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Article Design and Robust Performance Analysis of Low-Order Approximation of Fractional PID Controller Based on an IABC Algorithm for an Automatic Voltage Regulator System

Abdelhakim Idir ^{1,2,*}, Laurent Canale ^{3,*}, Yassine Bensafia ⁴ and Khatir Khettab ¹

- ¹ Department of Electrical Engineering, University Mohamed Boudiaf of M'sila, M'sila 28000, Algeria
- ² Applied Automation Laboratory, F.H.C, University of Boumerdes, Boumerdes 35000, Algeria
- ³ CNRS, LAPLACE, UMR 5213 Toulouse, France
- ⁴ Department of Electrical Engineering, Bouira University, Bouira 10000, Algeria
- * Correspondence: abdelhakim.idir@univ-msila.dz (A.I.); laurent.canale@laplace.univ-tlse.fr (L.C.)

Abstract: In this paper, a low-order approximation (LOA) of fractional order PID (FOPID) for an automatic voltage regulator (AVR) based on the modified artificial bee colony (ABC) is proposed. The improved artificial bee colony (IABC) high-order approximation (HOA)-based fractional order PID (IABC/HOA-FOPID) controller, which is distinguished by a significant order approximation and by an integer order transfer function, requires the use of a large number of parameters. To improve the AVR system's performance in terms of transient and frequency response analysis, the memory capacity of the IABC/HOA-FOPID controller was lowered so that it could fit better in the corrective loop. The new robust controller is named the improved artificial bee colony (IABC) loworder approximation (LOA)-based fractional order PID (IABC/LOA-FOPID). The performance of the proposed IABC/LOA-FOPID controller was compared not only to the original ABC algorithm-tuned PID controller, but also to other controllers tuned by state-of-the-art meta-heuristic algorithms such as the improved whale optimization algorithm (IWOA), particle swarm optimization (PSO), cuckoo search (CS), many optimizing liaisons (MOL), genetic algorithm (GA), local unimodal sampling (LUS), and the tree seed algorithm (TSA). Step response, root locus, frequency response, robustness test, and disturbance rejection abilities are all compared. The simulation results and comparisons with the proposed IABC/LOA-FOPID controller and other existing controllers clearly show that the proposed IABC/LOA-FOPID controller outperforms the optimal PID controllers found by other algorithms in all the aforementioned performance tests.

Keywords: improved artificial bee colony (IABC); fractional order proportional-integral-derivative controller (FOPID); low order approximation (LOA); stability; automatic voltage regulation (AVR)

1. Introduction

In power systems, the automated voltage regulator (AVR) is employed to maintain the terminal voltage of a synchronous generator at a suitable level. The AVR system regulates the constancy of the terminal voltage by adjusting the generator's exciter voltage [1,2]. In power system applications, maintaining a consistent input voltage has always been a difficult problem. When there is a sudden shift in load for power supply requirements, the AVR system is employed to stabilize the voltage value.

The AVR system is now receiving a lot of attention in the industry for keeping the synchronous generator's terminal voltage constant under all situations. Classical integer order proportional-integral-derivative (IOPID) [3–5], proportional-integral-derivative acceleration (PIDA) [6], fractional order PID (FOPID) [7–9], PID plus second-order derivative (PIDD2) controller [10], modified neural network (MNN) [11], genetic algorithm (GA) [12], interval type-2 fuzzy logic (IT2FL) [13], and a differential evolution—artificial electric field algorithm (DE-AEFA) [14].



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). Likewise, the objective function can also be of any type such as integral of time multiplied square error (ITSE) [15], integral of time multiplied absolute error (ITAE) [16], integral absolute error (IAE) [17] and integral square error (ISE) [18].

However, even for the same controllers, several optimization methods are available. For example, artificial bee colony (ABC) [15], stochastic fractal search [19], whale optimization algorithm (WOA) [20], improved whale optimization algorithm (IWOA) [21], sine-cosine algorithm (SCA) [22], tree seed algorithm (TSA) [23], particle swarm optimization (PSO) [24], improved kidney-inspired algorithm (IKIA) [25], cuckoo search (CS) [26], genetic algorithm [12,27], many optimizing liaisons (MOL) [28], grey wolf optimization (GWO) [18], crow search algorithm (CSA) [29], water wave optimization (WWO) [30], local unimodal sampling (LUS) [31], water cycle algorithm (WCA) [32], and ant colony optimization (ACO) [33], are optimization algorithms that have been proposed to tune the controller parameters of an AVR system. In refs. [14,34], the authors investigated the combined analysis of load frequency control (LFC) and automatic voltage regulation (AVR), where a differential evolution—artificial electric field algorithm—is presented and is applied to the combined LFC-AVR model. Further examples of the intelligent strategies for achieving optimal parameters in various systems can be found in [35–38].

Using fractional calculus, it is possible to improve the performance of the PID controller in AVR systems. The FOPID controller (FOPID) is a type of classical PID controller that employs fractions instead of integers in order of derivation and integration. Furthermore, as compared to the integer order PID controller, FOPID provides a better transient response while also being more robust and stable [39–45]. Because of the previously indicated benefits of the FOPID, this research focuses on this form of controller.

