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# Enhanced Sommerfeld coefficient near the quantum critical point in $\text{YbMn}_6\text{Ge}_{6-x}\text{Sn}_x$

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## Abstract

We investigate the  $\text{YbMn}_6\text{Ge}_{6-x}\text{Sn}_x$  alloys ( $4.00 \leq x \leq 5.55$ ) by means of specific heat measurements in the temperature range 1.9 to 200 K. For  $x$  near  $\sim 4.0$ , the Sommerfeld coefficient  $\gamma$  is close to that of a Lu-based counterpart ( $\gamma \sim 40 \text{ mJ.mole}^{-1}.\text{K}^{-2}$ ). The  $\gamma$  coefficient increases upon Sn for Ge substitution, enters the heavy fermion regime and peaks ( $\gamma \sim 210 \text{ mJ.mole}^{-1}.\text{K}^{-2}$ ) in the vicinity of the Yb magnetic instability ( $x_c \sim 5.23$ ), before diminishing upon further Sn content increase. The enhanced  $\gamma$  values near  $x_c$  agree with the close proximity of a quantum critical point previously inferred from electronic spectroscopy experiments.

*Keywords:* A. Yb-based intermetallics D. heavy fermion quantum criticality E. Specific heat

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## 1. Introduction

Strongly correlated electrons materials are intensively studied since they offer the possibility of stabilizing new and exotic ground states [1]. Among the numerous correlated materials families (high- $T_c$  cuprates and other oxides, heavy fermion systems, low-dimension materials ...),  $4f$  electron heavy fermion systems have the advantage to involve small energy scales that can be easily tuned by control parameters such as external pressure, magnetic field or chemical composition [2].

In the vast majority of  $4f$  heavy fermion compounds and alloys studied so far, the anomalous rare-earth (mainly Ce or Yb) is alloyed with non-magnetic

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elements [2, 3]. The ground state then results from the competition between two interactions that depend differently on the hybridization between the localized  $4f$  states and the conduction electrons [4]: the Kondo effect, which tends to demagnetize the system, and the Ruderman-Kittel-Kasuya-Yosida (RKKY) interaction that promotes magnetic order. Depending on the strength of the hybridization, various ground states can be realized (magnetically ordered, heavy fermion, intermediate valent...). When the RKKY and Kondo interactions are of comparable magnitude, the magnetic ordering is suppressed to absolute zero temperature, which corresponds to a quantum critical point (QCP) [5]. The quantum fluctuations at the QCP yields profound modifications in metal properties, even at finite temperature, such as non-Fermi-liquid behavior or unconventional superconductivity.

When Yb is alloyed with non-magnetic elements, the QCP occurs in most cases for nearly trivalent Yb (one of the most prominent counter-examples being  $\beta$ -YbAlB<sub>4</sub> [6, 7]) and the quantum critical effects are perceived only at low temperatures [1, 2, 3].

A few years ago, we identified and started to investigate a system where intermediate valent Yb and a magnetized  $3d$  sublattice coexist, namely YbMn<sub>6</sub>Ge<sub>6- $x$</sub> Sn <sub>$x$</sub> , using magnetization, neutron diffraction and spectroscopy experiments [8, 9, 10, 11, 12]. These hexagonal phases ( $P6/mmm$ , HfFe<sub>6</sub>Ge<sub>6</sub>-type) comprise a single site for the Mn atoms ( $6i$ ) and Yb atoms ( $1b$ ) and three sites for the  $p$  element ( $2c$ ,  $2d$  and  $2e$ ). In this system, the Yb valence decreases (i.e. the  $4f$  conduction electron hybridization is enhanced) through chemical pressure reduction upon Sn for Ge substitution [9, 10, 12]. Yb is (almost) trivalent in YbMn<sub>6</sub>Ge<sub>6</sub> [10], while its valency is  $\nu \sim 2.59$  in YbMn<sub>6</sub>Sn<sub>6</sub> [12]. The low-temperature Yb magnetic order disappears for  $x > 5.23$  when Yb is in the intermediate valence regime ( $\nu \sim 2.77$ ) [12]. The Mn sublattice magnetically orders at or above room-temperature and its behavior depends on the  $R$  = Yb valence [8, 11], a well-documented behavior in the wide  $RMn_6X_6$  family ( $X$  = Ge, Sn) [13, 14, 15]. In the Ge-rich YbMn<sub>6</sub>Ge<sub>6- $x$</sub> Sn <sub>$x$</sub>  alloys, the Mn sublattice is basically antiferromagnetic. Upon reducing the Yb valence through Sn for Ge substitution, a ferromagnetic region develops in the ( $x$ , T) phase diagram and the Mn sublattice is ferromagnetic over the whole ordered temperature range for  $x > 4.65$  (see Fig. 4 of Ref. [11]).

