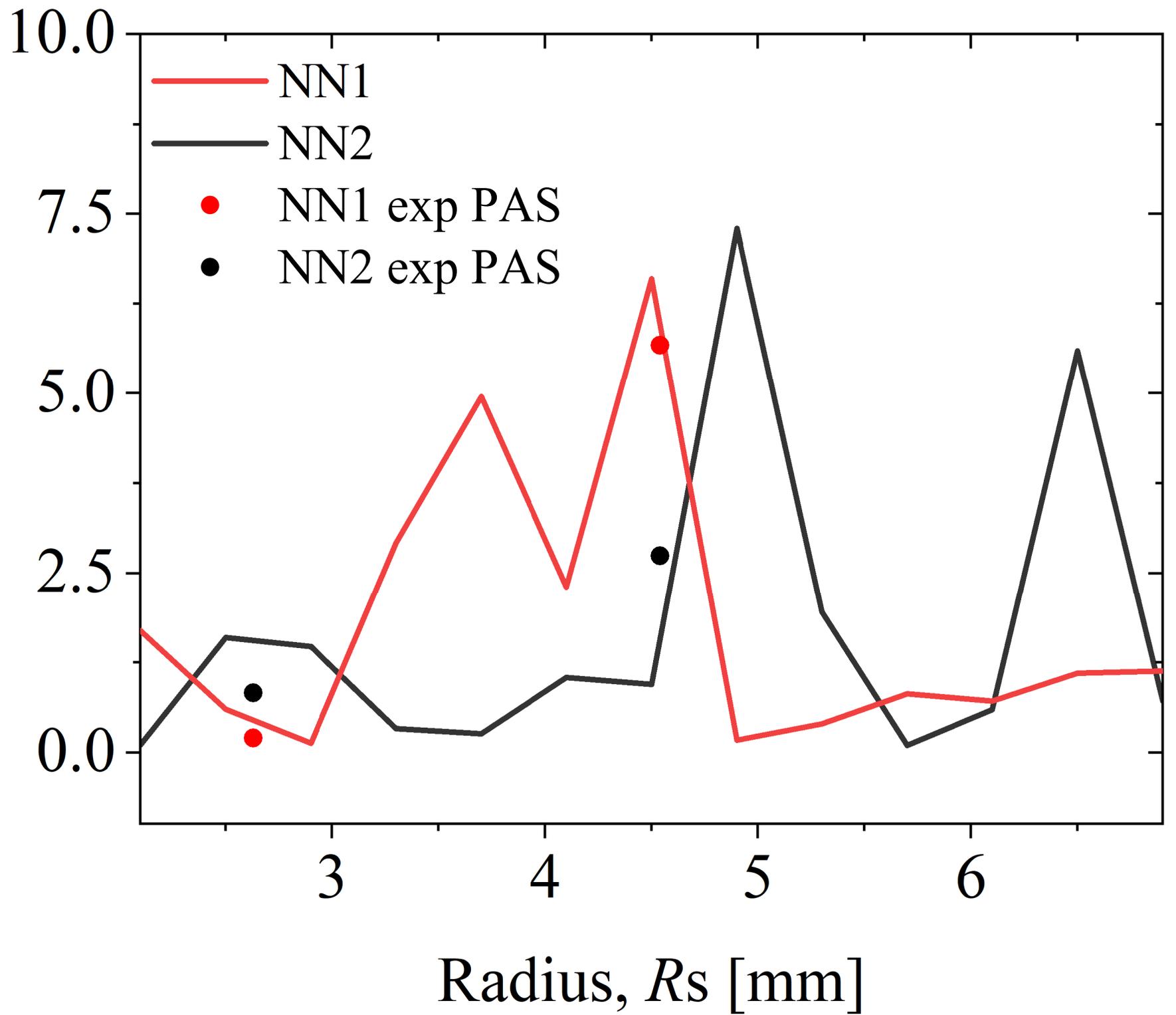


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