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Random survival forests for competing risks with multivariate longitudinal endogenous covariates

Anthony Devaux^{1,*}, Catherine Helmer¹, Carole Dufouil¹, Robin Genuer^{1,2,†}, and Cécile Proust-Lima^{1,†}

¹Univ. Bordeaux, INSERM, Bordeaux Population Health, UMR1219, Bordeaux, France

²INRIA Bordeaux Sud-Ouest, Talence, France

*Email: anthony.devaux@u-bordeaux.fr

†These authors contributed equally to this work

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Abstract: Predicting the individual risk of a clinical event using the complete patient history is still a major challenge for personalized medicine. Among the methods developed to compute individual dynamic predictions, the joint models have the assets of using all the available information while accounting for dropout. However, they are restricted to a very small number of longitudinal predictors. Our objective was to propose an innovative alternative solution to predict an event probability using a possibly large number of longitudinal predictors. We developed **DynForest**, an extension of random survival forests for competing risks that handles endogenous longitudinal predictors. At each node of the trees, the time-dependent predictors are translated into time-fixed features (using mixed models) to be used as candidates for splitting the subjects into two subgroups. The individual event probability is estimated in each tree by the Aalen-Johansen estimator of the leaf in which the subject is classified according to his/her history of predictors. The final individual prediction is given by the average of the tree-specific individual event probabilities. We carried out a simulation study to demonstrate the performances of **DynForest** both in a small dimensional context (in comparison with joint models) and in a large dimensional context (in comparison with

a regression calibration method that ignores informative dropout). We also applied **DynForest** to (i) predict the individual probability of dementia in the elderly according to repeated measures of cognitive, functional, vascular and neuro-degeneration markers, and (ii) quantify the importance of each type of markers for the prediction of dementia. Implemented in the R package **DynForest**, our methodology provides a solution for the prediction of events from longitudinal endogenous predictors whatever their number.

Keywords: Individual dynamic prediction; Multivariate predictors; Random survival forest; Longitudinal data; Survival data; Competing risks.

1 Background

Quantifying the patient specific risk of disease or of progression based on patient’s information has become a crucial issue in modern medicine. This may be done in order to monitor the disease progression, adapt therapeutic strategies or stratify patients according to their risk. One strategy is to predict the risk of event using only the data collected at the prediction time. However, in many contexts, patients data include repeated measures of markers which trajectories are highly predictive of the event. This is the case for instance with prostate specific antigen for the risk of prostate cancer recurrence [1] or serum creatinine for the risk of kidney graft failure [2]. Including the history of such markers in predictive tools usually provides more accurate predictions. In addition, since they can be updated each time new marker information becomes available, such individual predictions are said dynamic [1]. In prostate cancer or kidney graft failure, one specific marker is targeted for the clinical event prediction. However in other contexts, many potential markers may be relevant for the prediction of an event. This is for instance the case in the prediction of cardiovascular disease risk where many markers from electronic health records have been exploited [3].

Longitudinal markers are endogenous variables in the sense that they may be affected by the event of interest [4], and they are usually measured intermittently with a measurement error. This makes their statistical analysis challenging. Three approaches were proposed in the literature for the prediction of a clinical event given longitudinal endogenous information: *landmark models* [5],

joint models [1, 6] and *regression calibration* techniques [7].

Landmark models consist in considering only the subjects still at risk of the event at a prediction time t (also called landmark time) and including their information collected until this landmark time to build a prediction tool for subsequent risk of event [5, 8]. The longitudinal information of intermittently measured and prone-to-error markers can be included after a pre-processing step by mixed models [1, 3, 9, 10, 11]. In multivariate settings, the Cox model considered for a unique longitudinal marker has been replaced by more advance techniques from statistical learning adapted to survival [10, 11]. These techniques account for the possibly large dimensionality of the predictors and their correlation.

The landmark approach provides a relatively simple framework to predict a clinical endpoint given longitudinal information, and was shown to be robust to the misspecification of the marker trajectory or of the proportional assumption in the Cox model [8]. This makes it an appealing approach for extending the concept of individual dynamic prediction from a unique longitudinal marker to predictions from multivariate longitudinal markers. However, because it only relies on subjects at risk at the landmark time and exploits only the longitudinal information up to the landmark time, this approach suffers from a lack of efficiency, and is restricted to pre-determined prediction times.

When longitudinal and survival processes are inter-related as assumed in the dynamic prediction context, the joint modelling framework constitutes the most appropriate approach to handle this mutual dependence [4]. Joint models simultaneously model the longitudinal and survival processes over time while accounting for their association using shared latent quantities. Thus, the conditional individual probability of event given the history of the longitudinal endogenous predictors can be easily deduced. Initially developed for a single longitudinal predictor [1, 6], the method was then extended to a few longitudinal predictors [12, 13, 14]. In contrast with landmark approaches, joint models exploit all the available longitudinal information to build the prediction tool, thus leading to a better efficiency and application for all prediction times. However, the performances of these models are very sensitive to the correct specification of the model [8]. Moreover, due to the complexity of their estimation, these models are currently limited to the analysis of a small number of longitudinal markers (usually 2 or 3) and thus cannot be used to predict individual risk of event in more complex settings [15].

In the context of a large to high number of longitudinal predictors, regression calibration techniques were proposed as an alternative to joint models. Regression calibration is a 2-stage approach which first summarizes the longitudinal predictors into time-fixed features as in the landmark approach, and then includes the features into prediction models. Several regression calibration methods have been proposed with as the first step, using mixed models or functional data analysis [16] to summarize the multiple longitudinal predictors. Then, as the second step, using cox model [17], penalized regression [18] or random survival forests [19, 20] to derive the risk prediction. Although regression calibration techniques include all the available information on the markers and survival during the entire follow-up to build the prediction tool as in joint models, they neglect the informative truncation of the longitudinal data due to the event which may bias the estimates and impact the prediction tool accuracy [21].

In this work, we propose a novel methodology based on random survival forests (RSF) [22] to accurately predict a risk of event from possibly large-dimensional longitudinal predictors. RSF have become popular for prediction tasks as they can handle a high number of covariates and capture potentially complex associations with the event. However, RSF have been limited so far to time-independent predictors. To extend RSF to intermittently measured and error-prone longitudinal predictors, we use the same idea of pre-processing as in the landmark and regression calibration techniques. However, we directly incorporate this processing at each recursive step of the RSF tree building to better handle the informative truncation of the longitudinal endogenous data and thus provide more appropriate and accurate individual predictions.

The rest of this article is organized as follows. Section 2 introduces our random survival forest methodology, called **DynForest**, and describe how it can handle time-dependent endogenous predictors to predict competing risks of event. Section 3 reports the results of an extensive simulation study which aimed at validating **DynForest** methodology and at contrasting its performances with those of alternative approaches, namely the classical joint model when considering two longitudinal predictors and regression calibration RSF when considering more longitudinal covariates. In section 4, **DynForest** is applied to predict the probability of experiencing a dementia before death in a large population-based French cohort from multiple markers stemming from neuropsychological evaluation, clinical evaluation and brain Magnetic Resonance Imaging (MRI). Finally, section 5 closes the work with a discussion.