In this paper a low-order approximation (LOA) of fractional order PID (FOPID) based on the artificial bee colony (ABC) has been proposed. The IABC/FOPID controller approximation, which is distinguished by a transfer function of integer order and a long memory (or high order approximation (HOA)), named IABC/HOA-FOPID, and requires a lot of parameters to be used. To enhance the performance of the AVR system in terms of transient and frequency responses analysis, the complete IABC/HOA-FOPID controller's memory capacity was reduced so that it could fit better in the corrective loop, the new robust controller is named IABC/LOA-FOPID.

The following list summarizes this paper's originality contribution:

- For the first time, the low-order approximation of a FOPID controller based on the ABC algorithm (named IABC/LOA-FOPID) is used.
- In terms of transient response performance, the proposed IABC/LOA-FOPID controller was thoroughly compared to various strategies in the literature, such as IWOA-PID [21], PSO-PID [12], ABC-PID [15], CS-PID [26], MOL-PID [28], GA-PID [12], LUS-PID [31], and TSA [23]. The findings of the research clearly show that the LOA-FOPID controller tuned by IABC is better.
- To investigate the system's behavior, several robustness tests are specifically studied. All along the experiments, the LOA-FOPID regulator optimized by ABC outperforms the classical or fractional PID controller, whose parameters have been optimized by the other methods that have been researched in the literature.

This paper is organized as follows: Section 2 provides a brief overview of the AVR system's composition, the fundamentals of fractional calculus, and the stability of fractional order systems. Section 3 provides a thorough explanation and mathematical formulation of the proposed IABC/LOA-FOPID controller. The simulation results are displayed in Section 4 of this study. Section 5 summarizes the study's overall findings.

2. Materials and Methods

2.1. AVR System Description and Modeling

The basic role of an AVR system is to keep the generator's terminal voltage constant via the excitation system. A basic AVR system consists of four major components: an amplifier, an exciter, a generator, and a sensor. These components are represented by transfer functions [9,12,15,46] and modeled in the MATLAB/Simulink environment to study the dynamic performance of an AVR. A first-order transfer function with a gain and a time constant is used to represent each component of the AVR system. Table 1 shows the transfer functions of the aforementioned components. The closed-loop block diagram of the AVR system without a controller is shown in Figure 1 along with the transfer functions.

Table 1. Main components of AVR system.

Component of AVR System	Transfer Function	Gain Range	Time Constant Range [s]
Amplifier	$G_a = rac{K_a}{1+T_a s}$	$10 < K_a < 400$	$0.02 < T_a < 0.1$
Exciter	$G_e = rac{K_e}{1+T_es}$	$1 < K_e < 400$	$0.4 < T_e < 1$
Generator	$G_g = rac{K_g}{1+T_g s}$	$0.7 < K_g < 1$	$1 < T_g < 2$
Sensor	$G_s = \frac{K_s}{1+T_s s}$	$\overline{K_s} = 1$	$0.001 < T_s < 0.06$



Figure 1. AVR system block diagram without a PID controller.

To compare the results fairly, in this work, the AVR system's parameters are $K_a = 10$, $K_e = 1$, $K_g = 1$, $K_s = 1$, $T_a = 0.1$, $T_e = 0.4$, $T_g = 1$ and $T_s = 0.01$, which are the same as in the research works [12,15,21,23,26,28,31]. The closed loop transfer function for the AVR system is found as the following equation given the model parameter values mentioned above.

$$\frac{V_{out}}{V_{ref}} = \frac{0.1s + 10}{0.0004s^4 + 0.045s^3 + 0.555s^2 + 1.51 + 11}$$
(1)

Figure 2 depicts the output step voltage response of the aforementioned system, which makes it evident that it is oscillatory stable.



Figure 2. AVR system step response in the absence of a PID controller.

Table 2 presents the AVR system's transient response characteristics maximum overshoot (M_p [%]), settling time (t_s [s]) and rise time (t_r [s]) in the absence of the controller.

	N <i>I</i> [0/]	([.]	([.]
Controller Type	M _p [%]	t _s [s]	$t_r [s]$
AVR without controller	65.7226	6.9865	0.2607

Table 2. Values of the AVR system's transient response without a controller.

2.2. Fractional Calculus

Fractional calculus is a non-integer order operator aD_t^{α} extension of integration and differentiation, where a and t signify the operation's limits and denote the fractional order such that

$$aD_t^{\alpha} = \begin{cases} \frac{a^{\alpha}}{dt^{\alpha}} , & R(\alpha) > 0\\ 1 , & R(\alpha) = 0\\ \int_a^t (d\tau)^{-\alpha}, R(\alpha) < 0 \end{cases}$$
(2)

where it is commonly believed that $\alpha \in \mathbb{R}$, although it might alternatively be a complex number. The fractional differintegral has several definitions. A typical definition is the Riemann-Liouville differintegral [47].

