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Modeling the impact of rainfall and temperature on sterile insect control strategies in a Tropical environment

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Abstract

The sterile insect technique (SIT) is a biological control technique that can be used either to eliminate or decay a wild mosquito population under a given threshold to reduce the nuisance or the epidemiological risk. In this work, we propose a model using a differential system that takes into account the variations of rainfall and temperature over time and study their impacts on sterile males' releases strategies. Our model is as simple as possible to avoid complexity while being able to capture the temporal variations of an *Aedes albopictus* mosquito population in a domain treated by SIT, located in Réunion island. The main objective is to determine what period of the year is the most suitable to start a SIT control to minimize the duration of massive releases and the number of sterile males to release, either to reduce the mosquito nuisance, or to reduce the epidemiological risk. Since sterilization is not 100% efficient, we also study the impact of different levels of residual fertility within the released sterile males population. Our study shows that rainfall plays a major role in the dynamics of the mosquito and the SIT control, that the best period to start a massive SIT treatment lasts from July to December, that residual fertility has to be as small as possible, at least for nuisance reduction. Indeed, when the main objective is to reduce the epidemiological risk, we show that residual fertility is not necessarily an issue. Increasing the size of the releases is not always interesting. We also highlight the importance of combining SIT with mechanical control, i.e. the removal of breeding sites, in particular when the initial mosquito population is large. Last but not least our study shows the usefulness of the modeling approach to derive various simulations to anticipate issues and demand in terms of sterile insects' production.

Keywords: Vector control; *Aedes spp*; Sterile Insect Technique; Temperature; Rainfall; Residual fertility; Nuisance reduction; Epidemiological risk; Mathematical modeling; Numerical simulation.

1 Introduction

Being vectors of many diseases, like malaria, dengue, Lymphatic filariasis, zika, chikungunya, yellow fever, and japanese encephalitis, mosquitoes are one of the biggest killers in the world, and particularly in tropical and subtropical areas. Indeed, Female mosquitoes need blood meals to provide the nutrients for egg development. That is why they bite either during the night, like *anopheles spp*, at sunset or sunrise, like *aedes albopictus*, or along the day, like *aedes aegypti*, inside or outside houses. Since they can survive several weeks, they will bite several times depending on their gonotrophic cycle [14]. While opportunistic feeders, Anopheles and Aedes mosquitoes prefer biting mammals and, preferably, humans [26], with sometimes multiple blood feeding [8].

To eradicate mosquito-borne diseases, the initial option was the massive use of chemicals in the 1950's and 1960's, mainly against anopheles. Despite some successes, like in Réunion island where malaria has been eradicated since the fifties, thanks to the use of DDT [13], we know now that this was a huge mistake: even if the use of adulticides was successful against mosquitoes, the damages on the biodiversity were important. In addition, resistance to some adulticides raised, such that, in several places around the World, there is no option left to fight the mosquitoes, like in the French West Indies [17]. Fortunately, other eco-friendly control methods,

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more respectful of the biodiversity, have been developed. Among them, the Sterile Insect Technique (SIT) is the most promising one. This is an old control technique, proposed in the 30s and 40s by three key researchers in the USSR, Tanzania and the USA and, first, applied in the field in the 50's [11]. SIT has been used more or less successfully on the field against various kinds of Pests or Vectors (see [5, 11] for various examples). The classical SIT consists of mass releases of males sterilized by ionizing radiation. The released sterile males transfer their sterile sperms to wild females, which will have no viable offspring, resulting in a progressive decay of the targeted population. For mosquitoes, other sterilization techniques have been developed using either genetics (release of insects carrying a dominant lethal technique, in short, RIDL technique [25]) or bacteria (SIT-IIT : cytoplasmic incompatibility thanks to *Wolbachia* bacteria) [23]. Many SIT projects against mosquitoes are now ongoing around the World. It is important to keep in mind that controlling a vector population could have an impact on the ecosystem equilibrium. In fact, it depends if the targeted vector is an invasive species, i.e. established recently or if it has been established for a long time. If the establishment is recent (a couple of years), then with elimination, we can expect to recover the initial state of the ecosystem before the invasion starts. On the contrary, when the vector is established, then elimination is not necessarily the goal. Reduction is preferable in order to reduce the epidemiological risk. We will explore these two objectives in this work.

Several mosquito models have been developed, from very simple models to more sophisticated ones, according to the number of biological states that are taken into account. These models consider the mosquito population either at the individual level (see for instance [2]) or at the population level (see for instance [16]), taking eventually into account the spatial component (see for instance [3] for a brief review). Each of these approaches has advantages and disadvantages. However, it is always important to keep in mind that biological parameters are difficult to obtain in the field, such that for too complex models, it might be impossible to set the (right) values of the parameters. In addition, most of the biological parameters are linked to environmental parameters, like rainfall, humidity and temperature. The main goal of the present article will be to take into account these parameters in the mathematical model to find the best control.

Mathematically, it can make sense to consider constant or periodic parameters to derive the main dynamics of the mosquito population. However, for practical reasons, i.e. anticipating when the mosquito population is growing or decaying, it is better to have a mosquito model that takes into account the most important parameters, like rainfall, humidity and temperature, to derive simulations to adapt the control, i.e. for instance the size of the releases or/and the period of the releases. Last but not least, being able to derive several realistic simulations can help to anticipate the demand in terms of sterile insects production.

Since our work takes place within an ongoing SIT feasibility program (TIS 2B) against *Aedes albopictus* in La Réunion, a tropical French island located in the Indian Ocean, we will focus on this species in the rest of the paper. In La Réunion, *Aedes albopictus* has become the main vector of dengue and chikungunya [28]. However, we believe that our approach is sufficiently generic to be applied to other mosquito species.

While links between *Aedes albopictus* parameters and temperature have been studied in laboratory [9], for a fixed (laboratory) humidity, it is more challenging to take into account the effect of rainfall (and humidity).

Some weather-dependent mosquito models have been developed, mainly with Temperature-dependent parameters (see for instance [7, 10] and references therein) and very few with temperature and rainfall-dependent parameters (see [27] and references therein). However, in general, these last models are quite complex: they relied on statistical approaches and on the user's subjective choices, such that the calibration (of many parameters), with respect to the environmental parameters, is not generic and might not be able to provide a unique set of valuable values. We firmly believe that simple (but not too simple) models can rapidly provide useful and reliable information to help field experts to manage vector control campaigns.

That is why we consider a minimalistic model (minimal in terms of stages and thus parameters), based on [4], to build an approximation of the mosquito population over many years. Then, we show that the density variation (in time) of the mosquito population can help to improve vector-control strategies combining SIT with mechanical control, i.e. the removal of breeding sites to reduce the larvae carrying capacity.

It is well known that sterilization does not necessarily induce that the sperm of the sterilized males is 100% sterile (see for instance [20, 35]): it depends on the radiation source, the dose-rate, and the container. That is why quality control after sterilization is set up to control that the sterile males remain competitive and efficient. Efficiency is thus related to the effective sterility or the residual fertility (RF, shortly), i.e. the percentage of sperms that is still fertile despite the irradiation, that is equivalent to say, at the population level, that a small proportion, ε , of the sterile males is fertile. In our model, we will take into account the fact that residual fertility can occur within the sterile male population to study its impact on SIT control.

In general, in most of the SIT models (except in [5] and the present paper), residual fertility is never taken into account, while it can have a strong impact on SIT efficiency. Indeed, in [5], using a 2-dimensional mosquito model with constant parameters, the authors showed that the residual fertility, ε , is strongly linked to the basic offspring number, \mathcal{N} , of the wild population: when

$$\varepsilon < \frac{1}{\mathcal{N}}, \quad (1)$$

then SIT is efficient and the mosquito population can be lowered under any given threshold, provided that enough sterile males are released. However, when ε is below but close to $\frac{1}{\mathcal{N}}$, the amount of sterile males increases almost exponentially [5]. On the contrary, when $\varepsilon > \frac{1}{\mathcal{N}}$, then, whatever the size of the sterile males releases, the wild population cannot be lowered under a certain threshold value, that can be roughly estimated [5]. In fact, we suspect that a too-large residual fertility could partly explain failures in some SIT programs. For instance, in [35], a SIT program conducted on Mauritius island, which is close to Réunion island, the residual fertility was experimentally estimated at around 3.05% (2.29% – 3.92%), which could explain why mitigated results were obtained, before a cyclone occurred and broke the experiment. We believe that 3% of RF is too large such that the reduction of the wild population with SIT is limited. Indeed, in [5], the authors showed that if RF is too large, then, whatever the size of the sterile males releases, the population cannot be lowered under a given threshold.

The paper is organized as follows: In section 2, we build a temperature and rainfall-dependent entomological model and an impulsive periodic SIT model. Then, in section 3, we provide several numerical simulations to discuss the impact of the temperature, the rainfall, the residual fertility and the mechanical control on SIT starting period and duration to reduce either the nuisance or the epidemiological. Finally, in section 4, we end the paper with some conclusions and perspectives.

2 Rainfall, humidity, and temperature dependent SIT model

The first aim of the present work is to develop a temperature-rainfall-dependent entomological model, to take into account real field data, including mean daily rainfall and mean daily temperature.

Following [4], we will consider the following model

$$\begin{cases} \frac{dA}{dt} = \phi(Temp)F - (\gamma(Temp) + \mu_{1,A}(Temp) + \mu_{A,2}(Temp, Rain)A)A, \\ \frac{dM}{dt} = (1 - r(Temp))\gamma(Temp)A - \mu_M(Temp)M, \\ \frac{dF}{dt} = r(Temp)\gamma(Temp)A - \mu_F(Temp)F, \end{cases} \quad (2)$$

where A , M , and F represent, respectively the aquatic (larvae, pupae) stage, the adult (male and mated and fertile female) stages. Here, we implicitly assume that all emerging females will mate and become fertile. Note carefully that compartment A does not include the eggs since we consider a density mortality rate $\mu_{A,2}$ that concerned only the larval and pupal stages. Thus, the parameter ϕ represents the daily amount of deposited eggs that hatch to become larvae. All parameters of model (2) are described in Table 1. This model has been studied

Table 1: Description of the entomological parameters

Symbol	Description	Unit
ϕ	Number of hatched eggs at each deposit per capita	Day ⁻¹
γ	Maturation rate from larvae to adult	Day ⁻¹
$\mu_{A,1}$	Density independent mortality rate of the aquatic stage	Day ⁻¹
$\mu_{A,2}$	Density dependent mortality rate of the aquatic stage	Day ⁻¹ Individuals ⁻¹
r	Sex ratio	-
$1/\nu_m$	Average extrinsic incubation period (EIP)	Day
$1/\mu_F$	Average lifespan of fertilized and eggs-laying females	Day
$1/\mu_M$	Average lifespan of males	Day

in [4] when the parameters are supposed to be constant. In [4] the authors developed a new strategy to maintain the wild population under a certain threshold, using a permanent and sustainable low level of SIT control, thanks to a massive-small releases strategy. We set $\mathcal{N}_{\max} = \max_{t \in [0, +\infty)} \mathcal{N}(t)$, where \mathcal{N} represents the basic offspring number, defined as follows

$$\mathcal{N} = \frac{r\phi\gamma}{(\gamma + \mu_{A,1})\mu_F}.$$

In Réunion island, a network of Weather stations (from Météo France but also from CIRAD) allows us to estimate some weather parameters all around the island, and in particular where real SIT field experiments started in July 2021, in the site of Duparc, a 20-hectare urban area located within the commune of Sainte Marie

in the northern district of La Réunion [15]. These releases consist of manually weekly releases of 150 000 to 250 000 sterile males (once a week) produced and irradiated in La Réunion. The efficacy of sterile males releases is assessed over time by monitoring the induced sterility in eggs using ovitraps and the subsequent population suppression using adult traps, and, from time to time, Mark-Release-Recapture experiments. This experiment lasted until September 2022.

From the Weather station located in La Mare, close to the site of Duparc (1km), we are able to obtain the following daily data: the rainfall, the average daily temperature and also the humidity. Thus, following [30], we first define the breeding site carrying capacity to define the density death-rate $\mu_{A,2}$. Obviously, the persistence of breeding sites is a key factor for the mosquito population's survival. Indeed, rainfall creates breeding sites, while evapotranspiration tends to shrink them. Following [30], we define the variable $H(t)$ as the amount of water available at day t and defined as follows

$$H(t+1) = \begin{cases} 0 & \text{if } H(t) + \Delta(t) \leq 0, \\ H_{max} & \text{if } H(t) + \Delta(t) \geq H_{max}, \\ H(t) + \Delta(t) & \text{otherwise,} \end{cases}$$

with

$$H_{max} := \max_{t \in [t_0, t_0+T]} \{Rain(t)\}$$

and

$$\Delta(t) := Rain(t) - Evap(t),$$

where $Rain(t)$ is the daily rainfall and $Evap(t)$ the daily evaporation, t_0 is the starting date of the simulations, and T the total duration. Following [30], the evaporation function is defined as follows

$$Evap(t) = k \times (25 + Temp(t)^2) \times (100 - Hum(t)),$$

where $Temp(t)$ is the average temperature and $Hum(t)$ the humidity. Finally, the carrying capacity is defined

$$K(t) = K_{max} \frac{H(t)}{H_{max}} + K_0,$$

where $K_0 > 0$ can be seen as the fixed artificial carrying capacity, i.e. rainfall-independent, human-made, by watering, for instance, plants around houses (flower pots, plates, and vases), and K_{max} , the natural maximal carrying capacity.

The initialization in time of the variables (in particular of H) is explained in the simulations section, page 6. We notice that, in general, in the literature, the question of initialization is not always taken into account, while it can have a strong influence over several months on the population dynamic. We illustrate this fact in Figure 2, page 7.