Besides the Yb magnetic instability occurring at strong hybridization mentioned above, the YbMn<sub>6</sub>Ge<sub>6- $x$</sub> Sn <sub>$x$</sub>  alloys exhibit several other singular Yb behaviors which have been ascribed to the magnitude of the Mn-Yb exchange interaction [9, 11, 12], quite stronger than the usual Yb-Yb RKKY

interaction [16]. The Yb valence tends to increase upon cooling [9] at odds to the usual behavior [17]. The Yb magnetic ordering of Yb reaches the record value  $T_{Yb} \sim 125$  K for  $x = 4.65$  while, to the best of our knowledge, the highest Yb magnetic transition temperature otherwise observed is 32 K in  $\beta$ -YbAlB<sub>4</sub> under the external pressure of 8 GPa [7]. Finally, the peak in the composition dependence of the Yb valence (at 300 and 5 K) and XMCD signal (at 5 K) near  $x_c \sim 5.23$  has been analyzed as possible signatures of  $4f$  quantum criticality [12]. Thus,  $\beta$ -YbAlB<sub>4</sub> [7] and YbMn<sub>6</sub>Ge<sub>6- $x$</sub> Sn <sub>$x$</sub>  share the common feature of having a QCP in the intermediate valence regime ( $\nu \sim 2.75$  [6] *vs.*  $\nu \sim 2.77$  [12], respectively).

None of these works on YbMn<sub>6</sub>Ge<sub>6- $x$</sub> Sn <sub>$x$</sub>  are based on thermodynamic or transport measurements, valuable -if not indispensable- tools for studying heavy fermion behaviors and  $4f$  electron quantum criticality. To partially fill this gap, we investigate here the YbMn<sub>6</sub>Ge<sub>6- $x$</sub> Sn <sub>$x$</sub>  alloys (with  $4.00 \leq x \leq 5.55$ ) using specific heat measurements with the motivation of a better understanding of the  $4f$  electrons behavior in this series.

## 2. Experimental details

Most of the YbMn<sub>6</sub>Ge<sub>6- $x$</sub> Sn <sub>$x$</sub>  used in this study are from the same batches as those employed previously Refs. [11, 12]. A few supplementary Yb-based polycrystalline alloys were prepared as described in reference [8]. Two representative X-ray diffraction patterns (D8 Advance, Bruker,  $\lambda = 1.54056$  Å) are shown in figure 1. A single crystal with composition YbMn<sub>6</sub>Ge<sub>1.91</sub>Sn<sub>4.09</sub>, as determined by X-ray diffraction, was grown in Sn flux [18, 19]. The elements were placed in a quartz tube, in the ratio Yb:Mn:Ge:Sn=1:6:0.8:30, which was sealed under pure Ar atmosphere (0.25 atm.). The materials were heated to 1000 °C and kept there for four hours. The temperature was then reduced to 600 °C at a rate of 6 °C h<sup>-1</sup>. The excess Sn flux was removed by centrifugation. This yielded single crystals in the form of hexagonal prisms with typical volume of  $\sim 1$  mm<sup>3</sup>. Note that, using this protocol, we did not yet succeed in growing single crystals with composition close to that of the Yb magnetic instability ( $x_c \sim 5.23$ ) and only crystals with  $x$  close to 4 have been obtained even with widely varying the Ge content of the flux.

