

Intergranular corrosion in evolving media: Experiment and modeling by cellular automata

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1	Is there a memory effect of intergranular corrosion?
2	
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10	
11	Abstract
12	In this paper, we investigated the impact of the oxidizing character of the nitric medium on
13	the evolution of the intergranular corrosion of a 310L austenitic stainless steel. Corroded
14	surfaces were investigated by X-ray photoelectron spectroscopy. Optical observations were
15	made to characterize the dimensions of the grooves on samples cross sections. Modeling
16	and numerical simulations were carried out by using the cellular automata method. In two
17	different stationary oxidizing conditions ("severe" in presence of oxidizing ions and "soft"
18	without, respectively), we showed that the corroded surface of the steel reaches a different
19	steady state: the oxide is thicker, the intergranular grooves are thinner and the surface area
20	is larger with the oxidizing character of the nitric medium. Then we investigated the effect
21	of an alternative "severe then soft" corrosion sequence. We showed that the system re-
22	adapted to the soft conditions without memory effect from the previous severe ones.
23	Keywords
24	Austenitic stainless steel, Cellular automata modeling, Intergranular corrosion, Nitric
25	acid, XPS
26	Introduction
27	Grains boundaries in materials are often considered as a weakness regarding the chemical
28	attack by the environment. The preferential attack of these grains boundaries results in a
29	specific corrosion mode named intergranular corrosion (IGC). Challenges relative to
30	intergranular corrosion concern various materials such as nickel based alloys [1-3],
31	aluminum based alloys [4-6] or steels [7-9]. One specific issue is about IGC of non-
32	sensitized stainless steels (SSs) in nitric acid. This is mainly linked to the domain of the
33	spent nuclear fuel reprocessing, where SSs are used for containing nitric acid solutions at

various concentrations and temperatures [10-12]. IGC of non-sensitized SSs is induced by
a differential of reactivity between grains and grains boundaries. Therefore, grain
boundaries are preferentially dissolved compared to the grains themselves. Consequently,
grooves are formed along the grains boundaries, which progression in the SS generates a
periodic detachment of grains.

39 Over the last fifteen years, IGC of non-sensitized SSs has been investigated through both 40 experimental and modeling approaches. From the experimental point of view, different 41 techniques are used to characterize IGC. In addition to qualitative observations of the 42 surface, optical or scanning electron microscopy can be performed on the cross section of 43 the sample to geometrically characterize the intergranular grooves in 2D [13-23]. A 44 promising 3D characterization approach has also been attempted by μ -Xray-tomography 45 [24]. The measurement of the mass loss as the function of time gives also important 46 information regarding the kinetics of IGC [13, 15, 19-21, 25-32]. Sometimes, the chemical 47 characteristics of the surface are analyzed by X-ray photoelectron spectroscopy (XPS) [15, 48 28, 33, 34]. An attempt to characterize IGC with ultrasonic methods was proposed by 49 Jothilakshmi et al. [22]. In addition to this experimental information, different models were 50 recently proposed to simulate IGC of non-sensitized SSs in nitric acid. A simple analytical 51 approach was proposed for simulating the evolution of the mass loss [35]. A geometrical 52 approach in 2D was developed for simulating the evolution of the interface of the material 53 suffering IGC [21, 35]. More realistic models were also developed using the method of 54 cellular automata (CA) for simulating the geometrical evolution of the material in a 3D 55 realistic granular structure [18, 32, 36-38].

56 All these experimental and modeling approaches allowed studying the influence of 57 different metallurgical and chemical parameters on IGC. It appears that IGC could be 58 dependent on the surface exposed to corrosive medium regarding the rolling direction [19, 59 20, 29, 39], on the chemical composition of the SSs, which in turn influence the chemical 60 composition of the grains boundaries [13, 14, 18, 20, 28, 31, 33, 34, 40, 41], on the grains 61 size [30] and on the metallurgical treatment [25]. IGC of SSs was also studied in a pure nitric medium at different concentrations [28, 33] but also with the addition of different 62 63 oxidizing species at different levels [26, 27, 39, 41]. However, these parameters were only 64 correlated to the corrosion potential and corrosion kinetics, with no information on the 65 characteristics of the interface in terms of chemical composition and morphology. In this 66 paper, we intend to fill this gap by investigating IGC of a SS in two different nitric acid 67 media. We investigated the influence of the chemical medium nature on the elemental 68 composition of the oxide layer (analyzed by XPS) and the geometrical characteristics of 69 the interface. For this last one, as it was difficult to extract information from experiments, 70 we used CA modeling. Indeed, we showed that CA is able to reproduce accurately the 71 experimental behavior [23, 38].

Moreover, we also investigated cases where the corrosive environment evolves over time during a given experiment. The objective was to study how the IGC of a given SS sample may be influenced by the fact that this SS was previously corroded in a first medium. To our knowledge, this aspect has never been studied despite it may concern many industrial issues, for example: the case of equipments whose corrosive environment evolves with time or the case of the alternation of phases of rinsing (with one first chemical medium) and working (in a second chemical medium).

79

80

Experimental and modeling approaches

81 Experimental conditions and characterization methods

We performed corrosion tests (electrochemical measurements and immersion tests)
with an AISI 310L SS provided by Creusot Loire Industrie. This stainless steel has a low
carbon content and was annealed and quenched. The chemical composition is given in
Table 1. The mean grain size (84 μm) was determined using the normalized NF EN ISO
643:2003.

87

Table 1. Chemical Composition of AISI 310L SS (in wt.%).

-	Fe	С	Cr	Ni	Mn	Si	Р	S	Мо	Nb
-	bal.	0.006	24.32	21.13	1.03	0.13	0.016	0.001	0.08	0.115

88

For the corrosion tests, the corrosion medium was 8 mol.1⁻¹ nitric acid at boiling point 89 90 temperature (111 °C) containing or not 150/300 mg/L of vanadium(V) (introduced as 268/ 91 536 mg/L of V_2O_5). By introducing or not vanadium(V), we intended to impose different 92 oxidizing conditions to the material regarding the difference of standard potential in nitric 93 acid ($E^{\circ}(NO_3^{-}/HNO_2) = 0.934 \text{ mV/SHE}$ at 25 °C [42]) and in presence of vanadium(V), $(E^{\circ}(VO_2^+/VO^{2+}) = 1.004 \text{ V/SHE at } 25 \text{ °C } [42])$. For the rest of the paper, we name "soft" 94 95 conditions" the experiments without vanadium(V) and "severe conditions" the ones with additions of vanadium(V). 96

We performed electrochemical measurements (open circuit potential and linear voltammetry measurements) using a classical 3-electrodes configuration. The working and the counter electrodes were a 310L bullet shaped electrode (surface area 2 mm²) and a platinum basket, respectively. The reference electrode was a mercury/mercurous sulfate electrode (Hg/Hg₂SO₄ - MSE, E = +0.65 V/SHE at 25 °C). The electrochemical measurements were performed using a VSP workstation controlled by the software EC-Lab v.10.37 (Biologic).

