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Single-walled carbon nanotube reptation dynamics in submicron sized pores from randomly packed mono-sized colloids

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Abstract

Studying Brownian motion of fibers and semi-flexible filaments in porous media is key to understanding transport and mechanical properties in a variety of systems. Motion of semi-flexible filaments in gel-like porous media including polymer networks and cell cytoskeleton have been studied theoretically and experimentally, whereas the motion of these materials in packed-colloid porous media, advanced foams, and rock-like systems have not been thoroughly studied. Here we use video microscopy to directly visualize the reptation and transport of intrinsically fluorescent, semiflexible, semiconducting single-walled carbon nanotubes (SWCNT) in the sub-micron pores of packed colloids as fixed obstacles of packed-colloid porous media. By visualizing filament motion and Brownian diffusion at different locations in the pore structures, we study how the properties of the environment, like pore shape and pore structure of the porous media, affect SWCNT mobility. These results show that the porous media structure controls SWCNT reorientation during Brownian diffusion. In packed-colloid pores, SWCNTs diffuse along straight pores and bend across pores; conversely, in gel pores, SWCNTs consistently diffuse in curved pores, displaying faster parallel motion. In both gel and packed-colloid porous media, SWCNT finite stiffness enhances SWCNT rotational diffusion and prevents jamming, allowing for inter-pore diffusion.

Introduction

For confined fibers and semiflexible filaments, Brownian motion perpendicular to the filament motion is significantly suppressed in porous media where anisotropic filament motion in curvilinear confining tubes results in snake-like reptation in pores. Reptation theory was originally developed to describe polymer diffusion and resulting stress relaxation in polymer melts^{1–4} but has been successful at describing the dynamics of stiff or semiflexible polymer solutions^{5–7}, as well as filament motion in more complex confining potentials^{8,9}.

Semiflexible chain Brownian motion in submicron sized porous media is a core research topic to understand the mechanism of microfluidic separations^{10–12} and nanoparticle tracer dispersion¹³. Among various porous media with submicron sized pores, gels and packed colloids are two of the most widely used kinds. Gel-like porous media for biological applications^{8,10–12} has been intensively studied. The experiments by

Fakhri et al.¹⁴ on SWCNTs in agarose gels show that even a small bending compliance of a SWCNT dramatically enhances rotational diffusion, consistent with Odijk's prediction of a characteristic relaxation time $\tau_r \sim L^2 L_p$ that is independent of pore size and depends on the chain length L and persistence length L_p . In addition, recent microrheology experiments indicate accelerated rotation from thermal bending of component polymer chain in gel-like porous media^{15,16}. These and other studies demonstrate the use of single filament imaging to understand how the properties of the surrounding confining media affect filament behavior^{7,14,17,18}.

While several studies in gel-like porous media for biologically relevant media exist^{19–22}, there are only few simulation studies of molecular diffusivity of single semiflexible or rod-like filaments in packed colloids^{13,23}, let alone experiment¹⁸. Direct extension of Brownian motion from the gel pores to packed colloid pores is not straightforward due to pore structure differences. First, the packed-colloid pores have a much higher volume fraction (~ 60 v/v%) of solid than similarly sized gel pores ($0.5 - 2.0$ v/v%). This much higher solid content could contribute to less tortuous pore structures²⁴. Second, pores produced by packed colloids are essentially fixed for semiflexible rods to move within, while, based on a previous microscopy study in gel pores, the gel path fluctuates and SWCNTs bend to generate diffusion path¹⁴. Third, randomly packed mono-sized colloids produce a wide pore size and shape distribution²⁵ leading to higher pore heterogeneity than that in gel pores. Applications such as filtration and tracer studies²⁶ utilize packed colloids as porous media, where these studies track molecular concentration in the effluent stream to infer mobility. Single particle tracking of rigid rod-like bacteria in packed-colloid pore systems observes trapping and hopping motion at different pore locations²⁷. As such, these studies do not directly address the physics of single stiff, yet semiflexible, filament mobility in packed-colloid confining media. Finally, it is not known how semiflexible filament mobility in a gel-like porous media compares to transport in a packed-colloid porous media, which is directly relevant to studies of molecular transport in chromatography, where both gel-like²⁸ and packed-colloid porous systems^{11,12} are used.

Here, we apply near infrared video microscopy to directly study semi-conducting SWCNT diffusive behavior and bending dynamics in porous media at the single-SWCNT level. Convective self-assembly^{29,30} is used to create a pore space of packed colloid, with a tunable average pore size of 57% the colloid diameter in close packed areas²⁵. By controlling the assembly rate, we generate both randomly packed and ordered regions to study the effects of pore structure in the same experimental system. We simultaneously track center of mass (COM), orientation θ , and bending angle ϕ to study SWCNT Brownian motion in the pores between packed colloids and compare this behavior with the mobility of SWCNTs in gel-like porous media^{14,20,21}. In addition, we study the heterogeneity of the packed colloids on Brownian motion and molecular reptation. We find that, at locations with several pores of accessible orientations, SWCNTs rotate between multiple straight pores and display normal rotational diffusion. Conversely, at locations with few accessible pores, SWCNTs' rotation is confined and thus SWCNTs show subdiffusive behavior.

