



# Capillary-force-driven self-assembly of carbon nanotubes: from ab initio calculations to modeling of self-assembly

Stefania Carapezzi, Gabriele Boschetto, Aida Todri-Sanial

## ► To cite this version:

Stefania Carapezzi, Gabriele Boschetto, Aida Todri-Sanial. Capillary-force-driven self-assembly of carbon nanotubes: from ab initio calculations to modeling of self-assembly. *Nanoscale Advances*, 2022, 4 (19), pp.4131-4137. 10.1039/D2NA00295G . hal-03777645

**HAL Id: hal-03777645**

**<https://hal.science/hal-03777645>**

Submitted on 7 Oct 2022

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Distributed under a Creative Commons Attribution 4.0 International License

Cite this: *Nanoscale Adv.*, 2022, 4, 4131

# Capillary-force-driven self-assembly of carbon nanotubes: from *ab initio* calculations to modeling of self-assembly†

Stefania Carapezzi,<sup>‡</sup> Gabriele Boschetto<sup>‡</sup> and Aida Todri-Sanial<sup>‡</sup>\*Received 10th May 2022  
Accepted 22nd August 2022

DOI: 10.1039/d2na00295g

rsc.li/nanoscale-advances

In elasto-capillary driven self-assembly of arrays of carbon nanotubes (CNTs) different factors play a role, from the mechanical properties of CNTs to the array geometry. In this work, we provide a multi-scale investigation where we first use density functional theory (DFT) to predict fully *ab initio* relevant mechanical properties such as Young's modulus, Poisson's ratio, and surface energy. To the best of our knowledge, we are the first to report DFT calculations of the surface energy of CNTs. Then, we feed the computed DFT parameters into a model for capillary-force-driven self-assembly of CNTs. By doing so, we are able to derive and predict cross-correlation between material parameters and array architecture.

## 1 Introduction

The rational design of micro-/nano-scaled material architectures has recently attracted huge interest as a means to engineer their physical properties. For instance, vertically aligned nanowires (NWs) modulate the optical properties of surfaces because their geometry (diameter, height, pitch) can tailor light confinement and absorption. The consequent enhancement of light harvesting is greatly demanded in photovoltaic applications.<sup>1</sup> Arrays of carbon nanotubes (CNTs) allow to build highly-dense 3D integrated circuit architectures. The unprecedented increase in connectivity between different functional layers (*e.g.*, sensing, storing, processing)<sup>2</sup> is ideally suited to be exploited in data-intensive technologies like Internet-of-Things (IoT). For all the implementations mentioned above and others, the preservation of the vertical direction during processing of densely-packed arrays of 1D nano-structures is fundamental. However, different fabrication steps may deflect such a desired direction. The exposure to an electron beam, for instance, during characterization through scanning electron microscope, has been reported to bend semiconductor NWs with subsequent formation of NW bundles.<sup>3–6</sup> Procedures involving wet etching or cleaning also result in reshaping of the vertical arrangement of NWs<sup>7–9</sup> and CNTs. In all these cases, a drying step occurs where capillary menisci between adjacent nano-pillars induce lateral forces that may bring these in contact<sup>10,11</sup> and eventually assemble together.

Although self-assembly could have a detrimental impact, its purposeful exploitation can also drive the fabrication of aggressively scaled devices. More specifically, self-assembly stands for a large family of bio-inspired strategies, where components organize autonomously into desired patterns or structures with no human intervention.<sup>12–15</sup> The concept originated from the chemistry of molecular assemblies mediated by intermolecular bonds to build up supramolecular systems,<sup>16</sup> and it has subsequently broadened its meaning to indicate programmed aggregation of non-molecular parts whose size ranges from nano to macroscopic scale. Indeed, the current extreme shrinkage of the operative regime in various technological fields can be severely hindered by material and engineering limitations at such scales, especially when the fabrication of non-planar 3D structures is involved. Thus, new paradigms such as self-assembly may become a game-changer to enable 3D small scale manufacturing.<sup>12</sup>

A key aspect of both avoiding undesirable sticking effects and, on the contrary, harnessing them to build smart architectures and/or devices is the ability to engineer and control such effects. In particular, the elasto-capillary driven self-assembly of arrays of 1D nano-structures is a multi-faceted phenomenon where many different factors play a role: (1) the mechanical properties of the involved nano-structures, (2) the geometry of the array (inter-distance, aspect-ratio), (3) the evaporation rate and the surface tension of the fluid in which the nano-scaled beams are immersed. Although a wealth of literature exists concerning the mechanism of clustering in arrays of 1D nano-structures, usually its analysis is mainly based on the elasticity theory alone,<sup>10,11,17,18</sup> whereas the material properties are commonly taken from experimental literature. A multi-scale investigation able to integrate a rigorous calculation of mechanical properties into the established theoretical modeling of the phenomenon is still as yet missing.

Microelectronics Department, LIRMM, University of Montpellier, CNRS, 161 Rue Ada, Montpellier, France. E-mail: stefania.carapezzi@gmail.com; aida.todri@lirmm.fr

† Electronic supplementary information (ESI) available. See <https://doi.org/10.1039/d2na00295g>

‡ These authors contributed equally to this work.

