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A new methodology for a detailed investigation of quantized friction in ionic liquids[†]

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When confined at the nanoscale between smooth surfaces, an ionic liquid forms a structured film responding to shear in a quantized way, i.e. with a friction coefficient indexed by the number of layers in the gap. So far, only a few experiments have been performed to study this phenomenon, because of the delicate nature of the measurements. We propose a new methodology to measure friction with a Surface Force Balance, based on the simultaneous application of normal and lateral motions to the surfaces, allowing for a more precise, comprehensive and rapid determination of the friction response. We report on proof-of-concept experiments with an ionic liquid confined between mica surfaces in dry or wet conditions, showing the phenomenon of quantized friction with an unprecedented resolution. First, we show that the variation of the kinetic friction force with the applied load for a given layer is not linear, but can be quantitatively described by two additive contributions that are respectively proportional to the load and to the contact area. Then, we find that humidity improves the resistance of the layers to be squeezed-out and extends the range of loads in which the liquid behaves as a superlubricant, interpreted by an enhanced dissolution of the potassium ions on the mica leading to a larger surface charge. There, we note a liquid-like friction behavior, and observe in certain conditions a clear variation of the kinetic friction force over two decades of shearing velocities, that does not obey a simple Arrhenius dynamics.

1 Introduction

Lubrication consists in inserting a substance -generally a liquid- between two solid surfaces in order to produce a controlled and stable friction. Its study is an old but still active field of research, because of the complexity of the phenomena at play^{1,2}. As most real surfaces are rough, the contact between two macroscopic bodies involve in fact many mesoscopic asperities. A first consequence is that very large pressures, shear stresses and temperatures can be reached locally to promote tribological processes like wear, phase transitions or (electro)chemical reactions, making the role of the lubricant really challenging. A second consequence is that the lubricant should act at different scales simultaneously: for thick films, friction is governed by continuum hydrodynamics and depends on the lubricant viscosity (hydrodynamic regime); for thin films, friction is determined by subtle mechanisms at the molecular scale and depends on the lubricant chemical structure and its interactions with the solid surfaces (boundary lubrication regime). Ionics liquids, which are pure salts that are liquid at ambient temperature and pressure, are promising lubri-

cants thanks to their unique physico-chemical stability³. During the last decade, many experiments with a Surface Force Apparatus/Balance (SFA/SFB) or an Atomic Force Microscope (AFM) have been performed to measure the normal interactions on a single asperity across an ionic liquid. They consistently showed the presence of a structural force, i.e. a force profile exhibiting a decaying oscillation, that has been attributed to the ordering of ions in the confined film, with a structure consisting of alternating layers of anions and cations (as sketched in Figure 1(a))⁴⁻¹². Only a few studies have been conducted to measure the friction response in such structured film of ionic liquid, reporting on the phenomenon of “quantized friction”, namely the fact that the friction coefficient is indexed by the number of layers composing the film^{7,10,13-18}. Although the presence of such exotic behavior is now well-established experimentally, the fundamental mechanisms responsible for it are still debated. These outstanding questions motivate further detailed experimental investigations of quantized friction.

In this paper, we present a new methodology to measure friction in the boundary lubrication regime with a SFB. The principle consists in applying normal and lateral motions simultaneously - instead of alternatively- to the solid surfaces, allowing for a more precise, comprehensive and rapid determination of the friction-load relationship. First, we validate the method by measuring the

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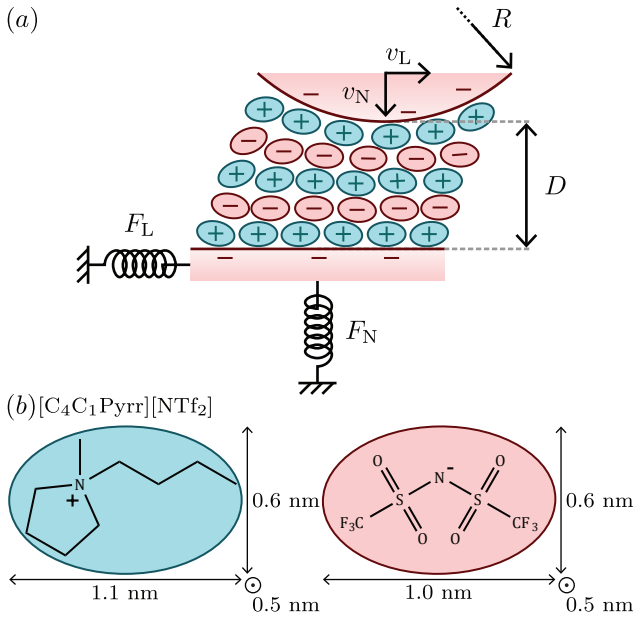


Fig. 1 (a) Schematic of the SFB experiment to measure interactions across a liquid (an ionic liquid in the present case) confined between two mica surfaces. The top surface is moved at normal velocity v_N and lateral velocity v_L , the bottom surface is mounted on springs to detect the normal force F_N and the lateral force F_L , the apical distance D and the radius of curvature R are measured by optical interferometry. (b) Chemical structure and sizes of $[C_4C_1Pyrr][NTf_2]$. Ion sizes are estimated from geometry, bond lengths and covalent radii, associated with the most stable configuration found by energy minimization (Chem3D 16.0, PerkinElmer Informatics).

phenomenon of quantized friction with an unprecedented resolution, for an ionic liquid confined between mica surfaces. This allows us to quantitatively explore the relationship between friction, load and contact area, as well as to elucidate the role of adhesion. Then, we show that traces of water induce an increase of the resistance of the layers to be squeezed-out, and an extension of the range of loads in which the liquid behaves as a superlubricant. There, we note a liquid-like friction behavior and observe that the kinetic friction force clearly depends on the shearing velocity, for a particular film composition in wet conditions. The dynamics is strongly non-linear, and is interpreted by means of different models of friction kinetics.

The paper is organised as follows. In section titled “Materials and Methods”, we summarize the general procedure to perform a SFB experiment, and we present the new methodology to measure friction. In section titled “Results and Discussion”, we describe and interpret the normal and lateral forces measurements performed across an ionic liquid, for different conditions of humidity and variable shearing velocities.

2 Materials and Methods

2.1 Surface Force Balance

The way the Surface Force Balance (SFB) works has been explained in details in previous publications^{19–22}. Here we briefly recall the principle of the instrument, illustrated in Figure 1(a), and the details particular to the present experiments.

Muscovite mica is cleaved to produce atomically-smooth facets of micrometric thickness and millimetric extension, that are back-silvered and glued onto glass (fused silica) cylindrical (radius $R \sim 1$ cm) lenses with an epoxy resin (EPON 1004, Shell Chemicals). Two surfaces are made with mica of the same thickness, and are arranged in a cross-cylinder geometry. First, calibrations are done in a dry atmosphere, which is achieved by inserting P_2O_5 , phosphorus pentoxide (Sigma-Aldrich, 99%), in the chamber and purging the chamber with N_2 , nitrogen, for about one hour prior to the calibrations. The undeformed mica thickness $e_{mica,0} = 7.431 \mu m$ is determined when the surfaces are in direct contact, following a procedure detailed in²³. Secondly, measurements are performed with an ionic liquid, $[C_4C_1Pyrr][NTf_2]$, 1-butyl-1-methylpyrrolidinium bis[(trifluoromethane)sulfonyl]imide (Iolitec, 99%), which chemical structure and sizes are indicated in Figure 1(b) (molar mass $M = 422.41$ g/mol, density $\rho = 1.405$ g/mL, refractive index $n = 1.422$ and dynamic viscosity $\eta = 74$ mPa.s at $25^\circ C$ ²⁴). This liquid is hygroscopic, and we use it either in dry or wet conditions. Dry conditions are achieved by drying the liquid in a Schlenck line at $60^\circ C$ and 5×10^{-3} mbar for ~ 10 hours and by inserting it in the chamber just after, which contains P_2O_5 and is purged again with N_2 for about one hour prior to the measurements. Such procedure is known to produce water content typically $\lesssim 100$ ppm^{11,15,25}. Wet conditions are achieved by simply letting the ionic liquid equilibrate with ambient atmosphere during several days before the experiment and by inserting it in the chamber, which does not contain any desiccant and is filled with ambient air. In this case, the water content corresponds to the thermodynamic equilibrium of the ionic liquid with ambient humidity ($\sim 50\%$).

