

# **Density determination of liquid iron-nickel-sulfur at high pressure**

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corresponding to those in the Earth's core.



determined using field emission-electron probe microanalysis before loading. The

sample pellets were cut into ϕ30–50-m pieces and loaded into a sample hole drilled in a







121 background signal function 
$$
I_{bg}(\theta)
$$
. Herein,  $I_{bg}(\theta)$  was obtained from the solid XRD signal

122 before melting. The scattering angle  $2\theta$  can be transformed into scattering momentum

123 (Q) with wavelength 
$$
(\lambda)
$$
 via  $Q = 4\pi sin\theta/\lambda$ . Then,  $I_{sample}(Q)$  can be written as

$$
I_{sample}(Q) = I_{mes}(Q) - bI_{bg}(Q),
$$
\n<sup>(1)</sup>

125 where *b* is a background factor. In this study, we used Krogh-Moe–Norman

126 normalization (Krogh-Moe 1956; Norman 1957; Morard et al. 2013) for processing

127 *I*<sub>sample</sub>(*Q*) to structure factor *S*(*Q*). Reduced pair distribution function  $G(r)$  and pair

128 distribution function *g*(*r*) were calculated from *S*(*Q*) using Fourier transform:

129 
$$
G(r) = 4\pi r [\rho(r) - \rho_0] = \frac{2}{\pi} \int_0^{Q_{Max}} Q \{ S(Q) - 1 \} \sin(Qr) dQ, \qquad (2)
$$

130 
$$
g(r) = G(r)/4\pi r \rho_0 + 1,
$$
 (3)

131 where  $r$ ,  $\rho(r)$ ,  $\rho_0$ , and  $Q_{Max}$  are the radial distance from the atom, atomic density, average

132 atomic density, and maximum scattering momentum in each data point, respectively.

133 Figure 2 shows the typical *S*(*Q*), *G*(*r*), and g(*r*) functions after completing the analytical

134 calculations. Owing to the repulsive force of an atom from a reference point (
$$
r = 0
$$
), no

135 atom should be closer than the first coordination shell  $r_{min}$ . Therefore, in the range  $0 < r$ 

136  $\langle r_{\text{min}} \rangle G(r)$  can be represented as a linear function:

$$
G(r) = -4\pi\rho_0 r.\tag{4}
$$

138 Using the above principle, it is necessary to integrate Eq. (2) from 
$$
Q = 0
$$
 to  $\infty$ , which is

139 not possible using experimental data. Additionally, 
$$
Q = 6-7 \text{ Å}^{-1}
$$
 is the upper limit when

140 using 30-keV X-rays because of the aperture angle of the DAC. Such a limited *Q* range

141 produces ripples (Fig. 2a) in the distribution functions. To minimize these ripples in *G*(*r*),

142 which are attributed to the Q truncation effect, the difference between ideal  $G(r) = -4\pi r$ 

143 and  $G(r) = G_0(r)$  directly obtained from the raw data (without iteration) was calculated

144 in the range 
$$
0 < r < r_{\text{min}}
$$
:

$$
\Delta G_0(r) = -4\pi r - G(r). \tag{5}
$$

146 Then, the function was integrated from 0 to *rmin* as the sum of the squares of the

147 differences:

148 
$$
\chi^2(\rho_0 b) = \int_0^{r_{min}} \Delta G_i(r)^2 dr.
$$
 (6)

- 149 To minimize  $\chi^2$ , background factors *b* and  $\rho_0$  were determined.
- 150 The density of the liquid sample can then be expressed as

151 
$$
\rho = \rho_0 \times M, \tag{7}
$$



166 The obtained density values were fitted using third-order Vinet EoS.

167 
$$
(P - Pr) = K_{TPr} x^{2/3} (1 - x^{-1/3}) \times exp \left[ \frac{3}{2} (K'_{TPr} - 1) (1 - x^{-1/3}) \right],
$$
 (8)

