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# The original and impactful exploitation of chemical energy in heat pumps

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## ABSTRACT

In light of reducing carbon emissions and the tension on non-renewable energy sources, heat pumps are being investigated as an alternative to fossil-fuel-dependent energy converters in heat demanding applications. On the basis of the impactful results the authors obtained in previous research around the potential of using reactive fluids—instead of inert ones—as novel working fluids in power cycles, the study has been extended to heat pump systems. The thermodynamic analysis of heat pumps operating with reactive gases as working fluids is thus the objective of the present work. More specifically, the analysis is based on the use of instantaneously equilibrated fictive gaseous reactions, with the aim to thoroughly assess the impact of different stoichiometries and thermochemical characteristics of chemical reactions. This studied heat pump is based on the reverse Brayton cycle. Furthermore, the behavior of the fluid in each unit operation of the cycle is investigated and all the results are compared to those of a heat pump utilizing comparable inert fluids; that is to preliminarily quantify the potential gains in performance. For the considered spectrum of reactive fluids, operating conditions, and reaction stoichiometries, the corresponding results show a range of potential reactive fluids that can be utilized in heat pumps and reveal an increase of more than 200% in the system's coefficient of performance compared to inert-fluid heat pumps.

## 1. Introduction

Heating is the largest global energy use. According to the International Energy Agency (IEA) [1], heating provided for residences, industrial processes, and other applications accounted for around 50% of the global energy consumption in 2021. Fossil-fuel based heating equipment, such as coal, oil, and gas boilers, dominated the global sales until 2020 (market share greater than 50%). However, a transition towards greener or more efficient technologies has been promoting systems like heat pumps (HP) and renewable heating equipment, and the market share of these technologies has been slowly yet steadily growing. In 2021, HPs were meeting only around 7% of the global building heating demand [2]. However, the IEA demonstrates that, in order to meet the net zero emissions by 2050 scenario, the installed HPs should increase from 180 million (current) to 600 million by 2030.

A HP is a thermodynamic cycle which absorbs heat from a heat source, upgrades this heat, and transfers it to a heat sink using compression work. HP systems can be a greener alternative to fossil-fuel based heating technologies by upgrading low quality heat to a higher quality one, especially in low-temperature waste heat recovery (WHR)

applications [3–5]. In fact, HPs provide 2.5 to 11 times more useful energy compared to other WHR systems for the same waste heat input, in the context of low-temperature WHR applications [4,6]. Furthermore, in line with the net zero emissions target, several countries are concentrating their efforts to motivate residents to switch to HP technologies in order to meet their space and water heating needs. In the United States, the share of HPs for the heating of new buildings is around 50% [2]. Furthermore, other countries like Canada and China are devoting efforts to encourage the installation of HP systems for space heating by offering subsidies to their citizens [2,7]. Moreover, techno-economical surveys have been recently financed by the Government of the Russian federation to identify the most suitable city to install air source and ground-source heat pumps [8].

However, there are still barriers limiting the wider commercialization of HPs. These include the high initial costs, limited availability of high-temperature-range refrigerants that have low global warming potential (GWP), immature technology, limited energy performance, and the competing fossil-fuel-dependent heating technologies [9,10].

Pertaining to the energy performance, improving the performance of a heat pump is carried out by selecting the favorable system technology (vapor compression, absorption, and reverse Stirling HP), optimizing the

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Nomenclature			
$A_m$	Molecule of $m$ fictive atoms A	$T_H$	Heat sink temperature
$A_n$	Molecule of $n$ fictive atoms A	$v$	Specific volume
COP	Coefficient of performance	$w_{comp}$	Compression specific work
$C_p$	Specific heat capacity	WHR	Waste heat recovery
$G$	Total Gibbs energy of the system	$W_{net}$	Net work input to the heat pump system
GWP	Global warming potential	$w_{net,in}$	Specific net work input to the cycle
$h$	Specific enthalpy	$w_{turb}$	Turbine expansion specific work
$H_{i,pure}(T)$	Molar enthalpy of species $i$	$z_i$	Molar fraction of species $i$
HP	Heat pump	$\gamma$	Specific heat ratio $\gamma = C_p / C_v$
HTHP	High temperature heat pump	$\eta_{II}$	Second-law efficiency
IEA	International Energy Agency	$\mu_i$	Chemical potential of species $i$
IHX	Internal heat exchanger	$\mu_i^\circ$	Chemical potential of pure ideal gas $i$ at the standard pressure $P^\circ$
$K_{eq}$	Equilibrium constant	$v_i$	Stoichiometric coefficient of species $i$
$M$	Molar mass of the working fluid (ideal gas mixture)	$\xi(T, P)$	Extent of reaction
$M_i$	Molar mass of species $i$	$\rho$	Density
$\dot{m}$	Mass flow rate	$\Delta n$	Variation in the total number of moles during a process (outlet minus inlet)
$n_i$	Number of moles of species $i$	$\Delta T_{H-C}$	Temperature difference between the heat sink and source
$n_{i,0}$	Initial number of moles of species $i$	$\Delta T_{pp}$	Pinch point temperature difference
$n_{tot}$	Total number of moles	$\Delta_f H_i^\circ$	Standard molar enthalpy change of formation of species $i$ at the reference temperature $T_0$
$n, m$	Number of atoms of molecules $A_n$ and $A_m$ , respectively	$\Delta_R G$	Gibbs-energy change of reaction
ODP	Ozone Depletion Potential	$\Delta_R H^\circ$	Standard enthalpy of reaction
$P$	Pressure	$\Delta_R S^\circ$	Standard entropy of reaction
$P^\circ$	Standard pressure (1 bar)		
$Q_C$	Heat absorbed from the heat source	<b>Subscripts</b>	
$Q_H, \dot{Q}_H$	Thermal power supplied to the heat sink	C	Cold (corresponding to the heat source)
$q_H$	Specific heat supplied to the heat sink	comp	Compression
$R$	Ideal gas constant	eq	Chemical equilibrium
$r_p$	Pressure ratio	H	Hot (corresponding to the heat sink)
$s$	Specific entropy	HX1	Heat sink side heat exchanger
$S_{i,pure}(T, P)$	Molar entropy of the pure ideal gas $i$	in	Inlet
$S_i^\circ(T_0)$	Standard molar entropy of species $i$ at 1 bar and the reference temperature $T_0$	max	Maximum
$T$	Temperature	tot	Total
$T_0$	Reference temperature (25°C)	turb	Turbine expansion
$T_C$	Heat source temperature		

system configuration according to the operating conditions, and selecting the most suitable working fluid [11–13]. A HP configuration can be optimized by applying modifications such as adding an internal heat exchanger (IHX) [14], compression intercooling, vapor injection compression (multi-stage compression with a flash chamber) [15], and cascaded HP system [16]. Other studies aim to improve the efficiency of HP-based systems by acting on the integration of HPs with original systems, providing renewable heat to the heat pump through its evaporator [17]. On the other hand, several considerations must be accounted for when selecting the working fluid of the heat pump. Environmental compatibility (GWP [18] and ODP), price and availability of the fluid, safety group classification, thermophysical properties (compressor discharge and suction temperatures, critical point, volumetric capacity...), and compatibility with the materials of a HP are key factors to select a high-performing working fluid for a HP system [19].

Some commercially available industrial (high temperature) HPs provide temperatures in the range of 130°C to 165°C (SGH 165 HP from Kobe Steel) with heat capacities reaching 20 MW (Titan OM from Johnson Controls) [9]. These systems utilize modifications like IHXs to ensure superheating, economizer cycles, turbo compressors with intermediate vapor injection, parallel piston compressors, and two-stage cascade systems. Furthermore, the refrigerants used are mainly R245fa, R717, R744, R134a, and R1234ze(E). As for the coefficient of performance (COP) values, they lie within the range of 1.6 to 5.8 with a

temperature lift of 130°C to 25°C, respectively.

On the other hand, these high temperature heat pumps (HTHP) are still under study and development in order to improve the system's performance, find suitable environmentally-friendly refrigerants, and achieve high heat sink temperatures (above 100°C) [9]. Arpagaus et al. [9] in their review of HTHPs, assessed 17 HPs that are still in research status. The highest heat sink temperature achieved experimentally is 160°C (developed by the Austrian Institute of Technology, Vienna, Chemours, Bitzer) using the R1336mzz(Z) refrigerant and an IHX, with heating capacities that range from 1.8 kW to several 100 kW. In such experimental system, compression is mainly carried out in piston compressors, and most of these systems are single stage. The system modifications adopted include IHXs, economizer cycles, and compression with intermediate vapor injection. Only a few studies focus on two-stage cycles or cycles with subcoolers for combined water heating. Additionally, the refrigerants under study are mainly R1336mzz(Z), R718, R245fa, R1234ze(Z), R600, and R601, besides other fluids whose chemical composition is not published yet. As for the COP values, they lie within the range of 5.7 to 6.5 at 30°C temperature lift and 2.2 to 2.8 at 70°C [9].

Similarly, Frate et al. [20] reviewed the suitability of a pool of working fluids for HTHP applications. The authors considered a highest level of heat sink temperature of 150°C and a lowest level of heat source temperature of 50°C. After imposing thermodynamic, environmental, safety, and technological constraints, 27 fluids were assessed for

different operating conditions. Acetone was recommended for high heat sink and low heat source temperatures whereas benzene was recommended for high heat sink and heat source temperatures. Additionally, dichloroethane was recommended for low heat sink and high heat source temperatures. However, the latter fluids are flammable or highly flammable. On the other hand, less efficient synthetic refrigerants like R1336mzz(Z), R1234ze(Z), R1233zd(E), and R1224yd provide effective alternatives since they don't pose flammability and toxicity issues [21].

Alternatively, Bamigbetan et al. [21] evaluated different working fluids with a close approximation to a physical high temperature 20 kW heat pump with 125°C as the target heat sink temperature. Fluids R600 and R1233zd(E) were prioritized. R600 offers the compatibility with well-developed compressor technologies and flexibility. While R1233zd (E) offers a high value of COP, its stability, flammability, and safety need further testing [21]. This is also one of the fluids recommended in a novel trigeneration cycle that is still under development [19].

On the other hand, novel working fluids are being investigated for thermodynamic cycles. The latter are referred to as reactive fluids based on equilibrated chemical reactions [22,23]. Therefore, they accommodate chemical reactions and composition alterations under the influence of thermodynamic transformations. A thorough literature review has been carried out by some of the authors on the utilization of reactive working fluids in power systems [23]. However, to their knowledge, the study of reactive fluids in heat pump applications is absent in the literature.

Other heat pumps utilizing chemical reactions within the cycle are absorption HP systems (e.g. the water-ammonia system or the recently patented system based on phosphoric acid) [24–28]. However, unlike the proposed reactive heat pumps, in these systems, the chemical reactions do not directly contribute to the heat provided to the heat sink, expansion process, or heat absorbed from the heat source. In addition, these systems are generally less efficient than the conventional compressor-driven HP, and their operation is mainly limited to high source temperatures.

Therefore, taking into consideration the aforementioned gaps in the literature, this study investigates the potential of reactive fluids – rather than inert ones – in a HP system. These fluids ground on a novel energy conversion concept since they offer the advantage of the simultaneous conversion of thermal and chemical energy throughout the HP cycle, achieving by that an enhanced system performance (higher COP values compared to inert HP systems). A spectrum of equilibrated fictive reactive gaseous fluids is assessed as working fluids for an ideal HP system based on a reverse Brayton cycle. The reactive fluid's behavior in each of the HP's units is assessed and benchmarked against the behavior of comparable inert fluids. The overall performance of the reactive system is also investigated for different reaction stoichiometries and operating conditions.

## 2. Methods

This section describes the methodology which has been followed and introduces: the considered HP system's configuration and its application, the path followed to design the reactive fluids, the thermodynamic calculations, and the parameters at the basis of the thermodynamic assessment of the system.

Note that a similar methodology has been implemented by the authors in order to assess the performance of reactive fluids in power systems [23]. Therefore, in this study, the methodology has been adapted to heat pumps.

### 2.1. System configuration

The HP system used to assess the performance of gaseous reactive working fluids is comprised of a compressor, turbine, heat exchanger at the heat source side, and another heat exchanger at the heat sink side, as illustrated in Fig. 1. One should note that no phase change occurs

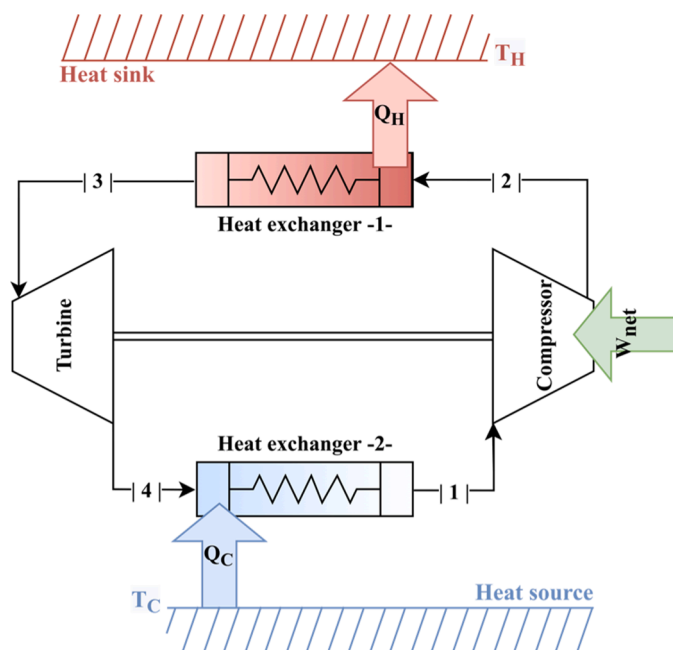


Fig. 1. The heat pump configuration considered in this study.

throughout the cycle and the fluid is considered a reactive ideal gas mixture, as detailed in Section 2.3. Therefore, this HP system represents a reverse ideal Brayton cycle. With reference to Fig. 1, the reactive fluid is compressed from point (1) to (2), then it is cooled down by rejecting heat to the heat sink (the useful effect of the HP) from point (2) to (3); this is followed by an expansion of the fluid in the turbine from point (3) to (4) and heat absorption at the heat source side. Pressure drops across the heat exchangers are neglected, and both the compressor and turbine are considered isentropic.