White light is passed through the confined medium, interferes in this optical resonator, and is then directed towards a spectrometer and collected by a CCD camera. The analysis of the Fringes of Equal Chromatic Order (FECO) then allows one to deduce the apical distance D , the contact radius a (when the surfaces are flattened) and the radius of curvature R ²⁶. In a separate paper²³, we show that the mica can be significantly compressed and that D incorporates the variations of thicknesses of the mica layers and of the liquid film, i.e the materials separating the two silver mirrors. For small changes of D , it is not possible to disentangle the contributions coming from the mica (indentation $2e_{mica,0} - 2e_{mica} = 2\delta e_{mica}$, defined positive for compression and negative for dilatation) and the liquid (thickness D_{liquid}) with the FECO. In fact, we effectively measure the distance between the silver mirrors $D_{mirrors} = D_{liquid} + 2e_{mica}$, from which we subtract the undeformed mica thickness $2e_{mica,0}$ calibrated in dry atmosphere, to finally obtain:

$$D = D_{mirrors} - 2e_{mica,0} = D_{liquid} - 2\delta e_{mica} . \quad (1)$$

D is measured with a precision of 0.02 nm given by the standard deviation of the signal, and an accuracy of 1 nm due to light displacement when changing the contact spot²⁷. As the glue thickness is heterogeneous, the top mica surface has a different curvature than the bottom glass lens, which has to be measured every time the contact spot is changed. The radius of curvature R as-

sociated to each measurement is indicated in the figure caption,¹⁷⁹ and is known with an uncertainty of ~ 0.01 cm (mainly caused¹⁸⁰ by the fact that the separation profile between the surfaces is ob-¹⁸¹served up to a maximum scale ~ 50 nm $\ll R \sim 1$ cm). The contact¹⁸² radius a is measured with a precision of 0.03 μm given by the stan-¹⁸³dard deviation of the signal, and an accuracy of 1 μm due to the uncertainty on the value of R , following a procedure explained in details in²³.

The top surface can be moved normally with a stepper motor¹⁸⁴ (large displacement range ~ 10 μm , poor linearity, mechanical vibrations induced), and also normally and laterally thanks to a¹⁸⁵ sectored piezoelectric tube (small displacement range ~ 1 μm ,¹⁸⁶ good linearity, no measurable mechanical vibrations induced).¹⁸⁷ For a given run, the velocity v can be determined with a preci-¹⁸⁸sion of $\sim 1\%$. From run to run, this velocity can typically vary¹⁸⁹ by $\sim 10\%$ for the same control parameters, because of thermal¹⁹⁰ drifts. In the following, some graphs result from the superpo-¹⁹¹sition of several runs, that is why the indicated velocities have¹⁹² to be associated with an error bar of $\sim 10\%$. The bottom lens¹⁹³ is mounted on two springs: a normal (resp. lateral) spring of¹⁹⁴ constant $k_N = 2670 \pm 84$ N/m (resp. $k_L = 379 \pm 2$ N/m), which¹⁹⁵ is calibrated before the experiment by measuring its deflection¹⁹⁶ (resp. its resonance frequency) when adding different masses.¹⁹⁷ The normal force F_N is deduced from the temporal evolution of¹⁹⁸ the distance $D(t)$ when applying a constant normal velocity v_N ¹⁹⁹ to the top surface, using a procedure that takes into account the²⁰⁰ viscous force that is not negligible at large separations (detailed²⁰¹ in²²). The lateral force F_L is directly measured with a capaci-²⁰²tance probe when applying a constant lateral velocity v_L to the²⁰³ top surface, with a sensitivity of $\sim 10^{-3}$ mN. In comparison to²⁰⁴ previous studies performed in our group, the normal spring is²⁰⁵ here about 20 times stiffer, in order to apply larger loads (at fixed²⁰⁶ displacement range). Together with the stepper motor, it enables²⁰⁷ the identification of the first layer consisting of a monolayer of²⁰⁸ cations (labelled $i = 1$, as sketched in inset of Figure 2(a)), and²⁰⁹ the assessment of the resistance of the liquid to be squeeze-out²¹⁰ under very large pressures. Together with the sectored piezoelec-²¹¹tric tube, it enables one to reach the first layer of ions and so to²¹² explore the whole friction-load relationship with the new method-²¹³ology (procedure detailed in next subsection). This comes with a²¹⁴ price in terms of sensitivity limit for the normal force, $\sim 10^{-2}$ mN,²¹⁵ which does not allow the detection of the anomalously long-range²¹⁶ electrostatic force that has been observed with concentrated elec-²¹⁷trolytes^{11,22,25,28-34}.

The SFB is therefore a tool of choice to study the molecular²¹⁷ mechanisms of friction: the two atomically-smooth surfaces are in²¹⁸ contact on a single asperity (pure boundary lubrication regime),²¹⁹ the apical distance D is measured with a resolution better than²²⁰ the molecular scale, and the geometry can be characterized *in*-²²¹*situ* (radius of curvature R , contact radius a). In the literature, the²²² measured normal force F_N is generally rescaled by the radius of²²³ curvature R to compute an equivalent surface energy F_N/R , con-²²⁴sidering that mechanical deformations are negligible and that the²²⁵ Derjaguin approximation applies¹⁹. In the opposite case when²²⁶ the surfaces are strongly flattened, it is reasonable to assume that²²⁷ the total force F_N is mainly due to the interaction on the flattened²²⁸

region, and so to rescale it by the contact area πa^2 to compute the²²⁹ local pressure $F_N/(\pi a^2)$. In this study, we explore a broad range²³⁰ of situations from no deformation to strong deformations, that is²³¹ why we have chosen to simply use the force F without any rescal-²³²ing in the plots.

2.2 New Methodology for friction measurement

So far, friction measurements with the SFA/SFB or the AFM were²³³ performed by applying normal and lateral motions alternatively:²³⁴ the surfaces were approached/retracted at a given distance un-²³⁵der a given load, then the liquid was sheared, and so on^{13,15}.²³⁶ The principle of the new methodology consists in applying nor-²³⁷mal and lateral motions simultaneously to the surfaces: if the²³⁸ approach/retraction rate is much smaller than the shearing rate²³⁹ (typically $v_N \sim 1$ nm/s $\ll v_L \sim 100$ nm/s), the distance and the²⁴⁰ load can be considered as constant within one shearing period.²⁴¹ Such procedure has been already used by Hoth et al.¹⁰ with a²⁴² AFM but without analyzing the data to deduce the friction-load²⁴³ relationship, and by Crespo et al.³⁵ and us³⁶ with a SFA but not²⁴⁴ in the context of a structured liquid film.

Simply imposing a continuous instead of stepped motion in the²⁴⁵ normal direction potentially offers significant advantages. (i) The²⁴⁶ measurements are more precise (i.e. less scattered), because less²⁴⁷ time is left for the system to drift between points (inevitable long-²⁴⁸term drifts due to thermal expansion and creep of the mechanical²⁴⁹ parts), which is necessary to investigate quantitatively the rela-²⁵⁰tionship between friction, load and contact area, and to finely test²⁵¹ proposed models. (ii) The method allows for a more comprehen-²⁵²sive exploration of friction-load relationship, in particular in the²⁵³ vicinity of spring instabilities (jump-out on retraction, jump-in on²⁵⁴ approach), which is crucial to elucidate the role of adhesion on²⁵⁵ friction, and to better understand the film dynamics during the²⁵⁶ squeeze-out transition. (iii) The whole friction phenomenology²⁵⁷ can be acquired more rapidly (in typically ~ 1 h instead of ~ 10 h²⁵⁸ to probe all the layers of a structured film), which is convenient to²⁵⁹ efficiently probe various physico-chemical systems and to assess²⁶⁰ the reproducibility of the measurements.

However, a careful implementation of the technique is re-²⁶¹quired to avoid possible artefacts. First, the liquid structure it-²⁶²self can be affected by the shearing motion, a phenomenon that²⁶³ has been qualitatively interpreted as a combing of long-chain²⁶⁴ molecules³⁷⁻⁴². Secondly, the friction force can be reduced by²⁶⁵ mechanical vibrations (potentially induced by the simultaneous²⁶⁶ normal motion), which qualitatively act as an effective temper-²⁶⁷ature that helps to overcome the energy barrier associated with²⁶⁸ the molecules passing each other⁴³⁻⁴⁸. For the experiments re-²⁶⁹ported in this paper, we ruled out these artefacts by systematically²⁷⁰ checking that the normal force profile is the same with a zero and²⁷¹ non-zero lateral velocity (see Supplementary Figure 1), and that²⁷² the friction-load relationship is the same with a zero and non-zero²⁷³ normal velocity (see Supplementary Figure 2).