In order to estimate $\mu_{2,A}$, we consider the positive equilibrium related to the carrying capacity, like in [10, 31, 32]. Thus, for a fixed value of K , the aquatic stage at equilibrium is given by

$$A_K^* = \left(1 - \frac{1}{\mathcal{N}}\right) K. \quad (3)$$

In our model, the aquatic stage at equilibrium is defined as follows

$$A^* = \frac{\gamma + \mu_{A,1}}{\mu_{A,2}} (\mathcal{N} - 1), \quad (4)$$

such that considering the equality between both equilibria given in (3) and (4), we derive the following relationship between $\mu_{A,2}$ and K , that is

$$\mu_{A,2} = \frac{\mathcal{N}(\gamma + \mu_{A,1})}{K} = \frac{r\gamma\phi}{\mu_F K}.$$

Thus, taking into account the dependency of the parameters to Temperature and Rainfall, we deduce that

$$\mu_{A,2}(Temp, Rain) = \frac{r(Temp)\gamma(Temp)\phi(Temp)}{\mu_F(Temp)K(Temp, Rain)}. \quad (5)$$

As it is well known, eggs are deposited above the waterline. They hatch once they are flooded by rainfall. However, the hatching rate can be seasonal. From *A. albopictus* eggs, picked up at Duparc, the mean hatching proportion is around 90% (G. Legoff, personal communication, TIS2B project).

For the other parameters, we will consider the data recalled in Appendix A, page 14, in Table 3, page 15, as used in [32] to obtain the parameters estimates given in Table 4, page 15.

Then, we can use simple interpolation polynomials (with cubic spline, like in [33]) to estimate these parameters for any given temperature $Temp$, within the range $[15^\circ, 35^\circ]$.

We will assume constant or periodic releases of sterile males, at rate $u_S(t)$ (either constant or variable), and μ_S , the sterile male mortality rate, which is supposed to be similar to the wild males mortality rate [34]. The dynamic of the sterile males is modeled by

$$\frac{dM_S}{dt} = u_S(t) - \mu_S(Temp)M_S. \quad (6)$$

Thus, based on model (2), we consider the following temperature and rainfall dependent SIT-model

$$\begin{cases} \frac{dA}{dt} &= \phi(Temp)F - (\gamma(Temp) + \mu_{1,A}(Temp) + \mu_{A,2}(Temp, Rain)A) A, \\ \frac{dM}{dt} &= (1 - r(Temp))\gamma(Temp)A - \mu_M(Temp)M, \\ \frac{dF}{dt} &= r(Temp)\gamma(Temp)\frac{M + \varepsilon\beta M_S}{M + \beta M_S}A - \mu_F(Temp)F, \\ \frac{dM_S}{dt} &= u_S(t) - \mu_S(Temp)M_S. \end{cases} \quad (7)$$

The parameter β is the competition parameter that is deduced from the Fried index [12]. Following [20], we will consider $\beta = 1$, which means that a sterile male is as competitive as a wild male. The Fried index is estimated through a protocol described in [12] (see also [29]). Last, as explained in the introduction, all irradiated males are not 100% sterile: a small proportion of their sperm can stay fertile. At the population scale, this is modeled by the parameter ε , which represents the proportion of sterile males that remain fertile and thus can fertilize emerging females. As already explained in [40][Remark 4], *A. albopictus* females got 3 spermathecae that allow to stock sperms such that, in general, one mating is sufficient to fulfill at least 2 spermathecae and to have enough sperms to fertilize eggs along its lifespan. Thus the nonlinear term related to SIT treatment occurs when females emerge from compartment *A* and not in the birth rate. Considering SIT impact on the birth rate, i.e. $\frac{M + \varepsilon\beta M}{M + \beta M}\phi$, is very convenient from the mathematical point of view, but it is not biologically realistic. We prefer to stick to the biological reality, at least for *A. albopictus*. Thus, altogether, in model (7), the term $\frac{M + \varepsilon\beta M}{M + \beta M}\phi$ represents the probability for an emerging female to be fertilized and thus to enter compartment *F*.

2.1 Impulsive SIT massive-small releases strategy

In the rest of this paper, we will consider the so-called massive-small releases strategy developed in [4]. Indeed, once a few sterile males are released, this induces a strong Allee effect, such that the elimination equilibrium, $\mathbf{0}$, and a positive equilibrium *E* are both asymptotically stable. In [4], we showed that it is possible to estimate the minimal amount of sterile males to release to stay in the basin of attraction of $\mathbf{0}$ when the wild population is sufficiently small. This means that massive releases have first to be used over a sufficient time period in order to enter in a particular subset of the basin of attraction of $\mathbf{0}$, that is estimated thanks to a given (small) release rate value. Once inside the basin of attraction of $\mathbf{0}$, it is possible to switch from massive releases to small releases. This strategy is particularly useful since SIT cannot be stopped in order to prevent the re-establishment of the targeted vector, either by introduction or by migration.

According to this massive-small releases strategy, we want to find the best period to start SIT control (without or with Mechanical Control) to minimize the number of massive periodic impulsive releases, and thus the amount of sterile males to release.

We provide some computations of the SIT-equilibria in Appendix B, page 16. Thanks to [4], and assuming that $\mathcal{N}\varepsilon \leq 1$, system (7) has the following long term behavior

- There exists a release rate threshold, u^* , such that when $u_S(t) > u^*$ then (A, M, F) converges to $\mathbf{0}$.
- When $0 < u_S(t) < u^*$, then there exist two positive equilibria, \mathbf{E}_1 and \mathbf{E}_2 such that $\mathbf{E}_1 < \mathbf{E}_2$. Moreover \mathbf{E}_1 is unstable while \mathbf{E}_2 is stable and $(\mathbf{0}, \mathbf{E}_1)$ lies in the basin of attraction of $\mathbf{0}$.

Remark 1. When $\mathcal{N}\varepsilon > 1$, then, elimination is not possible, whatever the size of the massive releases. Using the equilibrium value for the aquatic stage, *A*, given in appendix B, page 16, it is straightforward to show that there exists a lower bound for the SIT positive equilibrium, for all $u_S > 0$, given by

$$\begin{cases} A_l^* = 2\frac{\varepsilon\mathcal{N} - 1}{\mathcal{N} - 1}A^*, \\ M_l^* = \frac{(1 - r)\gamma}{\mu_M}A_l^*, \\ F_l^* = \frac{\gamma + \mu_{1,A} + \mu_{A,2}A_l^*}{\phi}A_l^*. \end{cases} \quad (8)$$

However, even if $\mathcal{N}\varepsilon > 1$ and nuisance reduction is not possible, it does not mean that it is not possible to reduce the epidemiological risk. The lower bound (8) will be useful in the epidemiological risk section.

We will consider two different levels of massive releases (6000 or 12000 sterile males per ha), such that $u > u^*$ for all $t \geq 0$, to decrease the wild population below a threshold set, $[0, \mathbf{E}_1]$, defined by (inexpensive) small releases (say 100 sterile males per ha), in a minimum time. We want to know how the duration of massive releases is influenced by temperate and rainfall conditions during the year, the residual fertility and the level of mechanical control. In other words, we search a control with the form

$$u(t) = \tau \Lambda_{\text{massive}} \sum_{i=1}^N \delta_{t_0+(i-1)\tau}(t), \quad (9)$$

where $\delta(t)$ is the Dirac function, t_0 is the starting time of the massive releases, τ the periodicity of the releases (here, $\tau = 7$), and N the number of weakly massive releases. The massive release Λ_{massive} and the small releases Λ_{small} are fixed. For a given t_0 there exists a $t_1(t_0) = t_0 + N_1(t_0)\tau$ (according to [4]) such that, after this time, the wild population (A, M, F) remains in the box $[0, \mathbf{E}_{1,\min}(\tau \Lambda_{\text{small}})]$ where $\mathbf{E}_{1,\min}(\tau \Lambda_{\text{small}})$ is defined as follow: For a given Λ_{small} , for each time t , we compute the equilibrium $\mathbf{E}_1(t)$ of the system associated to the parameters at time t , and we define $\mathbf{E}_{1,\min}(\tau \Lambda_{\text{small}}) = \min_t \mathbf{E}_1(t)$, where the minimum is taken between the beginning and the end of the time interval considered in the simulation.

The main goal is to find the (best) starting time of the massive releases, t_0 , in order to minimize the duration of the releases and thus, the number of massive releases.

System (6)-(9) can be rewritten as an impulsive differential system with fixed moments of impulse effect, that is

$$\begin{cases} \frac{dM_S}{dt} = -\mu_S(T)M_S, & t_0 + i\tau < t \leq t_0 + (i+1)\tau \\ M(t^+) = M(t) + \tau \Lambda_{\text{massive}}, & t = t_0 + i\tau, \end{cases} \quad (10)$$

for $i = 0, \dots, N-1$. Since, the right-hand side of (7)-(10)₁ is locally Lipschitz-continuous on \mathbb{R}^4 , we can use a classical existence Theorem (for instance Theorem 1.1 in [37], or Theorem 2.1 in [36]), to deduce that there exists $T_e > 0$ and a unique solution of system (7)-(10), defined from $(t_0, T_e) \rightarrow \mathbb{R}^4$.

3 Numerical simulations and discussion

System (7)-(10) is solved thanks to `odeint` of the python library `scipy.integrate`. The codes and the data corresponding to the temperature and the rainfall in Réunion island are available on

<https://github.com/michelduprez/Impact-of>

`-Rainfall-and-Temperature-on-IT-control-strategies.git`

Computations are not complex but very long. That is why we ran our code on the MESO@LR-Platform (University of Montpellier). The figures have been draw using the software Matlab [24].

We consider temperature, rainfall and humidity data based on (noised) data recorded in weather stations close to the site of Duparc (a 20 ha place), a neighborhood of Sainte Marie, located in the North of Réunion island from the 1st of January 2009 to the 14th of July 2021.

In La Réunion, since the sterile males are produced on-site, everything from the eggs to the sterilization is controlled (qualitatively), such that since the production started, the residual fertility is, in general, less than 1%, with an average value of around 0.6%, a very good results compared to other SIT projects, like [35]. That is why, in the forthcoming simulations, we will consider three cases of RF, namely 0%, 0.6% and 1.2%.

In Fig. 1, we consider the following values: $K_{\max} = 20 \times 10000$, $K_0 = 20 \times 100$ to derive the carrying capacity, K , and thus $\mu_{A,2}$.

It is interesting to see the behavior of $\mu_{A,2}$ in the second-half of 2020, which was a particularly dry period compared to previous years in La Réunion. Note also that when mechanical control is considered, it will impact $\mu_{A,2}$: for instance, thanks to Formula (5), 40% of Mechanical control increases $\mu_{A,2}$ by 66.7%.

The choice of the initial condition for H and the initial conditions for the mosquitoes will impact respectively the initialization of the carrying capacity and the dynamic of the system for at most 12 months (see Fig. 2, page 7, where we have considered extreme initial values for $H(0)$ and for the population). That is why, in order to have a reliable estimate of the wild mosquito population at the beginning of the control, i.e. the 1st of Sept. 2010, we start the simulations at the beginning of January 2009.

Using the parameters values and the estimates of $\mu_{A,2}$ given in Fig. 1, page 7, we derive the dynamic of the mosquito population in Duparc without release: see Fig. 3(c), page 19. In Fig. 3(a)-(b), page 19, we also show the time evolution if the mean daily Temperature and the mean daily rainfall (mm). As expected, periods, where the rainfall is low, imply a rapid decay of the population size, leading to an "almost" oscillatory behavior. This result is confirmed by Mark-Release-Recapture experiments derived in Duparc [15], where the ratio between the mosquito density/ha within the dry period and the mosquito density/ha within the wet period is a factor 10, which highlights the importance to consider a temporal dynamic in the parameters.

