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Unveiling Carbon Dioxide and Ethanol Diffusion in Carbonated Water-Ethanol Mixtures by Molecular Dynamics Simulations

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Abstract: The diffusion of carbon dioxide (CO₂) and ethanol (EtOH) is a fundamental transport process behind the formation and growth of CO₂ bubbles in sparkling beverages and the release of organoleptic compounds at the liquid free surface. In the present study, CO₂ and EtOH diffusion coefficients are computed from molecular dynamics (MD) simulations and compared with experimental values derived from the Stokes-Einstein relation on the basis of viscometry experiments and hydrodynamic radii deduced from former nuclear magnetic resonance (NMR) measurements. These diffusion coefficients steadily increase with temperature and decrease as the concentration of ethanol rises. The agreement between theory and experiment is suitable for CO₂. Theoretical EtOH diffusion coefficients tend to overestimate slightly experimental values although the agreement can be improved by changing the hydrodynamic radius used to evaluate experimental diffusion coefficients. This apparent disagreement should not rely on limitations of the MD simulations nor on the approximations made to evaluate theoretical diffusion coefficients. Improvement of the molecular models as well as additional NMR measurements on sparkling beverages at several temperatures and ethanol concentrations would help solve this issue.

Keywords: ethanol; carbon dioxide; diffusion; molecular dynamics; viscometry

1. Introduction

Sparkling alcoholic and non-alcoholic beverages are massively consumed since decades all over the world [1–3]. Dissolved carbon dioxide (CO₂) is obviously the gaseous species responsible for the sparkle in every sparkling beverage. In premium sparkling wines, for example, dissolved CO₂ results from a second in-bottle fermentation process promoted by adding yeasts and sugar in a still base wine stored in thick-walled glass bottles hermetically sealed with a crown cap or a cork stopper [4]. In bottled or canned beers, dissolved CO₂ is also the result of a natural fermentation process [5,6]. In carbonated soft drinks (and in some cheaper sparkling wines and sparkling waters) carbonation is rather undertaken by forcing exogenous gas-phase CO₂ to dissolve into still soft drinks, and by conditioning them in cans or in bottles most often sealed with crown or screw caps [1].

The capacity of gas-phase CO₂ to get dissolved in a liquid phase is ruled by Henry's law, which states that the concentration of dissolved CO₂ found in the liquid phase remains proportional to the partial pressure of gas-phase CO₂ found in the sealed bottle or can [7]. From the industrial angle, the level of dissolved CO₂ in the beverage is a parameter of importance, because it is responsible for the very much sought-after bubbling process. Under standard tasting conditions, the level of dissolved CO₂ found in a sparkling beverage directly impacts various sensory properties such as the growth rate of ascending bubbles [8,9], the overall number and size of bubbles likely to form in a glass [10,11], the release of aromas through bursting bubbles [12–14], the kinetics of the

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38 degassing process [15–19], and the very characteristic tingling sensation in mouth [20–
 39 22]. Suffice to say that the presence of dissolved CO₂ strongly modifies the organoleptic
 40 properties of the sparkling beverage.

In the past two decades, the chemical physics behind bubble dynamics has been thoroughly investigated in champagnes [3,8,23], beers [6,8,10,24], carbonated soft drinks [25,26], and sparkling waters [27–29], both experimentally and theoretically. In addition to the level of dissolved CO₂ responsible for modifying the overall sensory properties of carbonated beverages, as described above, another key parameter of CO₂ was pointed out as being significantly involved in the bubbling process, as well as in the degassing process under standard tasting conditions. This is the bulk diffusion coefficient of dissolved CO₂ in the liquid phase [30]. Indeed, the frequency of bubble nucleation in a glass as well as the growth rate of ascending bubbles both increase with the diffusion coefficient of dissolved CO₂ [23]. As exemplified in Figure 1, it was determined that small bubbles rising in-line in a glass of sparkling wine grow by diffusion, with a theoretical growth rate k expressed by the following relationship [9]:

$$k = \frac{dr}{dt} \approx 0.63 \frac{RT}{P} D^{2/3} \left(\frac{2\rho g}{9\eta} \right)^{1/3} (c_L - c_0) \quad (1)$$

41 where r is the bubble radius (in m), t is the time (in s), R is the ideal gas constant
 42 ($\approx 8.314 \text{ J K}^{-1} \text{ mol}^{-1}$), T is the liquid phase temperature (in K), P is the partial pressure
 43 of CO₂ within the bubble (close to 10^5 Pa), D is the bulk diffusion coefficient of CO₂ in
 44 the liquid phase (in $\text{m}^2 \text{ s}^{-1}$), ρ is the liquid density (in kg m^{-3}), g is the acceleration of
 45 gravity ($\approx 9.8 \text{ m s}^{-2}$), η is the liquid dynamic viscosity (in Pa s), c_L is the bulk concentration
 46 of dissolved CO₂ in the liquid phase (in mol m^{-3}), and c_0 is the concentration
 47 of dissolved CO₂ close to the bubble's interface in Henry's equilibrium with gas-phase
 48 CO₂ in the bubble (in mol m^{-3}). The previous equation, indeed valid for small CO₂
 49 bubbles rising in a carbonated beverage, reveals the crucial role of the bulk diffusion
 50 coefficient of CO₂ in the bubble growth.