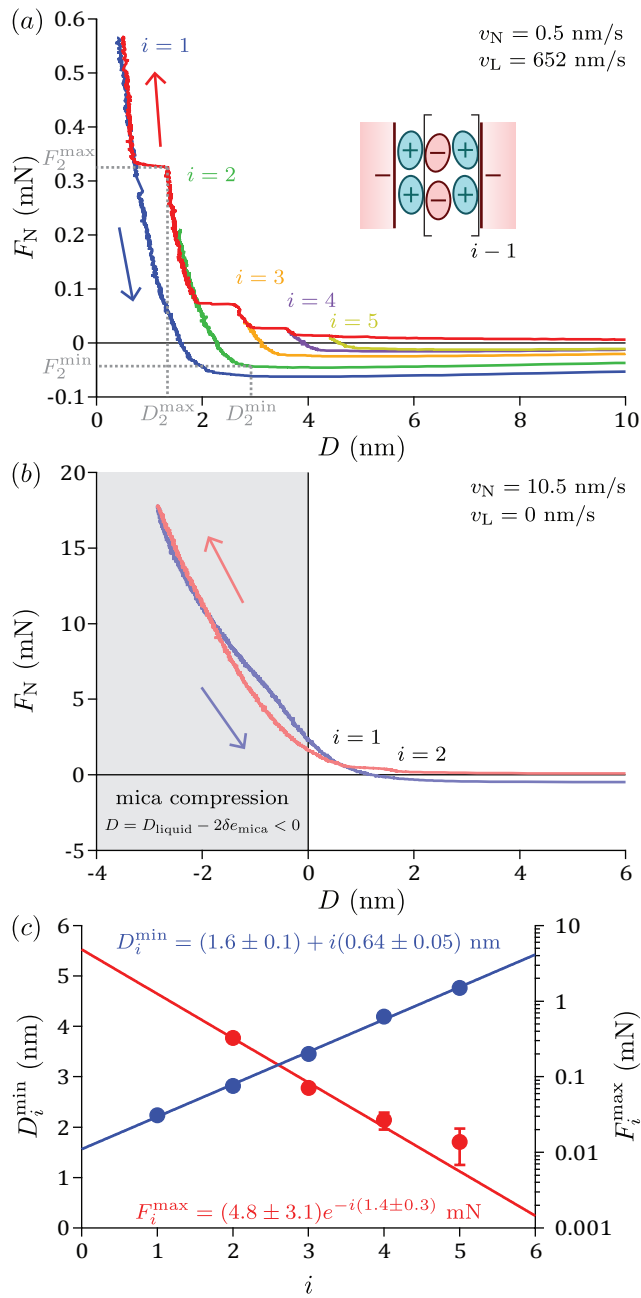


Fig. 2 Measurements for dry $[C_4C_1\text{Pyrr}][\text{NTf}_2]$ ($R = 0.92$ cm). (a) Normal force profile when moving the top surface with the piezoelectric tube at a normal velocity $v_N = 0.5$ nm/s and a lateral velocity $v_L = 652$ nm/s, showing structuring with 5 distinguishable layers labeled by i . For clarity, only the full approach is shown (in red), together with retractions from layers $i = 1$ (in blue), $i = 2$ (in green), $i = 3$ (in orange), $i = 4$ (in purple), $i = 5$ (in yellow). Inset: proposed structure of alternating layers of cations and anions. (b) Normal force profile when approaching (in faded red) or retracting (in faded blue) the top surface with the stepper motor at $v_N = 10.5$ nm/s. Negative distances D are reached at large loads, because the compression of mica exceeds the liquid thickness: $D = D_{\text{liquid}} - 2\delta e_{\text{mica}} < 0$. The curves measured on approach and retraction in layer $i = 1$ are not perfectly superimposed because of mechanical imperfections of the set-up (poor linearity of the stepper motor, tiny rotations of the solids, etc.). (c) Distances D_i^{min} at the points of minimum force, as a function of the layer index i , in lin-lin representation (in blue); forces F_i^{max} at the points of maximum force, as a function of the layer index i , in log-lin representation (in red). Straight lines are the corresponding linear and exponential fits (equations 2 and 3).

3 Results and Discussion

3.1 Normal force

We begin with presenting measurements of the normal interaction force. Figure 2(a) shows the normal force profile obtained when moving the top surface with the piezoelectric tube at a normal velocity $v_N = 0.5$ nm/s and a lateral velocity $v_L = 652$ nm/s across dry $[C_4C_1\text{Pyrr}][\text{NTf}_2]$. When the ionic liquid is confined at the nanoscale, a structural force profile is observed, with five distinguishable layers labeled by i . Such structural force has been observed many times with ionic liquids, and attributed to the ordering of ions in the film, with a structure consisting of alternating layers of anions and cations (as sketched in inset)⁴⁻¹². Because of the spring instability, the surfaces experience a jump-in on approach every time a layer is squeezed-out, and a jump-out on retraction from a given layer. Therefore several runs were in fact necessary for the most comprehensive exploration of the force profile. Supplementary Figure 3 shows the force profiles measured when approaching the top surface up to a given layer and retracting from this layer. From run to run, the whole force profile randomly shifts laterally by a fraction of nanometer. As the jump-in distances and the forces are reproducible, we consider that these shifts are non physical, but result from imperfections of the set-up like tiny rotations of the solids. That is why we have shifted manually the force profiles such that all the approaches are superimposed on the approach up to layer $i = 1$ (in red). Figure 2(a) shows the resulting force profile, with for clarity only the approach up to layer $i = 1$ (in red), and the retractions from the different layers ($i = 1$ in blue, $i = 2$ in green, $i = 3$ in orange, $i = 4$ in purple, $i = 5$ in yellow).

In a separate paper²³, we show that the oscillation due to local variations of liquid density in the confined film is in general convoluted with the mechanical response of the confining solids. For the system studied here, we found that (i) mica compression dominates liquid compression, i.e. the change of D within each layer is mainly due to the indentation of mica; (ii) contact mechanics is well described by the Derjaguin-Muller-Toporov (DMT) model^{19,49-52}, in particular the indentation of the solids is zero at the minimum force (jump-out point) and continuously increases up to the maximum force (jump-in point). For each layer i , we have measured the distance D_i^{min} at the point of minimum force (jump-out, as indicated in Figure 2(a) for $i = 2$), which does not include any influence of the mica compression. The variation of the distance D_i^{min} with the layer index i is shown in Figure 2(c), and exhibits a good linearity. It is fitted with the relation:

$$D_i^{\text{min}} = D_0^{\text{min}} + i\lambda^{\text{min}}, \quad (2)$$

where the slope $\lambda^{\text{min}} = 0.64 \pm 0.05$ nm represents the mean layer thickness and the intercept $D_0^{\text{min}} = 1.6 \pm 0.1$ nm corresponds to the position of the extrapolated layer $i = 0$. Another method consists in measuring the average jump-in distance, supposing an unchanged mica compression and a fast viscous relaxation during the squeeze-out events, and providing a consistent value of 0.64 ± 0.01 nm for the mean layer thickness. Interestingly, this value is smaller than the mean ion pair diameter of 0.79 nm (given

281 by $\left(\frac{M}{\rho N_A}\right)^{1/3}$ with M the molar mass of the ionic liquid, ρ its bulk
 282 density and N_A the Avogadro's number⁴), perhaps suggesting a
 283 denser packing of ions in confinement than in the bulk. However,
 284 our value is also smaller than the previous measurements per-
 285 formed with the same ionic liquid, reporting a mean layer thick-
 286 ness of 0.80 ± 0.04 nm between two mica surfaces with a SFB⁵³
 287 and 0.79 nm between a mica surface and a Si_3N_4 tip with an
 288 AFM⁵⁴. A possible explanation for this difference is the inher-
 289 ent contribution from viscosity to the force profile, in particular
 290 in vicinity to a spring instability. For the method using the dis-
 291 tances D_i^{\min} at the points of minimum force (giving a mean layer
 292 thickness of 0.64 ± 0.05 nm), viscosity tends to move the minima
 293 towards larger distances, even more than adhesion is larger (i.e.
 294 smaller layer index i). For the method using the jump-in distances
 295 (giving a mean layer thickness of 0.64 ± 0.01 nm), viscosity tends
 296 to reduce the size of the jumps. In both cases, viscous effects pos-
 297 sibly lead to an underestimation of the mean layer thickness. Pre-
 298 vious studies may be less affected by viscosity, as retractions were
 299 performed by slow steps in the SFB study⁵³ (with similar radius of
 300 curvature), and the radius of curvature was six orders of mag-
 301 nitude smaller in the AFM study⁵⁴ (with a velocity less than an
 302 order of magnitude larger). Therefore, applying a stepped motion
 303 is preferable to a continuous motion in order to accurately³³³
 304 determine the mean layer thickness. ³³⁴

