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# Type Ia supernova observations combining data from the *Euclid* mission and the Vera C. Rubin Observatory

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## ABSTRACT

The *Euclid* mission will provide first-of-its-kind coverage in the near-infrared over deep (three fields,  $\sim 10$ – $20$  square degrees each) and wide ( $\sim 10\,000$  square degrees) fields. While the survey is not designed to discover transients, the deep fields will have repeated observations over a two-week span, followed by a gap of roughly six months. In this analysis, we explore how useful the deep field observations will be for measuring properties of Type Ia supernovae (SNe Ia). Using simulations that include *Euclid*'s planned depth, area, and cadence in the deep fields, we calculate that more than 3700 SNe between  $0.0 < z < 1.5$  will have at least five *Euclid* detections around peak with signal-to-noise ratio larger than 3. While on their own, *Euclid* light curves are not good enough to directly constrain distances, when combined with legacy survey of space and time (LSST) deep field observations, we find that uncertainties on SN distances are reduced by 20–30 per cent for  $z < 0.8$  and by 40–50 per cent for  $z > 0.8$ . Furthermore, we predict how well additional *Euclid* mock data can be used to constrain a key systematic in SN Ia studies – the size of the luminosity ‘step’ found between SNe hosted in high-mass ( $> 10^{10} M_{\odot}$ ) and low-mass ( $< 10^{10} M_{\odot}$ ) galaxies. This measurement has unique information in the rest-frame near-infrared (NIR). We predict that if the step is caused by dust, we will be able to measure its reduction in the NIR compared to optical at the  $4\sigma$  level. We highlight that the LSST and *Euclid* observing strategies used in this work are still provisional and some level of joint processing is required. Still, these first results are promising, and assuming that *Euclid* begins observations well before the *Nancy Roman Space Telescope (Roman)*, we expect this data set to be extremely helpful for preparation for *Roman* itself.

**Key words:** supernovae: general – dust, extinction – distance scale.

## 1 INTRODUCTION

The *Euclid* survey is a space-based mission with the primary goal of understanding the accelerating expansion of the universe and the nature of its components. Its primary science is optimized for two complementary cosmological probes: weak gravitational lensing and baryonic acoustic oscillations. The telescope will allow for both high-precision photometric imaging in the near-infrared (NIR) as well as spectroscopy. While Astier et al. (2014) proposed for a transient survey for *Euclid* that would enable a Stage IV dark energy measurement (Albrecht et al. 2006) with Type Ia supernovae (SNe Ia), this survey is currently unplanned. In this paper, we study what may still be leveraged in terms of discovery and measurements of SNe Ia, given a survey that is not designed for such a study but is still unique in its capabilities.

The majority of surveys used for SN Ia cosmological studies are conducted in the optical wavelength range (ex., Pantheon+; Brout et al. 2022; Scolnic et al. 2022). In the NIR, there have been a

handful of surveys that discover or follow-up SNe Ia at low redshift ( $z < 0.08$ ) like CSP (Hamuy et al. 2006), CfA (Wood-Vasey et al. 2008; Friedman et al. 2015), DEHVILS (Peterson et al. 2023), HSF (Do et al. in prep.), but only the RAISIN survey (Jones et al. 2022) measured light curves of SNe at intermediate  $z$  ( $0.3 < z < 0.5$ ). The RAISIN program combined the NIR data with light curves measured in the optical from Pan-STARRS (Chambers et al. 2016) and the dark energy survey (Smith et al. 2020a), and the total number of light curves usable for cosmological studies was 37. Therefore, even a small number of light curves at higher redshift measured in the NIR would be a significant contribution to the field (ex., SUSHI; *HST*-GO 15363, Suzuki et al. 2016).<sup>1</sup>

The challenge for a transient survey with *Euclid* is its cadence. Typically, surveys of SNe Ia have cadences of 5–10 d in order to measure the rise, peak, and decline of the light curve in multiple passbands. In *Euclid*'s deep fields, as discussed below, there is a series of observations over approximately a week and then a gap of six months. The only works so far that have studied the viability of

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<sup>1</sup><https://www.stsci.edu/hst/phase2-public/15363.pdf>.

a transient survey with poor cadence optimization for SN studies are Inserra et al. (2018), Moriya et al. (2022), and Tanikawa et al. (2022), which are focused on long-duration transients like pair-instability SNe and superluminous SNe. We build off these works but change the focus to SNe Ia and explore the possibility of combining *Euclid* with the ground-based legacy survey of space and time (LSST; Ivezić et al. 2019). LSST, conducted on the Vera C. Rubin Observatory (hereafter Rubin), will measure optical light curves for hundreds of thousands of SNe Ia, and it is estimated that a large fraction of these light curves ( $>1$  million according to Frohmaier et al. in prep.) will have sufficient quality<sup>2</sup> to be used for high-precision cosmology (assuming we have redshift information for all these events). It is expected to have significant overlap in time and footprint with the *Euclid* mission (Capak et al. 2019), and this could yield a large SN sample with high quality optical and NIR data.

To enable a study of the usefulness of *Euclid* measurements of SNe Ia, we use the SuperNNova ANALysis software package (SNANA; Kessler et al. 2009a), which has been used for a large number of survey forecasts (Jones et al. 2017; Kessler et al. 2019a, b; Popovic et al. 2021; Vincenzi et al. 2021). We also rely on new work that extends the SN Ia spectral model into the NIR from recent studies using their SALT3 framework (Pierel et al. 2018; Kenworthy et al. 2021; Pierel et al. 2022). For *Euclid* simulations, we use the *Euclid* observing strategy and survey description presented by Euclid Collaboration (2022b; hereafter EC22). For LSST simulations, we leverage recent work in LSST Dark Energy Science Collaboration (LSST DESC 2021) and Sánchez et al. (2022) and recreate this work at the catalogue level. While the number of SNe measured with *Euclid* is likely a small fraction of the many thousands of SNe measured by LSST, the NIR information from *Euclid* can provide key tests of systematics that will enhance the dark energy constraints from LSST. One such area, in particular, is a better understanding of the intrinsic scatter of SNe Ia, which explains residual dispersion in standardized brightnesses after accounting for measurement uncertainties. One of the leading explanations for this scatter is that it is due to variations in the reddening ratios in different galaxies (Brout & Scolnic 2021). A prediction from the Brout & Scolnic (2021) model is that in the NIR, correlations seen between standardized brightnesses and host galaxy properties should disappear (Uddin et al. 2020; Johansson et al. 2021; Ponder et al. 2021a). As samples used to evaluate this prediction with NIR data are small and mostly at low- $z$  with specific selection biases, *Euclid* could make a critical measurement for future SNe Ia analyses.

Furthermore, SN data from *Euclid* can be an excellent preparatory sample for the *Nancy Grace Roman Survey Telescope* (*Roman*; Hounsell et al. 2018; Rose et al. 2021), which has been specifically designed for SNe Ia observations. For *Roman*, the cadence is  $\sim 5$  d, which will make it ideal for discovering and measuring SNe Ia. Still, as *Euclid* will launch more than a couple years before *Roman*, this could be a fantastic opportunity for *Roman* preparation. These statements all rely on whether *Euclid* data will be processed to discover and measure SNe. One of the main goals of this analysis is to advocate for this ability. The structure of this paper is as follows: In Section 2, we describe the *Euclid* and LSST surveys and the catalogue-level simulations. In Section 3, we show expected light curves as observed with *Euclid* along with numbers of SNe measured and distance constraints. In Section 4, we forecast

constraints on correlations between supernova properties and host-galaxy properties using *Euclid*. Our final remarks are in Section 5.

