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The paradigm of the filler's dielectric permittivity and aspect ratio in high- $k$  polymer nanocomposites for energy storage applications

The energy storage performances in ceramic/polymer nanocomposites are mainly linked to the dielectric permittivity and the aspect ratio of the nanofiller, though, the morphological effect (aspect ratio) is greater than the permittivity one.

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# The paradigm of the filler's dielectric permittivity and aspect ratio in high-*k* polymer nanocomposites for energy storage applications†

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Ceramic/polymer nanocomposites are promising materials for energy storage applications. The most common approach to optimize energy storage properties relies on combining a ceramic and a polymer having the highest possible dielectric permittivity and breakdown strength, respectively. It is also known that another significant factor is the aspect ratio of nanofillers where a higher aspect ratio gives rise to a higher effective dielectric permittivity of the composite. There is thus a duality between the dielectric permittivity of the ceramic and its aspect ratio that we propose to study in this paper. To achieve this, high-*k* nanocomposites were designed based on biodegradable polymer matrix polylactic acid (PLA) and different inorganic nanofillers having different shapes (spherical, rod and wire) and dielectric properties. The effects of the aspect ratio, core-shell structure, dielectric permittivity and volume fraction of the nanofillers on the dielectric and energy storage performances of PLA-based nanocomposites were assessed. An enhanced energy storage density and recovered energy density of 3.63 and 1.80 J cm<sup>-3</sup>, respectively, were obtained in nanocomposites based on rod-like fillers. We discussed, from a theoretical model, that, below the percolation threshold, the obtained properties resulted from a compromise between both the dielectric permittivity and the aspect ratio of the ceramic. This investigation provides an exciting opportunity to advance our knowledge of ceramic/polymer nanocomposites for energy storage applications.

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## 1. Introduction

Ferroelectric ceramics have high dielectric permittivity ( $\epsilon_r$ ), however, their high dielectric loss ( $\tan \delta$ ), low breakdown strength (BDS), poor processability and lack of flexibility significantly limit their integration in energy storage applications.<sup>1-6</sup> However, polymers usually have a high BDS and ease of processing, but most have a low  $\epsilon_r$ .<sup>7-9</sup> An ideal high-*k* material will not only have a high  $\epsilon_r$ , but will also display low  $\tan \delta$ , high BDS, and good processability.<sup>10-13</sup> Hence, it is reasonable to harness the advantages of both parts to design ceramic/polymer nanocomposites with enhanced energy storage performances.<sup>14-17</sup> In recent years, many efforts have been made to improve both the dielectric properties and the energy density of the ceramic/polymer

nanocomposites, for instance, (i) the use of polyvinylidene fluoride (PVDF) as a matrix because of its high  $\epsilon_r$  and BDS, and (ii) the fabrication of advanced nanostructures and the improvement of their dispersion into the polymer matrix.<sup>11,18</sup> Also, as these challenges include the need to understand the chemistry and the structure of the ceramic-polymer, the study of their interface become an attractive research topic.<sup>19,20</sup> In this respect, the preparation of core-shell structured nanoparticles by surface-initiated *in situ* polymerisation has aroused significant interest because of its unique advantages: (i) the nanoparticles can be well encapsulated with controllable polymer layer thickness, resulting in a significant reduction in the surface energy of nanoparticles. (ii) The properties of the nanocomposites can be adjusted by adapting the physical properties of the polymeric shell and/or the interaction between the polymeric shell and the polymer matrix.<sup>21-26</sup>

Indeed, the core-shell structure leads to improved dielectric, ferroelectric and energy storage properties.<sup>21,22,24,27</sup> Usually, this improvement is ascribed to the interface compatibility enhancement between the embedded core-shell fillers and the polymer matrix.<sup>27</sup> However, the dielectric properties depend also on the topological and morphological criteria.<sup>28</sup> In fact, the

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arrangement and the alignment of the nanofillers inside the polymer matrix play a pivotal role in fostering the dielectric properties of the high- $k$  nanocomposites.<sup>28,29</sup> Likewise, high aspect ratio fillers like nanowires are beneficial for designing high- $k$  nanocomposite films with enhanced performances for energy storage applications.<sup>30–34</sup> For instance, Tang *et al.* demonstrated that the  $\epsilon_r$  of the nanocomposite can be highly efficiently improved by the high aspect ratio of the fillers without additional fillers or defect incorporation into the nanocomposites.<sup>35</sup> Furthermore, Tang *et al.* reported that embedding PbZr<sub>0.52</sub>Ti<sub>0.48</sub>O<sub>3</sub> (PZT) nanowires in the PVDF matrix could enhance the energy storage density by 77.8% compared to that of PZT nanorods.<sup>36</sup>