305 An important aspect to interpret the structural force profiles is³³⁵
 306 to identify the composition of the layers. As the period is similar³³⁶
 307 to the mean ion pair diameter, it is qualitatively considered that³³⁷
 308 one squeeze-out event corresponds to the squeeze-out of an elec-³³⁸
 309 troneutral "slab" of one cation layer and one anion layer. In the³³⁹
 310 case of negatively charged surfaces, the first layer ($i = 1$) is then³⁴⁰
 311 assumed to be composed of a monolayer of cations (as sketched in³⁴¹
 312 inset of Figure 2(a)). Direct solid-solid contact is never reached,³⁴²
 313 because of the strong electrostatic attraction between the cations³⁴³
 314 and the negatively charged surfaces. For our experiment, one can³⁴⁴
 315 ask whether we really reach this single layer of cations within³⁴⁵
 316 the explored range of loads. The position of the first layer at³⁴⁶
 317 the point of minimum force (including no indentation of the sur-³⁴⁷
 318 faces) is $D_1^{\min} = 2.2 \pm 1.0$ nm, a bit larger than the cation sizes³⁴⁸
 319 (given in Figure 1(b)). However, the measurement of the absolute³⁴⁹
 320 distance D depends on many delicate steps (alignment of the³⁵⁰
 321 optics, calibration of the mica thickness in dry atmosphere, choice³⁵¹
 322 of a particular run to shift the force profiles laterally), and deduc-³⁵²
 323 ing the thickness of the monolayer from the cation sizes requires³⁵³
 324 to know their conformations, making accurate comparisons dif-³⁵⁴
 325 ficult. For each layer i , we have measured the force F_i^{\max} at the³⁵⁵
 326 point of maximum force (jump-in, as indicated in Figure 2(a) for³⁵⁶
 327 $i = 2$). The variation of the distance F_i^{\max} with the layer index i
 328 is shown in Figure 2(c) in log-lin representation, and exhibits a
 329 good linearity. It is fitted with the relation: ³⁵⁷

$$358 \quad F_i^{\max} = F_0^{\max} \exp\left(-i \frac{\lambda^{\max}}{\zeta^{\max}}\right), \quad (3) \quad 359 \quad 360 \quad 361$$

330 where the slope gives access to the ratio $\frac{\lambda^{\max}}{\zeta^{\max}} = 1.4 \pm 0.3$ of the³⁶²
 331 period of the oscillation on the decay length (i.e. typical dis-³⁶³
 332 tance from a surface on which the oscillations of local liquid den-³⁶⁴

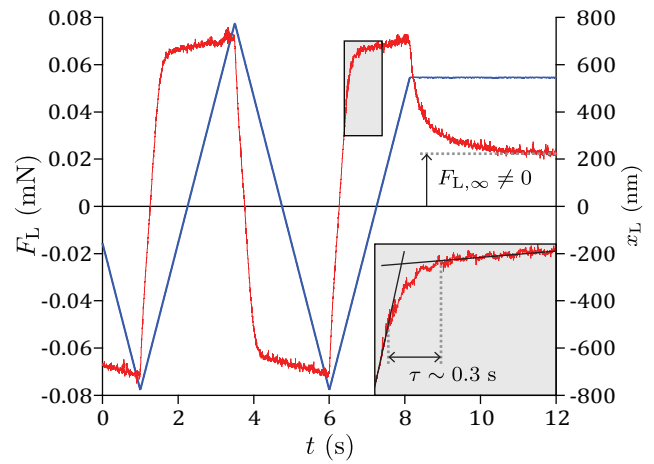


Fig. 3 Measurements for wet $[\text{C}_4\text{C}_1\text{Pyrr}][\text{NTf}_2]$ ($R = 1.45$ cm), at fixed load $F_N = 2.79$ mN, distance $D = -1.05$ nm (where $D = D_{\text{liquid}} - 2\delta e_{\text{mica}} < 0$) and contact radius $a = 12.86$ μm in layer $i = 2$. Temporal evolutions of the lateral displacement x_L and lateral force F_L , showing a liquid-like friction behavior. Inset: zoom on a part of the signal, delimited by a gray rectangle in the main graph. The tiny oscillation is due to the resonance of the mass-spring system at ~ 20 Hz.

sity are damped), and the intersect corresponds to the amplitude $F_0^{\max} = 4.8 \pm 3.1$ mN of the extrapolated layer $i = 0$. If we extrapolate this fit to the layer $i = 1$, it predicts that the next squeeze-out event would take place at a force $F_N = 1.3 \pm 0.6$ mN. Figure 2(b) shows the normal force profile obtained when approaching (in faded red) then retracting (in faded blue) the top surface with the stepper motor at a velocity $v_N = 10.5$ nm/s. We do not observe any additional jump-in for a force up to $F_N = 17.80$ mN. Thus, we think that the layer seen at the maximum load is indeed composed of a single layer of cations, and we identify it as $i = 1$. Note that negative distances D are reached at large loads, because the compression of mica exceeds the liquid thickness: $D = D_{\text{liquid}} - 2\delta e_{\text{mica}} < 0$ ²³.

On a practical point of view, we observe that applying a maximum load $F_N = 17.80$ mN does not lead to a complete squeeze-out of the confined liquid film, even if the confining solids are already strongly deformed: mica is compressed by a few nanometers and the surfaces are flattened on a contact radius $a = 21.61$ μm , corresponding to a pressure $\sim F_N / (\pi a^2) \sim 12$ MPa. The first layer, which consists of a monolayer of cations, is so strongly bounded to the oppositely charged mica surfaces that it is never squeezed-out. This is a very good property for a potential lubricant, because keeping the solid surfaces apart is an efficient way to prevent wear.

3.2 Lateral force

In this subsection, we identify the nature of the friction response, by analyzing the shape of the lateral force when the liquid film is sheared under constant conditions in the normal direction. Figure 3 shows the temporal evolutions of the lateral displacement x_L and lateral force F_L for wet $[\text{C}_4\text{C}_1\text{Pyrr}][\text{NTf}_2]$, at fixed load $F_N = 2.79$ mN, distance $D = -1.05$ nm (where $D = D_{\text{liquid}} - 2\delta e_{\text{mica}} < 0$) and contact radius $a = 12.86$ μm in layer $i = 2$. When

365 starting to apply a constant lateral velocity $v_L = 639$ nm/s, the^{e419}
 366 lateral force exhibits first a linear variation of slope $k_L \times v_L$, then^{e420}
 367 a relaxation with a typical timescale $\tau \sim 0.3$ s, there a smooth-^{e421}
 368 sliding creep of amplitude ~ 0.07 mN. When the direction of the^{e422}
 369 motion is reversed, the lateral force responds in a symmetric man-^{e423}
 370 ner with respect to the horizontal axis. If the lateral motion is^{e424}
 371 suddenly stopped, the lateral force exhibits a relaxation with a^{e425}
 372 similar timescale τ towards an amplitude $F_{L,\infty} \neq 0$.^{e426}

373 To interpret the observed friction behavior, we first recall the^{e427}
 374 response of a simple viscous liquid (bulk viscosity $\eta = 74$ mPa.s)^{e428}
 375 sheared between two planar surfaces (liquid thickness $D_{\text{liquid}} \sim$ ^{e429}
 376 1 nm, area $\mathcal{A} \sim \pi a^2 \sim 523$ μm^2), the top one being moved at a^{e430}
 377 lateral velocity $v_L = 639$ nm/s and the bottom one being attached^{e431}
 378 to a lateral spring of stiffness $k_L = 379$ N/m^{20,37}. For a charge-^{e432}
 379 less, Newtonian liquid in an incompressible and laminar flow be-^{e433}
 380 tween undeformable surfaces with a no-slip boundary condition,^{e434}
 381 the force opposing the motion is purely viscous and results from^{e435}
 382 the Couette flow in the gap. If the inertial term is negligible in the^{e436}
 383 equation of motion for the bottom surface, the temporal evolution^{e437}
 384 of the lateral force is given by the balance of the viscous force and^{e438}
 385 the restoring spring force. When starting to apply a constant lat-^{e439}
 386 eral velocity $v_L = 639$ nm/s, classical hydrodynamics predicts that^{e440}
 387 the lateral force exhibits first a linear variation of slope $k_L \times v_L$,^{e441}
 388 then an exponential relaxation with a timescale $\frac{\mathcal{A}\eta}{k_L D_{\text{liquid}}} \sim 10^{-4}$ s,^{e442}
 389 there a smooth-sliding plateau of amplitude $\frac{\mathcal{A}\eta v_L}{D_{\text{liquid}}} \sim 2 \cdot 10^{-5}$ mN.^{e443}
 390 When the direction of the motion is reversed, the lateral force re-^{e444}
 391 sponds in a symmetric manner with respect to the horizontal axis.^{e445}
 392 If the lateral motion is suddenly stopped, the lateral force exhibits^{e446}
 393 an exponential relaxation with the same timescale towards a zero^{e447}
 394 amplitude. Therefore, the phenomenology obtained in our ex-^{e448}
 395 periment is qualitatively similar to the one expected for a simple^{e449}
 396 viscous liquid, but with three important differences: (i) the forces^{e450}
 397 and timescales involved are more than three orders of magnitude^{e451}
 398 larger, (ii) there is creep instead of a plateau, (iii) a non-zero force^{e452}
 399 is sustained after stopping the motion. That is why the response^{e453}
 400 measured here is identified as a liquid-like friction behavior³⁷. In^{e454}
 401 past experiments with the same ionic liquid a friction response^{e455}
 402 with features typical of solid-like behavior has been observed. In^{e456}
 403 the Supplementary Material we discuss in detail the possible ori-^{e457}
 404 gin of this difference, and conclude that relative mica orientation^{e458}
 405 (twist angle) is most likely to be the underlying cause.^{e459}