Specific heat measurements  $C_p(T)$  were performed by a relaxation method using a Physical Properties Measurements System (PPMS, Quantum Design) [20, 21]. Most of the samples were investigated from 200 K down to 1.9 K while some of them were investigated only below 20 K. For the single crystal

( $x = 4.09$ ), the data presented here were obtained with one hexagonal face in contact with the sample platform. Data obtained in the perpendicular orientation are identical.

A Lu-based polycrystalline sample with composition  $\text{LuMn}_6\text{Ga}_{0.8}\text{Sn}_{5.2}$  was prepared in similar conditions to the Yb-based ones in order to allow for comparison of their Sommerfeld coefficients  $\gamma$ . In this compound, the Mn sublattice is ferromagnetic over the whole ordered temperature range ( $T_C \sim 340$  K) [22, 23], as in  $\text{YbMn}_6\text{Ge}_{6-x}\text{Sn}_x$  with  $x > 4.65$ , while  $\text{LuMn}_6(\text{Ge},\text{Sn})_6$  alloys are antiferromagnets with a possible commensurate - incommensurate transition [24] that might yield parasitic anomalies in the  $C_p(T)$  data.

### 3. Results and discussion

The temperature variation of the specific heat of some  $\text{YbMn}_6\text{Ge}_{6-x}\text{Sn}_x$  alloys is shown in figure 2. Two specific heat anomalies are observed for  $x \leq 4.45$ . The one near  $\sim 120$  K that weakly shifts towards lower temperature upon increasing  $x$ . The second one, at lower temperature, that goes to higher temperature and reduces in intensity upon increasing  $x$ . The high temperature peak is associated with changes in the Mn spins arrangement, from helimagnetic to skewed spiral upon cooling, previously detected by neutron diffraction [8, 11]. It is no longer observed in richer Sn alloys since the Mn sublattice is then ferromagnetic over the whole ordered temperature range. The low-temperature specific heat anomaly corresponds to the the magnetic ordering of Yb. The Yb magnetic ordering temperature is known to increase with  $x$  up to  $T_{Yb} \sim 125$  K for  $x = 4.65$ , before decreasing down to its suppression for  $x \sim 5.23$  [11, 12]. However, no corresponding specific heat anomaly is seen for  $x > 4.65$ , likely because the magnetic entropy associated with the then strongly reduced Yb magnetic moment ( $< 0.30 \mu_B$  [11]) is too low.

The electronic specific heat (Sommerfeld) coefficient,  $\gamma$ , and the Debye temperature,  $\Theta_D$ , were obtained by least-squares fitting of the low temperature  $C_p/T$  vs.  $T^2$  data (figure 3). The  $C_p/T$  curve of all polycrystalline samples comprises a peak near 2 K that is absent in the heat capacity data of the single crystal ( $x = 4.09$ ), as shown in the inset of figure 3. This peak is unambiguously due small amounts of  $\text{Yb}_2\text{O}_3$  which orders antiferromagnetically at  $T_N \sim 2.3$  K [25]. The  $\text{Yb}_2\text{O}_3$  impurity is often present in Yb-based intermetallic polycrystalline samples [26, 27, 28] and, from our own experience, can hardly be avoided in the  $\text{YbMn}_6\text{Ge}_{6-x}\text{Sn}_x$  series. Attempts to subtract the  $\text{Yb}_2\text{O}_3$  contribution to the total specific heat using  $C_p$  data

of commercial oxide were not satisfactory, the peak shape and exact temperature maximum being different to those of commercial  $\text{Yb}_2\text{O}_3$  and somewhat sample dependent. We therefore restricted the linear regression of the data, in the form  $C_p/T = \gamma + \beta T^2$ , to temperatures higher than 7 K where the magnetic contribution of the oxide is negligible.