2 Methods

2.1 Framework and notations

We consider a population of N subjects. For each individual $i \in \{1, \dots, N\}$, we denote T_i the event time, C_i the independent censoring time, and $\tilde{T}_i = \min(T_i, C_i)$ the observed time of event. We define δ_i the indicator of the cause of event with $\delta_i = k$ if subject experiences the event of cause $k \in \{1, \dots, K\}$ before censoring and $\delta_i = 0$ otherwise. We observe an ensemble \mathcal{M}_x of P time-independent covariates X_{ip} ($p = 1, \dots, P$), and an ensemble \mathcal{M}_y of Q time-dependent covariates Y_{ijm} for $m = 1, \dots, Q$ measured at subject-and-covariate-specific times t_{ijm} with $j = 1 \dots n_{im}$ the occasion and $t_{ijm} \leq \tilde{T}_i$.

Our methodology consists of a random survival forest for competing causes of event (RSF) that incorporates an internal processing for handling time-dependent covariates. A RSF is an ensemble of B survival decision trees that are ultimately aggregated together. Each single tree $b \in \{1, \dots, B\}$ is built from a bootstrap sample of the original sample of N subjects. This results, on average, in the exclusion of 37% of the subjects that constitute the out-of-bag (OOB) sample, noted OOB^b for tree b ($b = 1, \dots, B$).

2.2 The tree building

A tree is a recursive procedure designed to partition the subjects into groups that are homogeneous regarding the outcome of interest. The overall tree building procedure is summarized in Figure 1. Each tree recursively splits the bootstrap sample into two subgroups at junctions called nodes until the subgroups reach a minimal size. At each node $d \in \mathcal{D}$, the split is determined according to a dichotomized feature that maximizes the distance between the two groups; the distance definition depends on the nature of the outcome and is further detailed in section 2.2.2 for the competing risk setting. To improve accuracy and minimize the correlation between the trees, randomness is incorporated at each node d by considering only a random subset of candidate covariates $\mathcal{M}^{(d)} = \{\mathcal{M}_x^{(d)}, \mathcal{M}_y^{(d)}\} \subset \{\mathcal{M}_x, \mathcal{M}_y\}$ which size is a tuning parameter, and also called *mtry*.

2.2.1 Internal processing for time-dependent covariates

For all the time-dependent covariates, a node-specific pre-processing is achieved to summarize the covariate dynamics into a set of time-independent features to be included in the pool of candidates for the splitting (see Figure 1B). At each node d , the trajectory of time-dependent covariate $Y_m \in \mathcal{M}_y^{(d)}$ is modeled using a flexible mixed model [23] as:

$$Y_{ijm} = X_{im}^\top(t_{ijm})\beta_l^{(d)} + Z_{im}^\top(t_{ijm})b_{im}^{(d)} + \epsilon_{ijm}^{(d)} \quad (1)$$

where Y_{ijm} is the covariate value for subject i at time t_{ijm} , $X_{im}^\top(t_{ijm})$ and $Z_{il}^\top(t_{ijm})$ are the p_m - and q_m -vectors associated with the fixed effects $\beta_m^{(d)}$ and random effects $b_{im}^{(d)}$ (with $b_{im}^{(d)} \sim \mathcal{N}(0, B_m^{(d)})$), respectively. $\epsilon_{ijm}^{(d)}$ denotes the error measurement with $\epsilon_{ijm}^{(d)} \sim \mathcal{N}(0, \sigma_m^2)^{(d)}$.

We present the method for continuous Gaussian time-dependent covariates only. However, the pre-processing procedure could be easily adapted to other types of time-dependent covariates by replacing the linear mixed model in (1) by a generalized linear mixed model.

Any specification can be considered for $X_{im}^\top(t_{ijm})$ and $Z_{il}^\top(t_{ijm})$. To allow for a flexible modeling of the trajectory over time, we consider a basis of natural cubic splines with knots to be determined in input. Although the specification of the model is similar for each node, the maximum likelihood estimation of the parameters is performed at each node on the subset of subjects present at the node (i.e., $\forall i \in \mathcal{N}^{(d)}$). When the covariate had already been selected at a parent node, estimated parameters from the closest parent node are considered as initial values to drastically reduce the number of iterations during the likelihood maximization and speed-up the procedure.

Time-independent features are then derived as the predicted individual deviations to the mean trajectory:

$$\hat{b}_{im}^{(d)} = \hat{B}_m^{(d)} Z_{im}^\top \hat{V}_{im}^{-1(d)} (Y_{im} - X_{im} \hat{\beta}_m^{(d)}) \quad (2)$$

where X_{im} and Z_{im} are the matrices with j -row vectors $X_{im}^\top(t_{ijm})$ and $Z_{il}^\top(t_{ijm})$ (with $j = 1, \dots, n_{im}$), $\hat{V}_{im}^{(d)} = Z_{im} \hat{B}_m^{(d)} Z_{im}^\top + \hat{\sigma}_{em}^{(d)} I_{n_i}$, I_{n_i} the $n_i \times n_i$ identity matrix and the hat denotes the Maximum Likelihood Estimates.

At this stage, the ensemble of candidate features for the time-dependent covariates becomes

$\mathcal{M}_{y\star}^{(d)} = \{\widehat{b}_{im}^{(d)} \mid \forall m : Y_m \in \mathcal{M}_y^{(d)}\}$ and the total ensemble of candidate features $\mathcal{M}_{\star}^{(d)} = \{\mathcal{M}_x^{(d)}, \mathcal{M}_{y\star}^{(d)}\}$ is now only composed of time-independent features.

2.2.2 Splitting rule

At each node $d \in \mathcal{D}$, the subjects are to be split into the two daughter nodes that are the most different possible according to the outcome (Figure 1D). With survival outcome, the difference was previously quantified according to the log-rank statistic [24]. In the presence of competing risks, we propose to use instead the Fine & Gray test statistic [25] which directly quantifies the difference in terms of the probability of the cause of event of interest.

The splitting procedure requires that each feature $W \in \mathcal{M}_{\star}^{(d)}$ be dichotomized. For a continuous predictor, this is achieved by considering a dichotomization according to a threshold c : $w_i > c$ or $w_i \leq c$. In our work, we used each decile of W as a candidate threshold c . Alternatively c could be chosen according values randomly drawn from W . For a non-continuous predictor, the dichotomization can be achieved as $w_i \in c$ or $w_i \notin c$ with c each possible subset of modalities of W .

The Fine & Gray test statistic is computed for all potential dichotomized features (defined by couple $\{W, c\}$), and the dichotomized feature (couple $\{W_0^d, c_0^d\}$) that maximizes the test statistic is selected to create the left and right daughter nodes. The left and right nodes are then denoted $2d$ and $2d + 1$, respectively.

2.2.3 Stopping criteria

Criteria need to be established to end the recursive procedure of a tree construction. We distinguish two criteria to pursue with the splitting of a node:

- A minimum number of events called *minsplit*;
- A minimum number of subjects in each of the daughter nodes called *nodesize*.

These two parameters control the depth of the trees. They should be carefully determined as a tradeoff between the performances of the random forest (with the deeper the trees, the lower the error of prediction) and the computational time. In our examples, we often used *nodesize* = 3 and

$minsplit = 5$. When a stopping criterion is reached, the node is considered as a terminal node or leaf $h \in \mathcal{H}$.