### 2.2. The design of reactive fluids

A reactive fluid is a medium that accommodates chemical reactions. Similar to the author's previous study [23], in this work, the reactions involved are assumed to occur instantaneously. This means that the reaction rapidly reaches its equilibrium state for each set of operating conditions throughout the cycle. As the fluid thermodynamic state changes when it undergoes each of the four transformations in the HP cycle, the chemical reaction shifts according to chemical equilibrium either in the exothermic or endothermic direction. This entails an altered composition of the ideal gas mixture when undergoing thermodynamic transformations.

The reactive fluid of the present study is characterized by the equilibrated single chemical equation:



where  $A_n$  and  $A_m$  are molecules made of fictive atoms "A". Parameters  $n$  and  $m$  denote the number of atoms of the molecules involved, respectively, and their values dictate the reaction stoichiometry. In this study,  $n$  is considered greater than  $m$ , and the forward direction of the reaction indicates a dissociation reaction, while the backward direction indicates an association reaction. The reactive fluids assessed are considered ideal gas mixtures of gases  $A_n$  and  $A_m$ , where the molar mass of atom A is taken to be equal to 1g/mol.

The specific heat capacity of the involved ideal gases ( $A_n$  and  $A_m$ ) is assumed to be independent of temperature and defined according to the equipartition theorem [29]: the specific heat capacity of monoatomic molecules is given by  $C_{p,A} = (5/2)R$ , diatomic molecules  $C_{p,A_2} = (7/2)R$ , and polyatomic molecules  $C_{p,A_k} = 4R$  (with  $k > 2$ ), where

**Table 1**

Chemical reaction stoichiometric coefficients and initial number of moles.

Parameter	Value
Number of atoms of the ideal gas $A_n$ : $n$	2 or 4
Number of atoms of the ideal gas $A_m$ : $m$	1
Initial number of moles of $A_n$ : $n_{A_n,0}$	1 mol
Initial number of moles of $A_m$ : $n_{A_m,0}$	0 mol

$R$  is the ideal gas constant. The maximum value of  $k$  considered in this study is four. These specific heat capacity values are needed to compute all the thermodynamic properties, as presented in the thermodynamic assessment section.

The spectrum of reactive fluids studied is based on ranges of the standard entropy of reaction and standard enthalpy of reaction—referred to as the reaction coordinates in this study—( $\Delta_R S^\circ, \Delta_R H^\circ$ ), where each set of these coordinates resembles a unique reactive working fluid (unique equilibrated chemical reaction). In that matter, several points concerning the reaction coordinates need to be taken into account:

- The enthalpy change for a reaction under standard conditions ( $\Delta_R H^\circ$ ) is positive for endothermic reactions and negative for exothermic reactions.
- The dissociation of a molecule into two or more molecules requires energy (endothermic reaction).
- For a gas-phase reaction, the entropy change of reaction under standard conditions ( $\Delta_R S^\circ$ ) is positive when the total number of molecules of the products is greater than that of the reactants, and negative otherwise. Thus,  $\Delta_R S^\circ$  is also positive for gas-phase dissociation reactions.
- If a reaction is exothermic in the forward direction, it is endothermic in the reverse direction, and vice versa. Moreover, if the entropy change is positive in the forward direction, it is negative in the opposite direction, and vice versa.

Typical values of these reaction coordinates,  $\Delta_R S^\circ$  and  $\Delta_R H^\circ$ , fall within the ranges of 0 to 0.2 kJ/mol K for  $\Delta_R S^\circ$  and 0 to 200 kJ/mol for  $\Delta_R H^\circ$  [23] for the forward direction:  $A_{n(g)} \rightarrow (n/m) A_{m(g)}$ . Therefore,

**Table 2**

Thermophysical properties of the ideal gas mixture.

Property of the ideal gas mixture	Equation
Molar mass, $M$ (g/mol)	$M = \sum_i z_i M_i$ where, $z_i$ : molar fraction of each species $i$ involved ( $z_i = n_i/n_{tot}$ ) $M_i$ : molar mass of the involved chemical species
Specific entropy, $s$ (kJ/g K)	$s(T, P, \mathbf{z}) = (\sum_i z_i S_{i,pure}(T, P) - R \sum_i z_i \ln z_i) / M$
	$S_{i,pure}(T, P) = S_i^\circ(T_0) + C_{p,i} \ln \frac{T}{T_0} - R \ln \frac{P}{P^\circ}$
	Recall that, by definition, the standard entropy of reaction is given by: $\Delta_R S^\circ(T_0) = \sum v_i S_i^\circ(T_0)$ . where, $S_{i,pure}(T, P)$ : the molar entropy of the pure ideal gas $i$ involved in the mixture (either $A$ or $A_2$ ) $S_i^\circ(T_0)$ : standard molar entropy (i.e., at $P^\circ = 1$ bar) of pure ideal gas $i$ at temperature $T_0$ $C_{p,i}$ : specific heat capacity of pure ideal gas $i$ $T$ : temperature $T_0$ : reference temperature (25°C) $P$ : pressure $P^\circ$ : standard pressure (1 bar) $v_i$ : stoichiometric coefficient of species $i$
Specific enthalpy, $h$ (kJ/g)	$h = \sum_i z_i H_{i,pure}(T) / M$
	$H_{i,pure}(T) = \Delta_f H_i^\circ(T_0) + C_{p,i}(T - T_0)$
	Recall that, by definition, the standard enthalpy of reaction is given by: $\Delta_R H^\circ(T_0) = \sum v_i \Delta_f H^\circ(T_0)$ . where, $H_{i,pure}(T)$ : molar enthalpy of the pure ideal gas $\Delta_f H^\circ$ : standard molar enthalpy change of formation of the ideal gas $i$ at temperature $T_0$
Specific volume, $v$ (m <sup>3</sup> /g)	$v = RT / PM$
Density, $\rho$ (g/m <sup>3</sup> )	$\rho = v^{-1}$

these are the values considered in this work.

### 2.3. Thermodynamic assessment

In order to determine the thermodynamic state of each point in the HP cycle, the corresponding chemical composition should be evaluated.

As described in Section 2.2, the composition of the reactive fluid throughout the cycle is governed by chemical equilibrium. From classical thermodynamics, the criterion of chemical equilibrium can be expressed as:

$$\left( \frac{dG}{d\xi} \right)_{T,P} \stackrel{chem.}{\stackrel{def.}{=} \Delta_R G} \stackrel{eq.}{=} 0 \quad \text{where} \quad \Delta_R G = \sum_i v_i \mu_i \quad (1)$$

Where  $G$  is the total Gibbs energy of the system at temperature  $T$  and pressure  $P$  [30],  $\xi$  is the extent of reaction,  $\Delta_R G$  is the Gibbs-energy change of reaction,  $v_i$  is the stoichiometric coefficient of species  $i$ , and  $\mu_i$  is the chemical potential of species  $i$ .

The fugacity of species  $i$  in an ideal gas mixture is equal to its partial pressure [30], so its chemical potential  $\mu_i$  can be expressed as:

$$\mu_i(T, P, \mathbf{n}) = \mu_i^\circ(T) + RT \cdot \ln \left( \frac{P/P^\circ}{n_{tot}} n_i \right), \quad (2)$$

Where  $\mu_i^\circ$  is the chemical potential of pure ideal gas  $i$  at the standard pressure ( $P^\circ = 1$  bar) and temperature  $T$ ,  $n_{tot}$  is the total number of moles ( $n_{tot} = n_{A_n} + n_{A_m}$ ),  $n_i$  is the number of moles of species  $i$ .

By introducing the  $T$ -dependent equilibrium constant ( $K_{eq}$ ) defined as  $K_{eq} = \exp \left( -\frac{\sum v_i \mu_i^\circ}{RT} \right)$ , Eqs. (1) and (2) lead to:

$$K_{eq}(T) = \left( \frac{P/P^\circ}{n_{tot}} \right)^{\sum_{i=1}^{n_c} v_i} \prod_{i=1}^{n_c} n_i^{v_i}, \quad (3)$$

Where  $n_c$  is the number of different molecules forming the system. In the present case  $n_c = 2$  since there are only two types of molecules –  $A_n$  and  $A_m$  – constituting the system.

Furthermore, the number of moles of each chemical species  $i$  ( $n_i$ ) at temperature  $T$  and pressure  $P$  can be expressed as a function of the extent of the reaction  $\xi(T, P)$ , initial number of moles of the corresponding



chemical species  $n_{i,0}$ , and the stoichiometric coefficient  $v_i$  [30], as per Eq. (4):

$$n_i = n_{i,0} + v_i \cdot \xi(T, P). \quad (4)$$

Substituting the respective stoichiometric coefficients of the reaction in chemical Eq. (R1) ( $v_{A_n} = -1$ ;  $v_{A_m} = n/m$ ), number of moles representing the present chemical species ( $n_{A_n}$ ;  $n_{A_m}$ ), and Eq. (4) in Eq. (3), the latter becomes,

$$K_{eq} = \left( \frac{P/P^0}{n_{A_n,0} + n_{A_m,0} + \left(\frac{n}{m}-1\right) \cdot \xi(T, P)} \right)^{\frac{n}{m}-1} \frac{(n_{A_m,0} + \frac{n}{m} \cdot \xi(T, P))^{\frac{n}{m}}}{n_{A_n,0} - \xi(T, P)}. \quad (5)$$

Moreover, the equilibrium constant  $K_{eq}$  can be evaluated as a function of the temperature ( $T$ ), standard enthalpy of reaction ( $\Delta_R H^0$ ), and standard entropy of reaction ( $\Delta_R S^0$ ) [23,30,31] at the reference temperature  $T_0$  (25°C), according to the Ulich approximation:

$$\ln K_{eq}(T) = \frac{\Delta_R S^0(T_0)}{R} - \frac{\Delta_R H^0(T_0)}{RT}. \quad (6)$$

Therefore, at any thermodynamic point in the HP cycle, for a given set of reaction coordinates ( $\Delta_R S^0, \Delta_R H^0$ ) and temperature  $T$ , the equilibrium constant can be evaluated using Eq. (6). Then, substituting the stoichiometric coefficients and initial number of moles for each chemical species by their corresponding values (presented in Table 1 for this study) in Eq. (5), the extent of reaction can be evaluated at each temperature-pressure condition,  $\xi(T, P)$ . Knowing  $\xi(T, P)$ , the number of moles and molar fraction corresponding to each chemical species can be evaluated using Eq. (4), enabling the evaluation of the equilibrium composition of the reactive fluid.

All the aforementioned calculations are conducted using a Fortran code developed by the authors of this study.

Therefore, as demonstrated in Table 1, this study investigates two reaction stoichiometries,  $A_{2(g)} \rightleftharpoons 2A_{(g)}$  and  $A_{4(g)} \rightleftharpoons 4A_{(g)}$ , for the considered ranges of reaction coordinates ( $\Delta_R S^0, \Delta_R H^0$ ).

After determining the chemical equilibrium composition at each thermodynamic point in the cycle, knowing the corresponding pressure and temperature, the thermodynamic properties of the fluid can be evaluated following the ideal gas mixture thermodynamic model presented in Table 2 [30,32].

In this study, the heat sink (hot side) and heat source (cold side) are assumed to be at constant temperatures ( $T_H$  and  $T_C$ ). These temperatures, along with the heat exchangers' pinch point temperature difference ( $\Delta T_{pp}$ ), are used to determine the compressor and turbine inlet temperatures ( $T_1$  and  $T_3$ ), according to the following:

$$\begin{cases} T_1 = T_C - \Delta T_{pp} \\ T_3 = T_H + \Delta T_{pp} \end{cases} \quad (14)$$

Note that the pinch point temperature difference for both of the heat exchangers is considered to be the same. Denote by  $\Delta T_{H-C}$  the temperature difference  $T_H - T_C$  between the heat sink and heat source. This corresponds to the actual temperature lift provided by the heat pump.

Furthermore, the system's low pressure ( $P_1=P_4$ ) is fixed at 1 bar, as a reference value for this preliminary analysis. On the other hand, the system's high pressure ( $P_2=P_3$ ) is varied between 5 bar and 20 bar, and the effect on the system's performance is assessed. Similarly, the system's performance is assessed for different heat source temperatures  $T_C$  (between 5°C and 50°C), difference between the heat sink and source temperatures  $\Delta T_{H-C}$  (between 30°C and 100°C), and heat exchangers' pinch point temperature difference  $\Delta T_{pp}$  (equal to either 5°C or 10°C) in order to observe how the HP's performance varies with the operating conditions.