In the background, studies on ceramic/polymer nanocomposites raise the question of the design of the nanocomposite. Indeed, the energy storage properties are expected to depend on the individual dielectric properties of the polymer and the ceramic, the volume fraction and the morphological and topological characteristics of the ceramic.<sup>31,36,37</sup> From this perspective, an efficient design of the ceramic/polymer composite requires to define the optimal parameters that lead to the highest stored energy density. This is an important element to which there is no obvious answer at first glance. The reason for this is that (i) the storage properties result from complex interactions between the parameters listed above and (ii) some parameters may have antagonistic effects on the resulting storage properties. To better understand this, consider the first example, which will be studied in this paper, of the duality that exists between the  $\epsilon_r$  and the aspect ratio of the ceramic. All things being the same, the choice of a high  $\epsilon_r$  ceramic embedded in a polymer matrix results in a higher effective  $\epsilon_r$  of the composite. This, at first glance, goes in the direction of an increase in the stored energy density. However, the negative impact of a large difference in the  $\epsilon_r$  of the ceramic and the polymer that leads to local electric field intensification and interfacial polarization should also be taken into account, which induces a reduction of the effective BDS of the composite.<sup>38</sup> Thus, lower stored energy density is obtained. As a consequence, the use of a high  $\epsilon_r$  ceramic does not necessarily result in an increase of the stored energy density. Let us now consider the aspect ratio of the ceramic, a higher aspect ratio will inevitably improve the  $\epsilon_r$  of the nanocomposites.<sup>8,39,40</sup> There are two reasons behind this: first, the high aspect ratio fillers reach the percolation threshold ( $f_c$ ) more easily than the low aspect ratio fillers, which allows connectivity or a continuous path in the system and improves the dielectric properties of the composites.<sup>41</sup> Second, the high aspect ratio fillers have lower surface area than low aspect ratio fillers, which helps to reduce the surface energy, thus preventing agglomeration, enhancing the overall performance of the composites.<sup>42</sup>

These are important aspects to which it is difficult to provide answers and an obvious correlation exists with the energy storage properties of the nanocomposite. Through experimental and theoretical approaches, this paper aims to study and to better understand the effects of the volume fraction,

core-shell structure, dielectric permittivity and aspect ratio of the nanofillers on both the dielectric and energy storage properties of PLA-based nanocomposites. The polylactic acid (PLA) polymer was selected due to its biodegradability and biocompatibility, which could be encouraging to design eco-friendly high- $k$  nanocomposites for biomedical applications.<sup>43,44</sup> A comparison of the electrical properties of PLA, some biopolymers and petrol-based polymers are shown in Section S1.2 in the ESI.† Besides, the Ba<sub>0.85</sub>Ca<sub>0.15</sub>Zr<sub>0.10</sub>Ti<sub>0.90</sub>O<sub>3</sub> (BCZT) lead-free ceramic known for its excellent dielectric, ferroelectric and energy storage performances was chosen.<sup>45–53</sup>

In the first step, near-spherical BCZT was embedded in the PLA matrix. Moreover, a core-shell structuration step was designed *via* polydopamine (PDA), which is an extensively used organic compound for this process,<sup>21,54,55</sup> to enhance the compatibility between BCZT and PLA. In the second step, H<sub>2</sub>(Zr<sub>0.1</sub>Ti<sub>0.9</sub>)<sub>3</sub>O<sub>7</sub> nanowires were usually used as an inorganic template to design architected ferroelectric materials,<sup>56</sup> and rod-like BCZT fillers<sup>57</sup> were encapsulated in the PLA matrix. Both H<sub>2</sub>(Zr<sub>0.1</sub>Ti<sub>0.9</sub>)<sub>3</sub>O<sub>7</sub> nanowires and rod-like BCZT fillers have different dielectric permittivities and aspect ratios compared to those of near-spherical BCZT particles.

## 2. Experimental

Ba<sub>0.85</sub>Ca<sub>0.15</sub>Zr<sub>0.10</sub>Ti<sub>0.90</sub>O<sub>3</sub> near-spherical particles (B\_NP), H<sub>2</sub>(Zr<sub>0.1</sub>Ti<sub>0.9</sub>)<sub>3</sub>O<sub>7</sub> nanowires (HZTO\_NW) and Ba<sub>0.85</sub>Ca<sub>0.15</sub>Zr<sub>0.10</sub>Ti<sub>0.90</sub>O<sub>3</sub> rod-like (B\_NR) nanopowders were synthesised using soft-chemistry routes.<sup>45,57–59</sup> The elaborated nanofillers were shown to have different morphologies and/or permittivities (see Table 1 and Fig. 1). The core-shell structure of B\_NP using a polydopamine (PDA) layer will be designed by B\_NP@PDA. Using the solvent casting method, the elaborated nanofillers were then dispersed in the PLA matrix to form nanocomposites. In this study, the volume fraction of the fillers was set to less than or equal to 20 vol% because of the deterioration of the mechanical properties at high loading and the spherical packing limitations. The detailed experimental procedure, sample characterisations and structural properties of BCZT/PLA nanocomposites are provided in Sections S1 and S2 in the ESI.†

## 3. Results and discussions

### 3.1. Morphological properties of the PLA-based nanocomposites

Fig. S5 (ESI†) shows the morphological characteristics of the PLA-based nanocomposites at the surface and the cross-section after embedding 3 vol% of B\_NP, B\_NP@PDA, HZTO\_NW and

**Table 1** Comparison of the  $\epsilon_r$  (at 1 kHz) and microstructure properties of B\_NP, HZTO\_NW and B\_NR sintered ceramics at 1250 °C/10 h

Ceramic	Shape	Aspect ratio	Dielectric permittivity
B_NP	Near-spherical	1	12085
HZTO_NW	Nanowire	50	350
B_NR	Nanorod	10	11906