Definition 1. The mathematical definition of Grünwald–Letnikov is:

$$D^{\alpha}f(t) = \lim_{h \to 0} h^{-\alpha} \sum_{j=0}^{k} (-1)^{j} \binom{\alpha}{j} f(kh - jh)$$
(3)

Here, 'h' is the step time and the coefficients given above can be evaluated in relation to the expression given below;

$$\omega_j^{(\alpha)} = \binom{\alpha}{j} = \frac{\Gamma(\alpha+1)}{\Gamma(j+1)\Gamma(\alpha-j+1)}$$
(4)

Definition 2. *Mathematically, the Riemann-Liouville definition is:*

$$f(t) = \frac{d^n}{dt^n} \int_0^t \frac{f(\tau)}{(t-\tau)^{\alpha-n+1}} d\tau$$
(5)

The Oustaloup methodology performs by approximating the function from as:

$$G_f(s) = S^{\alpha}$$
 , $\alpha \in R^+$ (6)

Taking the rational function into consideration [48,49]:

$$G_f(s) = K \prod_{k=1}^{N} \frac{s + w'_k}{s + w_k}$$
(7)

However, gain, zeros, and poles can be calculated as follows:

$$K = w_h^{\gamma}, w_k = w_b.w_u^{(2k-1+\gamma)/N}, w_k' = w_b.w_u^{(2k-1-\gamma)/N}$$

where w_u represents the unity gain in frequency and the central frequency in a geometrically distributed frequency band. Let, $w_u = \sqrt{w_h w_b}$, where w_h represents the upper frequencies while w_b represents the lower frequencies, γ is the derivative order and N is the filter.

2.3. Stability of Fractional Order Systems

When developing a control system, stability is a fundamental and critical condition. In integer order, a linear time-invariant (LTI) system in continuous-time is stable if all of the characteristic equation's roots are on the left half of the 's' plane. The stability of fractional order is determined by more than simply the placements of the poles on the left half side. The fractional order determines it, which becomes progressively complicated as seen below. The characteristic equation of a general linear fractional differential equation is as follows:

$$\sum_{i=0}^{j} a_i s^{\alpha_i} = 0 \tag{8}$$

where, α_i is rational, the characteristic equation can be rewritten as;

$$\sum_{i=0}^{n} a_i s^{\frac{i}{m}} = 0$$
 (9)

where *m* is integer, $\alpha = 1/m$ and $\alpha_i > 0$.

Figure 3a shows the stability zone of a fractional order system when $0 < \alpha < 1$, which is greater than the stability region of an integer order system. Figure 3b shows the stability zone of a fractional order system when $1 < \alpha < 2$, which is smaller than the stability region of an integer order system [50,51].



Figure 3. Stable regions when $0 < \alpha < 1$ (**a**) and $1 < \alpha < 2$ (**b**).

3. Fractional PID Controller Based on IABC Algorithm

3.1. ABC Algorithm

The employed bees, following bees, and scout bees are the three categories that the basic algorithm of the artificial bee colony divides the population and assigns a search to each type of artificial bee phase [52,53]. As a starting point, the initial solution (food sources) is arbitrarily generated. All solutions $X_i = (i = 1, 2, ..., N)$; $X_i = (x_{i1}, x_{i2}, x_{i3}, ..., x_{id})^T$ stands for the position of all food sources.

Equation (10) is used by the employed bee to conduct a random search of the feasible domain in search of food sources. The deployed bee then passes the results of the food source multiplication to the next bee, which is waiting in the hive to perform the food source search.

$$x_{ij}' = x_{ij} + r_{ij} \left(x_{ij} - x_{kj} \right)$$
(10)

where k = 1, 2, ..., N and j = 1, 2, ..., d. k is a randomly selected indicator for different i. N stands for the population size, and D stands for the problem dimension, r_{ij} is a random number between -1 and 1.

In the following bee stage, the food source is selected by the onlooker bee based on likelihood. As can be seen from (Equation (11)) below, the probability value, *prob(i)*, is calculated:

$$prob(i) = \frac{fit(i)}{\sum_{i=1}^{N} fit(i)}$$
(11)

When an onlooker makes a decision about which food source to choose, it starts searching for it, generates an updated location by (10), assesses the profitability, and then remembers the better location. *fit*(*i*) in (11) represents the fitness value of the *i*th food source X_i .

The scout bees reject all food sources that have previously been used to make honey during this phase, going over the permitted intake for all food sources. A bee that has been working on a food source that has been abandoned eventually develops into a scout bee. The scout will investigate a new food source at random (12).

$$x_{ij} = x_{min,j} + rand(0,1)(x_{max,j} - x_{min,j})$$
(12)

3.2. Fractional Order PID Controller

Classical PID controllers are frequently used because of their basic design and simple implementation. The dynamic response of the AVR system can be improved by using controllers with fractional order PID (FOPID) or integer order PID (IOPID). With respect to the error signal, the PID controller executes three major control actions using proportional, integral, and derivative approaches. The PID controller transfer function is provided by:

$$G_{IOPID}(s) = K_p + \frac{K_i}{s} + K_d s$$
(13)

where K_p represents the proportional gain, and K_i and K_d represent the integral and derivative gains respectively.

The fractional order PID controller is an extension of the traditional PID controller, offering an integration of order λ and a differentiation of order μ , where λ and μ can be any positive real integer.

$$G_{FOPID}(s) = K_p + \frac{K_i}{s^{\lambda}} + K_d s^{\mu}$$
(14)

where the two additional parameters are λ (fractional order integration) and μ . (fractional order differentiation).

The fractional PID controller is the most popular kind of PID controller because of its original characteristics. There are various kinds of FOPID controllers, such as PID $(\lambda = 1, \mu = 1)$, PI $(\lambda = 1, \mu = 0)$, PD $(\lambda = 0, \mu = 1)$, and the P controller $(\lambda = 0, \mu = 0)$. The graphical representation of the various PID controllers is shown in Figure 4.