This is the more important when dealing with clustering of 1D nano-structures, where the techniques for experimental characterization of mechanical properties are still under development and the measured values are often prone to rather large experimental errors. Thus, in this work, we use density functional theory (DFT) to predict fully *ab initio* the relevant mechanical properties of CNTs, such as Young's modulus, Poisson's ratio, and surface energy. We also investigate the impact of both diameter and chirality on such properties. Then, we avail of such physics-based parameters to carry out a theoretical analysis of the self-organization of CNT arrays induced by capillary forces.

CNTs are on the forefront among 1D nano-structures for ground-breaking nano-technological implementations.<sup>19–21</sup> CNT field-effect transistors promise to improve the energy efficiency of current communication systems, due to their high charge carrier mobility, linearity, current carrying capability and low noise.<sup>22</sup> The good thermal conductivity of CNTs is beneficial for the fabrication of low power consumption sensors.<sup>23–25</sup> Overall, their exceptional electronic, optical, thermal, and mechanical properties make CNTs an ideal choice for flexible and printed electronics.<sup>26</sup> In particular, CNTs have demonstrated excellent suitability as active layers in energy autonomous wearable sensors<sup>27–30</sup> for control of health risk factors and achievement of lifelong health monitoring. A way to improve the signal-to-noise ratio is to fabricate devices based on CNT ensembles. In such a case, the alignment of CNTs affects their performance. Additionally, novel applications can be achieved by engineering the 3D organization of CNTs structures obtained using capillary aggregation methods.

Our paper is organized as follows: the first section is dedicated to predicting the relevant mechanical parameters of CNTs *via* DFT simulations; here, we describe the details of our simulations and present the results. Then, in the following section, the mechanism of capillary-force-driven self-assembly of CNTs is expressed through a simple model. The previously computed DFT parameters (Young's modulus, Poisson's ratio, and surface energy) are fed into such a model. Finally, inferences regarding the occurrence of self-assembly are consequently derived.

## 2 *Ab initio* simulations on Young's modulus, Poisson's ratio, and surface energy of CNTs

### 2.1 Simulation details

In this work, we considered CNTs with different radii (from  $\sim 2.5$  Å up to  $\sim 10$  Å) and with different chiralities, *i.e.*, armchair and zigzag. Atomistic simulations were carried out in the framework of density functional theory (DFT) with QuantumATK atomic-scale modelling software.<sup>31,32</sup> We performed the calculations in vacuum using the Perdew–Burke–Ernzerhof (PBE) exchange–correlation functional,<sup>33</sup> and to model core electrons, we used norm-conserving pseudopotentials from the PseudoDojo library.<sup>34</sup> The LCAO approach was used throughout this work with a density-mesh cut-off of 150 Ry and the

QuantumATK-optimized Medium basis set. We used a *k*-point mesh defined by a  $1 \times 1 \times 11$  Monkhorst–Pack (MP) grid.<sup>35</sup> When performing geometry optimizations, we enforced a  $0.01 \text{ eV Å}^{-1}$  threshold for the residual atomic forces. Finally, to avoid any spurious interaction between periodic images, we included a vacuum padding of 10 Å along the *x* and *y* directions. See Fig. 1 for a representative example of one of our CNT models.

To simulate strain ( $\epsilon$ ) along the tube (that is, along the *z* direction), we stretched the simulation cell and the C atoms contained therein at steps of 1%, and between  $-5\%$  (compressive strain) and  $+5\%$  (tensile strain). Then, at each step, we carried out a full geometry optimization in order to relax the position of the C atoms in the presence of strain, and we computed the total energy of the system. The mechanical properties of CNTs used throughout this study were extracted fully *ab initio*, *i.e.*, without the use of any empirical parameter. The Young's modulus ( $Y$ ) can be computed *via* the following equation:

$$Y = \frac{1}{V_0} \left( \frac{\partial^2 E}{\partial \epsilon^2} \right) \bigg|_{\epsilon=0}, \quad (1)$$

which is the second order derivative of the energy/strain curve at  $\epsilon = 0$ .<sup>36</sup> In this equation,  $E$  is the total energy of the system as computed by DFT and  $V_0$  is the equilibrium volume defined as:

$$V_0 = 2\pi r_0 l_0 \delta, \quad (2)$$

where  $r_0$  and  $l_0$  are the radius and the length of the CNT, respectively, at  $\epsilon = 0$ .  $\delta$  is the thickness of the tube. As per convention,<sup>37</sup> we chose  $\delta = 3.35$  Å, which is the interlayer

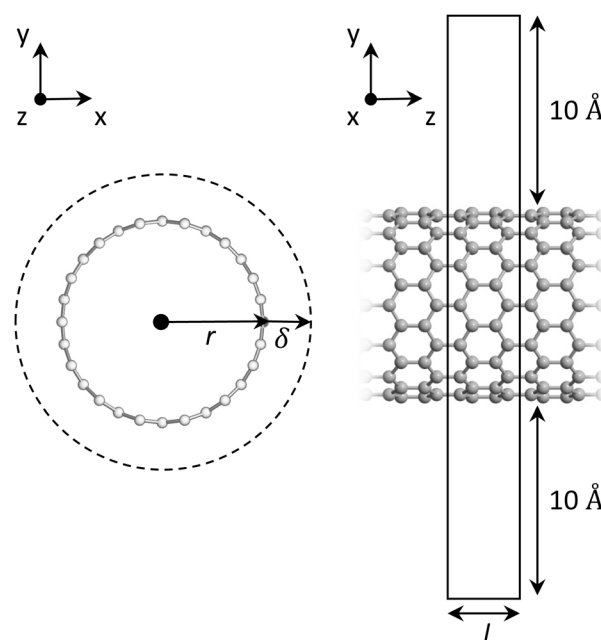


Fig. 1 Optimized structure of a representative zigzag (14,0)CNT, front and side views. On the left,  $r$  and  $\delta$  are the radius and the thickness of the nanotube, respectively. On the right,  $l$  is the tube length. The unit cell is also shown, highlighting the vacuum padding around the tube.