105

106 The conditions and durations of the 3 immersion tests are given in Table 2. SS specimens were $30 \times 20 \times 1.5$ mm³ parallelepiped samples. They were ultrasonic degreased with an 107 ethanol/acetone mixture. They were pickled with an H₂O/HCl/HNO₃/HF mixture for 108 109 around 15 minutes in order to dissolve a thickness of about 20 µm. The experimental device 110 consists of a 1 L glass reactor where 3 specimens are suspended to test the reproducibility 111 of the corrosion process (the metallic surface area on the solution volume S/V ratio was 112 $0.4 \text{ dm}^2/\text{L}$). The specimens were periodically removed from the reactor, rinsed with 113 demineralized water and ethanol, dried with compressed air and weighted (AT 20 balance 114 model from Mettler-Toledo, precision 0.01 mg). The solution was renewed after each corrosion period. The mass loss as a function of time was expressed in terms of equivalent 115 116 thickness loss assuming a hypothetical homogeneous corrosion, as follows:

$$\Delta e = \Delta m / (\rho \times S) \times 10^4$$
 Equation 1

- 117 With Δe the equivalent thickness loss (in μm)
- 118 Δm the measured mean mass loss (in g)
- 119 ρ the SS density (8 g/cm³ approx.).
- 120 S the sample surface (13.5 cm^2)

121 Periodically, one of the samples was cut and the ross-section of the sample was optically

- 122 observed (GX51 microscope model from Olympus).
- 123

124 Table 2: Conditions of the immersion corrosion tests. In tests n°1 and n°2, the corrosive

125 medium remained constant during the test. In test n°3, the corrosive medium was modified

126 after 1935 h.

Т	`est	Conditions	Duration		
Test n°1		Severe	$t_{severe} = 2564 h$		
Test n°2		Soft	t _{soft} = 16815 h		
	Phase n°1	Severe	t _{severe} = 1935 h		
Test n°3	Phase n°2	Soft	$t_{soft} = 16815 h$		
		5011	$(t_{test3} = t_{severe+soft} = 17783 \text{ h})$		

127

128 XPS analyses were carried out with a Thermofisher Escalab 250 XI spectrometer using 129 a monochromatic X-ray Al Ka source. The instrument was calibrated in energy with the 130 Ag Fermi level (0 eV) and the $3d_{5/2}$ core level of metallic silver (368.3 eV). The C-1s signal 131 was used to correct a possible charge effect: the CC/CH contribution of C-1s spectra was fixed at 285.0 eV. The analysis zone consisted of a 900 µm diameter spot. The data 132 processing was performed using the commercially available AvantageTM software. For the 133 134 fitting procedure, a Shirley background has been used and Lorentzian-Gaussian (L/G) ratio 135 was fixed at 30%. For the determination of relative proportions of oxide and metallic contribution, Ni-2p_{3/2}, Cr-2p_{3/2} and Fe-2p_{3/2} spectra have been deconvoluted. The main 136 137 contributions used are presented in Table 3. Several arbitrary contributions are necessary 138 to fit the iron and chromium oxide due to a multiplet splitting making the spectral analysis 139 particularly complex [43, 44]. Nickel element is observed only metallic chemical state. 140

141 Table 3: Parameters used for the deconvolution of Cr, Ni and Fe-2p_{3/2} core level spectra

	Ni-2p _{3/2}	Fe-2p _{3/2}				Cr-2p _{3/2}			
Chemical	Metallic	Metallic	Oxide		Metallic	Oxide			
state									
			Peak 1 Peak 2			Peak 1	Peak 2	Peak 3	
Binding	853.0 ±	853.0 ±	709.8	712.0	853.0 ±	576.1	577.3	578.5	
Energy	0.3	0.3	± 0.3	± 0.3	0.3	± 0.3	± 0.3	± 0.3	
(eV)									
FWHM	1.4	1.0	3.0	3.3	1.5	1.7	1.8	1.9	
(eV)									

142 (AvantageTM software) binding energies and full width at half maximum (FWHM).

144 <u>Cellular Automata model</u>

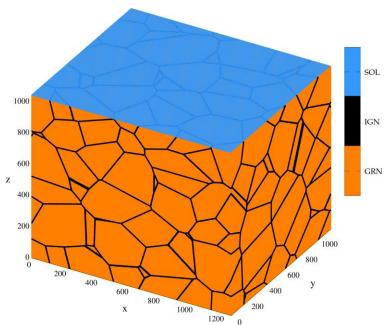
145 CA approach consists first in discretizing a volume (box) into a 3D hexagonal grid of 146 cells. In our model ([23]), a cell can belong to a grain (GRN state), a grain boundary (IGN 147 state) or the solution (SOL state). The material granular microstructure is obtained 148 numerically by a Voronoi diagram (Figure 1). Furthermore, the SOL state is assigned to 149 the three uppermost xy-layers: during dissolution, the solution path is conducted from the 150 top of the grid to the bottom.

151 The kinetics of the reactions are hereby converted into corrosion probabilities, which 152 drive the step from a time t to the following t + Δt . Given CA cells interact with their 153 neighbouring ones according to their states, following transition rules. IGN and GRN cells 154 change their states to SOL (this switch indicates that the IGN or GRN cell is corroded) 155 according to two probabilities (input data fixed by the user), P_{ign} for grain boundaries and P_{grn} for grains. The way to fix the values of P_{ign} and P_{grn} so as to reproduce adequately the 156 157 experimental results (with CA to experiments conversion factors) is described in reference 158 [23].

The code has been written in C language, in CUDA environment, and numerical simulations have been performed using NVIDIA Tesla K80 in Dell PowerEdge C4130 servers with Intel Xeon E5-2640 processors. In the case of a (XYZ dimensions) 3D grid, a simulation run for a single experiment takes from one to a few days, depending on the values that are given to P_{grn} and P_{ign} (the higher the values, the lower the simulation time). The grids taken for the simulation are boxes of 1280x1280x1280 cells, and the number of Voronoï structures are one hundred. This corresponds to a surface dimension of 13.5 mm²
and a depth of 395 μm, using the scale transformation of 0.309 μm/cell as described in [23].
The results are averaged over the hundred different Voronoï structures and the errors bars
given further in the paper represent their dispersion.