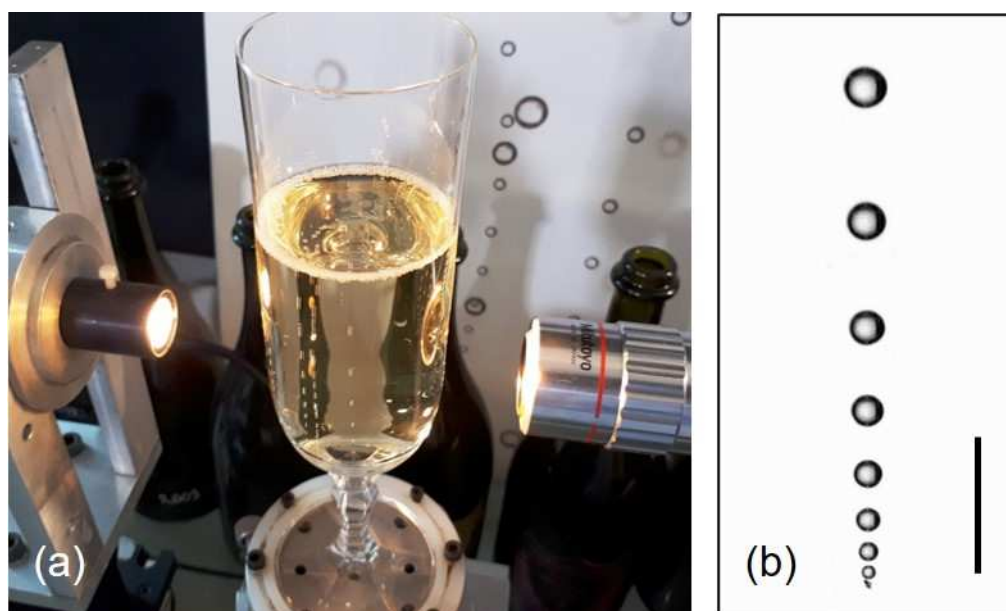


Figure 1. High-speed video imaging device aimed at filming ascending bubbles in glasses poured with sparkling wines (a), with a micrograph showing CO₂ bubbles rising in-line and growing by diffusion along the side of the glass (b) (bar = 1 mm). (photographs by G. Liger-Belair).

51 Moreover, in sparkling alcoholic beverages, the rate at which ethanol (EtOH) evaporates
 52 (and therefore also influences the sensory properties of the beverages) depends

53 on the diffusion coefficient of EtOH [13,14,31]. Actually, these crucial transport prop-
54 erties of both CO₂ and EtOH involved in sparkling beverage tasting were found to
55 strongly increase with the temperature of the liquid phase, as thoroughly described
56 through classical molecular dynamics (MD) and nuclear magnetic resonance (NMR)
57 spectroscopy in Brut-labelled Champagne wines (*i.e.*, champagnes with concentrations
58 of sugars < 12 g L⁻¹) [32–34]. Otherwise, from the lowest-alcohol beers and the sweet
59 ciders to the highest alcohol beers and sparkling wines, the sparkling alcoholic beverage
60 segment is characterized by a very wide range of ethanol levels (from close to 0
61 to almost 15 % ethanol by volume). Yet, by strongly modifying the viscosity of water-
62 ethanol mixtures and commercial beverages [35–37], no doubt that the concentration
63 of ethanol should significantly modify the subsequent transport properties of every
64 species found in the water-ethanol mixture, including the respective diffusion coeffi-
65 cients of both CO₂ and EtOH.

66 In this article, the diffusion coefficients of CO₂ and EtOH are evaluated by MD
67 simulations as a function of the volumetric alcoholic title at three temperatures relevant
68 for applications on carbonated alcoholic beverages. They are compared with experi-
69 mental values derived from the Stokes-Einstein relation on the basis of viscosity mea-
70 surements in the same section. The results are presented and compared with data from
71 the literature in Section 2. The influence of the hydrodynamic radius definition on the
72 comparison between theory and experiment and possible improvements of the theoret-
73 ical approach are discussed in Section 3. Details on MD simulations and experimental
74 measurements are provided in Section 5 together with the strategy followed to evaluate
75 CO₂ and EtOH diffusion coefficients, before proposing openings to the present study
76 in Section 4.

77 2. Results

78 Experimental viscosities are depicted in Figure 2 as a function of the EtOH level
79 expressed as percentage by volume at the three temperatures of interest. As expected,
80 they increase regularly as the alcoholic degree increases and the temperature decreases.
81 These results are in agreement with former measurements carried out on carbonated
82 hydroalcoholic solutions with ethanol concentrations representative of brut-labelled
83 champagnes (~ 12.5 % vol.). They are slightly smaller than viscosities expected in cham-
84 pagnes because of the broad variety of species other than water, CO₂, and EtOH, con-
85 tained in these beverages like glycerol, lactic and tartaric acids, and sugars [38].

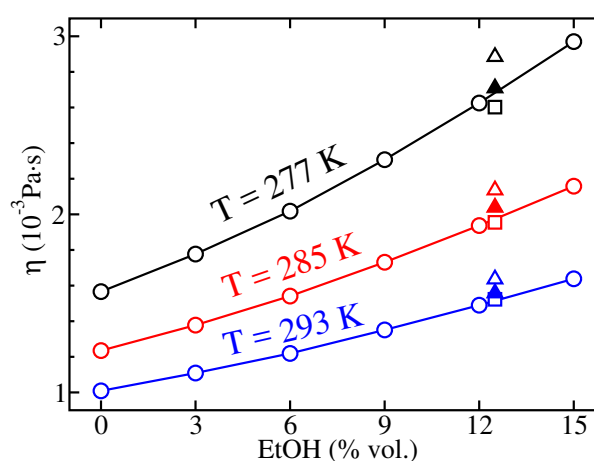


Figure 2. Experimental viscosities of hydroalcoholic solutions at $T = 277$ K (black circles), $T = 285$ K (red circles), and $T = 293$ K (blue circles). Viscosities from the literature obtained for hydroalcoholic solutions (open squares) and brut-labelled champagnes (triangles) are also indicated [33]. Data on brut-labelled champagnes are derived from viscometry (open triangles) and an Arrhenius law (closed triangles) [33,39].