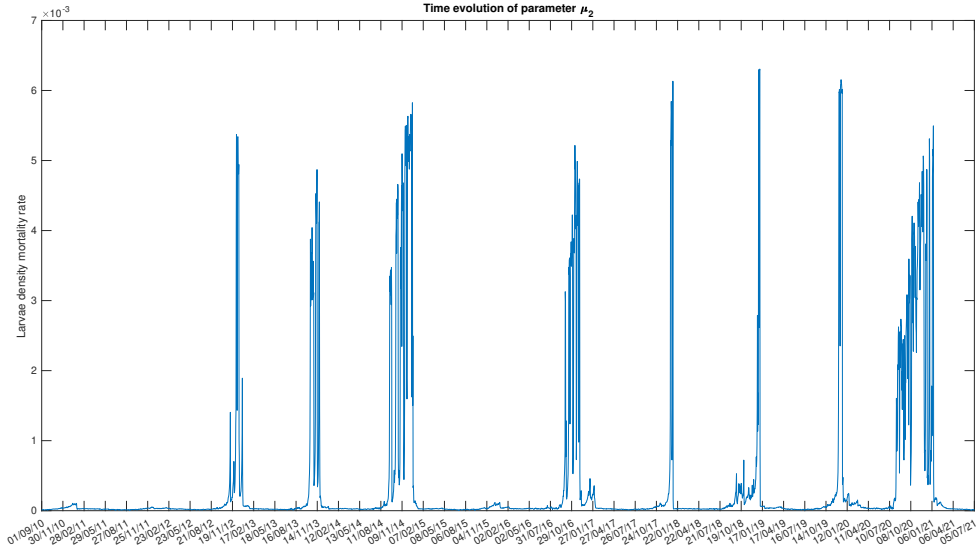


Figure 1: Time evolution of $\mu_{A,2}$ from the 1st of September 2010 until the 14th of July 2021

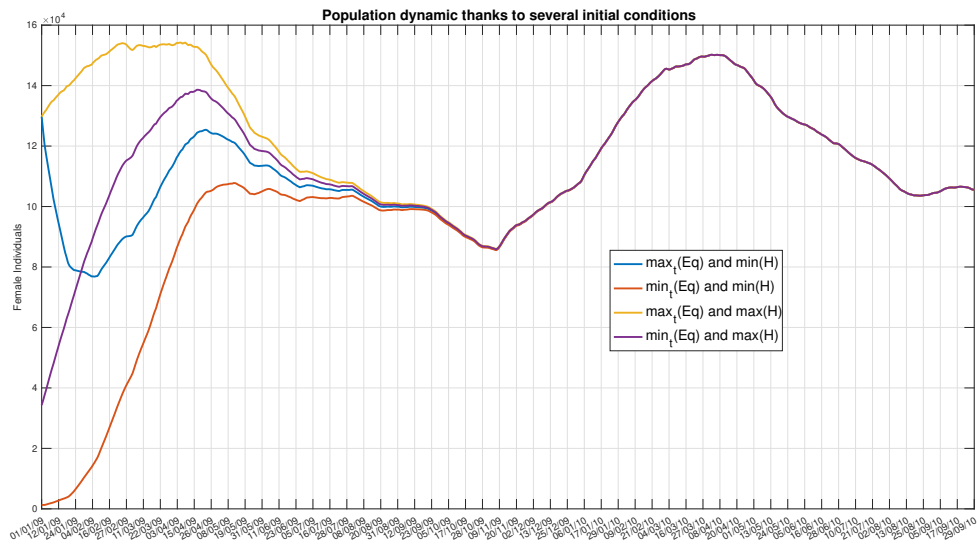


Figure 2: Temperature and rainfall dependent model - Simulations of the mosquito dynamics with several initial conditions, thanks to the initial rainfall data and the initial size of the mosquito population

3.1 Global sensitivity analysis

Before starting the simulations, we provide a global sensitivity analysis (GSA) using Latin hypercube sampling (LHS) and Partial rank correlation coefficient (PRCC), within the range of values for the temperature and rainfall given in Fig. 3(a)-(b), page 19. The main objective of this GSA is to identify key parameters that most drive the variables and the dynamics of our system. Briefly, the objective of the LHS-PRCC sensitivity analysis is to identify key parameters whose uncertainties contribute to prediction imprecision and to rank these parameters by their importance in contributing to this imprecision. We refer the interested reader to [1, 18] for further information about LHS-PRCC analysis. The forthcoming LHS-PRCC figures are made using R [21] and R-studio [22].

In Fig. 4, page 20, the main sensitive parameters for all variables of model (2) are $\mu_{A,2}$, Φ and ν_A , as expected.

An important outcome is that since $\mu_{A,2}$ is strongly related to the temperature and rainfall, mechanical control, i.e. the removal of breeding sites, is more than useful to increase $\mu_{A,2}$, and, thus, to impact (negatively) all compartments. This fact is also confirmed in the next LHS-PRCC analysis of the SIT model with continuous and periodic releases: see Fig. 5, page 21, and 6, page 22. Also, as expected Λ_S and β are sensitive parameters in the SIT models. Contrary to the initial entomological model, the parameter μ_F has become more sensitive in the SIT models. All these informations show that a combined effort mixing SIT and mechanical control will have a strong impact on the wild population control. Last, if an additional control tool against females is able to increase μ_F , using, for instance, killing traps, the overall control will be even more efficient. Last but not least, for τ varying from 1 (daily releases) to 14, its impact on the periodic SIT-model is negligible: what matters are the size of the releases and the competition parameters.

3.2 Reducing mosquito nuisance

As studied in [4], we consider the massive-small strategy, which consists first of periodic massive releases, such that $\tau\Lambda_{massive} = 20 \times 6000$ or 20×12000 individuals, until the wild population has become lower than $\mathbf{E}_{1,\min}(\Lambda_{small})$, where here $\tau\Lambda_{small} = 20 \times 100$ individuals, such that

$$\mathbf{E}_{1,\min}(\Lambda_{small}) \approx \begin{cases} (37.0, 29.8, 0.511) & \text{if } \varepsilon = 0.0, \\ (17.97, 14.47, 0.24) & \text{if } \varepsilon = 0.006, \\ (1.38, 0.350, 0.0059) & \text{if } \varepsilon = 0.012. \end{cases}$$

The previous values have been estimated thanks to the equilibria computed in Appendix B, page 16. We notice that, when the residual fertility increases, then the size of the box $[0, \mathbf{E}_{1,\min}(\Lambda_{small})]$ becomes smaller: SIT introduces a strong Allee effect while the residual fertility weakens it. Thus, in the forthcoming simulations, it will not be surprising to find large duration time values when the residual fertility is large. Once $[0, \mathbf{E}_{1,\min}(\Lambda_{small})]$ is reached, the periodic releases continue at rate Λ_{small} . Using the numerical simulations, we are able to estimate the date where the system can switch from massive releases to small releases and thus evaluate the duration of the (very) massive releases.

According to the time variation of the parameters, the basic offspring number \mathcal{N} will vary between 29.7 and 85.7 with a mean of 48.41 over the considered period. Thus even if Formula (1) is not verified at each time, it is satisfied in mean, i.e.

$$\varepsilon < \frac{1}{T} \int_0^T \frac{1}{\mathcal{N}(t)} dt = 0.0222. \quad (11)$$

An important issue in SIT control is to estimate the duration of the massive releases. Thanks to contrasted environmental conditions, within the period [2010 – 2020], we show that the minimal time to decay the wild population under a certain threshold can greatly vary.

In general, in the literature, many SIT simulations are done with constant parameters, except, for instance, in [10, 38]. If we consider the mean value for each parameter over the whole period, we derive $\mathcal{N} \approx 49.3$ which is a quite large basic offspring number, but not surprising within a tropical context.

Before starting the simulations, we would like to emphasize that our meteorological data last from 01/01/2009 and 14/07/2021. Our simulations intend to derive an estimate of SIT treatment duration within this interval when the SIT control starts 01/09/2010. Thus, the reader does not have to be surprised to see that our results curves do not end at the same time: this is simply because the simulations were not able to enter $[0, \mathbf{E}_{1,\min}(\Lambda_{small})]$ before the 14th of July 2021. Thus the simulation stops.

In the forthcoming simulations of model (7)-(10), we will consider four cases to illustrate the importance of considering all (or not) environmental parameters:

1. Model 1: model (7)-(10) with temperature and rainfall dependent parameters.
2. Model 2: model (7)-(10) with temperature-dependent parameters only.
3. Model 3: model (7)-(10) with a constant average temperature and rainfall-dependent parameters.
4. Model 4: model (7)-(10) with average parameters values estimated from September 2010 to mid-July 2021.

We first provide Fig. 7, page 23, where simulations of the four models are given for different values of RF, 0%, 0.6% and 1.2%, with $\tau\Lambda = 120000$ individuals, and without mechanical control. It is easy to check that the greater RF, the larger the amount of releases. However, the increase is reasonable when $RF = 0.6\%$, it is really important when $RF = 1.2\%$. It is interesting to notice that model 1 and model 3 behave similarly more or less: this is due to the fact that rainfall is taken into account in parameter $\mu_{A,2}$. Thus, for RF equal to 0% and 0.6%, model 3 is close to the variations of model 1. In contrary, when $RF = 1.2\%$, then it seems that the temperature-dependent parameters are taken over since model 1 and model 2 are now close, while model 3 provides very different and lower estimates. Model 4 provides a constant value for the amount of releases: while this average value seems to be realistic when residual fertility is small, this is no more the case when residual fertility is large: see Figs. 7 and 8. Model 2, where the parameters are only temperature dependent, provide the

worst estimates, except in the years where rainfall was abundant, i.e. 2010 and 2011. However, along the decade, except when RF is equal to 1.2%, model 2 is the worst one. In addition, the main disappointment with model 2, with temperature-dependent parameters only, comes from the fact that the inter-annual periodic behavior, for which the best period to start SIT would (roughly) be between May and September. This is exactly the same conclusion reached by entomologists.

In Fig. 8, page 24, we consider the same simulations than in Fig. 7, page 23, but with the release of $\tau\Lambda = 240000$ individuals per week. The results, in terms of behavior, are almost the same with some improvements in terms of the releases amount. However, thanks to the sterile males production effort, the gain are very little. This shows that increasing the release rate does not necessarily improve the duration of massive releases.

The death rate of mosquitoes is mainly linked to the temperature, such that we can intuitively think that the best period to act is during the Austral winter, i.e. from the end of June to the end of September. However, According to Figs. 7, 8, and 9, page 23, 24 and 25, and following model 1 (and model 3), the best intervention period, i.e. the SIT starting-time, lasts, in general, from July to December. Indeed, as seen in these figures, in particular in Fig. 9, page 25, the amount of releases oscillates with various amplitudes but with its minimal value always reached around the last two weeks of November, except in 2020 that was a particularly dry year in La Réunion. After November, we usually enter in the rainy season, and that is why the amount of releases increases fast. In fact, each year, from June-July to December, we observe that the amount of releases needed to reach elimination reaches its lowest value and is, more or less, decreasing from June to December. Thus, the window to start SIT control is larger than expected and is not necessarily reduced to the Austral winter period (from June to September) but can also include the Spring period (from October to December).

We now focus on simulations of model 1, with temperature and rainfall dependent parameters, taking into account the impact of residual fertility and Mechanical control: see Fig. 9, page 25. In Fig. 9(a), the straight line represents the average value of the numerical simulations. Thanks to Fig. 7, we can see that that this value is 4 weeks larger than the value obtained by model 4, where all parameters are supposed to be constant. However, around this average value, we can see that the results are very contrasted, mainly related to the average rainfall. In Fig. 9(b), we show the impact of residual fertility: while 0.6% of residual fertility "only" increase the amount releases up to 20 weeks, a residual fertility of 1.2% increases drastically the amount of the releases, between 80 and 110 weeks. Finally, in Fig. 9(c), we show the benefit of Mechanical control, i.e. reducing the breeding sites. However, we recover the fact that mechanical control is more beneficial within rainy periods, when the mosquito population is large, than in dry periods: compare the years 2010-2011 with the years 2016, 2019, and 2020, in Fig. 9, page 25. This is quite obvious but this is important to highlight this fact in terms of control strategies and cost.

From the practical point of view, since we are not yet capable of predicting weather data accurately, it is important to have an initial estimate for the duration of the massive treatment and then refine this estimate while the process is in progress. Thus the "mean constant" simulations, obtained with model 4, provide reasonable values, at least for small residual fertility, that can help to evaluate an average duration of the massive releases with and without mechanical control. However, this approach does not provide any information on the best period to start the SIT treatment to reduce the duration of the massive releases and, thus, optimize the sterile males production.

Based on the average value given by model 4, we can estimate, roughly at least, the duration and the amount production of sterile males needed for the massive releases to reduce the nuisance. In general, the amount of sterile males to produce is considerable. However, all along the treatment, the size of the massive releases can be adapted to the wild male population, using Mark-Release-Recapture experiments, as well as the periodicity of the releases, like in [5, 39].

Last, if the residual fertility is too large, say to 2%, then it is impossible to reduce (in a reasonable amount of time) the wild population under the given threshold, such that the wild population can be controlled with small releases of $\tau\Lambda_M = 20 \times 100$ individuals. The recommendation is thus to improve the sterilization process to have a residual fertility as small as possible, at least, less than 0.6%, for instance.

Our simulations took place in the context of nuisance reduction, i.e. to reduce the wild mosquito population in order to reduce the number of bites. It is not always necessary to reach this objective. In particular, in a tropical context, where people are used to mosquitoes. There, the most important goal is to reduce the epidemiological risk.

3.3 Reducing the epidemiological risk

In the previous simulations, we derive numerics to lower the mosquito population under a given release threshold for sterile males, for instance, 100 Ind/ha/week. As explained, in a tropical context, another option is to reduce the population in order to reduce the epidemiological risk, to prevent the risk of an epidemic. Since dengue is often circulating in La Réunion, we can couple our entomological model with a dengue model, like the one developed in [40]. According to the epidemiological model developed in [40], and recalled in Appendix C, page

Table 2: **DENV** epidemiological constant parameter values [40]

Symbol	μ_h	η_h	N_h
Value	$\frac{1}{365 \times 78}$	1/7	2000
Unit	day ⁻¹	day ⁻¹	Ind

18, we derive the following formula for the SIT basic reproduction number

$$\mathcal{R}_{0,SIT}^2 = \frac{\nu_m}{\nu_m + \mu_F} \frac{B\beta_{mh}}{\mu_F} \frac{B\beta_{hm}}{\eta_h + \mu_h} \frac{F_S^*}{N_h}, \quad (12)$$

where F_S^* is the amount of susceptible adult females at the Disease Free Equilibrium (DFE) equilibrium, estimated according to the value taken by $\tau\Lambda_{Massive}$. In [40], the authors showed that F_S is either strictly positive or equal to zero, depending on the amount of sterile males released. The positive parameters μ_h and $1/\nu_h$ represent respectively the average human mortality rate and the average viremic period. Since no disease-induced mortality is considered, the total human population is supposed to be constant and equal to N_h . The average rate of mosquito bites per individual is denoted $B > 0$, and $\beta_{mh} > 0$ ($\beta_{hm} > 0$) is the probability of dengue transmission from an infected female mosquito (human) to a susceptible human (mosquito) during such an event. The positive parameter $\nu_m > 0$ is the extrinsic incubation rate (EIR). However, it is well known that the previous epidemiological parameters, B , ν_m , β_{hm} , and β_{mh} , are Temperature-dependent. Using results from [41], we consider the following transmission probability for an infected *Aedes albopictus* to transmit DENV-2, using a Lactin-1 function

$$\beta_{mh}(T) = \exp(\alpha \times T) - \exp\left(\alpha \times T_{max} - \frac{(T_{max} - T)}{\delta_T}\right),$$

with $\alpha = 0.20404$, $T_{max} = 37.354$, and $\delta_T = 4.89694$. The probability of transmission from humans to mosquitoes is negligible for "low" temperatures, increases linearly to one at a maximum temperature and remains at one for higher temperatures. Thus, following [42], we consider

$$\beta_{hm}(T) = \frac{T^7}{T^7 + \beta_h^7},$$

with $\beta_h = 18.9871$. Last but not least, the EIP (Extrinsic incubation Period) decreases according to the temperature. Using again [41], we derive the following interpolation:

$$\nu_m(T) = aT^2 + bT + c,$$

with $a = -0.001$, $b = 0.0670$, and $c = -0.866$. All other (epidemiological) parameters are supposed to be constant.

