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Disclamer

I would like to apologise to the reader for the crudeness of this version. References are sparse and results lack discussion. Please keep in mind this is a work in progress.

A physical baseline to model photovoltaic development and estimate its net product

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Abstract

Photovoltaic production dynamic is usually modeled using a sigmoïd or Scurve function, without any physical bases. This paper aims at developing a physical model based on energy conservation and ERoEI definition, that could reproduce a S-curve function and allow to investigate the net energy delivered by the photovoltaic industry. This approach gives some new insights on the discussion on energy delivered by renewable and low carbon energy, as it highlights the role of energy re-investment in ERoEI calculation. It also allows to investigate energy policies that could lead to a smooth energy transition.

Keywords: PV production, ERoEI, dynamic model, net energy, energy transition

¹ Introduction

In the frame of fossil fuel depletion and climate change, development of 2 renewable, or at least low carbon energy source is a major issue for mod-3 ern societies. In particular, photovoltaic (PV) system development is often 4 model by a logistic (sigmoïd or S-curve) function (Cherp et al. (2021)), the solution of the Verhulst equation. Despite the ability of the S-curve to fit PV 6 development in most countries, as in Cherp et al. (2021), there is no physical bases for such model, hence the analysis of its parameters does not provide 8 insight on the PV development capability. In this article, a physical model 9 is suggested for PV system development, based on energy conservation and 10 EROEI, as previously done for fossil liquid fuel in Lamorlette (2022). This 11

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model is discussed to see how it can provide a S-curve, in accordance with 12 Cherp et al. (2021). It is also applied to global PV system development 13 to investigate the re-investment trend of the PV industry. This allows to 14 estimate the net energy provided by PV systems to society, which depends 15 indirectly on ERoEI, contrary to the common assumption that net energy 16 on gross energy is equal to (ERoEI - 1)/ERoEI (as presented in Murphy 17 (2014) for instance). This point is discussed in details, providing insights on 18 the controversy on PV net energy discussed in Ferroni and Hopkirk (2016) 19 and Raugei et al. (2017). Finally, investment for energy source development 20 in the frame of energy transition is discussed, based on recent work on fos-21 sil fuel depletion, to suggest adequate policies that could ensure a smooth 22 energy transition. 23

²⁴ 1. Development of the PV industry

As proposed in Lamorlette (2022) for the development of the oil industry, based on energy conservation and ERoEI definition, a model is here developed to describe the development of the PV industry. It is firstly derived based on yearly (discrete) production, then the model is written using a continuous formalism, what leads to an ODE.

30 1.1. Discrete approach

The growth and decay is here considered over a one year time laps ($\Delta t = 1$ year). The growth is due to the industry expansion coming from energy re-investment. The decay is due to the closing of production sites, which are designed to last for a period τ , according to their ERoEI calculation, with $\tau \sim 20 - 30$ years (a PV unit lifespan). PV unit efficiency decrease is indirectly taken into account in the growing term, as explained in the next section.

38 1.1.1. Growing

Let us consider a yearly production of PV energy Q, available at point of use. A fraction k of this production (dimensionless, with k in [0; 1]) is re-invested to develop the PV industry on a year n. Energy conservation and ERoEI definition allow to write the increase in production ΔQ^+ on a year n, considering an equivalent homogeneous production over the whole lifespan τ of a PV unit (i.e. smoothing the efficiency decrease of a PV unit over its whole lifespan). With an energy investment $Q_n k$, one get an energy ⁴⁶ $Q_n k E Ro E I_n$ during τ years after the investment is done, based on ERoEI ⁴⁷ definition. The energy increase per unit time reads $Q_n k E Ro E I_n / \tau$. It leads ⁴⁸ to:

$$\Delta Q_n^+ = Q_n k_n \frac{ERoEI_n}{\tau} \Delta t \,. \tag{1}$$

49 1.1.2. Decay

The decay on a year n, ΔQ^- , is equal to the increase on year $n - \tau$, as it is due to the closing of sites developed τ years before. Hence one get:

$$\Delta Q_n^- = \Delta Q_{n-\tau}^+ = Q_{n-\tau} k_{n-\tau} \frac{ERoEI_{n-\tau}}{\tau} \Delta t .$$
 (2)

Using Eq.(1) and Eq.(2), the increase in production on a year n, $Q_{n+1}-Q_n$ can be written:

$$Q_{n+1} - Q_n = \Delta Q_n^+ - \Delta Q_n^- = \frac{1}{\tau} \left(Q_n k_n E Ro E I_n - Q_{n-\tau} k_{n-\tau} E Ro E I_{n-\tau} \right) \Delta t \,.$$
(3)