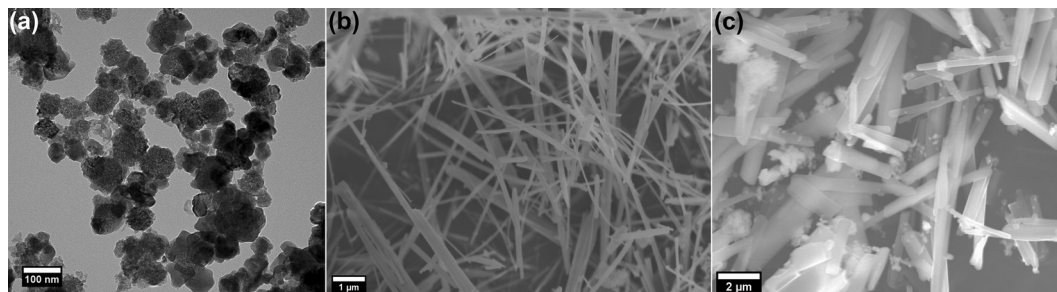


Fig. 1 (a) TEM micrograph of B\_NP, and (b and c) FESEM micrographs of HZTO\_NW and B\_NR, respectively.

B\_NR fillers in the PLA matrix. The black region corresponds to the PLA matrix, while the white spots represent the fillers. It is observed that all nanofillers are correctly dispersed in the PLA matrix. To gain insight into the compatibility between the different nanofillers and PLA matrix, Fig. 2e–h provide an overview of the distribution of B\_NP, B\_NP@PDA, HZTO\_NW and B\_NR fillers inside the PLA matrix *via* cross-section views. The nanofillers show excellent dispersion in the PLA matrix and a large number of fillers are covered with the PLA matrix, especially in nanocomposites with high aspect ratio fillers. This suggests the excellent compatibility between the matrix and the loads. To study the effect of core–shell structure using PDA, 20 vol% of B\_NP and B\_NP@PDA were introduced in the PLA matrix, and the morphological characteristics of both films are presented in Fig. 2. Even though high filler content was embedded, a good dispersion of the fillers in PLA matrix is

clearly observed. It is worth mentioning that several B\_NP@PDA particles are bound together (see inset of Fig. 2b), which could be due to the high dopamine concentration used in the core–shell formation step. Remarkably, at a high filler concentration, B\_NP@PDA particles form noticeable acicular paths in the PLA matrix (see the red eclipse in Fig. 2d), leading to the formation of well-connected ellipsoidal agglomerations of B\_NP@PDA particles as illustrated in Fig. 2f. This further proves the chemical bounding of B\_NP@PDA and PLA *via* the PDA shell.

### 3.2. Dielectric properties of the PLA-based nanocomposites

The frequency-dependencies of the dielectric permittivity ( $\epsilon_r$ ) and the dielectric loss ( $\tan \delta$ ) of B\_NP/PLA, B\_NR@PDA/PLA, HZTO\_NW/PLA and B\_NR/PLA nanocomposite films with different volume fractions are provided in the S2.2 Section in the ESI.† Besides, Fig. 3 summarises the values of  $\epsilon_r$  and  $\tan \delta$  at different volume fractions as measured at 1 kHz for all nanocomposite films. From a global point of view, it appears that both  $\epsilon_r$  and  $\tan \delta$  gradually increase with the increase in the volume fraction. It can also be pointed out that for all filler concentrations, the dielectric properties of B\_NP@PDA/PLA nanocomposites are systematically improved with respect to B\_NP/PLA. Furthermore, the nanocomposites with high aspect ratio fillers (rods and nanowires) exhibit enhanced dielectric properties compared to those based on B\_NP and B\_NP@PDA although the dielectric permittivity of the fillers is lower than those of B\_NP (see Table 1). For instance, at 20 vol%, the dielectric permittivity values of B\_NP/PLA, B\_NP@PDA/PLA, HZTO\_NW/PLA and B\_NR/PLA nanocomposite films are found to be 9.11, 11.24, 16.00 and 20.28, respectively. More interestingly, the dielectric loss is decreased in the nanocomposites based on fillers with a high aspect ratio, *e.g.*, embedding PLA matrix with 20 vol% B\_NR can enhance the dielectric permittivity more than two-fold compared to B\_NP with the same loading, while keeping low dielectric loss.

### 3.3. Energy storage properties of the PLA-based nanocomposites

To gain insights into the energy storage of PLA-based nanocomposite films, Fig. S7 in the ESI† displays the positive branch of the dielectric displacement–electric field ( $D$ – $E$ ) loops of the PLA-based nanocomposites measured at 100 Hz and under an electric field of  $1 \text{ MV cm}^{-1}$ . The maximum electric displacement