## 2 SIMULATIONS

### 2.1 Simulation framework

Simulations used in this analysis are generated and analysed using the SNANA software package (Kessler et al. 2009a).<sup>3</sup> SNANA is an open-source package designed to generate catalogue level simulations of transient surveys.<sup>4</sup> In this analysis, we only simulate SNe Ia and their host galaxies, and we assume a flat  $\Lambda$ CDM cosmological model with Hubble constant  $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$  and  $\Omega_M = 0.311$ .

The main steps that constitute the SNANA simulation are the following. First, SN Ia volumetric rate measurements are used to estimate the absolute number of SNe expected to explode within a volume and time interval. In this work, we model rates following Hounsell et al. (2018) and consider a time window of five years (out of the 6-yr duration of the *Euclid* mission, when the two southern deep fields will be regularly observed) and a redshift range of  $0 < z < 1.5$ . SNe Ia are then simulated using the SN Ia SALT3 model presented by Kenworthy et al. (2021) and extended into the NIR by Pierel et al. (2022). Compared to its predecessor, SALT2, the SALT3 model is trained on a larger SN sample, with many high-quality, high-redshift SNe, which improves the coverage in the rest-frame UV. This model well constrains the spectral energy distribution (SED) of an SN Ia within a wavelength range of 3000–20 000 Å and between a phase range of  $-15$  to  $+45$  (rest frame) d from peak brightness.

The SALT3 model is described by five parameters: SN redshift  $z$ , an amplitude term  $x_0$ , SN light-curve ‘stretch’ term ( $x_1$ ), SN restframe  $B - V$  colour at peak ( $c$ ) and time of peak brightness  $t_0$ . In our simulations, SN peak times are uniformly generated across the six years of the mission, and SN  $c$  distributions are simulated following Scolnic & Kessler (2016a). We generate SNe Ia brightnesses ( $x_0$ ) so that their intrinsic scatter in luminosity follows Guy et al. (2010) and we parametrize the linear luminosity–stretch correlation ( $\alpha$ ) and luminosity–colour correlations ( $\beta$ ) assuming slopes of  $\alpha = 0.14$  and  $\beta = 3.1$ . For the baseline simulation, we generate the SN colours using the distributions by Scolnic & Kessler (2016b). In order to model SN  $x_1$  values and their correlation with host galaxy stellar masses,  $M_*$ , we use the approach and distributions by Popovic et al. (2021).

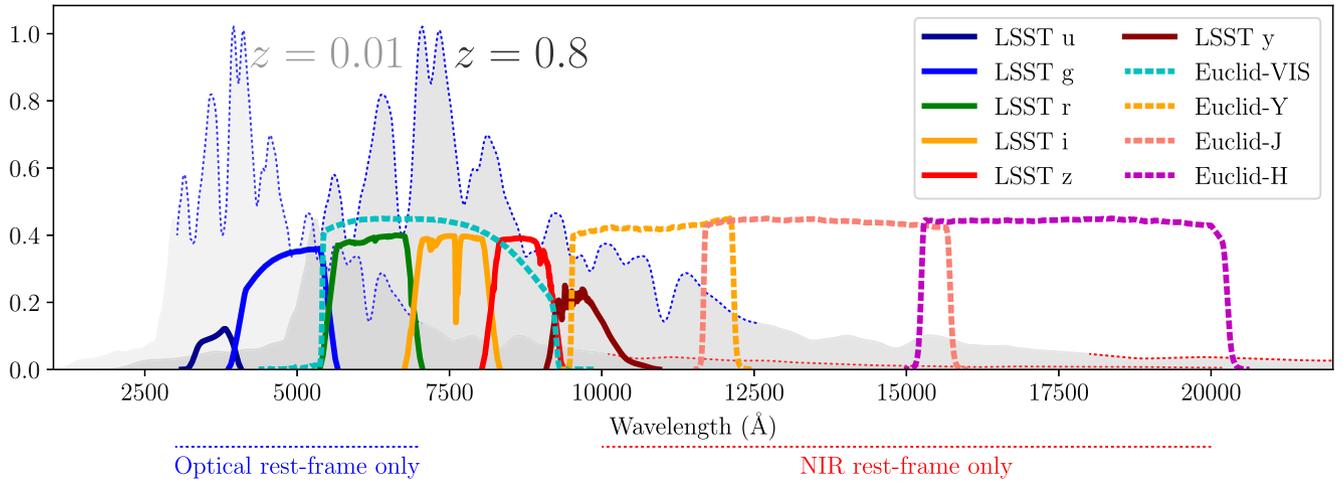
After generating the sample of SNe Ia and associated SED models, various astrophysical effects are applied, including redshifting, cosmological dimming, and dust extinction from host galaxy and Milky Way. We use a Cardelli, Clayton & Mathis (1989) dust law with  $R_V = 3.1$  for Milky Way dust extinction.

Each simulated SN is then associated to a host galaxy, which in this analysis is chosen using the galaxy catalogue presented by Smith et al. (2020b). This catalogue was generated from DES Science Verification data and includes  $\sim 380\,000$  galaxies at  $0 < z < 1.5$ . Galaxy association is implemented following measurements of SN Ia rates as a function of galaxy properties (as described in Vincenzi et al. 2021). We use the rates presented by Wiseman et al. (2021) and simulate correlations between SN stretch and SN host galaxy stellar mass following Popovic et al. (2021).

<sup>2</sup>In SN Ia cosmological analyses, we apply several selection cuts based on the light-curve fitted parameters and their uncertainties, see Section 3.2 for more details.

<sup>3</sup>[https://github.com/RickKessler/\(0:sc\)snana/\(0:sc\)](https://github.com/RickKessler/(0:sc)snana/(0:sc)).

<sup>4</sup>SNANA is not developed to generate pixel-level simulated images, it simulates the ‘extracted’ SN data-points.



**Figure 1.** Transmission function of the LSST filters (*ugrizy*) and the *Euclid* filters (*VIS + YJH*). We compare the spectral energy distribution at peak brightness of an SN Ia at  $z = 0.01$  and  $z = 0.8$ . LSST filters throughput curves include atmospheric extinction estimated assuming 1.2 airmass (see <https://github.com/lstt/throughputs> for more details).

Given the final SED model and SN host galaxy, the ‘true’ broadband photometry of each simulated source is estimated by integrating the SN SED over the survey filters (in this analysis, the LSST and *Euclid* filters illustrated in Fig. 1). From the ‘true’ SN photometry, we estimate the ‘observed’ SN photometry by applying observational noise and adding background light from the host galaxy. This step uses the observing conditions provided in a pre-computed observational library (referred to as a ‘SIMLIB’) that includes information on cadence, zeropoints, sky noise, and PSF size for every night of observation, for every survey. In Sections 2.2 and 2.3, we discuss the LSST and *Euclid* observing libraries used in our simulations.