54 1.2. Continuous equivalence

Eq.(3) can be written as an ODE, taking $\Delta t \to 0$. It leads to $(Q_{n+1} - Q_n)/\Delta t = \dot{Q}$ and therefore:

$$\dot{Q} = \frac{1}{\tau} \left(Q(t)k(t)ERoEI(t) - Q(t-\tau)k(t-\tau)ERoEI(t-\tau) \right) .$$
(4)

This equation shows a convolution term which could make it complicated or even impossible to solve analytically. Nevertheless, as discussed later, the term ΔQ^- can be neglected at short or medium time scale, which would lead to analytical solutions for Eq.(4).

⁶¹ 2. Solution for a linear investment policy at medium time scale, ⁶² recovering the S-curve

Let us first discuss the relative contribution of decay in the production dynamic, that is $\Delta Q^-/\Delta Q^+$. At a time scale smaller than τ (i.e. short time scale), this contribution is strictly zero. During the development phase of a PV industry (at local scale (a country), or at global scale), according to all the measured values presented in Cherp et al. (2021), Q evolves at a time scale way smaller than τ . It means that practically, $\Delta Q^-(t) \ll \Delta Q^+(t)$ and ⁶⁹ then ΔQ^- can be neglected at medium time scale, the time scale at which ⁷⁰ PV is developing. It leads to:

$$\dot{Q} = \frac{1}{\tau}Q(t)k(t)ERoEI(t).$$
(5)

⁷¹ Let us now consider a linearly evolving investment over a period on which a ⁷² PV industry plans to develop from $Q(t_0) = Q_0$ (an initial, external energy ⁷³ input) to $Q(t_f) = Q_{goal}$ (a goal of production), where t_0 is the time at the ⁷⁴ beginning of the investment and t_f the time at the end of the investment. ⁷⁵ Then k = 1 at the beginning of the investment $(k(t_0) = 1), k = 0$ when the ⁷⁶ industry is fully developed (i.e. $k(t_f) = 0$) and k evolves as $1 - Q/Q_{goal}$ in ⁷⁷ between (i.e. k proportional to -Q). This leads to:

$$\dot{Q} = \frac{1}{\tau} Q(t) \left(1 - \frac{Q(t)}{Q_{goal}} \right) ERoEI(t) .$$
(6)

⁷⁸ Eq.(6) is strictly a Verhulst equation, with Q_{goal} the carrying capacity. With ⁷⁹ constants τ and ERoEI, it leads to a S-curve solution, which is in line with ⁸⁰ the work of Cherp et al. (2021).

This approach does not directly take into account the potential lack of material to produce PV units or the lack of space to due to geophysical constraints, but it actually takes it into account via a future decrease of PV EROEI. However, this aspect is not developed in this study as it considers only constant EROEI as a baseline, in order to investigate the different analytical solution one can get from Eq.(3) or Eq.(4).

⁸⁷ 3. Short time scale analysis of global PV production

Contrary to many countries where the saturation (or "market size") has 88 been reached (as Portugal, Germany, Belgium or Greece, according to Cherp 89 et al. (2021)), the global PV production seems to be in its development 90 phase. Indeed, according to BP (2021), the PV product follows an expo-91 nential growth, with a characteristic time $t_{exp} \sim 2.82$ years (this fit provides 92 a determination coefficient higher than 0.98 on the period 2000-2021). At 93 short or medium time scale, Eq.(3) or Eq.(4) can be solved at constants τ 94 and EROEI, leading to an exponential solution. This solution exhibits the 95 following characteristic time: 96

$$t_{exp} = 1/ln(1 + kERoEI/\tau).$$
(7)

⁹⁷ Identification can then leads to an estimation of the PV industry investment.

98 3.1. Estimation of PV industry investment

The previous remark suggests a way to estimate the re-investment of the 99 PV industry on itself in order to ensure a self-growing business. This as-100 sumption seems reasonable, since PV industry can hardly expect external 101 energy for its development, as global energy consumption ensure the global 102 GNP (as suggested by the work of Tim Garrett), and our economy requires 103 GNP to keep increasing. Therefore, without external energy input, the pre-104 vious relationships allow to estimate the investment, as long as averaged, 105 effective values can be evaluated for τ and *ERoEI*. τ is taken equal to 20 106 to 30 years, based on a PV unit lifespan. As remarked in section 1.1.1, the 107 production Q that is considered is taken at point of use, which means ERoEI 108 should be evaluated accordingly. This would refer to an ERoEI at point of 109 use. According to Raugei et al. (2017), $ERoEI \sim 9 - 10$. 110