From the corroded sample at a time t, we can estimate the mass loss and the mean groove angle α' ([23]), as well as the relative surface in contact with the corrosive medium (see appendix 1 and 2). Note that the notation α' refers to the angle determined in 2D from virtual cross-sections of the 3D grid and that its distribution is slightly different from the 3D angles α distribution as discussed in [23, 24].

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175

Figure 1: Representation of a 3D initial grid considered for the IGC model obtained
numerically by a Voronoï diagram (GRN state cell in orange, IGN state cell in black
and SOL state cell in blue).

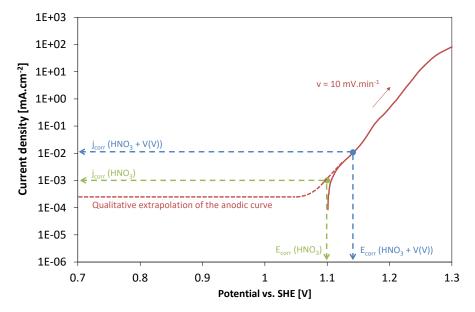
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- 180

Results

181 <u>Electrochemical measurements</u>

We performed preliminary electrochemical measurements in order to specify the conditions of corrosion in both configurations "severe" and "soft". Figure 2 presents the anodic linear polarization of the 310L SS in nitric acid HNO₃ 8 mol.l⁻¹ at boiling point temperature. Based on the results obtained for a similar system [15], we qualitatively extrapolated the anodic curve below the corrosion potential E_{corr} (that is not directly measurable by electrochemistry because of the cathodic reactions) in order to visualize the respective position of the passive and transpassive domain of the SS. Thus, we observe that in these conditions, the SS is polarized ($E_{corr} \sim 1.11 \text{ V } vs. \text{ SHE}$) in the transition of the passive to transpassive domains, where IGC is expected. In addition to vanadium(V), E_{corr} is shifted to a higher anodic potential ($E_{corr} \sim 1.14 \text{ V } vs. \text{ SHE}$) in the transpassive domain, where IGC is also expected. The expected corrosion currents are given in Figure 2, which shows that a higher corrosion rate is expected in presence of vanadium(V). In conclusion, SS is polarized in both conditions in the transpassive domain, where IGC is

195 expected. The objective of the following parts is to characterize IGC in both conditions.



196

197Figure 2: Anodic linear polarization curve of 310L SS in HNO3 8 mol.l⁻¹ at boiling198point temperature (red continuous line). The red dashed line represents the199qualitative extrapolation of the anodic curve in the passive domain. The200characteristics (E_{corr} and j_{corr}) of the system are in green. Those of the system Uranus20165 in HNO3 8 mol.l⁻¹ + V(V) 150 mg.l⁻¹ are in blue.

202

203 <u>Immersion tests</u>

In this part, we discuss the case IGC in both oxidative conditions, respectively, when the chemical medium remains the same as a function of time. The corrosion kinetics is given in terms of morphology (Figure 3 (a) for severe and Figure 5 (a) for soft conditions) and mass loss (expressed in terms of equivalent thickness loss as described in the experimental section) and corrosion rate (Figure 4 for severe and Figure 6 for soft conditions). The behavior is typical of the IGC observed for non-sensitized stainless steels and has been extensively discussed in references [15, 21, 35]. 211 IGC begins with the creation of tight grooves at grains boundaries (80 h and 240 h in Figure 212 3 (a)) that progressively penetrate the steel. This leads to an increase of the SS/solution interface area, which is correlated to the corrosion rate increase as estimated by mass loss 213 214 (Figure 4). This also leads to the detachment of grains that progressively affect the whole 215 surface (2484 h in Figure 3 (a)) increasing the corrosion rate even more. When the grains 216 detachment has affected the whole surface, the system reaches a corrosion steady state. The 217 surface area does not evolve anymore, since the progression of grooves (increasing 218 interface area) is counter-balanced by the grains detachment (decreasing the interface area). 219 The phenomenology is similar for both oxidizing conditions, but the kinetics is different. 220 It has been shown that this kind of IGC can be described by two different corrosion rates: 221 V_{grn} and V_{ign} which correspond to corrosion rates of the grains and grains boundaries respectively. From the kinetics of IGC (Figure 4 and Figure 6), it is possible to estimate 222 223 the values of V_{grn} and V_{ign}^* (corresponding to the projection of V_{ign} on the vertical axis) by 224 a semi-empirical approach presented in [35]. V_{ign} is deduced from V_{ign}* using a tortuosity 225 factor k: $V_{ign} = V_{ign}^* \times k$, with k = 1.18 [23]. Results are given in Table 4. Both corrosion 226 rates are faster in severe than in soft conditions. This confirms the forecasting from the electrochemical results (Figure 2). 227

228 The transient time necessary to reach the steady state can be estimated as follows [35]:

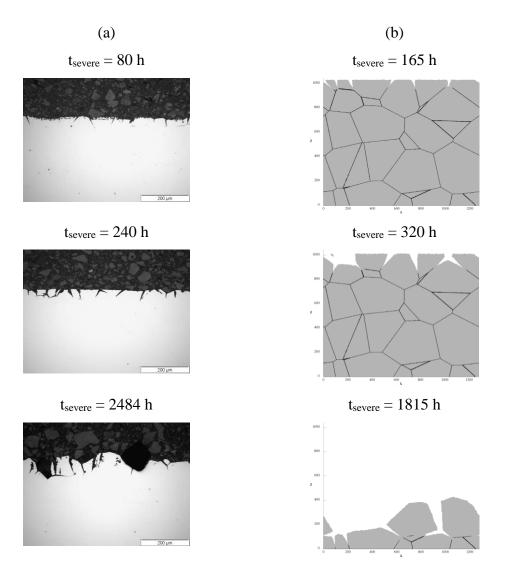
$$\frac{3}{2} \frac{D}{V_{ign}}$$
 Equation 2

where D represents the average grains diameter ($84 \mu m$). Therefore, the transient time is lower in severe conditions (Table 4). Durations of the experiments were fixed so that the steady state could be almost reached in both cases, that is 2564 h for severe and 16815 h for soft conditions, respectively. The objective of the following characterizations is to investigate the surface properties at steady state.