2.2.4 Leaf summary

The subjects classified in the same leaf are supposed to be homogeneous in terms of their probability of event of interest. Each leaf h^b of tree b is thus summarized by the cumulative incidence function (CIF) for cause k ($k = 1, \dots, K$):

$$\pi_k^{h^b}(t) = P(T_i < t, \delta_i = k \mid i \in h^b), \forall t \in \mathbb{R}^+ \quad (3)$$

An estimate $\widehat{\pi}_k^{h^b}(t)$ of the CIF $\pi_k^{h^b}(t)$ is given by the Aalen-Johansen estimator [26].

2.3 Individual prediction of the outcome

2.3.1 Out-of-bag individual prediction

Let us consider an individual \star with the P -vector of time-independent covariates X_\star and the ensemble of time-dependent covariate observations $\mathcal{Y}_\star = \{Y_{\star jm}, m = 1, \dots, Q, j = 1 \dots n_{\star m}\}$. The individual-specific CIF for individual \star in any tree b is given by:

$$\begin{aligned} \pi_{\star k}^b(t) &= P(T_\star < t, \delta_\star = k \mid \mathcal{Y}_\star, X_\star, b) \\ &= P(T_\star < t, \delta_\star = k \mid \star \in h_\star^b) \\ &= \pi_k^{h_\star^b}(t) \end{aligned} \quad (4)$$

where h_\star^b is the leaf in which individual \star ends when dropping into tree b . Specifically, at each node d , subject \star is recursively assigned to the left or right node according to whether $w_\star > c_0^d$ or $w_\star \leq c_0^d$. In the case where W_0^d is a predicted random-effect from time-dependent covariate m , the random-effect prediction for individual \star , $\widehat{b}_{\star m}^{(d)}$, is computed using formula (2) with the estimated parameters obtained at this specific node d .

An ensemble estimate of the individual CIF $\widehat{\pi}_{\star k}(t)$ for cause k can finally be defined by aggregating the tree-specific individual predictions $\widehat{\pi}_{\star k}^b(t) = \widehat{\pi}_k^{h_\star^b}(t)$ over all the trees $\mathcal{O}_\star \subset \{1, \dots, B\}$ for

which \star is *OOB*, as:

$$\widehat{\pi_{\star k}}(t) = \frac{1}{|\mathcal{O}_\star|} \sum_{b \in \mathcal{O}_\star} \widehat{\pi_k^{h_\star^b}}(t) \quad (5)$$

where $|\mathcal{O}_\star|$ denotes the length of \mathcal{O}_\star and $\widehat{\pi_k^{h_\star^b}}(t)$ is the Aalen-Johansen estimator in leaf h_\star^b of the b -th tree.

2.3.2 Individual dynamic prediction from a landmark time

The methodology described in subsection 2.3.1 for an out-of-bag individual can be used to provide the individual dynamic prediction of the outcome of cause k from the information collected up to a landmark time s . Let consider a new subject \star still at risk of the event at time s . The covariate information available at the time of prediction is the P -vector of time independent covariates X_\star and the history of time-dependent covariates observations up to time s $\mathcal{Y}_\star(s) = \{Y_{\star jm}, m = 1, \dots, Q, j = 1 \dots n_{\star m}, t_{\star jm} < s\}$. The probability of experiencing cause k of event at a horizon time w is then defined as:

$$\begin{aligned} \pi_{\star k}(s, w) &= P(s < T_\star \leq s + w, \delta_\star = k | T_\star > s, \mathcal{Y}_\star(s), X_\star) \\ &= \frac{\pi_{\star k}(s + w) - \pi_{\star k}(s)}{1 - \sum_{l=1}^K \pi_{\star l}(s)} \end{aligned} \quad (6)$$

where each $\pi_{\star k}(t)$ (for $k = 1, \dots, K$) can be estimated using equation (5) with the history of the time-dependent covariates $\mathcal{Y}_\star(s)$ up to the landmark time s only, and $\mathcal{O}_\star = \{1, \dots, B\}$.

2.4 Error of prediction

The error of prediction can be used in RSF with two objectives:

- tuning the hyper-parameters of the RSF (*mtry*, *minsplit* and *nodesize*) to achieve an optimal RSF. This is done by minimizing the OOB error of prediction.
- assessing the predictive performances of the optimal RSF. This is achieved by computing the error of prediction for an external validation sample, that is a sample where subjects are OOB for all the trees.

In this work, we considered mainly the Brier Score measure [27], and its integrated version (IBS) between two time points τ_1 and τ_2 to assess the error of prediction.

2.4.1 IBS for optimizing the RSF

For the optimization of the RSF, the IBS estimator is given by $\widehat{IBS}(\tau_1; \tau_2) = \int_{\tau_1}^{\tau_2} \widehat{BS}(t) dt$ with the Brier Score estimated by:

$$\widehat{BS}(t) = \frac{1}{N} \sum_{i=1}^N \widehat{\omega}_i(t) \left\{ I(\tilde{T}_i \leq t, \delta_i = k) - \widehat{\pi}_{ik}(t) \right\}^2 \quad (7)$$

where $\widehat{\pi}_{ik}(t)$ is the estimated probability of event of cause k given Y_i and X_i defined in (5), and $\widehat{\omega}_i(t)$ are Inverse Probability of Censoring Weights (IPCW) that account for the censoring between τ_1 and τ_2 [28]. We used in this work the Kaplan-Meier estimator to compute the probability of censoring in IPCW.

By default, (τ_1, τ_2) corresponds to the span of the time to event data.

2.4.2 External assessment of RSF predictive performances

For the external evaluation of the RSF performances, the IBS computation slightly differs. First, it is now computed on an external sample of size N^* , and the information considered is now the information up to the prediction time s , with $s \leq \tau_1$, so that $\widehat{IBS}^s(\tau_1; \tau_2) = \int_{\tau_1}^{\tau_2} \widehat{BS}^s(t) dt$ with:

$$\widehat{BS}^s(t) = \frac{1}{N^*} \sum_{\star=1}^{N^*} \widehat{\omega}_{\star}^s(t) \left\{ I(\tilde{T}_{\star} \leq t, \delta_i = k) - \widehat{\pi}_{\star k}(s, t - s) \right\}^2 \quad (8)$$

where $\widehat{\pi}_{\star k}(s, t - s)$ is the estimated probability of event of cause k between s and t given the information on Y_{\star} and X_{\star} up to s (see definition in (6)), and $\widehat{\omega}_{\star}^s(t) = \widehat{\omega}_{\star}(t) I(\tilde{T}_{\star} > s)$.

This external validation step can be incorporated into a k-fold cross-validation strategy. This is what was done in the application in the absence of an actual external dataset, and repeated 50 times to account for the k-fold cross-validation variability.

2.5 Importance of the predictors

Beyond the overall predictive performance of the approach, one can be interested in the identifying which predictors are the most predictive. We propose to evaluate the association between event and predictors through two measures: the variable importance and the minimal depth.