## 2.2 Simulations of the *Euclid* deep survey

We simulate SN Ia light curves as observed by the *Euclid* satellite according to planned observations of its deep field survey. The *Euclid* telescope will be equipped with a visible imager, with one broad filter referred to as *VIS*, a near-infrared imager with *Y, J, H* filters (see Fig. 1 and Euclid Collaboration 2022a) and NIR grisms. *Euclid* will perform a ‘wide’ survey (15 000 sq. deg.) and a ‘deep’ survey (50 sq. deg.) over six years.

There are three main deep fields planned: *Euclid* Deep Survey North (EDF-North, 17:58:55.9 +66:01:03.7, 20 sq. deg.), *Euclid* Deep Survey South (EDF-South, 04:04:57.84 –48:25:22.8, 23 sq. deg.), and *Euclid* Deep Survey Fornax (EDF-Fornax, 03:31:43.6 –28:05:18.6, 10 sq. deg.). Every six months, EDF-South and EDF-Fornax will be repeatedly observed for two weeks every 2–4 d, whereas EDF-North is scheduled for inhomogeneous cadence in observations, with consecutive visits ranging from 16 to 55 d. Therefore, for this analysis, we only consider EDF-South and EDF-Fornax. EDF-Fornax will be observed every six months for 6 consecutive nights, while EDF-South will be observed for 3–4 times over a time range of 13 d, every six months (see Inserra et al. 2018, for more details).

For *Euclid*, we use the ‘*Euclid* reference survey definition’ presented by EC22 (see fig. 29 and sec. 8). This is the latest version of the full *Euclid* schedule, and it includes observing cadence for both the wide and deep *Euclid* surveys, as well as observations of calibration

fields. This is the most up-to-date, publicly available schedule for *Euclid*. It predicts that *Euclid* will observe EDF-South and EDF-Fornax in August and February every year, i.e. at the beginning and towards the end of each LSST season (see Fig. 2 and Section 2.3). In Section 2.4, we discuss the caveats related to potential changes in the *Euclid* reference survey.

The two *Euclid* Deep Fields have excellent overlap with two of the five LSST deep drilling fields (see Fig. 2) and similar depth ( $5\sigma$  limiting magnitude of 26 for *VIS* and 24.1–24.5 for *YJH*, see EC22). Thus, there is potential for synergies with LSST transient science, despite the *Euclid* observing strategy not being optimized for it.

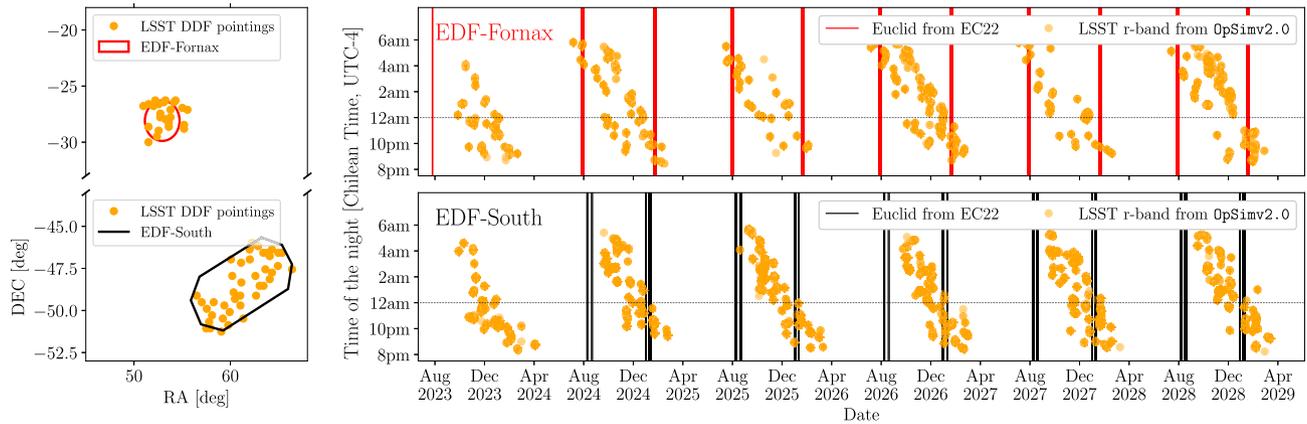
## 2.3 Simulations of the LSST deep drilling fields

Following the same approach and software used for *Euclid*, we simulate SN Ia light curves as observed by LSST. LSST is an optical imaging survey conducted on the Vera Rubin Observatory. It includes a wide fast deep survey (18 000 sq. deg.) and five deep drilling fields (DDF, approximately 100 sq. deg., depending on the dithering pattern). In this analysis, we focus on the two LSST DDFs that overlap with EDF-Fornax and EDF-South. The overlap between the two surveys in these sub-fields spans 10 and 23 sq. deg., respectively (Capak et al. 2019), and these are the solid angles assumed in our simulations. We note that the LSST DDF South was not originally planned and has been recently added due to the strong synergistic science possibilities presented by Guy et al. (2022).<sup>5</sup>

The cadence, exposure times, and observational noise for the considered LSST DDFs are simulated based on the output of the LSST Operations Simulation software. This software computes the LSST pointing history and relative observing conditions based on the LSST Feature-Based Scheduler (Naghieb et al. 2019). In our analysis, we use the LSST Operations Simulation version 2.0 (baseline, OpSim-v2.0),<sup>6</sup> and translate it into SNANA-readable

<sup>5</sup>The ‘Rubin–*Euclid* Derived Data Products: Initial Recommendations’ document. See also announcement in <https://community.lsst.org/t/scoc-endorsement-of-euclid-deep-field-south-observations/6406>.

<sup>6</sup>The simulations can be downloaded at [https://epyc.astro.washington.edu/~lynnj/opsim\\_downloads/fbs\\_2.0/baseline/](https://epyc.astro.washington.edu/~lynnj/opsim_downloads/fbs_2.0/baseline/), OpSim-v2.0 Summary Infor-

LSST starting date October 2023 and *Euclid* starting operations end of December 2022


**Figure 2.** Comparison between *Euclid* and LSST mock observing strategies in the Deep Fornax and Deep South fields. *Left:* Footprint of the *Euclid* Deep Fornax (red) and Deep South fields (black) footprints, compared to LSST pointings in the equivalent deep drilling fields. *Right:* Distribution of LSST *r*-band observations as a function of time of the night (in Chilean time, i.e. UTC-4) over five years and distribution of *Euclid* observations (red and black vertical lines, note that *Euclid* observes over 24 hr). LSST observing strategy is from OpSim-v2.0 and *Euclid* observing strategy is the ‘*Euclid* reference survey’ from EC22. EDF-Fornax field will be observed by *Euclid* every six months for six consecutive nights, EDF-South will be observed by *Euclid* every five and seven months, 3–4 times over a time range of 13/14 d. The EDF-Fornax and EDF-South will be visible from the Rubin Observatory only between August and February.

format (i.e. into a ‘SIMLIB’, as explained in Section 2.1), using the package published by Biswas et al. (2020). The extracted SIMLIB encapsulate all the information (sky noise, depth, zero-point) to simulate SN fluxes and flux uncertainties as if they were extracted from a ‘coadded’ LSST DDF image (LSST DDF images will be built by coadding 10/20/20/26/20 exposures for *grizly*, but we assume image coaddition and image subtraction steps have already been performed). We note that this cadence is not yet set, and further optimization of the observing strategy is ongoing (Gris et al. 2023).