Experimental

Sample Preparation

We use a solution of (6,5) chirality enriched single walled SG65i SWCNT (Southwest Nanotechnologies) in 1% weight sodium deoxycholate (DOC, G-biosciences deoxycholic acid sodium salt, >99% purity) solution. The solution is prepared by speedmixing 1 mg SWCNT per 1 mL 4 % weight DOC solution for 48 h, followed by centrifuging at 13.4 krpm for 2 h (Eppendorf minispin centrifuge). Then the supernatant DOC concentration is diluted to 1 wt% for further processing. The protocol from Gui³¹ is used to selectively obtain long SWCNTs ($>5 \mu\text{m}$). Briefly, we add 4 wt% polystyrene sulfonate (PSS, average molecular weight $\sim 70,000$ g/mol, Aldrich) in water to the supernatant after centrifugation to reach a total concentration of 1 wt% PSS in solution. This procedure selectively precipitates long SWCNTs from the solution. The 1 wt% PSS mixture is then centrifuged at 13.4 krpm for 1 minute. The centrifuged pellet is dispersed in 1 wt% DOC solution to obtain long SWCNTs. Measurements of unconfined chains are performed in a slit pore. A $0.5 \mu\text{L}$ drop of SWCNT DOC suspension is placed on a large coverslip (Gold Seal, thickness #1, 40x24 mm) and a small coverslip (Gold Seal, thickness #1, 18x18 mm) is gently placed on top to avoid trapped bubbles in the imaging cell. This forms a quasi-2D imaging chamber $\sim 2 \mu\text{m}$ thick. The edges of the small coverslip are sealed with epoxy (Hardman Double Bubble Red Extra Fast Epoxy) to prevent convective flow caused by evaporation^{29,30}. The following procedure is used for preparing

imaging cells with packed colloids. First, a concentrated solution of silica particles (1.97 μm diameter, Bangs Labs, 10 v/v%) is prepared by centrifugation and disposal of the excess water leaving behind a centrifugal pellet of concentrated silica particles cell is allowed to rest for a few minutes to allow colloid packing. Next, the silica particle-SWCNTs solution is prepared by mixing 1 μL DOC SWCNTs with 5 μL centrifugal pellet. Finally, the imaging cell is prepared by sandwiching a 5 μL drop of a prepared silica particle-SWCNTs solution between two microscope coverslips to form quasi-2D cell as described above. Prior to sealing the cell with epoxy, however, the sandwiched cell is allowed to rest for a few minutes to allow colloid packing.

NIR microscopy setting

NIR microscopy is performed on a Nikon Ti-E inverted microscope in combination with a liquid nitrogen cooled 2D-OMA InGaAs NIR camera from Roper Scientific³². The camera in transmitted light mode is capable of capturing the morphology of silica colloids (**Figure 2(a)**). SWCNT fluorescence is excited by a 660 nm external diode laser (Newport LQC660-110C, 110mW). To selectively visualize only (6,5) chirality SWCNTs, a 980 nm wavelength, 10nm bandpass filter (Edmund optics #65186) is used. Videos of the SWCNT motion are collected with a Nikon PlanApo 100x/1.40 N.A./0.13 W.D. oil immersion objective and 1.5x magnification at 15.7 fps and a 50 ms exposure time.

Image Analysis

An automated image analysis MATLAB code is developed to extract backbone points, orientation (θ), and center of mass (COM) frame-by-frame from the NIR microscopy video. Orientation and COM are determined from ellipse fitting¹⁴ and illuminating pixel points location (built-in MATLAB function). Rotation and translational diffusion coefficients cannot be evaluated easily because multiple diffusion categories, such as subdiffusion, and normal diffusion, are involved in this system. The wide spread time interval power-law index makes diffusion coefficient unit inconsistent. Here, we use a MSD (δ^2) at t time with interval of 1 second to evaluate diffusion rate at different time with equation:

$$\delta_x^2(t) = (\chi(t + 0.5s) - \chi(t - 0.5s))^2 \quad (1)$$

For comparison convenience between different time spot, the spontaneous MSD is normalized by time average of MSD, which is defined commonly as time-averaged MSD (TA-MSD, $\delta^2 / \langle \delta^2 \rangle$) in literatures.

The bending angle ϕ is extracted from the end-point tangent vectors of a fit rotated parabola to the SWCNT backbone. To obtain optimal parabola rotation with smallest error, the MATLAB minimal search function `fminsearch` is used to find the parabola rotation angle with minimal normalized residual error after rotation. We define the bending angle ϕ as the difference between the tangential angles at the ends of the rotated fit parabola. The backbone points extraction procedure uses the protocol by Gittes³³.