2.5.1 Variable importance

The variable importance (VIMP) measures the variable prediction ability by computing the increase in OOB error obtained after breaking the link between a given variable and the event. More precisely, for each covariate p (time-fixed or time-dependent), the link between variable p and the event is broken by permuting the values of variable p at the individual level when p is time-fixed and at the observation level when p is time-dependent. Then, the mean over the trees of the OOB errors ($\widehat{IBS}_b(\tau_1, \tau_2)$ for $b = 1, \dots, B$) is compared to the mean over the trees of OOB errors obtained after permuting the values of covariate p ($\widehat{IBS}_b(\tau_1, \tau_2)^{(p)}$ for $b = 1, \dots, B$). The VIMP statistic for covariate p , called $VIMP^{(p)}$, is given by:

$$VIMP^{(p)}(\tau_1, \tau_2) = \frac{1}{B} \sum_{b=1}^B \widehat{IBS}_b(\tau_1, \tau_2)^{(p)} - \frac{1}{B} \sum_{b=1}^B \widehat{IBS}_b(\tau_1, \tau_2) \quad (9)$$

where $\widehat{IBS}_b(\tau_1, \tau_2)^{(p)}$ and $\widehat{IBS}_b(\tau_1, \tau_2)$ are defined similarly as the IBS by computing the Brier Score (in equation (7)) only on b -tree OOB subjects and using the estimate of b -tree individual prediction $\widehat{\pi}_k^{h_k^b}(t)$ defined under equation (5).

Large VIMP value indicates a loss of predictive ability when removing covariate p whereas null VIMP value indicates no predictive ability. Due to the permutation procedure, negative VIMP may be obtained. They are interpreted as null VIMP.

2.5.2 Variable group importance

Because of the potential correlation between variables, the VIMP computed at the variable level may not always indicate the correct variable-specific predictive ability. To assess the predictive ability of correlated variables, Gregorutti *et al.* [29] proposed the grouped variable importance (gVIMP) statistic in standard RF. It consists in simultaneously noising-up all the variables of a given group. We considered the same methodology for our RSF. The overall gVIMP statistic for group $g \in \{1, \dots, G\}$ is defined as $gVIMP^{(g)} = \frac{1}{B} \sum_{b=1}^B \widehat{IBS}_b^{(g)} - \frac{1}{B} \sum_{b=1}^B \widehat{IBS}_b$ where $\widehat{IBS}_g^{(g)}$ denotes the OOB error obtained when noising-up all the variables from group g .

2.5.3 Average minimal depth

The minimal depth of a variable in a tree corresponds to the distance between the root node and the first node that used the variable for splitting the data. The minimal depth can be averaged across all the trees allowing to rank the predictors. Indeed, during the tree building, the most predictive variables are expected to be chosen for the first splits so the closer the average minimal depth from 1, the better the predictive ability of the variable. When only a random subset of variables are considered at each node ($mtry < P + Q$), the interpretation of the minimal depth may be blurred. We thus recommend to compute this statistic only for the maximal $mtry = P + Q$. Moreover, because the depth of the trees may vary and some predictors may not be systematically used in the tree building process, we recommend to report the number of trees where the predictor was selected along with the average minimal depth. Note that, compared to the VIMP, the minimal depth can be computed at both the summary feature and the covariate level allowing to fully understand the tree building process.

3 Simulation study

We carried out a simulation study to illustrate the behaviour of **DynForest** in comparison with alternative methods under two scenarios:

- repeated data of two longitudinal predictors possibly in association with a clinical event. We compared the performances of **DynForest** with a joint model estimated using **JMBayes** R package [13]. For **JMBayes**, we considered the same specification for the linear mixed models as in **DynForest** and modelled the association with the event with a proportional hazard model (baseline risk function approximated by 4 cubic splines) that included the current levels and current slopes of the two predictors as covariates.
- repeated data of 20 longitudinal predictors possibly in association with a clinical event. In this case, we could not compare with a joint modelling approach anymore. Instead, we compared **DynForest** with a regression calibration technique in which the exact same specification for the linear mixed models and the exact same strategy for the RSF were considered. The difference in the regression calibration was that the linear mixed models were estimated once

and for all prior to inclusion in the RSF.

For both scenarios, we additionally included two time-fixed predictors unrelated to the event. Finally, we compared the predictive performance of the techniques in predicting the clinical event occurrence at two horizon times $w = 1, 2$ from two landmark times $s = 2, 4$. We measured the performance with both the Brier Score (defined in section 2.4.1) and the Area Under the ROC curve (AUC) with estimators adapted to survival data and dynamic prediction [27].

3.1 Design

For both scenarios, $R = 250$ samples of $N = 500$ individuals were built for the learning step and a single external validation sample of $N = 500$ individuals was generated for evaluating the predictive performance. The generation procedure is detailed in the simulation section and Tables S1/S2 in supplementary material and summarized below. Individual trajectories are also displayed in figure S1 in supplementary material.

For each subject, we generated two time-fixed covariates (one continuous according to a standard Gaussian distribution and one binary according to a Bernoulli with probability 0.5). We also generated repeated data of 2 or 20 continuous time-dependent predictors, for small and large dimension scenarios, respectively. Times of measurement were at baseline and then randomly drawn (using an exponential departure) around theoretical annual visits up to 10 years. Each marker trajectory followed a latent class linear mixed model with 4 classes and either class-specific linear individual trajectories or class-specific nonlinear individual trajectories. The risk of event was then generated using a proportional hazard model with a Weibull baseline hazard with shape and scale parameters equals to 0.1 and 2, respectively. Linear predictor in the survival model was generated using functions of the predictors. More precisely, we included as linear predictor either the random-effects from multiple predictors or the latent class membership. Time-fixed covariates are not included as linear predictor in any scenario. For both scenarios, we considered several sub-scenarios according to the form of the dependence function between the predictors and the risk of event: (i) non-linear using random-effects and two-by-two interactions between random-effects; (ii) non-linear using latent class membership.

3.2 Results

3.2.1 Small dimension scenario

Predictive performances on the external dataset are reported in terms of BS and AUC in Figure 2 for the non-linear dependency assumption. For **DynForest**, we fixed $nodesize = 3$ and $minsplit = 5$ whereas we chose to report the results with each possible value of $mtry$ to underline the importance of this tuning parameter. As expected, the results varied substantially according its value. The best performances in terms of BS (minimal BS) was systematically obtained with the largest $mtry$, that is 4 (2 time-dependent and 2 time-fixed predictors), and the worse with $mtry = 1$. For the AUC, the differences were less visible. In comparison with the joint model estimated with **JMbayes**, **DynForest** showed overall better predictive abilities, in particular in terms of Brier Score. Again, conclusions were more tempered when considering AUC. It should be noted that the joint model in this simulation was misspecified in terms of both the individual deviation from the mean trajectory (since simulated using latent classes), and of dependence association since it has been generated as a non-linear function. The objective here was to illustrate that even in small dimension scenarios, **DynForest** could already be of interest and constituted a competing alternative for individual dynamic prediction purpose.