For this mock observing strategy, the average cadence in the LSST DDFs is 5 d, and the  $5\sigma$  limiting magnitude is approximately 26th magnitude. In Fig. 2, we compare the distribution of LSST observations in the Fornax and South deep fields (all filters combined) with the distribution of observations from *Euclid*.

## 2.4 Uncertainties on the LSST and *Euclid* observing strategies

Our analysis uses publicly available observing strategies both for *Euclid* (EC22) and for LSST (Delgado et al. 2014; Delgado & Reuter 2016; Reuter et al. 2016). The ‘*Euclid* reference survey’ from EC22 assumes that *Euclid* will launch in 2022 October and begin survey operations in 2022 December. The LSST OpSim-v2.0 assumes that the beginning of survey operations for Rubin will be in 2023 October.

Both the LSST and *Euclid* surveys have been subject to significant delays in the last couple of years, therefore these publicly available starting dates are outdated. For LSST, the starting date is likely to be delayed by approximately one year (beginning of the survey in early 2025). For *Euclid*, the starting date is currently scheduled for 2023 July. Despite the uncertain starting dates, the visibility windows for the two fields considered in this analysis are very well defined, both for Rubin and for *Euclid*. Therefore, the overlap between the two

surveys presented in Fig. 2 is unaffected by shifts in the surveys’ starting dates. We further justify this statement below.

The visibility interval of the EDF-South and EDF-Fornax from Rubin is between August and February<sup>7</sup>, independently on which year operations will start. This is shown in Fig. 2. In August, the two deep fields start to become visible towards the end of the night. They remain observable until February, when they can be observed only at the very beginning of the night.

*Euclid* restrictions on the visibility windows for EDF-South and EDF-Fornax come from the fact that the telescope always must observe at 90 degrees from the Sun (forwards and backwards, see sec. 6.3. in EC22). For this reason, we can confidently assume that the time of year during which *Euclid* will observe EDF-South and EDF-Fornax will be roughly August and January. Even though generating an updated *Euclid* schedule would require the (not yet publicly available) scheduling software ECTILE (see sec. 6.3. and 7 in EC22), we expect minor changes compared to the ‘*Euclid* reference survey’ schedule (in particular, for the EDF-Fornax and EDF-South observations).

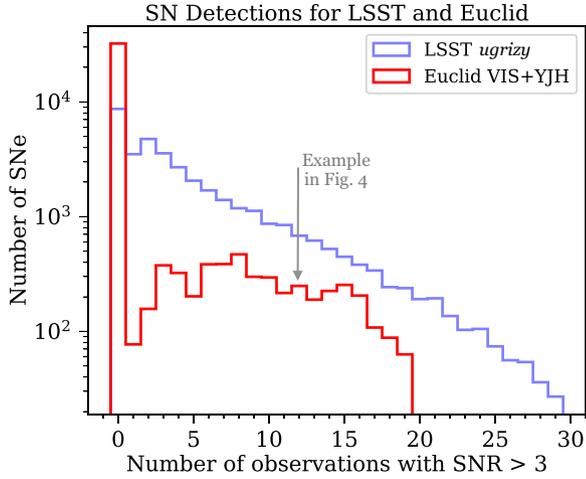
We highlight that changes in the LSST observing strategy also have the potential to affect the quality of LSST optical light curves and our ability to measure SN optical properties. This has the potential to significantly affect our results and SN Ia cosmology in the LSST DDFs in general.

## 2.5 Auxiliary spectroscopic observations

In our analysis, we assume spectroscopic redshifts are available for all measured SNe Ia. We expect most of these spectroscopic redshifts to be observed through the ground-based time-domain extragalactic survey (Swann et al. 2019) on the multi-object spectrograph 4MOST (de Jong et al. 2019) and, for EDF-Fornax, other multi-object spectrographs in the Northern hemisphere (Keck DEIMOS and potentially

Information Document and release can be found at <https://community.lsst.org/t/survey-simulations-v2-0-release-nov-2021/6059> and links therein. References for the LSST operation simulations: Delgado et al. (2014), Delgado & Reuter (2016), Reuter et al. (2016).

<sup>7</sup>This is when the two fields are at airmass  $\leq 1.5$  and  $20^\circ \leq$  altitude  $\leq 86.5^\circ$  and are observable for 34 min (68 visits) for the deep fields (Gris et al. 2023).



**Figure 3.** Frequency of SNe with detections with signal-to-noise ratio (SNR) larger than three in any LSST filter (empty blue histogram) and in any *Euclid* filter (empty red histogram). We consider only the (rest-frame) phase window of  $-15$  to  $+50$  d. No SN will have more than 20 observations from *Euclid*. This is because *Euclid* observes for a maximum of five nights (in four filters) every six months. In our simulations, we only record SNe with at least one detection with  $\text{SNR} > 3$  in LSST *griz* filters; all other SNe are ignored.

DESI-II, Subaru Prime Focus Spectrograph, Takada et al. 2014).<sup>8</sup> The *Euclid* telescope will also measure spectroscopic redshifts using NIR grisms (Euclid Collaboration 2022a). However, *Euclid* spectroscopic redshifts will only be available at the end of the *Euclid* survey which will be about five years after it begins operation.

### 3 SN LIGHT-CURVE QUALITY

In this section, we present the number and quality of SN Ia light curves simulated for LSST and *Euclid*. When running our simulations, we only record SNe that have at least one detection with signal-to-noise ratio (SNR) larger than three in one of the LSST filters at any phase. We remind that a detection is defined as a measurement from an already coadded LSST image.

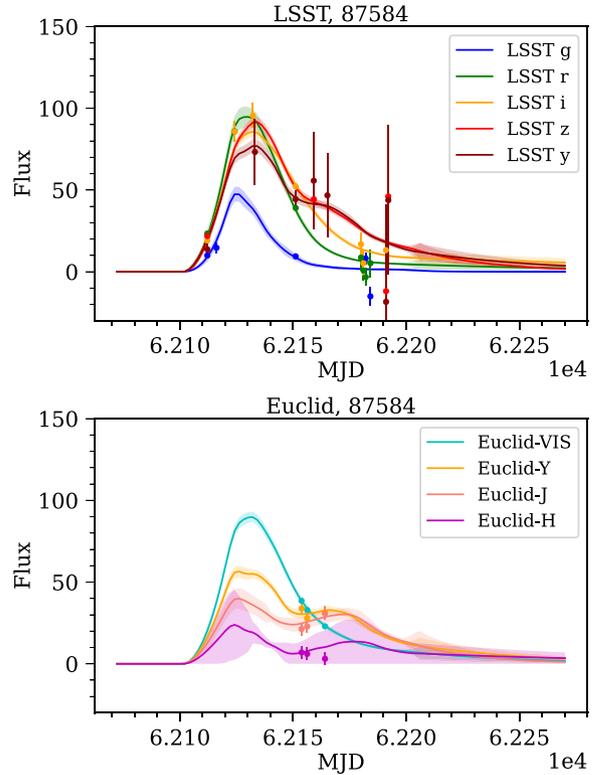
#### 3.1 SN detection

For each simulated SN, we consider a phase window of  $-15$  to  $+50$  (rest-frame) d from peak and we estimate the number of observations with SNR larger than three from *Euclid* (all filters combined) and from LSST (all filters combined). We present the distributions relative to the two surveys in Fig. 3.