The fitted slope  $\beta$  allows calculating the Debye temperature using the relationship [29]:

$$\Theta_D^3 = \frac{12\pi^4 n R}{5\beta}$$

where  $R$  is the gas constant and  $n$  the number of atoms in a formula unit (here  $n = 13$ ). The fits results in  $\Theta_D$  values decreasing slightly and steadily with increasing Sn content from  $\Theta_D \sim 260$  K for  $x = 4$  down to  $\Theta_D \sim 240$  K for  $x = 5.55$  (see inset of figure 4). That can be explained by a weakening of the chemical bonds in the Mn-[Yb,Sn/Ge(2d)]-Mn slab upon Sn for Ge substitution. In the investigated composition range ( $4 < x < 6$ ), the  $2c$  and  $2e$  metalloid sites are full of Sn atoms and the Sn for Ge substitution occurs only on the  $2d$  site [8, 11]. The replacement of Ge by larger Sn results in a weakening of the Mn-metalloid chemical bonds and, in addition, the concomitant reduction of  $5d$  electrons count on Yb - associated with the lowering of the Yb valence - weakens the Mn-Yb bonds. A similar decrease of the Debye temperature and Yb valence upon substitution with a larger isoelectronic element has been observed for instance in  $\text{YbFe}_2\text{Zn}_{20-x}\text{Cd}_x$  [30].

The composition dependence of  $\gamma$  is less regular (figure 4). For compositions near  $x \sim 4.0$ ,  $\gamma \sim 40 \text{ mJ.mole}^{-1}.\text{K}^{-2}$ , close to that of  $\text{LuMn}_6\text{Ga}_{0.8}\text{Sn}_{5.2}$ . This indicates that at this Sn content, when Yb is almost trivalent [12], there is no renormalization of the effective mass  $m^*$  of the charge carriers. Upon  $x$  increase,  $\gamma$  value becomes larger, goes to a maximum ( $\gamma \sim 210 \text{ mJ.mole}^{-1}.\text{K}^{-2}$ ) for  $x$  close to the Yb magnetic instability ( $x_c \sim 5.23$  [11]), before decreasing a little ( $\gamma \sim 150 \text{ mJ.mole}^{-1}.\text{K}^{-2}$  for  $x = 5.55$ ). Concomitantly, the previously found Yb valence  $\nu$  reduces upon  $x$  increase but peaks close to the Yb magnetic instability ( $x_c \sim 5.23$ ), which has been analyzed as a signature of quantum criticality [12].

The  $\text{YbMn}_6\text{Ge}_{6-x}\text{Sn}_x$  alloys with  $x \gtrsim 5$  are moderately heavy fermion materials with  $\gamma > 100 \text{ mJ.mole}^{-1}.\text{K}^{-2}$ . Since  $\gamma \propto m^* \propto 1/T_K$ , genuine heavy fermion behaviors are generally observed for almost trivalent Yb [3, 31, 32] and, in a series of compounds, the Sommerfeld coefficient tends to reduce with the Yb valence [26, 27, 28, 33]. In  $\text{YbMn}_6\text{Ge}_{6-x}\text{Sn}_x$ , the increase of  $\gamma$

whilst the Yb valence reduces (i.e. the Kondo temperature  $T_K$  increases) is somewhat unusual and at odds to expected dependence of  $T_K$  vis-a-vis the hybridization between the  $4f$  states and conduction electrons.

Enhanced effective mass  $m^*$  is one of the usual signatures of quantum criticality [1, 2] and has been experimentally observed for instance in  $\text{CeNi}_{1-x}\text{Ni}_x\text{Ge}_2$  [34]. Hence, the enhanced Sommerfeld coefficients near  $x_c \sim 5.23$  agree with the conclusion of the spectroscopic study about the vicinity a QCP, deep in the intermediate valence regime [12]. The low-temperature limit of our measurements (1.9 K) and the presence of the  $\text{Yb}_2\text{O}_3$  impurity, which overshadows the main phase behavior below  $\sim 7$  K, do not allow determining  $\gamma(T \rightarrow 0)$  nor evidencing a possible non-Fermi-liquid behavior (e.g. a divergence of the magnetic specific heat on approaching 0 K), another hallmark of quantum criticality [2, 3].