3.2.2 Large dimension scenario

In the large dimension scenario, we report in Figure 3 the predictive performances on the external dataset of **DynForest** and its regression calibration counterpart (or 2-stage counterpart) for scenario assuming non-linear dependency. For both techniques, we fixed $nodesize = 3$ and $minsplit = 5$ whereas $mtry$ parameter was tuned. Regarding the range of possible values of $mtry$ (from 1 to 22 for **DynForest** and from 1 to 62 for regression calibration method), tuning this parameter on each dataset was too computationally intensive. Thus, we decided to tune this parameter using an unique dataset, and used the optimal value for all replications. With non-linear association using random-effect with interactions, we found as optimal value $mtry = 9$ and $mtry = 46$ for **DynForest** and regression calibration, respectively, and $mtry = 5$ and $mtry = 6$ in non-linear association using latent class membership. **DynForest** outperformed the regression calibration technique for both BS and AUC with non-linear association using latent class membership (Figure 3B). Under non-

linear association using random-effect with interactions, the results are still slightly in favor of **DynForest**. This underlines the substantial impact of not including the time-dependent predictor modeling step within the survival tool construction to correctly account for the correlation between the longitudinal and survival processes.

4 Application

The objective of the application was to predict the individual probability of dementia occurrence in the presence of competing risk of death by leveraging the history of repeated data on clinical exam, neuropsychological battery and brain Magnetic Resonance Imaging (MRI) exam. A secondary objective was to identify the value of each type of predictor for predicting dementia. We relied for this on the Three-city (3C) cohort study [30].

4.1 The 3C study

The 3C study is a French prospective population-based cohort study which enrolled individuals aged 65 years and older from electoral rolls in three French cities. Extensive follow-up interviews were conducted at baseline and then 2, 4, 7, 10, 12, 14 and 17 years after the enrollment including an extensive clinical and neuropsychological exam done in-person at home by a trained psychologist. At 1, 4 and 10 years, a subsample underwent an additional MRI exam. The diagnosis of dementia relied on a 2-step procedure with suspected cases of dementia reviewed and validated by an independent expert committee of neurologists and geriatricians. Deaths were continuously recorded but were considered as a competing event for dementia only in the 3 years after a negative diagnosis. Our analytical sample included all the individuals free of dementia at baseline and with at least 1 measure at each of the 29 predictors under study during the follow-up in Bordeaux and Dijon cities. This led to a sample of $N = 2140$ subjects (with 10766 observations) among which 234 were diagnosed with an incident dementia and 311 died before any dementia (see cumulative incidences displayed in Figure S5 in supplementary material).

We considered a total of 24 time-dependent and 5 time-fixed predictors structured into 9 groups: Cognition (4 time-dependent cognitive tests), Functional dependency (1 time-dependent scale of instrumental activities of daily living), Neurodegeneration (8 time-dependent brain MRI markers

including regional volumes and global measures), Vascular brain lesions (6 time-dependent markers of white matter hyperintensities), depressive symptomatology (1 time-dependent scale of depressive symptomatology), Cardio-metabolic factors (3 time-dependent markers with body mass index, diastolic and systolic blood pressure, and 1 time-fixed with diabetes status at baseline), medication (time-dependent number of medication), socio-demographic (time-fixed age at baseline, education, gender), genetic (time-fixed APOE e4 allele carrier status). Complete information on the predictors are provided in Table S3 to S8 in supplementary material. For longitudinal predictors, individual trajectories are displayed in Figures S2, S3 and S4 in supplementary material.

4.2 DynForest specification

The probability of dementia was predicted according to time in the study. MRI data were collected 1.7 times on average resulting to a simpler modeling using quadratic and linear trajectories at the population and the individual level, respectively. Others time-dependent predictors were measured 5.1 times on average. Their trajectory according to time in the study were modeled using natural splines with one internal knot both at the population and individual level. To satisfy the normality assumption of the linear mixed model, all time-dependent predictors were previously normalized using splines transformations [31].

In the absence of an external dataset available with the same longitudinal predictors and the same target population, predictive abilities were assessed using a 10-fold cross-validation procedure to avoid over-fitting. For each of the 10 folds, the random survival forest was trained on the sample that excluded the fold (learning step on 90%) and individual probabilities of dementia were computed on the fold (prediction step on the remaining 10%). The cross-validation procedure was repeated $R = 50$ times to evaluate the variability of the results.

During the learning step, we systematically fixed parameters $minsplit = 5$ and $nodesize = 3$ to favor deep trees. Parameter $mtry$ was tuned within the range of possible value from 1 to 29 (i.e. number of predictors) to minimize the OOB IBS. On the total sample, we first observed that the OOB IBS decreased rapidly with increasing $mtry$ until a stabilization around $mtry = 15$ (see Figure S6 in additional file). So for each fold, we ran **DynForest** twice with $mtry = 15$ and $mtry = 20$ and selected the optimal $mtry$ according to the OOB IBS. For prediction step, individual probabilities of dementia were computed for the remaining fold according to the methodology detailed in section

2.3.2). We considered two landmark times $s = 5, 10$, resulting in 1727 and 1150 individuals still at risk of dementia, respectively. We focused on the individual probability of dementia between s and $s + w$ with horizon times $w = 3, 5$. The predictive performances were assessed through the AUC and the time-dependent BS.

4.3 Results

Cross-validated predictive performances of the random survival forest are reported in Figure 4. The AUC varied from 0.78 to 0.80 and BS from 0.048 to 0.086 depending on the landmark time and the horizon.

To better understand the value of each predictor, we report the VIMP statistics in Figure 5A, and the minimal depth in supplementary Figure S7. To reduce the variability due to the permutation procedure, the VIMP statistics were computed 10 times and averaged across the replications. IADL (functional dependency) was the most important marker for predicting dementia with a mean gain in IBS of 4.5%. Followed neuro-degeneration markers with the right hippocampus and lobe medio-temporal volumes (gains of 4.2% and 3.1%, respectively), cognitive tests with the Isaacs Set Test and Benton test (with gains of 3.4% and 2.6%, respectively) and body-mass index with a mean gain of 1.8%. Since the VIMP may not correctly translate the importance of variables that are correlated, we also reported in Figure 5B the gVIMP statistics grouped by dimensions. The 8 neuro-degeneration predictors reached a mean gain of 10.3% of IBS, and the 4 cognitive tests a mean gain of 9.2%. The 6 markers of vascular brain lesions followed the functional dependency unique marker with a mean gain of 3.6% in the IBS.

5 Discussion

In this paper, we developed an original methodology, called **DynForest**, to compute individual dynamic predictions by using multiple longitudinal predictors. **DynForest** extends the random survival forests for competing risks limited to time-fixed predictors to the inclusion of endogenous longitudinal predictors. This is achieved by including in the tree building a node-specific internal processing to translate the longitudinal predictors into time-fixed features. **DynForest** can be used to compute individual dynamic predictions of events, but it can also quantify the importance of the

longitudinal predictors using VIMP and grouped-VIMP statistics adapted to longitudinal data.

Through a simulation study, we first showed in a small dimensional context that **DynForest** could be a relevant alternative to the joint models that constitute the reference technique [8, 32]. Indeed, in contrast with joint models, **DynForest** does not need to pre-specify the association structure with the event, and may account for nonlinear associations and interactions. In the second scenario, we considered a larger dimensional context, with 20 longitudinal markers, for which joint models could not be estimated anymore. In the literature, regression calibration techniques were proposed instead. They consist in first deriving time-fixed features from the longitudinal markers and then running random survival forests [17, 19, 20], thus ignoring the informative dropout induced by the event [21]. We showed in this larger dimensional scenario that **DynForest** outperformed a regression calibration alternative. Indeed, in contrast with regression calibration technique, **DynForest** accounts for the truncation of the repeated data due to the event by re-estimating the mixed models at each node on the node-specific subsample. Since these subsamples become more and more homogeneous regarding the event, the missing at random assumption of the mixed models becomes more and more valid.