Therefore, the compressor and turbine outlet temperatures ( $T_2$  and  $T_4$ ) are the only unknowns, and they can be evaluated on the basis that the compression and expansion processes are isentropic ( $\Delta s = 0$ ). To determine these temperatures, and consequently the equilibrium

composition and other thermodynamic properties of the fluid, the equation  $\Delta s = 0$  is solved between the inlet and exit of the compressor and turbine using an iterative process. The temperatures  $T_2$  and  $T_4$  are varied – respectively at pressures  $P_2$  and  $P_4$  – until the obtained entropy values,  $s_2$  and  $s_4$ , result to be equivalent to those at the inlet.

To assess the performance of the HP, the COP is calculated according to the equation:

$$COP = \frac{q_H}{w_{net,in}}, \quad (15)$$

Where  $q_H$  is the specific heat (specific to the mass) rejected at the heat sink heat exchanger, and it is given by the difference between the specific enthalpies at the heat exchanger's inlet ( $h_2$ ) and exit ( $h_3$ ) according to:

$$q_H = h_2 - h_3, \quad (16)$$

and  $w_{net,in}$  is the net specific work provided to the system and is equal to the difference between the compression work ( $w_{comp}$ ) and the expansion work ( $w_{turb}$ ),

$$w_{net,in} = w_{comp} - w_{turb} = (h_2 - h_1) - (h_3 - h_4). \quad (17)$$

Where,  $h_1$  and  $h_4$  are the specific enthalpies at the compressor's inlet and turbine's exit, respectively.

In the case where, for a given reactive fluid and specific operating conditions, the heat transfer values are negative (heat flows in the opposite direction to the intended one), the system is deemed infeasible because it operates as a Brayton cycle (power cycle), instead of a reverse Brayton cycle (heat pump). Therefore, these cases are excluded from the analysis.

After assessing the performance of the reactive fluid-based HP, the latter is benchmarked against HPs operating with comparable inert gases, that are molecules  $A$  and  $A_2$  if the reactive fluid under analysis is  $A_{2(g)} \rightleftharpoons 2A_{(g)}$ , or  $A$  and  $A_4$  if the considered reaction is  $A_{4(g)} \rightleftharpoons 4A_{(g)}$ . The required mass flow rate, heat rejected at the heat sink, and compressor and turbine outlet temperatures of the reactive system are also compared to those of the inert ones in order to assess the technological feasibility of the system.

### 3. Results

This section presents the results of the methodology applied to an ideal HP cycle considering the set of operating conditions recorded in Table 3 in order to assess the behavior of reactive working fluids in a HP system. These operating conditions are arbitrary and serve the purpose of understanding how the reactive fluid behaves in each of the system's devices as a function of the reaction coordinates ( $\Delta_R S^0, \Delta_R H^0$ ) compared to inert fluids  $A$  and  $A_2$ . The fluid's performance is presented in Section 3.1 for the isentropic compression, Section 3.2 for the heat sink heat exchanger, and Section 3.3 for the isentropic expansion. Then, the overall reactive system performance is assessed for different reaction coordinates in Section 3.4 considering two different reaction stoichiometries. Furthermore, the effect of changing the preliminarily defined operating conditions – presented in Table 3 – on the system's

**Table 3**  
Preliminary system operating conditions.

System operating condition	Specification
Chemical reaction	$A_{2(g)} \rightleftharpoons 2A_{(g)}$
Low pressure $P_1=P_4$	1 bar
High pressure $P_2=P_3$	5 bar
Heat source temperature $T_C$	10°C
Heat sink temperature $T_H$	50°C
Heat exchangers pinch point temperature difference $\Delta T_{pp}$	5°C
Compressor inlet temperature $T_1=T_C-\Delta T_{pp}$	5°C
Turbine inlet temperature $T_3=T_H+\Delta T_{pp}$	55°C

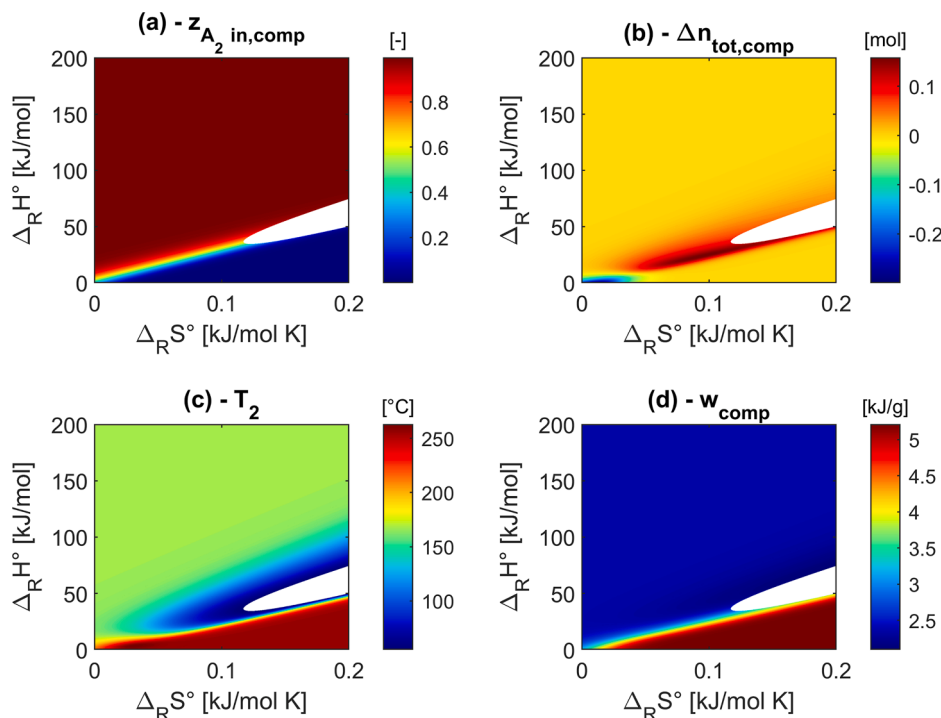


Fig. 2. Behavior of the reactive fluid ( $A_{2(g)} \rightleftharpoons 2A_{(g)}$ ) for different reaction coordinates ( $\Delta_R S^\circ$ ,  $\Delta_R H^\circ$ ) under isentropic compression (from point 1→2); equilibrium molar fraction of  $A_2$  at the compressor's inlet ( $5^\circ\text{C}, 1 \text{ bar}$ ),  $z_{A_2 \text{ in,comp}}$ , Fig. (a); variation in the total number of moles (outlet minus inlet) of the system during compression  $\Delta n_{\text{tot,comp}}$ , Fig. (b); compression outlet temperature,  $T_2$ , Fig. (c); compression specific work,  $w_{\text{comp}}$ , Fig. (d).

performance is assessed in Section 3.5. A similar discussion was performed in a previous paper [23] dedicated to power systems.

### 3.1. Isentropic compression

As a first step, the compression process is assessed to observe how the fluids' thermochemical characteristics ( $\Delta_R S^\circ, \Delta_R H^\circ$ ) affect the temperature gradient in the compressor, as well as the compression work needed by the system. Thus, the equilibrium composition at the compressor's inlet ( $z_{A_2 \text{ in,comp}}$ ), the variation in the total number of moles during compression ( $\Delta n_{\text{tot,comp}}$ ), the compressor's outlet temperature ( $T_2$ ), and the specific compression work ( $w_{\text{comp}}$ ) are presented in Fig. 2. In fact,  $z_{A_2 \text{ in,comp}}$  at the inlet of the compressor and  $\Delta n_{\text{tot,comp}}$  are indicators of the reaction evolution during compression (direction and variation in the equilibrium composition).

In Fig. 2, the white zones in the colormaps represent the infeasible zones for the operation of a HP system, where the system acts as a Brayton cycle, that is as a power cycle. Indeed, heat flows in the opposite direction than the intended one. Therefore, these zones have been excluded from the analysis in this study, which is focused on heat pumps.

Fig. 2(a) presents the molar fraction at chemical equilibrium of the molecule  $A_2$  for different reactive fluids at the compressor's inlet. It can be observed that for low values of  $\Delta_R S^\circ$  and high values of  $\Delta_R H^\circ$ , the fluid is solely comprised of  $A_2$  molecules (100%  $A_2$ ). On the other hand, for high values of  $\Delta_R S^\circ$  and low values of  $\Delta_R H^\circ$ , the fluid is merely composed of  $A$  molecules (100%  $A$ ). This signifies that the equilibrium constant  $K_{eq}$  at the compressor's inlet is extremely low for the region of pure  $A_2$  and high for the region of pure  $A$ . These extreme values of  $K_{eq}$  justify the regions of negligible reaction shift (negligible shift in the number of moles) during isentropic compression, as observed in Fig. 2(b). However, for intermediate values of  $\Delta_R S^\circ$  and  $\Delta_R H^\circ$ , the compressor's inlet composition becomes highly sensitive as a function of the reaction coordinates (Fig. 2(a)), and significant variations in the total number of moles in the system result from the fluid compression (Fig. 2

(b)). Nonetheless, the reaction shifts towards the endothermic direction, characterized by an increasing number of moles ( $\Delta n_{\text{tot,comp}} > 0$ ) for some of these intermediate values, and in the opposite, exothermic, direction ( $\Delta n_{\text{tot,comp}} < 0$ ) for the others, as illustrated in Fig. 2(b).

The reason of the possible opposite directional shift of the reaction is related to the impact of its thermochemistry (enthalpy and entropy of reaction) and to the effects of pressure and temperature change in a compression process. If no chemical reaction occurs, the thermodynamic effect of increasing the pressure of a fluid adiabatically is that the **temperature increases**. If an equilibrated reaction occurs in a fluid, the law of mass action states that the increase of its pressure (at constant temperature) shifts the reaction in the direction dictated by the reduction of the number of moles, which is the association–**exothermic, reaction**. The exothermic reaction in an adiabatic compression, as well as the inherent inert fluid-heating process, tend to increase the temperature of the system and, thus, to shift the equilibrium in the **endothermic direction**, as dictated by the Van't Hoff equation. These are two opposite effects and the prevalence of one or the other depends on the enthalpy and entropy of reaction: when those are low, the effect of pressure on equilibrium is prevalent (exothermic reaction,  $\Delta n_{\text{tot,comp}} < 0$ ), otherwise the effect of temperature is prevalent, and the reaction moves in the endothermic direction ( $\Delta n_{\text{tot,comp}} > 0$ ).

Note that in the case where the fluid is composed of pure  $A_2$  or pure  $A$  molecules, and the variation in the number of moles is negligible ( $\Delta n_{\text{tot,comp}} = 0$  in Fig. 2(b)), the fluid behaves as an inert fluid in the considered transformation. Therefore, the behavior and properties of these **inert fluids**, observed at the bottom right corner (for **fluid A**) and top left corner (for **fluid A<sub>2</sub>**) of each colormap in Fig. 2, can be used as a **benchmark to assess the behavior of reactive fluids** (intermediate values of  $\Delta_R S^\circ$  and  $\Delta_R H^\circ$ ).

From Fig. 2(c), it can be observed that for some of the reactive domain, the compressor's outlet temperature  $T_2$  is higher – reaching a maximum of  $263.8^\circ\text{C}$  – compared to inert fluids  $A$  or  $A_2$  ( $256.3^\circ\text{C}$  for  $A$  and  $167.4^\circ\text{C}$  for  $A_2$ ). Indeed, this reactive domain is characterized by exothermic reactions. However, this maximum outlet temperature

resulting from the reactive working fluid is comparable to that of inert fluid  $A_2$  (3% deviation). On the other hand, for the majority of reactive fluids,  $T_2$  is lower than that of the inert ones, and it can reach a minimum of  $55^\circ\text{C}$ . This means that in the case of reactive fluids, the temperature gradient during compression is much smaller compared to inert fluids. This provides more flexibility when it comes to the compressor's technology since the outlet temperature is one of the focal points in a compressor's design process. On the other hand, a sufficiently high temperature is needed at the inlet of the heat sink heat exchanger in order to reject an adequate amount of heat, which is the purpose of the HP.

Furthermore, from Fig. 2(d), it can be observed that the compression work is the highest for inert fluid  $A$ , amounting to  $5.2\text{ kJ/g}$ . Thus, for all the considered reactive fluids, the work input required is less compared to reactive fluid  $A$ . Operating with inert fluid  $A_2$  requires a compressor's work of  $2.4\text{ kJ/g}$ . The reactive fluids that exhibit specific work values less than  $2.4\text{ kJ/g}$  are characterized by the endothermic, dissociation reaction ( $A_{2(g)} \rightarrow 2A_{(g)}$ ), as illustrated in Fig. 2(b) and Fig. 2(d), and by a low compression outlet temperature. The minimum compression work value that can be achieved by the considered reactive fluids amounts to  $2.1\text{ kJ/g}$ . That is around 60% reduction in the compression work needed compared to fluid  $A$ , and 11% reduction compared to fluid  $A_2$ .

Examining Fig. 2(a) and Fig. 2(d), it can be observed that the compression of inert fluid  $A$  requires more work than the compression of fluid  $A_2$ . This is due to the fact that the molecular complexity and weight are higher for molecule  $A_2$ , which results in the reduction of the compression work [22,33].