#### 4. Conclusion

Our results show that charge carriers in  $\text{YbMn}_6\text{Ge}_{6-x}\text{Sn}_x$  with  $x \gtrsim 5$  are heavy fermion particles. Further, the enhanced effective mass  $m^*$  near  $x_c$  confirms that the Yb magnetic instability corresponds to a quantum critical point, as previously inferred from spectroscopic experiments. A better understanding of the physics near the quantum critical point now requires  $C_p$  measurements below 1.9 K as well as transport measurements (resistivity, thermoelectric power) carried out, preferably, on single crystals.

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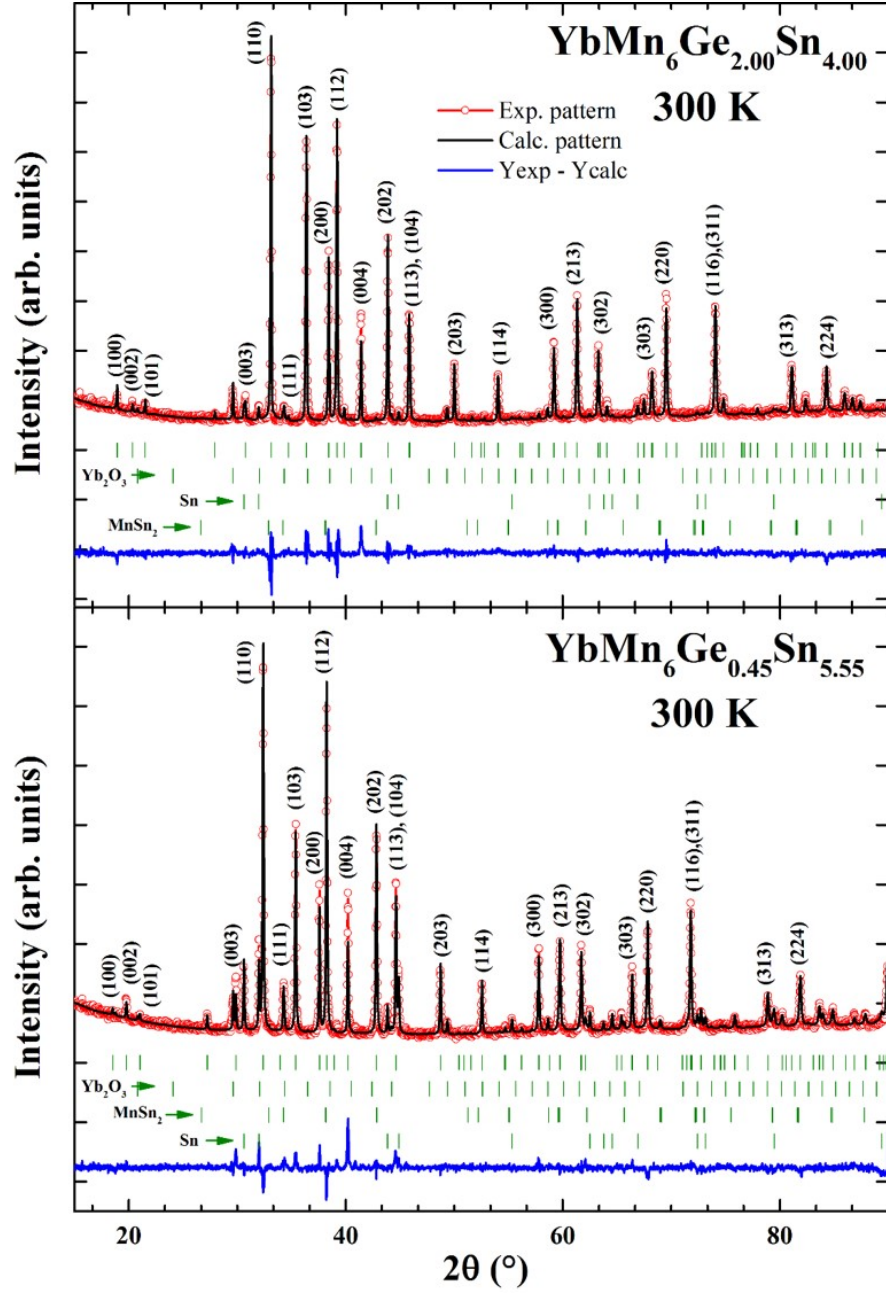


Figure 1: Refined X-ray diffraction pattern of  $\text{YbMn}_6\text{Ge}_{6-x}\text{Sn}_x$  for a)  $x = 4.00$  and b)  $x = 5.55$ .