distance in graphite as obtained by our DFT simulations. We computed the Poisson's ratio ( $\nu$ ) as:

$$\nu = -\frac{1}{\varepsilon} \left( \frac{r_\varepsilon - r_0}{r_0} \right), \quad (3)$$

where  $r_\varepsilon$  is the radius of the CNT at each percentage of strain.<sup>36</sup> Finally, we extracted the surface energy per unit area ( $\gamma$ ) by adapting the equation discussed by Medasani *et al.*:<sup>38,39</sup>

$$\gamma = \frac{nE_{\text{graphene}}^{\text{coh}} - E_{\text{CNT}}^{\text{b}}}{2\pi r_0 l_0}, \quad (4)$$

where  $E_{\text{graphene}}^{\text{coh}}$  is the cohesive energy of graphene,  $n$  is the number of atoms,  $E_{\text{CNT}}^{\text{b}}$  is the total binding energy of the CNT, and the denominator is the surface area of the CNT.

## 2.2 Results and discussion

We computed the mechanical properties of CNTs as a function of both radius and chirality (armchair and zigzag). The results are shown in both Table 1 and Fig. 2.

First, our simulations predict  $Y$  to increase with respect to the tube diameter and to converge to  $\sim 1.02$  TPa when  $d \geq 12$ – $13$  Å. However, we note that even at smaller diameters,  $Y$  is still reasonably close to 1 TPa. Our computed value of  $Y$  compares well with both experimental and theoretical data, although it is worth pointing out that there exists a rather large variability reported in the literature. Regarding experimental data, such variability is due to the employed measurement technique and the quality of the CNT samples, as it is known that defects can have a non-negligible effect. On the other hand, in theoretical models, the variability is primarily due to the CNT thickness (as previously mentioned, here we use  $\delta = 3.35$  Å). Overall, typical values of  $Y$  for single-wall CNTs oscillate around 1 TPa.<sup>40,41</sup> Chirality does not seem to have a major effect on  $Y$ , although the increasing trend with respect to the tube diameter is somewhat less smooth in armchair CNTs. Overall, our results suggest the stiffness of CNTs to slightly increase with respect to their diameter.

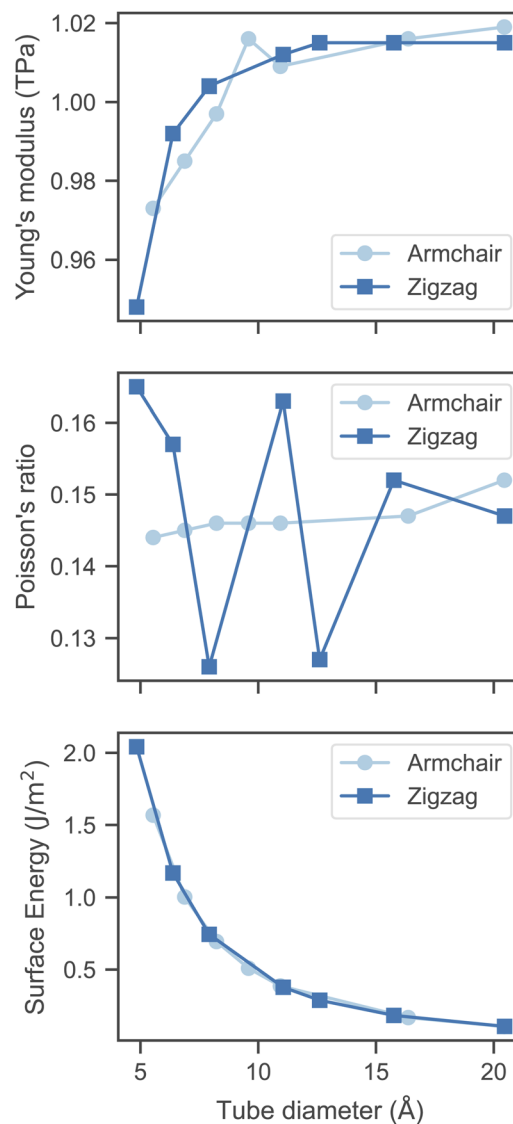


Fig. 2 Mechanical properties of the CNT structures considered in this work (armchair and zigzag) as a function of the tube diameter, as obtained *via* DFT simulations.

