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Querying Inconsistent Prioritized Data with ORBITS:
Algorithms, Implementation, and Experiments

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Abstract
We investigate practical algorithms for inconsistency-tolerant query answering over prioritized knowledge bases, which consist of a logical theory, a set of facts, and a priority relation between conflicting facts. We consider three well-known semantics (AR, IAR and brave) based upon two notions of optimal repairs (Pareto and completion). Deciding whether a query answer holds under these semantics is (co)NP-complete in data complexity for a large class of logical theories, and SAT-based procedures have been devised for repair-based semantics when there is no priority relation, or the relation has a special structure. The present paper introduces the first SAT encodings for Pareto- and completion-optimal repairs w.r.t. general priority relations and proposes several ways of employing existing and new encodings to compute answers under (optimal) repair-based semantics, by exploiting different reasoning modes of SAT solvers. The comprehensive experimental evaluation of our implementation compares both (i) the impact of adopting semantics based on different kinds of repairs, and (ii) the relative performances of alternative procedures for the same semantics.

1 Introduction
The question of how to handle data that is inconsistent w.r.t. expressed constraints, be they given by database dependencies or ontologies, has great practical relevance. Data cleaning addresses this problem by modifying datasets so that they satisfy the constraints, often using heuristics to decide how to resolve contradictions, which may result in wrong facts being kept, or true facts removed (as discussed e.g. in (Fan 2015)). An alternative, more principled, approach is to adopt inconsistency-tolerant semantics in order to extract meaningful information from the contradictory data.

In the database setting, such an approach goes by the name of consistent query answering (CQA) and has been extensively studied since the seminal work of Arenas, Bertossi, and Chomicki (1999), see e.g. the recent survey by Wijsen (2019). A central notion is that of a (subset) repair, defined as a maximal subset of the dataset that satisfies the constraints. Intuitively, repairs represent all different ways of minimally modifying the data to satisfy the constraints. As we do not know which repair corresponds to the true part of the data, the CQA semantics stipulates that a tuple is a query answer if it is an answer w.r.t. every repair (in line with how skeptical inference is defined in many KR settings).

Inconsistency-tolerant semantics have also drawn considerable interest in the setting of ontology-mediated query answering (OMQA) (Poggi et al. 2008; Bienvenu and Ortiz 2015; Xiao et al. 2018), where the ontology not only specifies constraints on the data but also captures other forms of domain knowledge, which can be exploited at query time. In addition to the AR semantics (the OMQA analog of the CQA semantics), several other inconsistency-tolerant semantics have been proposed (see (Bienvenu and Bourgaux 2016; Bienvenu 2020) for surveys and references), among which: the brave semantics (Bienvenu and Rosati 2013), which only requires a tuple to be an answer w.r.t. some repair, provides a natural notion of possible answer, and the IAR semantics (Lembo et al. 2010), which answers queries over the intersection of the repairs, identifies the most reliable answers.

The basic notion of repair can be refined by exploiting preference information. A prominent approach, introduced by Staworko, Chomicki, and Marcinkowski (2012) in the database setting and recently explored in the OMQA setting (Bienvenu and Bourgaux 2020), assumes that preferences are given by a binary priority relation between conflicting facts. Three notions of ‘best’ repairs w.r.t. a priority relation were proposed, namely, Pareto-optimal, globally-optimal, and completion-optimal repairs, and can be used in place of subset repairs in any repair-based semantics.

The complexity of answering queries under (optimal) repair-based semantics has been extensively studied in the database and OMQA settings, refer to (Wijsen 2019; Bienvenu and Bourgaux 2016) for an overview and references. We can briefly summarize these (many!) complexity results as follows: query answering under the AR (or CQA) semantics is coNP-hard in data complexity even in the simplest of settings (e.g. key constraints, class disjointness), and adopting optimal repairs in place of subset repairs leads to (co)NP-hardness for the brave and IAR semantics as well. Membership in (co)NP holds for AR, brave, and IAR semantics w.r.t. subset, Pareto-optimal, and completion-optimal repairs in the most commonly considered settings i.e. for database constraints given by primary keys or more generally, functional dependencies (FDs), and for ontologies formulated in data-tractable description logics such as those of the DL-Lite family (Calvanese et al. 2007).

The preceding (co)NP complexity results naturally suggest the interest of employing SAT solvers. Two recent sys-
tems, CQAPri and CAVSAT, have begun to explore such an approach. CQAPri (Bienvenu, Bourgaux, and Goasdoué 2014; 2019) uses tractable approximations together with calls to SAT solvers to answer queries over inconsistent DL-Lite knowledge bases, under the AR, brave, and IAR semantics, w.r.t. subset repairs as well as optimal repairs for the restricted class of score-structured priority relations. CAVSAT (Dixit and Kolaitis 2019) targets relational databases equipped with denial constraints (which include FDs as a special case) and computes query answers under the AR semantics w.r.t. subset repairs. While geared to different forms of constraints, the two systems solve essentially the same problem, yet they employ SAT solvers in different ways. CQAPri makes a single SAT call for each candidate query answer, whereas CAVSAT treats all candidate answers at the same time via calls to a weighted MaxSAT solver.

This paper presents a comprehensive study of the use of SAT-based approaches for inconsistency-tolerant query answering, which abstracts from the particular setting and provides a solid foundation for the future development of such systems. Our contributions can be summarized as follows. In Section 3, we provide propositional encodings of the AR, brave, and IAR semantics, including the first encodings for Pareto- and completion-optimal repairs. Our encodings are generic and are built in a modular manner from a core set of basic formulas. Based upon these encodings, we develop in Section 4 several SAT-based algorithms, which utilize different functionalities of modern SAT solvers: weighted MaxSAT, MUS enumeration, iterative SAT calls with assumptions. In Section 5, we present our implemented system, ORBITS, which computes query answers under the chosen semantics using the selected encoding and algorithm. Section 6 presents the result of our extensive experimental evaluation, using existing OMQA and database benchmarks, aimed at comparing the different semantics, and understanding the relative performances of different encodings and/or algorithms for the same semantics. Proofs, pseudo-code for algorithms, and details on the experimental evaluation are provided in the appendix of (Bienvenu and Bourgaux 2022).