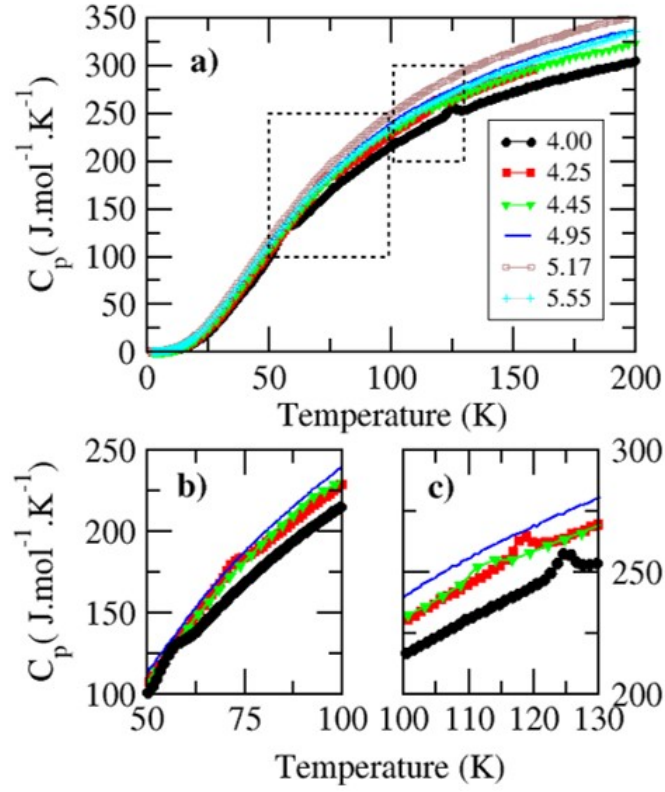


Figure 2: a) Temperature variation of the specific heat of  $\text{YbMn}_6\text{Ge}_{6-x}\text{Sn}_x$  between 1.9 and 200 K. b) and c) Zoom on the 50-100 K and 100-130 K temperature range, respectively, for the alloys with  $4.00 \leq x \leq 4.95$ .