Figure 4. PID/PI^{λ}D^{μ} controllers' graphical representation.

3.3. Design of the FOPID Controller Using IABC

To optimize the parameters of the FOPID controller (K_p , K_i , K_d , λ , μ), the modified ABC algorithm presented in [52], which is based on the use of cyclic exchange neighborhood and chaos (CNC), is used. Figure 5 depicts an AVR system with an IABC-FOPID controller. A food source location represents a potential solution of the FOPID controller to be optimized, which is represented by a vector with five components, $X = (K_p, K_i, K_d, \lambda, \mu)$. Each solution's fitness is determined by (15).



Figure 5. Proposed IABC/LOA-FOPID controller applied to the AVR system.

The modified ABC algorithm described in [50], which is based on the use of the cyclic exchange neighborhood and chaos (CNC), is used to optimize the parameters of the FOPID controller (K_p , K_i , K_d , λ , μ). An AVR system with an IABC/LOA-FOPID controller is shown in Figure 5. The FOPID controller to be optimized has a potential solution represented by a food source location, which is represented by a vector with five components, $X = (K_p, K_i, K_d, \lambda, \mu)$.

The fitness of each solution is given by (15).

$$J(K_{P}, K_{I}, K_{D}, \lambda, \mu) = \int_{0}^{\infty} \left| y(t)^{*} - y(t) \right| dt = \int_{0}^{\infty} |e(t)| dt$$
(15)

where: y(t) represents the output of the system, in our case is the output voltage of the generator; noted V_{out} . $y(t)^*$ is the reference voltage; noted V_{ref} .

The following are the main design steps [52].

Step 1: Start with the basic solution.

Step 2: Determine each initial solution's fitness x_i .

Step 3: Set cycle to 1.

Step 4: Bees are used to produce new solutions x_i , and fitness is calculated, both using (16) and (15);

$$x'_{ij} = \begin{cases} x_{Nj} + r_{ij} (x_{ij} - x_{kj}), & i = 1\\ x_{i-1j} + r_{ij} (x_{ij} - x_{kj}), & 2 \le i \le N \end{cases}$$
(16)

Step 5: Use the greedy selection to select the best one between x'_i and x_i .

Step 6: Using Equation (11), compute the probability values prob(*i*) of the solutions. Step 7: Onlooker bees select the solution based on prob(*i*), then look for a neighbor to generate new solutions by (10) and calculate fitness by (15).

Step 8: Use a greedy choice to find the right and best solution.

Step 9: If a solution requires improvement, scouts should conduct a search for chaos. Step 10: Commit the best answer so far to memory.

Step 11: Cycle = cycle + 1; if cycle is greater than the allowed number of cycles, the process is stopped; if not, move on to step 4.

Figure 5 illustrates the block design for the proposed IABC/LOA-FOPID controller used in an AVR system.

3.4. Sub-Optimal Reduction Algorithm

Figure 6 shows the error signal for model reduction, where the initial model is provided by:

$$G(s) = \frac{b_{n-1}s^{n-1} + \dots + b_1s + b_0}{s^n + a_{n-1}s^{n-1} + \dots + a_1s + a_0}$$
(17)



Figure 6. Error signal for model reduction.

Our present goal is to develop a low-order approximation (LOA) integer-order model of the type in [54]:

$$G_{r/m}(s) = \frac{\beta_1 s^r + \ldots + \beta_r s + \beta_{r+1}}{s^m + \alpha_1 s^{m-1} + \ldots + \alpha_{m-1} s + \alpha_m}$$
(18)

An objective function to reduce the H2 norm of the reduction error signal is as follows:

$$J_r = \min_{a} \|\hat{G}(s) - G_{r/m}(s)\|_2$$
(19)

With θ the parameters are to enhance such that:

$$\theta = [\beta_1, \dots, \beta_r, \alpha_1, \dots, \alpha_m] \tag{20}$$

To find the low-order approximation (LOA) model of the fractional-order model characterized by a long memory, use the following approaches [55]:

- 1. Choose an initial simplified model $\hat{G}_r^0(s)$.
- 2. Get an error function $\|\hat{G}(s) \hat{G}_{r/m}(s)\|_2$
- 3. Use the Powell optimization method [55] to iterate a step to obtain a better estimation of the $\hat{G}_{r/m}^1(s)$ model.

4. Set
$$\hat{G}^0_{r/m}(s) \leftarrow \hat{G}^1_{r/m}(s)$$
, go to step 2 until an optimal LOA model $\hat{G}^*_{r/m}(s)$ is obtained

4. Results and Discussion

The algorithm's performance in managing the AVR system specified in Equation (1) is validated by the simulations that follow. The simulations were created using the MAT-LAB/SIMULINK software. Table 3 provides a list of the proposed IABC algorithm's parameters.

 Table 3. IABC-FOPID Parameters for solving optimization problems.

Parameter	Value
Population size	40
Maximum cycle number	200
Lower bound for $[K_p; K_i; K_d; \lambda; \mu]$	[0.001; 0.001; 0.001; 0.001; 0.001]
Upper bound for $[K_p; K_i; K_d; \lambda; \mu]$	[15; 10; 10; 2; 2]
Dimension for optimization problem	5

Table 4 shows the parameters of the IABC/LOA-FOPID controller that was identified during the optimization process.