Results and discussion

SWCNT Brownian motion in packed-colloid pores

Randomly packed colloid pores have a complicated pore structure and size distribution. **Figure 1 (a)** and **(b)** illustrate the pore structure of two types of media: packed colloids and a gel, respectively. The pore space in packed-colloid (grey area) has a complex structure with wide compartments (i.e., pore body, green sphere in **Figure 1 (a)**) and narrow connectors (i.e., pore throat, blue sphere in **Figure 1 (a)**) between compartments. Based on the particle packing protocol, the monosized colloids used to form the porous media are tens of layers thick with an approximate average pore size ξ_a of 0.57 times the colloid diameter³⁴ and average pore throat size ξ_t is 0.19 times the colloid diameter³⁵. **Figure 1 (b)** shows a gel-like porous structure. Compared to colloids packing pores, gel-like pores have lower solids volume fraction, higher porosity, higher transparency and higher homogeneity.

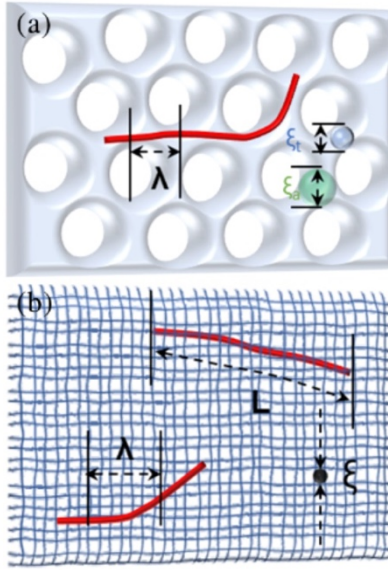


Figure 1. Structure comparison between (a) randomly ordered packed-colloid pores of this work and (b) agarose gel pores systems. (a) Packed particles have high solid (grey sphere) volume percentage (~ 60 v/v%), low porosity (~ 34 v/v%), and are translucent to opaque depending on media thickness. Representative pore is drawn with the light grey volume where ξ_a and ξ_t represent the average pore size and average pore throat size. (b) Porous media produced by agarose gels have low solids (blue curved lines) volume ($0.5 \sim 2.0$ v/v%), high porosity (> 98 v/v%), and are transparent. In the gel-like porous media system only one pore size exists where ξ corresponding to ξ_a in packed-colloid pores. Long semiflexible filaments (red curved lines) are drawn in each with contour length L display confined diffusion with deflection length λ .

In this experiment, we use SWCNTs with length ranges from 3 to 12 μm in randomly packed multiple layers of mono-sized colloids (**Figure 2** (a)). **Figure 2** (b) shows the morphology of this randomly packed pores from 2 μm diameter colloids. The porous media generated with 2 μm diameter packed colloids has a 1.14 μm average pore size with a 0.38 μm pore throat size. Inset fluorescent frames shows reptation of a ~ 7.0 μm SWCNT diffusing between several straight pores with different orientation. Tracked SWCNT COMs show the tortuous porous structure in packed-colloid pores. SWCNT fluorescent images shows conformations during diffusion. In single straight pore confinement, SWCNT (second and forth marked point from left in **Figure 2** (b)) completely align with the pore orientation. While diffusing across two pores (first and third marked point from left), SWCNT moderate flexibility enables quick chain bending across pores. This flexibility enabled bending across pores is also observed in gel-like porous structure¹⁴.

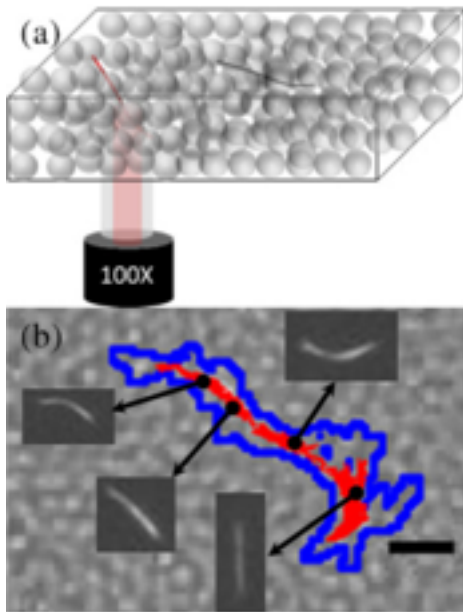


Figure 2. Experiment settings of semiflexible filament molecule, SWCNT, diffusion (red curved line) in randomly packed silica colloids (grey beads) pores. (a) Illustration of single molecule microscopy. Surfactant-wrapped SWCNTs dispersed in silica colloid filled glass imaging cell. (b) SWCNT travel area (blue line) and COM (red) overlap with the bright-field image of the 2 μm in diameter randomly pack colloids. Inset images show the configuration of SWCNT at marked locations. Scale bar 5 μm .

With COM and orientation tracking from fluorescence microscopy in **Figure 2**, we can further study SWCNT rotational and translational Brownian motion at different lag time with mean square displacement (MSD) and mean square angular displacement (MSAD) in packed-particle pores³⁶.