Compared with the other methodologies adapted to the large dimensional and longitudinal context, our methodology has the assets of (i) using all available information when landmark approaches [10, 11] only include subjects still at risk at landmark time, resulting in a lack of efficiency [8]; (ii) simultaneously analyzing the longitudinal and time-to-event processes when the other methods based on 2-step regression calibration [17, 19, 20] neglect the association leading to a potential bias in the prediction; (iii) allowing for complex and nonlinear association structures between the predictors and the event; (iv) allowing the analysis of potentially high dimensional data (i.e. hundreds/thousands of predictors). Indeed, the longitudinal markers are independently modeled multiple times for each node through each decision tree of the forest, and therefore could be easily applied no matter the number of longitudinal markers. Finally, we introduced two stopping criteria defining the minimum number of events and of subjects required to proceed to a subsequent split. This allows some leaves to have an homogeneous group with no events. In the literature, the stopping rule was based on a minimal number of events in the leaves [22] possibly leading to non-optimal splitting.

Our methodology has also drawbacks. First, although the methodology may be applied what-

ever the number of predictors, the computation time may become enormous in high dimensional settings. Indeed, mixed models are to be estimated at each node of each tree. By using the estimates previously obtained as initial values, we managed to fasten the estimation. But this may remain computationally intensive with a large number of candidates *mtry*. Second, we focused on continuous longitudinal markers only. However, the method could be easily extended to other natures of repeated markers (e.g. binary, categorical, counts) using generalized mixed models. Third, we considered linear mixed models for deriving time-fixed predictors. Functional principal components analysis [16] could be considered instead. We leave such development for future research. Finally, although we were able to provide the strength of the association between the predictors and the event using the VIMP and gVIMP statistics, these tools do not inform on the sign of the association.

6 Conclusion

Using the framework of the random survival forests combined with mixed models for internally processing longitudinal predictors, we tackled the challenge of predicting an event from a potential high number of longitudinal endogenous predictors. **DynForest** offers a innovative solution accompanied by a user-friendly R package.

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Figures

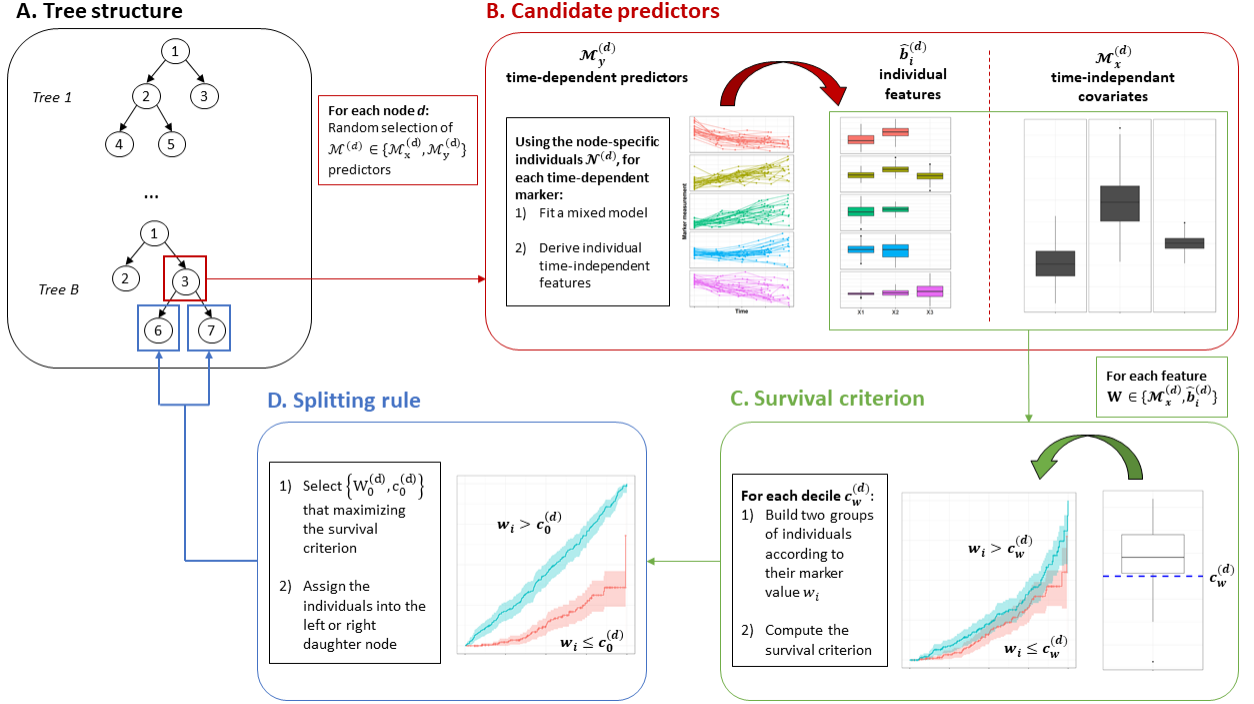


Figure 1: Overall scheme of the tree building in DynForest with (A) the tree structure, (B) the node-specific treatment of time-dependent predictors to obtain time-fixed features, (C) the dichotomization of the time-fixed features, (D) the splitting rule.