**Table 1** Computed mechanical parameters of the CNT structures considered in this work by DFT.  $d$  is the tube diameter,  $Y$  the Young's modulus,  $\nu$  is the Poisson's ratio, and  $\gamma$  is the surface energy

Structure	$d$ (Å)	$Y$ (TPa)	$\nu$	$\gamma$ (J m <sup>-2</sup> )
(6,0)	4.84	0.948	0.165	2.042
(8,0)	6.38	0.992	0.157	1.167
(10,0)	7.92	1.004	0.126	0.744
(14,0)	11.06	1.012	0.163	0.377
(16,0)	12.61	1.015	0.127	0.287
(20,0)	15.76	1.015	0.152	0.182
(26,0)	20.46	1.015	0.147	0.106
(4,4)	5.54	0.973	0.144	1.568
(5,5)	6.88	0.985	0.145	1.003
(6,6)	8.23	0.997	0.146	0.694
(7,7)	9.59	1.016	0.146	0.509
(8,8)	10.94	1.009	0.146	0.386
(12,12)	16.37	1.016	0.147	0.167
(15,15)	20.45	1.019	0.152	0.105

The Poisson's ratio ( $\nu$ ) is the second parameter that we have computed. Interestingly, we observed that the chirality of the tube appears to have some effect on this quantity. As can be seen from Fig. 2, armchair CNTs possess roughly the same value of  $\nu$  (0.14–0.15) regardless of the tube diameter, whereas, in zigzag CNTs, such a value oscillates between 0.125 and 0.165. However, for  $d > 15$  Å, we observe that for both zigzag and armchair CNTs, the Poisson's ratio converges to  $\sim 0.15$ . Once again, we point out that our results are consistent with published experimental data, in which  $\nu$  was found to range between 0.149 and 0.340.<sup>42</sup>

Finally, we computed the surface energy ( $\gamma$ ) of CNTs, which, to the best of our knowledge, has never been previously computed *via* DFT simulations for this class of materials. As per its definition, surface energy is the energy required to create one unit of surface area. In this work, we computed  $\gamma$  by considering



graphene as the reference structure from which CNTs are derived (see Simulation details). Therefore,  $\gamma$  can be seen as a measure of the excess energy induced by the curvature of the C–C bonds in the structure of CNTs. Indeed, our results predict a decrease of  $\gamma$  with respect to the diameter of the tubes, regardless of the chirality. For  $d \approx 5 \text{ \AA}$ , we found a rather high value of  $\sim 2.0 \text{ J m}^{-2}$ , which reduces to  $\sim 0.1 \text{ J m}^{-2}$  for diameters larger than 2 nm. It is worth noting that there exists a large variability in the experimental value of the surface energy of CNTs, although on average  $\gamma = 0.26 \text{ J m}^{-2}$ , larger and smaller values have also been reported.<sup>43</sup> Nevertheless, our results appear to be within the accepted range of values. The decreasing trend of  $\gamma$  with respect to the CNTs diameters can be easily explained by the amount of strain induced by the curvature to the  $\text{sp}^2$  C–C bonds, which should normally be planar. Smaller diameters would lead to a larger distortion of the planarity of C–C bonds and, thus, increase the surface energy.

### 3 Elastocapillary self-assembly of carbon nanotube arrays

The self-assembly of CNTs mediated by elasto-capillary forces is due to the combination of two different mechanisms (Fig. 3). First, (A) the process of bending the CNTs to favor the contact between their surfaces (Fig. 3a). To this aim, the CNTs are immersed in a liquid, whose evaporation induces their bending, provided that the capillary forces acting during the drying step defeat the elastic forces that would reset them back to the original vertical alignment. Second, (B) the process of CNT bundling (Fig. 3b). This occurs if the adhesion forces acting between the touching surfaces of CNTs are larger than the elastic forces that would tend to set them apart. In the following, we model the elasto-capillary self-assembly of CNTs by considering the simplest possible bundled unit composed of two CNTs. For simplicity's sake, we assume that both CNTs have the same geometry and physical properties. It has been demonstrated<sup>10</sup> that the lateral forces resulting from capillary menisci interaction are those responsible for the clustering of micro-sized pillars after liquid evaporation. The capillary force between two cylindrical structures ( $F_C$ ) when they are partially

immersed in a liquid can be estimated through Kralchevsky's asymptotic solution<sup>44</sup> as:

$$F_C = \frac{\pi \gamma_{\text{liq}} R^2 \cos^2(\theta)}{\sqrt{x^2 - R^2}}, \quad (5)$$

where  $\gamma_{\text{liq}}$  is the liquid surface tension,  $\theta$  is the equilibrium contact angle between the cylindrical surface and the liquid,  $R$  is the cylinder's radius, and  $2x$  is the inter-distance between axes of two structures (Fig. 3a). Regarding the elastic force that would restore each pillar to the original straight position, this can be estimated from the Euler–Bernoulli elementary beam theory<sup>44</sup> as the elastic force deflecting a beam clamped at one end, of height  $h$ , such that the free end is deflected of  $w$ :

$$F_{\text{el}} = \frac{3EIw}{h^3}, \quad (6)$$

where  $E$  is the pillar's Young modulus and  $I$  is its area moment of inertia.