2 Querying Inconsistent Knowledge Bases

We introduce notation and terminology for talking about knowledge bases and then recall different inconsistency-tolerant semantics. We shall assume throughout the paper that readers are familiar with propositional and first-order logic. Key notions are illustrated in Example 1.

Knowledge bases By knowledge base (KB), we mean a pair $K = (D, T)$ consisting of a dataset $D$ and a logical theory $T$. The dataset $D$ is a finite set of ground facts, i.e., atoms $P(t_1, \ldots, t_n)$ where $P$ is an $n$-ary predicate and each $t_i$ is a constant. The theory $T$ is a finite set of first-order logic (FOL) sentences. An $L$ KB is a KB whose theory is formulated in the $L$ fragment of FOL. Typically, $T$ will be either an ontology (with $L$ a description logic or decidable class of existential rules) or a set of database constraints, for instance, letting $L$ be the class of denial constraints, which take the form $\forall \bar{x} \lnot (\alpha_1 \land \ldots \land \alpha_n)$, where each $\alpha_i$ is a relational or inequality atom whose variables are among $\bar{x}$. De-
pair to exploit priority relations (Staworko, Chomicki, and Marcinkowski 2012; Bienvenu and Bourgaux 2020):

**Definition 4.** Consider a prioritized KB $K_\prec$ with $K = (D, T)$, and let $R \in SRep(K)$.

- A Pareto improvement of $R$ is a $T$-consistent $B \subseteq D$ such that there is $\beta \in B \setminus R$ with $\beta \succ \alpha$ for every $\alpha \in R \setminus B$.
- The repair $R$ is a:
  - Pareto-optimal repair of $K_\prec$ if there is no Pareto improvement of $R$.
  - completion-optimal repair of $K_\prec$, if $R$ is a Pareto-optimal repair of $K_\prec$, for some completion $\succ'$ of $\succ$.

We denote by $PRep(K_\prec)$ and $CRep(K_\prec)$ the sets of Pareto- and completion-optimal repairs.

It is known that $CRep(K_\prec) \subseteq PRep(K_\prec) \subseteq SRep(K)$, with each of the inclusions potentially strict. Interestingly, however, if $\succ$ is induced by assigning scores to facts, then Pareto- and completion-optimal repairs coincide:

**Definition 5.** A priority relation $\succ$ for $K = (D, T)$ is score-structured if there exists a scoring function $s : D \to \mathbb{N}$ such that for every pair of facts $\alpha$ and $\beta$ that appear together in a conflict of $K$, we have $\alpha \succeq \beta$ iff $s(\alpha) > s(\beta)$.

**Theorem 1.** (Livshits and Kimelfeld 2017; Bourgaux 2016)

Let $K_\prec$ be a prioritized KB such that $\succ$ is score-structured. Then $CRep(K_\prec) = PRep(K_\prec)$.

Bourgaux (2016) further shows that for score-structured priorities, Pareto- and completion-optimal repairs also coincide with the $\subseteq$-$\rho$-repairs from (Bienvenu, Bourgaux, and Goadoué 2014) based upon lexicographic set inclusion.

**Repair-based semantics** We next recall three prominent inconsistency-tolerant semantics (brave, AR, and IAR), which we parameterize by the considered type of repair:

**Definition 6.** Fix $X \in \{S, P, C\}$ and consider a prioritized KB $K_\prec$ with $K = (D, T)$, query $q(x)$, and tuple of constants $\bar{a}$ from $D$ with $|\bar{a}| = |\bar{a}|$. Then $\bar{a}$ is an answer to $q$ over $K_\prec$.

- under X-brave semantics, denoted $K_\prec \models_X^\text{brave} q(\bar{a})$, if $(R, T) \models q(\bar{a})$ for some $R \in XRep(K_\prec)$.
- under X-AR semantics, denoted $K_\prec \models_X^\text{AR} q(\bar{a})$, if $(R, T) \models q(\bar{a})$ for every $R \in XRep(K_\prec)$.
- under X-IAR semantics, denoted $K_\prec \models_X^\text{IAR} q(\bar{a})$, if $(B, T) \models q(\bar{a})$ where $B = \bigcap_{R \in XRep(K_\prec)} R$.

The AR semantics is arguably the most natural way of defining plausible query answers, and it is the semantics used for consistent query answering in databases (Bertossi 2011). The brave semantics captures the notion of possible answers, while the IAR semantics identifies the answers that can be obtained using only the most reliable facts. Observe that $K_\prec \models_X^\text{IAR} q \Rightarrow K_\prec \models_X^\text{AR} q \Rightarrow K_\prec \models_X^\text{brave} q$.

**Example 1.** Let $K = (D, T)$ where $D$ contains four facts $\alpha = R(a, b)$, $\beta = R(a, c)$, $\gamma = S(d, c)$, and $\delta = S(d, b)$, and $T$ contains FDs $\forall x, y, z. R(x, y) \land R(x, z) \land y \neq z$.

The conflicts of $K$ are $\{\alpha, \beta\}$, $\{\gamma, \delta\}$, $\{\alpha, \delta\}$ and $\{\beta, \gamma\}$, hence $SRep(K) = \{\{\alpha, \beta\}, \{\gamma, \delta\}\}$. If we define $\succ$ by $\alpha \succ \beta$ and $\gamma \succ \delta$, we obtain $PRep(K_\prec) = SRep(K)$ but $CRep(K_\prec) = \{\{\alpha, \gamma\}\}$. Indeed, any completion $\succ'$ of $\succ$ is such that $\alpha \succ' \delta$ or $\gamma \succ' \beta$ by acyclicity.

If $q(x) = \exists y R(x, y)$, Causes$(q(\bar{a}), K) = \{\{\alpha\}, \{\beta\}\}$. Hence, $K_\prec \models_\text{IAR}^C q(\bar{a}), K_\prec \models_\text{AR}^P q(\bar{a})$ but $K_\prec \not\models_\text{IAR}^P q(\bar{a})$.

We briefly recall what is known about the complexity of query answering under (optimal) repair-based semantics. Note that when we speak of complexity, we mean data complexity, measured solely in terms of the size of the dataset.

Theorems 2 and 3 summarize upper and lower bounds from the database and ontology settings. All of them are known (Staworko, Chomicki, and Marcinkowski 2012; Bienvenu and Bourgaux 2020; Rosati 2011), except the lower bounds for X-brave and X-IAR semantics in the case of FDs, proven in (Bienvenu and Bourgaux 2022). We say that a logic $L$ enjoys PTIME consistency checking (resp. query entailment) if the problem of deciding whether $K \models q(\bar{a})$ for an input $L$ KB is in PTIME.