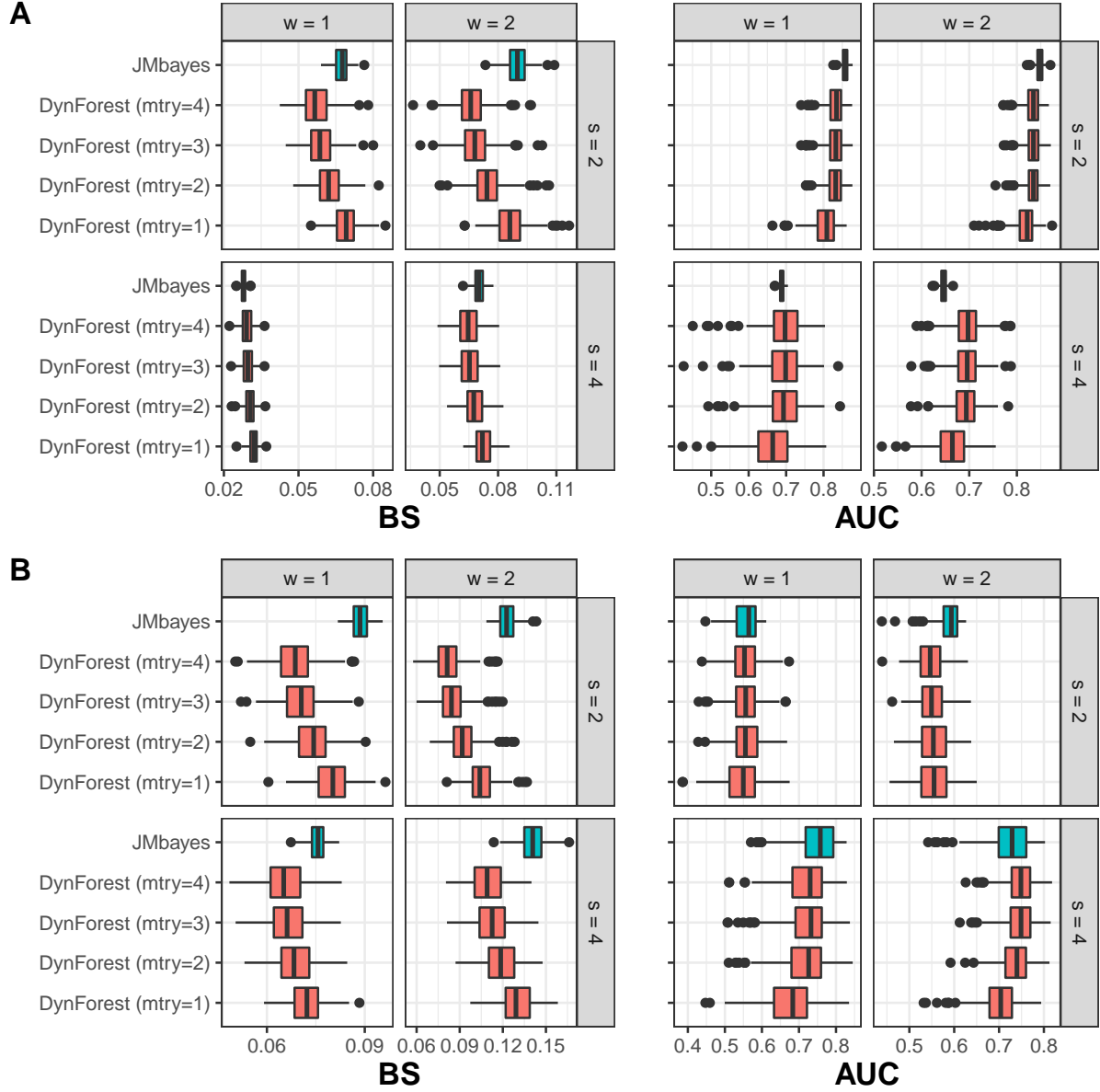


Figure 2: External predictive performances of **DynForest** and **JMbayer** in the small dimension scenario of simulations (2 predictors) for the 250 replications. Are reported the Brier Score (BS) and the Area Under the ROC Curve (AUC) at two landmark times $s = 2, 4$ and two horizons $w = 1, 2$. The generated joint model included non-linear association between the markers and the event, using random-effects with two-by-two interaction (A) or latent class membership (B). In these scenarios, **JMbayer** is considered as misspecified. For **DynForest**, we fixed $nodesize = 3$ and $minsplitted = 5$, and their results are reported for all mtry values to underline the importance of this tuning parameter.

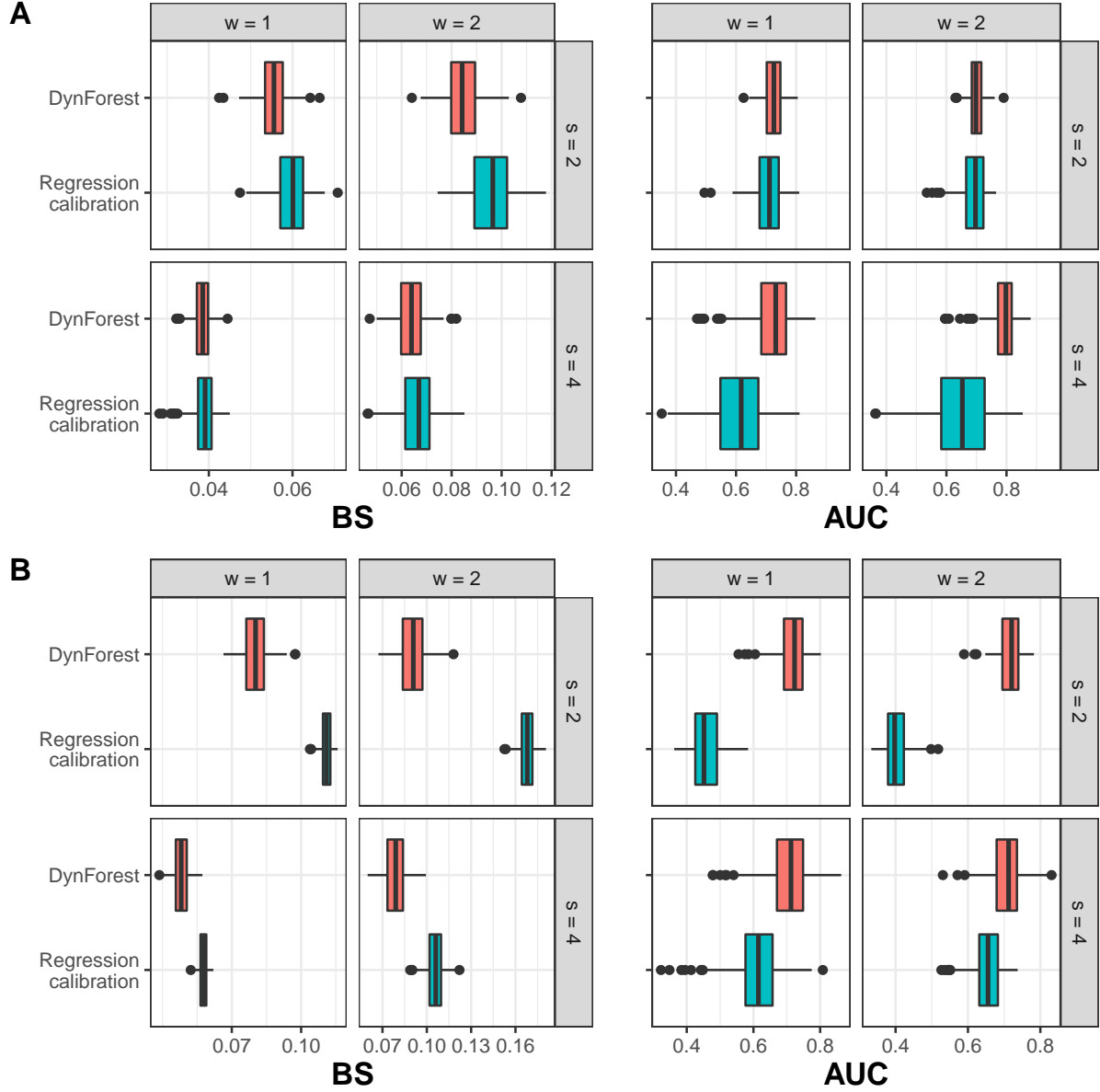


Figure 3: External predictive performances of **DynForest** and its regression calibration version in the large dimension scenario of simulations (20 predictors) for the 250 replications. Are reported the Brier Score (BS) and the Area Under the ROC Curve (AUC) at two landmark times $s = 2, 4$ and two horizons $w = 1, 2$. Non-linear association between the markers and the event was displayed using random-effects with two-by-two interactions (A) or latent class membership (B). The regression calibration version of **DynForest** consisted in summarizing the time-dependent markers into time-fixed features once for all prior to inclusion in the RSF. We fixed $nodesize = 3$ and $minsplit = 5$. $mtry$ parameter was also fixed for all replications after tuning process on an unique dataset.