We determine  $F_C$  from eqn (5) for all the CNTs considered, whose radii  $R_{\text{CNT}}$  are listed in Table 1. We use values of  $w$  ranging from 1 to 100 nm. We consider water as the liquid catalyzing the coalescence of CNTs, as frequently reported in literature. Consequently, we use  $\theta$  equal to  $86^\circ$ <sup>45</sup> and  $\gamma_{\text{H}_2\text{O}} = 72 \text{ mN m}^{-1}$ . Fig. 4 shows the behavior of calculated  $F_C$  vs.  $w$  for CNT armchair (4,4) (Fig. 4a; green dotted line) and for CNT armchair (15,15) (Fig. 4b; green dashed line).  $w$  is  $x - R_{\text{ext}}$ , for  $R_{\text{ext}} = R_{\text{CNT}} + \delta$  being the external radius of CNT, where  $\delta = 0.335 \text{ nm}$  is CNT thickness. The magnitude of  $F_C$  decreases from 8.36 to 0.124 pN for CNT armchair (4,4), and from 31.8 to 0.6 pN for CNT armchair (15,15), within the probed interval of  $w$ . We determine  $F_{\text{el}}$  from eqn (6) for all the CNTs, where the corresponding Young's moduli are reported in Table 1. We calculate  $I_{\text{CNT}}$  as the area moment of inertia of a tube,  $\pi \times (R_{\text{ext}}^4 - R_{\text{int}}^4)/4$ , with  $R_{\text{int}} = R_{\text{CNT}}$ . Fig. 4 shows calculated  $F_{\text{el}}$  vs.  $w$  for different values of CNT height  $h_{\text{CNT}}$  (from 24 nm to 10  $\mu\text{m}$ ). By comparing  $F_C$  and  $F_{\text{el}}$  values, we can assess when capillary forces are stronger than elastic forces. In case of CNTs armchair (4,4) (Fig. 4a) and  $h_{\text{CNT}}$  equal or smaller than 24 nm,  $F_{\text{el}}$  is larger than  $F_C$  for all probed  $w$  values. This means that CNTs are not brought into contact by capillary forces. For  $h_{\text{CNT}}$  larger than 24 nm and smaller than 500 nm, it exists a threshold value of  $w$

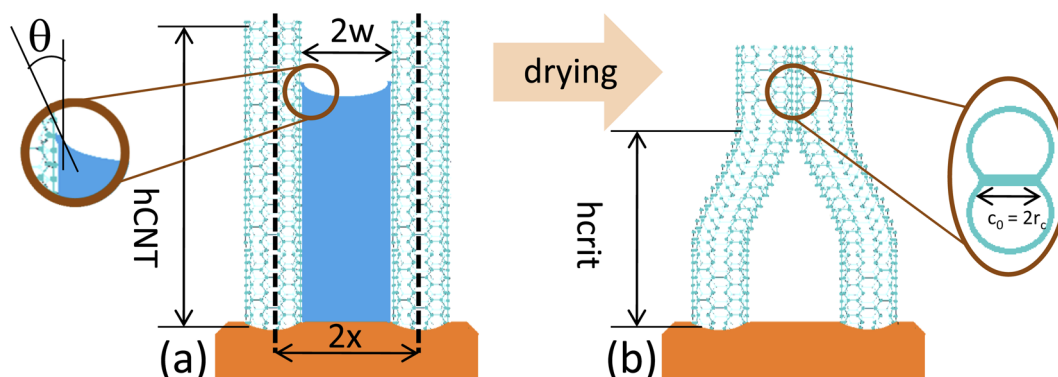


Fig. 3 (a) Capillary meniscus between two CNTs, the distance between whose axes being  $2x$ . In the inset is magnified the interface vapor/liquid close to the CNT surface, where  $\theta$  is the contact angle. (b) Lateral collapsing between two adjacent CNTs.





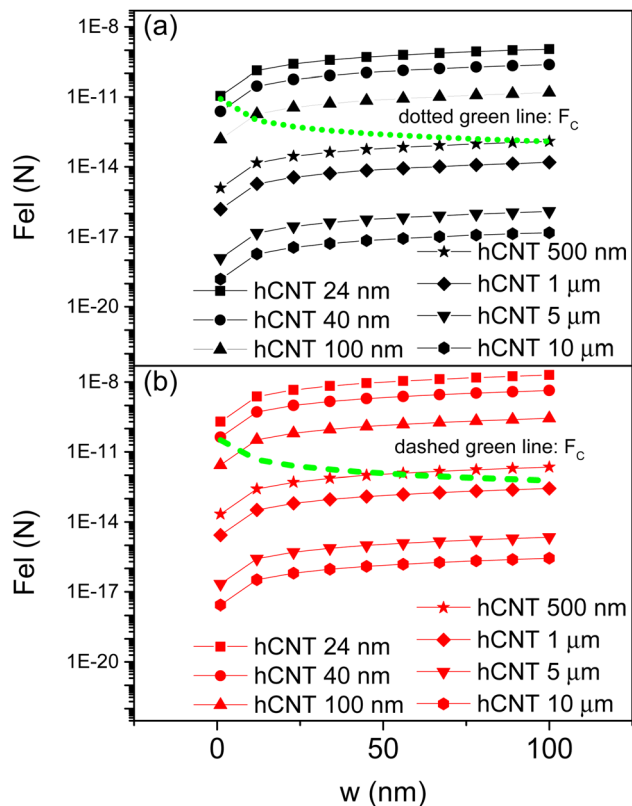


Fig. 4 Behavior with  $w$  of  $F_c$  from eqn (5) (green lines) and of  $F_{el}$  from eqn (6) (symbols), for (a) armchair (4,4) CNT and (b) armchair (15,15) CNT.

above which  $F_c$  becomes smaller than  $F_{el}$ . Finally, for CNTs taller than 500 nm capillary forces are stronger than elastic forces for all considered  $w$  values. The same analysis is qualitatively applicable to other armchair CNTs (results of armchair (15,15) are shown in Fig. 4b) and to zigzag CNTs (Fig. ESI† of the ESI†).