86 CO₂ diffusion coefficients derived from MD simulations and experimental viscosi-
87 ties determined by applying the Stokes-Einstein relation are reported in Figure 3. The
88 agreement between theory and experiment is generally satisfactory at all temperatures
89 and alcoholic degrees provided that statistical uncertainties are taken into account. Cor-
90 recting theoretical diffusion coefficients for their possible system-size dependence only
91 yields a slight increase of diffusion coefficients that does not alter the overall agreement
92 with experimental data. Strikingly, the worst agreement is obtained at $T = 293$ K and
93 low concentrations of ethanol whereas the OPC water model reproduces accurately wa-
94 ter self-diffusivity at such a temperature [40], a behavior that we checked in simulation
95 boxes only filled with water molecules. However, it is worth noting that CO₂ diffu-
96 sion coefficients in fizzy water was found to be $1.85 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$ [30] and previous
97 MD simulations modeling CO₂ diffusion in SPC/E (Extended Simple Point Charge)
98 water [41] lead to CO₂ diffusion coefficients of about $2.1 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$ with relatively
99 large uncertainties: In Het Panhuis et al. [42] and Perret et al. [32] respectively found
100 values of $(2.1 \pm 0.3) \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$ and $(2.11 \pm 0.14) \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$ when computing
101 the MSD of diffusing CO₂ molecules, and In Het Panhuis et al. [42] obtained values
102 of $(2.1 \pm 0.08) \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$ and $(1.8 \pm 1.33) \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$ after calculating the veloc-
103 ity and force autocorrelation functions, respectively. Apart from the apparent devia-
104 tion at low EtOH concentration that might be mitigated by enlarging the simulation
105 box or averaging over several trajectories, several studies focused on CO₂ diffusion
106 in brut-labelled champagnes. The experimental diffusion coefficients estimated in the
107 present work are in very close agreement with previous ¹³C NMR experiments per-
108 formed in carbonated hydroalcoholic solutions respecting brut-labelled champagnes
109 proportions [33] although we are aware that there might be a bias in this comparison be-
110 cause the hydrodynamic radii used to get our experimental diffusion coefficients were
111 derived from the same NMR measurements. The most recent theoretical CO₂ diffusion
112 coefficients obtained for these systems [34] are also in good agreement with our results
113 unlike former results obtained with the TIP5P (Transferable Intermolecular Potential
114 with 5 Points) and SPC/E water models [41,43] that sometimes significantly depart
115 from the experimental curve.

116 Theoretical and experimental EtOH diffusion coefficients are illustrated in Figure 4.
117 Experimental data remain in perfect agreement with former NMR measurements per-
118 formed on carbonated hydroalcoholic solutions respecting brut-labelled champagnes
119 proportions and EtOH diffusion coefficients in champagnes are once again lowered
120 due to the multicomponent nature of these mixtures [33]. In contrast, theoretical results
121 overestimate slightly experimental data and correcting EtOH diffusion coefficients for
122 system-size dependence due to periodic boundary conditions degrades even more the
123 agreement with experiments. These theoretical results are however in agreement with
124 recent MD simulations carried out on carbonated hydroalcoholic mixture with an EtOH
125 concentration of ~ 12.4 % vol. [34] and water molecules described by the TIP4P/2005
126 (Transferable Intermolecular Potential with 4 Points / 2005) [44] and OPC models [40].
127 No clear trend emerge from former results of MD simulations achieved by using the
128 SPC/E and TIP5P water models since they can underestimate, overestimate or even be
129 in good agreement with experiments depending on temperature.

130 Finally, theoretical densities only overestimate experimental values by 1 to 4 kg
131 m^{-3} at all temperatures and EtOH concentrations (see Tables S1 and S2 of the supple-
132 mentary materials). The high quality of these theoretical densities contrasts with con-
133 clusions brought in a recent publication [34] where theoretical densities obtained with
134 the OPC water model were found to underestimate experimental ones by $\sim 6 \text{ kg m}^{-3}$
135 at temperatures ranging from 277 K to 293K and an EtOH concentration of 12.4% [33].
136 This discrepancy comes from the use of different benchmark experimental densities, the
137 set of measurements considered in the present work being of higher quality. Indeed, for-
138 mer experimental densities obtained for hydroalcoholic solutions extended from 990 kg
139 m^{-3} to 993 kg m^{-3} , namely about 8 kg m^{-3} above the expected values.