### 3.2. Heat sink side heat exchanger

Following the isentropic compression between points (1) and (2) in the HP cycle presented in Fig. 1, the fluid rejects heat into the heat sink ( $q_H$ ), which is the main purpose of the system. As the amount of  $q_H$  increases, the COP also increases since both quantities are directly proportional (Eq. (15)).

The molar fraction of  $A_2$  at the inlet of the heat exchanger ( $z_{A_2, \text{in,HX1}}$ ),

the variation in the total number of moles between the exit and the inlet of the heat exchanger ( $\Delta n_{\text{tot,HX1}}$ ), and the amount of specific heat rejected to the heat sink ( $q_H$ ) are presented in Fig. 3.

Similar to the compressor inlet's composition presented in Fig. 2(a), the equilibrium composition of the hot side heat exchanger's inlet is pure  $A$  for high values of  $\Delta_R S^\circ$  and low values of  $\Delta_R H^\circ$  and pure  $A_2$  for low values of  $\Delta_R S^\circ$  and high values of  $\Delta_R H^\circ$ . The equilibrium composition becomes highly sensitive as a function of the reaction coordinates for the intermediate values of  $\Delta_R S^\circ$  and  $\Delta_R H^\circ$ .

Observing Fig. 3(b), in the hot side heat exchanger where fluid's temperature is decreased at constant pressure, the reaction always shifts in the exothermic-association direction ( $\Delta n_{\text{tot,HX1}} < 0$ ), complying with the Van't Hoff equation. This means that the reaction is in favor of the heat rejection to the heat sink. Fig. 3(a) together with Fig. 3(b) enable the assessment of the molar composition at the end of the heat exchange process. Furthermore, comparing the heat rejected by reactive fluids and non-reactive ones—presented in Fig. 3(c)—some of the reactive region (the region around the white zone) shows a very low value of heat rejected compared to inert fluids  $A$  and  $A_2$  and the other reactive fluids. On the other hand, some of the reactive fluids exhibit values of  $q_H$  higher than those corresponding to inert fluids  $A$  and  $A_2$ . Specifically, the highest value of  $q_H$  achieved by reactive fluids is around  $4.5\text{ kJ/g}$ , and that is characterized by a thermochemistry that allows the maximum reduction of the number of moles. Compared to inert fluid  $A$ , this entails a 7.4% increase, and a 175% increase compared to inert fluid  $A_2$ .

### 3.3. Isentropic expansion

Another factor that affects the HP's performance is the expansion work since it offsets the work required by the system.

The molar fraction of molecule  $A_2$  at the inlet of the isentropic turbine ( $z_{A_2, \text{in,turb}}$ ), the variation in the total number of moles during expansion ( $\Delta n_{\text{tot,turb}}$ ), the turbine's outlet temperature ( $T_4$ ), and the expansion specific work ( $w_{\text{turb}}$ ) are presented in Fig. 4.

As can be observed in Fig. 4, similar conclusions can be drawn out concerning the molar composition at the turbine's inlet as the other

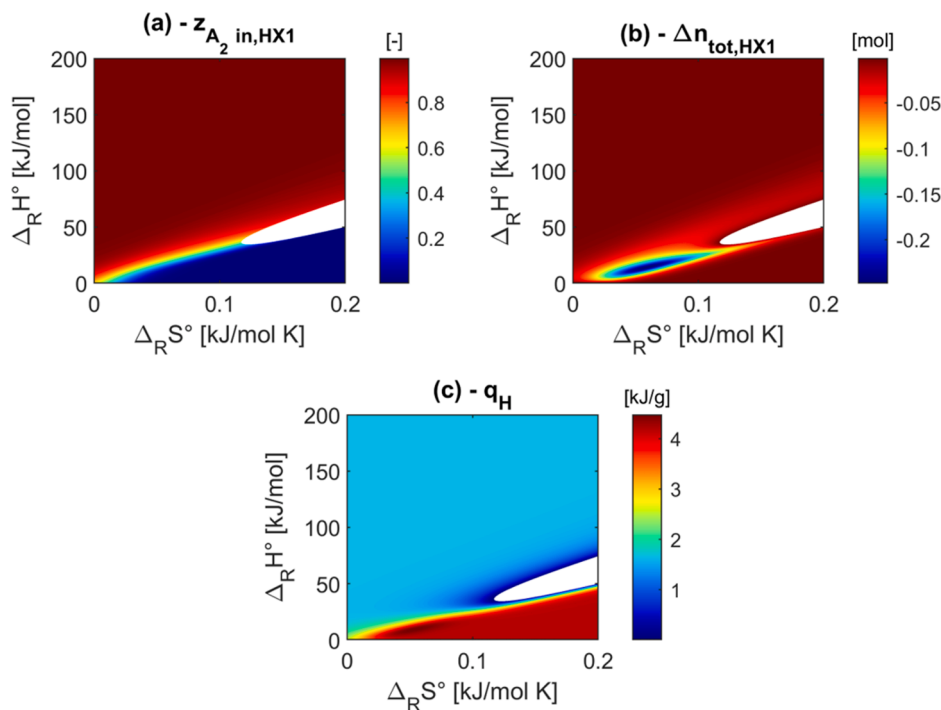
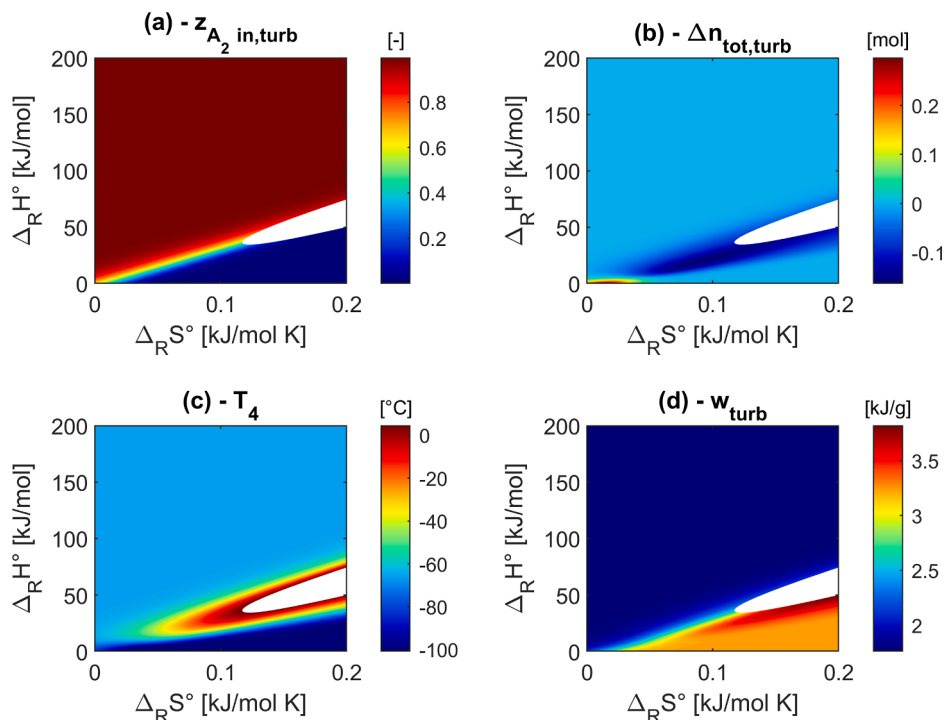


Fig. 3. Behavior of the reactive fluid ( $A_{2(g)} \rightleftharpoons 2A_{(g)}$ ) for different reaction coordinates ( $\Delta_R S^\circ$ ,  $\Delta_R H^\circ$ ) in the hot-side heat exchanger (from point 2→3); equilibrium molar fraction of  $A_2$  at the heat exchanger's inlet  $z_{A_2, \text{in,HX1}}$ , Fig. (a); variation in the total number of moles (outlet minus inlet) of the system during the heat exchange,  $\Delta n_{\text{tot,HX1}}$ , Fig. (b); specific heat rejected through the heat exchanger  $q_H$ , Fig. (c).





**Fig. 4.** Behavior of the reactive fluid ( $A_{2(g)} \rightleftharpoons 2A_{(g)}$ ) for different reaction coordinates ( $\Delta_R S^\circ$ ,  $\Delta_R H^\circ$ ) under isentropic expansion (from point 3→4); equilibrium molar fraction of  $A_2$  at the turbine's inlet (55°C, 5 bar),  $z_{A_2, in, turb}$ , Fig. (a); variation in the total number of moles (outlet minus inlet) of the system during expansion  $\Delta n_{tot, turb}$ , Fig. (b); turbine's outlet temperature,  $T_4$ , Fig. (c); expansion specific work,  $w_{turb}$ , Fig. (d).

devices in the cycle. As in Fig. 2 and Fig. 3, also Fig. 4(a) and (b) are useful because they allow assessing the evolution of the reaction, during the expansion process, with respect to the initial compositional state.

It is observed that the majority of the reactive fluids undergo an association reaction during isentropic expansion ( $\Delta n_{tot, turb} < 0$ ), as demonstrated in Fig. 4(b). This means that the reaction is exothermic, and the reaction shifts in the direction of decreasing number of moles.

On the contrary, observing Fig. 4(c), the temperature drop in the turbine for reactive fluids is much smaller than those corresponding to fluids A and  $A_2$ . For inert fluid A, during expansion, the temperature drops from 55°C to around -101°C (156°C difference), and to around -66°C (121°C difference) for fluid  $A_2$ . However, for reactive fluids, the temperature drop during expansion can reach a minimum of 50°C. This is disadvantageous to the heat transfer in the heat source heat exchanger since the higher  $T_4$  is, less heat ( $q_C$ ) can be absorbed from the heat sink.

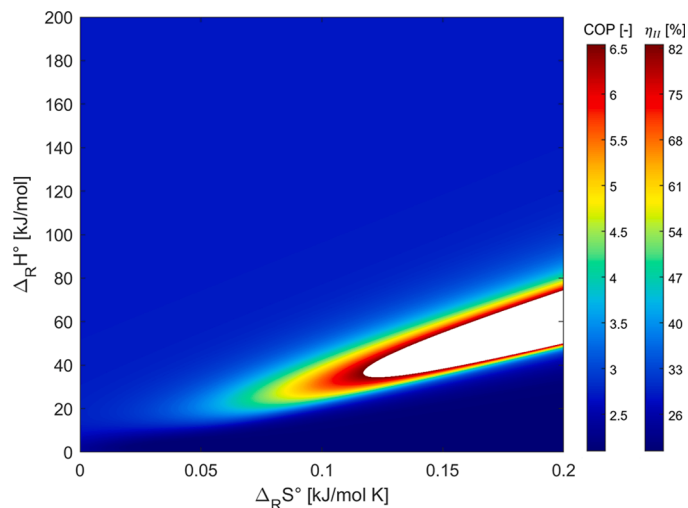
On the other hand, Fig. 4(d) reveals that reactive fluids can generate an expansion work greater than that produced by inert fluids A and  $A_2$ . This work can reach a maximum of 3.8 kJ/g for the considered reaction coordinates. This is 118% higher than the work produced by fluid  $A_2$  and 18% higher than that produced by inert fluid A. Note that the highest expansion work region is characterized by a moderate association reaction ( $\Delta n_{turb} < 0$ ).

Furthermore, as illustrated in Fig. 4(d), the expansion work produced by inert fluid A (3.2 kJ/g) is 84% greater than that produced by fluid  $A_2$  (1.7 kJ/g). This is due to the lower molecular complexity of molecule A.

### 3.4. The heat pump system

In this section, the global behavior and performance of the reactive fluid in the HP system is assessed. The COP is considered as the key performance indicator of the HP system for each of the reactive fluids considered in this study. This performance is, then, benchmarked against the performance of inert fluids A and  $A_2$ .