Once the conditions for capillary-forces-driven contact of CNTs are established, we also need to assess when the adhesion forces between their surfaces are such to keep them self-assembled. In this respect, we avail of a theoretical model obtained studying the contact behavior of fibrillar interfaces.<sup>17,46</sup> Such model has been validated against experimental results for a variety of material interfaces, like arrays of poly(dimethylsiloxane) fibrils<sup>17</sup> and gallium arsenide nanowires.<sup>3</sup> It is important to note that fibrillar interfaces are intensively investigated to mimic the efficiency of adhesiveness of some natural contact surfaces, for example, the ones of lizards. These interfaces are simply modeled as arrays of pillars (called fibrils) extruding from a substrate. The surfaces of two next-neighbor pillars may stick together, once they are brought to touch each other, due to the influence of van der Waals forces. In this case, the elastic strain energy  $U_b$  of the system is concentrated into the noncontact region of length  $H$ , which is deformed by the bending (Fig. 3b). The increase of  $H$  by a small amount  $dH$  implies a consequent strain energy variation of  $(9EIw^2) \times dH/H^4$ . If the system is in equilibrium, then it must be equal to the

work  $dW$  necessary to shrink the contact area. For cylindrical-shaped pillars, the contact radius  $r_c$  is smaller than cylinder's radius. Also, some elastic deformation occurs near the contact region<sup>17</sup> (inset of Fig. 3b). JKR theory<sup>18</sup> allows to calculate the equilibrium contact width  $c_0 = 2r_c$ , and thus the energy to separate the two surfaces is determined to be  $(2\gamma_{\text{sup}}c_0 - U_c) \times dH$ , where  $U_c$  is the elastic energy stored into the deformed region of contact<sup>17</sup> and  $\gamma_{\text{sup}}$  is the surface energy.  $c_0$  and  $U_c$  are<sup>17</sup> as follows:

$$\frac{c_0}{2} = r_c = \left( \frac{32R^2\gamma_{\text{sup}}}{\pi E^*} \right)^{1/3} \quad (7)$$

$$U_c = \frac{\pi E^* R^2}{32} \left( \frac{r_c}{R} \right)^4 \quad (8)$$

respectively, for  $E^* = E/(1 - \nu^2)$ ,  $\nu$  being the Poisson's ratio. The consideration of energy balancing yields a criterion of critical height for lateral collapse that reads as:

$$h_{\text{crit}} = \left[ \frac{9EIw^2}{2\gamma_{\text{sup}}c_0 - U_c} \right]^{1/4} \quad (9)$$

where CNTs bundle if their height is larger than  $h_{\text{crit}}$ . It is noteworthy to observe that  $h_{\text{crit}}$  increases monotonically with  $w$ . Then, a stable bundling is obtained with taller and taller CNTs for arrays with larger and larger inter-distance between CNTs. Fig. 5 shows  $h_{\text{crit}}$  as determined from eqn (9) for all armchair CNTs considered, plotted against  $w$ . It can be seen that  $h_{\text{crit}}$  ranges from 5.7 to 57 nm for CNT armchair (4,4), up to from 25 to 255 nm for CNT armchair (15,15). The ranges in which CNT self-assembly is predicted to occur can be assessed by comparison between Fig. 4 and 5. Thus, in the case of CNT armchair (4,4), for  $h_{\text{CNT}}$  below  $h_A = 24$  nm, capillary-force-driven self-assembly does not occur, given that capillary forces are not

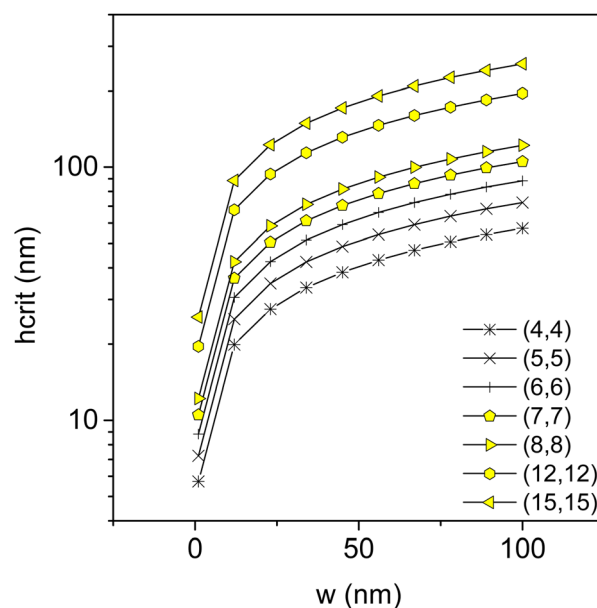


Fig. 5 Critical height  $h_{\text{crit}}$  of lateral collapse by eqn (9), from armchair (4,4) CNT to armchair (15,15) CNT.

able to overcome elastic forces. For  $h_{\text{CNT}}$  above  $h_A$  and below  $h_B$ ,  $= 500$  nm, capillary forces are able to bring CNTs into contact only for  $w$  below a threshold  $w_{\text{th}}$ , which depends on  $h_{\text{CNT}}$ . In this latter case,  $h_{\text{CNT}}$  results to be above  $h_{\text{crit}}$ , thus, the CNTs brought into contact form a bundle. For  $h_{\text{CNT}}$  above  $h_B$  the capillary-force-driven bundling of CNTs occurs for every value of  $w$ , and the adhesion forces are always able to keep the CNT bundle stable. The above discussion can be repeated for the other armchair (and zigzag) CNTs, where  $R_{\text{CNT}}$  modulates the value of  $h_A$  and  $h_B$ : for example,  $h_A = 40$  nm for CNT armchair (15,15).