Finally, following [19][Table A in the supplementary material], we consider the following Brière function for the biting rate B :

$$B(T) = c \times T \times (T - T_{min}) \sqrt{T_{max} - T},$$

where $c = 1.93e - 04$, $T_{min} = 10.25$, and $T_{max} = 38.32$ are the parameters related to *Aedes albopictus* mosquito.

The threshold \mathcal{R}_{0,SIT_c}^2 is related to the long-time behavior of the system. For practical purpose, we will consider \mathcal{R}_{eff} , the effective reproduction number, that is defined as follow

$$\mathcal{R}_{eff}(t) = \frac{\nu_m(t)}{\nu_m(t) + \mu_F(t)} \frac{B(t)^2 \beta_{mh}(t) \beta_{hm}(t) F_S(t)}{\mu_F(t) (\eta_h + \mu_h) N_h}. \quad (13)$$

In fact, assuming that t_{DENV} is the time where a DENV virus starts circulating, we will estimate \mathcal{R}_{eff} at time t_{DENV} . Clearly, if $\mathcal{R}_{eff}(t_{DENV}) < 1$ and $\mathcal{R}_{0,SIT_c}^2 < 1$, then no epidemics will occur. In contrary, even if $\mathcal{R}_{0,SIT_c}^2 < 1$ but $\mathcal{R}_{eff}(t_{DENV}) > 1$ then an outbreak may occur.

In the forthcoming simulations, we will estimate the time needed to lower \mathcal{R}_{eff} below 0.5 for different sizes of massive releases, i.e. 6000 or 12000 sterile males per ha, and for different residual fertility, with and without mechanical control. Thus, it suffices to find t^* such that the wild female population verifies

$$F(t^*) < \frac{\nu_m(t^*) + \mu_F(t^*)}{\nu_m(t^*)} \frac{\mu_F(t^*) (\eta_h + \mu_h) N_h}{B(t^*)^2 \beta_{mh}(t^*) \beta_{hm}(t^*) 2}, \quad (14)$$

for a given N_h . For the numerical simulations, we will consider the parameters values given in Table 2, page 10.

Assume that the weekly release rate is $\tau\Lambda = 120000$ individuals. In Fig. 10, page 26, for a given SIT starting date, we compute the number of releases necessary to reach $\mathcal{R}_{eff}(t^*) < 0.5$ for the four models, like in the

nuisance reduction case. However, contrary to the nuisance reduction case, the results between model 1 and model 3 are quite different, while the results obtained with model 2 are more homogeneous and look like periodic, varying between 19 and 31 weeks. With model 4, with constant average parameters, between 29 and 31 weeks are necessary to decrease the epidemiological risk, depending on residual fertility. Contrary to the nuisance reduction case, the impact of residual fertility is low: see Fig. 10(b)-(c). At some point this is a very good news. A special case occurs: end of November 2020, where the wild initial population is so small that, for model 1, no release is necessary. If we assume $\tau\Lambda = 240000$ individuals, we derive Fig. 11, page 27. There is no substantial change thanks to the case $\tau\Lambda = 120000$, only a gain in the amount of releases, for instance 7 weeks for model 4, and only in periods where the wild population is very large (2010, 2011, for instance). Again, the impact of the residual fertility is negligible. Last, we focus on simulations derived with model 1, when residual fertility and mechanical control occurs: see Fig. 12, page 28.

As expected by the previous simulations, there is no impact of the residual fertility on the amount of releases. In fact, we can even consider larger residual fertility, for instance 5%: see Fig. 13, page 29. Like for the other residual fertility cases, the duration of SIT releases increases only within periods (of the year) where the wild population is large, while there is almost no impact of the residual fertility in periods where the population is small. In fact, the female population size to reach to get $\mathcal{R}_{eff} < 0.5$, given in (14), is so small that it is always above the lower bound given in (8), page 5, i.e. $F(t^*) > F_l^*$. This is very important to have in mind: if from time to time the residual fertility may change thanks to issues during the ionization process, our results show that this may not impact the objective of reducing the epidemiological risk.

However, like in the nuisance reduction case, mechanical control may have an impact, but only in periods where the mosquito population is large, i.e. when rainfall is abundant: the amount of releases can be divided by a factor 2. Otherwise, when the population is small (from September to December in general), SIT alone, with massive releases, could work. Thanks to Fig. 12 and Fig. 13, the larger the residual fertility, the more useful the mechanical control during the rainy season.

Of course, once $\mathcal{R}(t^*) < 0.5$ is reached, it will be necessary to continue to release enough sterile males to maintain $\mathcal{R}(t^*)$ below 0.5, as long as needed: the smaller the wild population after the massive releases, the smaller the releases to keep $\mathcal{R}(t^*) < 0.5$. This can be evaluated through numerical simulations.

Remark 2. *In fact for this particular objective of reducing the epidemiological risk, and because in La Réunion we have some seasonality, the meaningful strategy, as already proposed in [10, Fig.4], would be to consider massive releases only over the wet period to maintain the mosquito population at a level corresponding to the population size during the dry period, the Austral winter, where, in general, the epidemiological risk is low because the vector population is low, except, of course, when rainfalls occur during this period, like in 2010 and 2011. Thus, we would have a "massive and stop" SIT strategy, contrary to the nuisance reduction where a "massive and small" releases strategy seems more appropriate. Thus, according to the temperature and rainfall dependent model, massive releases could only occur from October-November to May-June, that is over 8 months, with, eventually, a reduction of the size of the releases, using, for instance, a closed-loop control strategy [5, 39].*

4 Conclusion

We have built a minimalistic rainfall-temperature entomological model to derive the dynamics of *Aedes albopictus* population in the place of Duparc (Sainte-Marie), La Réunion island. Since we are in a sub-tropical environment, our simulation shows that rainfall definitively plays a great role in the dynamics of the mosquito population, with rapid decay or growth. In fact, it seems that they are periods where the mosquito dynamics are mainly driven by temperature, while in other periods the dynamic is more driven by rainfall. Other approaches, based either on constant (model 4), temperature-dependent (model 2) or rainfall-dependent parameter values (model 3), provide similar results on average. However, they are not always satisfactory enough to be an "accurate" alternative, except model 3 when residual fertility is not too large.

Quality control within SIT is an important issue: if it fails, then release cannot occur. Within the quality control, we focus on residual fertility. We show that it may have an important impact on SIT duration and, eventually on its efficacy. In nuisance reduction, the lower the residual fertility, the lower the number of massive releases needed to switch from a massive releases strategy to a small releases strategy. However our results show that the massive releases duration for "high" residual fertility can greatly vary depending if the model takes into account the temperature, the rainfall or both. While the constraint $\varepsilon < 1/\mathcal{N}$ is needed for elimination, it is not necessary to reduce the epidemiological risk.

When SIT is considered, coupled or not with Mechanical control, we recommend starting the releases of sterile males within a period that last from July to December, when the mosquito population is, in general, at its lowest. However, the duration of the SIT treatment or the number of periodic releases, constant in size, of sterile males may vary thanks to the environmental parameters.

Clearly, combining Mechanical control with SIT is strongly recommended, in particular when the SIT treatment starts within a humid year: see for instance the years 2010 and 2011 where the dry period was more rainy than usual.

The massive and small releases strategy is only useful to reduce substantially the nuisance due to mosquitoes, i.e. to reach nearly elimination and to maintain the population under a certain level, related, here, with the number of sterile male individuals considered in the small releases strategy. If the objective of SIT control is only to reduce the epidemiological risk, i.e. $\mathcal{R}_{eff} < 0.5$, then the duration of the SIT treatment, with massive releases, will be short compared to elimination. In addition, having non-zero residual fertility, with $\varepsilon > 1/\mathcal{N}$, seems to be less problematic to reach $\mathcal{R}_{eff} < 0.5$, than to reach elimination. From a practical point of view, this can be very convenient. However, once $\mathcal{R}_{eff} < 0.5$ or elimination is reached, it will be necessary to continue to release a sufficient amount of sterile males in order to keep the wild population under a certain threshold. At this stage, a closed-loop control (taking into account feedback from the system, like the size of the mosquito population through Mark Release and Recapture experiments) can be used from time to time, in order to reduce the overall cost, as described in [5,39]. Whatever the objective, i.e. nuisance reduction or lower the epidemiological risk, it is better to have a residual fertility as small as possible in order to gain in the amount of sterile males to release, in the number of releases, and, thus, in sterile insects production.

Our model, while minimalistic from the variables and parameters point of view, captures relatively well the dynamics of the *Aedes albopictus* population throughout the year, without too many details. However, as with all models, improvements can be made. For instance, by taking into account the migration of males and females from neighboring places. Indeed, we have considered our area closed, in the sense that no external mosquitoes invade the treated area. Migration is another major concern in SIT treatment. We recently showed that if migration is small, SIT can be performed [6]. Otherwise, it is necessary to isolate the target domain. This is not easy with mosquitoes because, so far, no (killing) attractant is efficient.

The main objective of SIT is to reduce the wild population, and in particular the wild females, because they are those who transmit diseases, like Dengue. So far, in our model, we assumed that no sterile females are released. In fact, we know that this is not the case: there is always a percentage of sterile females that are released. In [40], outside an epidemic period, we show that releasing sterile females is not an issue. Within an epidemic period, releasing sterile females is not an issue as long as the sterile females release rate is lower than a given threshold, Λ_F^{crit} , as estimated in [40]. In particular, this sterile females threshold was estimated with constant parameters values and we know that it depends on $\mu_{A,2}$ and \mathcal{R}_0^2 . Thus, according to our parameters variations, it is more than certain that the sterile females release rate threshold will vary greatly, such that the releases of sterile females will be more problematic in periods, when the wild population is small and the epidemiological risk is (very) low. If, in the past, only less than 5% of sterile females was acceptable [43], this is not the case now. IAEA recommends not to release more than 1% of sterile females. This is part of the control quality process. Thus, following [40], accidental releases of females could be taken into account, in order to derive how they could impact the SIT releases strategy, to reduce the epidemiological risk. Most certainly, there will be an impact in the duration of the releases, i.e. an increase, such that it will be necessary to adapt the releases strategy.

Last, of course, it would be more than interesting to compare our SIT duration estimates with real (entomological and epidemiological) data recorded during a whole SIT campaign.

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5 Appendix A: Parameters values

See Table 3, page 15, and Table 4, page 15.

Table 3: Entomological parameters of *Aedes albopictus* at different temperatures (from [9])

Symbol	Name	T=15°	T=20°	T=25°	T=30°	T=35°
r_{viable}	Proportion of viable eggs (E-L1)	8.2	66.9	49.2	51.4	10
N_{eggs}	Number of eggs deposited	0	50.8	65.3	74.2	48.7
τ_{gono}	Duration of the gonotrophic cycle	NA	8.1	3.1	3.9	1.3
τ_A	Time from hatching to emergence	35	14.4	10.4	8.8	12.3
s_A	Survivorship from larva first instar to adult	50	77.5	76.3	67.5	2.5
τ_M	Adult male half-life	15.45	10.25	9.6	8.55	7.4
τ_F	Adult female half-life	19.65	15.15	15.3	16.9	10

Table 4: Parameter values for system (2) deduced from Table 3, page 15

Symbol	Name	Formula	mean value at 15°	mean value at 20°	mean value at 25°	mean value at 30°	mean value at 35°
ϕ	Effective fecundity	$\frac{r_{viable}N_{eggs}}{\tau_{gono}}$	0	4.1957	10.3637	9.7792	3.7462
$\mu_{A,1}$	Aquatic death rate	$-\frac{\log(s_A)}{\tau_A}$	0.0198	0.0177	0.0260	0.0447	0.2999
ν_A	Aquatic to adult transition rate	$\frac{1}{\tau_A}$	0.0286	0.0694	0.0962	0.1136	0.0813
μ_M	Adult male death rate	$\frac{\log(2)}{\tau_M}$	0.0449	0.0676	0.0722	0.0811	0.0937
μ_F	Adult female death rate	$\frac{\log(2)}{\tau_F}$	0.0353	0.0458	0.0453	0.0413	0.0693

The formula given in Table 4 are similar to those given in [32]. Let us explain how we deduce μ_M from τ_M . Since τ_M is the adult-male half-life, it means that half of the population has disappeared in τ_M days. Then, assuming that the dynamic of adult males follows an exponential law, i.e. $x(t) = x(0)e^{-\mu_M t}$, it is straightforward to deduce that μ_M is solution of $\frac{1}{2} = e^{-\mu_M \times \tau_M}$, that is $\mu_M = \frac{\log 2}{\tau_M}$. The other parameter values follow the same reasoning.

6 Appendix B: Equilibria

We are looking for the positive equilibria with and without SIT releases:

- Without SIT releases.