An identification of k is then performed based on t_{exp} global value and 111 theoretical expression (Eq.(7)). The following behaviour is observed: For 112 $\tau = 20$ years, an *ERoEI* of 7 or lower would lead to $k \ge 1$. For $\tau = 30$ years, 113 an *ERoEI* of 11 or lower would lead to $k \geq 1$ which seems economically 114 impossible, as it would mean that PV industry is an energy sink. This 115 emphases the result of Raugei et al. (2017) on the minimum possible value 116 of PV ERoEI. It also suggests that global PV development is close to its 117 maximum with k(t) = 1 from the beginning of PV development. 118

119 3.2. Estimation of the net production

¹²⁰ Contrary to what the development of Eq.(4) could suggest, based on the ¹²¹ energy available at point of use, it does not strictly provides the net energy ¹²² from PV systems. Indeed, a fraction k is taken for re-investment, hence the ¹²³ net product Q_N reads:

$$Q_N(t) = (1 - k(t))Q(t).$$
(8)

According to the previous remark on the averaged, effective, value of k, 124 it suggests that net energy from PV was and is still close to zero. This 125 could be a reason that motivated the study of Ferroni and Hopkirk (2016) 126 which claims that PV is not producing any net energy and could even be an 127 energy sink. The answer of Raugei et al. (2017) to the study of Ferroni and 128 Hopkirk (2016) seems right in term of ERoEI values, however the study of 129 Ferroni and Hopkirk (2016) seems right in term of net energy delivery. This 130 whole result on net energy from PV systems is nevertheless very far from 131

the classical relationship presented in Murphy (2014) for oil (for instance),
where net energy is supposed to depend directly on gross energy and ERoEI
through the relation:

$$Q_N = Q \frac{ERoEI - 1}{ERoEI} \,. \tag{9}$$

It seems that the confusion might come from the original derivation of this relationship, which was done for oil. Indeed, for oil, this relationship almost applies according to energy conservation, with two corrections. Firstly, as highlighted in Lamorlette (2022), it should read:

$$Q_N = Q \frac{ERoEI - 1}{ERoEI_W} \,, \tag{10}$$

where $ERoEI_W$ is the ERoEI at the wellhead. The paper of Hall et al. 139 (2009) contains everything in the text to develop Eq.(10), even a numerical 140 application in Table 3. The paper of Lamorlette (2022) merely presents a 141 more complete mathematical formulation of the concepts presented in Hall 142 et al. (2009). Secondly, as discussed in Lamorlette (2022), Q_N in Eq.(10) 143 still misses the role of energy re-investment. Hence a (1-k) (with k being 144 the investment of the oil industry) correction was added. As k for oil is 145 historically lower than 1% (see Lamorlette (2022)), Eq.(10) is practically 146 applicable to oil with accurate results. 147

This whole rational however breaks down for the PV industry during its development phase, as PV industry development depends straightforwardly on *ERoEI* but its net energy does not, mainly because re-investment is close to unity. As the same energy development modeling can be applied to wind, nuclear or other low carbon energy, net energy from these sources should be carefully evaluated during the industry development.

154 4. Toward a smooth energy transition

155 4.1. Sustaining a steady-state dynamic at long time scale

Solutions presented in this article in section 2 and 3 are valid at short and medium time scale, neglecting ΔQ^- . However, a steady-state at long time scale requires to take it into account, changing the required value of k to sustain this dynamic. This steady-state investment can be evaluated thanks to Eq.(4): Let us consider a constant \dot{Q} , at constant *ERoEI*. Eq.(4) leads to k = 1/ERoEI and $\dot{Q} \to 0$ when $t \gg \tau$. It means that when k decreases

according to a given energy policy, in order to "replace" the lack of energy 162 due to fossil fuel depletion, it should be kept above 1/ERoEI or equal to 163 1/ERoEI once this value is reached, to ensure the investment needed at long 164 time scale. When this long time scale steady-state is reached, it is worthy to 165 notice that $Q_N = (1-k)Q = Q(ERoEI - 1)/ERoEI$. Hence this relation 166 actually applies to any energy source that follows equations similar to Eq.(4)167 and Eq.(8) (i.e. PV, nuclear and wind), but only once a steady-state is 168 reached. This result can explain the controversy about PV ERoEI: if one 169 considers ERoEI at the most extreme boundary of the PV industry, that 170 is $ERoEI_{EXT}$, it should take into account the whole re-investment and its 171 value seems to be close to 1, since k seems to be close to 1, what is in line 172 with Ferroni and Hopkirk (2016) and de Castro and Capellán-Pérez (2020). 173 This extended ERoEI is somehow "dynamic", as it takes into account the 174 industry dynamic. On the other hand, an ERoEI at point of use could be 175 considered as "static" as it does not depends on the industry dynamic. At 176 the industry steady-state, both dynamic and static ERoEI have the same 177 value, according to the result above, however the dynamic value does not 178 provide any insight on the ability of a technology to develop, which suggests 179 it is not a proper index to compare technologies. 180