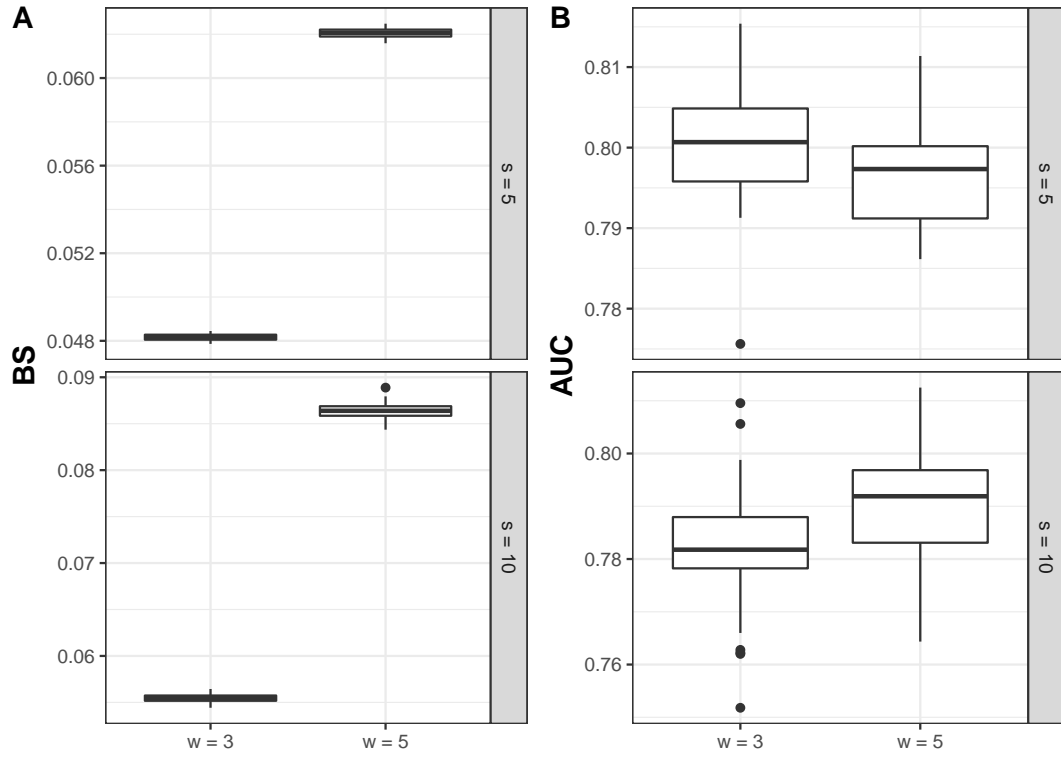


Figure 4: Predictive assessment of dementia at landmark times $s = 5, 10$ and horizon times $w = 3, 5$ using Brier Score (figure A) and Area Under the ROC Curve (figure B).

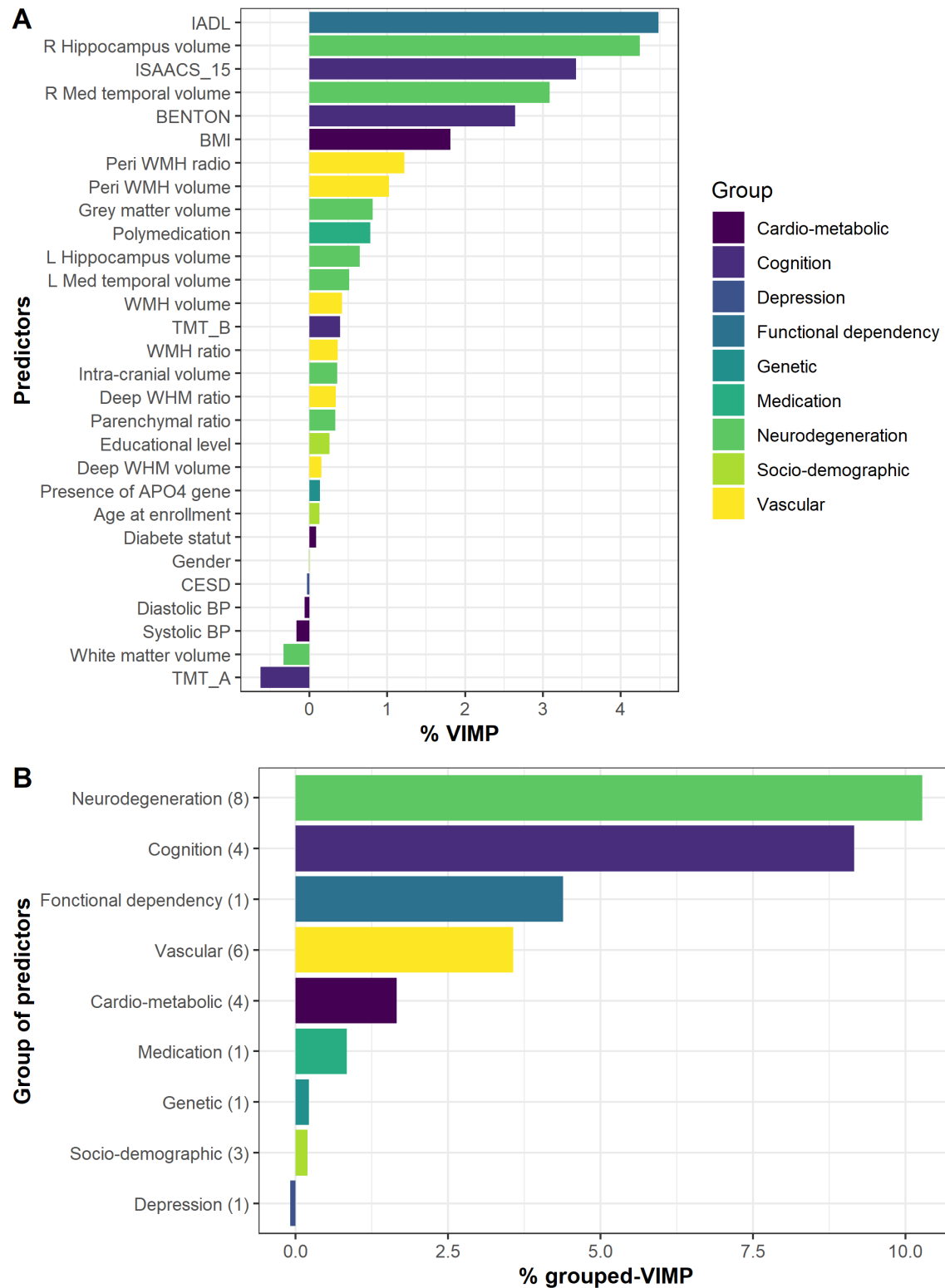


Figure 5: (A) Importance variable (VIMP) and (B) Grouped importance variable (gVIMP) averaged over 10 permutation procedures for each dementia predictor or group of dementia predictors.