In the case of constant coefficients, the equilibria of System (2) are 0 and

$$\begin{cases} A^* = \frac{\gamma + \mu_{A,1}}{\mu_{A,2}}(\mathcal{N} - 1), \\ M^* = \frac{(1-r)\gamma A^*}{\mu_M} = Q(\mathcal{N} - 1), \\ F^* = \frac{r\gamma A^*}{\mu_F}, \end{cases} \quad (15)$$

where $Q = \frac{(1-r)\gamma(\gamma + \mu_{1,A})}{\mu_{2,A}\mu_M}$.

- With SIT releases.

In the case of constant coefficients, some calculations are needed to find the release threshold, $M_{T_1,\varepsilon}$ and also to derive the equilibria. We have to solve

$$\begin{cases} \phi F = (\gamma + \mu_{1,A} + \mu_{2,A}A)A, \\ (1-r)\gamma A = \mu_M M, \\ \frac{M + \varepsilon\beta M_T}{M + \beta M_T} r\gamma A = \mu_F F. \end{cases}$$

Using the first and the third equalities leads to

$$\frac{M + \varepsilon\beta M_T}{M + \beta M_T} r\gamma = \frac{\mu_F}{\phi} (\gamma + \mu_{1,A} + \mu_{2,A}A),$$

and using the fact that

$$M = \frac{(1-r)\gamma}{\mu_M} A,$$

we have

$$\frac{(1-r)\gamma A + \varepsilon\mu_M\beta M_T}{(1-r)\gamma A + \mu_M\beta M_T} r\gamma = \frac{\mu_F}{\phi} (\gamma + \mu_{1,A} + \mu_{2,A}A),$$

that is

$$r\gamma\phi((1-r)\gamma A + \varepsilon\mu_M\beta M_T) = \mu_F((1-r)\gamma A + \mu_M\beta M_T)(\gamma + \mu_{1,A} + \mu_{2,A}A),$$

leading to second order polynomial

$$\begin{aligned} \mu_F(1-r)\gamma\mu_{2,A}A^2 + [\mu_F(1-r)\gamma(\gamma + \mu_{1,A}) + \mu_F\mu_M\beta M_T\mu_{2,A} - r\gamma\phi(1-r)\gamma]A \\ + \mu_F\mu_M\beta M_T(\gamma + \mu_{1,A}) - r\gamma\phi\varepsilon\mu_M\beta M_T = 0 \end{aligned}$$

$$\begin{aligned} (1-r)\gamma\mu_{2,A}A^2 + \left[(1-r)\gamma(\gamma + \mu_{1,A}) + \mu_M\beta M_T\mu_{2,A} - \frac{r\gamma\phi}{\mu_F}(1-r)\gamma \right]A \\ + \mu_M\beta M_T(\gamma + \mu_{1,A}) - \frac{r\gamma\phi}{\mu_F}\varepsilon\mu_M\beta M_T = 0 \end{aligned}$$

$$\begin{aligned} (1-r)\gamma\mu_{2,A}A^2 + [(1-r)\gamma(\gamma + \mu_{1,A})(1-\mathcal{N}) + \mu_M\beta M_T\mu_{2,A}]A \\ + \mu_M\beta M_T(\gamma + \mu_{1,A})(1-\varepsilon\mathcal{N}) = 0, \end{aligned}$$

or equivalently

$$\frac{(1-r)\gamma}{\mu_M}A^2 - [Q(\mathcal{N} - 1) - \beta M_T]A + \beta M_T\frac{(\gamma + \mu_{1,A})}{\mu_{2,A}}(1 - \varepsilon\mathcal{N}) = 0,$$

that is, using (15),

$$\frac{(1-r)\gamma}{\mu_M}A^2 - [M^* - \beta M_T]A + \beta M_T\frac{(\gamma + \mu_{1,A})}{\mu_{2,A}}(1 - \varepsilon\mathcal{N}) = 0. \quad (16)$$

We compute the discriminant of the last equation

$$\Delta(\varepsilon) = [M^* - \beta M_T]^2 - 4Q\beta M_T(1 - \varepsilon\mathcal{N}).$$

We will distinguish three cases:

– Assume $\varepsilon > 1/\mathcal{N}$, then $\Delta(\varepsilon) > 0$, such that there always exists one positive equilibrium

$$A_\varepsilon^* = \mu_M \frac{M^* - \beta M_T + \sqrt{\Delta(\varepsilon)}}{2(1-r)\gamma}.$$

After straightforward computations, we can show that whatever the size of the massive releases, the aquatic equilibrium is bounded from below by

$$2 \frac{\varepsilon \mathcal{N} - 1}{\mathcal{N} - 1} A^*.$$

All other values, M_ε^* and F_ε^* , follow.

- Assume $\varepsilon = 1/\mathcal{N}$. Then $\Delta(\varepsilon) = 0$ iff $\beta M_T = M^*$. In fact if $\beta M_T > M^*$, then $A_\varepsilon^* = 0$.
- Assume $\varepsilon < 1/\mathcal{N}$. Setting $y = \beta M_T$, we derive

$$\begin{aligned} \Delta(\varepsilon) &= [Q(\mathcal{N} - 1) - y]^2 - 4Q(1 - \varepsilon \mathcal{N})y \\ &= y^2 - 2Q((\mathcal{N} - 1) + 2(1 - \varepsilon \mathcal{N}))y + (Q(\mathcal{N} - 1))^2 \end{aligned}$$

The discriminant of the equation $\Delta(\varepsilon) = 0$ following the variable y is given by

$$\begin{aligned} \delta(\varepsilon) &= (2Q)^2((\mathcal{N} - 1) + 2(1 - \varepsilon \mathcal{N}))^2 - (2Q(\mathcal{N} - 1))^2 \\ &= 16(1 - \varepsilon \mathcal{N})(1 - \varepsilon)Q^2\mathcal{N}. \end{aligned}$$

Since $\varepsilon < 1/\mathcal{N}$, then $\delta(\varepsilon) > 0$, and we obtain two roots

$$\beta M_{T_1, \varepsilon} = Q \left(\mathcal{N} + 1 - 2\varepsilon \mathcal{N} - 2\sqrt{(1 - \varepsilon \mathcal{N})(1 - \varepsilon)\mathcal{N}} \right)$$

and

$$\beta M_{T_2, \varepsilon} = Q \left(\mathcal{N} + 1 - 2\varepsilon \mathcal{N} + 2\sqrt{(1 - \varepsilon \mathcal{N})(1 - \varepsilon)\mathcal{N}} \right).$$

When $\varepsilon = 0$, we recover the result obtained in [4]

$$\beta M_{T_1, 0} = Q \left(\sqrt{\mathcal{N}} - 1 \right)^2.$$

Assume $0 < \varepsilon < \frac{1}{\mathcal{N}}$. Then, when $0 < M_T < M_{T_1, \varepsilon}$, we have $\Delta(\varepsilon) > 0$, and thus two equilibria

$$A_{1, \varepsilon} = \mu_M \frac{Q(\mathcal{N} - 1) - \beta M_T - \sqrt{[Q(\mathcal{N} - 1) - \beta M_T]^2 - 4Q\beta M_T(1 - \varepsilon \mathcal{N})}}{2(1-r)\gamma},$$

and

$$A_{2, \varepsilon} = \mu_M \frac{Q(\mathcal{N} - 1) - \beta M_T + \sqrt{[Q(\mathcal{N} - 1) - \beta M_T]^2 - 4Q\beta M_T(1 - \varepsilon \mathcal{N})}}{2(1-r)\gamma}.$$

Since

$$\begin{aligned} A_{1, \varepsilon} + A_{2, \varepsilon} &= \frac{\mu_M}{2(1-r)\gamma} (Q(\mathcal{N} - 1) - \beta M_T) \\ &> \frac{\mu_M}{2(1-r)\gamma} (Q(\mathcal{N} - 1) - \beta M_{T_1, \varepsilon}) \\ &= \frac{\mu_M}{2(1-r)\gamma} \left(Q \left(2\varepsilon \mathcal{N} + 2 \left(\sqrt{(1 - \varepsilon \mathcal{N})(1 - \varepsilon)\mathcal{N}} - 1 \right) \right) \right). \end{aligned}$$

We remark that

$$(1 - \varepsilon \mathcal{N})(1 - \varepsilon)\mathcal{N} - 1 = \mathcal{N} - 1 - (\mathcal{N} + 1)\varepsilon + \mathcal{N}\varepsilon^2.$$

The discriminant of the last polynomial in ε is given by

$$\Delta_\varepsilon = (\mathcal{N} + 1)^2 - 4\mathcal{N}(\mathcal{N} - 1) = -3\mathcal{N}^2 + 6\mathcal{N} + 1$$

In general, \mathcal{N} is large, i.e. $\mathcal{N} \gg 1 + \frac{2}{\sqrt{3}}$, such that $\Delta_\varepsilon < 0$, such that the ε -polynomial is always positive. Then $A_{1, \varepsilon} + A_{2, \varepsilon} > 0$. Moreover, since the last term in (16), we have also $A_{1, \varepsilon} A_{2, \varepsilon} > 0$. Thus the two roots $A_{1, \varepsilon}$ and $A_{2, \varepsilon}$ are positive. Therefore the system has two equilibria $\mathbf{E}_{1,2} = (A_{1,2}, M_{1,2}, F_{1,2})$ such that $\mathbf{0} \ll \mathbf{E}_1 \ll \mathbf{E}_2$.

In practice, we are, in general, in the case $\varepsilon < 1/\mathcal{N}$, see (11) and $\mathcal{N} > 1 + \frac{2}{\sqrt{3}}$.

Appendix C: The epidemiological Model We briefly recall the SIR-SEI model of dengue transmission, studied in [40], without taking into account the accidental releases of sterile females. The evolution of the human population is given by the following SIR model, with Susceptible, Infected, and Recovered compartments:

$$\begin{cases} \dot{S}_h = \mu_h N_h - B\beta_{mh}(T)F_I \frac{S_h}{N_h} - \mu_h S_h, \\ \dot{I}_h = B\beta_{mh}(T)F_I \frac{S_h}{N_h} - (\eta_h + \mu_h)I_h, \\ \dot{R}_h = \eta_h I_h - \mu_h R_h, \end{cases} \quad (17)$$

Extending the model of evolution of the mosquito population described in the previous sections, we use here a SEI model for the wild female mosquitoes, with Susceptible, Exposed and Infected compartments, adapted from (7):

$$\begin{cases} \frac{dA}{dt} = \phi(T)(F_S + F_E + F_I) - (\gamma(T) + \mu_{1,A}(T) + \mu_{A,2}(T, R)A) A, \\ \frac{dM}{dt} = (1 - r(T))\gamma(T)A - \mu_M(T)M, \\ \frac{dF_S}{dt} = r(T)\gamma(T)\frac{M + \varepsilon\beta M_S}{M + \beta M_S}A - B\beta_{mh}(T)F_S \frac{I_h}{N_h} - \mu_F(T)F, \\ \dot{F}_E = B\beta_{mh}(T)F_S \frac{I_h}{N_h} - (\nu_m(T) + \mu_F(T))F_E \\ \dot{F}_I = \nu_m(T)F_E - \mu_F(T)F_I. \end{cases} \quad (18)$$

where M_S is driven by (6). All parameters are described in the Table below

Table 5: **Description of the epidemiological and entomological parameters**

Symbol	Description	Unit
$1/\mu_h$	Average lifespan of human	Day
$1/\eta_h$	Average viremic period	Day
B	Daily average mosquito bites	Day ⁻¹
β_{mh}	Transmission probability from infected mosquito	-
β_{hm}	Transmission probability from infected human	-
ϕ	Number of eggs at each deposit per capita	Day ⁻¹
γ	Maturation rate from larvae to adult	Day ⁻¹
$\mu_{A,1}$	Density independent mortality rate of the aquatic stage	Day ⁻¹
$\mu_{A,2}$	Density dependent mortality rate of the aquatic stage	Day ⁻¹ Individuals ⁻¹
r	Sex ratio	-
$1/\nu_m$	Average extrinsic incubation period (EIP)	Day
$1/\mu_F$	Average lifespan of fertilized and eggs-laying females	Day
$1/\mu_M$	Average lifespan of males	Day