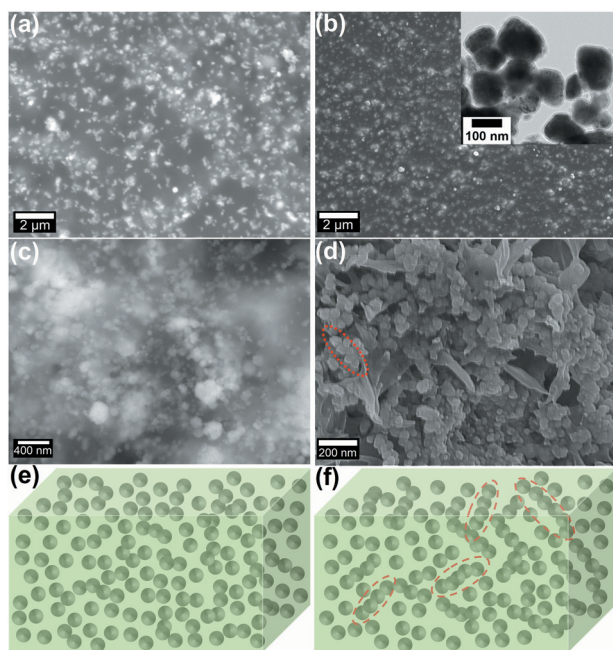


Fig. 2 Morphological properties of B\_NP/PLA and B\_NP@PDA/PLA at 20 vol% of nanofillers. FESEM images at the surface (a and b) and the cross-section (c and d). The inset of b shows agglomerated B\_NP@PDA particles. Schematic illustrations of the dispersion of the fillers inside the PLA matrix in (e) 20 vol% B\_NP/PLA and (f) 20 vol% B\_NP@PDA/PLA nanocomposite films, respectively.



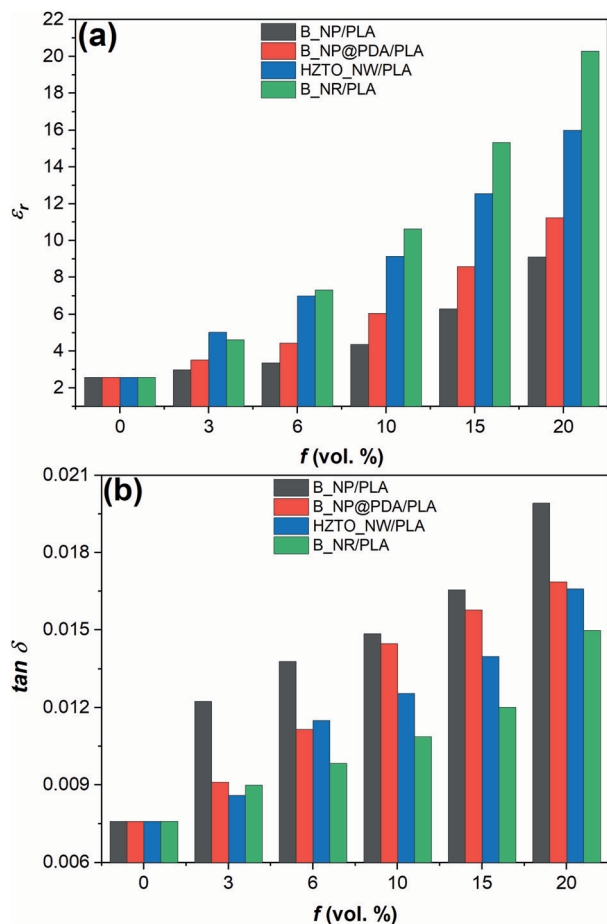


Fig. 3 Effect of the volume fraction of B\_NP, B\_NP@PDA, HZTO\_NW and B\_NR fillers on the (a) dielectric permittivity and (b) dielectric loss of PLA-based nanocomposites.

( $D_{\max}$ ) and the remnant electric displacement ( $D_r$ ) of each nanocomposite increase with increasing filler concentration. Furthermore,  $D_{\max}$  and  $D_r$  of B\_NR/PLA nanocomposites are higher than those of HZTO\_NW/PLA, B\_NP@PDA/PLA and B\_NP/PLA. From the recorded  $D$ - $E$  loops, the total energy density ( $W_{\text{tot}}$ ) of the nanocomposites can be estimated using Eqn (1).<sup>60</sup>  $W_{\text{tot}}$  was calculated *via* numerical integration by adding the area around the closed area of the  $D$ - $E$  hysteresis loops (energy loss density,  $W_{\text{loss}}$ ) and the area between the polarisation axis and the upper

branch curve of the unipolar  $D$ - $E$  hysteresis loop (recovered energy density,  $W_{\text{rec}}$ ). The calculated values of the energy density at 1 MV cm<sup>-1</sup> are presented in Fig. 4a. The total stored energy density increases with increasing nanofiller concentration. It should be noted that the observed energy density values of B\_NR/PLA nanocomposites are systematically higher than those of HZTO\_NW/PLA, B\_NP@PDA/PLA and B\_NP/PLA due to the enhanced dielectric displacement in B\_NR/PLA nanocomposites. At a nanofiller concentration of 20 vol%, the  $W_{\text{tot}}$  values are 3.63, 3.13, 2.47 and 1.43 J cm<sup>-3</sup> for B\_NR/PLA, HZTO\_NW/PLA, B\_NP@PDA/PLA and B\_NP/PLA, respectively.