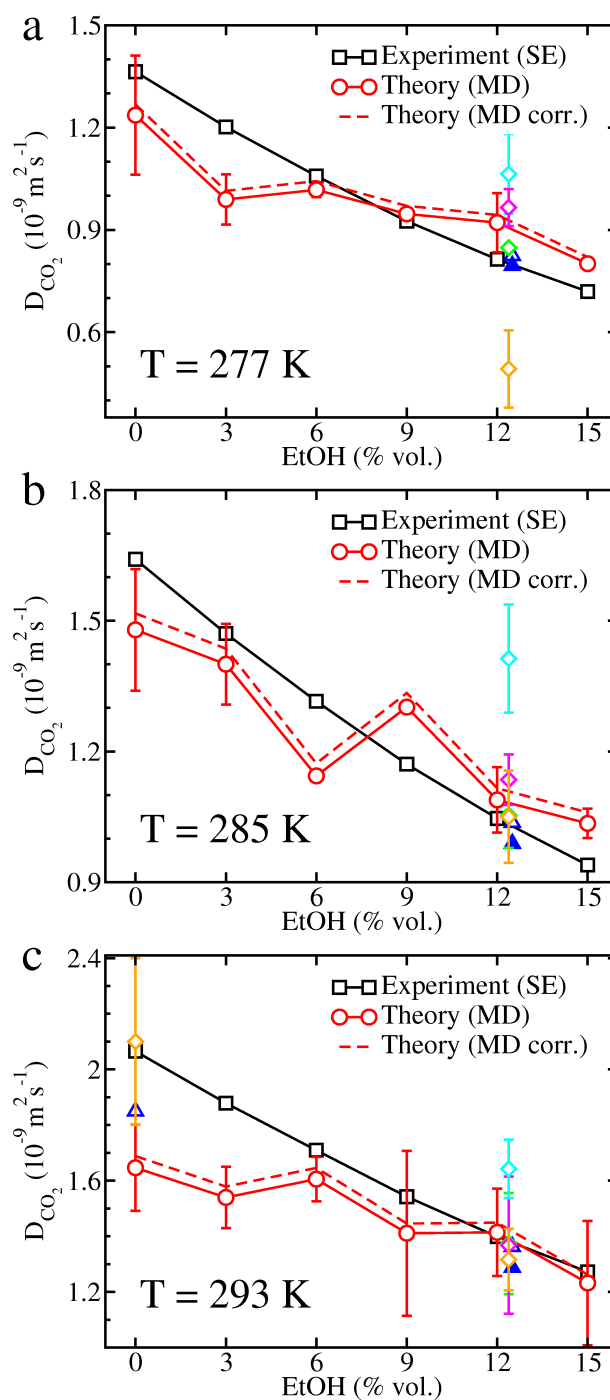


Figure 3. Experimental and theoretical CO₂ diffusion coefficients in carbonated hydroalcoholic solutions at (a) $T = 277 K$, (b) $T = 285 K$, and (c) $T = 293 K$. Experimental values (black squares) derived from the Stokes-Einstein (SE) relation and theoretical values deduced from MD simulations (red circles) are reported together with theoretical diffusion coefficients corrected for system-size dependence (red dashed curve). Data from the literature are also indicated: MD simulations on carbonated hydroalcoholic solutions (EtOH at 12.4% vol.) where water is described by the OPC model (green diamond) [34], TIP4P/2005 model (magenta diamond) [34], SPC/E model (orange diamond) [33,42], and TIP5P model (cyan diamond) [33]; ¹³C NMR measurements on carbonated hydroalcoholic mixtures [33] or fizzy water [30] (blue open triangles) and brut-labelled Champagnes (blue closed triangles) [33].

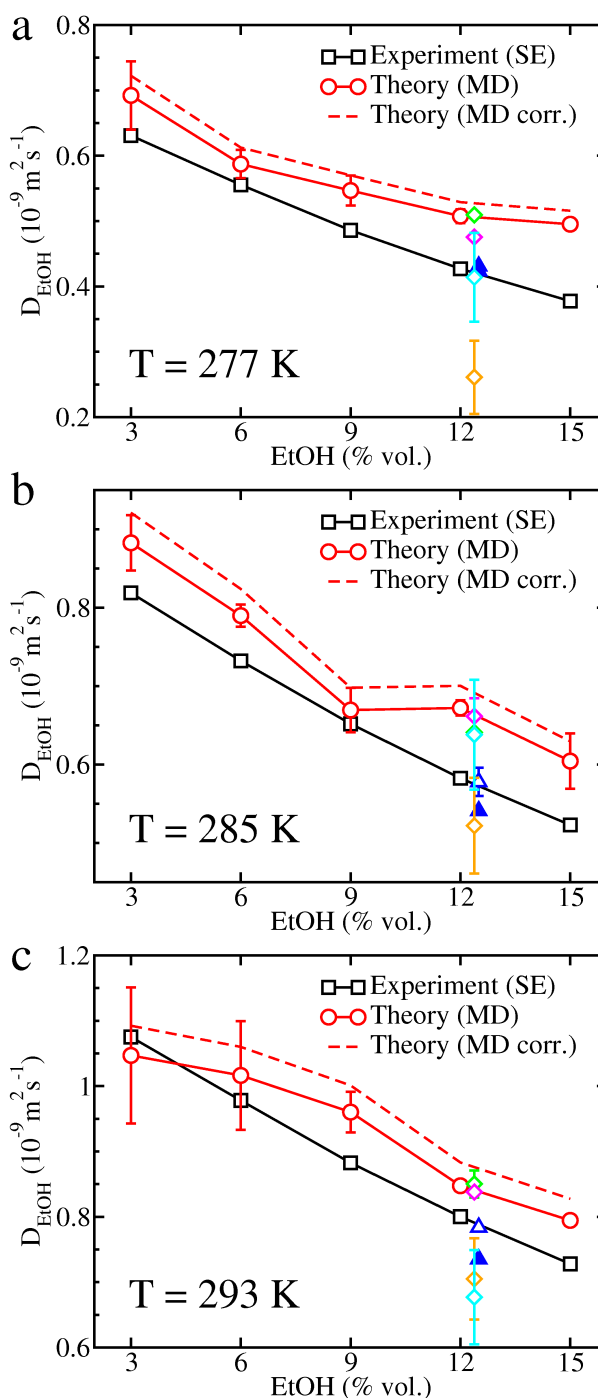


Figure 4. Experimental and theoretical EtOH diffusion coefficients in carbonated hydroalcoholic solutions at (a) $T = 277 \text{ K}$, (b) $T = 285 \text{ K}$, and (c) $T = 293 \text{ K}$. The definition of symbols and colors is the same as in Figure 3.

140 3. Discussion

141 3.1. Definitions of hydrodynamic radii

142 Experimental diffusion coefficients are determined by applying the Stokes-Einstein
143 relation where the radii of CO_2 and EtOH are former estimates based on ^{13}C NMR
144 measurements on carbonated hydroalcoholic solutions respecting brut-labelled cham-
145 pagnes concentrations [33]. Thus, it seems relevant to evaluate the sensitivity of exper-
146 imental diffusion coefficients to the magnitude of these radii, all the more since vari-
147 ations in these diffusion coefficients may alter our conclusions when comparing with
148 theoretical values extracted from MD simulations.

149 The Stokes-Einstein relation is a mathematical formula primarily devised to evalu-
150 ate the diffusion of a large spherical particle within a solvent composed of much smaller
151 molecules where the Stokes' law applies [45]. However, this formula was proved use-
152 ful in other contexts provided that an effective radius could be guessed for the dif-
153 fusing particle. In particular, it was found well suited to evaluate the diffusion of
154 CO₂ in multicomponent mixtures like champagnes [33,38,39]. Intuitively, we might
155 approximate the hydrodynamic radius R of a species in a mixture as $R = (3V/4\pi)^{1/3}$
156 where V would be the volume occupied by the species in the mixture but such a defi-
157 nition might be involved to apply in multicomponent liquids. Conversely, several sim-
158 ple structural radii can be defined for a molecule, like the rms distance of its atoms
159 to its center of mass (R_{rms}) or its radius of gyration (R_{gyr}). In our MD simulations
160 devoted to carbonated hydroalcoholic mixtures, these structural radii do not change
161 when varying the temperature or alcoholic degree because bonds are constrained. For
162 CO₂ we found $R_{rms} \approx 0.94 \text{ \AA}$ and $R_{gyr} \approx 0.98 \text{ \AA}$, values alike those derived from
163 other CO₂ models, like TraPPE [46] or MSM-ZD [34,47], or from the CO₂ structure
164 available in the NIST database [48], namely $R_{rms} \approx 0.95 \text{ \AA}$ and $R_{gyr} \approx 0.99 \text{ \AA}$. For
165 EtOH we found $R_{rms} \approx 1.58 \text{ \AA}$ and $R_{gyr} \approx 1.19 \text{ \AA}$ in agreement with values deduced
166 from the EtOH structure available in the NIST database, namely $R_{rms} \approx 1.58 \text{ \AA}$ and
167 $R_{gyr} \approx 1.18 \text{ \AA}$. These radii can also be compared with the NMR-based radii used to
168 determine the experimental diffusion coefficients, namely $R_{CO_2} = 0.95 - 1.05 \text{ \AA}$ and
169 $R_{EtOH} = 1.80 - 1.88 \text{ \AA}$ at temperatures ranging from 277 K to 293 K and EtOH con-
170 centrations of $\sim 12.5 \%$ vol. [33]. Both structural radii R_{rms} and R_{gyr} provide a proper
171 estimate of the NMR-based radii for CO₂ but they underestimate strongly the experi-
172 mental values for EtOH and replacing the NMR-based radii by R_{rms} or R_{gyr} to plot ex-
173 perimental data reported in Figures 3 and 4 can have an influence on the comparisons
174 between theory and experiment.