Over short time scales, a given SWCNT diffuses freely without being affected by its porous surroundings. After the SWCNT entangles with a single pore, it diffuses back and forth along the pore. All non-aligned motions with pore orientation are frozen, including perpendicular motion and rotation. The average time of a SWCNT being confined is defined as entanglement time τ_e . In this experiment, the frame time (50 ms) is shorter than the estimated entanglement time (around 1 s). When the SWCNT probes more than one straight pore, the SWCNT bends to diffuse into the new pore. The disentanglement time τ_d is the average time it takes for the SWCNT to diffuse out of one pore. This reptation motion is reflected in the SWCNT Brownian motion as shown in **Figure 3**. At time longer than rotation time $\tau_r = 1/(2D_r)$, the SWCNT loses its memory of initial orientation, and the diffusion become isotropic, which is well-described by Perrin-Smoluchowski theory³⁷.

Figure 3 (a) shows SWCNT rotational dynamics in particle random packing pores. At short times, between entanglement time τ_e and disentanglement time τ_d , the MSAD displays a subdiffusive regime with the power law index being smaller than one. However, above the disentanglement time τ_d , SWCNT rotation follows normal diffusion with a temporal exponent of one. Translational Brownian motion is studied after decomposing SWCNT motion as parallel s and perpendicular n to the SWCNT molecular axis in **Figure 3 (b)**. At short times during in-pore diffusion ($\tau_e < \tau < \tau_d$), perpendicular diffusion is frozen as shown by the plateau in the MSD. The parallel motion at short times still displays subdiffusive behavior with a 3/4 power law index from SWCNT chain thermal bending^{36,38–40}, which is the same behavior observed when SWCNTs diffuse in gel pores¹⁴. At longer time ($\tau > \tau_d$), cross-pore diffusion occurs and both parallel and perpendicular translational Brownian motion are once again the same as the case of SWCNT diffusing in gel pores. The disentanglement time τ_d is marked on both MSD and MSAD curves (**Figure 3**) to show the coupled SWCNT rotational and translation diffusion in packed colloid pores. At the cross-pore time interval ($\tau > \tau_d$), the perpendicular MSD shows a super diffusive regime (exponent > 1) due to coupling between rotational and translational motion when the SWCNT diffuses out of a single pore.

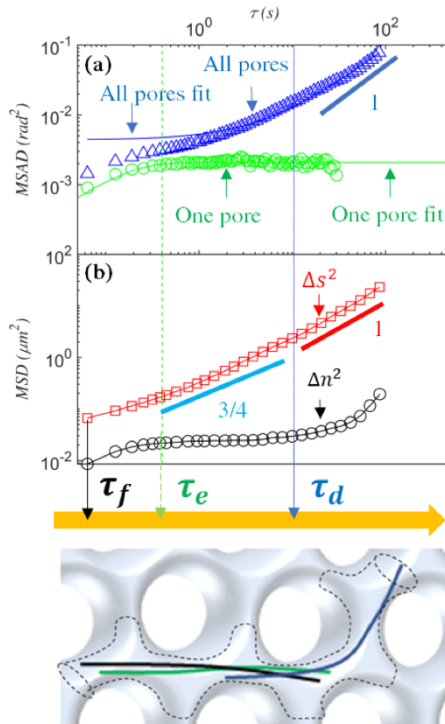


Figure 3. SWCNT Brownian dynamics in randomly packed mono-sized colloids pores. (a) Rotation dynamic in multi-pores (All, blue) and single straight pore (SP, green). Curve fitting on straight pore and multi-pores of MSAD data to extract entanglement time (τ_e) from single pore (SP) and disentanglement time (τ_d) from all data. (b) Parallel (Δs^2) and perpendicular (Δn^2) translation Brownian dynamics showing three time-scales: τ_f is frame time, τ_e is entanglement time from (a), and τ_d is disentanglement time. τ_d plotted here is obtained by equation $\tau_d = \langle \Delta \theta_0^2 \rangle / (2D_r)$ with parameters from fitting MSAD all sample data (blue). Bottom figure shows SWCNT status with increasing lag time. Black molecule is the initial state. Green molecule first gets entanglement of pore. Dark blue molecule has diffused into a new pore. This same (6,5) chirality SWCNT 9.8 μm long and a 27 μm persistent length is shown in Figures 3, 5, 6, 7. The bottom scratch shows the SWCNT behavior at correspondent time interval of the same colour of mark arrow.

In all cases of SWCNT rotation in packed-colloid pores, the exponent of the MSAD changes at around 1.0 second, which is the entanglement time τ_e required for the filament motion to feel the hindrance caused by the pore surface⁴¹. Before entanglement, the SWCNT explores the pore structure which has a wide pore size distribution that corresponds to a wide distribution of entanglement times. Thus, MSAD curves before the entanglement time show a complex pattern from averaged entanglements. To study the rotation dynamics of entanglement ($\tau_f < \tau < \tau_e$), we directly sample a subset of the data during straight pore confinement an observation. From the MSAD obtained from single pore confinement (green data, **Figure 3 (a)**), the entanglement time τ_e and rotation confinement $\langle \Delta\theta_0^2 \rangle$ can be estimated by assuming a single-exponential model for the MSAD, with $\langle \Delta\theta^2(\tau) \rangle = \langle \Delta\theta_0^2 \rangle (1 - e^{-\tau/\tau_e})$. Note that the entanglement time τ_e effect is not observed in the MSAD curves of the reported SWCNTs diffusing in gel pores²². The expected entanglement time ($\tau_e \propto \xi^2/D_{||} \approx 0.04s$) in the agarose gel system used to produce gel-like porous media from the prior study¹⁴ cannot be captured due to the temporal resolution of the video microscopy experiments. To show the consistency of SWCNT Brownian dynamics scaling law in packed-colloid pores, we have plotted averaged MSD and MSAD of (6,5) chirality SWCNT with same length at different locations of randomly packed 2.0 μm diameter colloid pore in Figure S1 of supplementary material. We find the MSAD and MSD scaling law are consistent with that displayed in **Figure 3**.