Over the five-year window considered in this analysis, we predict to have 18 000 SNe Ia with at least five LSST observations (in any filter) with  $\text{SNR} > 3$ . The majority of these SNe will have no detections from *Euclid*. This is expected given the sparse cadence of the *Euclid* mission. However, we predict that approximately 3700 SNe will have at least five *Euclid* detections with  $\text{SNR} > 3$ , and 1900 SNe will have at least ten detections with  $\text{SNR} > 3$  from *Euclid*.

In Fig. 4, we show an example of a simulated light curve with LSST optical photometry and *Euclid* optical (*VIS*) and NIR (*YJH*)

<sup>8</sup>For example, the Hawaii Two-0 Survey (H20) is currently planning to perform deep Subaru Hyper-SuprimeCam imaging and Keck DEIMOS spectroscopic follow-up of the two *Euclid* deep fields EDF-North and EDF-Fornax, <https://h20.ifa.hawaii.edu/about>.



**Figure 4.** Example of an SN Ia (ID: 633) light curve simulated as seen with LSST (top) and as seen with *Euclid* (bottom). We provide these simulated light curves as examples of what output can be expected from plotting real data light curves. For this particular event, we simulate redshift  $z = 0.50$ , SN peak time  $t_0^{\text{true}} = 62131.27$ , SN peak brightness  $m_B^{\text{true}} = 22.73$ , SN stretch  $x_1^{\text{true}} = 0.25$ , and SN colour  $c^{\text{true}} = -0.04$  and recover  $t_0 = 62131.18 \pm 0.38$ ,  $m_B = 22.77 \pm 0.05$ ,  $x_1 = 0.06 \pm 0.35$ , and  $c = -0.07 \pm 0.04$  after fitting with SALT3. The SALT3 fitted light curves and relative uncertainties are presented as solid lines and shaded areas.

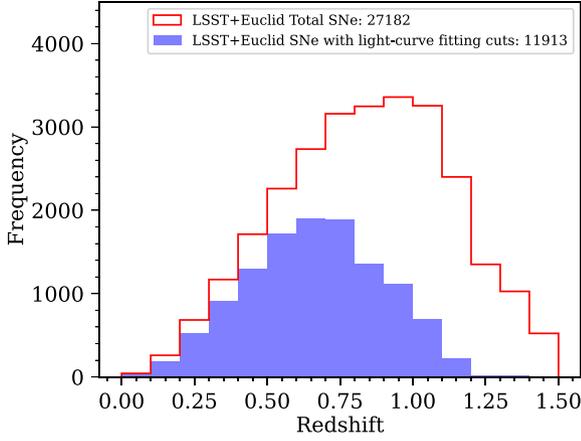
photometry. We expect a few hundred SNe to have similar data coverage and quality in the NIR (as shown in Fig. 3). In the next section, we show how the additional *Euclid* NIR data can significantly improve SN distance measurements inferred using LSST optical data alone.

#### 3.2 Supernova light-curve fitting and distances

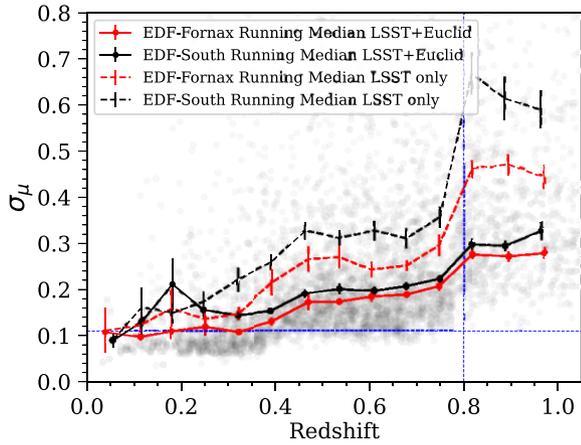
SNe Ia can serve as standard candles for measuring cosmological distances and constrain the expansion history of the Universe. Generally, we measure SN distances using the SN rest-frame *B*-band peak brightness. However, not all SNe are always measured at maximum light and in their rest-frame *B* band. For this reason, it is necessary to use SN Ia SED time-series models to perform light-curve fitting and determine SN light-curve properties and peak brightness.

For our analysis, we fit the simulated light curves using the same SALT3 model introduced in Section 2.1. In the fit, we assume the SN spectroscopic redshift is known and we only fit for the observed SN peak brightness in rest-frame *B*-band  $m_B$  (also defined as  $-2.5 \log_{10}(x_0)$ ), the SN light-curve stretch  $x_1$ , SN colour  $c$ , and time of peak brightness  $t_0$ , and we estimate the relative uncertainties.

Using LSST and *Euclid* mock data combined, we find that for approximately 27 000 SNe Ia the SALT3 fit converged, and 11 000 of these SNe pass the light-curve fitting quality cuts generally applied



**Figure 5.** Redshift distribution of the SNe Ia successfully fitted with the SALT3 model, and SNe Ia passing the SALT-based quality cuts discussed in Section 3.2.



**Figure 6.** Uncertainties in  $\mu$  for both EDF-Fornax (red lines) and EDF-South (black lines) considering combined LSST and *Euclid* data (solid lines) as well as LSST independently (dashed lines). We present these uncertainties as running medians of binned data, and we include the typical value for  $\sigma_{\text{int}}$  for cosmological analysis of optical SNe Ia sample ( $\sim 0.106$ , horizontal dashed blue line, see Brout et al. 2019). We also include a vertical dashed blue line at  $z = 0.8$  to show the redshift value below which sample selection effects are less important.

in SN Ia cosmological analyses (i.e.  $-0.3 < c < 0.3$ ,  $-3 < x_1 < 3$ ,  $\sigma_{x_1} < 1$ , and  $\sigma_{t_0} < 2$ , Betoule et al. 2014). In Fig. 5, we present the redshift distributions of the fitted SNe Ia.

Given the results from the light-curve fitting, we can standardize SN brightnesses and infer distances using the Tripp formula (Tripp 1998; Astier et al. 2006):

$$\mu_{\text{obs}} = m_B + \alpha x_1 - \beta c - \mathcal{M}_B, \quad (1)$$

where  $\alpha$  and  $\beta$  are the colour and stretch corrections coefficients and  $\mathcal{M}_B$  is the SN Ia intrinsic brightness in rest-frame  $B$  band for an SN Ia with  $x_1 = 0$  and  $c = 0$ .

In Fig. 6, we consider SNe with at least five *Euclid* observations with SNR  $> 3$ , and we compare uncertainties on  $\mu$  separately for the two EDFs (Fornax and South) for LSST + *Euclid* combined data and for LSST alone. In Fig. 7, we present the improvement in uncertainties on SN fitted parameters  $m_B$ ,  $x_1$ , and  $c$  when considering LSST + *Euclid* and when considering LSST alone.