## 4 Conclusions

In this work, we show a rigorous approach integrating *ab initio* calculation of CNT mechanical properties into theoretical modeling of capillary-force-driven self-assembly of CNTs, with the purpose of providing guidelines to exploit this phenomenon. We use DFT to predict Young's modulus, Poisson's ratio, and surface energy of CNTs. We investigate the impact of both diameter and chirality on such properties. We find that (1) Young's modulus increases and (2) surface energy decreases with respect to CNT diameter. To the best of our knowledge, we are the first to report DFT calculations of CNT surface energy. Then, we feed the relevant DFT parameters into a model for capillary-force-driven self-assembly of CNTs. We find that there exists height values  $h_A$  and  $h_B$  such that (A) for  $h_{\text{CNT}} < h_A$  capillary-force-driven self-assembly does not occur, (B) for  $h_A < h_{\text{CNT}} < h_B$  capillary forces bend CNTs into contact only for  $w$  below threshold values  $w_{\text{th}}$ , and (C) for  $h_{\text{CNT}} > h_B$  the capillary-force-driven bundling of CNTs occurs for every value of  $w$ . Finally, we find that such values  $h_A$ ,  $h_B$  depend on  $R_{\text{CNT}}$ .

## Author contributions

SC and GB conceived the study concept and designed the simulations. GB performed DFT simulations and analyzed the data. SC performed elastic theory calculations and evaluated and interpreted the data. SC and GB drafted the manuscript. ATS critically revised the manuscript. ATS supervised the study. The manuscript has been read and approved by all authors.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

This project has received funding from the European Union's Horizon 2020 Research and Innovation Programme, EU H2020 SmartVista (<https://www.smartvista.eu>), grant agreement no. 825114.

## References

- W. Chen and P. R. i Cabarrocas, *Nanotechnology*, 2019, **30**, 194002.
- M. M. Shulaker, G. Hills, R. S. Park, R. T. Howe, K. Saraswat, H.-S. P. Wong and S. Mitra, *Nature*, 2017, **547**, 74–78.
- S. Carapezzi, G. Priante, V. Grillo, L. Montès, S. Rubini and A. Cavallini, *ACS Nano*, 2014, **8**, 8932–8941.
- N. Senthilnathan and T. P. Radhakrishnan, *Chem. Mater.*, 2020, **32**, 8567–8575.
- L. A. Bitzer, C. Speich, D. Schäfer, D. Erni, W. Prost, F. J. Tegude, N. Benson and R. Schmechel, *J. Appl. Phys.*, 2016, **119**, 145101.
- V. M. Kaganer, S. Fernández-Garrido, P. Dogan, K. K. Sabelfeld and O. Brandt, *Nano Lett.*, 2016, **16**, 3717–3725.
- S. Carapezzi and A. Cavallini, *Beilstein J. Nanotechnol.*, 2019, **10**, 2094–2102.
- T. Ghosh, E.-C. Fritz, D. Balakrishnan, Z. Zhang, N. Vrancken, U. Anand, H. Zhang, N. D. Loh, X. Xu, F. Holsteyns, C. A. Nijhuis and U. Mirsaidov, *ACS Appl. Mater. Interfaces*, 2022, **14**, 5537–5544.
- N. Vrancken, T. Ghosh, U. Anand, Z. Aabdin, S. W. Chee, Z. Baraissov, H. Terry, S. D. Gendt, Z. Tao, X. Xu, F. Holsteyns and U. Mirsaidov, *J. Phys. Chem. Lett.*, 2020, **11**, 2751–2758.
- D. Chandra and S. Yang, *Langmuir*, 2009, **25**, 10430–10434.
- P. Kralchevsky, V. Paunov, I. Ivanov and K. Nagayama, *J. Colloid Interface Sci.*, 1992, **151**, 79–94.
- K. S. Kwok, Q. Huang, M. Mastrangeli and D. H. Gracias, *Adv. Mater. Interfaces*, 2020, **7**, 1901677.
- M. De Volder and A. J. Hart, *Angew. Chem., Int. Ed.*, 2013, **52**, 2412–2425.
- K. J. M. Bishop, C. E. Wilmer, S. Soh and B. A. Grzybowski, *Small*, 2009, **5**, 1600–1630.
- G. M. Whitesides and B. Grzybowski, *Science*, 2002, **295**, 2418–2421.
- J.-M. Lehn, *Science*, 1993, **260**, 1762–1763.
- N. J. Glassmaker, A. Jagota, C.-Y. Hui and J. Kim, *J. R. Soc. Interface*, 2004, **1**, 23–33.
- C. Y. Hui, Y. Y. Lin, J. M. Baney and A. Jagota, *J. Adhes. Sci. Technol.*, 2000, **14**, 1297–1319.
- Y. Che, H. Chen, H. Gui, J. Liu, B. Liu and C. Zhou, *Semicond. Sci. Technol.*, 2014, **29**, 073001.
- M. F. L. D. Volder, S. H. Tawfick, R. H. Baughman and A. J. Hart, *Science*, 2013, **339**, 535–539.
- G. Boschetto, S. Carapezzi and A. Todri-Sanial, *IEEE Open J. Nanotechnol.*, 2021, **2**, 120–128.
- M. Hartmann, J. Tittmann-Otto, S. Böttger, G. Heldt, M. Claus, S. E. Schulz, M. Schröter and S. Hermann, *ACS Appl. Mater. Interfaces*, 2020, **12**, 27461–27466.
- K. Chikkadi, M. Muoth, V. Maiwald, C. Roman and C. Hierold, *Appl. Phys. Lett.*, 2013, **103**, 223109.
- K. Chikkadi, M. Muoth, C. Roman, M. Haluska and C. Hierold, *Beilstein J. Nanotechnol.*, 2014, **5**, 2179–2191.
- S. Carapezzi, S. Reggiani, E. Gnani and A. Gnudi, *IEEE Trans. Electron Devices*, 2020, **67**, 4682–4686.
- A. Kamysny and S. Magdassi, *Chem. Soc. Rev.*, 2019, **48**, 1712–1740.
- A. S. Dahiya, J. Thireau, J. Boudaden, S. Lal, U. Gulzar, Y. Zhang, T. Gil, N. Azemard, P. Ramm, T. Kiessling,