406 3.3 Friction-Load relationship

407 In this subsection, we use the new methodology to explore the^{e463}
 408 friction-load relationship for dry $[\text{C}_4\text{C}_1\text{Pyrr}][\text{NTf}_2]$. Figure 4(a)^{e464}
 409 shows the temporal evolutions of the apical distance D and lat-^{e465}
 410 eral force F_L , when moving the top surface with the piezoelec-^{e466}
 411 tric tube at a normal velocity $v_N = 0.5$ nm/s and a lateral veloc-^{e467}
 412 ity $v_L = 652$ nm/s. The amplitude of the lateral force is below^{e468}
 413 the sensitivity limit of $\sim 10^{-3}$ mN before reaching layer $i = 2$,^{e469}
 414 then very small but discernible in this layer, and finally larger in^{e470}
 415 layer $i = 1$. In the inset of Figure 4(a) is plotted the variation^{e471}
 416 of the lateral force during the squeeze-out transition from layer^{e472}
 417 $i = 2$ to layer $i = 1$, a measurement that is possible with the new^{e473}
 418 methodology. The apical distance varies by ~ 0.64 nm in ~ 10 s,^{e474}

during which about four shearing cycles are performed. In this
 particular case, we are in fact probing the friction response of a
 transient film configuration, integrated over a time ~ 2.5 s. The
 amplitude of the lateral force increases continuously during the
 squeeze-out transition, showing that an heterogeneous film com-
 posed of a mixture of $i = 2$ and $i = 1$ areas gives a friction response
 that is intermediate between the responses of homogeneous $i = 2$
 or $i = 1$ films.

To analyze quantitatively the large amount of data generated
 by this new methodology, we have written a simple code. For each
 shearing period, it automatically extracts the average lateral force
 during the creep stage, identified as the kinetic friction force $F_{L,k}$,
 as well as the average load F_N , apical distance D and contact ra-
 dius a . We have done this for all the runs that were necessary for
 the most comprehensive exploration of the structural force pro-
 file (see for example Supplementary Figure 4, that shows the full
 temporal evolutions of the apical distance D and lateral force F_L
 during the approach up to layer $i = 1$ and the retraction from
 this layer). Figure 4(b) shows the kinetic friction force $F_{L,k}$ as a
 function of the load F_N , when moving the top surface with the
 piezoelectric tube at a normal velocity $v_N = 0.5$ nm/s and a lateral
 velocity $v_L = 652$ nm/s. The friction coefficient -evaluated as the
 slope in this friction-load representation- is clearly indexed by the
 number of ions composing the liquid film, which is the signature
 of the quantized friction phenomenon. This implies that friction
 is a multi-valued function of the load. In layer $i = 2$ (retraction
 branch in green), the friction coefficient is $\mu_2 = 0.0064 \pm 0.0006$,
 i.e. the film composed of two cations layers plus one anions layer
 behaves as a superlubricant (conventionally defined by a kinetic
 friction coefficient $< 0.01^2$). In layer $i = 1$ (retraction branch in
 blue), the friction coefficient is $\mu_1 = 0.210 \pm 0.003$ (almost two
 orders of magnitude larger!), i.e. the film composed of a mono-
 layer of cations behaves as a poor lubricant. The transition be-
 tween the two regimes happens at a load $F_N = 0.33$ mN, corre-
 sponding to a pressure $\sim F_N / (\pi a^2) \sim 2$ MPa (given a contact ra-
 dius $a = 6.45$ μm).

In comparison to previous studies, the new methodology pro-
 vides much less scattered data points. This allows us to quanti-
 tatively tests different empirical laws of friction, that we briefly
 recall in the following. For smooth adhering surfaces, it has
 been argued that the friction force $F_{L,k}$ should increase propor-
 tionally with the load F_N , i.e. $F_{L,k} = \mu (F_N - F^{\text{min}})$ (with μ the
 friction coefficient and F^{min} the adhesion force), due to the in-
 crease of the pressure in the film -the adhesion acting as an in-
 ternal pressure-⁵⁵⁻⁵⁸. It has also been suggested that the friction
 force $F_{L,k}$ should increase proportionally with the contact area \mathcal{A} ,
 i.e. $F_{L,k} = \sigma_c \mathcal{A}$ (with σ_c the critical shear stress), due to the in-
 crease of the surface on which shear stress is integrated^{52,59-63}.
 More generally, it has been proposed that friction comes from
 these two contributions, i.e. $F_{L,k} = \mu F_N + \sigma_c \mathcal{A}$ ⁶⁴. For the system
 studied here, we show in a separate paper²³ that contact me-
 chanics is well described by the Derjaguin-Muller-Toporov (DMT)
 model^{19,49-52}. The relation between the contact area and the
 load is $\mathcal{A} = \pi \left(\frac{R}{K}\right)^{2/3} (F_N - F^{\text{min}})^{2/3}$, with R the radius of curva-
 ture and $K = 16.7 \pm 0.5$ GPa the fitted effective elastic modulus
 -the adhesion again acting as an internal pressure-. Finally, we

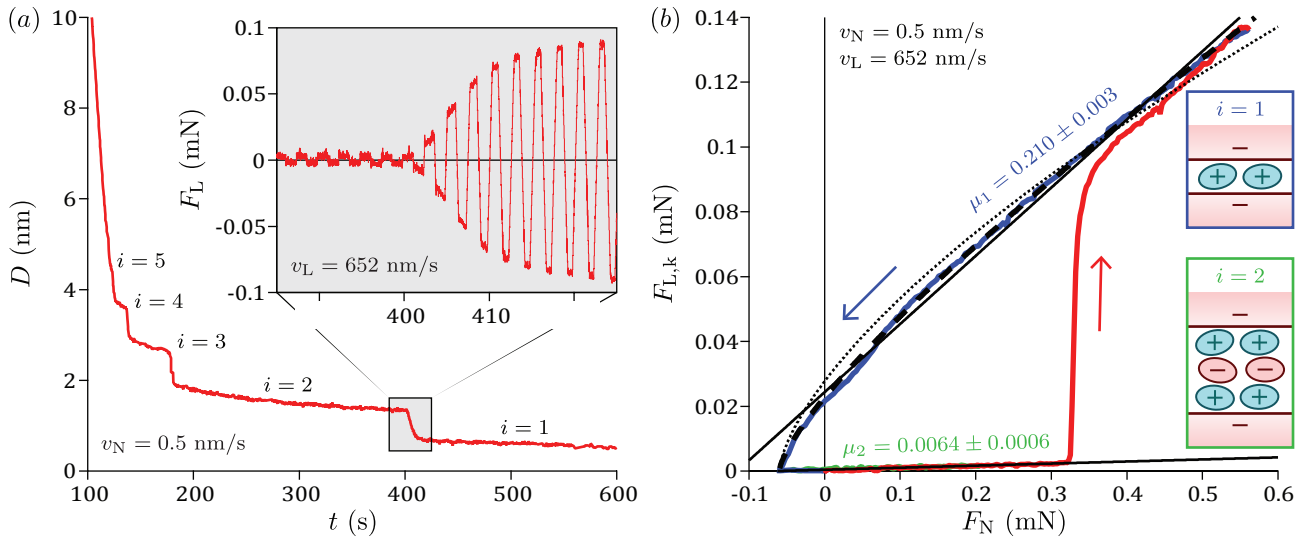


Fig. 4 Measurements for dry $[C_4C_1\text{Pyrr}][\text{NTf}_2]$ ($R = 0.92$ cm), when moving the top surface with the piezoelectric tube at a normal velocity $v_N = 0.5$ nm/s and a lateral velocity $v_L = 652$ nm/s. (a) Temporal evolution of the apical distance D on full approach. The inset shows the temporal evolution of the lateral force F_L during the squeeze-out transition from layer $i = 2$ to layer $i = 1$. (b) Kinetic friction $F_{L,k}$ as a function of load F_N on full approach (in red) then retraction from layer $i = 1$ (in blue). Friction is above the sensitivity limit for the layers $i = 1$ and $i = 2$ (proposed film structures in insets). Straight lines are fits with the left-hand term of equation 4, with $\{\mu_1 = 0.210 \pm 0.003, F_1^{\min} = -0.12 \pm 0.01$ mN} and $\{\mu_2 = 0.0064 \pm 0.0006, F_2^{\min} = -0.062 \pm 0.008$ mN}. The dotted line is a fit for layer $i = 1$ with the right-hand term of equation 4, with $\{\sigma_{c,1} = 857 \pm 6$ kPa, $F_1^{\min} = -0.06$ mN}. The dashed line is a fit for layer $i = 1$ with the whole equation 4, with $\{\mu_1 = 0.092 \pm 0.004, \sigma_{c,1} = 529 \pm 13$ kPa, $F_1^{\min} = -0.06$ mN}.