We find that uncertainties on SN fitted parameters and SN distances are reduced compared to when including *Euclid* data compared to when using LSST data alone. The impact of the additional measurements from *Euclid* is strongest at higher redshift SNe ( $z > 0.8$ ), where the rest-frame optical SN flux starts to redshift into observer-frame  $Y$  and  $J$  bands, and SN flux in observer-frame  $g$ -band drops significantly, thus making fits of LSST-only light curves more uncertain (see Fig. 1). For  $z > 0.8$ , we expect the additional *Euclid* mock data to reduce uncertainties on SN distances by 40–50 per cent.

#### 4 CONSTRAINING THE SNE IA ‘MASS STEP’ USING LSST AND *Euclid* MOCK DATA

Various SN Ia analyses have shown that the intrinsic brightness of SNe Ia correlates with host galaxy properties, and in particular SNe Ia found in more massive galaxies are more luminous than SNe Ia found in lower mass galaxies. The astrophysical origin of this correlation is still uncertain, therefore many SN Ia cosmological analyses have empirically modelled this dependency as a step function at host galaxy stellar mass  $10^{10} M_{\odot}$ . Analysing a compilation of a thousand of spectroscopically confirmed SNe Ia with high quality optical data, Brout & Scolnic (2021) showed how dust, and in particular different properties of dust for SNe in high- and low-mass galaxies, can explain the observed mass step and other correlations between SNe Ia intrinsic scatter and SN colour. Given SN distances and their uncertainties, we measure the mass step as:

$$\gamma = \langle \mu_{\text{res}} \rangle_{M_* > 10^{10} M_{\odot}} - \langle \mu_{\text{res}} \rangle_{M_* < 10^{10} M_{\odot}}, \quad (2)$$

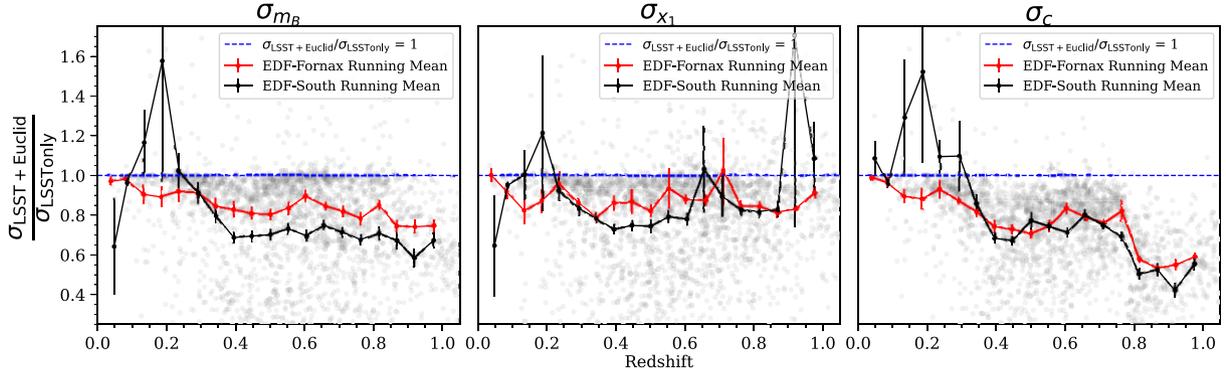
where  $\langle \mu_{\text{res}} \rangle$  is the *weighted* average of Hubble residuals, with weights defined as  $1/\sigma_{\mu_{\text{obs}}}^2$  (see equation 3).

Rest-frame NIR SN data can provide compelling evidence for whether dust is the cause of the mass step. In fact, if dust is the main cause of the luminosity step observed in the optical, we expect the luminosity step in the NIR to be significantly reduced. Uddin et al. (2020) and Ponder et al. (2021b) measured the mass step from SNe Ia with rest-frame NIR data. Both analyses measure mass steps larger than 0.07 in the rest-frame NIR, with  $> 2\sigma$  significance. These results were obtained analysing limited ( $< 150$  likely SNe Ia) low- $z$  SN samples with ground-based NIR data from the Carnegie SN project and other literature compilations (Contreras et al. 2010; Stritzinger et al. 2011; Weyant et al. 2014).

As discussed in Section 3, we expect the *Euclid* mission to obtain hundreds of high-quality SN light curves with good rest-frame NIR coverage and a well-understood selection function. In this section, we show how *Euclid* mock data, combined with optical data from LSST, can be used to give a definitive answer on the origins of the mass step.

##### 4.1 Simulating the SN Ia mass step

For this part of our analysis, we generate three sets of LSST + *Euclid* simulations. We follow the same simulation framework presented in Section 2.1, but we vary the modelling of SNe Ia intrinsic properties and the modelling of the mass step. The first simulation is generated as described in Section 2.1, i.e. assuming the SN Ia intrinsic scatter model by Guy et al. (2010), using distributions of SN colour and stretches from Scolnic & Kessler (2016b) and Popovic et al. (2021), assuming  $\alpha = 0.14$  and  $\beta = 3.0$  and fixing the intrinsic mass step to zero. In the second simulation, we generate SNe Ia following the same approach, but we additionally introduce a wavelength-independent (‘grey’) mass step of 0.08 mag at  $10^{10} M_{\odot}$ .



**Figure 7.** Fractional comparison of uncertainties on  $m_B$  (left),  $x_1$  (center), and  $c$  (right) when including or excluding *Euclid* mock data. We present the fractional plots with the error in *Euclid* combined with LSST as a fraction of the error in LSST with a running mean (blue points and line) of the binned data. We show the running means for EDF-Fornax (red points and line) and EDF-South (black points and solid line) separately. We have identified where the errors are equivalent and the fractional values, subsequently, equal to 1 (black dashed line).

In the third simulation, we include luminosity–stretch correlations ( $\alpha = 0.14$ ) and correlations between SN stretch and SN host mass, but we follow the modelling presented by Brout & Scolnic (2021) to generate SN intrinsic colours ( $c_{\text{int}} = -0.084$ ,  $\sigma_c = -0.042$ ), intrinsic luminosity–colour correlations ( $\beta_{\text{int}} = 2.0$ ), extrinsic dust reddening ( $\tau_E = 0.14$ , see equation 12 from Brout & Scolnic 2021) and dust total-to-selective absorption ( $R_V = 1.5$  in high-mass galaxies,  $R_V = 2.75$  in low-mass galaxies, with  $\sigma_{R_V} = 1.3$ ). For each sample of simulated SNe Ia, we perform light-curve fitting and standardization in the rest-frame optical only and rest-frame NIR only (see Section 4.2) and measure the recovered mass step (see Section 4.3).