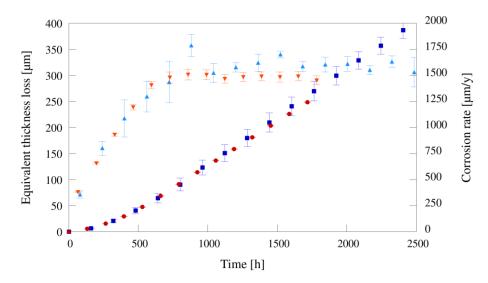
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Table 4. Corrosion rates and transient time for the severe and soft IGC cases

IGC	V_{grn} / $\mu m.y^{-1}$	V_{ign} * / μ m.y ⁻¹	V_{ign} / $\mu m.y^{-1}$	Transient time / h
severe	273	1656	1954	565
soft	12	56	66	16703

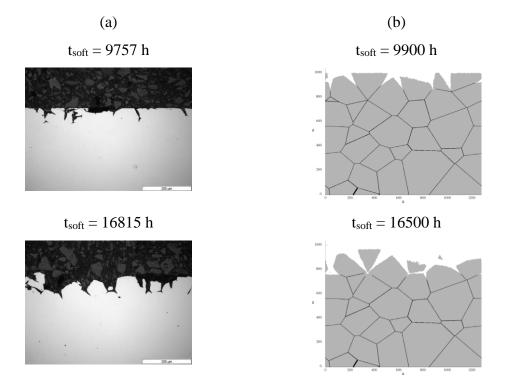


- 237 Figure 3: Evolution of the IGC observed on cross-sections in the case of a severe IGC.
- 238 (a) Experiment (b) CA simulations at different times.
- 239

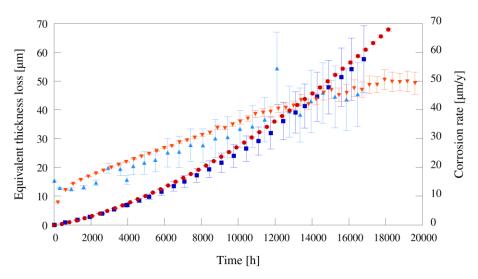


240

Figure 4: Comparison between experimental results (in blue) and CA simulations (in
red) in the case of a severe IGC. Squares represent the equivalent thickness loss and
triangles the corrosion rate.



- Figure 5: Evolution of the IGC observed on cross-sections in the case of a soft IGC.
- 246 (a) Experiment (b) CA simulations at different times.
- 247

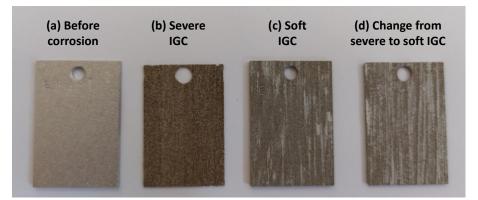


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Figure 6: Comparison between experimental results (in blue) and CA simulations (in red) in the case of a soft IGC. Squares represent the equivalent thickness loss and triangles the corrosion rate.

Figure 7 presents the observation of the samples before (a) and after the corrosion tests in severe (b) and soft (c) conditions. In both conditions, samples are darker after corrosion then indicating an effect of the corrosion on the surface. Moreover, the aspect of samples is different between the severe (dark grey) and the soft (light grey). This shows that the aspect of the corroded SS is also dependent on the conditions of corrosion. The origin of the difference of aspect is further discussed in terms of chemical composition and IGC morphology of the interface.

260



261

Figure 7: Aspect of the samples before (a) and after the corrosion tests in the severe

263 $(t_{severe} = 2564 h)$ (b), soft $(t_{soft} = 16815 h)$ (c) and change from severe $(t_{severe} = 1935 h)$

264 to soft ($t_{soft} = 16815 h$, *i.e.* $t_{severe+soft} = 17783 h$) conditions (d).

266 Therefore, we analyzed the chemical composition of the surface using XPS relative 267 quantification in both conditions (Figure 8). The XPS response is qualitatively similar in severe and soft conditions. The spectra show the presence of oxide and metal (associated 268 to the presence of the metal under the oxide layer). The relative proportions of the oxide 269 270 and metal contributions (for the major elements contained in the 310L SS: Iron, nickel, 271 chromium) are reported in Figure 8 (a). The relative contribution of the oxide is larger in 272 the severe than in the soft IGC conditions. This indicates that the oxide layer is thicker in 273 the severe IGC conditions (with a higher corrosion potential E_{corr} as illustrated in Figure 2) 274 than in the soft IGC conditions. This is in accordance with the results of Tcharkhtchi et al. 275 who showed an increase of the oxide thickness of a 304L SS in nitric acid with the increase 276 of the corrosion potential E_{corr} [15].

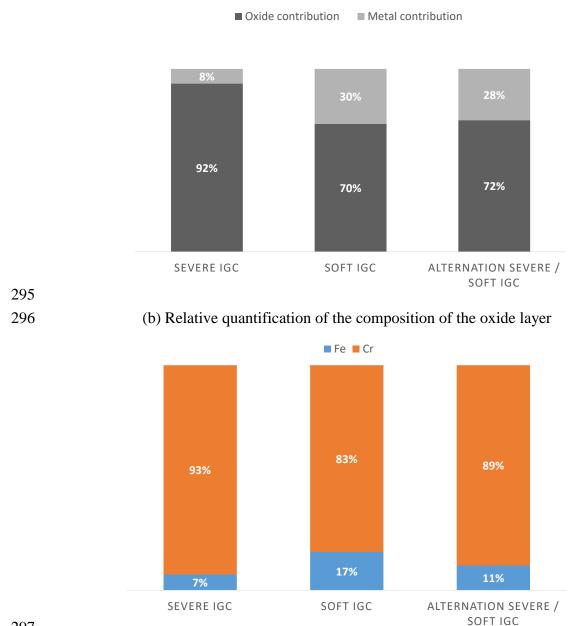
Figure 8 (b) gives the chemical composition of the oxide layer. As classically observed for these SSs corroded in nitric acid media [15, 34, 45], the oxide is mainly composed of chromium with a small proportion of iron. Nickel oxide is not observed. The severe/soft IGC conditions have a small influence on the chromium/iron ratio: a little larger relative enrichment in chromium is observed for the severe condition.