It means that ERoEI is not a sufficient index to evaluate the worthiness 181 of a given technology development, it can only evaluate its sustainability 182 once the industry is developed. The present results suggests a value of 7 183 would be enough to sustain a production, with roughly 15% of the production 184 dedicated to sustain the production. In our case, with PV, according to the 185 results of section 3.1 and Eq.(8), the net production at steady-state will be 186 approximately 90% of the global PV production. It seems that the problem 187 of energy transition actually requires to answer the following question for 188 a given technology: "How long will it take to reach this steady-state? Is it 189 possible to reach it before facing fossil fuel depletion ?", what is not depending 190 only on ERoEI, as explained in the next section for PV and nuclear. 191

192 4.2. Estimating the ability of an energy industry to grow

In order to evaluate the growing capacity of a given technology over a period t_{trans} , Eq.(3) could be used, with adaptation specific to each considered technology. For PV, it can be used straightforwardly. Considering an energy increase I_{PV} , starting with a yearly amount Q_0 , according to Eq.(3), the PV growth rate g_{PV} is $g_{PV} = 1 + ERoEI/\tau$, then, with $G_{PV} = g_{PV}$:

$$I_{PV} = Q_0 g_{PV}^{t_{trans}} = Q_0 G_{PV}^{t_{trans}}.$$
 (11)

For nuclear (and wind), Eq.(3) should take into account the time t_{invest} needed to develop a production site (a nuclear power plant). This requires to apply Eq.(3) on a time laps $\Delta t = t_{invest}$, using the same rational as previously. For nuclear, it leads to (subscript Nu relates to nuclear):

$$Q_{Nu_{n+t_{invest}}} - Q_{Nu_n} = \frac{t_{invest}}{\tau_{Nu}} \left(Q_{Nu_n} k_{Nu_n} E Ro E I_{Nu_n} - Q_{Nu_{n-\tau_{Nu}}} k_{Nu_{n-\tau_{Nu}}} E Ro E I_{Nu_{n-\tau_{Nu}}} \right)$$
(12)

²⁰² Based on Eq.(12), the growth rate g_{Nu} is $g_{Nu} = 1 + t_{invest} ERoEI_{Nu}/\tau_{Nu}$. ²⁰³ This growth rate is applied over $t_{trans}/t_{invest} \sim 2$ investment time steps. It ²⁰⁴ means that the increase in energy I_{Nu} , starting with a yearly amount Q_0 can ²⁰⁵ be estimated the following way, with $G_{Nu} = g_{Nu}^{1/t_{invest}}$:

$$I_{Nu} = Q_0 g_{Nu}^{t_{trans}/t_{invest}} = Q_0 G_{Nu}^{t_{trans}}.$$
(13)

The quantity I/Q_0 (or G) represents the ability of a given technology to 206 grow in t_{trans} years (or per annum for G). For PV, $G_{PV} = 1.38$ based on the 207 previous analysis. Taking $\tau_{Nu} = 40$ years and considering $t_{invest} = 8$ years for 208 nuclear, according to EDF (2018), $G_{Nu} = 1.31 - 1.38$ (depending on the value 209 used for $ERoEI_{Nu}$, 40 or 60 according to World Nuclear Association (2018)). 210 This result suggests that nuclear is actually not a safer investment to cope 211 with the end of fossil fuels, contrary to what the *ERoEI* values suggest. It 212 also highlights that the ability of a technology to replace an energy source 213 does not depend only on its *ERoEI* but also on t_{invest}/τ and t_{trans}/t_{invest} , 214 due to the general expression of I/Q_0 . 215