#### 4.2 The optical rest-frame and NIR rest-frame Hubble diagrams

We fit simulated LSST and *Euclid* light curves using rest-frame optical data only (3000–7000 Å) and rest-frame NIR data only (1–2 μm). These fits are different from the one presented in Section 3.2, Figs 6 and 7, where we used the full wavelength range (3000 Å to 2 μm), and they aim to disentangle the information encoded in the optical-only and NIR-only light curves. As shown in Fig. 1, with the *Euclid* mock data we can obtain good coverage in the rest-frame NIR up to  $z = 0.8$ . We perform light-curve fitting using the SALT3 model by Kenworthy et al. (2021) and Pierel et al. (2022) (see also Section 2.1). When using optical rest-frame data only, we fit for the four light-curve fitting parameters  $m_B$  (or  $x_0$ ),  $x_1$ ,  $c$ , and  $t_0$  (similarly to the approach presented in Section 3.2). When using NIR rest-frame data only, we fit for the amplitude term  $x_0$  only. The times of peak  $t_0$  and the stretch values  $x_1$  are fixed to the values fitted from the rest-frame optical data, while SN colour is fixed to zero. In general, NIR light curves are significantly less sensitive to colour and stretch and their intrinsic brightness is remarkably homogeneous even before colour and stretch corrections are applied. For this reason, SN Ia in the NIR are often described as ‘true standard candles’, while SN Ia in the optical are ‘standardizable candles’ (i.e. their brightness at peak is fully standardized only after stretch and colour corrections, see Pierel et al. 2022; Peterson et al. 2023). The higher cadence optical data provides significantly better constraints on time of peak compared to the lower-cadence NIR data, and NIR light curves are significantly less sensitive to stretch.

After performing light-curve fitting, we select SNe that pass the SALT-based cuts discussed in Section 3.2. Every SN experiment is affected by selection effects that are generally introduced by

**Table 1.** Number of fitted SNe and recovered mass steps for each simulation tested.

Simulation	$N_{\text{SNe}}$ Optical fit	$N_{\text{SNe}}$ NIR fit	$\gamma_{\text{Opt}}$	$\gamma_{\text{NIR}}$
‘Zero’ mass step	8449	3932	−0.001(3)	0.006(13)
‘Grey’ mass step	8485	3965	−0.081(3)	−0.075(11)
Dust-based mass step	8036	3878	−0.078(3)	−0.027(11)

the choice of the survey strategy and cadence, and by the flux-limited nature of these experiments. These selection effects are generally larger at higher redshifts, where fainter SNe become progressively harder to detect. Multiple sophisticated techniques have been implemented to correct for these biases (Rubin et al. 2015; Kessler & Scolnic 2017). For simplicity, in this analysis we apply a redshift cut at  $z < 0.8$  and neglect corrections for selection effects.<sup>9</sup> In Table 1, we present the numbers of SNe Ia for each generated simulation, both for optical rest-frame and NIR rest-frame fits.

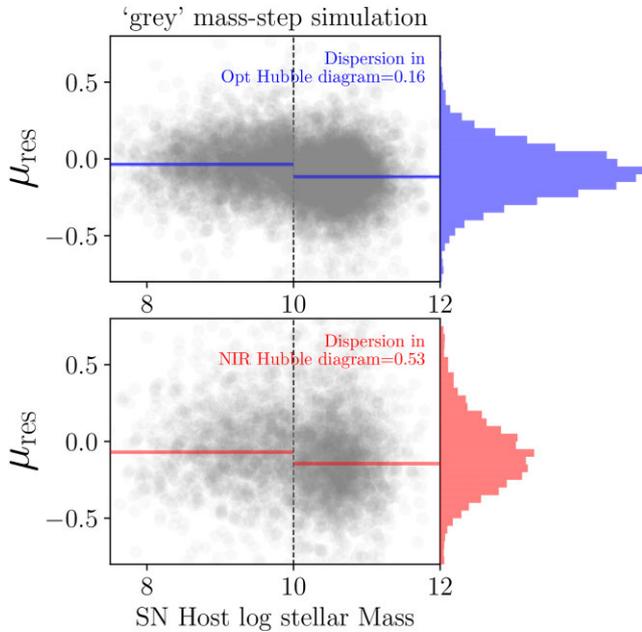
Given the SN light-curve fitting, SNe Ia standardized distances are measured applying equation (1). Modern cosmological analyses include the estimation of  $\mu_{\text{obs}}$  corrections for selection effects (so-called bias corrections) and determine the nuisance parameters  $\alpha$ ,  $\beta$ , and  $\mathcal{M}_B$  while performing cosmological fitting. For simplicity, in our analysis we assume bias corrections to be negligible and we fix the nuisance parameters to the simulated values ( $\alpha = 0.14$ ,  $\beta = 3.0$ , and  $\mathcal{M}_B = -19.365$ ).

We define uncertainties on  $\mu_{\text{obs}}$  as

$$\sigma_{\mu_{\text{obs}}}^2 = \sigma_{m_B}^2 + (\alpha\sigma_{x_1})^2 + (\beta\sigma_c)^2 + \alpha C_{x_1, m_B} - \beta C_{c, m_B} - \alpha\beta C_{x_1, c} + \sigma_{\text{int}}^2, \quad (3)$$

where  $\sigma_{\text{int}}$  is the SN Ia intrinsic scatter which is fixed to the simulated value of 0.11 (see table 5, Kenworthy et al. 2021), while we assume a conservative value of 0.17 for NIR distances (following the results in table 4, Pierel et al. 2022).  $C_{x_1, m_B}$ ,  $C_{c, m_B}$ , and  $C_{x_1, c}$  are the fitted covariance matrices among the SALT3 parameters. This definition provides a realistic estimate of the expected SN distance uncertainties.

<sup>9</sup>When testing the approach of applying redshift-dependent bias corrections, we find no significant difference in our results.



**Figure 8.** SN Hubble residuals as a function of SN host stellar mass, measured using rest-frame optical data only (3000–7000 Å, upper plot) and rest-frame NIR data only (1–2 μm, lower plot). Dispersion on the Hubble diagram built using NIR rest-frame data only is three times larger compared to the Hubble diagram built using optical data. Uncertainties on the recovered mass steps are 0.003 and 0.011 from the optical and NIR Hubble residuals, respectively.

The SN Ia standardized distances and distance uncertainties are then used to build the redshift-distance diagram, usually referred to as a ‘Hubble diagram’, and constrain cosmological parameters. The residuals between  $\mu_{\text{obs}}$  and distances predicted by the best-fit cosmology are usually defined as ‘Hubble residuals’. In our analysis, we do not perform the full cosmological fit of our simulated data and we simply define Hubble residuals as:

$$\mu_{\text{res}} = \mu_{\text{obs}} - \mu_{\Lambda\text{CDM}} \quad (4)$$

where  $\mu_{\Lambda\text{CDM}}$  are SN distances predicted by the input cosmological model (rather than the best-fit one) used in our simulations.

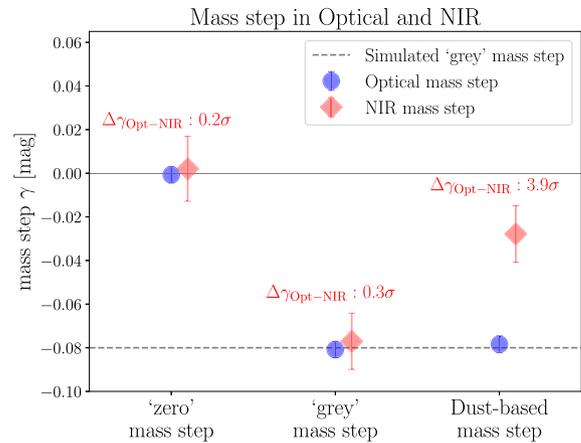
In Fig. 8, we present simulated Hubble residuals as a function of SN host stellar mass. The typical dispersion of simulated Hubble residuals when using optical rest-frame data only is  $\sim 0.16$ , while for NIR rest-frame data only the dispersion is larger ( $> 0.5$  mag). This affects our ability to constrain the mass step.