Controller Type	K_p	K _i	K _d	λ	μ
IABC/LOA-FOPID [Proposed]	1.9605	0.4922	0.2355	1.4331	1.5508
IWOA-PID [21]	0.8167	0.6898	0.2799	1	1
PSO-PID [12]	0.6254	0.4577	0.2187	1	1
ABC-PID [15]	0.6352	0.4235	0.2241	1	1
CS-PID [26]	0.6198	0.4165	0.2126	1	1
MOL-PID [28]	0.5857	0.4189	0.1772	1	1
GA-PID [12]	0.8851	0.7984	0.3158	1	1
LUS-PID [31]	0.6190	0.4222	0.2058	1	1
TSA [23]	1.1281	0.9567	0.5671	1	1

Table 4. Gain parameters of the proposed controller and other compared controllers.

For the AVR model system given in Equation (1) with the following fractional PID parameters: $K_p = 1.9605$, $K_i = 0.4922$, $K_d = 0.2355$, $\lambda = 1.4331$ and $\mu = 1.5508$, an IABC algorithm is used to build a fractional PID controller.

The IABC/FPID controller is given by:

$$G_{IABC/FOPID}(s) = 1.9605 + 0.4922s^{-1.4331} + 0.2355s^{1.5508}$$
(21)

Consequently, the Oustaloup approach with $\omega_b = 0.1$ rad/s, $\omega_h = 10$ rad/s and unity feedback yields the IABC/HOA-FOPID controller's closed loop transfer function as follows:

$$G_{CL_{IABC/HOA-FOPID}}(s) = \frac{0.08371s^{13} + 10.18s^{12} + 197.6s^{11} + 1756s^{10} + 9249s^9 + 3.152e04s^8 + 7.033e04s^7 + 1.016e05s^6 + 9.449e04s^5 + 5.696e04s^4 + 2.234e04s^3 + 5553s^2 + 786.3s + 47.43}{0.0004s^{15} + 0.05533s^{14} + 1.776s^{13} + 34.72s^{12} + 400.2s^{11} + 2787s^{10} + 1.261e04s^9 + 3.876e04s^8 + 8.072e04s^7 + 1.115e05s^6 + 1.006e05s^5 + 5.936e04s^4 + 2.289e04s^3 + 5619s^2 + 789.3s + 47.43$$

and it can be observed that the approximation model's order is 15, which is rather high.

We can now obtain the low-order approximation, such as r = 3, m = 5. The following equation gives the reduced model:

$$G_{CL_{IABC/LOA-FOPID}}(s) = \frac{12.78s^3 + 0.7049s^2 + 0.7921s + 0.04369}{s^5 + 3.157s^4 + 13.22s^3 + 0.9005s^2 + 0.8154s + 0.04369}$$
(23)

Figure 7 illustrates the Bode diagrams of the high- and low-order approximation models.



Figure 7. Bode diagram approximations.

The low-order approximation model, as it can be seen from the Figure 7, is remarkably close to the high-order approximation model.

The PID controller parameters shown in Table 4 were utilized for comparison with other current techniques such as IWOA-PID [21], PSO-PID [12], ABC-PID [15], CS-PID [26], MOL-PID [28], GA-PID [12], LUS-PID [31], and TSA [23]. Consequently, the closed loop transfer function G_{CL} derived via IWOA-PID [21], PSO-PID [12], ABC-PID [15], CS-PID [26], MOL-PID [28], GA-PID [12], LUS-PID [31], and TSA [23], are as follows:

$$G_{CL_{IWOA-PID}} = \frac{0.028s^3 + 2.882s^2 + 8.236s + 6.898}{0.0004s^5 + 0.0454s^4 + 0.555s^3 + 4.31s^2 + 9.167s + 6.898}$$
(24)

$$G_{CL_{PSO-PID}} = \frac{0.02187 \,\mathrm{s}^3 + 2.25\mathrm{s}^2 + 6.3\mathrm{s} + 4.557}{0.0004\mathrm{s}^5 + 0.0454\mathrm{s}^4 + 0.555\mathrm{s}^3 + 3.697\mathrm{s}^2 + 7.254\mathrm{s} + 4.577} \tag{25}$$

$$G_{CL_{ABC-PID}} = \frac{0.02241 \,\mathrm{s}^3 + 2.304\mathrm{s}^2 + 6.395\mathrm{s} + 4.235}{0.0004\mathrm{s}^5 + 0.0454\mathrm{s}^4 + 0.555\mathrm{s}^3 + 3.75\mathrm{s}^2 + 7.352\mathrm{s} + 4.235} \tag{26}$$

$$G_{CL_{CS-PID}} = \frac{0.02126 \,\mathrm{s}^3 + 2.188 \mathrm{s}^2 + 6.24 \mathrm{s} + 4.165}{0.0004 \mathrm{s}^5 + 0.0454 \mathrm{s}^4 + 0.555 \mathrm{s}^3 + 3.636 \mathrm{s}^2 + 7.198 \mathrm{s} + 4.165} \tag{27}$$