**Theorem 2.** Let $L$ be any FOL fragment that enjoys PTIME consistency checking and query entailment, and let $X \in \{S, P, C\}$. Then query entailment for $L$ KBs is

- in NP under X-brave semantics, and
- in coNP under X-AR and X-IAR semantics.

**Theorem 3.** Query entailment for $L$ KBs is

- NP-hard under X-brave semantics ($X \in \{P, C\}$)
- coNP-hard under X-AR semantics ($X \in \{S, P\}$)
- coNP-hard under X-IAR semantics ($X \in \{P\}$)

for any $L$ that extends DL-Litecore, EL, or FDs.

**Remark 1.** Query entailment under S-brave and S-IAR is tractable both for DL-Lite ontologies and denial constraints (Bienvenu and Rosati 2013).

### 3 SAT Encodings

The (co)NP complexity results from the previous section suggest a SAT-based approach to query entailment under (optimal) repair-based semantics. While our work is not the first to explore SAT encodings for inconsistency-tolerant semantics, our contribution is a uniform approach that covers a wide range of semantics and settings, and provides the first encodings for Pareto- and completion-optimal repairs.

#### 3.1 Overview

Our propositional encodings are built from:

- the set $Conf(K)$ of conflicts of the considered KB $K$,
- a set $PotAns$ of potential answers, and for each $\bar{a} \in PotAns$, the (non-empty$^2$) set Causes$(q(\bar{a}), K)$,
- the priority relation $\succ$ of $K$,

and are of polynomial size w.r.t. to these inputs. Note that for DL-Lite ontologies and denial constraints, the sets of conflicts, candidate answers, and their causes, can be computed in PTIME via database query evaluation, so our encodings will yield procedures of the expected co(NP) complexity.

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$^2$If Causes$(q(\bar{a}), K) = \emptyset$, $q(\bar{a})$ holds for none of our semantics.
To simplify the treatment, we shall assume that every conflict contains at most two facts, a property that is satisfied by the most common DL-Lite dialects and for FDs. (The extension to non-binary conflicts is discussed later in the section.) By restricting our attention to binary conflicts, we can use a convenient notation \(\alpha \perp \beta\) in place of \{\(\alpha, \beta\)\} \(\in\) Conf\((K)\), and define a graph representation of conflicts and priorities. The directed conflict graph \(\mathcal{G}_{<}\) has facts from Conf\((K)\) as nodes and an edge from \(\alpha\) to \(\beta\) iff \(\alpha \perp \beta\) and \(\alpha \not\perp \beta\).

Our encodings will use variables of the form \(x_\alpha\) to indicate whether fact \(\alpha\) appears in a (partial) repair. Including such one variable for each fact in \(\mathcal{D}\) would yield prohibitively large encodings, which is why we use \(\mathcal{G}_{<}\) to focus on relevant facts: given any \(F \subseteq \mathcal{D}\), we let \(R(F)\) be the set of all facts that are reachable in \(\mathcal{G}_{<}\) from some \(\alpha \in F\).

Before proceeding to the details, let us give a high-level overview of our encodings. All of the encodings try to construct a set of facts that is consistent with the theory (i.e. does not contain any conflicts) and that can be extended to an optimal repair. For the X-AR semantics, we are trying to build an optimal repair that does not entail the considered query answer(s), which can be done by including facts that contradict each of the answer(s) causes. For the X-brave semantics, we must ensure that the repair entails the considered query answer(s), achieved by requiring the presence of some cause in the chosen subset. Finally, for the X-IAR semantics, we ensure the existence of optimal repairs that omit a given cause or fact appearing in a cause by including facts that contradict the considered cause or fact.

In the next section, we will present SAT-based algorithms that consider each potential answer in turn, as well as algorithms that treat all potential answers conjointly. For that reason, in what follows, we will present encodings both for a single answer and for several answers at a time.

### 3.2 Basic Building Blocks

Our various encodings rely upon some common ingredients, which are presented next.

**Absence or presence of causes** To contradict a specific cause \(C\), we use \(\varphi_{\neg C}\), with two alternative definitions inspired respectively by the CQAPri and CAVSAT encodings:

\[
\varphi_{\neg C} = \bigvee_{\alpha \in C} \bigwedge_{\alpha \perp \beta, \alpha \not\perp \beta} x_\beta \quad (\text{neg}_1)
\]

\[
\varphi_{\neg C} = \bigwedge_{\alpha \in C} \neg x_\alpha \wedge \bigvee_{\alpha \in C} \bigwedge_{\alpha \perp \beta, \alpha \not\perp \beta} x_\beta \quad (\text{neg}_2)
\]

For encodings with multiple answers, we use a variant \(\varphi'_{\neg C}(y)\) obtained by adding \(\neg y\) as a disjunct of the (first) clause of \(\varphi_{\neg C}\), so it is only ‘active’ when the given variable \(y\) is true. To block all causes of the BCQ \(q(\bar{a})\), we can use

\[
\varphi_{\neg q(\bar{a})} = \bigwedge_{C \in \text{Causess}(q(\bar{a}), K)} \varphi_{\neg C}
\]

or, in the case of encodings for several answers, a variant \(\varphi'_{\neg q(\bar{a})}\) obtained by replacing \(\varphi_{\neg C}\) by \(\varphi'_{\neg C}(x_\bar{a})\).

If instead we want to force that cause \(C\) holds, we use:

\[
\varphi_C = \bigwedge_{\alpha \in C} x_\alpha
\]

and to ensure some cause for BCQ \(q(\bar{a})\) is present, we use:

\[
\varphi_{q(\bar{a})} = \bigwedge_{C \in \text{Causess}(q(\bar{a}), K)} \bigwedge_{\alpha \in C} \neg x_\alpha \vee x_\alpha
\]

or, for multi-answer encodings, a variant \(\varphi'_q(\bar{a})\) obtained from \(\varphi_{q(\bar{a})}\) by adding \(\neg x_\bar{a}\) as a disjunct of the first clause.