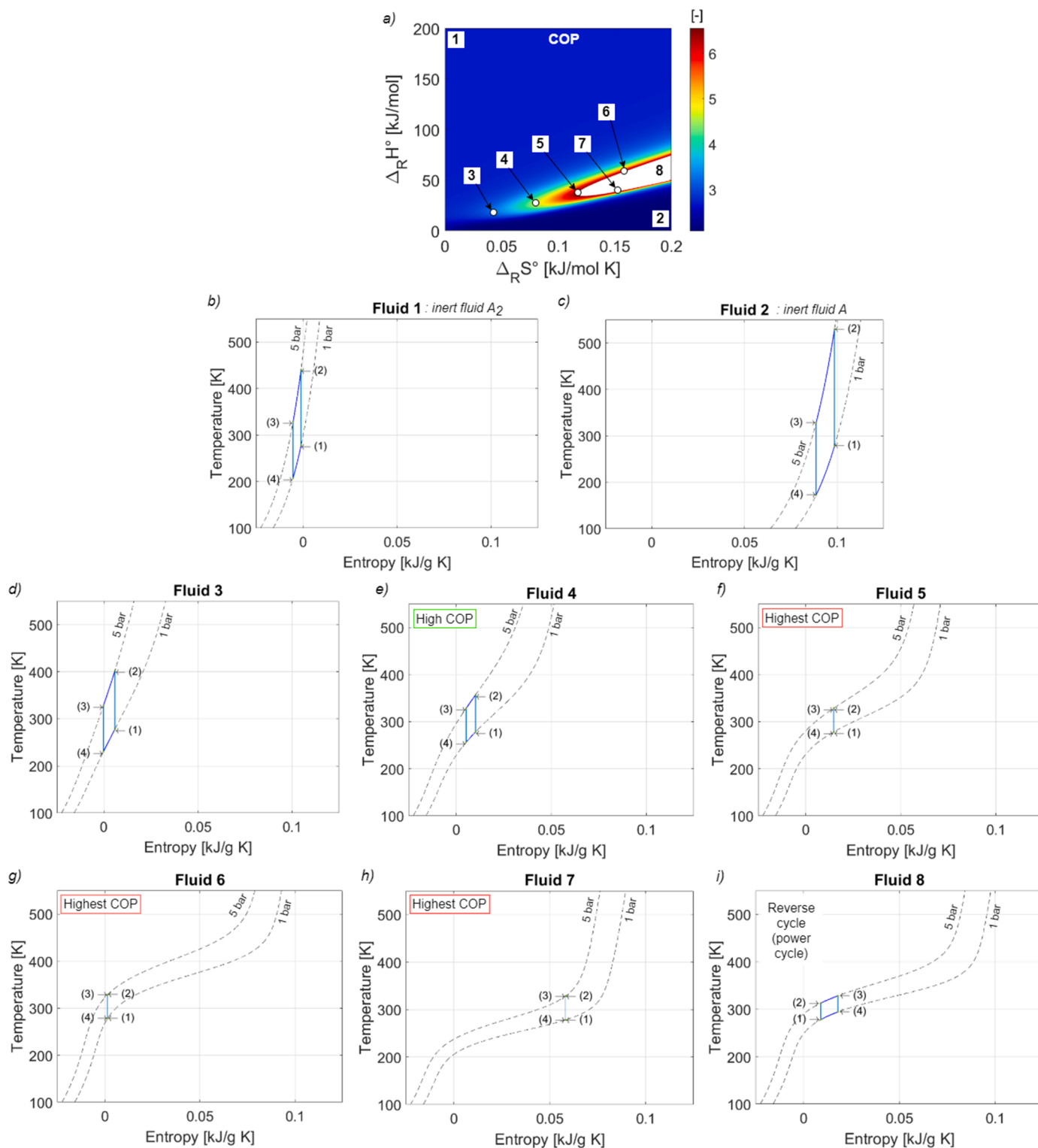
Therefore, the COP is defined as the ratio of the heat rejected at the heat sink side to the net work required by the HP system (Eq. (15)) and



**Fig. 5.** Coefficient of performance (COP) and second-law efficiency ( $\eta_{II}$ ) of the preliminary heat pump system with reaction stoichiometry  $A_{2(g)} \rightleftharpoons 2A_{(g)}$  for different reaction coordinates ( $\Delta_R S^\circ$ ,  $\Delta_R H^\circ$ ) and the following operating conditions:  $T_1=5^\circ\text{C}$ ,  $T_3=55^\circ\text{C}$ ,  $P_1=1$  bar, and  $P_2=5$  bar.

presented in Fig. 5 for the preliminarily defined system conditions in Table 3.

Fig. 5 demonstrates that the COP that can be achieved by reactive fluids in a HP system can reach a maximum of around 6.6 for the considered ranges of reaction coordinates and operating conditions. This means an increase in the COP by a factor of around 3.1 (214% increase) compared to inert fluid A and 2.4 (144% increase) compared to  $A_2$  for the same operating conditions. As for the second-law efficiency, defined as the COP value of the corresponding fluid against the Carnot/reversible performance of the HP system ( $\eta_{II} = \text{COP}/\text{COP}_{\text{Carnot}}$ ), the best performing reactive fluid achieves  $\eta_{II} = 80\%$  ( $\eta_{II,A} = 26\%$  and  $\eta_{II,A_2} = 33\%$ ).



**Fig. 6.**  $T$ - $s$  diagrams (Figs. (b)-(i)) of Fluids 1-8 characterized by the different reaction coordinates represented in Fig. (a) for the reaction stoichiometry  $A_{2(g)} \rightleftharpoons 2A_{(g)}$  and the following operating conditions:  $T_1=5^\circ\text{C}$ ,  $T_3=55^\circ\text{C}$ ,  $P_1=1$  bar, and  $P_2=5$  bar; Figs. (b)-(i) show the two isobars at the system's high and low pressures (black dashed curves) for each of the considered Fluids 1-8. In the  $T$ - $s$  diagrams, points (1) – (4) represent: (1) compressor's inlet; (2) compressor's outlet; (3) turbine's inlet; (4) turbine's outlet.

For completeness, it is specified that  $\text{COP}_{\text{Carnot}} = T_H / (T_H - T_C) \approx 8.1$ . However, the high COP region in Fig. 5 is also characterized by low values of specific heat rejected at the heat sink heat exchanger ( $q_H$ ), as presented in Fig. 3(c). This means that for a certain application there is a trade-off between the HP's performance and the amount of heat

provided by the system. Additionally, if  $q_H$  is small for the highest COP values, this means the net work required by the system is also small for these reaction coordinates. In fact, for the highest COP values, the corresponding net specific work required by the system is nil, compared to around 2 kJ/g for inert fluid A and 0.6 kJ/g for A<sub>2</sub>.

To better understand the work and heat quantities, temperature gradients, and entropy variations of the processes involved, the temperature-entropy ( $T$ - $s$ ) diagrams have been plotted in Fig. 6 for a selection of 8 sets of reaction coordinates spanning the different COP-level zones.

The selected fluids for examination are indicated on the colormap in Fig. 6(a). The corresponding  $T$ - $s$  diagram of each of the selected 8 fluids is illustrated in Fig. 6(b) to Fig. 6(i). Fig. 6(b) and Fig. 6(c) correspond to inert fluids  $A_2$  (Fluid 1) and  $A$  (Fluid 2), respectively. Additionally, Fig. 6(i) corresponds to the  $T$ - $s$  diagram of a fluid (Fluid 8) that lies in the infeasible white region of the colormap.

Observing Fig. 6(a), the COP increases from reactive Fluids 3 to 7. Examining the  $T$ - $s$  diagrams of the corresponding fluids in Fig. 6(d) to Fig. 6(h), several conclusions can be drawn. First, as the COP of the reactive fluid increases, the variation in specific entropy during heat gain and heat rejection in the two heat exchangers (between thermodynamic points (2) and (3), and (4) and (1) in the  $T$ - $s$  diagrams) decreases, until it becomes nil for the highest COP values. Therefore, the  $T$ - $s$  diagram would look like a vertical line or a narrow “reverse Carnot cycle” for the fluids achieving the highest COP values like Fluids 5, 6, and 7, as shown in Fig. 6(f), Fig. 6(g), and Fig. 6(h). Furthermore, as the COP achieved by a reactive fluid increases, the compressor’s outlet temperature  $T_2$  decreases whereas the turbine’s outlet temperature  $T_4$  increases. This can also be observed by comparing the  $T$ - $s$  diagrams of reactive Fluids 3 and 4. Recall that the compressor’s inlet temperature  $T_1$  and the turbine’s inlet temperature  $T_3$  are fixed at  $5^\circ\text{C}$  and  $55^\circ\text{C}$ , respectively, for all the studied fluids. Hence, as the COP value increases, the corresponding fluid’s  $T$ - $s$  diagram shrinks; the temperature gradients during compression, heat rejection, expansion, and heat absorption decrease, and the variation in entropy in the two heat exchangers also decreases.

It is noteworthy to point out that the reactive fluids characterized by the highest COP values lie at the border of the infeasible white zone. Beyond this border, lines (1-2) and (3-4) that correspond to compression and expansion, respectively, switch, and the system acts as an ideal Brayton cycle (isentropic compression, heat gain, isentropic expansion, and heat rejection). This is represented in Fig. 6(i). Although, for high COP values, the heat rejected into the heat sink decreases to almost nil (negative effect), the expansion work and compression work almost have identical values so that the expansion work compensates for the compression work, and the resulting net work required approaches zero, which is the reason behind the high COP value. On the other hand, slight differences in the COP value and temperature gradients are obtained for Fluids 5 to 7, as exhibited in Fig. 6(f)- Fig. 6(h). However, the main difference is the entropy values at the corresponding thermodynamic

points, which is dependent on the entropy of reaction relevant to the reactive fluid in question.

Given that Fig. 6(b) and Fig. 6(c) correspond to inert fluids  $A_2$  and  $A$  (Fluids 1 and 2), the difference between these two  $T$ - $s$  diagrams justifies why fluid  $A_2$  achieves a higher COP value than  $A$  as a working fluid in a HP system. Analogous conclusions can be drawn by comparing the  $T$ - $s$  diagrams of these inert fluids to the reactive ones.

Comparing the isobars in Fig. 6(b) and Fig. 6(c) that correspond to inert fluids  $A_2$  and  $A$ , respectively, to the ones corresponding to the reactive fluids (Fig. 6(d) to Fig. 6(i)), it can be deduced that the fluid’s reactivity affects the shape of the isobars. This shape depends on the variation of the fluid’s composition, and it is responsible for the shrinking of the  $T$ - $s$  diagram as the fluid becomes more reactive (achieving a higher COP value).

Given that the specific heat  $q_H$  results to be small for the highest performing reactive fluids, in order to achieve the same levels of thermal power,  $\dot{Q}_H$ , provided by comparable HPs operating with inert working fluids  $A$  and  $A_2$ , several reactive HPs can be utilized in series [34,35], or the mass flow rate of the reactive fluid based HP should be increased to guarantee an equivalent thermal power  $\dot{Q}_H = \dot{m} \cdot q_H$  to that of the inert fluids  $A$  and  $A_2$ , according to Eq. (18).

$$\begin{aligned} \dot{m}_{\text{reactive}} \cdot q_{H, \text{reactive}} &= \dot{m}_A \cdot q_{H,A} \\ \text{or} & \\ \dot{m}_{\text{reactive}} \cdot q_{H, \text{reactive}} &= \dot{m}_{A_2} \cdot q_{H,A_2} \end{aligned} \quad (18)$$

In fact, each set of reaction coordinates is characterized by a COP value and the ratios of the respective fluid’s COP to that of the inert fluids ( $\text{COP}_{\text{reactive}}/\text{COP}_A$  and  $\text{COP}_{\text{reactive}}/\text{COP}_{A_2}$ ) can be evaluated accordingly. Similarly, the ratios of the reactive fluid’s mass flow rate to that of the inert fluids ( $\dot{m}_{\text{reactive}}/\dot{m}_A$  and  $\dot{m}_{\text{reactive}}/\dot{m}_{A_2}$ ) can be computed for each set of reaction coordinates according to Eq. (18). The ratios  $\text{COP}_{\text{reactive}}/\text{COP}_{\text{inert}}$  and  $\dot{m}_{\text{reactive}}/\dot{m}_{\text{inert}}$  can be plotted against each other in order to observe the trade-off between the required mass flow rate and the COP achieved by the cycle, as shown in Fig. 7.

Several conclusions can be drawn from Fig. 7:

- The COP value achieved by inert fluid  $A_2$  is higher than that achieved by  $A$ . In fact, for inert fluids, the COP is only dependent on the pressure ratio of the cycle  $r_p = P_2/P_1$  and the ratio  $(\gamma-1)/\gamma$  where  $\gamma$  is the specific heat ratio  $C_p/C_v$  (the ratio of the specific heat capacity of the gas at a constant pressure to its specific heat capacity at a constant volume), according to Eq. (19):

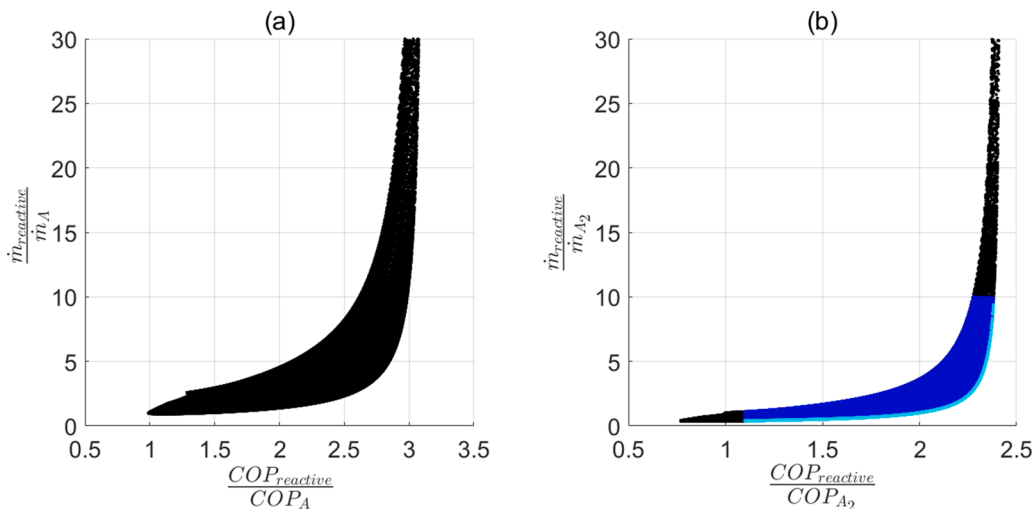
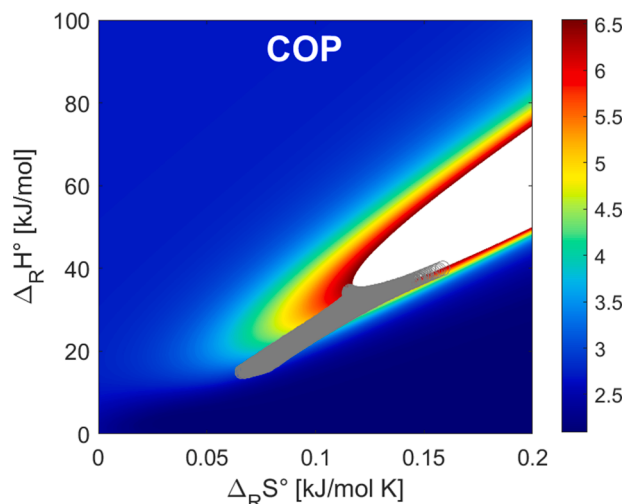


Fig. 7. Mass flow rate ratios of the studied fluids compared to inert fluids  $A$  (Fig. a) and  $A_2$  (Fig. b) as a function of the respective COP ratios with reaction stoichiometry  $A_{2(g)} \rightleftharpoons 2A_{(g)}$  for different reaction coordinates ( $\Delta_R S^\circ$ ,  $\Delta_R H^\circ$ ) and the following operating conditions:  $T_1 = 5^\circ\text{C}$ ,  $T_3 = 55^\circ\text{C}$ ,  $P_1 = 1$  bar, and  $P_2 = 5$  bar; suitable reactive working fluids that satisfy the conditions:  $\text{COP}_{\text{reactive}}/\text{COP}_{A_2} \geq 1.1$  and  $\dot{m}_{\text{reactive}}/\dot{m}_{A_2} \leq 10$  (marked in blue in Fig. (b)); selected reactive working fluids (marked in cyan in Fig. (b)).