$$G_{CL_{MOL-PID}} = \frac{0.01772 \,\mathrm{s}^3 + 1.831 \,\mathrm{s}^2 + 5.899 \mathrm{s} + 4.189}{0.0004 \mathrm{s}^5 + 0.0454 \mathrm{s}^4 + 0.555 \mathrm{s}^3 + 3.282 \mathrm{s}^2 + 6.857 \mathrm{s} + 4.189} \tag{28}$$

$$G_{CL_{GA-PID}} = \frac{0.03158 \text{ s}^3 + 3.247 \text{s}^2 + 8.931 \text{s} + 7.984}{0.0004 \text{s}^5 + 0.0454 \text{s}^4 + 0.555 \text{s}^3 + 4.668 \text{s}^2 + 9.851 \text{s} + 7.984}$$
(29)

$$G_{CL_{LUS-PID}} = \frac{0.02058 \,\mathrm{s}^3 + 2.12\mathrm{s}^2 + 6.232\mathrm{s} + 4.222}{0.0004\mathrm{s}^5 + 0.0454\mathrm{s}^4 + 0.555\mathrm{s}^3 + 3.568\mathrm{s}^2 + 7.19\mathrm{s} + 4.222} \tag{30}$$

$$G_{CL_{TSA-PID}} = \frac{0.05671s^3 + 5.784s^2 + 11.38s + 9.567}{0.0004s^5 + 0.0454s^4 + 0.555s^3 + 7.181s^2 + 12.28s + 9.567}$$
(31)

4.1. Transient Response Analysis Comparison

Figures 8-11 present the results of the step response and transient response comparison analysis for AVR control systems designed using different approaches. Figure 8 shows the step response comparisons while bar chart comparisons of maximum overshoot (in %), settling time (for $\pm 2\%$ tolerance) and rise times (for $10\% \rightarrow 90\%$) are given by Figures 10–12.

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Figure 8. AVR terminal voltage comparison with existing techniques: IWOA-PID [21], PSO-PID [12], ABC-PID [15], CS-PID [26], MOL-PID [28], GA-PID [12], LUS-PID [31], and TSA [23].



Figure 9. Percentage of overshoots for different techniques.



Figure 10. Settling times for different techniques.



Figure 11. Rise times for different techniques.



Figure 12. Bode plots comparison with existing techniques.

According to these figures, the IABC/LOA-FOPID controller obviously has a superior time response than the others, including the ABC-PID controller. As a result, the suggested controller design technique outperforms not only the ABC-based design approach, but also various methods for controller design, such as IWOA-PID [21], PSO-PID [12], CS-PID [26], MOL-PID [28], GA-PID [12], LUS-PID [31], and TSA [23], with higher transient stability, quick damping characteristics, and less overshoot.

Taking into consideration different parameters such as rise time, settling time and overshoot percentage, we made a comparative study and evaluation of our controller used in an AVR system application with other tuning PID techniques available in the literature. The results are shown in Table 5.

Controller Type	Maximum Overshoot M _p [%]	Settling Time t _s [s]	Rise Time t _r [s]	IAE
IABC/LOA-FOPID [Proposed]	2.3323	0.3129	0.1373	0.109
IWOA-PID [21]	6.9064	0.6466	0.2266	0.3150
PSO-PID [12]	0.4349	0.4609	0.3007	0.2917
ABC-PID [15]	0.0081	1.2041	0.2957	0.2892
CS-PID [26]	0.0198	1.1681	0.3082	0.2916
MOL-PID [28]	1.9547	0.5154	0.3432	0.3086
GA-PID [12]	8.6338	0.6055	0.2042	0.3048
LUS-PID [31]	0.5896	0.4778	0.3125	0.2930
TSA-PID [23]	15.4763	0.7582	0.1321	0.3553

Table 5. Comparative analysis of the transient response.

Table 5 shows that the performance indices of maximum overshoot values ($M_p[\%]$) obtained with PSO-PID [12], ABC-PID [15], CS-PID [26] and LUS-PID [31] have less overshoot and oscillations than the proposed controller. However, these controllers are slower in terms of rise time and settling time than other PID controllers. On the other hand, the proposed IABC/LOA-FOPID controller shows superior performance over the different optimized PID controllers in terms of settling time and rise time. Furthermore, the presented algorithm significantly reduces the performance index value.

4.2. Comparison of Frequency Domain Analyses

Bode plots with different controller settings are compared in Figure 12. Table 6 summarizes the results of the comparative frequency response performance study. Gain margin (G_m : in decibels), phase margin (φ_m : in degrees) and bandwidth (B_w : in Hertz) are all parts of the performance criteria.

Controller Type	Gain Margin G _m [db]	Phase Margin φ_m [°]	Bandwidth B_w [Hz]
ABC/LOA-FOPID [Proposed]	Inf	178.7980	15.7280
IWOA-PID [21]	Inf	161.6094	9.6571
PSO-PID [12]	Inf	173.8067	7.5015
ABC-PID [15]	Inf	180	7.6998
CS-PID [26]	Inf	180	7.3393
MOL-PID [28]	Inf	180	6.3391
GA-PID [12]	Inf	116.3886	10.6594
LUS-PID [31]	Inf	180	7.1673
TSA-PID [23]	Inf	77.3967	16.2326

Table 6. Comparative analysis of the frequency response.

The data clearly shows that the proposed IABC/LOA-FOPID and TSA-PID controllers are the most stable systems in terms of the frequency response criteria.