SWCNT flexibility enhanced diffusion in packed-colloid pores

The rotational diffusion coefficient D_r is extracted from the MSAD curves by fitting data with the equation $\langle \Delta\theta^2(\tau) \rangle = 2D_r\tau + \langle \Delta\theta_0^2 \rangle$. For SWCNTs of this length range confined in the randomly ordered packed-colloid pores, the estimated entanglement time τ_e is around 1 second. For simplicity of extracting rotational diffusivities from the MSAD, only MSAD with lag time longer than estimated entanglement time are used in this work. The disentanglement time τ_d can be estimated by the equation $\tau_d = \langle \Delta\theta_0^2 \rangle / (2D_r)$ by fitting the results above. It should be noted that two kinds of observations have been neglected. The first case is subdiffusion rotation with R-squared ($R^2 < 0.99$). The disentanglement time of this kind is too long to observe at these experimental settings. The second case is negative rotational confinement $\langle \Delta\theta_0^2 \rangle$ obtained from fitting the MSAD data. In this case, rotational confinement $\langle \Delta\theta_0^2 \rangle$ is too small to observe by direct curve fitting.

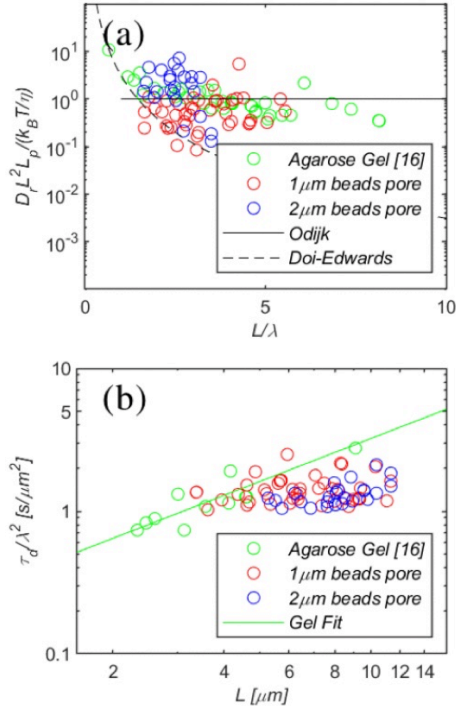


Figure 4. Quantification of SWCNT rotation rate in packed-colloid pores. (a) Normalized rotational diffusion coefficient for SWCNTs in packed-colloid pores and gel pores. (b) Normalized disengagement time (τ_d/λ^2) obtained shows a very weak relationship with SWCNT length (correlation factor are 0.14, 0.60 for packed-particle pores produced by 1 μm diameter and 2 μm diameter colloids respectively) due to pore heterogeneity and rotational confinement from packed-colloid pores. Data from prior work with gel-like porous media is shown in green.

Since porous media from colloidal packing provides SWCNT confinement, it is interesting to examine whether the SWCNT finite stiffness can enhance rotational diffusion, following Odijk's theory⁴¹, or show confined behavior as in the Doi-Edwards' theory for completely rigid rods¹. **Figure 4(a)** shows a master curve of $D_r L^2 / (k_B T / \eta)$ versus L/λ including both published results for SWCNT diffusion in gel pores and our new results in pores formed with packed colloids of different sizes. The blue and red data shown in the master scatter plot shows that SWCNT motion in packed-colloid pores distribute around Odijk's theory line as in the previous case for SWCNTs in gel-like pores (shown in green). The packed-particle pores data, however, shows wider scatter than those of gel pores, likely due to the higher pore heterogeneity. Diffusing semiflexible chains in a gel-like porous media display a linear relationship between disentanglement time τ_d normalized by its deflection length, λ , and filament contour length ($\tau_d / \lambda^2 \sim L$)^{14,41}. In packed-colloid pores, we expect the same linear relationship. **Figure 4(b)** shows normalized disentanglement time τ_d / λ^2 versus SWCNT length L in packed-colloid pores obtained from the ellipse fitting method. Rather than a strong linear correlation as seen in the gel pores ($R^2 = 0.91$)¹⁴, we observe a weak linear relationship with a $R^2 = 0.14$ correlation factor. This is related to additional heterogeneous factors that affect SWCNT mobility in packed-particle pores. Specifically, in addition to deflection length λ and contour length L , the semiflexible chain disengagement time τ_d in colloids packed pores is affected by pore junction size and available angular paths^{41,42} which are highly location-dependent in randomly packed colloids. As such, the resulting diffusion can be thought of as occurring on a rough energy landscape. In addition to the spatial heterogeneity of the medium, however, the energy landscape also depends on the conformation of the SWCNT. These effects are likely the cause of the greater spread of our measured disentanglement time in packed-colloid pores as compared to that observed in gel pores.