In order to evaluate the effective energy storage capability of our samples, the recovered energy density ( $W_{\text{rec}}$ ) was determined. As shown in Fig. 4b, the recovered energy density values of B\_NR/PLA nanocomposites are systematically higher than those of HZTO\_NW/PLA, B\_NP@PDA/PLA and B\_NP/PLA, respectively. At 20 vol%, the  $W_{\text{rec}}$  values, determined from eqn (2), are 1.80, 1.31, 1.11 and 0.55 J cm<sup>-3</sup> for B\_NR/PLA, HZTO\_NW/PLA, B\_NP@PDA/PLA and B\_NP/PLA, respectively. The energy storage efficiency ( $\eta$ ) can be defined as the ratio of recovered energy density to the total stored energy density, as estimated in eqn (3).<sup>61</sup> As shown in Fig. 4c, at a filler concentration of 20 vol%, the calculated values of  $\eta$  are 49.58, 41.85, 44.94 and 38.48% for B\_NR/PLA, HZTO\_NW/PLA, B\_NP@PDA/PLA and B\_NP/PLA, respectively.

$$W_{\text{tot}} = \int_0^{D_{\max}} E dD \quad (1)$$

$$W_{\text{rec}} = \int_{D_r}^{D_{\max}} E dD \quad (2)$$

$$\eta(\%) = \frac{W_{\text{rec}}}{W_{\text{tot}}} \times 100 = \frac{W_{\text{rec}}}{W_{\text{rec}} + W_{\text{loss}}} \times 100 \quad (3)$$

It is observed that the total stored energy density of the nanocomposite with 20 vol% of B\_NR is ten times higher than that of the pure PLA polymer (0.365 J cm<sup>-3</sup>). Meanwhile, the recovered energy density of the nanocomposite with 20 vol% B\_NR is more than six-fold that of PLA polymer (0.365 J cm<sup>-3</sup>). Surprisingly and although the permittivity of HZTO is much smaller than BCZT (approximately thirty times lower), the energy storage performances of HZTO\_NW/PLA are much better than

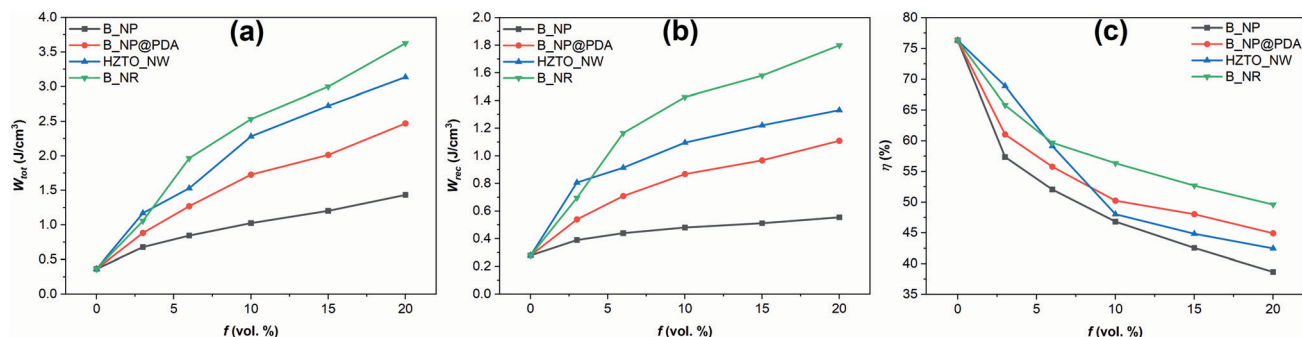


Fig. 4 Energy storage performances of the PLA-based nanocomposites. (a) The total, (b) recovered energy densities and (c) energy storage efficiency.



those of both B<sub>NP</sub>/PLA and B<sub>NP</sub>@PDA/PLA. In order to go further in this direction, it is interesting to note that  $W_{\text{tot}}$ ,  $W_{\text{rec}}$  and  $\eta$  of HZTO<sub>NW</sub> are higher than those of other PLA-nanocomposites at  $f = 3$  vol% (Fig. 4). This can be related to a higher effective permittivity and lower dielectric loss of the HZTO<sub>NW</sub>/PLA at 3 vol% (Fig. 3). As the matrix is identical in all the cases studied, this can be reasonably attributed to the large aspect ratio of HZTO which beneficially affects both the effective permittivity and dielectric loss of the nanocomposite. At a higher filler content, HZTO fillers tend to aggregate in the matrix because of their large specific surface energy. After the completion of the formation of a percolation network in the polymer matrix the dipoles of polymer are pinned by the surface charges or defects at the interface between the matrix and the filler. Accordingly, the electrical properties are degraded.<sup>28</sup> Such behaviour was also observed by Wang *et al.* when comparing four kinds of nanowires (Na<sub>2</sub>Ti<sub>3</sub>O<sub>7</sub>, TiO<sub>2</sub>, BaTiO<sub>3</sub> and SrTiO<sub>3</sub>).<sup>10</sup>

From the above results and as expected, the energy storage properties depend on both the effective dielectric permittivity and the dielectric loss of the nanocomposite. The two physical quantities are shown to result from a compromise between the dielectric permittivity and the aspect ratio of the filler. This point goes against the most common approach that consists in combining a ceramic and a polymer having the highest possible dielectric permittivity and breakdown strength, respectively. The alternative approach may be to focus more on the aspect ratio of the filler than its dielectric permittivity. However, this requires a better understanding of their relative contributions. This is an important point for the design of ceramic/polymer nanocomposites for high-efficiency energy storage applications. In the following section, we will discuss the results obtained *via* theoretical calculations.