**Consistency** We use \(\varphi_{\text{cons}}(F)\) to ensure that the valuation of \(\{x_\alpha \mid \alpha \in F\}\) corresponds to a \(T\)-consistent set of facts:

\[
\varphi_{\text{cons}}(F) = \bigwedge_{\alpha, \beta \in F, \alpha \perp \beta} (\neg x_\alpha \vee \neg x_\beta).
\]

**Extension to optimal repair** The most intricate part of the encoding is ensuring that the selected set of facts can be extended to a repair of the desired type. To this end, we introduce formulas of the form \(\varphi_{x_{\max}}(F), \) where \(F\) provides the facts that may appear, and \(X\) is the type of repair.

- **Subset repairs:** we can simply set \(\varphi_{S\text{-max}}(F) = \top\), as every consistent set of facts extends to some \(S\)-repair.
- **Pareto-optimal repairs:** we prove that the following encoding of maximality for \(\subseteq_p\)-repairs (w.r.t. score-structured \(\succ\)) from Bienvenu et al. (2014) in fact also works for Pareto-optimal repairs and arbitrary \(\succ\):

  \[
  \varphi_{p_{1\text{-max}}}(F) = \bigwedge_{\alpha \in R(F)} (x_\alpha \vee \bigvee_{\alpha \perp \beta, \alpha \not\perp \beta} x_\beta)
  \]

  Essentially, it states that a relevant fact can only be omitted if we include a non-dominated contradicting fact. We also propose an alternative encoding with fewer variables:

  \[
  \varphi_{p_{2\text{-max}}}(F) = \bigwedge_{\alpha \in R^{-}(F)} \bigwedge_{\beta \succ \alpha} (\neg x_\alpha \vee \bigvee_{\beta \perp \gamma, \beta \not\perp \gamma} x_\gamma)
  \]

  where \(R^{-}(F) = \bigcup_{i=1}^{\infty} R_i\) with \(R_0 = F\) and \(R_{i+1} = R_i \cup \{\gamma \mid \exists \alpha \in R_i, \beta \succ \alpha, \beta \perp \gamma, \beta \not\perp \gamma\}\).

  Intuitively, to include \(\alpha \in F\), we must contradict every more preferred fact that conflicts with \(\alpha\), then do the same for selected contradicting facts.

- **Completion-optimal repairs (w.r.t. arbitrary \(\succ\))**: we use

  \[
  \varphi_{C\text{-max}}(F) = \varphi_{\text{pref}} \wedge \varphi_{\text{compl}} \wedge \varphi_{\text{acyc}}
  \]

  where the subformulas \(\varphi_{\text{pref}}, \varphi_{\text{compl}}\) and \(\varphi_{\text{acyc}}\) are defined in Figure 1. The formula \(\varphi_{\text{pref}}\) states that if \(x_\alpha\) is omitted, then we must include a contradicting fact \(\beta\) that is preferred to \(\alpha\) according to \(\succ\). We use \(\varphi_{\text{compl}}\) to ensure that \(\succ\) compares all contradicting facts and extends \(\succ\), while the acyclicity of \(\succ\) is ensured by \(\varphi_{\text{acyc}}\), which uses variables \(t_{\alpha, \beta}\) to compute the transitive closure of \(\succ\).

**Non-binary conflicts** We briefly discuss how to modify the preceding formulas to handle non-binary conflicts. The most essential difference is that instead of choosing a single contradicting fact, we may need to choose a conjunction of facts, and use additional variables to refer to them. We must also redefine \(\mathcal{G}_{<}\) as a directed hypergraph, and use hypergraph reachability to define \(R(F)\). Details of the required modifications are provided in (Bienvenu and Bourgaux 2022).
\[ \varphi_{\text{pref}} = \bigwedge_{\alpha \in R(F)} \left( \varphi_{\alpha} \lor \bigwedge_{\beta \in R(F)} x_{\alpha \rightarrow \beta} \right) \land \bigwedge_{\alpha, \beta \in R(F), \alpha \not\supset \beta} \left( \neg x_{\alpha \rightarrow \beta} \lor x_{\beta \rightarrow \alpha} \right) \land \bigwedge_{\alpha, \beta \in R(F), \alpha \not\supset \beta} \left( \neg x_{\beta \rightarrow \alpha} \lor x_{\beta \supset \alpha} \right) \]

\[ \varphi_{\text{compl}} = \bigwedge_{\alpha, \beta \in R(F), \alpha \not\supset \beta} \left( \neg x_{\alpha \rightarrow \beta} \lor x_{\beta \rightarrow \alpha} \right) \land \bigwedge_{\alpha, \beta \in R(F), \alpha \not\supset \beta} \left( \neg x_{\beta \rightarrow \alpha} \lor \neg x_{\beta \supset \alpha} \right) \land \bigwedge_{\alpha, \beta \in R(F), \alpha \not\supset \beta} x_{\alpha \supset \beta} \]

\[ \varphi_{\text{acyc}} = \bigwedge_{\alpha, \beta \in R(F), \alpha \not\supset \beta} \left( \neg x_{\alpha \rightarrow \beta} \lor \neg t_{\alpha, \beta} \right) \land \bigwedge_{\alpha, \beta \in R(F), \alpha \not\supset \beta} \left( \neg x_{\beta \rightarrow \alpha} \lor \neg \neg t_{\alpha, \beta} \right) \land \bigwedge_{\alpha, \beta, \gamma \in R(F), \alpha \not\supset \beta} \left( \neg x_{\alpha \rightarrow \beta} \land x_{\beta \rightarrow \gamma} \land t_{\alpha, \gamma} \right) \]

Figure 1: Subformulas of \( \varphi_{\text{c-max}}(F) \), which is used to ensure it is possible to extend the selected subset of \( F \) to a completion-optimal repair.

### 3.3 Propositional Encodings

We now present our encodings, built from the preceding components following the intuitions given in Section 3.1.

Note that the following results hold no matter which variant of \( \varphi_C \) we use and with \( \varphi_{\text{c-max}} \) instantiated as either \( \varphi_{\text{p-max}} \) or \( \varphi_{\text{p-max}} \). The notation \( \text{facts}(\varphi) \) will be used for the set of facts \( \alpha \) such that the variable \( x_{\alpha} \) occurs in \( \varphi \).