282 The chemical composition of the underlying metal is given in Figure 8 (c). Its relative 283 composition differs from the bulk material: relatively enriched in nickel, compared to chromium and iron. This observation has already been reported for SSs in nitric acid [15]. 284 285 It could be due to the fact that nickel is less oxidized than chromium and iron (as illustrated 286 in Figure 8 (b)) and consequently accumulates under the oxide. This nickel enrichment 287 seems to be larger in the severe conditions than in the soft conditions. This could be linked 288 to the fact that the metallic zone that is analyzed by XPS is thicker (because the oxide is 289 thinner) in soft conditions than in severe conditions. Therefore, the nickel relative 290 enrichment in the underlying metal is more averaged with the bulk metal composition in 291 the soft than in the severe conditions.

293 (a) Relative quantification of the total oxide and the underlying metal contributions (for

the major elements contained in the 310L SS: Fe, Ni, Cr)

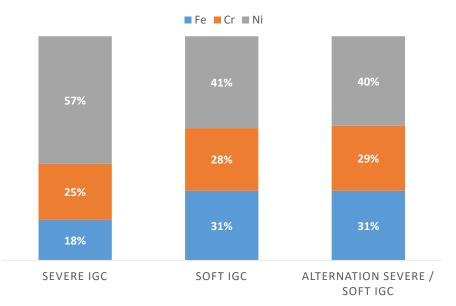
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(c) Relative quantification of the composition of the underlying metal



299

Figure 8: XPS relative quantification of the chemical characteristics of the surface of 301 310L SS samples corroded in the severe ($t_{severe} = 2564$ h), soft ($t_{soft} = 16815$ h) and 302 change from severe ($t_{severe} = 1935$ h) to soft ($t_{soft} = 16815$ h, i.e. $t_{severe+soft} = 17783$ h) 303 conditions.

305 In order to get a quantitative description of the morphology, we used a CA modeling of the 306 experiments. In a previous work [23], we showed that this model reproduces accurately the 307 morphological evolution of IGC. This CA numerical approach enables to quantify 308 precisely the morphological characteristics of the system, in terms of grooves angles α ' 309 distribution and the surface in contact with the solution.

The input corrosion probabilities are given in Table 5 for both IGC conditions. Moreover, conversion factors were also used in order to convert space and time scales from CA modeling to real experiments [23]: the space scaling factor A and time the scaling factor B were fixed to 0.31 μ m/cell and 0.825 h/iteration, respectively. CA simulated time evolutions of the mass loss (as expressed in terms of equivalent thickness loss) are given in Figure 4 and Figure 6.

The distribution of the grooves angle α ' (in degrees) at steady state of IGC is given in Figure 9. It appears that the grooves are thinner in severe (mean value 20.5, standard deviation 5.0) than in soft (mean value 26.59, standard deviation 5.9) conditions. From Beaunier [46, 47], the groove angle α is theoretically related to the V_{ign}/V_{grn} ratio by the relation:

$$\frac{V_{ign}}{V_{grn}} = \frac{1}{\sin(\alpha/2)}$$
 Equation 3

- 322 This theoretical value is in agreement with the one estimated by CA.
- 323 In conclusion, it appears that the more oxidant the corrosive solution, the thinner the 324 grooves and the larger the ratio V_{ign}/V_{grn} .

325 SEM images of the corroded samples are given in Figure 10. It is clearly visible that there are less "small grains" that remain attached to the bulk in the severe case (a) than in soft 326 327 case (b). It is due to a larger V_{ign}/V_{grn} in case (a) (Table 4), which leads to a larger grains 328 detachment rate. From the time they are in contact with the corrosive solution, small grains 329 are more rapidly detached from the bulk than large ones, which explains the lack of small 330 grains on a given surface picture in the case of severe corrosion, given their shorter "life-331 time". As another effect of the grains life-time, it is also clearly visible in (b) and (c) that 332 large grains that remain attached to the bulk are more deeply corroded than the small ones. 333

Table 5: Corrosion probabilities used as input data in the CA model and calculated from the experimental results based on the procedure given in reference [23].

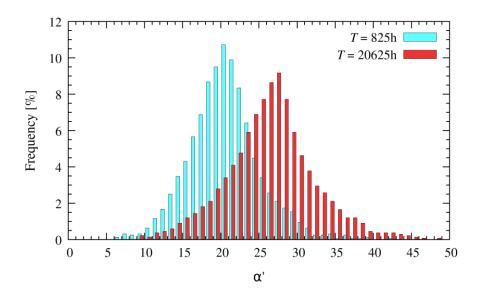
	P _{ign}	Pgrn
Severe	$P_{ign,severe} = 1$ (arbitrary maximized in order to	$P_{grn,severe} = P_{ign,severe} \times \frac{V_{grn,severe}}{V_{ign,severe}}$
	minimize the calculation durations)	$P_{ign,soft} = 0.140$
Soft	$P_{ign,soft} = P_{ign,severe} \times \frac{V_{ign,soft}}{V_{ign,severe}}$	$P_{grn,soft} = P_{ign,soft} \times \frac{V_{grn,soft}}{V_{ign,soft}}$
	$P_{ign,soft} = 0.0338$	$P_{grn,soft} = 0.00614$

337 Table 6: Intergranular grooves angles α ' characteristics at steady state in the different

338 corrosion conditions (CA simulations)

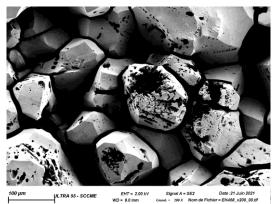
Exp., time	Mean value (degrees)	Standard deviation (degrees)	Error	$1/(\sin(\alpha'/2))$
Severe condition $t_{severe} = 825 h$	20.54	5.00	0.13	5.61
Soft condition $t_{soft} = 20 625 h$	26.59	5.89	0.16	4.35
Change severe $t_{severe} = 825 \text{ h}$	20.67	4.88	0.14	5.57
to soft condition $t_{severe+soft} = 20\ 625\ h$	26.04	5.92	0.17	4.44

339



340

Figure 9: Distribution of the grooves angles α ' in the steady state in severe (in blue, evaluated at t_{severe} = 825 h) and in soft (in red, evaluated at t_{soft} = 20625 h) conditions (CA simulations). In both cases, histograms are realized with the same classes but are slightly shifted for a better view.





ULTRA 55 - SCCME EHT = 2.00 kV WD = 8.1 mm nal A = SE2 Date :21 Juin 2021 200 X Nom de Fichier = EH398_x200_01.tit

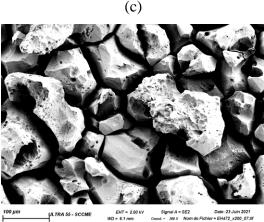


Figure 10: Observation of the samples by Scanning Electron Microscope after the 346 347 corrosion tests in the severe (t_{severe} = 2564 h) (a), soft (t_{soft} = 16815 h) (b) and change 348 from severe ($t_{severe} = 1935 h$) to soft ($t_{soft} = 16815 h$, i.e. $t_{severe+soft} = 17783 h$) conditions 349 (c).