175 We have previously noticed that, apart from some intriguing deviation at $T =$
176 293 K and low EtOH concentrations, theoretical and experimental CO₂ diffusion coef-
177 ficients were in good agreement with each other. Moreover, replacing the NMR-based
178 radii by the CO₂ rms radius or radius of gyration to calculate the experimental CO₂ dif-
179 fusion coefficients would not significantly alter this conclusion since the deviation be-
180 tween all these radii does not exceed 10%. Experimental diffusion coefficients would be
181 somewhat lower at $T = 277 \text{ K}$ with R_{gyr} and higher at $T = 285 \text{ K}$ and $T = 293 \text{ K}$ in both
182 cases which would degrade the agreement at low EtOH concentrations but improve it
183 at the three highest EtOH concentrations at $T = 285 \text{ K}$ (see Figure S1 of the supplement-
184 ary materials). In contrast, both structural definitions of radii underestimate the experi-
185 mental radius for EtOH, the discrepancy growing to $\sim 14 - 17 \%$ for R_{rms} and $51 - 55 \%$
186 for R_{gyr} . Replacing the NMR-based radii by R_{rms} to determine the experimental EtOH
187 diffusion coefficients would improve the agreement at $T = 277 \text{ K}$ but theoretical EtOH
188 diffusion coefficients would tend to underestimate slightly experimental values and us-
189 ing R_{gyr} instead of R_{rms} would increase even more this underestimation (see Figure
190 S2 of the supplementary materials). Moreover, the experimental EtOH diffusion coeffi-
191 cients would then differ from NMR data. Obviously, no structural definition is perfectly
192 suited to model non-spherical molecules like CO₂ or EtOH, and we can at most expect
193 that the volume occupied by the molecule is fairly reproduced. However, in absence of
194 exhaustive tables of experimental radii, R_{rms} appears to be a more accurate definition
195 for the effective radius to be used in the Stokes-Einstein relation than R_{gyr} as pointed
196 out in a previous work [34]. This comes from the mass-weighting of atomic positions
197 in the definition of the radius of gyration that gives, for instance, too much weight to
198 the central carbon atoms at the expense of the peripheral hydrogen atoms in the case of
199 EtOH.

200 The most appropriate way to unravel the mystery behind the partial disagreement
201 between theory and experiment would probably be to compare our experimental re-
202 sults with NMR data on carbonated hydroalcoholic solutions at several temperatures

203 and alcoholic degrees, data that are unfortunately unavailable to the best of our knowl-
204 edge. This would enable us to evaluate the accuracy of former NMR-based radii in
205 predicting the diffusion coefficients of CO₂ and EtOH at several ethanol concentrations
206 and temperatures, then getting more accurate results to compare with realistic alcoholic
207 sparkling beverages.

208 3.2. Possible improvements of the theoretical approach

209 Beside the question on the definition of an optimal hydrodynamic radius represen-
210 tative of non-spherical molecules in carbonated hydroalcoholic beverages, the quality
211 of theoretical results derived from MD simulations might also be improved by averag-
212 ing the statistical data over additional molecules or longer times, employing a more
213 sophisticated approach to evaluate diffusion coefficients, or optimizing the parameters
214 of the molecular models. Although increasing the system size and simulation time
215 could mechanically improve the accuracy of diffusion coefficients, at the expense of ad-
216 ditional computational cost, we do not expect significant improvements of the results
217 because equilibrium was reached after 20 ns, statistical uncertainties and corrections for
218 system-size dependence are already included in our calculations, and diffusion coeffi-
219 cients of CO₂, the species less abundant for which averages should be the least accurate,
220 are already of good quality when compared with experiments.

221 Maxwell-Stefan [49] or Fick [50] multicomponent diffusion coefficients could also
222 be evaluated without assuming low concentrations of some species in the mixture, as
223 done by Garcia-Ratés et al. to describe CO₂ diffusion in brines [51], although this ap-
224 proach is best suited for high concentrations of solutes. As an example, Garcia-Ratés
225 et al. performed MD simulations in boxes containing ~ 3000 water molecules, up to
226 120 CO₂ molecules and 216 monatomic ions (Na⁺ or Cl⁻). Our simulations contain
227 4×10^4 water molecules, 200 CO₂ molecules and up to 2199 EtOH molecules which
228 suggests that CO₂ can probably be considered as traces in the mixture but this assump-
229 tion is more questionable for EtOH when its abundance reaches several thousands of
230 molecules. It is however worth noting that the worse agreements with experiments oc-
231 curs at low ethanol levels rather than high ones (see Figure 4) which would suggest that
232 our approach to evaluate EtOH diffusion coefficient is not the main source of discrep-
233 ancy, event at the higher EtOH concentrations. The accuracy of our theoretical method
234 should therefore mainly rely on the efficiency of the molecular models.