**X-AR semantics** Formula \( \Phi_{X-AR}(q(\vec{a})) \) in Figure 2 is used to test whether a particular tuple \( \vec{a} \) holds. Roughly speaking, it selects a way to contradict every clause, checking that the resulting set of facts is contained in a \( X \)-optimal repair. The second formula \( \Psi_{X-AR}(\text{PotAns}) \) simultaneously handles all tuples in \( \text{PotAns} \). Clauses of the form \( x_{\alpha} \) can be added to activate \( \varphi_{\text{c}}(\vec{a}) \).

The correctness of our encodings is given in the next result, which applies to all \( X \in \{S, P, C\} \) and \( \vec{a} \in \text{PotAns} \):

**Theorem 4.** The following are equivalent: (i) \( K \models \Phi_{X-AR}(q(\vec{a})) \), (ii) \( \Phi_{X-AR}(q(\vec{a})) \) is unsatisfiable, and (iii) \( x_{\vec{a}} \) is false in every satisfying assignment of \( \Psi_{X-AR}(\text{PotAns}) \).

**X-brave semantics** Figure 2 presents our encodings for the X-brave semantics. Formula \( \Phi_{X-brave}(q(\vec{a})) \) checks a particular tuple \( \vec{a} \) and is essentially the same as \( \Phi_{X-AR}(q(\vec{a})) \), but with \( \varphi_{\vec{a}} \) in place of \( \varphi_{\vec{a}} \). A variant \( \Phi_{X-brave}(C) \) can be used to check whether a particular clause \( C \) holds in some \( X \)-optimal repair. For a multi-answer encodings, we use the formula \( \Psi_{X-brave}(\text{PotAns}) \), again adding clauses of the form \( x_{\alpha} \) to activate \( \varphi'_{\vec{a}}(\vec{a}) \). We obtain an analogous correctness result:

**Theorem 5.** The following are equivalent: (i) \( K \models \Phi_{X-brave}(q(\vec{a})) \), (ii) \( \Phi_{X-brave}(q(\vec{a})) \) is satisfiable, (iii) \( \Phi_{X-brave}(C) \) is satisfiable for some \( C \in \text{Causes}(q(\vec{a}), K) \), and (iv) \( x_{\vec{a}} \) is true in some satisfying assignment of \( \Psi_{X-brave}(\text{PotAns}) \).

**X-IAR semantics** Formula \( \Phi_{X-IAR}(C) \) from Figure 2 can be used to test whether there exists an \( X \)-optimal repair that excludes clause \( C \). To check a potential answer \( \vec{a} \), we use \( \Phi_{X-IAR}(q(\vec{a})) \), which is essentially the conjunction of \( \Phi_{X-IAR}(C) \) for every clause \( C(\vec{a}) \), where the conjuncts for different causes use distinct variables \( x_{\alpha} \) in place of \( x_{\alpha} \). A multi-answer encoding \( \Psi_{X-IAR}(\text{PotAns}) \) can be obtained by taking the conjunction of \( \Phi_{X-IAR}(q(\vec{a})) \) for all \( \vec{a} \in \text{PotAns} \), but with \( \varphi_{\vec{a}} \) replaced by \( \varphi_{\text{c}}(x_{\vec{a}}) \) (see the appendix of (Bienvenu and Bourgaut 2022) for details). We obtain the following:

**Theorem 6.** The following are equivalent: (i) \( K \models \Phi_{X-IAR}(\alpha) \), (ii) \( \Phi_{X-IAR}(q(\vec{a})) \) is unsatisfiable, (iii) \( \Phi_{X-IAR}(C) \) is satisfiable for some \( C \in \text{Causes}(q(\vec{a}), K) \), and (iv) \( x_{\vec{a}} \) is false in every satisfying assignment of \( \Psi_{X-IAR}(\text{PotAns}) \).

We shall also require encodings for individual facts, using \( \Phi_{X-IAR}(\alpha) = \Phi_{X-IAR}(\{\alpha\}) \) to test if \( \alpha \) holds in all \( X \)-optimal repairs. We also consider a multi-fact version \( \Psi_{X-IAR}(\text{Rel}) \), parameterized by a set of facts \( \text{Rel} \), and to which we add clause \( y_{\alpha} \) to activate \( \varphi'_{\alpha}(\vec{a}, y_{\alpha}) \).

**Theorem 7.** For every \( \alpha \in \text{D} \), the following are equivalent: (i) \( K \models \Phi_{X-IAR}(\alpha) \), (ii) \( \Phi_{X-IAR}(\alpha) \) is unsatisfiable, and (iii) if \( \alpha \in \text{Rel} \) then \( y_{\alpha} \) is false in every satisfying assignment of \( \Psi_{X-IAR}(\text{Rel}) \).

### 4 Algorithms

Inspired by the different use of SAT solvers made by CQAPri and CAvSAT, we propose several algorithms based on the encodings of Section 3. The pseudo code of all algorithms is available in (Bienvenu and Bourgaut 2022).

Before describing the algorithms, note that we can show that the encodings of Section 3 are still valid if \( \text{Causes}(q(\vec{a}), K) \) is actually a superset of the causes such that every superfluous \( B \) in it either (1) includes a real cause of \( q(\vec{a}) \) or (2) contains two distinct facts that form a conflict. Since checking consistency and minimality to obtain the real causes can be costly in practice, our algorithms accept such ‘sets of causes’. They actually even accept the presence of self-inconsistent facts in the ‘causes’ (which would make the encodings for X-AR and X-IAR not applicable) and handle them in a preprocessing step.

Our high-level algorithm takes as input a semantics \( \text{Sem} \in \{\text{brave, AR, IAR}\} \), a repair notion \( X \in \{S, P, C\} \), a directed conflict graph \( G_{K_{\text{C}}} \), and a set of potential answers \( \text{PotAns} \) with their causes, and outputs the set of tuples from \( \text{PotAns} \) that are answers under the \( X \)-\text{Sem} semantics.

An initial preprocessing step serves to (1) check whether \( G_{K_{\text{C}}} \) contains some self-inconsistent facts, remove them from \( G_{K_{\text{C}}} \), discard all causes that contain such facts, then all answers that do not have any cause left, and (2) find some answers that trivially hold under X-Sem. To do so, it removes from the causes all facts that do not have any outgoing edge in the directed conflict graph, and thus trivially belong to all
optimal repairs. The trivial answers that have some cause that contains only such facts hold under X-Sem semantics and are filtered during this step.