4.3. An energy policy based on fossil fuel depletion and growth capacity of PV and nuclear

On the one hand, according to the study of Lamorlette (2022), it is sug-218 gested that the net peak oil might arrive as soon as 2028 (based on the results 219 obtained with the most reliable ERoEI data for oil), with a 40% production 220 decrease in 2035 and a 85% production decrease in 2050. The study of Lam-221 orlette (2022) can also be extrapolated to estimate the net peak gas around 222 2036 (based on the results obtained with the ERoEI data for oil and gas), in 223 accordance with the results of Delannoy et al. (2021a), with a decrease rate 224 similar to oil (40%) production decrease in 2043 and a 85\% production de-225 crease in 2058). According to the study of Delannoy et al. (2021b), net peak 226 oil might arrive as soon as 2024, with a production decrease of roughly 25%227 in 2030. On the other hand, according to the Paris agreement, use of fossil 228

fuel should stop in 2050. Based on these consideration, a worst case scenario can be build for energy substitution, taking also into account the need for an increasing energy input for our societies. This need is here evaluated using a business as usual assumption for energy consumption similar to the one suggested in Lamorlette (2022), that is a linear increase of the global energy consumption, which fits the data of BP (2021) on the period 1950-2021 with a determination coefficient higher than 0.99.

These data suggest energy transition should begin in 2024, at the net 236 peak oil. Considering PV (or a mix of sources with equal growth rate G) 237 as the unique substitute, since PV accounts for 1.63% of the global energy 238 mix in 2021 (BP (2021)) and considering oil account for 30.9% of the global 239 energy mix in 2021 BP (2021)), PV production needs to be multiplied by 5.1240 by 2030 and multiplied by 8.8 by 2035. Considering gas account for 24.4%241 of the global energy mix in 2021 (BP (2021)), PV production needs to be 242 multiplied by 18.4 by 2040. In order to follow the Paris agreement, it needs 243 to be multiplied by 66 by 2050. 244

The following transition scenario is proposed: PV growth rate is based 245 on its fitted value on the period 2000-2021, k is kept equal to 1 until 2023, 246 where it begins to decrease linearly until reaching the value 1/ERoEI in 20 247 years. k is then kept constant to reach the steady-state depicted in section 248 4.1. Eq.(4) and Eq.(8) are solved numerically from 2021 and the ratio R249 of net energy at time t on gross energy in 2021 is computed to compare 250 it with the requirement presented above. Table 1 presents the comparison 251 between the two, showing a smooth transition can be achieved without any 252 additional external energy input. Nevertheless, it shows that around 2030, 253 14% of the lack of energy, hence 3.5% of the global energy mix (compared 254 to the business as usual) cannot be covered. It suggests a plateau of energy 255 might occur around 2030 before reaching the business as usual again, until 256 a steady-state is reached around 2060, after a slight overshoot between 2050 257 and 2060. Also, as mentioned in section 2, this behaviour requires a constant 258 ERoEI, which should be satisfied to ensure the energy transition and the 259 steady-state after 2060. 260

Finally, it is worth noting here that this rational has been conducted at global scale, but it could also be applied at local scale (i.e. a country) to determine a specific, efficient investment policy, based on the resources and energy mix of a given country.

time (year)	required R	computed R	relative difference
2030	5.1	4.4	-14%
2035	8.8	20	+127%
2040	18.4	56	+204%
2050	66	100	+52%

Table 1: Ratio of PV net energy at time t on gross energy in 2021

²⁶⁵ Conclusion and opening

In this article, a model is presented to study PV production dynamic.
This model is able to reproduce the behavior of the previous S-curve function
model. It also shows the following features:

- The model development, based on energy conservation and ERoEI definition, is applied to PV but can be applied also to wind and nuclear.
- It allows to explain why the usual relationship between gross, net energy and ERoEI ($Q_N/Q = 1 - 1/ERoEI$) does not apply to any low carbon technology during its development, before a steady-state production is reached.
- It provides new insights on the PV net energy discussion, explaining how the investment dynamic can modify artificially the ERoEI measurement. This point highlights why ERoEI should be calculated at point of use to compare technologies.
- It shows that a technology development ability depends on ERoEI, but also on two dimensionless times: t_{invest}/τ and t_{trans}/t_{invest} .
- It suggests an energy policy that ensure a smooth energy transition, which leads to a steady-state production of energy around 2060.

Finally, it seems important to notice that, according to Barrau (2022), climate change is "the tree that hides the forest". The collapse of ecosystems is a deeper and more important problem our societies are facing. The steady-state presented before is very unlikely low enough to ensure the balance of earth ecosystems. Therefore, a sequel to this work could be to ask: "What steady-state (i.e. global human energy per unit time) could allow the ecosystems to recover a regime made of quasi-static transformations, maximising the lifespan of the earth system as we know it, by minimising entropy creation ?".

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