As shown in Table 6, the AVR systems with the ABC-PID [15], CS-PID [26], MOL-PID [28] and LUS-PID [31] controllers have the maximum phase margin of 180°, while the proposed IABC/LOA-FOPID controller has an acceptable phase margin (almost 180°). On the other hand, the proposed IABC/LOA-FOPID and TSA-PID [23] controllers have the largest bandwidth and the quickest response. It is worth mentioning that a broad bandwidth enables the system to precisely follow random inputs.

4.3. Stability Assessment

The three most important stability measurement criteria, namely, pole-zero map, rootlocus plot, and Bode analyses, were performed to evaluate the stability of the proposed IWOA-based AVR design, and are illustrated in Figures 13–15, respectively.



Figure 13. Pole-zero map (x, pole; o, zero).



Figure 14. Root locus plot.



Figure 15. Bode plot.

Figures 13 and 14 show that the closed-loop poles of the ABC/LOA-FOPID-based AVR system are located at s1 = -2.49×10^{-3} , s2 = $-2.16 \times 10^{-1} + 7.75 \times 10^{-1}$ i, s3 = $-2.16 \times 10^{-1} + 7.75 \times 10^{-1}$ i, s4 = $-1.25 \times 10^{+1} + 1.12 \times 10^{+1}$ i, and s5 = $-1.25 \times 10^{+1} + 1.12 \times 10^{+1}$ i, with comparable damping ratios of 1.00, 2.68 × 10^{-1} , 2.68 × 10^{-1} , 7.46 × 10^{-1} , and 7.46 × 10^{-1} . Since all of the closed-loop poles are on the left half of the s-plane, the system is stable and has an acceptable frequency response.

The AVR system (or any control system) provides information on the AVR system's time-dependent response and stability. Any root locus diagram may be used to compute the poles (Eigen values) and damping ratio. Larger stability is associated with more negative poles and a higher damping ratio. Table 7 compares the simulation results of

PID Tuning Methods Closed-Loop Poles Damping Ratio Time Constant [s] Frequency [rad/s] -2.49×10^{-3} $4.01 \times 10^{+2}$ 1.00 2.49×10^{-3} $-2.16 \times 10^{-1} + 7.75 \times 10^{-1}$ i $8.05 imes 10^{-1}$ 2.68×10^{-1} 4.64 ABC/LOA-FOPID $-2.16 \times 10^{-1} + 7.75 \times 10^{-1}$ i $2.68 imes 10^{-1}$ 8.05×10^{-1} 4.64[Proposed] $-1.25 \times 10^{+1} + 1.12 \times 10^{+1}i$ $7.46 imes 10^{-1}$ $1.68 imes 10^{+1}$ 8.00×10^{-2} $-1.25 \times 10^{+1} + 1.12 \times 10^{+1}i$ 8.00×10^{-2} $7.46 imes 10^{-1}$ $1.68\times10^{+1}$ $-1.01 \times 10^{+2}$ $1.01\times 10^{+2}$ $9.92 imes 10^{-3}$ 1.00 $-1.35 + 6.77 \times 10^{-1}$ i $8.93 imes 10^{-1}$ 1.51 $7.43 imes 10^{-1}$ IWOA-PID [21] $-1.35 + 6.77 \times 10^{-1}i$ $8.93 imes 10^{-1}$ 1.51 $7.43 imes 10^{-1}$ $5.78 imes 10^{-1}$ 1.99×10^{-1} -5.02 + 7.09i8.68 -5.02 + 7.09i $5.78 imes 10^{-1}$ 8.68 $1.99 imes 10^{-1}$ -1.01×10^{-2} 1.00 $1.01 \times 10^{+2}$ 9.94×10^{-3} $-1.30 + 3.92 \times 10^{-1}i$ 9.58×10^{-1} 1.36 7.67×10^{-1} PSO-PID [12] $9.58 imes 10^{-1}$ 1.36 $7.67 imes 10^{-1}$ $-1.30 + 3.92 \times 10^{-1}i$ $6.56 imes 10^{-1}$ -5.14 + 5.91i 7.84 1.94×10^{-1} -5.14 + 5.91i $6.56 imes 10^{-1}$ $1.94 imes 10^{-1}$ 7.84 $-1.01\times10^{+2}$ $1.01 \times 10^{+2}$ 9.94×10^{-3} 1.00 -1.121.00 1.12 8.97×10^{-1} ABC-PID [15] $6.66 imes 10^{-1}$ -1.501.00 1.50 $6.47 imes 10^{-1}$ $1.95 imes 10^{-1}$ -5.13 + 6.04i7.93 $6.47 imes 10^{-1}$ 1.95×10^{-1} -5.13 + 6.04i7.93 $-1.01 \times 10^{+2}$ $1.01\times 10^{+2}$ 1.00 $9.94 imes 10^{-3}$ -1.07 9.31×10^{-1} 1.00 1.07 CS-PID [26] -1.621.00 1.62 $6.15 imes 10^{-1}$ $6.63 imes 10^{-1}$ 1.96×10^{-1} -5.11 + 5.76i7.70 -5.11 + 5.76i $6.63 imes 10^{-1}$ 1.96×10^{-1} 7.70 $-1.00 \times 10^{+2}$ $1.00 \times 10^{+2}$ 1.00 9.95×10^{-3} -1.061.00 1.06 $9.41 imes 10^{-1}$ MOL-PID [28] -2.11 1.00 2.11 $4.74 imes 10^{-1}$ $7.21 imes 10^{-1}$ -4.92 + 4.72i6.82 2.03×10^{-1} -4.92 + 4.72i 7.21×10^{-1} 2.03×10^{-1} 6.82 $-1.00 \times 10^{+2}$ $1.01 \times 10^{+2}$ $9.91 imes 10^{-3}$ 1.00 8.43×10^{-1} $-1.29 + 8.20 \times 10^{-1}i$ 1.52 7.78×10^{-1} GA-PID [12] $-1.29 + 8.20 \times 10^{-1} \mathrm{i}$ $8.43 imes 10^{-1}$ 1.52 $7.78 imes 10^{-1}$ $5.45 imes 10^{-1}$ $1.99 imes 10^{-1}$ -5.03 + 7.73i9.23 5.45×10^{-1} 1.99×10^{-1} -5.03 + 7.73i9.23 $-1.01 \times 10^{+2}$ $1.01 \times 10^{+2}$ 9.94×10^{-3} 1.00 9.40×10^{-1} -1.061.00 1.06 LUS-PID [31] -1.741.00 1.74 $5.75 imes 10^{-1}$ -5.06 + 5.57i $6.73 imes 10^{-1}$ 7.53 1.97×10^{-1} -5.06 + 5.57i 6.73×10^{-1} 7.53 $1.97 imes 10^{-1}$ $-1.01\times10^{+2}$ $1.02 \times 10^{+2}$ 1.00 9.85×10^{-3} $7.48 imes 10^{-1}$ $-9.26 \times 10^{-1} + 8.22 \times 10^{-1}$ i 1.24 1.08 TSA-PID [23] $-9.26 \times 10^{-1} + 8.22 \times 10^{-1}$ i $7.48 imes 10^{-1}$ 1.24 1.08 $1.24 imes 10^{+1}$ $1.98 imes 10^{-1}$ $4.07 imes 10^{-1} imes 10^{-1}$ $-5.05 + 1.13 \times 10^{+1}i$ $-5.05 + 1.13 \times 10^{-1}i$ 4.07×10^{-1} $1.24 \times 10^{+1}$ 1.98×10^{-1}