It then remains to filter the remaining potential answers. The four first algorithms we propose to do so are generic in the sense that they can be used for all semantics.

- Simple is similar to the algorithm used by CQA Pri. For each answer to filter \(q\), it checks whether \(\Phi_{X-Sem}(q(\bar{a}))\) is satisfiable, which decides whether \(K_\succ \models_X \text{Sem} q(\bar{a})\).
- All-MaxSAT is similar to the CAV SAT algorithm. It constructs a weighted MaxSAT instance \(\Psi_{X-Sem}(PotAns)\) and \(\bigwedge_{\bar{a} \in PotAns} x_{\bar{a}}\), where the \(x_{\bar{a}}\) are soft clauses, and all other clauses are hard. It then relies on the solver to maximize the number of soft clauses satisfied, which filters the corresponding answers. After each iteration, the \(\neg x_{\bar{a}}\) corresponding to the satisfied soft clauses are added to the set of assumed literals for the next iteration.
- All-MUSes is based on the observation that if \(x_{\bar{a}}\) is false in every satisfying assignment of \(\Psi_{X-Sem}(PotAns)\), then \(\{x_{\bar{a}}\}\) is a minimal unsatisfiable subset (MUS) of \(\bigwedge_{\bar{a} \in PotAns} x_{\bar{a}}\) w.r.t. \(\Psi_{X-Sem}(PotAns)\). All-MUSes relies on the solver to compute all MUSes, and decides whether \(K_\succ \models_X \text{Sem} q(\bar{a})\) by looking at those of size one.
- Assumptions iteratively evaluates \(\Psi_{X-Sem}(PotAns)\), treating the variables \(x_{\bar{a}}\), with \(\bar{a} \in PotAns\) as assumptions. If \(\Psi_{X-Sem}(PotAns)\) w.r.t. \(\Psi_{X-Sem}(PotAns)\) is satisfiable, there exists a satisfying assignment of \(\Psi_{X-Sem}(PotAns)\) in which \(x_{\bar{a}}\) is true, which decides whether \(K_\succ \models_X \text{Sem} q(\bar{a})\).

While we may need to consider all causes to decide whether an answer holds under X-AR semantics, in the X-brave or X-IAR case it is sufficient to find a single cause that belongs to some or all optimal repairs. Moreover, the encoding \(\Phi_{X-IAR}(q(\bar{a}))\) is a conjunction of independent subproblems built on distinct variables for each cause, which does not seem very fit for a SAT solver. We hence propose algorithms specific to these cases.

- Cause-by-cause can be used for X-brave and X-IAR. For each answer to filter \(q\), it checks whether there is a cause \(C\) of \(q(\bar{a})\) such that \(\Phi_{X-Sem}(C)\) is (un)satisfiable: if \(\text{Sem} = \) brave and \(\Phi_{X-Sem}(C)\) is satisfiable, or \(\text{Sem} = \) IAR and \(\Phi_{X-Sem}(C)\) is unsatisfiable, then \(K_\succ \models_X \text{Sem} q(\bar{a})\); if no cause witnesses \(K_\succ \models_X \text{Sem} q(\bar{a})\), then \(K_\succ \not\models_X \text{Sem} q(\bar{a})\).

- IAR-causes is specific to X-IAR. It considers the answers in turn while maintaining two sets of facts: the X-IAR facts that belong to the intersection of the optimal repairs and the non-X-IAR facts. For each cause \(C\) of \(q(\bar{a})\) that does not contain any known non X-IAR fact, it removes the known X-IAR facts from \(C\). If \(C\) becomes empty, then \(K_\succ \not\models_{X-IAR} q(\bar{a})\). Otherwise, for each remaining \(\alpha \in C\), it checks whether \(K_\succ \models_{X-IAR} \alpha\) using \(\Phi_{X-IAR}(\alpha)\) and adds \(\alpha\) to the corresponding set of facts. If every \(\alpha \in C\) is such that \(K_\succ \models_{X-IAR} \alpha\), then \(K_\succ \models_{X-IAR} q(\bar{a})\).

- IAR-facts is also specific to X-IAR and considers the answers in turn while maintaining the two sets of X-IAR and non X-IAR facts. The difference is that for each answer, it uses \(\Psi_{X-IAR}(Rel)\) and \(\bigwedge_{\bar{a} \in Rel} y_{\bar{a}}\) and a weighted MaxSAT solver to decide which facts hold under X-IAR among the set \(Rel\) of facts that belong to some cause and have not already been assigned to one of the two sets. Then it checks whether there is a cause that only contains X-IAR facts.

5 Implementation & Experimental Setting

We implemented the algorithms presented in Section 4 in java 11. Our system ORBITS (Optimal Repair-Based Inconsistency-Tolerant Semantics) takes as input two JSON files containing the directed conflict graph \(G_{\mathcal{K}^{-}}\) and the potential answers \(PotAns\) of the query associated with their causes. The user specifies a semantics (AR, IAR, or brave), a value \(X\) (among S, P1, P2, or C) to use in \(\varphi_{X-max}(F)\), the desired encoding for \(\varphi_{\neg C}(\neg e_{\mathcal{G}} \text{ or } \neg e_{\mathcal{G}})\), and the algorithm to use to compute the answers w.r.t. the chosen semantics. The set of answers is output as a JSON file.

ORBITS relies on the code4j java library (version 2.3.4) to solve the SAT, weighted MaxSAT, and MUS enumeration problems (Berre and Parrain 2010). In principle, a standalone solver could be used, but we found that the time needed to print out the encoding to pass it to an external solver tends to be prohibitive compared to using Sat4j.
The source code of ORBITS is available at https://github.com/bourgaux/orbits, the inputs files we used in the experiments at https://zenodo.org/record/5946827, and details on the experimental setting in (Bienvenu and Bourgaux 2022).

**Experimental Environment** All experiments were run with 16GB of RAM in a cluster node running CentOS 7.9 with linux kernel 3.10.0, with processor 2x Cascade Lake Intel Xeon 5218 16 cores, 2.4GHz. Reported times are averaged over 5 runs, with a 30 minutes time-out. Since we aim at comparing our different algorithms and encodings, in what follows, we focus on the time needed to filter the candidate answers, excluding the time needed to load the inputs from the JSON files or serialize the output. This input loading time is generally below 1 second and never exceeds a few seconds. However, in real-world applications, we would not use ORBITS as a standalone tool, but rather make it a library to be integrated in a full query answering system.