350

351 Moreover, we investigated how the grooves angles distributions affect the surface in 352 contact with the corrosive solution. For this purpose, the relative surface was determined 353 from the CA simulations as described in the appendix 1 and 2. Results are given in Figure 354 11. In both severe and soft conditions, the relative surface increases from its initial "flat 355 surface value" (100%) to reach a larger steady state value. The steady state value is higher 356 $(238.4 \pm 0.4\%)$, estimated in the interval t_{severe} = 1568 - 1732 h) for the severe conditions 357 (therefore for the thinner grooves angle) than in soft conditions (223.7 \pm 0.5%, estimated 358 in the interval $t_{soft} = 17325 - 20625$ h). This is in agreement with the results of Gwinner et 359 al. obtained with a model based on a 2D geometrical approach [35].

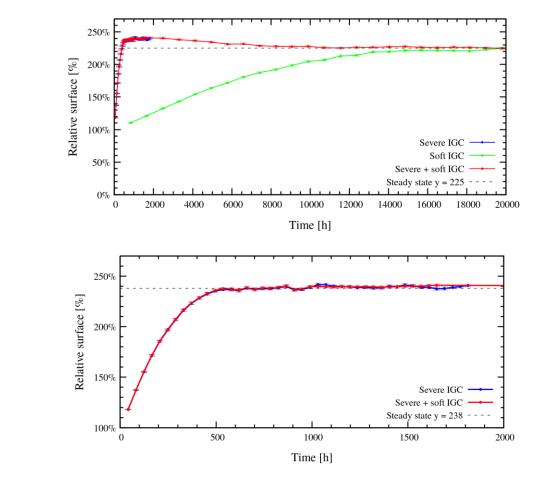


Figure 11: Relative surface for sections of the lattice for the three IGC corrosion
regimes (CA simulations). The bottom plot is a zoom of the top one at short times.

We showed that in stationary conditions, the IGC characteristics depend on the oxidizing 366 power of the corrosive medium. In more severe conditions, the SS is polarized at higher 367 potential in the transpassive domain which has different consequences on the corrosion of 368 369 the SS. Firstly, the dissolution of the SS is faster (Vgrn is larger). This has to be related to 370 the presence of a thicker oxide on the surface evidenced by XPS. Secondly, the 371 intergranular corrosion is faster (V_{ign} is larger), which leads to a shorter transient time to 372 reach the IGC steady state (in accordance with [35], where the transient time is shown to 373 be inversely proportional to V_{ign}). Moreover, the global corrosion rate reached at steady 374 state (which corresponds to V_{ign}*) is larger. Thirdly, the ratio V_{ign}/V_{grn} is increased which 375 has the consequence that the grooves angles are thinner. Finally, the total surface reached 376 at steady state is larger.

377

361

As discussed in the introduction, it is of practical interest to investigate the influence of changing the nature of the corrosive medium during the life duration. This is the objective of the following part.

381

382 Change from severe to soft IGC conditions

In order to study the effect of a change in the IGC conditions, we firstly corroded samples during 968 h in the conditions of severe IGC (with vanadium(V)) until the steady state is reached. Figure 12 and Figure 13 display the evolution of the mass and the morphology as a function of time, respectively. At the end of this early stage, the steady state is reached in terms of mass loss (Figure 12) and surface morphology (Figure 13).

388 Then we changed the solution into soft conditions (without vanadium(V)). The evolution 389 of the corrosion rate is given in Figure 14 and is compared to the one in soft conditions 390 only. The corrosion rate suddenly decreases in accordance with the new soft IGC 391 conditions. However, it does not keep a constant value. It slowly decreases as a function of time even if the solution (that means the corrosiveness) remains the same. The system 392 393 reaches a new steady state, which is identical to the previous soft IGC stationary case in terms of corrosion rate (about 50 μ m.y⁻¹). Moreover, the steady state is reached at the same 394 395 time in both cases. This transient time is in accordance with the one estimated by Equation 396 2. This corresponds to the time necessary to remove a thickness equivalent to the mean 397 grains size. Thus, whatever the history of the SS (already corroded in severe IGC 398 conditions or not), the corrosion needs to consume the equivalent of a layer of grains to 399 erase the effects of this history.

400 Figure 13 shows the evolution of the IGC morphology from the severe conditions at steady 401 state (at $t_{severe} = 968$ h) to the soft conditions (until $t_{severe+soft} = 17783$ h). A slow evolution 402 is observed between a highly rough surface (resulting from the severe IGC conditions) to 403 a less rough surface (resulting from the soft IGC conditions). In the same way, SEM 404 observations in Figure 10 show that the soft conditions tend to smooth the serious 405 intragranular corrosion induced by severe conditions. CA simulations were performed to 406 investigate quantitatively this point. The same input corrosion probabilities were 407 considered as for the previous simulations (Table 5). The first step was first modeled in 408 severe conditions during 990 h. Then the probabilities were changed into soft conditions 409 to model the rest of the simulation.

410 Simulations reproduce correctly the mass loss kinetics (Figure 12) and the evolution of the 411 morphology (Figure 13) observed experimentally. Figure 15 shows that the characteristics 412 of the grooves angles evolve from relatively thin angles under severe conditions to larger 413 angles in soft conditions. Consequently, the relative surface in contact with the solution 414 decreases slowly from a value of 238.7 \pm 0.7% (estimated in the interval t_{severe} = 1568 -415 1733 h) in severe conditions to about 225.4 \pm 0.5% (estimated in the interval t_{severe+soft} = 416 17325 - 20625 h) in soft conditions, the same value as the experiment in steady soft 417 conditions.