Pore heterogeneity effect on SWCNT Brownian motion

In randomly packed-colloid porous media, the pore orientation θ , pore throat size ξ_t , and pore size ξ_a are location dependent (**Figure 5(a)**)³⁵. Hence, the SWCNT Brownian motion inside such porous media shows location-dependent dynamics due to the structural heterogeneity. To study the pore heterogeneity effects, a single SWCNT is studied at five different locations in the packed-colloid pores where the orientation (**Figure 5 (a)**) and COM (**Figure 5 (c)**) are tracked at every frame.

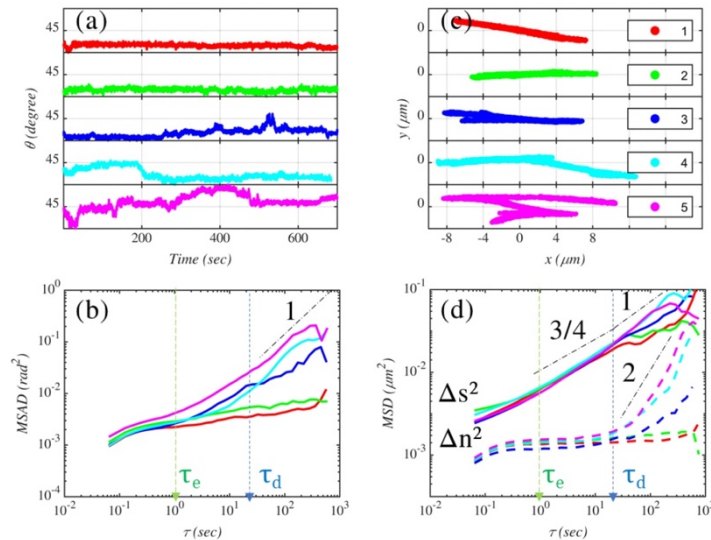


Figure 5. Pore location dependent SWCNT dynamics of the same SWCNT. Colours represent five observations at different locations in packed-colloid pores. (a) Orientation tracking over frames. Each grid has 200 seconds width and 45-degree height. (b) Center of mass tracking from five videos. Each grid has $4 \mu\text{m}$ width and height. (c) Mean square angular displacement (MSAD) results from tracking orientation data. (d) Mean square displacement (MSD) parallel (Δs^2 , solid line) and perpendicular (Δn^2 , dashed line) to the projected SWCNT motion

The MSAD is calculated to quantify the rotational dynamics that reflect the heterogeneity in angular confinement. In observation 5 (magenta data), the SWCNT bends to access multiple straight pores (>3) with distinct pore orientations (**Figure 5 (a) and (b)**). Thus, the MSAD (**Figure 5 (b)**) resembles the rotational dynamics in gels¹⁴. The disengagement time (τ_d) is the average time required for SWCNT to travel across pores. At short times ($\tau < \tau_d$), the MSAD shows a sub-diffusive relationship (slope <1) with time lag, while at long times ($\tau > \tau_d$), the MSAD shows a diffusive relationship (slope=1) with time lag. In observations 1 and 2 (red and green traces), the orientation of the SWCNTs changes minimally during the observation, i.e., the SWCNT only reptates within the original straight pore during the video. This high level of confinement yields a sub-diffusive rotation. The remaining observations, where the SWCNT diffuses in a single pore for the majority of the time but briefly samples other pores by bending, show a mixed MSAD effect between these two limit regimes.

As for the effect of pore heterogeneity on translational Brownian motion, we calculate the MSD parallel and perpendicular to the SWCNT (**Figure 5 (d)**). Due to the coupling between rotational and translational motion, the entanglement time τ_e and disentanglement time τ_d can be clearly observed from the MSD of the motion perpendicular (dashed lines) to the SWCNT backbone. When confined to a single straight pore, as for observations 1 and 2, the MSD perpendicular to the SWCNT backbone Δn^2 shows a location-independent plateau between entanglement time τ_e and disengagement time τ_d . This is different from the gel case where the perpendicular MSD shows a $3/4$ power law dependence on lag time, which indicates thermal fluctuation dominated perpendicular motion. For colloidal packings, the broad distribution of pore diameters and the rigidity of the medium appear to effectively suppress transverse motion within a given pore. On longer time scales the MSD perpendicular to the initial backbone shows a super-diffusive regime, corresponding to inter-pore diffusion. Moreover, the wide spread in transition times between these regimes indicates a wide distribution of disentanglement times for a given SWCNT in different pore environments.

SWCNT reptation motions in packed-colloid porous media

To study the effect of pore heterogeneity, we tracked SWCNT bending and transport at different locations in the packed-colloid pores. SWCNT finite flexibility introduces molecular bending when diffusing across two pores with different orientation. We track this effect via the bending angle ϕ . For simplicity, we fit the SWCNT with a rotated quadratic polynomial. The positive bending angle is defined as counter clock-wise bend when observing the molecule from left to right. SWCNT bending angle is used to infer the local pore curvature without directly measuring the colloid pore structure.