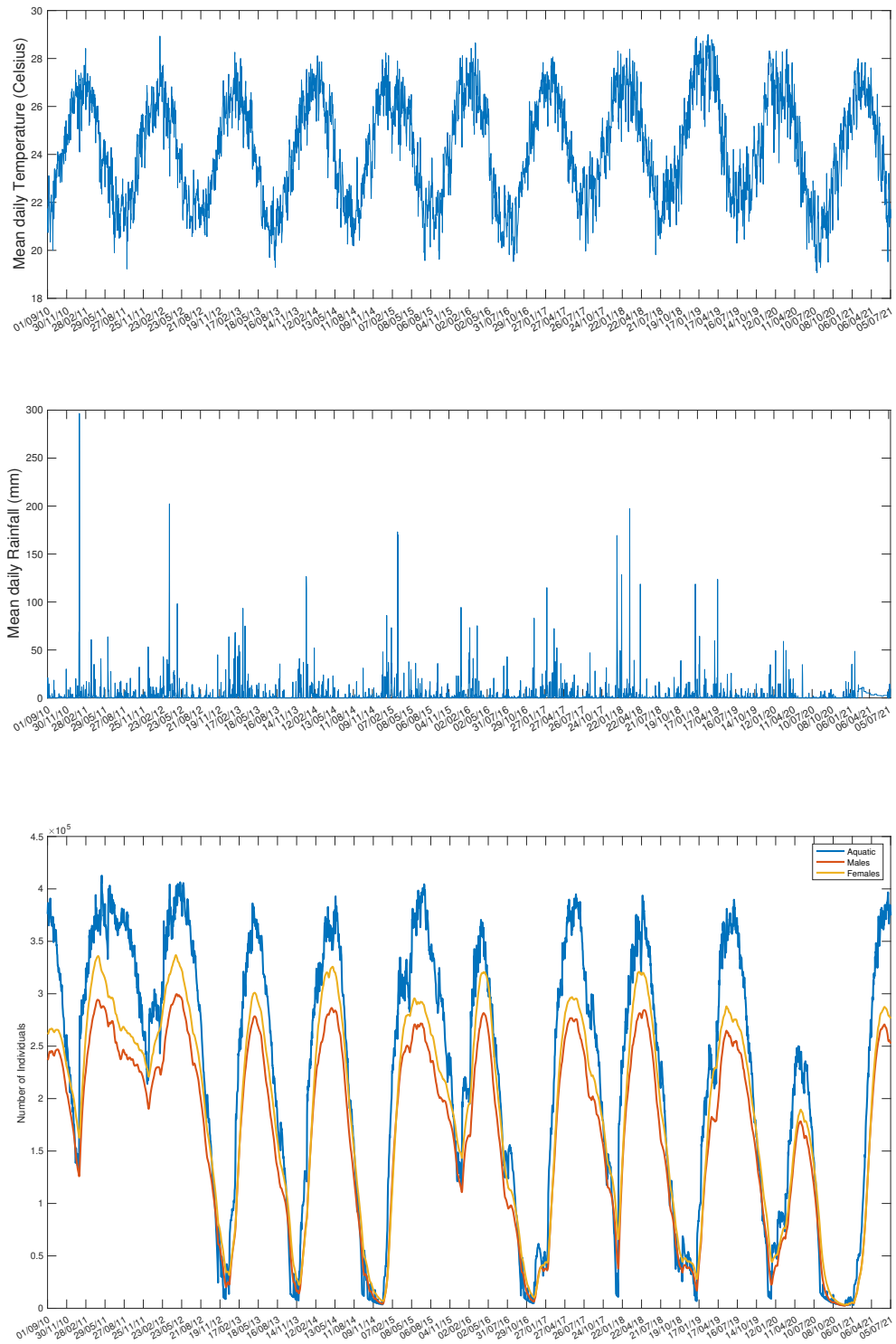


Figure 3: Temperature and rainfall dependent model: (a) Mean Daily Temperature (Celsius) - (b) Mean daily rainfall (mm) - (c) Mosquito population dynamics from the 1st of September 2010 until the 14th of July 2021

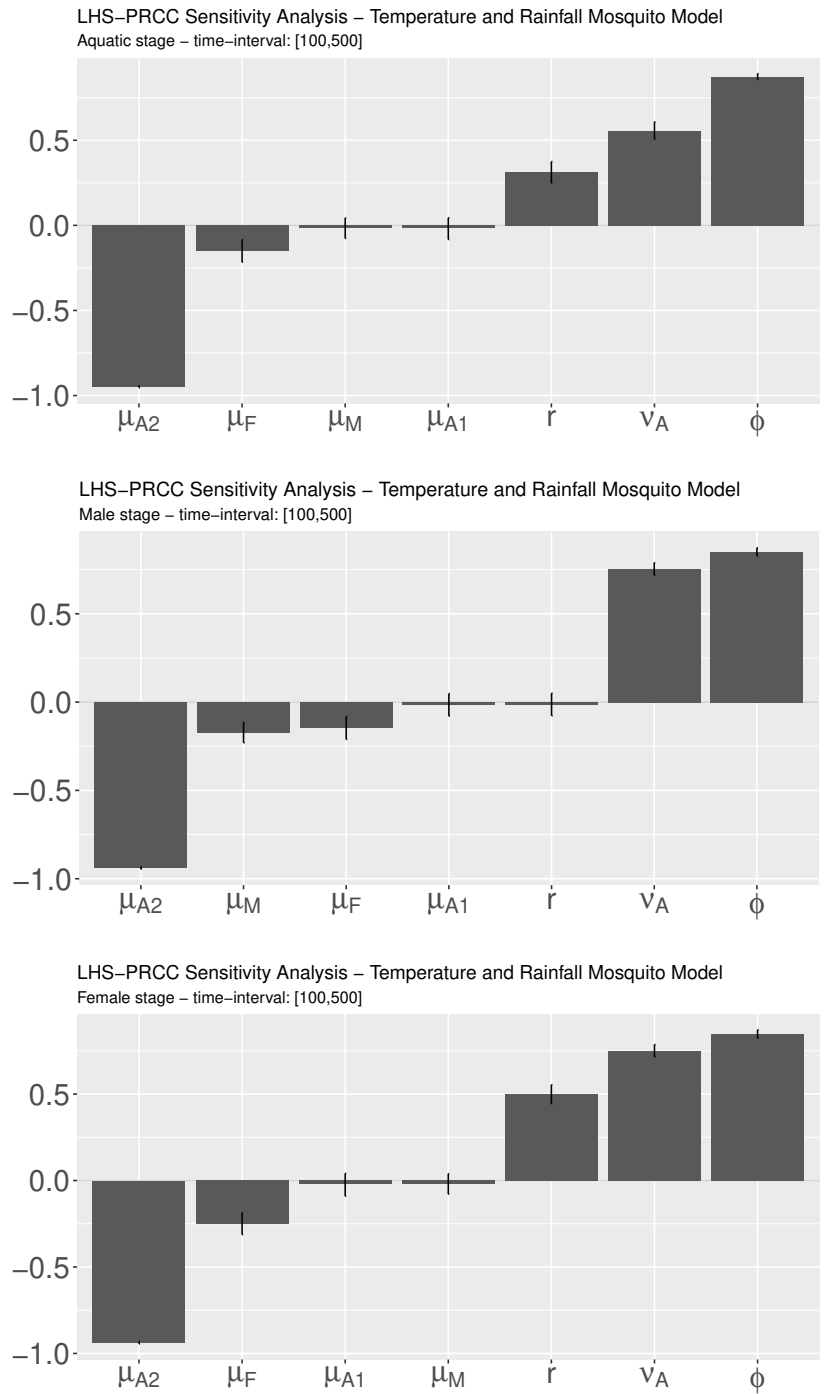


Figure 4: LHS-PRCC analysis of model (2)

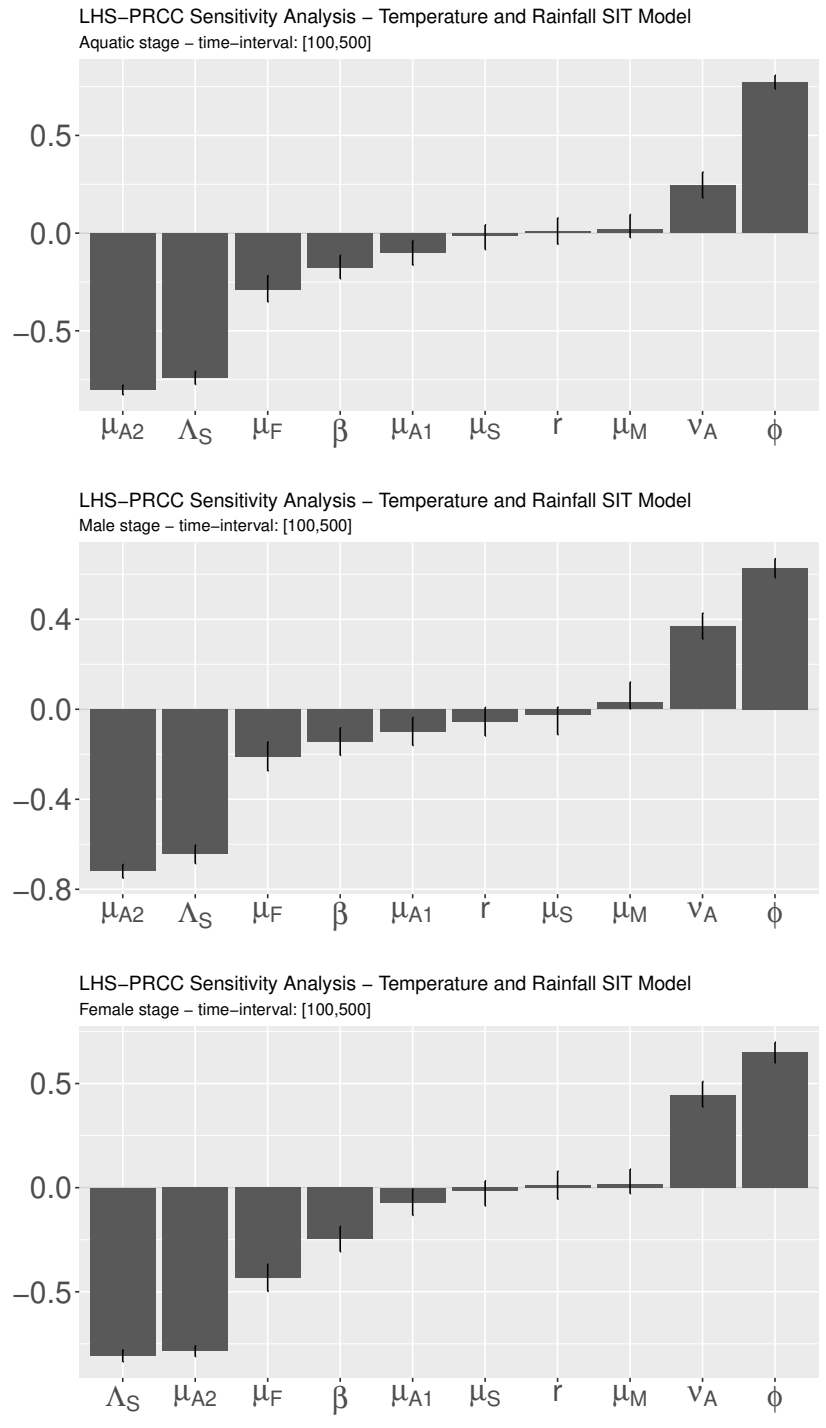


Figure 5: LHS-PRCC analysis of the SIT-model (7)