- C. O'Murchu, F. Sebelius, J. Tilly, C. Glynn, S. Geary, C. O'Dwyer, K. M. Razeed, A. Lacampagne, B. Charlot and A. Todri-Sanial, *J. Electrochem. Soc.*, 2019, **167**, 037516.
- 28 A. S. Dahiya, T. Gil, J. Thireau, N. Azemard, A. Lacampagne, B. Charlot and A. Todri-Sanial, *Adv. Electron. Mater.*, 2020, **6**, 2000547.
- 29 R. R. Pandey, J. Liang, D. Cakiroglu, B. Charlot and A. Todri-Sanial, *Electrochemical Glucose Sensor Using Single-Wall Carbon Nanotube Field Effect Transistor*, 2020, <https://arxiv.org/abs/2006.12973>.
- 30 G. Boschetto, T. Xu, M. Yehya, J. Thireau, A. Lacampagne, B. Charlot, T. Gil and A. Todri-Sanial, *2021 IEEE International Conference on Flexible and Printable Sensors and Systems (FLEPS)*, 2021, pp. 1–4.
- 31 S. Smidstrup, T. Markussen, P. Vancraeyveld, J. Wellendorff, J. Schneider, T. Gunst, B. Verstichel, D. Stradi, P. A. Khomyakov, U. G. Vej-Hansen, M.-E. Lee, S. T. Chill, F. Rasmussen, G. Penazzi, F. Corsetti, A. Ojanperä, K. Jensen, M. L. N. Palsgaard, U. Martinez, A. Blom, M. Brandbyge and K. Stokbro, *J. Phys.: Condens. Matter*, 2020, **32**, 015901.
- 32 *QuantumATK Version S-2021.06*, Synopsys QuantumATK, <https://www.synopsys.com/silicon/quantumatk.html>, last accessed, April 25, 2022.
- 33 J. P. Perdew, K. Burke and M. Ernzerhof, *Phys. Rev. Lett.*, 1996, **77**, 3865–3868.
- 34 M. J. van Setten, M. Giantomassi, E. Bousquet, M. J. Verstraete, D. R. Hamann, X. Gonze and G.-M. Rignanese, *Comput. Phys. Commun.*, 2018, **226**, 39–54.
- 35 H. J. Monkhorst and J. D. Pack, *Phys. Rev. B: Solid State*, 1976, **13**, 5188–5192.
- 36 E. Hernández, C. Goze, P. Bernier and A. Rubio, *Phys. Rev. Lett.*, 1998, **80**, 4502.
- 37 J. P. Lu, *Phys. Rev. Lett.*, 1997, **79**, 1297.
- 38 B. Medasani, Y. H. Park and I. Vasiliev, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2007, **75**, 235436.
- 39 B. Medasani and I. Vasiliev, *Surf. Sci.*, 2009, **603**, 2042–2046.
- 40 A. Krishnan, E. Dujardin, T. W. Ebbesen, P. N. Yianilos and M. M. J. Treacy, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1998, **58**, 14013.
- 41 R. S. Ruoff, D. Qian and W. K. Liu, *C. R. Phys.*, 2003, **4**, 993–1008.
- 42 Z.-C. Tu and Z.-C. Ou-Yang, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2002, **65**, 233407.
- 43 M. R. Roenbeck, X. Wei, A. M. Beese, M. Naraghi, A. Furmanchuk, J. T. Paci, G. C. Schatz and H. D. Espinosa, *ACS Nano*, 2014, **4**, 124–138.
- 44 R. C. Hibbeler, *Mechanics of Materials*, Prentice-Hall, Englewood Cliffs, NJ, 3rd edn, 1997.
- 45 H. Liu, J. Zhai and L. Jiang, *Soft Matter*, 2006, **2**, 811–821.
- 46 A. Jagota and C.-Y. Hui, *Mater. Sci. Eng., R*, 2011, **72**, 253–292.