**Fig. 8.** Zoom on Fig. 5 with the further indication (gray empty circle mark “o”) of the potential reactive working fluids  $A_{2(g)} \rightleftharpoons 2A_{1(g)}$  leading to  $COP / COP_{A_2} \geq 1.1$  (COP improvement with respect to the best inert fluid,  $A_2$ ) and  $\dot{m} / \dot{m}_{A_2} \leq 10$  (minimum feasible mass flow rate increase required), for the studied HP system ( $T_1=5^\circ\text{C}$ ,  $T_3=55^\circ\text{C}$ ,  $P_1=1$  bar, and  $P_2=5$  bar).

$$COP_{inert} = \frac{r_p^{-1}}{r_p^{\frac{\gamma-1}{\gamma}} - 1} \quad (19)$$

Therefore, since  $C_{p,A} < C_{p,A_2}$ , the coefficient of performance  $COP_{A_2}$  is higher than  $COP_A$ , given that the two systems are operating with the same pressure ratio.

- As the ratio of the COP versus  $COP_A$  or  $COP_{A_2}$  increases, the mass flow rate ratios ( $\dot{m}_{reactive} / \dot{m}_A$  and  $\dot{m}_{reactive} / \dot{m}_{A_2}$ ) also increase reaching thousands for certain reaction coordinates/fluids. The reason behind these high values is the presence of a boundary in the figure separating the feasible and infeasible regions. At this boundary, the net specific work required by the system and the specific heat provided to the heat sink become negligible (Fig. 6(f), Fig. 6(g), and Fig. 6(h)), and, beyond this boundary, in the white zone, the system functions as a Brayton cycle -providing work- rather than a HP that absorbs work. However, for some fluids, also allowing an increase in COP, the mass flow rate ratio is reasonable and technologically feasible; it is also less than that required for an inert fluid system in some cases ( $\dot{m}_{reactive} / \dot{m}_{inert} < 1$ ).

Since inert fluid  $A_2$  is better performing than  $A$  in the heat pump system considered ( $COP_{A_2} / COP_A \cong 1.3$ ), the reactive fluids can be

**Table 4**

Temperature  $T$ , pressure  $P$ , molar fraction of  $A_2$  in the working fluid mixture  $z_{A_2}$  (in percentage), and enthalpy  $h$  at each point of the thermodynamic cycle presented in Fig. 1 for a selected reactive fluid ( $\Delta_R S^\circ = 0.115$  kJ/mol K,  $\Delta_R H^\circ = 30$  kJ/mol, and reaction stoichiometry  $A_{2(g)} \rightleftharpoons 2A_{1(g)}$ ) and inert fluid  $A_2$  as working fluids in the HP system for the following operating conditions:  $T_1=5^\circ\text{C}$ ,  $T_3=55^\circ\text{C}$ ,  $P_1=1$  bar, and  $P_2=5$  bar.

Thermodynamic point	Working fluid				Inert fluid $A_2$ (best comparable inert fluid)		
	Selected reactive fluid		$z_{A_2}$ [%]	$H$ [kJ/g]	$T$ [°C]	$P$ [bar]	$h$ [kJ/g]
1	$T$ [°C]	$P$ [bar]					
2	5	1	24%	8.8	5	1	4.0
3	69.5	5	14%	12.2	167.4	5	6.4
4	55	5	19%	10.7	55	5	4.8
System's COP	-2.9	1	30%	7.5	-66	1	3.0
System's $\eta_{HP}$	5.5				2.7		
	68%				34%		

benchmarked only against fluid  $A_2$  in order to estimate the potential performance improvements compared to the best performing inert fluid. For the considered reaction stoichiometry, operating conditions, and system configuration, the suitable reactive working fluids should guarantee an improvement in the COP against inert fluid  $A_2$ , as well as an acceptable mass flow rate ratio  $\dot{m}_{reactive} / \dot{m}_{A_2}$ . In this study, a mass flow rate ratio of 10 or below is considered acceptable. Also, a minimum of 10% increase in the COP against inert fluid  $A_2$  is considered an adequate improvement in the performance. Therefore, the region of suitable reactive fluids should provide an intersection of these two conditions ( $COP_{reactive} / COP_{A_2} \geq 1.1$  and  $\dot{m}_{reactive} / \dot{m}_{A_2} \leq 10$ ). This region of suitable reactive working fluids can be observed in Fig. 7(b) marked by a blue color. Indeed, these boundaries/conditions can be adjusted based on the application considered. However, in this blue region of Fig. 7(b), for each value of  $COP_{reactive} / COP_{A_2}$ , the best performing reactive fluid is the one that results in the least value of  $\dot{m}_{reactive} / \dot{m}_{A_2}$  possible (least system cost and complexity). This corresponds to the lower boundary of the blue region (marked by a cyan color in Fig. 7(b)). Therefore, the reactive fluids that lie in this boundary are candidate working fluids for the heat pump system considered. Each one of these fluids are identified by a unique set of reaction coordinates,  $\Delta_R S^\circ$  and  $\Delta_R H^\circ$ . Thus, they can be labeled on the COP colormap, previously presented in Fig. 5, with a shaded region according to Fig. 8.

The reactive fluids identified in Fig. 8 form a starting point in the process of detecting potential real – rather than fictive – reactive fluids using the corresponding ranges of reaction coordinates ( $\Delta_R S^\circ, \Delta_R H^\circ$ ).

In order to better understand how the thermodynamic properties of the cycle vary between a reactive fluid and an inert one, a potential reactive working fluid is selected from the region shown in Fig. 8 with the following reaction coordinates:  $\Delta_R S^\circ = 0.115$  kJ/mol K and  $\Delta_R H^\circ = 30$  kJ/mol. The latter is compared to the better-performing inert fluid  $A_2$ , and the thermodynamic properties at each point of the HP cycle – labelled from 1 to 4 in Fig. 1 are presented in Table 4. The mass flow rate ratio  $\dot{m}_{reactive} / \dot{m}_{A_2}$  is 1.1 whereas the coefficient of performance ratio for the selected reactive fluid against  $A_2$  ( $COP_{reactive} / COP_{A_2}$ ) is 2.0 (103% increase in COP). For completeness, the  $T$ - $s$  and  $P$ - $h$  diagrams of inert gas,  $A_2$ , and the reactive fluid selected as potential candidate are shown in Fig. 9.

The HP's performance is assessed for a different reaction stoichiometry ( $A_{4(g)} \rightleftharpoons 4A_{1(g)}$ ) and the same operating conditions listed in Table 3. It is observed that all the considered fluids in this study (for the entire ranges of reaction coordinates) are feasible for operation in the HP system for the aforementioned stoichiometry. The corresponding compression work, expansion work, heat supplied to the heat sink, and coefficient of performance are presented in Fig. 10.

As presented in Fig. 10 for the considered ranges of reaction coordinates, it can be concluded that as the stoichiometry of the reaction changes from  $A_{2(g)} \rightleftharpoons 2A_{1(g)}$  to  $A_{4(g)} \rightleftharpoons 4A_{1(g)}$ , the overall performance of the system with the higher stoichiometric ratio is characterized by a highest COP value of around 4.7 (Fig. 10(d)). This signifies a 124%

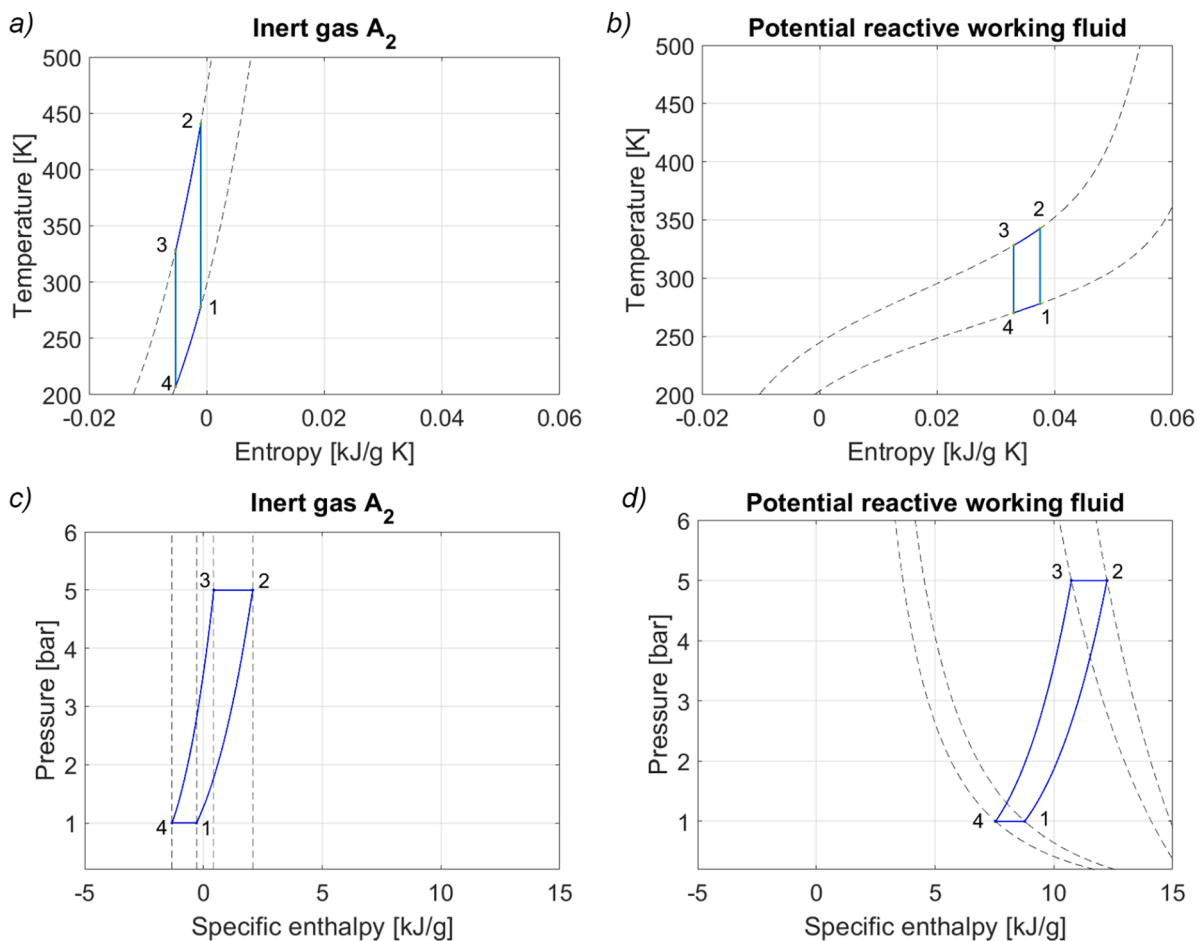


Fig. 9.  $T$ - $s$  diagrams and  $P$ - $h$  diagrams for the better-performing inert gas,  $A_2$  and one of the potential working fluids  $A_{2(g)} \rightleftharpoons 2A_{(g)}$  identified by  $\Delta_R S^\circ = 0.115$  kJ/mol K and  $\Delta_R H^\circ = 30$  kJ/mol.