 Table 7. AVR system closed-loop poles, damping ratios frequencies and time constants.

frequencies and time constants.

several optimization-technique-based AVR systems for closed-loop poles, damping ratios,

4.4. Noise Attenuation

Additive noise is considered in the input of the process to be regulated. Figures 16 and 17 depict the temporal response characteristics of different integer order and fractional order PID controllers with random output noise of 2% and 20% of the reference signal amplitude, respectively. The overshoot produced with the various integer order PID and fractional controllers is extremely similar, as shown in Figure 16.



Figure 16. Controller's comparison with random output noise for 2% of the amplitude of the reference signal.



Figure 17. Controller's comparison with random output noise for 20% of the amplitude of the reference signal.

Due to noise, the performance of the IABC/LOA-FOPID has obviously degraded, with an increased overshoot. However, due to the derivative term, the IABC/LOA-FOPID controller achieves better settling time in the range of 0.29 s, compared to the other existing techniques, as can be seen in Figure 17.

4.5. Analysis of Robustness Comparison

In order to maintain the system's responsiveness within acceptable limits, a robust controller is needed. Therefore, a robustness analysis was performed to determine how stable the proposed method is under step perturbations.

In Figure 18, the proposed IABC/LOA/FOPID controller's disturbance rejection performance is compared to that of the IWOA-PID [21], PSO-PID [12], ABC-PID [15], CS-PID [26], MOL-PID [28], GA-PID [12], LUS-PID [31] and TSA/PID [23] controller designs for the identical transfer function of an AVR system.



Figure 18. Disturbance rejection comparison for different techniques.

The most efficient control mechanism for disturbance rejection is provided by the proposed controller IABC/LOA-FOPID, which has a more stable structure, as shown in Figure 18. Although all the controllers have high peak errors, the IABC/LOA-FOPID controller performs noticeably better.

5. Conclusions

In this paper, a low-order approximation (LOA) model of a fractional order PID (FOPID) based on a modified artificial bee colony (ABC) technique for an integer-order automatic voltage regulator (AVR) was proposed. The new robust controller is named IABC/LOA-FOPID. This proposed controller improved on the performance of the ABC/FOPID controller, which is characterized by a large (or high-order) approximation using an integer order transfer function, which necessitates the employment of a large number of parameters. The transient and frequency response characteristic parameters of the AVR system, such as maximum overshoot, settling time, rise time, bandwidth, gain margin, and phase margin, were evaluated using the proposed IABC/LOA-FOPID and other existing controllers such as IWOA-PID [21], PSO-PID [12], ABC-PID [15], CS-PID [26], MOL-PID [28], GA-PID [12], LUS-PID [31], and TSA [23]. The results show that the proposed controller enhanced dynamic performance, namely speed convergence, and is well suited for the AVR system. Furthermore, robustness, root locus, and Bode analyses were used and compared to recently published findings to demonstrate the superiority of the proposed IABC/LOA-FOPID controller. The result reveals that the proposed controller has characteristics of high stability for AVR systems and performs better in terms of noise attenuation and disturbance rejection.

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