475 fit the friction-load relationship in layer $i = 1$ with the following
476 empirical law:

$$F_{L,k} = \mu_i \times (F_N - F_i^{\min}) + \sigma_{c,i} \times \pi \left(\frac{R}{K}\right)^{2/3} (F_N - F_i^{\min})^{2/3}, \quad (4)$$

477 where μ_i , $\sigma_{c,i}$ and F_i^{\min} are respectively the friction coefficient,
478 critical shear stress and adhesion force associated with layer i .
479 This equation gives $F_{L,k} = 0$ at $F_N = F_i^{\min}$, which is in agreement
480 with our systematic observation that the friction force goes to zero
481 at the jump-out point. If we suppose first that friction is purely
482 load-controlled and we fit with the left-hand term of equation 4
483 only (straight line in Figure 4(b)), we get $\{\mu_1 = 0.210 \pm 0.003,$
484 $F_1^{\min} = -0.12 \pm 0.01$ mN} (two free parameters). The fit is clearly
485 not satisfactory and overestimate the adhesion force (compared
486 to the directly measured $F_1^{\min} = -0.06$ mN), because it does not
487 describe the significant concave curvature that is observed experi-
488 mentally. If we suppose on the contrary that friction is purely con-
489 tact area-controlled and we fit with the right-hand term of equa-
490 tion 4 only (dotted line in Figure 4(b)), we get $\{\sigma_{c,1} = 857 \pm 6$ kPa,
491 $F_1^{\min} = -0.06$ mN} (one free parameter, the adhesion force being
492 fixed). The fit is much better in the vicinity of the adhesion min-
493 imum, but now overestimates the concavity of the curve. In fact,
494 the experimental data lie in between the two previous fits, and if
495 we fit with the full equation 4 (dashed line in Figure 4(b)), we ob-
496 tain a very good fit with $\{\mu_1 = 0.092 \pm 0.004, \sigma_{c,1} = 529 \pm 13$ kPa,
497 $F_1^{\min} = -0.06$ mN} (two free parameters, the adhesion force being
498 fixed).

499 To summarize, the measured friction-load relationship can be
500 described quantitatively with an empirical law, providing that two
501 additive contributions are included, the first proportional the load

502 and the second proportional to the contact area. In the previous
503 experimental studies of quantized friction across ionic liquids, the
504 friction-load relationship was found to be compatible with a linear
505 variation (i.e. a load-controlled friction), given the scattering
506 on the data points^{13,15}. It is thanks to the new methodology that
507 we are able to measure the friction-load relationship with an un-
508 precedented resolution, and to quantitatively test the different
509 empirical laws of friction. This is crucial not only for a better
510 understanding of the physics of friction in general, but also to ex-
511 tract quantities μ and σ_c that are intrinsic to the physico-chemical
512 system used and not affected by the particular geometry of the ex-
513 periment. Unfortunately, such high-resolution measurements are
514 not always possible, for example when friction is small or varies
515 slowly, or cannot be measured on a wide range of loads (like for
516 layer $i = 2$ in Figure 4(b)). However, we note that the differ-
517 ent fits in layer $i = 1$ provide friction coefficients of same order
518 of magnitude. That is why we have decided to fit linearly the
519 friction-load relationships measured with a low resolution, as a
520 semi-quantitative evaluation of the lubrication performances.

3.4 Effect of humidity

In this subsection, we present an experiment performed with wet
 $[C_4C_1\text{Pyrr}][\text{NTf}_2]$, illustrating the versatility and the efficiency of
the new methodology. The measurements, shown in Figure 5, are
qualitatively similar to the dry case, in the sense that we also ob-
serve a structural force profile, a liquid-like friction behavior, and
a quantized friction-load relationship. But important differences
emerge when comparing the results quantitatively.

Figures 5(a) and 5(b) show the normal force profile obtained
when moving the top surface normally with the piezoelectric
tube at $v_N = 0.5$ nm/s or with the stepper motor at $v_N = 3.4$ nm/s

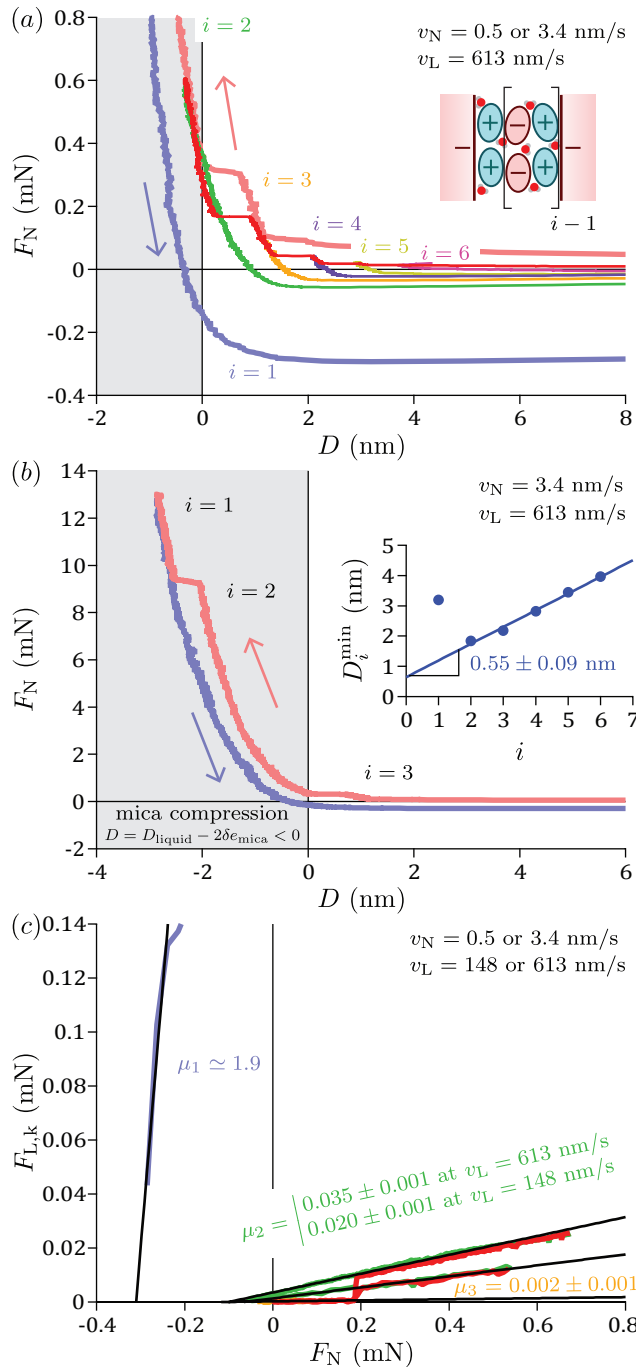


Fig. 5 Measurements for wet $[C_4C_1\text{Pyrr}][\text{NTf}_2]$ ($R = 1.45$ cm). (a) Normal force profile when moving the top surface normally with the piezoelectric tube at $v_N = 0.5$ nm/s or with the stepper motor at $v_N = 3.4$ nm/s (faded red and faded blue) and laterally at $v_L = 652$ nm/s, showing structuring with 6 distinguishable layers labeled by i . For clarity, only the two full approaches are shown (in red for the piezoelectric tube, in faded red for the stepper motor), together with retractions from layers $i = 1$ (in faded blue), $i = 2$ (in green), $i = 3$ (in orange), $i = 4$ (in purple), $i = 5$ (in yellow), $i = 6$ (in pink). Inset: proposed structure of alternating layers of cations and anions with water traces. (b) Normal force profile when approaching or retracting the top surface with the stepper motor at $v_N = 3.4$ nm/s. Inset: distances D_i^{\min} at the points of minimum force, as a function of the layer index i , and corresponding linear fit (equation 2). (c) Kinetic friction $F_{L,k}$ as a function of load F_N . Straight lines are fits with the left-hand term of equation 4, with $\{\mu_1 \sim 1.9, F_1^{\min} \sim -0.3$ mN $\}$, $\{\mu_2 = 0.035 \pm 0.001, F_2^{\min} = -0.101 \pm 0.004$ mN $\}$ and $\{\mu_3 = 0.002 \pm 0.001, F_3^{\min} = -0.12 \pm 0.03$ mN $\}$. Friction clearly depends on lateral velocity in layer $i = 2$, with $\{\mu_2 = 0.020 \pm 0.001, F_2^{\min} = -0.07 \pm 0.01$ mN $\}$ at $v_L = 148$ nm/s. As retraction from $i = 1$ has been performed at a relatively large velocity, μ_1 and F_1 are strongly affected by viscous effects, and μ_1 is estimated with only a few shearing periods.