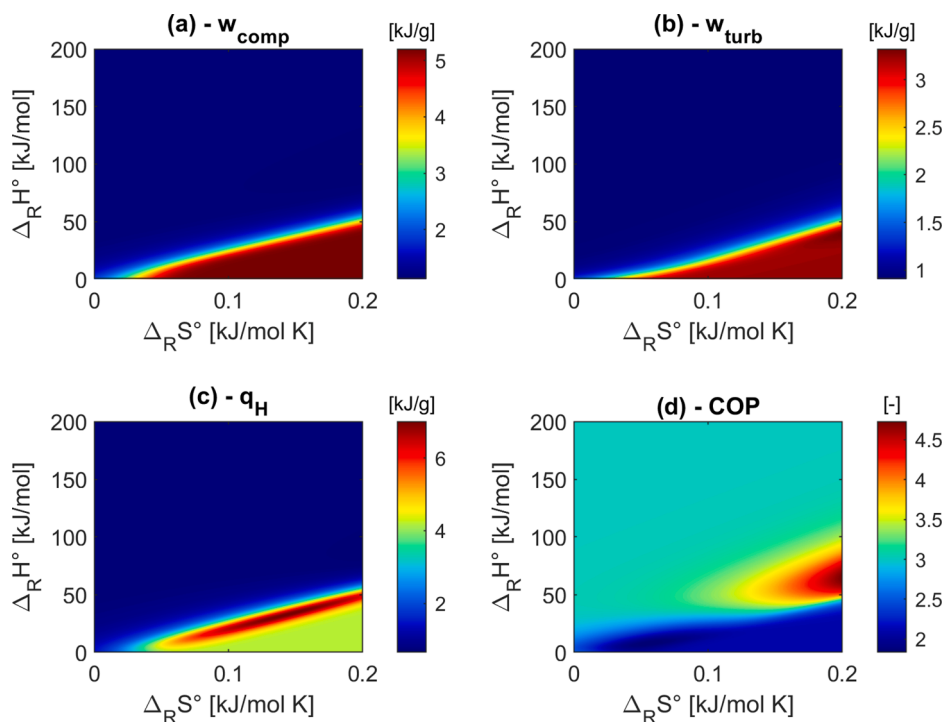


Fig. 10. Compression work, expansion work, heat supplied to the heat sink, and coefficient of performance for the different reaction coordinates ( $\Delta_R S^\circ$ ,  $\Delta_R H^\circ$ ) for reaction stoichiometry  $A_{4(g)} \rightleftharpoons 4A_{(g)}$  and the following operating conditions:  $T_1=5^\circ\text{C}$ ,  $T_3=55^\circ\text{C}$ ,  $P_1=1$  bar, and  $P_2=5$  bar.



improvement in performance compared to a system utilizing pure fluid A, and 57% improvement compared to that of a system utilizing working fluid A<sub>4</sub>. Therefore, the best performing reactive fluid, for the given reaction stoichiometry and operating conditions, achieves a second law efficiency  $\eta_{II} = 57\%$  ( $\eta_{II,A} = 26\%$  and  $\eta_{II,A_4} = 37\%$ ). Compared to reactive fluids characterized by the reaction stoichiometry  $A_{2(g)} \rightleftharpoons 2A_{(g)}$ , the COP values obtained due to the stoichiometry  $A_{4(g)} \rightleftharpoons 4A_{(g)}$  are lower, where the highest attainable COP is 4.7 instead of 6.6. This is due to the fact that the corresponding high COP region is characterized by lower values of  $q_H$  (Fig. 10(c)). On the other hand, the highest heat provided  $q_H$  achievable increases and reaches around 7.0 kJ/g. However, the corresponding COP value is lower than that of inert fluid A<sub>4</sub> and higher than that of A by around 35%.

Furthermore, evaluating the mass flow rate ratios according to Eq. (18) for the stoichiometry  $A_{4(g)} \rightleftharpoons 4A_{(g)}$  results in values that do not exceed 6.4 for the ratio  $\dot{m}_{reactive}/\dot{m}_A$  and 1.1 for  $\dot{m}_{reactive}/\dot{m}_{A_2}$  (similar to the stoichiometry  $A_{2(g)} \rightleftharpoons 2A_{(g)}$  for low and intermediate COP values, away from the boundary).

However, upon increasing the standard entropy of reaction  $\Delta_R S^\circ$  from 0.2 kJ/g K to 0.4 kJ/g K (increasing the range of fluids considered in the study), an infeasible zone appears in the colormaps of the system with reaction stoichiometry  $A_{4(g)} \rightleftharpoons 4A_{(g)}$ . The highest COP achievable by the system increases from 4.7 (Fig. 10(d)) to around 6.6, and this value is obtained at the boundary between the feasible and infeasible regions. Furthermore, the plots of the mass flow ratios compared to inert fluids A and A<sub>4</sub> as a function of the COP ratios become similar to the ones displayed in Fig. 7.

### 3.5. System's performance as a function of the operating conditions

After assessing a preliminary HP system with the operating conditions provided in Table 3, these conditions are varied in order to evaluate their effect on the system's performance. Therefore, in this section, the effect of changing the difference between the heat sink and heat source temperatures  $\Delta T_{H-C}$ , the temperature of the heat source  $T_C$ , the heat exchangers' pinch point temperature difference  $\Delta T_{pp}$ , and the system's high pressure  $P_2$  (or pressure ratio) is assessed. Note that a reaction stoichiometry of  $A_{2(g)} \rightleftharpoons 2A_{(g)}$  and the reaction coordinates ranges  $\Delta_R H^\circ = [0, 200]$  kJ/g and  $\Delta_R S^\circ = [0, 0.2]$  kJ/g K are considered.

For a heat source temperature fixed at 5°C, system's pressure ratio at 5.0, and heat exchangers' pinch point temperature difference at 5°C, the difference between the heat source and heat sink temperatures has been varied from 30°C to 100°C in order to study its effect on the system's performance. For  $\Delta T_{H-C} = 30^\circ\text{C}$ , the highest COP achievable among the considered reactive fluids is 7.8, as shown in Fig. 11(a). This accounts for

a 271% increase in performance compared to inert fluid A and 189% increase compared to A<sub>2</sub>. Note that the mass flow rate ratios ( $\dot{m}_{reactive}/\dot{m}_A$  and  $\dot{m}_{reactive}/\dot{m}_{A_2}$ ) corresponding to this best performing reactive fluid are in the order of thousands. However, as observed in Fig. 7, some other fluids with acceptable values of the mass flow ratios—offering a comparable improvement in the system's performance—can be selected. On the other hand, for  $\Delta T_{H-C} = 100^\circ\text{C}$ , the highest COP achievable by the reactive fluid  $A_{2(g)} \rightleftharpoons 2A_{(g)}$  and the considered ranges of reaction coordinates is 3.5, as presented in Fig. 11(b). This value is 67% higher than the COP corresponding to inert fluid A and 30% higher compared to A<sub>2</sub>. Therefore, as the temperature difference between the heat source and sink increases, the improvement in the COP of the heat pump system compared to inert fluids A and A<sub>2</sub> decreases. In other words, the advantage of using a reactive fluid over an inert one is more prominent for a lower value of  $\Delta T_{H-C}$ . It is noteworthy to mention that varying  $\Delta T_{H-C}$  does not affect the COP of inert fluids A and A<sub>2</sub> since the latter is only dependent on the pressure ratio and the specific heat capacities (constant for perfect gases), as demonstrated in Eq. (19). Furthermore, as  $\Delta T_{H-C}$  increases, the range of potential (feasible) reactive fluids decreases (the white infeasible zone grows). Considering the second-law efficiency, for  $\Delta T_{H-C} = 30^\circ\text{C}$ , the best performing reactive fluid provides an improved efficiency ( $\eta_{II} = 76\%$ ) compared to inert fluids A (20%) and A<sub>2</sub> (26%). Increasing  $\Delta T_{H-C}$  to 100°C, the highest second-law efficiency achievable becomes  $\eta_{II} = 92\%$ , which is an improvement compared to inert fluid A (55%) and A<sub>2</sub> (71%).

On the other hand, in order to investigate the effect of changing the heat source temperature  $T_C$  on the system's performance, the COP is evaluated for a heat source temperature of 50°C and two values of  $\Delta T_{H-C}$  (30°C and 100°C), similar to the results presented in Fig. 11. The rest of the operating conditions are maintained ( $r_p = 5.0$  and  $\Delta T_{pp} = 5^\circ\text{C}$ ). Observing Fig. 12(a), for a heat source temperature  $T_C = 50^\circ\text{C}$  and  $\Delta T_{H-C} = 30^\circ\text{C}$ , the highest COP achievable by the studied reactive fluids amounts to 9.0. Thus, the corresponding reactive fluid provides a 329% performance improvement compared to inert fluid A and 233% compared to A<sub>2</sub>. This improvement in the COP compared to the inert fluids is more prominent than the one obtained for a heat source temperature of 5°C. This can be observed by comparing Fig. 11(a) and Fig. 12(a). A similar conclusion can be drawn by comparing Fig. 11(b) and Fig. 12(b). At a higher source temperature (50°C) – for  $\Delta T_{H-C} = 100^\circ\text{C}$  – the improvement in the system's performance against that of inert fluids A and A<sub>2</sub> is more pronounced (90% and 48%, respectively, compared to 67% and 30% at  $T_C = 5^\circ\text{C}$ ). This improvement can be attributed to the fact that a higher heat source temperature means a higher quality and quantity of the heat absorbed by the system. Therefore, in order to provide the same amount of heat at the heat sink  $q_H$ , the system requires a lower work input. Furthermore, as demonstrated in

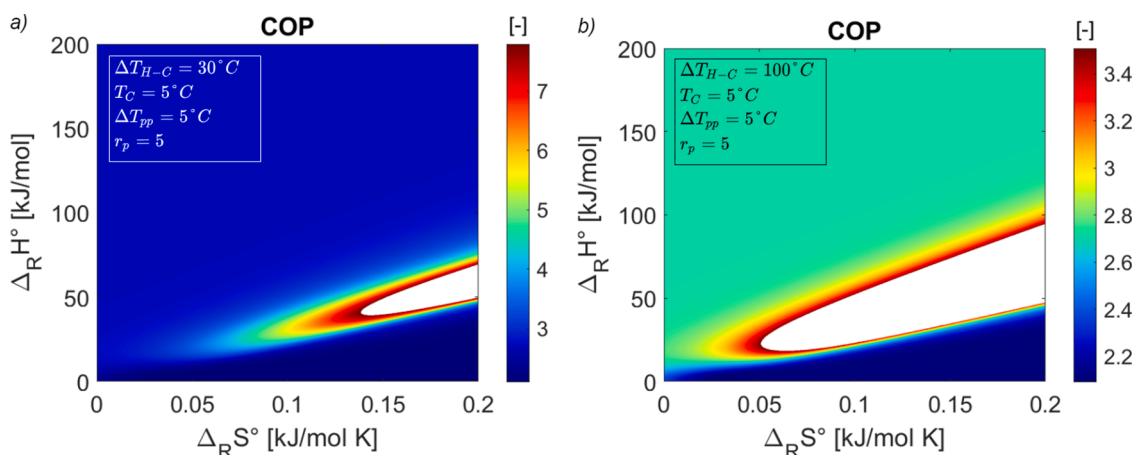
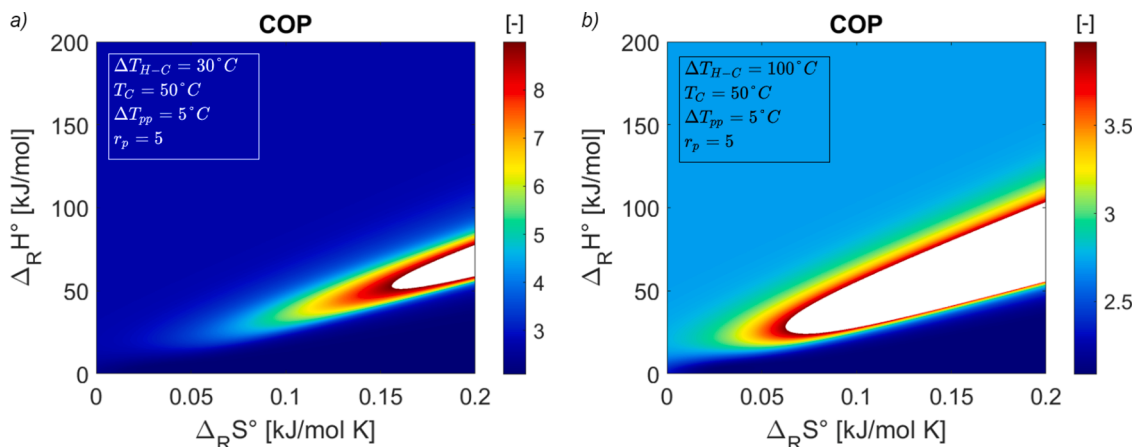


Fig. 11. Effect of the temperature difference between the heat sink and heat source on the performance of the heat pump system for reaction stoichiometry  $A_{2(g)} \rightleftharpoons 2A_{(g)}$  and the following operating conditions:  $T_C = 5^\circ\text{C}$ ,  $\Delta T_{pp} = 5^\circ\text{C}$ ,  $P_1 = 1$  bar, and  $P_2 = 5$  bar.



**Fig. 12.** System's performance for a heat source temperature  $50^\circ\text{C}$  and two different values of  $\Delta T_{H-C}$  ( $30^\circ\text{C}$  and  $100^\circ\text{C}$ ) given the reaction stoichiometry  $A_{2(g)} \rightleftharpoons 2A_{(g)}$  and the following operating conditions:  $\Delta T_{pp}=5^\circ\text{C}$ ,  $P_1=1$  bar, and  $P_2=5$  bar.