168 where 
$$
Pr
$$
,  $K_{TPr}$ ,  $K_{TPr}$ , and  $x$  are the reference pressure, isothermal bulk modulus, its first

169 pressure derivative at reference pressure and 3400 K, and 
$$
x = \rho/\rho_{\text{Pr, 3400K,}}
$$
 respectively. A

170 structural transition at around 20 GPa has been suggested for liquid  $Fe_{46.5}Ni_{28.5}S_{25}$  from

- 171 sound velocity determination (Kawaguchi et al., 2017). Considering the structural
- 172 transition below 20 GPa, we performed the fitting based on measured density data at the
- 173 lowest pressure point. We derived the pressure dependence of the density of liquid
- 174 Fe<sub>46.5</sub>Ni<sub>28.5</sub>S<sub>25</sub>. The best fit for the compression curve of the density data yielded  $K_{TPr}$  =
- 175 110.5(250) GPa and *K'*<sub>*TPr</sub>*= 7.2(25) with a fixed  $\rho_{Pr,3400K} = 6.434$  g/cm<sup>3</sup> (Table 2). Figure</sub>
- 176 3 shows the confidence ellipsoid of the determined  $K_{TPr}$  and  $K'_{TPr}$ . As reported in Angel
- 177 (2000), the confidence ellipsoid is expressed as

178 
$$
\Delta = (K_{\text{TPr}}, K'_{\text{TPr}}) \begin{pmatrix} \sigma_{K_{\text{TPr}}K_{\text{TPr}}} & \sigma_{K_{\text{TPr}}K'_{\text{TPr}}} \\ \sigma_{K'_{\text{TPr}}K_{\text{TPr}}} & \sigma_{K'_{\text{TPr}}K'_{\text{TPr}}} \end{pmatrix}^{-1} \begin{pmatrix} K_{\text{TPr}} \\ K'_{\text{TPr}} \end{pmatrix},
$$
\n(9)

179 with the covariance of  $K_{TPr}$  and  $K_{TPr}$ <sup>'</sup>, where  $\Delta$  is the chi-square distribution (here,  $\Delta$  =

180 2.3 for 1σ-level confidence with two degrees of freedom).





#### pressures.





#### 241 **Implications**

242 The density deficit in the outer core in terms of pure liquid Fe was estimated to be 243 7.5%–7.6% (Kuwayama et al. 2020). To discuss the density of the Earth's outer core, we 244 used a constant  $\alpha K_T$  relationship:

245 
$$
P(\rho, T) = P(\rho, T_0) + \Delta P_{th}
$$
, (10)

$$
\Delta P_{th} = \alpha K_T (T - T_0),\tag{11}
$$

247 where  $\alpha$ ,  $K_T$ , and  $T_\theta$  are the thermal expansion coefficient, isothermal bulk modulus, and 248 reference temperature (3400 K), respectively. Additionally,  $\alpha \times K_T$  can be considered as 249 constant from reference pressure and temperature to the pressure–temperature (*P–T*) 250 condition of interest ( $\alpha \times K_T = \alpha_{\text{Pr}} \times K_{TPr}$ ). Assuming that the temperature effect on the 251 sound velocities can be negligible, we refitted the sound velocity data of Kawaguchi et 252 al. (2017) using  $\rho_{Pr,3400\text{ K}}$  determined herein, yielding an adiabatic bulk modulus  $K_{SPr}$  = 253 186.8 GPa at 24.6 GPa and 3400 K. The relation between *KSPr* and *KTPr* can be expressed 254 as  $K_{SPr}/K_{TPr} = (1 + \alpha_{Pr} \times \gamma_{Pr} \times T_{Pr})$ , where  $\gamma_{Pr}$  of pure Fe is from Kuwayama et al. (2020). 255 Combination of  $K_{SPr}$ ,  $K_{TPr}$ , and  $\gamma_{Pr}$  yielded  $\alpha_{Pr} \times K_{TPr} = 1.18 \times 10^{-2} \text{ GPa/K}$ .