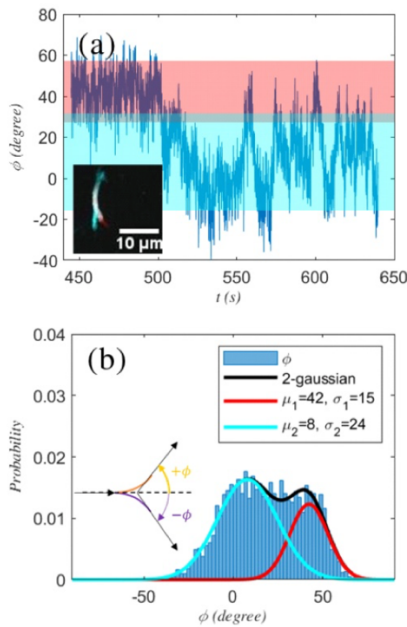


Figure 6. SWCNT Bending angle (ϕ) tracking in packed-colloid pores. (a) Bending angle tracking of SWCNT diffusing from pore transition (red block) to one straight pore (cyan block). Inset: false coloured SWCNT trajectory overlapping. Red marks straight pore location and green marks pore transition. (b) Bending angle distribution

We further study the pore location and shape effect on SWCNT orientation and angular displacement (Erreur ! Source du renvoi introuvable. (a) - (c)) and the parallel and perpendicular translation with corresponding diffusions (Figure 7 (d) – (f)) of the same SWCNT in Figure 7 but for a longer tracking duration. Inset image of Figure 7 (f) shows that SWCNT first diffuses from a 42 degree pore transition (red area) to a straight pore (cyan area). Between these two regions, the SWCNT is moving through the straight pore as it approaches the transition (white area in Figure 7).

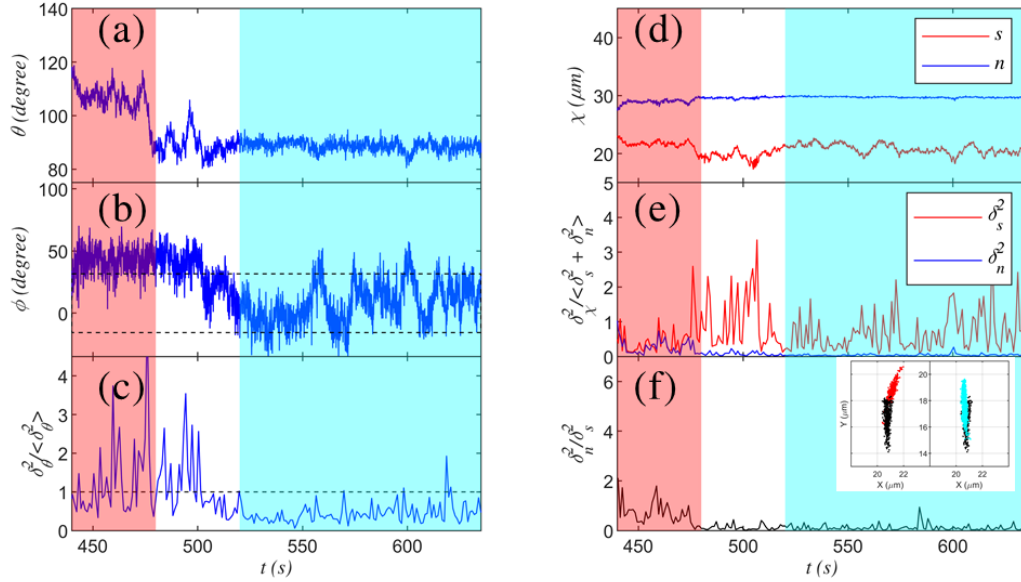


Figure 7. SWCNT reptation motion tracking in packed-colloid porous media. (a)-(c) angular motion tracking. (d)-(f) translational motion tracking. Cyan area is a straight pore example. Red area is a pore-transition. White area reflects straight pore that is close to pore transition. Inset (f) shows the COM of the straight pore to pore transition procedure. Inset left shows the COM from red to white region (black dots); right shows region from white (black dots) to cyan area

In this example, we observe three types of pore structures: pore-transition where the highly bent SWCNT ends locates at two straight pores of different orientations (red area), straight pore ends where the SWCNT moves back and forth between pore transition and the new straight pore (white area), and straight pore center which the SWCNT fully enters the new straight pore (cyan area). The straight pore center (cyan area) shows orientation confinement on both rotation and molecular bending, which shows a noisy plateau at the pore orientation (Figure 7 (a)) and bending angle (dotted line Figure 7 (b)) with close to zero average bending angle (Figure 7 (b)). The power law index of the normalized MSAD in the straight pore confinement falls below 1, which indicates high rotational confinement in a straight packed-colloid pore (Figure 7 (a)). This pore confinement yields anisotropic hindrance on parallel and perpendicular translation. The perpendicular motion (n) in the straight pore is frozen, while parallel motion diffuses back and forth (Figure 7 (d)). Hence, the parallel time averaged MSD (TA-MSD, $\delta_s^2 / \langle \delta_s^2 \rangle$) fluctuates significantly while the perpendicular TA-MSD ($\delta_n^2 / \langle \delta_n^2 \rangle$) is close to zero (Figure 7 (e)).