235 In a recent study, Ahmed Khaireh et al. have analyzed the effect of six water
236 models and three CO₂ models, by constraining bonds or leaving them free, on CO₂
237 diffusion in carbonated hydroalcoholic mixtures respecting brut-labelled champagne
238 proportions as a function of temperature [34]. CO₂ diffusion coefficients were derived
239 from MSDs and the integration of velocity autocorrelation functions. They concluded
240 that the most accurate CO₂ diffusion coefficients were obtained for the OPC water
241 model, and to a lesser extent the TIP4P/2005 water model, with little influence of the
242 CO₂ model in use. By following the same approach we confirmed the quality of CO₂
243 diffusion coefficients in carbonated hydroalcoholic mixtures, especially at EtOH con-
244 centrations in between 6 and 15 % vol. (see Figure 3). However, Ahmed Khaireh et
245 al. only considered the OPLS-aa force field to parameterize EtOH and testing other
246 force fields, like CHARMM (Chemistry at HARvard Macromolecular Mechanics) [52]
247 might improve EtOH diffusion coefficients. In particular, studies using CHARMM
248 had been undertaken on brut-labelled champagnes with the SPC/E and TIP5P water
249 models [32,33]. Although the TIP5P model yielded an overestimation of the CO₂ diffu-
250 sion coefficients, these coefficients were properly described at the higher temperatures
251 ($T \gtrsim 285$ K) with the SPC/E model. Conversely, the TIP5P water model lead somewhat
252 better agreement with experimental EtOH diffusion coefficients than the SPC/E water
253 model. Combining the CHARMM force field with the OPC water model and the EPM2
254 CO₂ model might be an opening of the present work although we must remind that

255 OPLS-aa should be a choice force field to describe EtOH since this molecule is natively
256 parameterized in OPLS-aa.

257 It is also worth noting that molecular mechanics is probably more suited to repro-
258 duce the properties of rigid nonpolar CO₂ molecules than the properties of the more
259 flexible EtOH molecules, which would be better modeled by quantum-mechanical ap-
260 proaches. At the molecular mechanics level of accuracy, Perret et al. [32] estimated
261 the number of hydrogen bonds (H bonds) in carbonated hydroalcoholic solutions rep-
262 resentative of brut-labelled champagnes by assuming a H bond is formed between a
263 hydrogen atom and an oxygen atom if the O_d-O_a distance between the donor oxygen
264 atom O_d and the acceptor oxygen atom O_a remains below 0.35 nm and the H-O_d-O_a
265 angle does not exceed 35°, as advocated by Chandler [53]. From this definition of H
266 bonds, they found that EtOH created roughly fifty times more H bonds than CO₂ when
267 water molecules were described by the SPC/E and TIP5P models. This result, later
268 confirmed by Lv et al. [54], contributed to account for the smallness of EtOH diffusion
269 coefficients compared with CO₂ ones. Although it is hard to predict how an accurate
270 description of the rotation of EtOH methyl groups would precisely alter the number of
271 H bonds involving EtOH molecules, we may expect an increase of this number. In such
272 a case, the mobility of these molecules, and subsequently the values of their diffusion
273 coefficients, might decrease which should improve the agreement with experiments.

274 4. Conclusion

275 The analysis of transport phenomena in sparkling beverages, among which CO₂
276 and EtOH diffusions occupy a choice position, is essential to better comprehend the
277 mechanisms behind the formation and growth of CO₂ bubbles and the release of organo-
278 leptic compounds at the free surface of the liquid. In the present study, MD simu-
279 lations carried out on carbonated hydroalcoholic mixtures at three temperatures and
280 six alcoholic degrees were proved useful to predict CO₂ diffusion coefficients whereas
281 EtOH diffusion coefficients seemed somewhat overestimated. Disagreements with ex-
282 periments are mainly attributed to limitations of the molecular models, especially that
283 of EtOH, although an increase of the statistics and improvements of the method to eval-
284 uate diffusion coefficients might also influence the results. However, this conclusion
285 was drawn on the basis of experimental diffusion coefficients derived from the Stokes-
286 Einstein relation. The values of these diffusion coefficients therefore depend on the
287 accuracy of viscosity measurements and on the definition of the effective radii used for
288 the diffusing species (CO₂ and EtOH here). This observation made us assert that accu-
289 rate ¹³C NMR measurements at several temperatures and alcoholic degrees would be
290 recommended to confirm the quality of experimental diffusion coefficients reported in
291 our study and, equivalently, ensure the suitability of the molecular radii inserted in the
292 Stokes-Einstein relation to get them.

293 Despite possible inaccuracies from both the experimental and theoretical sides, this
294 comprehensive investigation of the influence of the alcoholic degree on CO₂ and EtOH
295 diffusion at several temperatures, together with a recent work focused on the effect of
296 water and CO₂ models on CO₂ diffusion coefficients in carbonated hydroalcoholic so-
297 lutions respecting brut-labelled champagnes proportions [34], open new avenues for
298 theoretical studies on sparkling beverages. First of all, they can serve as reference data
299 to evaluate the influence of other species, like sugars, on CO₂ diffusion. As an exam-
300 ple, champagnes are mainly composed of water, CO₂, and EtOH but a more sophisti-
301 cated model would include glycerol, tartaric and lactic acids, and various amounts of
302 sugar [38] to evaluate how the degassing of CO₂ is influenced by the concentration of
303 sugar. CO₂ bubbles, whose size depends on gas exchanges at the interface between
304 the bubble and bulk champagne, are also known to take organoleptic compounds with
305 them during their ascent to the free surface of the liquid, and their subsequent explo-
306 sion releases a cloud of droplets with a composition slightly different from the bulk
307 one [12]. Nanometer-sized hydroalcoholic droplets could be first designed to tackle the

308 evaporation dynamics of small droplets and compare the corresponding results with
 309 available experimental data [13], before making the droplet bigger and its composition
 310 closer to that of aerosols representative of sparkling wines. Finally, a proper molecular
 311 modeling of sparkling beverages is needed to investigate the diffusion of CO₂ through
 312 the walls of cellulose fibers, nucleation sites responsible for the formation of CO₂ bubbles [55].
 313 The present work is therefore an additional brick laid to better understand the
 314 influence of molecular models on CO₂ and EtOH diffusion in sparkling beverages that
 315 calls for future theoretical studies in this field of research.