**Test KBs** We evaluate ORBITS on three (sets of) KBs. The first is the CQAPri benchmark (Bourgaux 2016), a synthetic benchmark crafted to evaluate inconsistency-tolerant query answering over DL-Lite KBs, adapted from the LUBM benchmark (Lutz et al. 2013). The two others, called Food Inspection and Physicians, are real-world datasets built from public open data, which have already been used to evaluate data cleaning and consistent query answering systems (Rekatsinas et al. 2017; Dixit and Kolaitis 2019). They consist of relational databases built from the original csv files, on which typical integrity constraints have been added. We briefly summarize their main characteristics below.

We use the DL-Lite ontology (which includes 875 disjointness axioms) and 20 queries of the CQAPri benchmark, together with the 18 datasets named $uXcY$ with $X \in \{1, 5, 20\}$ and $Y \in \{1, 5, 10, 20, 30, 50\}$. Parameters $X$ and $Y$ are related to the size and the proportion of facts involved in some conflicts respectively (the higher the bigger), and the datasets are such that $uXcY \subseteq uXc'Y$ for $Y \leq Y'$ and $uXcY \subseteq uX'cY$ for $X \leq X'$. Their sizes range from 75K to 2M facts and their proportions of facts involved in some conflict from 3% to 46%. The induced conflict graphs contain from 2K to 946K facts and from 2K to 3M conflicts.

The Food Inspection dataset contains data about inspection of restaurants in New York and Chicago (Dat c; Dat a). We use the database schema and six queries proposed by Dixit and Kolaitis (2019): there are four relations, each having a key constraint and one having a further FD. The dataset contains 523K facts, 37% of them belong to some conflict. The conflict graph contains 192K facts and 219K conflicts.

We build the Physicians dataset from the National Downloadable File provided by the Centers for Medicare & Medicaid Services (Dat b). It contains information on medical professionals and their affiliations. We decompose it into seven relations, add four reasonable key constraints and two FDs, and design six queries. In total, the dataset contains more than 8M facts and 2% of them are in some conflict. The conflict graph contains 183K facts and 2.7M conflicts.

**Priority Relations** We build score-structured priority relations by randomly assigning each fact a score between 1 and $n$. To construct a non-score-structured priority relation, we consider each conflict and assign a random direction to the corresponding edge in the conflict graph with a probability $p$, except if doing so creates a cycle, and verify that the resulting priority is indeed not score-structured. On the Food Inspection and Physicians datasets, we build four priority relations: two score-structured with $n = 2$ and $n = 5$, and two non-score-structured with $p = 0.5$ and $p = 0.8$. For the CQAPri benchmark, we build two priority relations, one score-structured with $n = 5$ and one non-score-structured with $p = 0.8$, on our largest dataset (u20c50), then propagate them to the other datasets.

**Experimental Evaluation**

Our experimental evaluation aims at assessing (i) the impact of adopting different kinds of repairs, and (ii) the relative performances of alternative procedures for the same semantics. More precisely, we consider the following questions.

- What is the impact in terms of number of answers of adopting optimal repairs rather than standard repairs, or completion-optimal repairs instead of Pareto-optimal repairs when the priority relation is not score-structured?
- What is the impact of using one kind of repairs rather than another on the computation time?
- Given a semantics and type of repair, what is the impact in terms of computation times of the choice of:
  - how to encode optimality ($P_1$ or $P_2$ for Pareto-optimal repairs, $P_1$, $P_2$ or $C$ when $\succ$ is score-structured)?
  - how to encode contradictions ($\varphi \not\in C$ with neg$_1$ or neg$_2$)?
  - the algorithm used to filter the non-trivial answers?

In what follows, we summarize our main observations. Detailed results are given in (Bienvenu and Bourgaux 2022).

**Comparing Semantics w.r.t. Number of Answers** Table 1 shows the impact on the number of answers of the type of priority relation and chosen notion of optimal repairs for an example query. For each priority relation and repair type $X$, it gives the number of answers that: are trivially $X$-IAR (i.e. some cause contains only facts without outgoing edges in the directed conflict graph), hold under $X$-IAR but not trivially, hold under $X$-AR but not under $X$-IAR, hold under $X$-brave but not $X$-AR, and do not hold under $X$-brave semantics.

<table>
<thead>
<tr>
<th>Relation</th>
<th>$p=0.5$</th>
<th>$p=0.8$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P_1$</td>
<td>$C$</td>
<td>$P_2$</td>
</tr>
<tr>
<td>$C$</td>
<td>$P_1$</td>
<td>$P_2$</td>
</tr>
<tr>
<td>$P_2$</td>
<td>$C$</td>
<td>$P_1$</td>
</tr>
<tr>
<td>$C$</td>
<td>$P_1$</td>
<td>$P_2$</td>
</tr>
</tbody>
</table>

Table 1: Number of answers of q1 over the Physicians dataset depending on the priority relation (none, score-structured with $n = 2$ or $n = 5$, and not score-structured with $p = 0.5$ or $p = 0.8$) and type of repairs (standard, Pareto- or completion-optimal).
Comparing Semantics w.r.t. Computation Time

Figure 3: Best running times (in milliseconds) for each semantics and priority relation (none, score-structured with \( n = 2 \) or \( n = 5 \), not score-structured with \( p = 0.5 \) or \( p = 0.8 \)) for query q2 over the Food Inspection dataset. An empty bar means that the query ran out of time / memory for all possible algorithms and encodings. The lower part of bars is the time to identify self-inconsistent facts and trivial answers, the upper part the time to filter non-trivial answers.

Priority relations lead to fewer edges in the directed conflict graph, which in turn makes more answers hold trivially. The more the priority relation sets preferences between facts (higher parameter \( n \) or \( p \) of the priority relation), the more trivially X-IAR answers we obtain. Adopting optimal repairs also significantly increases the number of potential answers that do not hold under X-brave semantics, which are very rare when using classical subset repairs.

An interesting observation is that while, in the absence of a priority relation, many queries of the CQAPri benchmark do not have any AR answers that are not trivial, which makes trivial answers a good approximation of AR, this is no longer the case for optimal repairs. It hence seems even more important to actually compute the answers that hold under the desired semantics rather simply computing the polynomial lower bound given by the trivial answers.