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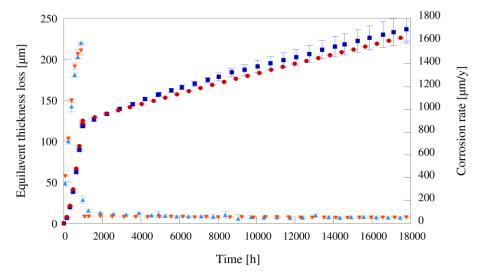
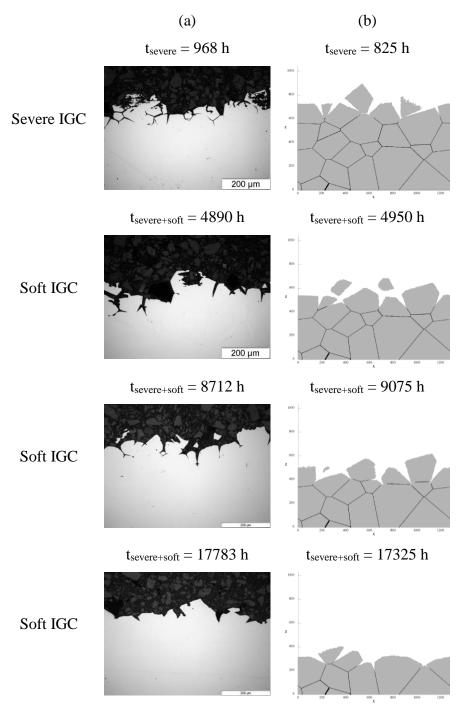
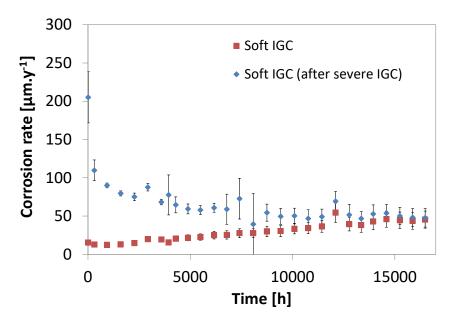


Figure 12: Comparison between experimental results (in blue) and CA simulations
(in red) in the case of alternation a severe and a soft IGC. Squares represent the
equivalent thickness loss and triangles the corrosion rate.

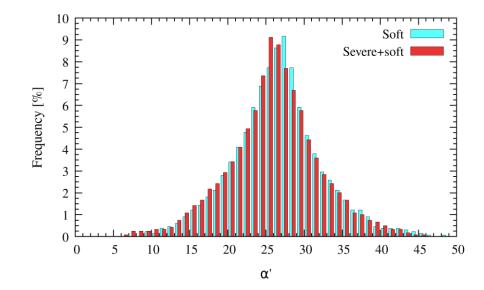


- 424 Figure 13: Evolution of the IGC observed on cross-sections in the case of alternation
- 425 a severe and a soft IGC. (a) experiment and (b) CA simulations.
- 426



428 Figure 14: Comparison of the corrosion rate estimated for soft IGC only and soft IGC

- 429 after severe IGC (experimental results).
- 430



431

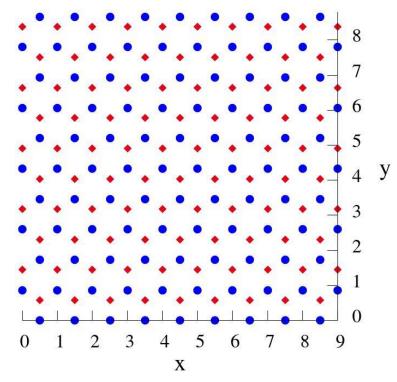
432 Figure 15: Distribution of the grooves angles α ' in the steady state in soft (in blue, 433 evaluated at t_{soft} = 20625 h) and in change from severe to soft (in red, evaluated at 434 t_{severe+soft} = 20625 h) conditions (CA simulations). In both cases, histograms are 435 realized with the same classes but are slightly shifted for a better view.

The characteristics of the oxide layer on the surface also re-adapts to the new soft
conditions (Figure 8). In particular, the apparent oxide thickness is similar in soft
conditions and in change from severe to soft conditions (Figure 8 (a)).

439 Because of the oxide and morphology re-adaptation to the new soft conditions, the aspect 440 of the surface also changes from dark grey (characteristic of the severe conditions) to light 441 grey (characteristic of the soft conditions) as shown in Figure 7. 442 443 444 Conclusions 445 We first investigated the impact of the oxidizing character of the nitric medium on the 446 evolution of the IGC of an austenitic SS. In two different stationary chemical conditions 447 (severe and soft, respectively), we showed that the SS reaches a different steady state in 448 terms of the oxide and the geometrical natures of the interface: the oxide is thicker, the 449 intergranular grooves are thinner and the surface area is larger with the oxidizing character 450 of the nitric medium. Then we investigated the effect of an alternative "severe then soft" 451 corrosion sequence. We showed that the system re-adapted to the soft conditions after a 452 certain duration (which corresponds to the time necessary to corrode a thickness equivalent 453 to the mean grains size of the SS) without memory effect from the previous severe ones: 454 the corrosion rate, the geometrical nature of the interface and the thickness of the oxide 455 become similar to the system corroded in soft conditions only. In other words, whatever 456 the IGC history of a SS, the new conditions of IGC corrosion need to consume the equivalent of a layer of grains to erase the effects of this history. 457 458 459 Acknowledgments 460 461 The authors thank Orano for financial support. They thank also R. Golchha for his careful proofreading. D. di Caprio would like to thank Dr. B. Diawara for fruitful 462 463 discussions and introducing him to the marching cubes algorithm. 464

465	Appendix
466	
467	Appendix 1: solid/solution frontier estimation, marching square type algorithm
468	In this section, we detail the algorithm used to measure the length of the border line
469	between the solution cells and the solid corresponding to GRN or IGN cells. For 3D objects,
470	the marching cubes algorithm [48] is often used to determine contour lines. Given its
471	simplicity, the algorithm finds applications in video games but also in medicine, for 3D
472	visualization of volume data from magnetic resonance imaging and computed tomography
473	scans [48, 49]. In the case of 2D images, the algorithm is referred to as marching squares.
474	In the context of this paper, the algorithm is further adapted for a 2D grid based on
475	rectangles paving the plane instead of squares. The details about the system coordinates
476	used for the hexagonal lattice are given hereafter.
477	
478	The hexagonal lattice

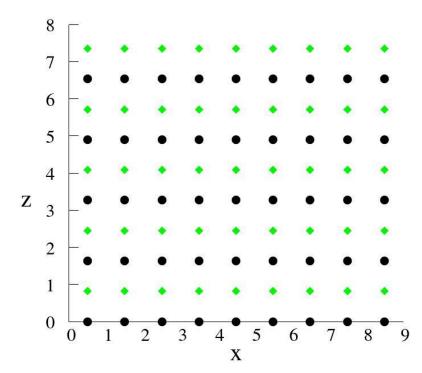
The plane of the hexagonal lattice structure is the horizontal 0xy plane, with, for z = 0, the first line y = 0, points starting at x = 0.5 and placed in the Ox direction at a distance of 1 as shown in Figure 16 in blue points.