316 5. Materials and Methods

317 5.1. Molecular dynamics simulations

318 A total of 18 MD simulations were carried out with the open-source massively parallel
 319 GROMACS software (2018 versions) [56–59] on carbonated hydroalcoholic solutions at six ethanol (EtOH)
 320 concentrations and three temperatures relevant for sparkling alcoholic beverage applications,
 321 namely 277 K (fridge temperature), 285 K (cellar temperature), and 293 K (ambient temperature).
 322 A cubic box, containing 4×10^4 water molecules described by the OPC (Optimal Point Charge) 4-point
 323 rigid water model [40], 200 CO₂ molecules described by the popular EPM2 (Elementary Physical Model 2)
 324 model [60], and a variable number N of EtOH molecules described by the OPLS-aa (Optimized Potentials
 325 for Liquid Simulations-all atom) force field [61], is built with periodic boundary conditions
 326 imposed in the three spatial directions, as illustrated in Figure 5.
 327
 328

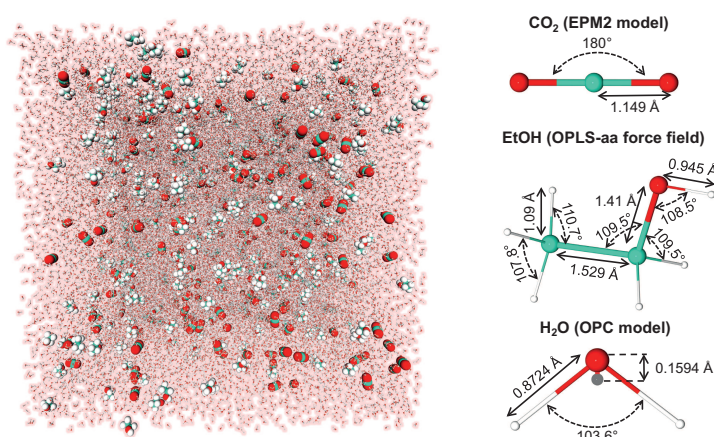


Figure 5. Example of simulation box containing 4×10^4 H₂O, 200 CO₂ and 385 EtOH (3% vol.). Bond distances and angles of the three molecules used in our model are indicated on the right panel. Pictures were generated with the VMD (Visual Molecular Dynamics) and Protein Imager softwares [62,63].

329 An alike simulation box has been recently employed by Ahmed Khairah et al. to investigate
 330 CO₂ diffusion in brut-labelled champagnes (alcoholic degree of ~ 12.4 % vol.) as a function of
 331 temperature [34]. N is calculated for water and EtOH properties at
 332 $T = 285$ K, temperature at which wines undergo their second fermentation.

$$N = N_{\text{H}_2\text{O}} \frac{\rho_{\text{EtOH}} M_{\text{H}_2\text{O}}}{\rho_{\text{H}_2\text{O}} (r - 1) M_{\text{EtOH}}} \quad (2)$$

333 where $N_{\text{H}_2\text{O}} = 4 \times 10^4$, $\rho_{\text{H}_2\text{O}} = 999.49 \text{ kg m}^{-3}$, $\rho_{\text{EtOH}} = 796.06 \text{ kg m}^{-3}$, M_i is the molar
 334 mass of species i , and $r = V_{\text{tot}}/V$ is the ratio between the total volume of the mixture and that
 335 occupied by EtOH. Table 1 reports the values of N for alcoholic degrees ranging from 0 to 15 %
 336 vol. by steps of 3 % vol. Lennard-Jones and van der Waals interactions are truncated at a distance
 337 of 1.5 nm, a smooth particle-mesh Ewald (SPME) summation technique is applied to handle long-range
 338 electrostatic interactions [64–66],

and bonds are constrained during the simulations. The whole range of temperatures and EtOH abundances spanned during our simulations only yield a 5 % increase of the box side length L from ~ 10.6 nm to ~ 11.2 nm.

Table 1. Number of EtOH molecules (N) in simulation boxes composed of 4×10^4 water molecules and 200 CO_2 molecules for EtOH levels ranging from 0 to 15 % vol. N values are computed at a reference temperature of 285 K.

EtOH (% vol.)	0	3	6	9	12	15
N	0	385	795	1232	1699	2199

For each MD simulation, the system is first equilibrated for 1 ns in the NVT ensemble by fixing the appropriate temperature and density. A subsequent 19-ns equilibration run is performed in the NPT ensemble at a pressure of 1 bar and followed by a 10-ns production run devoted to the storage of statistical data, atomic positions and velocities every 1 ps. Temperature is controlled by applying a Nosé-Hoover thermostat with a time constant of 0.5 ps [67,68] and pressure is maintained by a Parinello-Rahman barostat with a time constant of 0.2 ps [69]. Carbonated hydroalcoholic solutions being mainly composed of water, their isothermal compressibility is taken as that of pure water, namely $\kappa(277\text{ K}) = 4.95 \times 10^{-5} \text{ bar}^{-1}$, $\kappa(285\text{ K}) = 4.73 \times 10^{-5} \text{ bar}^{-1}$, and $\kappa(293\text{ K}) = 4.59 \times 10^{-5} \text{ bar}^{-1}$ [34,70,71].

5.2. Theoretical diffusion coefficients

Carbonated hydroalcoholic solutions, and more generally sparkling beverages, are multicomponent systems and the diffusion coefficients of solvated species should be evaluated by solving the generalized Fick equations [50,72] or alike systems of equations based on Maxwell-Stefan or Onsager theories [49,73,74]. However, recent works on brut-labelled champagnes have shown that the properties of these mixtures (*e.g.*, water representing 95% of the quantity of matter, homogeneity and isotropy of the liquid on average, no chemical reaction on short time scales) make them properly modeled by a Fick's law very similar to that specific to simple fluids or binary liquids [32]. The probability density of diffusing species is therefore gaussian and the diffusion coefficients D of CO_2 and EtOH can be estimated by computing their mean-squared displacement (MSD) since $MSD(t) = \langle [\vec{r}(t) - \vec{r}(0)]^2 \rangle = 6Dt$ at long times. Each MSD is averaged over the number of diffusing molecules (*i.e.* 200 for CO_2 and up to 2199 for EtOH) and 10^4 time origins representative of our data storage frequency [32]. However, it is worth noting that diffusion coefficients computed from MD simulations with stick periodic boundary conditions should be corrected because the results can depend on the system size as pointed out by Yeh and Hummer [75]. Typical corrections depend on the viscosity of the liquid (η) but, by applying the Stokes-Einstein relation, we can find a formula for the corrected diffusion coefficient (D_0) that only depends on the original diffusion coefficient (D_{PBC}), the simulation box side length (L), and the hydrodynamic radius of the species (R).