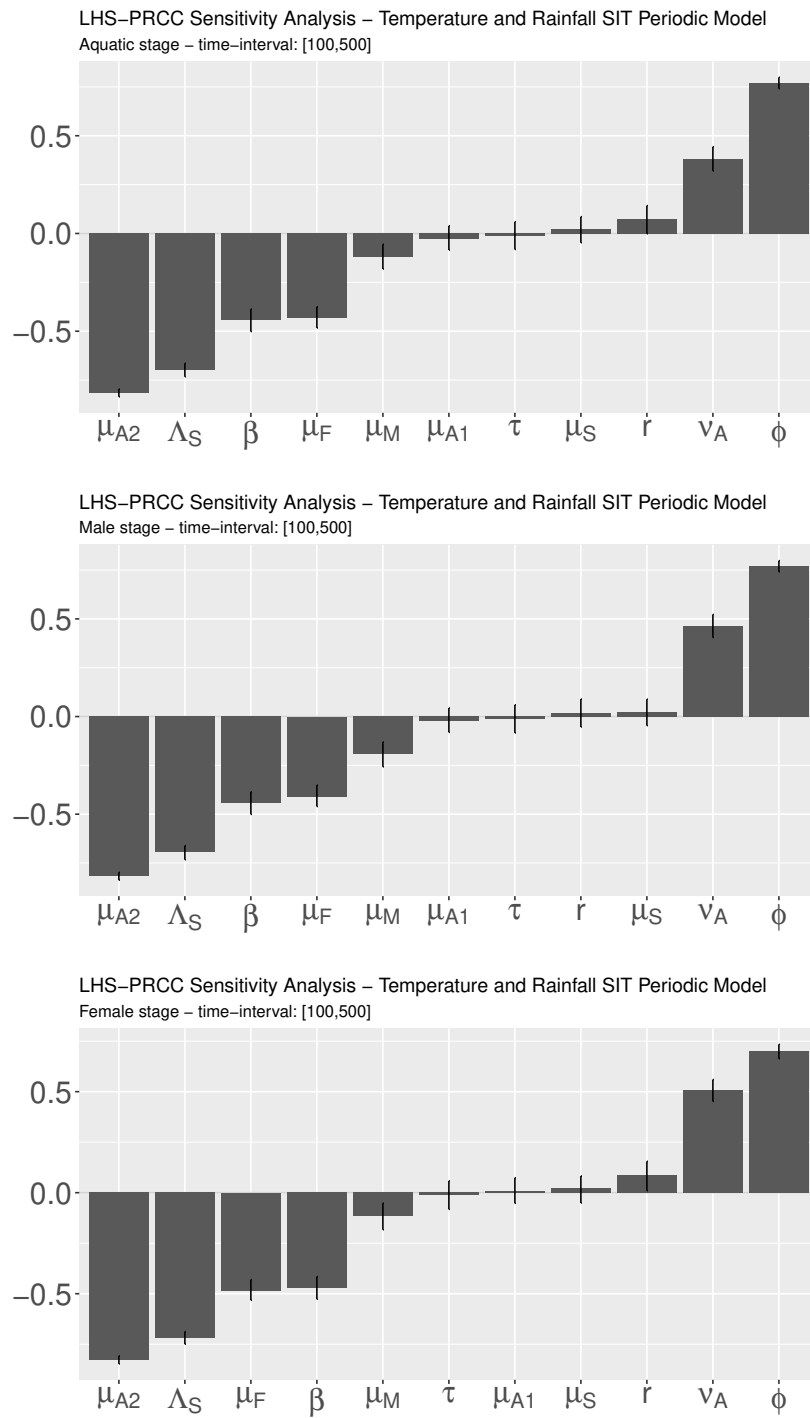


Figure 6: LHS-PRCC analysis of the SIT-model (7) with periodic releases

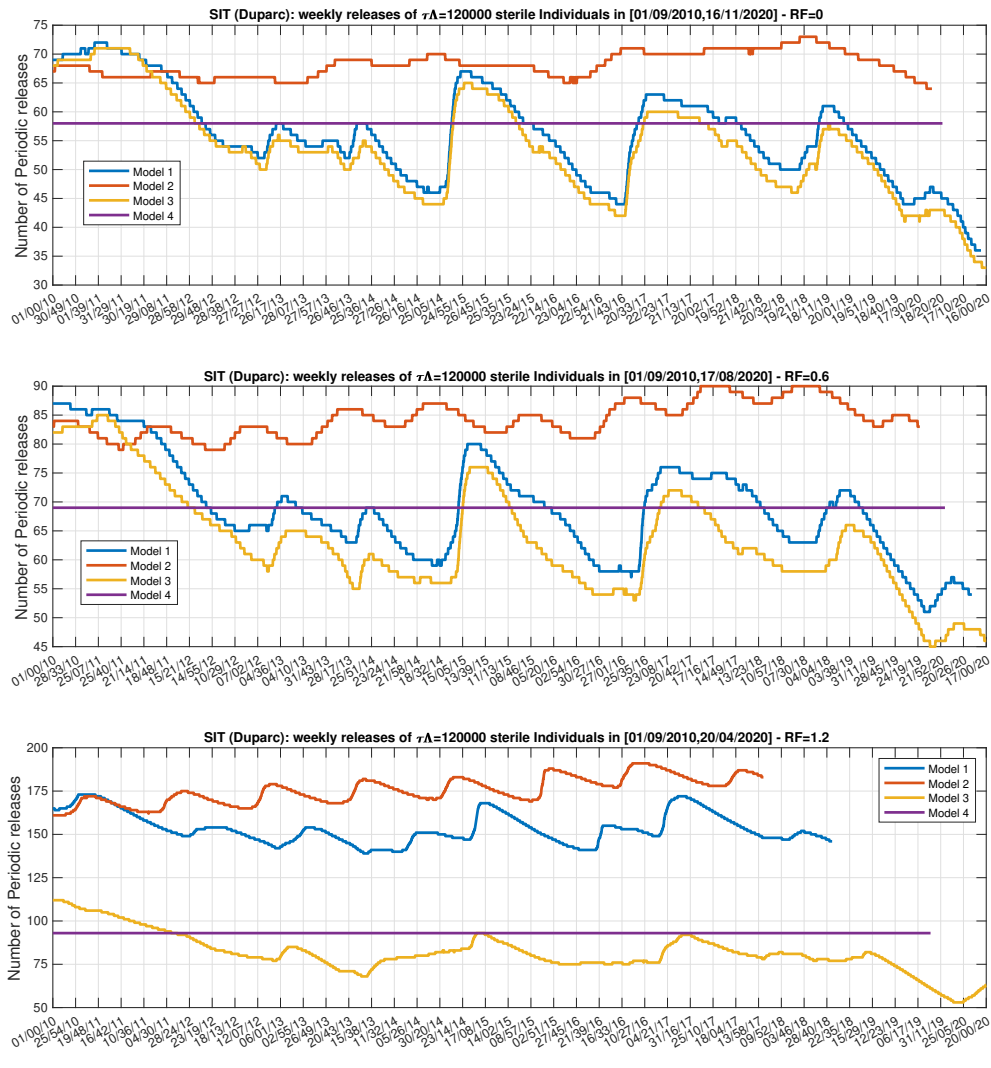


Figure 7: Comparison of the amount of weekly SIT releases calculated using the four models: (a) 0% of residual fertility; (b) 0.6% of residual fertility; (c) 1.2% of residual fertility without mechanical control - The weekly release rate is $\tau\Lambda = 120000$ Individuals

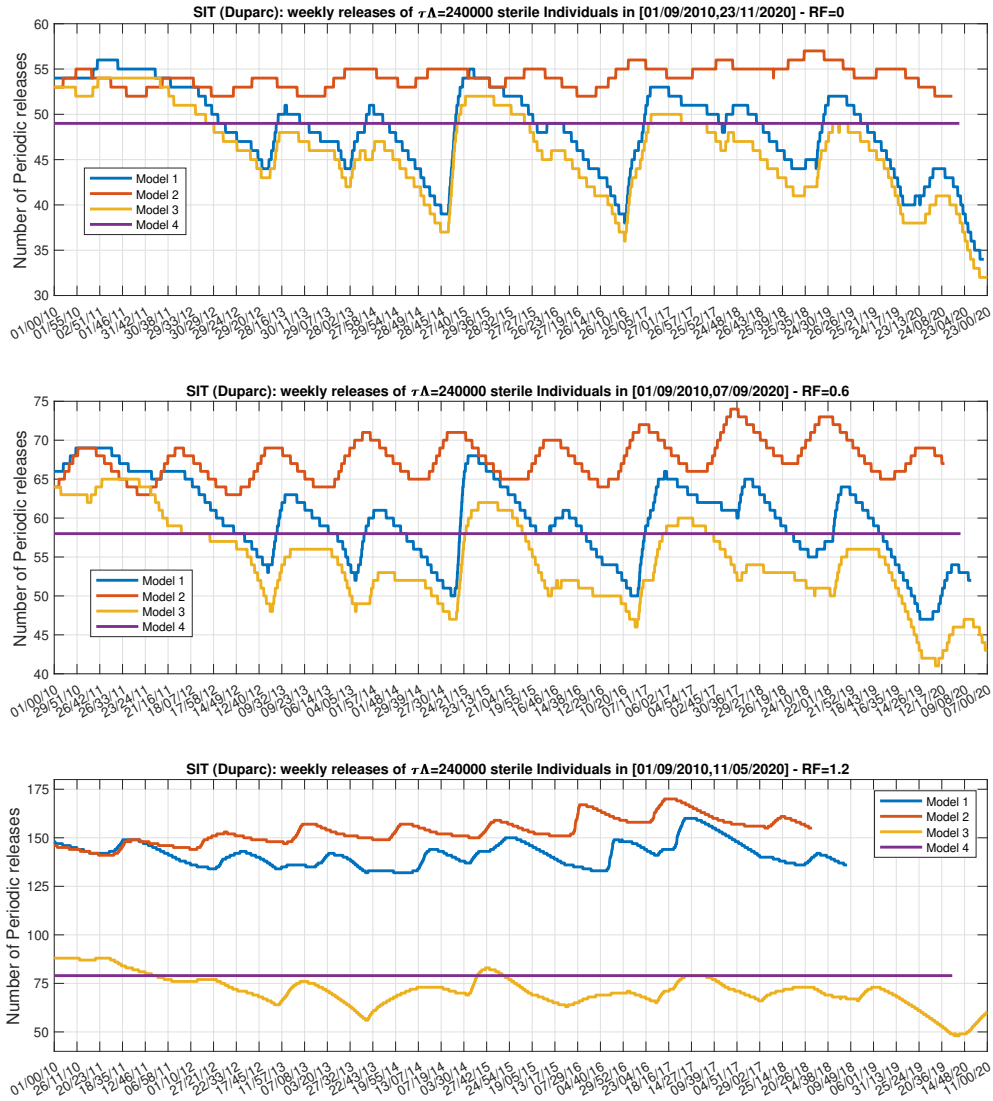


Figure 8: Comparison of the amount of weekly SIT releases calculated using the four models: (a) 0% of residual fertility; (b) 0.6% of residual fertility; (c) 1.2% of residual fertility without mechanical control - The weekly release rate is $\tau\Lambda = 240000$ Individuals.

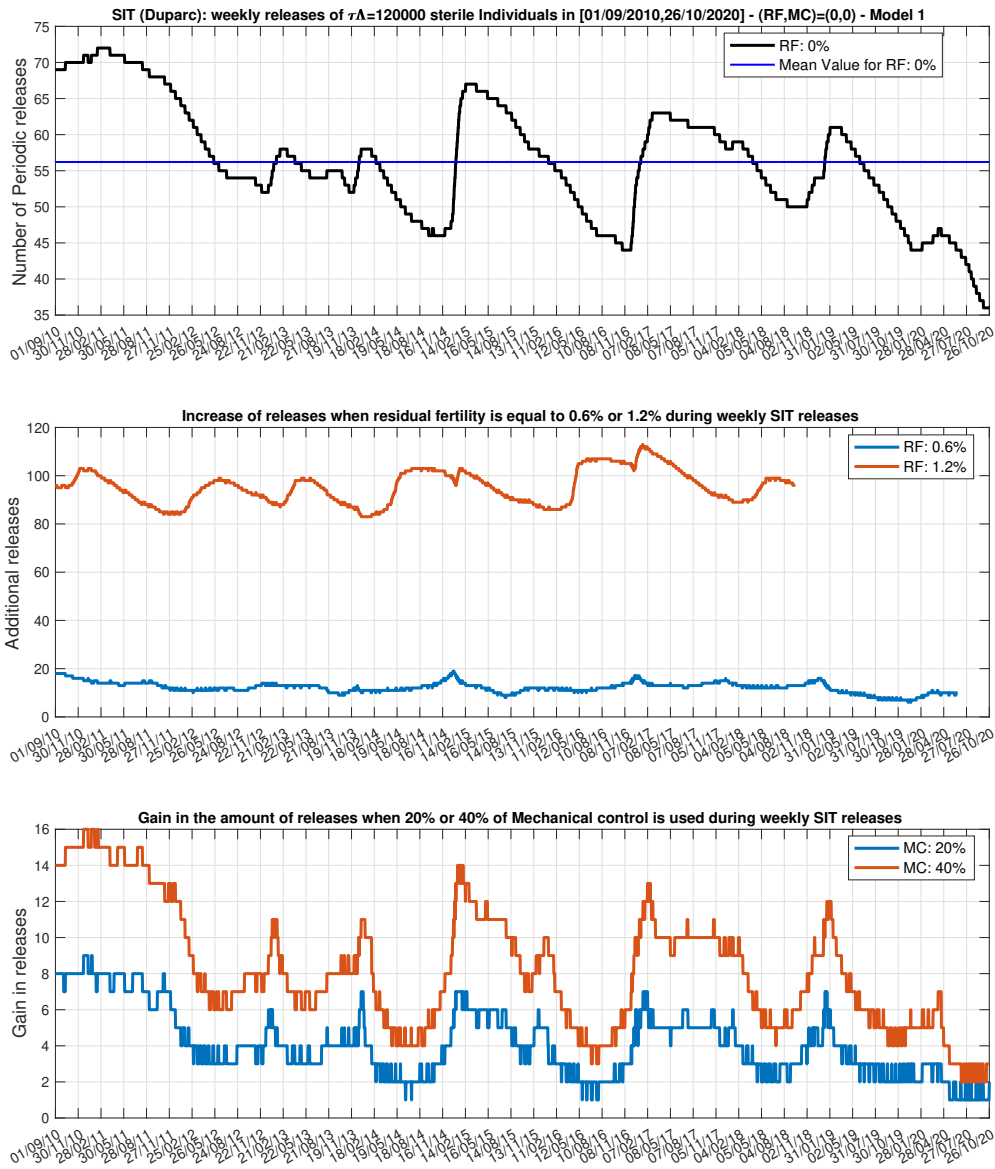


Figure 9: Simulations of Model 1 with $\tau\Lambda = 120000$ Individuals: (a) Variation of the amount of SIT releases; (b); Impact in terms of additional releases when 0.6% and 1.2% residual fertility occurs; (b) Gain in the releases when 20% and 40% of Mechanical control is used

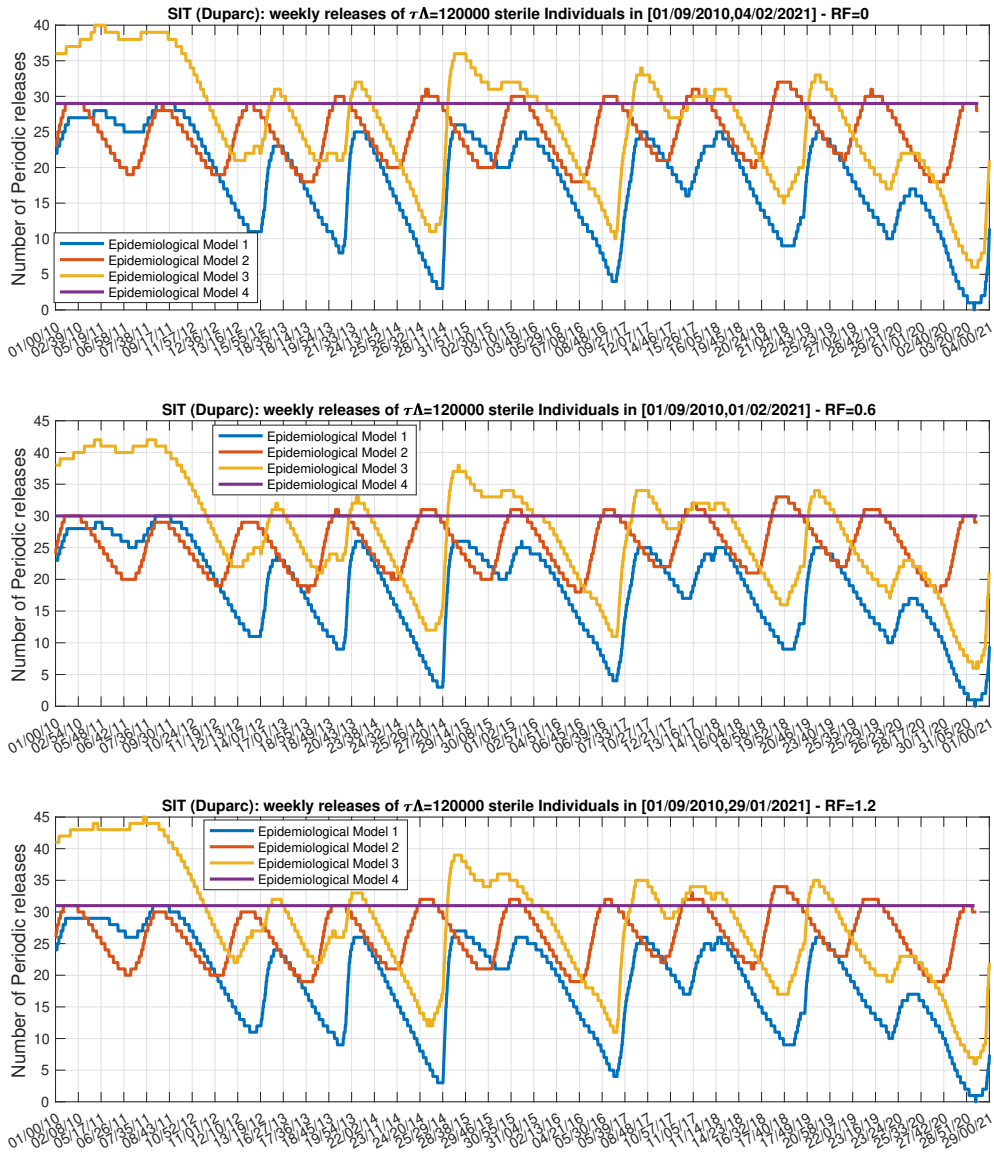


Figure 10: Reducing the epidemiological risk. Comparison of the amount of weekly SIT releases calculated using the four models: (a) 0% of residual fertility; (b) 0.6% of residual fertility; (c) 1.2% of residual fertility without mechanical control - The weekly release rate is $\tau\Lambda = 120000$ Individuals