### 3.4. Effect of the core-shell structure

Many works have demonstrated that polydopamine is very promising for utilization as a surface modifier to improve the inclusion of nanofillers inside polymer matrices, because of its powerful adhesion ability.<sup>18,62,63</sup> It was found that the dielectric properties of the core-shell structured nanocomposites (B<sub>NP</sub>@PDA/PLA), were higher compared to the non-core-shell structured ones (B<sub>NP</sub>/PLA). This enhancement of the dielectric properties in B<sub>NP</sub>@PDA/PLA films could be related to the improved interfacial compatibility between the nanoparticles and the PLA matrix, which suppresses the dipolar polarisation loss of the PLA matrix.<sup>64</sup> Furthermore, the surface water layer and other impurities may be removed during the introduction of the PDA layer onto the B<sub>NP</sub> nanoparticle's surface, resulting in reduced electrical conduction and/or interfacial polarisation loss.<sup>21</sup> Moreover, the dielectric losses in B<sub>NP</sub>@PDA/PLA are lower while it exhibits a higher permittivity than B<sub>NP</sub>/PLA. Another important reason for the improvement of the dielectric properties of B<sub>NP</sub>@PDA/PLA nanocomposite films could be the formation of well-connected ellipsoidal agglomeration of B<sub>NP</sub>@PDA particles observed in Fig. 2d, which could affect both the 3D topology and the effective aspect ratio; the particles can no longer be considered

spherical but rather ellipsoidal. This point will be discussed further. Nevertheless, it has been recognised that the functionalisation does not have a very pronounced effect on dielectric properties of the nanocomposites.

### 3.5. Effect of the filler volume fraction on the iso-aspect ratio

Permittivity is a property that characterises the electrical polarisation of a material under an external electric field. In our composites, the PLA polymer shows a low permittivity ( $\epsilon_r = 2.7$ ), while the B<sub>NP</sub> ceramic exhibits high permittivity as-sintered ( $\epsilon_r = 12\,085$ ). For the latter, the high dielectric permittivity reflects the spontaneous polarisation of ferroelectrics; a small electric field is enough to create large polarisation. In order to better understand the evolutions of the effective permittivity of the nanocomposites, the fundamental question that arises is how the inclusions of the B<sub>NP</sub> ceramic into host PLA polymer influence the polarisation field. However, the answer depends on many factors such as morphology, 3D distribution and orientation of inclusions, the norm and the frequency of the external field applied, and the dielectric mismatch between the PLA polymer and the B<sub>NP</sub> ceramic. From a general aspect, the problem that has arisen in determining the effective permittivity of heterostructures. It is a complex problem that has attracted attention beginning with the pioneering work of Maxwell.<sup>65</sup> Section S2.3 in the ESI<sup>†</sup> provides step-by-step possible answers to the previous question. It was observed that the measured dielectric permittivities show a linear dependence on the volume fraction of BCZT (Fig. S8 in the ESI<sup>†</sup>). Moreover, below the percolation threshold ( $f_c = 27\%$  for spheres), the volume fraction effect is certainly present but much less than that beyond the percolation threshold. This can be explained by the fact that the domains are spatially separated, and electrostatic interactions between each inclusion and its neighbours are relatively weak when the volume fraction of fillers are below the percolation threshold.<sup>66</sup>

### 3.6. Effect of the dielectric permittivity on the iso-aspect ratio

As observed experimentally, below the percolation threshold the effective permittivity increases linearly with both increasing volume fraction and permittivity of B<sub>NP</sub>. However, based on theoretical calculations, for a critical value of permittivity of around 100 (that corresponds to a dielectric mismatch of  $\frac{100}{2.7} \approx 37$ ), the effective permittivity no longer evolves. In other terms, when spherical inclusions do not touch each other, there is a critical permittivity of B<sub>NP</sub> from which the effective permittivity does not increase even for giant permittivities of the B<sub>NP</sub> ceramic (Fig. 5). As demonstrated in S2.3 Section in the ESI<sup>†</sup> the polarisability  $\alpha$  increases with increasing B<sub>NP</sub> permittivity to reach a stagnant stage for a value of B<sub>NP</sub> permittivity around 200 (Fig. S9, ESI<sup>†</sup>). Besides, the internal field inside inclusions decreases dramatically with increasing B<sub>NP</sub> permittivity. This means that the penetration of the electrical field into B<sub>NP</sub> inclusions is difficult when the electrical contrast between B<sub>NP</sub> and PLA becomes high.<sup>67,68</sup> There are reasons why the effective permittivity of the



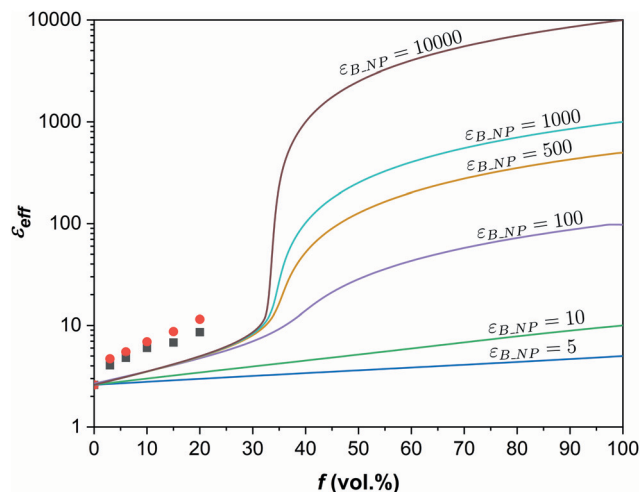


Fig. 5 Evolution of the effective permittivity of the composite as a function of B\_NP volume fraction for different values of B\_NP permittivity. Comparison with the experimental data.