$$D_0 = D_{PBC} + \frac{\zeta k_B T}{6\pi\eta L} \approx D_{PBC} \left(1 - \frac{\zeta R}{L}\right)^{-1} \quad (3)$$

where k_B is the Boltzmann constant, T is the temperature, and $\zeta = 2.837297$ is a constant [75]. Moreover, comparisons with ^{13}C NMR spectroscopic measurements carried out on carbonated hydroalcoholic solutions respecting brut-labelled champagnes proportions have shown that the dynamic viscosity of these mixtures could be properly predicted by replacing the hydrodynamic radius by the root-mean-square (rms) atomic distance of a diffusing species like CO_2 or EtOH [33,34]. The same definition of R , easily extracted from MD simulations, is therefore chosen in the present work to calculate the corrections brought to theoretical CO_2 and EtOH diffusion coefficients.

381 5.3. Viscometry and experimental diffusion coefficients

382 A rolling ball viscometer, Lovis 2000 M/ME (Anton Paar, Austria), was used to de-
383 termine the dynamic viscosity of hydroalcoholic solutions (with alcoholic degrees rang-
384 ing from 0 to 15 % vol.). This equipment measures the rolling time of a ball through
385 liquids according to Hoeppler's falling ball principle [76]. The samples were measured
386 with a steel ball and a 1.59 mm diameter capillary (0.3 – 90 mPa · s), at three temper-
387 atures $T = 277$ K, 285 K and 293 K. The repeatability in the viscosity measurement is
388 up to 0.1 %, and its reproducibility is up to 0.5 %, according to the manufacturer [76].
389 The required values of density for each hydroalcoholic solution were obtained from the
390 literature [77].

391 Experimental CO₂ and EtOH diffusion coefficients are derived from viscosity mea-
392 surements by applying the Stokes-Einstein relation

$$D = \frac{k_B T}{6\pi\eta R} \quad (4)$$

393 where k_B is the Boltzmann constant, T is the temperature (in K), η is the viscosity (in
394 Pa · s), and R is the hydrodynamic radius of the species under consideration (in m). To
395 the best of our knowledge there is no extensive data set in the literature on CO₂ and
396 EtOH hydrodynamic radii as a function of temperature and alcoholic degree. However,
397 these hydrodynamic radii have been evaluated as a function of temperature for car-
398 bonated hydroalcoholic mixtures with a concentration of ethanol representative of brut-
399 labelled champagnes [33]. They were derived from Eq.(4) by using diffusion coefficients
400 determined from ¹³C NMR measurements and viscosities measured with a similar ex-
401 perimental setup as in the present study. For carbon dioxide, hydrodynamic radii were
402 $R_{\text{CO}_2}(277 \text{ K}) = 0.95 \text{ \AA}$, $R_{\text{CO}_2}(285 \text{ K}) = 1.03 \text{ \AA}$, and $R_{\text{CO}_2}(293 \text{ K}) = 1.03 \text{ \AA}$. For ethanol,
403 they were $R_{\text{EtOH}}(277 \text{ K}) = 1.81 \text{ \AA}$, $R_{\text{EtOH}}(285 \text{ K}) = 1.85 \text{ \AA}$, and $R_{\text{EtOH}}(293 \text{ K}) = 1.80 \text{ \AA}$.
404 These experimental hydrodynamic radii will be used as reference values to evaluate ex-
405 perimental CO₂ and EtOH diffusion coefficients at all alcoholic degrees and compared
406 with theoretical radii extracted from MD simulations.

407 **Supplementary Materials:** The following are available online at <https://www.mdpi.com/1420-3049/1/1/>,
408 Table S1: Experimental densities (ρ_{exp}) and viscosities (η_{exp}) of carbonated hydroalcoholic mix-
409 tures at three temperatures and six alcoholic degrees, and corresponding CO₂ and EtOH dif-
410 fusion coefficients ($D_{\text{CO}_2}^{exp}$ and D_{EtOH}^{exp}) derived from the Stokes-Einstein relation and NMR-based
411 radii, Table S2: Average pressures $\langle P \rangle$ and densities (ρ) derived from MD simulations as well
412 as diffusion coefficients of species i deduced from MSDs (D_i) and diffusion coefficients corrected
413 for size-system dependence (D_i^0) at three temperatures and six alcoholic degrees, Figure S1: Ex-
414 perimental and theoretical CO₂ diffusion coefficients in carbonated hydroalcoholic solutions at
415 three temperatures and six alcoholic degrees, Figure S2: Experimental and theoretical EtOH dif-
416 fusion coefficients in carbonated hydroalcoholic solutions at three temperatures and six alcoholic
417 degrees.

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420 investigation D. A. B., M. A. and M. A. K.; resources: C. C., D. A. B., and G. L.-B.; data curation,
421 D. A. B., M. A. and M. A. K.; writing—original draft preparation, C.C., D. A. B. and G. L.-B.;
422 writing—review and editing, D. A. B. and G. L.-B.; visualization, D. A. B., G. L.-B. and M. A.
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438 **Abbreviations**

439 The following abbreviations are used in this manuscript:

440	CHARMM	Chemistry at HARvard Macromolecular Mechanics
	EPM2	Elementary Physical Model 2
	MD	Molecular Dynamics
	MSD	Mean-Squared Displacement
	MSM-ZD	Murthy, Singer, and McDonald - Zhang and Duan
	NIST	National Institute of Standards and Technology
	NMR	Nuclear Magnetic Resonance
441	OPC	Optimal Point Charge
	OPLS-aa	Optimized Potentials for Liquid Simulations-all atom
	RMS	Root Mean Square
	SPC/E	Extended Simple Point Charge
	TIP4P/2005	Transferable Intermolecular Potential with 4 Points / 2005
	TIP5P	Transferable Intermolecular Potential with 5 Points
	TraPPE	Transferable Potentials for Phase Equilibria

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