At the pore transitions (red region), the SWCNT bends between two pores with different orientations. Thus, the SWCNT bending angle shows a non-zero noisy plateau in the bending angle tracking (Figure 7 (b)) with a 42 degrees average bending angle (Figure 7 (b)). Transitioning between two pores at different orientations corresponds to a high TA-MSAD ($\delta_\theta^2 / \langle \delta_\theta^2 \rangle$) at pore transition (red region in Figure 7 (c)). Hence, rotation coupled to perpendicular motion (Figure 7 (d)) shows an accelerated perpendicular TA-MSD compared to the pore center region (Figure 7 (e)). At the same time, SWCNT parallel motion is hindered with lower parallel TA-MSD compared with the straight pore center region (Figure 7 (e)).

The white region in **Figure 7** shows the SWCNT diffusing into a straight pore center from the pore transition. In this case, SWCNT orientation aligns with the destination pore orientation, and the SWCNT bending angle decreases and fluctuates around zero under the straight pore confinement (**Figure 6 (b)**). The SWCNT TA-MSAD from the partially-confined SWCNT is higher than in the full confinement of the straight pore. However, in this observation, SWCNT parallel TA-MSD of partial pore confinement is closer to that in a straight pore than that in a pore transition. Further, the SWCNT COM of each location is displayed in the inset of **Figure 7 (f)**. The pore transition area (red) has large curvature and thus confines the SWCNT to a highly bent conformation. The pore curvature effect leads to a significantly lower parallel TA-MSD (**Figure 7 (e)**) and higher translational anisotropic ratio of perpendicular and parallel TA-MSD (**Figure 7 (f)**) than at the non-pore transition pore site. While in the straight pore (cyan COMs) and partially straight pore (black COMs), SWCNT reptates along the orientation of target straight pore with much smaller pore confinement at perpendicular direction. Straight pores limit the SWCNT COM perpendicular range to the pore size. While in a curved pore moving through pore transition, the SWCNT perpendicular motion range increases significantly. In conclusion, the transport properties of stiff semiflexible filaments are dominated by the distribution of pore throat orientations at pore junctions, which dictates the curvature of the filament during inter-pore transitions.

Conclusions

SWCNTs in tightly confined porous media diffuse along the pore path and enter new pores by reorienting themselves by bending induced by chain thermal fluctuations. Although the motion is still reptational, the discrete and pre-set distribution of pore sizes and orientations controls chain dynamics and loosens the coupling of parallel and perpendicular MSDs; this differs from reptation in gel pores, where SWCNTs can bend around multiple, thin, fluctuating gel strands and diffuse along tortuous paths where parallel and perpendicular MSDs are coupled and display a characteristic $3/4$ power law. SWCNTs in the heterogeneous pores of packed colloids have their own peculiar dynamics. When motion is confined to a single straight pore, the SWCNT perpendicular mobility is significantly limited by the pore walls while the parallel mobility is only slightly reduced. Hence, the parallel MSD shows thermal fluctuations with a $3/4$ power law, while the perpendicular MSD remains the same size of the straight pore diameter before traversing into another straight pore.

Gels have high porosity ($\geq 98 \text{ v/v\%}$)⁴³; their pore structure is tortuous and SWCNTs essentially create their own pores by slaloming around gel network strands. Conversely, randomly packed colloids have low porosity ($\sim 34 \text{ v/v\%}$) and interconnected pores with different orientations and tortuosity; SWCNTs must bend by discrete, prescribed angles to access these pores. Moreover, the pore structure is spatially heterogeneous. Even for long observation times, we observe wide, location-dependent variability of the number of SWCNT disentanglements from one pore to the next. Locations where pore junctions provide numerous widespread pore orientations display normal SWCNT rotational diffusion; locations with more limited pore orientations lead to strong rotational confinement and subdiffusive rotational diffusion.

SWCNT stiffness plays a role via the higher (or lower) energy required to attain a specific bending angle. At pore transitions with different orientations, we observe that SWCNT enter new pores whenever thermal fluctuations produce a sufficient bending angle to navigate the orientational change. The amplitude of such bending angle further helps to categorize heterogeneous pore locations into classes: straight pore center, straight pore end, and transition across pores. The observed rotational and translational TA-MSD are distinctly different in these pore classes.

Via single-molecule photoluminescence imaging, we accurately track SWCNT motion in porous media and show how location-dependent pore structure and SWCNT flexibility combine to control rotational and translational diffusion. This new method and model system offer a powerful tool for studying semiflexible filament motion in complex media beyond gels^{19,44,45}. This novel physical understanding will impact the development of applications of semiflexible molecules in heterogeneous porous media, such as SWCNT separations^{10,12}, and the development of electromagnetically active rod-like nano-robots for reservoir in-situ sensing^{26,46,47}.

Conflicts of interest

There are no conflicts to declare.

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