### 4.3 Measuring the mass step

In Fig. 8, we compare the mass step estimates for one of our simulations (‘grey’ mass step simulation) with the Hubble diagram dispersion. Despite the large dispersion in the NIR Hubble diagram, the large number of SNe Ia allows us to recover a mass step with a  $\sim 0.01$  mag uncertainty.

When considering the rest-frame optical SN fits, all the terms in equations (1) and (3) are non-zero. For the rest-frame NIR SN fits, colour corrections are equal to zero by definition (as SN  $c$  is fixed to zero in the fits), as well as the stretch and colour uncertainties  $\sigma_{x_1}$  and  $\sigma_c$  (as both  $x_1$  and  $c$  are not floated in the fit).

The recovered mass steps are presented in Fig. 9 and in Table 1. When considering optical rest-frame data, we find no significant mass step for the ‘zero’ mass step simulation. For our ‘grey’ mass step simulation and dust-based simulation, we recover a mass step



**Figure 9.** Mass step measured using rest-frame optical-only (3000–7000 Å, blue circles) and rest-frame NIR-only (1–2 μm, red diamonds) data. We measure the recovered mass steps for three simulations: a simulation generated assuming the intrinsic scatter model presented by Guy et al. (2010) with a zero mass step, a simulation generated assuming the intrinsic scatter model presented by Guy et al. (2010) with a mass step of 0.05 mag, and a simulation generated assuming the dust-based scatter model presented by Brout & Scolnic (2021).

of  $-0.081 \pm 0.003$  and  $-0.078 \pm 0.003$ , in good agreement with the simulated value ( $\gamma = 0.08$ ). When considering NIR rest-frame fits, we again find no significant mass step for the ‘zero’ mass step simulation. For our ‘grey’ mass step simulation we have a mass step of  $-0.075 \pm 0.011$ , in excellent agreement with the simulated value and with the mass step recovered in the optical. Finally, when considering our dust-based simulation, we find that the recovered mass step is  $-0.027 \pm 0.011$ . This  $4\sigma$  difference between the mass step recovered using optical-only and NIR-only rest-frame data constitutes one of the main results of this paper and it demonstrates that using Rubin and *Euclid* mock data we will be able to confirm (or rule out) with high confidence whether the (optical and NIR) mass steps are well described by a dust-based model or requires an alternative astrophysical explanation.

## 5 DISCUSSION AND CONCLUSIONS

We exploit public information from previous transient analyses within LSST and *Euclid* and produce simulations of SN Ia light curves as measured by the joint LSST and *Euclid* surveys. While the cadence is non-ideal for supernova studies, the *Euclid* deep fields offer short windows where high-cadence, high SNR, measurements can be obtained. We study two utilities of the *Euclid* data. The first is combining *Euclid* NIR data with LSST optical data. As shown in Fig. 7, this significantly improves the constraining power on distances at high redshifts, by as much as a factor of 2x at  $z \gtrsim 1$ . The second utility is in a stand-alone *Euclid* measurement of the canonical ‘mass step’. This NIR measurement has significant implications for one of the largest systematics for optical supernova studies. We find that we can measure a predicted mass step by up to  $4\sigma$  and can distinguish between different models (dust and non-dust driven) at  $4\sigma$ . This will be a first-of-its-kind measurement with high statistics at high redshift.

This analysis is complementary to those of Inserra et al. (2018), Moriya et al. (2022), and Tanikawa et al. (2022); it uses only public information on the LSST and *Euclid* observing strategies and it is designed so that the community could quickly use this to forecast other transient studies, like what was done for the LSST Photometric

LSST Astronomical Time Series Classification Challenge (Kessler et al. 2019a). As both LSST and *Euclid* are in the process of finalizing their observing strategies, our results are still preliminary. In Appendix A, we discuss our data release and our simulation inputs.

The assumption of this analysis is that SNe can be detected and measured with *Euclid*. While this absolutely can be done, the data must be processed in specific ways that are not applicable to static science surveys (see Sánchez et al. 2022, for a description of what is planned for LSST). We hope that this study will provide useful additional information to the *Euclid* and LSST consortia as they finalize their observing strategies and data-processing pipelines.

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*Software:* NUMPY (Oliphant 2006), MATPLOTLIB (Hunter 2007), PANDAS (Wes McKinney 2010), SCIPY (Virtanen et al. 2020), SNANA (Kessler et al. 2009b), PIPPIN (Hinton & Brout 2020).5

## DATA AVAILABILITY

We release our simulated catalogues, as well as all the SNANA input files needed to reproduce our results in: [https://github.com/maria-vincenzi/Euclid\\_LSST\\_SNIaSims](https://github.com/maria-vincenzi/Euclid_LSST_SNIaSims).

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## APPENDIX A: SNANA INPUTS

All the SNANA input files necessary to create the simulations presented in this paper are available on GitHub ([https://github.com/maria-vincenzi/Euclid\\_LSST\\_SNIaSims](https://github.com/maria-vincenzi/Euclid_LSST_SNIaSims)). Table A1 presents a summary of the files needed to reproduce the simulations and their usage.

**Table A1.** Inputs of the SNANA simulations.

File name	Usage	SNANA key
—EUCLID_LSST_DDF.INPUT	<b>Master file</b> used to generate all simulations	Input file
—SIMLIB_baseline.v2.0_10yrs_DDF.simlib.COADD	LSST cadence	SIMLIB.FILE
—SIMLIB_baseline.v2.0_10yrs_DDF.wEUCLID.simlib.COADD	LSST and <i>Euclid</i> cadences combined	SIMLIB.FILE
—kcor_LSST_EUCLIDvis.fits	LSST and <i>Euclid</i> filters and filter calibration	KCOR.FILE
—DES_SVA2+LOGMASS_LOGSFR.Sullivan10.HOSTLIB	Host galaxy library for SN host simulation	HOSTLIB.FILE
—sn.ia.salt2.g10.input	Simulate SN Ia intrinsic properties using intrinsic scatter model by Guy et al. (2010)	INPUT.FILE.INCLUDE
—sn.ia.salt2.bs20.input	Simulate SN Ia intrinsic properties using intrinsic scatter model by Brout & Scolnic (2021)	INPUT.FILE.INCLUDE
—DES_WGTMAP_MassSFR.Wiseman2021.HOSTLIB	SN Ia rates as a function of host properties (no mass step)	HOSTLIB_WGTMAP_FILE
—DES_WGTMAP_MassSFR.Wiseman2021_STEP.HOSTLIB	SN Ia rates as a function of host properties and 0.08 mag mass step	HOSTLIB_WGTMAP_FILE
—SIMGEN_TEMPLATE_LSST_EUCLID.INPUT	General set-up	SIMGEN.INFILE.Ia

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