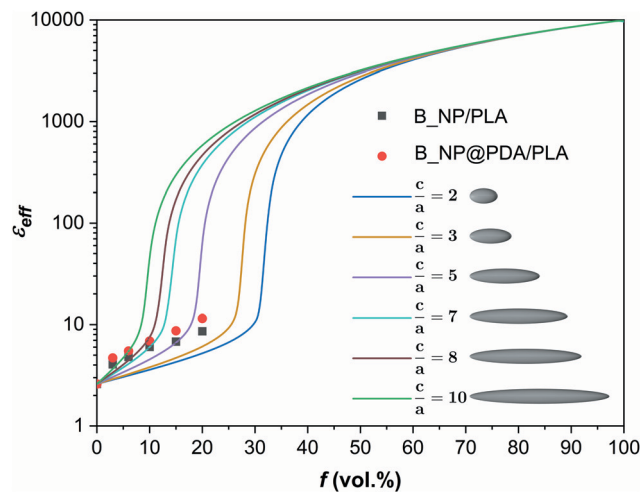


Fig. 6 Evolution of the effective permittivity of the B\_NP/PLA composite as a function of the aspect ratio of the B\_NP charge. For all calculations, the permittivity of the B\_NP ceramic was considered equal to 10 000.

composite is no longer increased beyond a critical permittivity of B\_NP (evaluated at around 200 in this work) for volume fractions of B\_NP lower than the percolation threshold. This latter is thus the key parameter for controlling the resulting properties of the nanocomposites.

In the case of non-spherical inclusions and/or the non-random distribution of inclusions, the percolation threshold is expected to decrease as it becomes more likely for the inclusions to touch each other. In our study, this is an interesting aspect since the morphology of dispersed B\_NP is clearly not spherical in the B\_NP@PDA/PLA composite and there is little chance that the distribution of B\_NP into the composite is perfectly homogeneous. These are the probable reasons that would explain that the effective permittivities measured are located above the curves calculated (see Fig. 5).

### 3.7. Effect of the filler's aspect ratio on iso-permittivity

As explained before, the morphology of the dispersed B\_NP ceramic can influence the effective permittivity of the composites. In order to study this effect, the model developed for a mixture of randomly oriented ellipsoids of the B\_NP ceramic into the PLA matrix was adapted,<sup>69</sup> as discussed in section S2.4 in the ESI.† For a given permittivity of B\_NP of 10 000, increasing the aspect ratio of B\_NP ceramic leads to an increase of the effective permittivity of the composite because the induced polarisability is enhanced with the aspect ratio. Interestingly, From Fig. 6, it is observed that a prompt increase of the effective permittivity at a given volume fraction of B\_NP depends on the aspect ratio. These occur as if the effective permittivity is highly improved at a volume fraction corresponding to the percolation threshold. In other words, this enhancement of the effective permittivity is attributed to the increase in the aspect ratio, which decreases the percolation threshold of the embedded fillers (Fig. S10, ESI†).<sup>70</sup> These theoretical calculations corroborate those obtained experimentally, where an enhancement of the dielectric properties

in the fillers with a high aspect ratio compared to near-spherical particles was noticed.

It was reported that the high aspect ratio fillers can improve the dielectric properties of the composites.<sup>35,71,72</sup> Theoretically, the high aspect ratio fillers reach the percolation threshold more easily than the low aspect ratio fillers, which allows connectivity or continuous path in the system and improves the dielectric properties of the composites.<sup>41,73</sup> Moreover, the high aspect ratio can improve the dielectric permittivity of the composites due to the large dipole moment.<sup>35</sup> Besides, the high aspect ratio fillers have lower surface area than low aspect ratio fillers, which helps to reduce the surface energy, thus preventing agglomeration and enhancing the overall performance of the composites.<sup>42</sup> Therefore, these results suggest that the use of high aspect ratio nanofiller could enhance the energy storage performance of PLA-based nanocomposites.<sup>8,31,74</sup>

### 3.8. Compromise between dielectric permittivity and the aspect ratio

Two main results were highlighted previously. For volume fractions of B\_NP lower than the percolation threshold, the effective permittivity of the composite is no longer increased beyond a critical permittivity of B\_NP (evaluated around 200 in this work). The development of ceramic/polymer composites is mainly motivated by the large difference in the dielectric properties of the ceramic as a filler and polymer as the matrix. It was observed that the composites based on ceramic fillers owning relatively low dielectric permittivity (B\_NR and HZTO\_NW) exhibit enhanced dielectric properties and energy storage performances compared to those with fillers with large dielectric permittivity (B\_NP). As discussed before, according to the modelling results, there is a critical value of the ceramic fillers' permittivity; beyond which, the effective permittivity of the composite is no longer increased. Besides, it was argued before that the percolation threshold is a crucial parameter to control the resulting properties of the composites. Below the





percolation threshold, the effective permittivity increases linearly with increasing volume fraction and permittivity of B\_NP. However, when tuning the shape and/or the distribution of the inclusions inside the polymer the percolation threshold is expected to decrease as it becomes more likely for the inclusions to touch each other. The composites based on ceramic fillers with a high aspect ratio percolate easily at a low filler content, hence enhanced electrical properties were observed at a low filler loading. Hence, there is a mutual effect of the dielectric permittivity and the aspect ratio of the ceramic filler on the dielectric properties and energy storage performances in the ceramic/polymer nanocomposite. A paradigm emerges, which can be summarised as follows: for improving the dielectric properties of the composite, it is not necessary to use ceramics with high permittivity, but we should instead control their geometry.