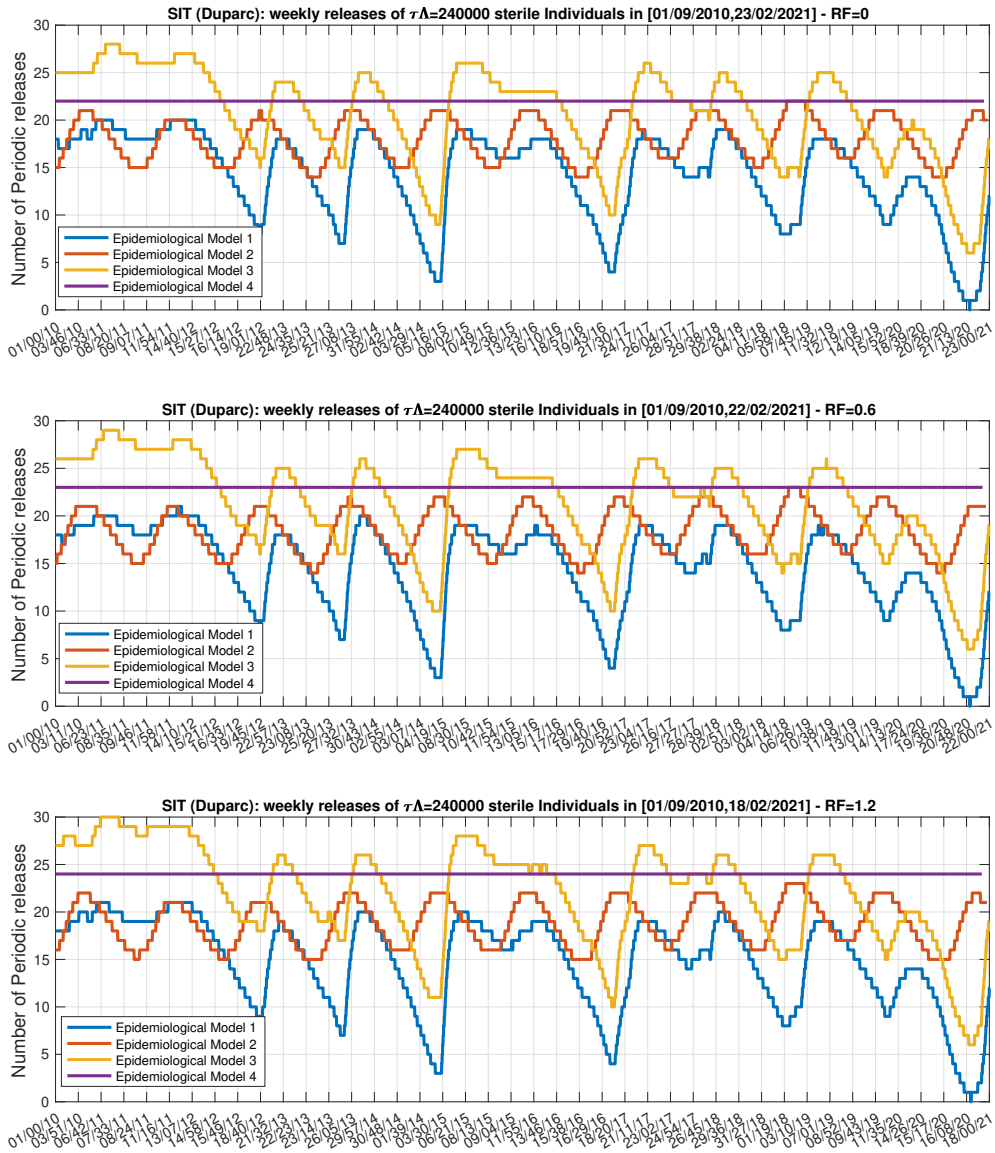


Figure 11: Reducing the epidemiological risk. Comparison of the amount of weekly SIT releases calculated using the four models: (a) 0% of residual fertility; (b) 0.6% of residual fertility; (c) 1.2% of residual fertility without mechanical control - The weekly release rate is $\tau\Lambda = 240000$ Individuals.

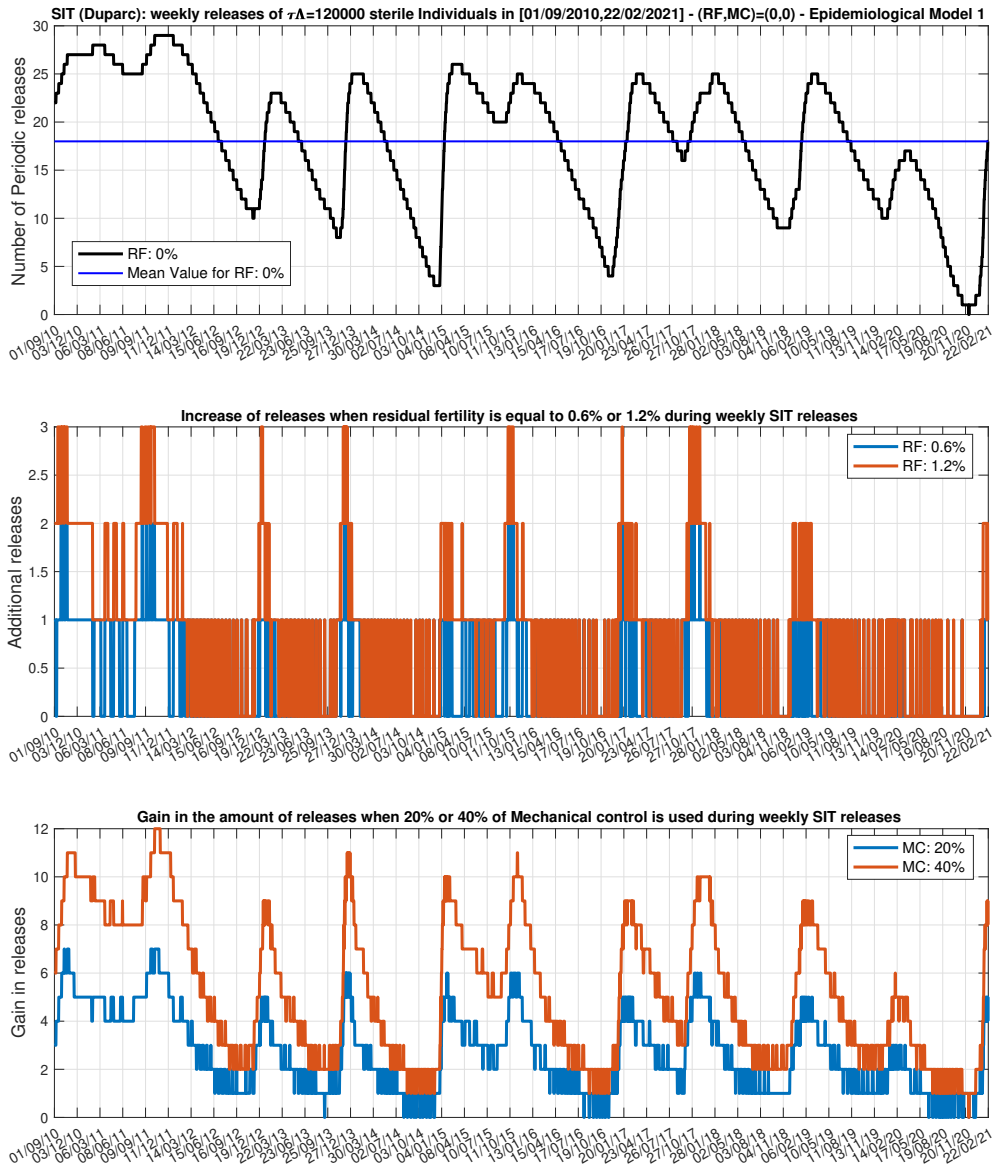


Figure 12: Reducing the epidemiological risk. Simulations of Model 1 with $\tau\Lambda = 120000$ Individuals: (a) Variation of the amount of SIT releases; (b); Impact in terms of additional releases when 0.6% and 1.2% residual fertility occurs; (b) Gain in the releases when 20% and 40% of Mechanical control is used

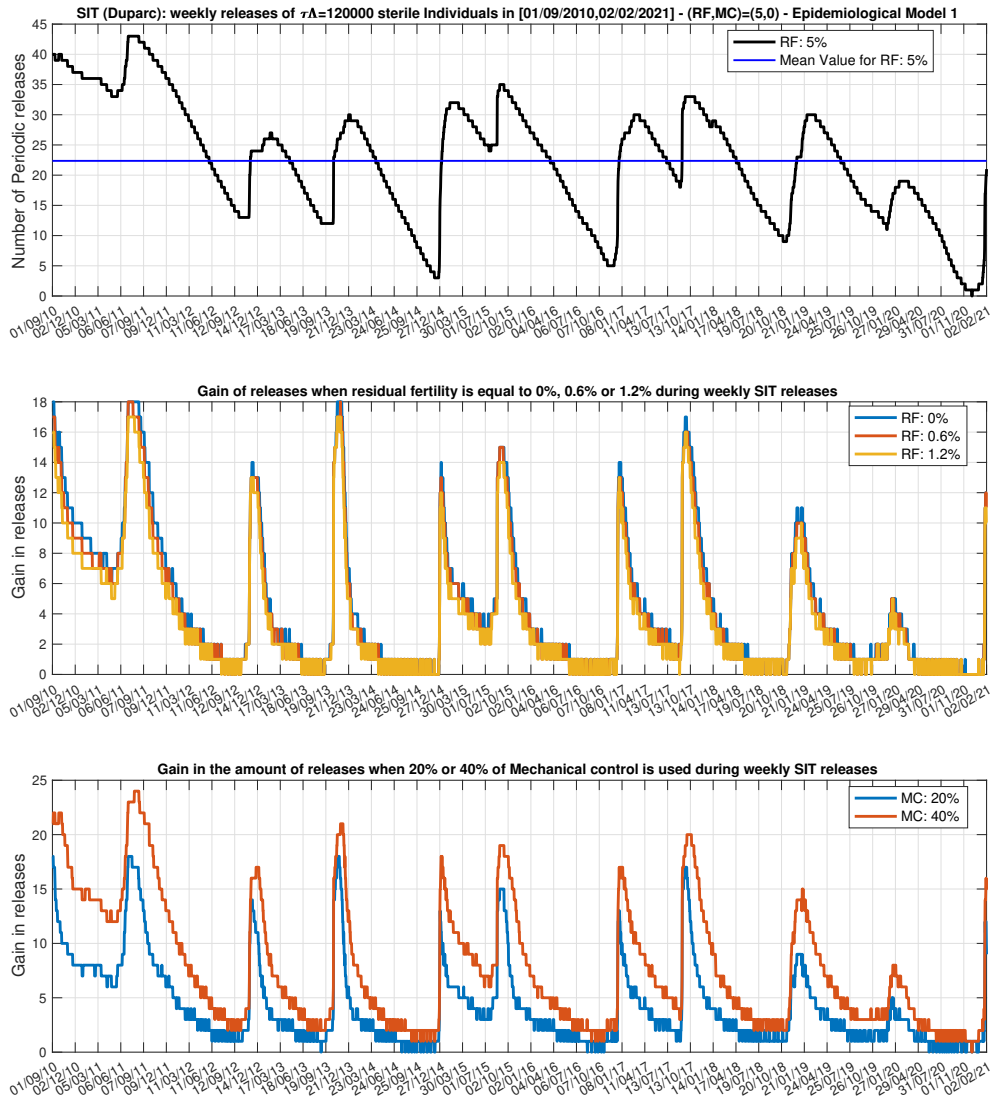


Figure 13: Reducing the epidemiological risk. Simulations of Model 1 with a residual fertility of 5% and $\tau\Lambda = 120000$ Individuals: (a) Variation of the amount of SIT releases; (b) Gain in the releases when residual fertility is 0%, 0.6% or 1.2%; (b) Gain in the releases when 20% and 40% of Mechanical control is used