**Table 5**

The studied heat pump's performance, for the three cases of operating with inert gas A, inert gas  $A_2$ , and the best performing reactive fluid, for the considered eight sets of operating conditions, given the reaction stoichiometry  $A_{2(g)} \rightleftharpoons 2A_{(g)}$ .

System operating conditions			$\text{COP}_{\text{Carnot}}$	$\text{COP}_A$	$\text{COP}_{A_2}$	$\text{COP}_{\text{react,max}}$	$\eta_{II,A}$	$\eta_{II,A_2}$	$\eta_{II,\text{react,max}}$
$\Delta T_{H-C}$ $30^\circ\text{C}$	$T_C$ $5^\circ\text{C}$	$\Delta T_{pp}$ $5^\circ\text{C}$	10.3	2.1	2.7	7.8	20%	26%	76%
		$\Delta T_{pp}$ $10^\circ\text{C}$				6.4			62%
	$50^\circ\text{C}$	$\Delta T_{pp}$ $5^\circ\text{C}$	11.8	9.0	18%	23%	76%		
		$\Delta T_{pp}$ $10^\circ\text{C}$					7.3	62%	
$100^\circ\text{C}$	$5^\circ\text{C}$	$\Delta T_{pp}$ $5^\circ\text{C}$	3.8	3.5	55%	71%	92%		
		$\Delta T_{pp}$ $10^\circ\text{C}$					3.2	84%	
	$50^\circ\text{C}$	$\Delta T_{pp}$ $5^\circ\text{C}$	4.2	4.0	50%	64%	95%		
		$\Delta T_{pp}$ $10^\circ\text{C}$					3.7	88%	

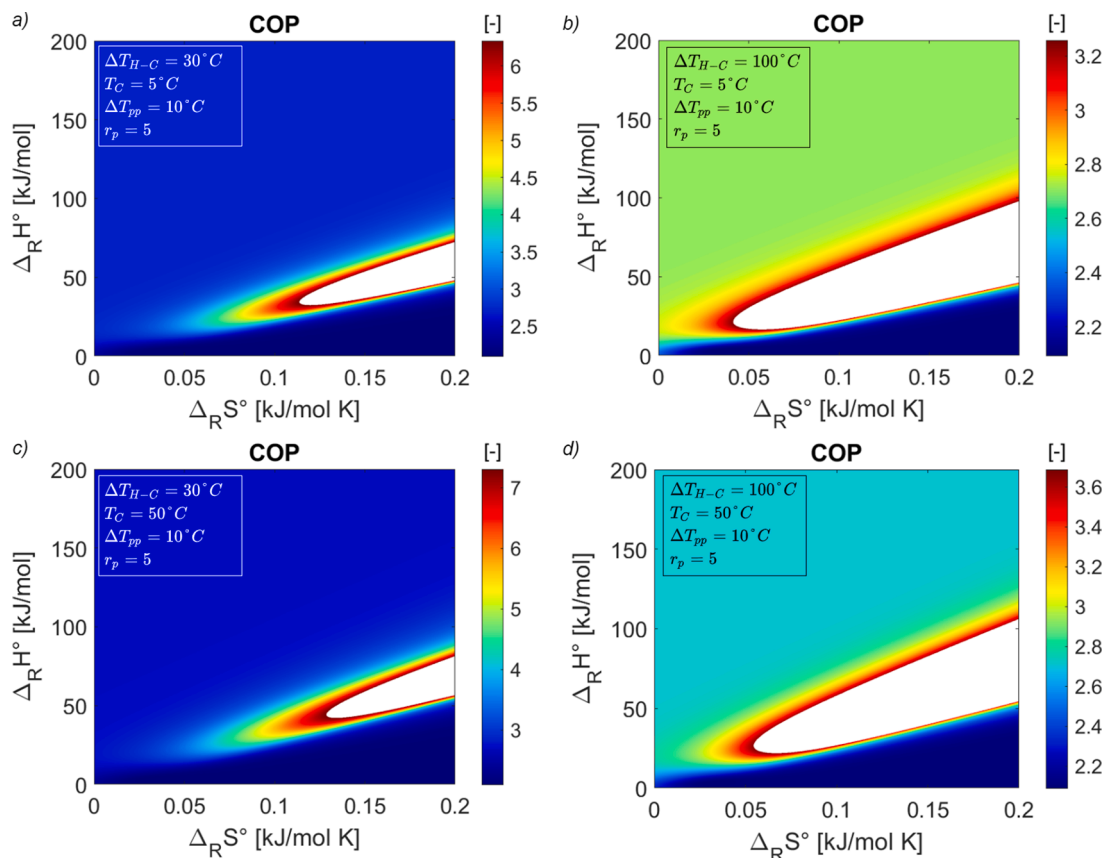
Fig. 11 and Fig. 12, as the heat source temperature increases from  $5^\circ\text{C}$  to  $50^\circ\text{C}$ , the range of potential reactive working fluids also increases (the white infeasible regions in the colormaps become smaller). Concerning the second-law efficiency of the system  $\eta_{II}$ , the best-performing reactive fluid achieves a second law efficiency of  $\eta_{II}=76\%$  for  $T_C=50^\circ\text{C}$  and  $\Delta T_{H-C}=30^\circ\text{C}$ . This is an improvement in the performance compared to inert fluid A ( $\eta_{II,A}=18\%$ ) and  $A_2$  ( $\eta_{II,A_2}=23\%$ ). Similarly, for  $T_C=50^\circ\text{C}$  and  $\Delta T_{H-C}=100^\circ\text{C}$ , the highest  $\eta_{II}$  achievable among the studied reactive fluids amounts to 95%, whereas the second-law efficiency corresponding to inert fluid A is 50% and that of  $A_2$  is 64%. Therefore, it can be concluded that as the heat source temperature increases, the improvement in the system's second-law efficiency  $\eta_{II}$  – due to utilizing a reactive working fluid – compared to that of inert fluids A and  $A_2$  is amplified.

In order to assess the effect of varying the heat exchangers' pinch point temperature difference  $\Delta T_{pp}$  on the system's performance compared to inert fluids A and  $A_2$ , the COP is evaluated for four different scenarios – that are included in Table 5 – at  $\Delta T_{pp}=10^\circ\text{C}$  instead of  $5^\circ\text{C}$  and presented in Fig. 13. The calculations have been conducted for two different values of  $\Delta T_{H-C}$  ( $30^\circ\text{C}$  and  $100^\circ\text{C}$ ), two different values of  $T_C$  ( $5^\circ\text{C}$  and  $50^\circ\text{C}$ ), and a pressure ratio  $r_p=5.0$ . Comparing Fig. 13(a) with Fig. 11(a), it can be observed that as  $\Delta T_{pp}$  increases from  $5^\circ\text{C}$  to  $10^\circ\text{C}$ . The highest COP achievable by the system decreases from 7.8 to 6.4 (19% decrease). The reason behind the decrease in performance of the HP system is that as the pinch point temperature difference increases, the performance of the heat exchangers decreases. The same conclusion can be drawn by comparing Fig. 13(b) and Fig. 11(b), Fig. 13(c) and Fig. 12(a), and Fig. 13(d) and Fig. 12(b). However, as the temperature difference between the heat sink and source increases, the effect of varying  $\Delta T_{pp}$  on the system's performance becomes less significant. For instance, for  $\Delta T_{H-C}=30^\circ\text{C}$  and  $T_C=5^\circ\text{C}$ , increasing  $\Delta T_{pp}$  from  $5^\circ\text{C}$  to  $10^\circ\text{C}$  results in a 19% reduction in the system's highest COP whereas for

$\Delta T_{H-C}=100^\circ\text{C}$  and the same heat source temperature, it results in a 9% reduction. On the other hand, for a constant value of  $\Delta T_{H-C}$ , as the heat source's temperature varies, the effect of changing  $\Delta T_{pp}$  on the COP is negligible. For instance, increasing  $\Delta T_{pp}$  from  $5^\circ\text{C}$  to  $10^\circ\text{C}$  for  $\Delta T_{H-C}=100^\circ\text{C}$  results in a comparable reduction the system's highest COP for both source temperatures  $5^\circ\text{C}$  and  $50^\circ\text{C}$ . Furthermore, comparing Fig. 11, Fig. 12, and Fig. 13, as the pinch point temperature difference increases, the range of potential reactive fluids is reduced. As for the second law efficiency  $\text{COP}/\text{COP}_{\text{Carnot}}$  the results for the studied cases are summarized in Table 5. Table 5 also summarizes the aforementioned results presented in this section for the eight sets of operating conditions.

Lastly, the system's high pressure  $P_2$  is increased from 5 bar to 20 bar in order to observe the effect on the system's performance. Accordingly, as the system high pressure increases, the range of potential reactive fluids increases (the white infeasible zone decreases). Furthermore, the performance (COP) of the reactive fluids compared to that of inert fluids A and  $A_2$  increases as the pressure increases. In example, for  $P_2=5$  bar, the increase in COP for the best-performing reactive fluid is 271% compared to inert fluid A and 189% compared to  $A_2$  (for  $T_2=5^\circ\text{C}$ ,  $\Delta T_{H-C}=30^\circ\text{C}$ , and  $\Delta T_{pp}=5^\circ\text{C}$ ). For the same operating conditions, with  $P_2=20$  bar, the performance of the system utilizing the best performing reactive fluid becomes 343% higher than that of pure fluid A and 265% than that of  $A_2$ . This means that the advantage of using a reactive fluid in a HP system is more prominent at higher pressures when compared to the performance of inert fluids A and  $A_2$ . However, this conclusion cannot be generalized for the second law efficiency,  $\text{COP}/\text{COP}_{\text{Carnot}}$ , where the change in the system's  $\eta_{II}$  (increase/decrease) is also influenced by other operating conditions.

Therefore, for the considered reaction coordinates and reaction stoichiometry, compared to the performance of inert fluids A and  $A_2$ , the advantage of utilizing a reactive fluid in a HP system (in terms of the COP) is more pronounced for a lower temperature difference between



**Fig. 13.** System's performance for a heat exchangers' pinch point temperature difference  $\Delta T_{pp}=10^{\circ}\text{C}$ , two different values of  $\Delta T_{H-C}$  ( $30^{\circ}\text{C}$  and  $100^{\circ}\text{C}$ ) and  $T_C$  ( $5^{\circ}\text{C}$  and  $50^{\circ}\text{C}$ ), pressure ratio  $r_p=5$ , and reaction stoichiometry  $A_{2(g)} \rightleftharpoons 2A_{(g)}$ .

the heat sink and source ( $\Delta T_{H-C}$ ), higher heat source temperature ( $T_C$ ), lower heat exchangers' pinch point temperature difference ( $\Delta T_{pp}$ ), and higher pressure ratio.

#### 4. Conclusion

In pursuit of assessing the potential of heat pumps operating with novel fictive reactive fluids – rather than inert ones – this work studies the performance of a spectrum of reactive fluids in each of the heat pump's devices for different operating conditions. Chemical equilibrium has been respected at each thermodynamic point in the cycle (compressor's inlet and exit and turbine's inlet and exit) in order to evaluate the chemical composition of the reactive fluid. In addition, the reactive fluid is assumed to be a mixture of ideal gases, and the heat pump system is considered ideal. Thus, the thermodynamic calculations were conducted accordingly, and two reaction stoichiometries have been considered in this study.

Results show that for the reaction stoichiometry  $A_{2(g)} \rightleftharpoons 2A_{(g)}$ , the coefficient of performance that can be achieved by reactive fluids in a heat pump system is 214% higher than that achieved by inert fluid A and 144% higher than that achieved by fluid  $A_2$ . This is due to the fact that the net work required by the heat pump system significantly decreases for the highest-performing reactive fluids compared to the inert ones. However, compared to inert fluids A and  $A_2$ , the heat provided by a heat pump system operating with the highest-performing reactive fluids to the heat sink is significantly lower. Therefore, there exists a trade-off between the system's COP and the required mass flow rate that is needed to compensate for the decrease in the heat output and ensure that the systems provide comparable thermal power. Hence, a set of criteria for selecting suitable working fluids can be defined to take into account these two parameters. In this study, a range of potential working

fluids has been identified based on the increase in the system's performance (COP) compared to that of the inert fluids and the mass flow rate required by the system in order to provide a comparable thermal power to that of the inert fluids. One of these potential reactive fluids was benchmarked against the better-performing inert fluid  $A_2$  in order to understand how the thermodynamic properties vary due to the occurrence of equilibrated chemical reactions within the working fluid. Results show an increase by 103% in the COP compared to a system utilizing fluid  $A_2$  where the required system's mass flow rate is only 10% higher than that needed for a system operating with inert fluid  $A_2$ .

For a reaction stoichiometry of  $A_{4(g)} \rightleftharpoons 4A_{(g)}$ , the highest COP is around 124% higher than that corresponding to inert fluid A and 57% higher than that of  $A_4$  for the considered ranges of reaction coordinates ( $\Delta_R S^{\circ}, \Delta_R H^{\circ}$ ).

On the other hand, the performance (COP) of the reactive heat pump system—compared to that utilizing inert fluid A or  $A_2$ —is seen to improve for a lower temperature difference between the heat sink and source, higher heat source temperature, lower heat exchangers' pinch point temperature difference, and higher pressure ratio.

As a next step, the performance of the heat pump will be assessed for real – rather than fictive – reactive fluids in order to grasp a more realistic sense of the potential gains of reactive heat pump systems.

#### Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

## Data Availability

Data will be made available on request.

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