The analyses performed in Section S2.4 in the ESI† show that both permittivity and aspect ratio of B\_NP ceramic control the effective permittivity of the composite. Then, one might ask oneself what couples  $(\epsilon_{B\_NP}, \frac{c}{a})$  might fit the experimental data. The results of the calculations presented in Fig. 7 evidence that the solution is not unique; there exists an infinite. The most striking result that emerges is that the experimental data can be fitted with very different values of B\_NP permittivity but relatively close values of aspect ratio (see for example the couples  $(\epsilon_{B\_NP} = 10\,000, \frac{c}{a} = 3.9)$  and  $(\epsilon_{B\_NP} = 200, \frac{c}{a} = 5.5)$ ). We show here that a drastic decrease of the B\_NP permittivity can be compensated by a relatively slight increase of the aspect ratio of B\_NP. This is a key point for improving the energy storage properties of the composite since the large difference between the dielectric permittivity of the inclusions and the matrix can lead to local electric field intensification and interfacial polarization.<sup>23,42,75,76</sup> Thus, there is a mutual interaction between the dielectric permittivity and the aspect ratio of the

ceramic filler, and the resulting dielectric properties and energy storage performances are based on a compromise between the dielectric permittivity and the aspect ratio of the ceramic filler.

## 4. Summary and conclusions

High-*k* nanocomposites based on biodegradable polymer matrix polylactic acid (PLA) and different inorganic nanofillers with various shapes (spherical, rod and wire) and arrangements were successfully fabricated. The effects of nanofiller's permittivity, aspect ratio and the core-shell structure were explored by experimental and theoretical approaches. Very surprisingly, the core-shell structure does not have a very pronounced effect on the dielectric properties of the nanocomposites (effective permittivity and dielectric loss). Subsequently, the effect of the aspect ratio was studied after observing the ellipsoidal arrangement in the core-shell structured nanocomposites. It was concluded that a substantial decrease of the B\_NP permittivity could be compensated by a relatively slight increase of the aspect ratio of B\_NP. Consequently, a paradigm has emerged since the development of ceramic/polymer composites is mainly motivated by the significant differences in the dielectric properties of the ceramic as the filler and polymer as a matrix. To address this issue, two types of ceramic fillers possessing adverse properties, *i.e.*, B\_NR with high dielectric permittivity and high aspect ratio and HZTO\_NW with low dielectric permittivity and very high aspect ratio, were embedded in the PLA matrix. The enhancement of the dielectric properties in fillers with a high aspect ratio compared to near-spherical particles was attributed to the low percolation threshold of such fillers with a high aspect ratio. Finally, the energy storage performances of PLA-based nanocomposites were evaluated by *D-E* loops using spherical, rod, and wire-shaped particles. The highest  $W_{tot}$  and  $W_{rec}$  of 3.63 and 1.80 J cm<sup>-3</sup>, respectively, were obtained in the nanocomposites based on rod-like fillers. Hence, the use of high-aspect-ratio nanofiller with high dielectric permittivity enhances the energy storage performance of PLA-based nanocomposites. Accordingly, this study reveals a paradigm between the dielectric permittivity and the aspect ratio of the ceramic filler. The resulting dielectric properties and energy storage performances in ceramic/polymer nanocomposite were based on a compromise between the dielectric permittivity and the aspect ratio of the ceramic filler.

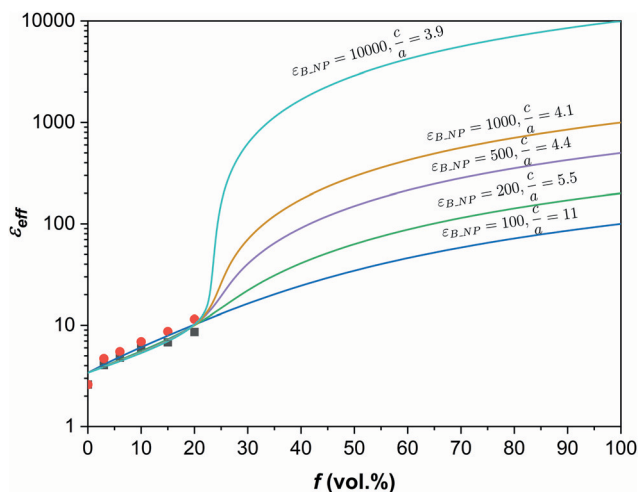


Fig. 7 Calculation of the effective permittivity of the B\_NP/PLA composite as a function of the B\_NP volume fraction for different couples  $(\epsilon_{B\_NP}, \frac{c}{a})$  and comparison with the experimental data.

## Conflicts of interest

There are no conflicts to declare.

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