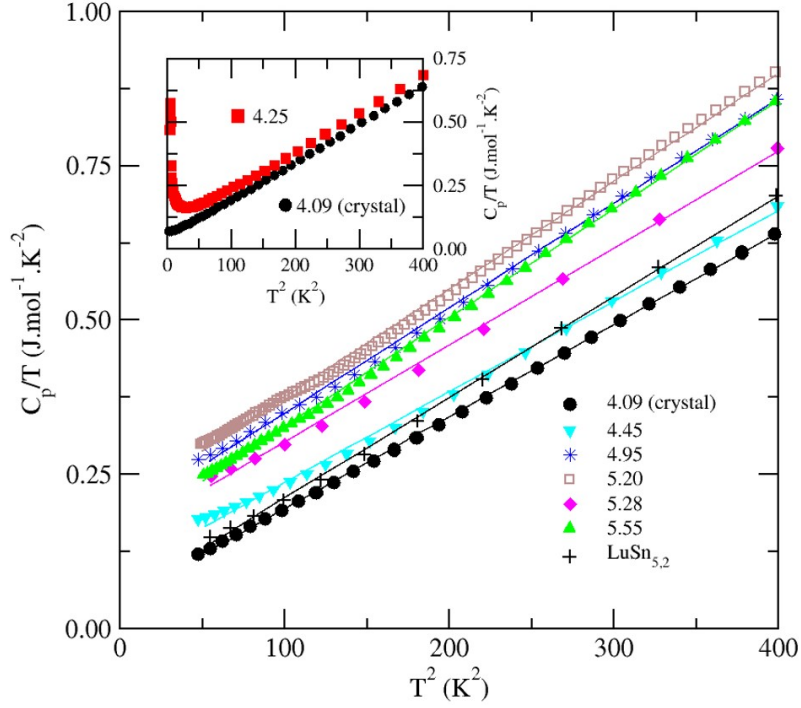


Figure 3: The  $C_p/T$  vs.  $T^2$  plot for  $\text{YbMn}_6\text{Ge}_{6-x}\text{Sn}_x$  and  $\text{LuMn}_6\text{Ga}_{0.8}\text{Sn}_{5.2}$  from  $\sim 7$  K ( $50 \text{ K}^2$ ) to  $\sim 20$  K ( $400 \text{ K}^2$ ). The straight lines correspond to the least-squares fits. The inset shows  $C_p/T$  vs.  $T^2$  data down to  $\sim 1.9$  K for  $x = 4.09$  (single crystal) and  $x = 4.25$  (polycrystal).

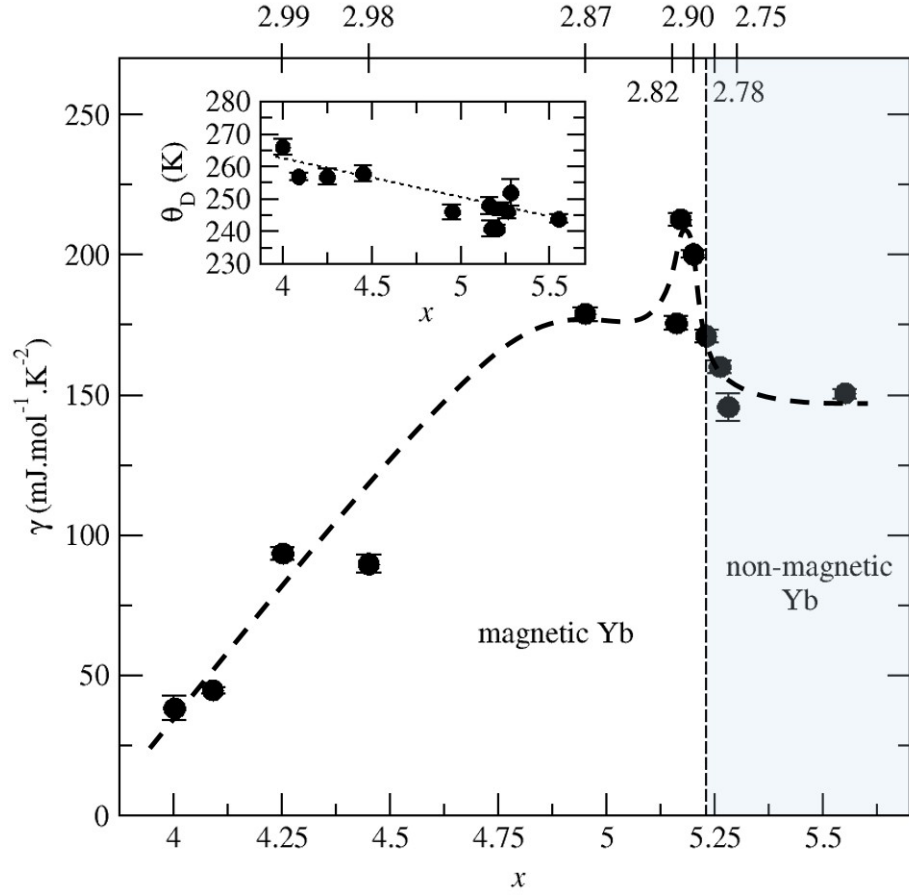


Figure 4: Composition dependence of the Sommerfeld coefficient  $\gamma$  in  $\text{YbMn}_6\text{Ge}_{6-x}\text{Sn}_x$ . Some Yb valence values at 5 K taken from reference [12] are indicated on the top axis. The thin vertical line marks the Yb magnetic instability [11, 12]. The dashed curved line is a guide to the eye. The inset shows the composition dependence of the Debye temperature  $\Theta_D$ . The dotted straight line is a guide to the eye