and laterally at $v_L = 652$ nm/s. The wet ionic liquid gives rise to a structural force, with six distinguishable layers. The mean layer thickness is found to be 0.55 ± 0.09 nm by linearly fitting the variation of the distance D_i^{\min} with the layer index i (see inset of Figure 5(b)), or 0.68 ± 0.16 nm by measuring the average jump-in distance. These values are close to the ones obtained in dry conditions, suggesting a picture of minority water molecules sitting between ions without disrupting the film structure (as sketched in inset of Figure 5(a)). Such scenario is consistent with a previous SFB study using different mixtures of $[C_4C_1\text{Pyrr}][\text{NTf}_2]$ and propylene carbonate⁵³, which showed that the period of the structural force undergoes an abrupt transition at a threshold ion concentration, i.e. that the mean layer thickness is basically determined by the majority compound. But our observation is in contrast with previous SFB/SFA experiments using $[C_{10}C_1\text{Im}][\text{NTf}_2]$, 1-decyl-1-methylpyrrolidinium bis[(trifluoromethane)sulfonyl]imide¹⁷, or $[C_2C_1\text{Im}][\text{FAP}]$, 1-ethyl-3-methylimidazolium tris(pentafluoroethyl)trifluorophosphate²⁵, which reported on a dilation of the layers with humidity by respectively ~ 0.4 nm and ~ 0.2 nm (close to the water size estimated as $(\frac{M}{\rho N_A})^{1/3} = 0.31$ nm, with $M = 18.02$ g/mol the molar mass of water, $\rho = 1$ g/mL its bulk density and N_A the Avogadro's number), interpreted by a segregation of the water molecules towards the polar moieties of ions. In fact, molecular dynamics simulations have shown that the influence of humidity on layer thickness depends on the shape of the ions and on the surface charge, and that the addition of water may even induce a thinning of the layers, attributed to an increase of the dielectric constant and so a reduction of the electrostatic interactions between the ions⁶⁵. Returning to our measurements, we find that the amplitude of the structural force is much larger than in the dry case. Striking illustrations of this structural strengthening are the facts that a sixth layer can be detected, and that the squeeze-out transition from layer $i = 2$ to layer $i = 1$ happens at a very large load $F_N = 9.22$ mN (corresponding to a pressure $\sim F_N / (\pi a^2) \sim 8$ MPa, given a contact radius $a = 18.94$ μm), which can be reached within the range of the stepper motor only thanks to the choice of a large normal spring constant. In comparison with the dry case, this corresponds to a load ~ 28 times larger, or a pressure ~ 4 times larger. A similar behavior has been observed with SFA experiments using $[C_2C_1\text{Im}][\text{NTf}_2]$, 1-ethyl-3-methylimidazolium bis[(trifluoromethane)sulfonyl]imide¹¹. Qualitatively, such amplification of the ion density oscillations can be attributed to an enhanced dissociation of the potassium ions on the mica, leading to a larger surface charge.

Figure 5(c) shows the kinetic friction $F_{L,k}$ as a function of the load F_N for the wet ionic liquid. Again, the friction coefficient is indexed by the number of ions composing the liquid film, i.e friction is quantized. However, the lateral force is above the sensitivity limit for three layers, instead of two for the dry case. In layer $i = 3$ (retraction branch in orange), the friction coefficient is $\mu_1 = 0.002 \pm 0.001$, i.e. the film composed of three cations layers plus two anions layers behaves as an extremely good superlubricant. In layer $i = 2$ (retraction branch in green), the friction

587 coefficient is $\mu_2 = 0.035 \pm 0.001$, i.e. the film composed of two⁶⁴¹
588 cations layers plus one anions layer is almost a superlubricant.⁶⁴²
589 For layer $i = 1$ (retraction branch in faded blue), the friction co-⁶⁴³
590 efficient is $\mu_3 \sim 1.9$, i.e. the film composed of a monolayer of⁶⁴⁴
591 cations is a poor lubricant. Note that retraction from layer $i = 1$ ⁶⁴⁵
592 has been performed at a relatively large velocity, so the value of⁶⁴⁶
593 μ_1 is estimated with only a few shearing periods. Supplementary⁶⁴⁷
594 Figure 2 shows the friction-load relationship that has been mea-⁶⁴⁸
595 sured in a larger range of loads for layer $i = 2$, by approaching the⁶⁴⁹
596 surfaces by discrete steps with the stepper motor. Similarly to the⁶⁵⁰
597 dry case, a good fit can be achieved with equation 4, providing⁶⁵¹
598 that the two contributions are included, the first proportional to⁶⁵²
599 the load and the second proportional to the contact area (with⁶⁵³
600 $\{\mu_2 = 0.0129 \pm 0.003, \sigma_{c,2} = 56 \pm 2 \text{ kPa}, F_2^{\min} = -0.06 \text{ mN}\}$).⁶⁵⁴

601 Overall, humidity is found to strongly increase the resistance of⁶⁵⁵
602 the layers to be squeezed-out, without changing significantly their⁶⁵⁶
603 corresponding thicknesses and friction coefficients. Consequently,
604 it leads to an extension of the range of loads in which the liquid
605 behaves as a superlubricant. Such beneficial effect of water on
606 the lubricating performances is extremely interesting for applica-⁶⁵⁷
607 tions, given that ionic liquids are hygroscopic and that lubricated⁶⁵⁸
608 systems are never perfectly insulated from ambient moisture.⁶⁵⁹

609 3.5 Kinetics aspects

610 In this subsection, we consider the influence of the shearing ve-⁶⁶³
611 locity on the friction force. Supplementary Figure 5 shows the⁶⁶⁴
612 friction-load relationships measured in dry conditions at $v_L =$ ⁶⁶⁵
613 652 nm/s and $v_L = 67.9 \text{ nm/s}$. No clear trend is found within⁶⁶⁶
614 the experimental errors, whether in layer $i = 1$ or in layer $i = 2$.⁶⁶⁷
615 Figure 5(c) shows the friction-load relationships measured in wet⁶⁶⁸
616 conditions at $v_L = 613 \text{ nm/s}$ and $v_L = 148 \text{ nm/s}$. In layer $i = 3$, no⁶⁶⁹
617 clear trend is found within the experimental errors, and layer $i = 1$ ⁶⁷⁰
618 was explored at only one shearing velocity. In layer $i = 2$, how-⁶⁷¹
619 ever, the friction clearly depends on the shearing velocity. More⁶⁷²
620 precisely, the kinetic friction force goes to zero at the same adhe-⁶⁷³
621 sion minimum in both cases, but with a friction coefficient that⁶⁷⁴
622 is larger with the largest shearing velocity. These observations⁶⁷⁵
623 are consistent with previous SFB experiments performed with the⁶⁷⁶
624 same ionic liquid in our group, showing that in dry conditions⁶⁷⁷
625 the kinetic friction is independent of the shearing velocity in the⁶⁷⁸
626 range $v_L \in [200; 1000] \text{ nm/s}$, whatever the layer considered⁶⁷⁹¹⁵. Our
627 findings are also comparable with previous colloidal probe AFM
628 experiments performed with protic ionic liquids (ethylammonium
629 nitrate (EAN), propylammonium nitrate (PAN), ethylammonium
630 formate (EAF), etc.) between a silica sphere ($R \sim 10 \mu\text{m}$) and a⁶⁸⁰
631 mica surface, reporting on an increase of the friction coefficient⁶⁸¹
632 with the shearing velocity in the range $v_L \in [5000; 40000] \text{ nm/s}$, for⁶⁸²
633 some particular film compositions^{13,14,16}. However, it is not clear⁶⁸³
634 why a dependence of the shearing velocity on the friction force is⁶⁸⁴
635 found or not, depending on the physico-chemical system and the⁶⁸⁵
636 layer considered.⁶⁸⁶

637 To investigate this dynamics quantitatively, we have sheared⁶⁸⁷
638 the liquid under constant conditions in the normal direction,⁶⁸⁸
639 exploring two decades of lateral velocities. Figure 6(a) shows⁶⁸⁹
640 the lateral force F_L as a function of the lateral displacement x_L ⁶⁹⁰

when shearing wet $[\text{C}_4\text{C}_1\text{Pyrr}][\text{NTf}_2]$ at different velocities $v_L \in$
 $\{32; 128; 639; 1918; 3197\} \text{ nm/s}$ (with same displacement range),
at fixed load $F_N = 2.79 \text{ mN}$, distance $D = -1.05 \text{ nm}$ (where
 $D = D_{\text{liquid}} - 2\delta e_{\text{mica}} < 0$) and contact radius $a = 12.86 \mu\text{m}$ in
layer $i = 2$. A liquid-like friction behavior is obtained for all
the friction loops, but with a kinetic friction force that increases
monotonically with the the shearing velocity. Finally, Figure 6(b)
shows the kinetic friction force $F_{L,k}$ as a function of the lateral ve-
locity v_L , in lin-log representation (Supplementary Figures 6(a)
and 6(b) show the same data, respectively in lin-lin and log-log
representations). The dynamics is strongly non-linear, and is in-
terpreted with different models of friction kinetics in the follow-
ing.