We calculated the adiabatic temperature as follows:

257 
$$
T = T_{ref} exp \left[ \gamma_{ref} \left( 1 - \frac{\rho_{ref}}{\rho} \right) \right],
$$
 (12)

258 where  $T_{\text{ref}}$  is the reference temperature, and  $\gamma_{\text{ref}}$  is the Grüneisen parameter at 24.6 GPa





suggest a volume of 5.8-7.5wt% S in the Earth's outer core.





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422

#### 423

424



426 **FIGURE 1.** 1D XRD patterns of solid (gray symbols) and liquid (pink symbols)



428 30 keV X-ray and (**b**)  $\sim$ 37 GPa using a 50 keV X-ray. Blue and green lines indicate the

429 whole pattern profile fitting results of  $(Fe, Ni)$ <sub>3</sub>S (space group:  $I\overline{4}$ ) and KCl B2 (space

430 group:  $Pm\overline{3}m$ ) using the Le Bail method and the differences between the observed and





432

434 **FIGURE 2.** Typical Faber–Ziman structure factor *S*(*Q*), reduced pair distribution 435 function *G*(*r*), and pair distribution function *g*(*r*). (**a**) Comparison of *G*(*r*) functions

- 436 before and after five iterative optimization calculations; (**b**)–(**d**) typical *S*(*Q*), *g*(*r*), and
- 437 *G*(*r*) functions after optimization at 34, 56, and 74 GPa (light blue, light green, and pink



438 lines, respectively).





442 circular symbol with errors of  $K_{TPr} = 110.5(250)$  GPa and  $K'_{TPr} = 7.2(25)$ .

443

444







455 **FIGURE 5.** Densities of liquid and solid Fe–Ni–S and Fe–S alloys and Fe. The data of  $456$  Fe<sub>46.5</sub>Ni<sub>28.5</sub>S<sub>25</sub> obtained in this study are represented by solid pink circles. The pink line 457 indicates the fitting result using Vinet EoS. Previous measurements using a similar XRD 458 method for liquid  $Fe_{76}Ni_4S_{20}$  (Morard et al. 2013), XRD method in Paris–Edinburgh 459 press for liquid  $Fe_{77.1}S_{22.9}$  and  $Fe_{70.6}S_{29.4}$  (Morard et al. 2018), and X-ray absorption 460 method in multianvil press (Terasaki et al. 2019) for liquid  $Fe_{73}Ni_{10}S_{17}$  and  $Fe_{60}Ni_{10}S_{30}$ 

- are represented by the open diamonds and squares, respectively. The gray and light blue
- lines indicate the calculated densities of liquid Fe using the EoS in Kuwayama et al.
- (2020) and solid Fe3S using the EoS in Thompson et al. (2020), respectively, at 3400 K.
- Dotted and broken lines indicate the calculated isothermal density profiles of liquid
- Fe46.5Ni28.5S25 at 2700 and 3900 K.





- 472 ellipsoids at 80% probability level. Red and yellow symbols indicate the thermal
- 473 vibrations of Fe/Ni and S, respectively.
- 474





and (**c**) unit-cell volume *V* (purple); (**d**) a comparison of the expansion rates of the a and

c axes based on the values at 300 K.

482

483



485 **FIGURE 8.** Densities of liquid Fe–Ni–S alloys and Fe along adiabats with *TCMB* = 3600

486 and 4300 K (blue and pink curves, respectively). Density profiles of  $Fe_{46.5}Ni_{28.5}S_{25}$ 

487 calculated from the present results and pure Fe (Kuwayama et al. 2020) are shown with

488 broken and dashed lines, respectively. Solid blue and red curves indicate the best fits to





**FIGURE 9.** Isothermal density profiles of liquid Fe46.5Ni28.5S25 (16wt% S) and pure Fe

(0 wt% S) in the pressure range corresponding to the Martian core at 1500 (blue), 1900

(green), and 2300 K (pink).