Regarding the impact of the choice between Pareto- and completion-optimal repairs, in many cases ORBITS did not manage to compute the answers for completion-optimal repairs in our given time and memory limits. When it does manage to compute them (for 5 queries on the Physicians dataset; none on the Food Inspection dataset; and from between 7 and 13 on uXc1 to less than 3 on uXc50), we observe a difference with Pareto-answers in only two cases.

Choosing Semantics for Given Semantics

Table 2 presents the time needed to filter the candidate answers that hold under brave semantics based on optimal-repairs (score-structured case) for some example queries. It illustrates the huge impact that the choice of an algorithm and encoding can have. For example, q6 answers are filtered in 3.5s with algorithm Cause-by-cause and \( \varphi_{P_{\max}} \), but need at least 546s with the Assumptions algorithm, at least 5.9s with \( \varphi_{P_{\max}} \), and cannot be filtered in our time and memory limits with encoding \( \varphi_{C_{\max}} \). For X-AR and X-IAR semantics, we also observe sometimes huge variations when using the neg_1 or neg_2 version of \( \varphi_{-c} \). For example, for X-AR semantics on u20c50 with a score-structured priority relation, the best times for queries q2 and q18 are both obtained more trivial answers, but the encodings are more complex.

Given a dataset, query and semantics, if we compare two priority relations of the same kind (score-structured or not), the one that sets preferences between more facts leads to lower running times. This can be explained by the increase of the number of trivial answers and maybe by the fact that the encodings involve less facts and encode more ‘forced choices’ between facts so that there are less possibilities to explore. When we compare the ‘easiest’ non score-structured priority relations (\( p = 0.8 \)) and the hardest score-structured ones (\( n = 2 \)), which lead to comparable sizes of directed conflict graphs, score-structured priority relations seem to be easier than non-score-structured ones.

Finally, we conclude that our procedures do not perform well for completion-optimal repair-based semantics, which form most of the cases that fail due to lack of time or memory, and very often have higher running times than Pareto-optimal-based semantics with the same priority relation.
with algorithm All-MaxSAT and ϕP1-max, but with the neg2 variant for q2 (50 seconds versus 85 with neg1) and neg1 for q18 (23 seconds versus 47 with neg2). The comparison of the possible procedures for each semantics on the different datasets and queries shows that there is not a ‘best’ method in general. However, we still gain some relevant insights.

The first one concerns the choice of ϕX-max. The encoding ϕP1-max is generally the best one for Pareto-optimal repairs, in the sense that it achieves ‘close to best times’ (cf. Table 2) much more often than the others. However, there are a few cases where ϕP2-max performs significantly better, especially on the CQAAPri datasets with fewer conflicts (e.g., on u20c1 with a score-structured priority relation, the best time for filtering q9 answers under P-AR semantics is 480ms with ϕP2-max, while the best time with another encoding is 825ms). When the priority relation is score-structured, ϕC-max never significantly outperforms ϕP1-max and ϕP2-max and leads to much more time or memory failures.

The second concerns the choice of algorithm for X-IAR semantics. For all kinds of repairs, algorithm IAR-causes is generally better than the others in terms of frequency of ‘close to best times’. It is sometimes outperformed by algorithms Cause-by-cause or IAR-facts. The ‘generic’ algorithms (Simple, All-MaxSAT, All-MUSES, Assumptions) perform quite poorly, except on the simplest cases.

For the AR and brave semantics, it is more difficult to find an algorithm that is superior to the others. For non-score-structured priority relations and completion-optimal repairs, algorithm Simple seems to be the best choice for both C-AR and C-brave semantics, but all algorithms fail in most cases. A related observation is that algorithms that consider answers individually and use smaller encodings seem to be often more robust in terms of time-out and out-of-memory, with a notable exception for P-AR and P-brave semantics on u20c50 with non-score-structured priority, where algorithms All-MaxSAT and All-MUSES are more robust. For S-AR, P-AR and P-brave, we observe different behaviours depending on the benchmark: All-MaxSAT and All-MUSES tend to perform better for the CQAAPri benchmark, while Simple tends to perform better for the Food Inspection dataset.

Finally, comparing neg1 and neg2 versions of ϕ¬c, we observe that the relative performance depends on the dataset, query, algorithm, and choice of ϕX-max. However, we note that ϕP2-max usually works better with neg1. Even if there

is not a direct relationship between the encoding sizes and the running times, this is probably due to the fact that neg2 enforces that both the facts that occur in the causes and their conflicts are part of the encoding, which significantly increases the size of ϕP2-max, but has little impact on ϕP1-max.

Figure 4 shows the evolution of the running times of three algorithms using the same encoding variants as the proportion of facts involved in some conflicts grows, on the u20cY datasets with a score-structured priority for X-AR semantics (X ∈ {P,C}). It illustrates the fact that the relative performance of the algorithms depends on the query and dataset (here, the proportion of facts involved in some conflict): For example, All-MaxSAT is the best for q9 over the three first datasets, but runs out of time on the three last (more than 20% of facts in conflict), while Simple can handle them.

## 7 Conclusion

We have presented a comprehensive exploration of SAT-based approaches to querying inconsistent data using (optimal) repair-based inconsistency tolerant semantics, including the proposal of novel encodings and algorithms. Our generic framework places existing approaches into a broader context and makes our results and system directly applicable to both the (pure) database and OMQA settings.

Our experimental comparison of different SAT-based algorithms and encoding variants shows that the choice of algorithm and encoding may have huge impact on the computation time. While in some cases our results can be used to single out some approaches as more effective, more often there are no clear winner(s). This suggests that to minimize runtimes, it may make sense to launch multiple algorithms in parallel, and/or devise methods that can help predict which algorithm and encoding will perform best on a given dataset and query, e.g. using machine learning techniques.

Our work lays important foundations for the future development of mature systems for querying inconsistent data. We plan to investigate different ways of improving the performance for optimal repair-based semantics. For example, it would be interesting to explore alternative approaches for completion-optimal repairs based upon SAT modulo graph techniques (Gebser, Janhunen, and Rintanen 2014). Another promising direction is to employ more refined polynomial lower approximations than the trivial answers, such as the grounded semantics (Bienvenu and Bourgaux 2020).
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References