In friction experiments between smooth surfaces, dynamics is
generally found to be thermally-activated, i.e. obeying an Arrhe-
nius law of the form:

$$F = F_0 \ln \frac{v}{v_0}. \quad (5)$$

Qualitatively, such thermally-activated dynamics is associated
with the picture of molecules that must overcome energy barriers
in order to pass each other, with the external force inducing
a potential bias and with the temperature allowing for the cross-
ing of non-zero barriers. It has been observed for dry friction
(between Langmuir-Blodgett films with a SFA⁶⁶, between a NaCl
surface and a silicon tip with an AFM⁶⁷), as well as for lubricated
friction in the boundary regime (between mica surfaces across
apolar liquids or aqueous electrolytes with a SFA^{68,69}, between
mica surface and silicon colloid across protic ionic liquids with a
colloidal probe AFM^{13,14,16}). We have fitted our data with equa-
tion 5 (red curve in Figure 6(b)), giving $\{F_0 = (23 \pm 4) \cdot 10^{-3} \text{ mN},$
 $v_0 = 18 \pm 10 \text{ nm/s}\}$. Clearly, an Arrhenius law does not provide
a satisfactory fit of the dynamics measured over two decades
of velocities in the range $v_L \in [30; 3000] \text{ nm/s}$, which exhibits
a significant curvature in a lin-log representation. This is in
contrast with the previous colloidal probe AFM studies of fric-
tion across ionic liquids^{13,14,16}, showing a dynamics compati-
ble with an Arrhenius law over one decade of velocities in the
range $v_L \in [5000; 40000] \text{ nm/s}$. A modified Arrhenius law has been
proposed, in the case where the potential bias induced by the ex-
ternal force is so large that the energy barrier almost disappears
(i.e. at the vicinity of the spinodal)⁷⁰⁻⁷²:

$$F = F_c - \Delta F \left(\ln \frac{v_c}{v} \right)^{2/3}. \quad (6)$$

Our data have been fitted with this model (green curve in Fig-
ure 6(b)), giving $\{F_c = 0.13 \pm 0.02 \text{ mN}, v_c = (3.4 \pm 1.5) \cdot 10^3 \text{ nm/s},$
 $\Delta F = (36 \pm 7) \cdot 10^{-3} \text{ mN}\}$. It better reproduces the curvature of
the data, and predicts that the spinodal transition is reached just
at the top of the explored range of lateral velocities. However,
several experimental, numerical and theoretical works in the lit-
erature propose to describe the lubricated friction dynamics by
means of a shear-thinning rheology with an effective viscosity that
decreases as $v_L^{-2/3}$, or equivalently a friction force that increases
as $v_L^{1/3}$ ⁷³⁻⁷⁸. This can be written as an empirical power-law of
the form:

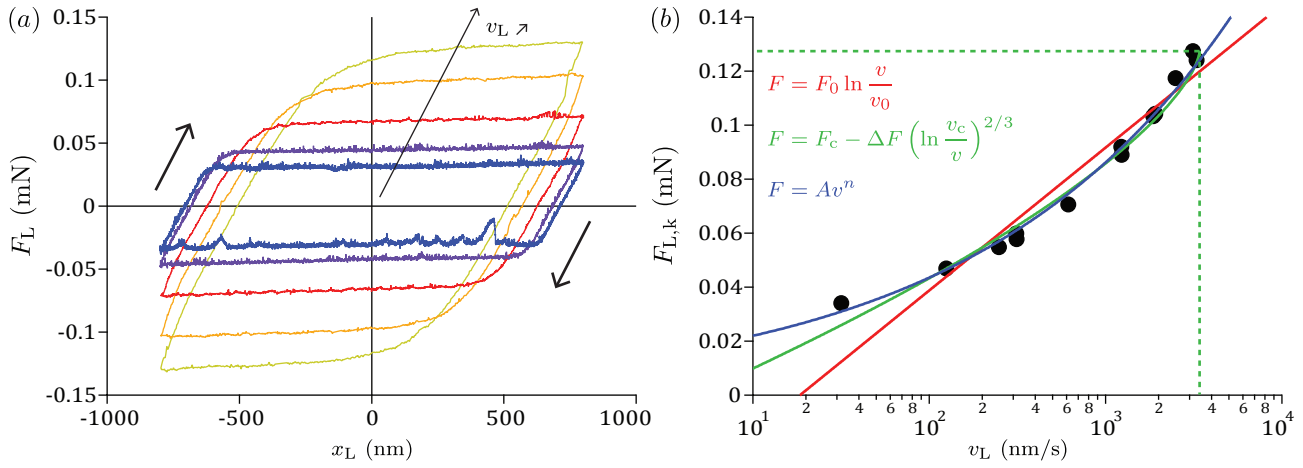


Fig. 6 Measurements for wet $[\text{C}_4\text{C}_1\text{Pyrr}][\text{NTf}_2]$ ($R = 1.45$ cm), at fixed load $F_N = 2.79$ mN, distance $D = -1.05$ nm (where $D = D_{\text{liquid}} - 2\delta e_{\text{mica}} < 0$) and contact radius $a = 12.86$ μm in layer $i = 2$. (a) Lateral force F_L as a function of lateral displacement x_L , for different lateral velocities $v_L \in \{32; 128; 639; 1918; 3197\}$ nm/s respectively in blue, purple, red, orange and yellow. The bumps on the signals, particularly visible for the blue curve, are due to external vibrations that are not totally suppressed by the damping elements of the SFB. (b) Kinetic friction $F_{L,k}$ as a function of lateral velocity v_L , in lin-log representation. The red curve is a fit with equation 5 giving $\{F_0 = (23 \pm 4) \cdot 10^{-3}$ mN, $v_0 = 18 \pm 10$ nm/s). The green curve is a fit with equation 6 giving $\{F_c = 0.13 \pm 0.02$ mN, $v_c = (3.4 \pm 1.5) \cdot 10^3$ nm/s, $\Delta F = (36 \pm 7) \cdot 10^{-3}$ mN}. The blue curve is a fit with equation 7 giving $n = 0.30 \pm 0.02$.

$$F = Av^n,$$

(7)

listed below, that would require dedicated experimental investigations.

This model also fits reasonably our data (blue curve in Figure 6(b)), with an exponent $n = 0.30 \pm 0.02$ close to the reported value of $1/3$. Therefore, these measurements of the friction force over two decades of shearing velocities allow us to unambiguously reject a description of the friction kinetics by an Arrhenius law, but not to discriminate between the modified Arrhenius law and the empirical power-law.

4 Conclusions

In this paper, we have presented proof-of-concept experiments for a new methodology to measure friction in the boundary lubrication regime with a SFB. By applying simultaneous normal and lateral motions to the surfaces, the friction-load relationship can be measured more precisely, comprehensively and rapidly. The quality achieved opens the way to more quantitative investigations to relate friction, load, contact area, adhesion and shearing velocity, while the efficiency and the versatility of the method allow for efficient probing of various physico-chemical systems. Using ionic liquids as a proof-of-concept, we have measured the phenomenon of quantized friction with an unprecedented resolution. Contrary to the existing studies in the area, we have found (i) a liquid-like friction behavior; (ii) a variation of the kinetic friction force with the applied load that is not simply linear, but can be quantitatively described by two additive contributions proportional to the load and to the contact area; (iii) a dynamics over two decades of shearing velocities that does not obey a simple Arrhenius law, appealing for more sophisticated models of friction kinetics. Furthermore, we have observed that humidity can improve the lubrication performances of ionic liquid, by increasing the resistance of the layers to be squeezed-out and so extending the range of loads in which the liquid behaves as a superlubricant.

The results presented in this study raise a number of questions,

- **Does the increase of mica surface charge with humidity explain the amplification of the ion density oscillation?** This aspect could be specifically addressed by performing measurements with conductive surfaces, which surface potential can be controlled externally.
- **Can the relative orientation of the mica surfaces induce a transition from a solid-like to a liquid-like friction behavior also for ionic liquids?** This hypothesis could be verified by measuring the friction behavior while varying systematically the twist angle between the mica surfaces.
- **Should friction kinetics across ionic liquids be described by a thermally-activated process, or by a shear-thinning rheology, or another approach?** The different models could be discriminated by exploring the dynamics over a wider range of shearing velocities to identify or not a spinodal transition, and by performing friction measurements at different temperatures.
- **Is the variability on the lateral force measurement when changing the contact spot correlated to the presence of large domains of uniform orientation on the surfaces?** This scenario could be tested by combining X-ray scattering and friction measurements in a modified SFA/SFB.

Conflicts of interest

There are no conflicts to declare.

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