483 Figure 16: Horizontal sections of the hexagonal lattice. Two consecutive planes, z = 0484 and $z = (2/3)^{1/2}$, are shown with respectively blue and red points.

485 Once these first two planes are defined, the rest of the lattice is derived. In particular, in 486 the experiments and in the simulations vertical sections are studied. The layout of points in 487 the vertical sections for the simulation is shown in Figure 17 where we have considered 488 vertical Oxz planes with constant y coordinate.

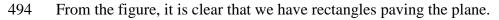
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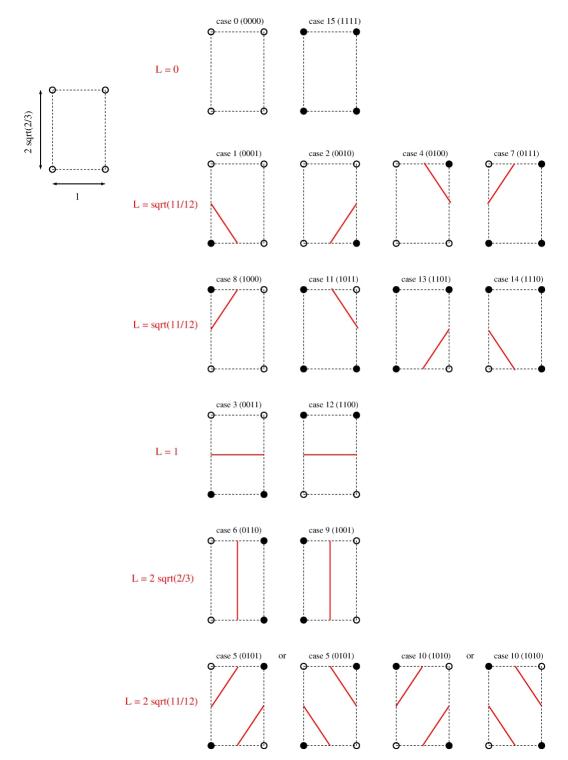
491 Figure 17: Vertical sections of the lattice. Two consecutive planes for y = 0 and y =492 (3)^{1/2}/2 are shown with respectively black and green points.

493



- 495
- 496 The marching rectangles algorithm

Then, the algorithm consists in summing the contributions to the solution/solid border coming from each rectangle in the plane. For this aim, we first list all possible contributions coming from the configurations as shown in Figure 18. By assigning "1" to an intergranular or granular point and "0" to a solution point and starting from the bottom left corner, in an anticlockwise order, we obtain a binary number which is assigned to the corresponding case.



505 Figure 18: On the top left the elementary rectangle and its dimensions. On the right 506 are listed the length contributions and the corresponding layout of the points. Empty 507 circles are for solution points and black points are for solid granular or intergranular 508 cells.

509

510 The cases in the first line correspond to cases inside the solution or inside the solid and

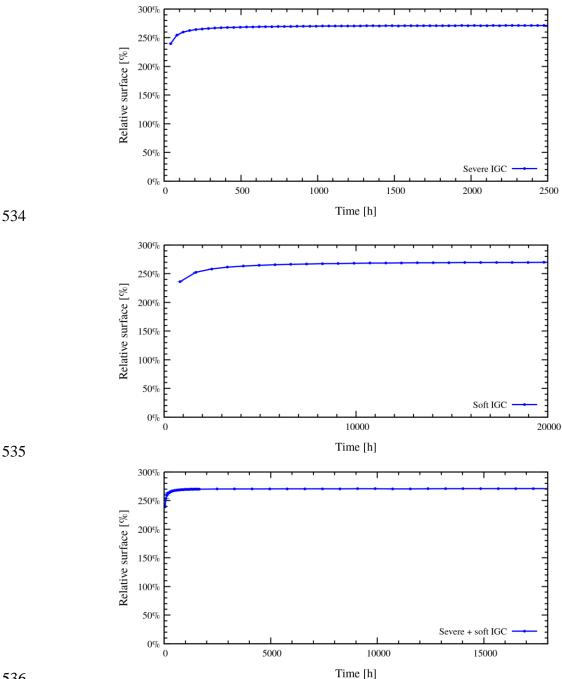
511 they naturally do not contribute to the border length: L = 0. The cases in the last line

- 512 correspond to a saddle point situation where we have two lines but for which the line 513 orientation can be ambiguous. However, the contribution to the border length is the same 514 for both orientations so that the result is unchanged despite the ambiguity. Other border 515 lengths correspond to their geometrical contribution. All rectangles constituting the lattice 516 are computed and their contribution is summed up which gives the final estimation of the 517 border length. The ratio of this length divided by the straight lateral length of the system is 518 what we consider to be the relative surface, which is in fact a line for the 2D sections.
- 519

520 Appendix 2: extracting the grain scale relative surface

521 Simulated sections of the system in Figure 3, Figure 5 and Figure 13 clearly show that we 522 have two types of relative surface contributions. One with short length scale variations 523 corresponding to the dissolution of a single grain and one at a larger scale, the scale of 524 grains, due to IGC and detachment of grains. It is this last contribution that we are interested 525 in. However, the algorithm presented above does not distinguish the two, as it provides the 526 total separation line between solid and solution.

We present, hereafter, the method used to separate the contribution from IGC and grain detachment from the contribution at a short length scale due to dissolution. For this aim, we perform supplementary simulations for the dissolution of an exclusively granular material with an initial plane surface and in the identical conditions of severe, soft and variable IGC conditions as for the IGC material model. Results are obtained averaging over 2000 sections. Figure 19 shows the relative surface, roughness for the three cases.





537 Figure 19: Solid/solution relative interface for successively the severe, soft and variable IGC conditions for granular dissolution. 538

540 The relative surface varies with time: it increases before reaching a steady state. This is 541 why we use this time dependent quantity to renormalize the relative surface and not the 542 steady state value. Thus the relative surface corresponding to IGC and grain detachment is 543 obtained from the relative surface obtained by the algorithm by dividing it by the relative 544 surface for exclusively granular dissolution. The procedure has been tested by applying it

545	to the	study presented in [23], and the results compare well within the error bars. The results
546	in the	case of the present paper study are presented in Figure 11. Averages are performed
547	using	100 Voronoï structures with for each 9 sections, this ensures that sections are
548	suffici	ently spaced to avoid undesirable correlations.
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