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# Closed-loop-based observer approach for tunneling current parameter estimation in an experimental STM\*

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#### Abstract

This paper is about parameter estimation in quantum effect of tunneling current, and is based on an experimental device of Scanning Tunneling Microscope (STM) type. Since this effect needs feedback control in order to be obtained and kept, a closed-loop stability analysis is first presented prior to any estimation. Then, in this context of closed-loop operation, an observer approach is proposed to estimate the couple of parameters which characterize the tunneling current (nonlinear) model. An extension of this observer technique to topography estimation is also discussed, and all the methodologies are illustrated with experimental data.

*Keywords:* Tunneling current, proportional integral control, nonlinear system, stability analysis, state observer, parameter identification.

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#### 1. Introduction

Tunneling effect is a quantum phenomenon which was first used by G. Gamow in 1928 to explain radioactivity [3]. It translates into what is called *tunneling current* when describing the electrical current that can be measured between a conductive  $_{30}$ 

- tip and a surface subject to a voltage applied between them, and with a relative distance lower than 1 *nm*. This effect is typically at the heart of the so-called *Scanning Tunneling Microscope* (STM), invented in 1981 by G. Binnig and H. Roher [4], and allowing to obtain information about a surface, provided <sup>35</sup>
- that some appropriate control is applied. This intrinsic need for feedback gave rise to advanced control studies from the end of 1990's on, as in [5, 6] for instance, where inversion-based techniques were considered, in [7], where a variable structure
- <sup>15</sup> control was studied, in [8, 9], where methodologies of robust 40 digital pole placement with sensitivity function shaping were proposed, in [10] with a multivariable Linear Quadratic Integral approach, up to more recent works as in [11, 12] presenting self-tuning PI control, [13] about MIMO H<sub>∞</sub> robust control,
   <sup>20</sup> [14] with robust observer-based control, or even in the very re-45
- cent reference [15] proposing a MEMS-based STM system.

In fact, tunneling current does admit a model, basically as an exponential law of the distance between tip and sample sur-

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face, but with parameters depending on the operation conditions (such as materials and environment) [16]. The knowledge of such parameters is yet useful, for the control design on the one hand (see e.g. [17]), but also for topography applications of STM for instance, where the surface variations over a sample can be retrieved via this tunneling current model (e.g. as in [18]), or even in other possible tunneling applications [19, 20]. This motivates the study of estimation techniques for those paramaters. In [17] for instance, a frequency-based closed-loop identification is proposed for an STM operation, providing in particular one of the two crucial coefficients of tunneling current model, and motivated by control improvement. In the present paper instead, a time-domain direct approach is studied, with observer techniques combining and extending our preliminary results of [1] for the case of one parameter to be estimated, and [2] for the case of two parameters, and rather focused on topography imaging improvement. The latter means that here the control is used for the estimation purpose, with a full stability analysis for the closed-loop system being provided, while the observer approach improves those of [1, 2], and includes an extension discussion towards surface variations estimation. This observer approach thus provides a unifying framework for both tunneling current calibration and possible surface imaging, as an alternative to classical off-line current characterization (e.g. curve fitting) and control-based imaging [16]. In addition, it provides more information (two parameters) with less constraints (no dither for instance) than in socalled 'gap modulation methods' [11, 12], leading to some selfcalibration tool, and possible quantitative analysis (see propositions 1 and 2 hereafter). Finally, all the proposed methodological developments are also illustrated with real data recorded on an experimental prototype of STM type developed in Gipsa-lab [21, 22], and can enrich the area of measurement and control at nanoscale that has been attracting an increasing attention in the

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last decade (as in [23, 24, 25, 26, 27, 28, 29] for instance, and references therein).

The paper is thus organized as follows: section 2 first states the tunneling current modeling problem under consideration (based on our STM prototype), and section 3 provides a full closed-loop stability analysis when considering a simple proportional integral control design. The proposed observer-based approach for estimation of tunneling current parameters is then presented in section 4, and extended to the estimation of surface variations. Section 5 is dedicated to illustrative results based on

<sup>70</sup> experimental data, while section 6 finally concludes the paper.

#### 2. Modeling problem

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The main problem we consider is that of estimating parameters of tunneling current (exponential) model. To that end, let us rely on a typical STM operation where tunneling current is measured. Such an operation means that a sharp conductive tip is approached close enough to a conductive sample, with a bias voltage being applied between both of them. The tip is driven

- <sup>80</sup> by a piezo actuator fed via a voltage amplifier, while the tunneling current is measured via an appropriate sensor and used in a feedback loop to control the tip vertical position. This overall configuration is summarized by figure 1 hereafter, where u denotes the input driving voltage,  $u_a$  its amplified version,  $i_t$  the
- tunneling current which is established, and  $y_m$  its measurement (the feedback control loop is in grey dashed line). <sup>100</sup>



Figure 1: Tunneling current control.

For a formal dynamical description of this operation, we will refer to a corresponding prototype of Gipsa-lab [21], with a 120kHz PSt 150 actuator for the vertical motion, a 13kHz high gain sensor for current measurement, and a 4kHz voltage amplifier for piezo feeding, shown in figure 2.

Mathematically, the main characteristics of each element can <sup>5</sup> be summarized as follows:

• The current sensor dynamics can be captured by a first order model of the form:

$$\dot{x}_1(t) = -a_1 x_1(t) + i_t(t) y_m(t) = c x_1(t) + v_y(t)$$
 (1)



Figure 2: STM prototype (Gipsa-lab).

where  $x_1$  denotes its state variable,  $a_1$  represents its bandwidth, c adjusts its DC gain, and  $v_y$  represents some possible additive noise in its measurement  $y_m$ .

• The voltage amplifier can be also represented by a first order model as:

$$\dot{x}_2(t) = -a_2 x_2(t) + u(t) u_a(t) = c_2 x_2(t)$$
 (2)

where  $x_2$  is its state variable, and  $a_2$ ,  $c_2$  gather bandwidth and gain parameters.

• The piezoactuator dynamics can be reduced to its DC gain only, denoted by  $G_p$ , since in our prototype it is much faster than the current sensor and the voltage amplifier.

Now the tunneling current can be obtained as a function of the distance between the tip and the sample surface [16], which can be expressed as:

$$d = z_s - z_t \tag{3}$$

where  $z_t$  refers to the vertical position of the tip, and  $z_s$  to that of the sample surface, both here considered downwards, with respect to a given reference (as in figure 3).



Figure 3: Tip and sample positions.

Formally, it is an exponential function of d, when d is small enough, as follows:

$$i_t(t) = gV_b exp(-kd(t)) \quad if \ d < d_i = 0 \qquad if \ d \ge d_i$$
(4)

where  $d_i$  is typically around 1 *nm*, *k*, *g* are positive constants depending on the materials (tip, sample), and  $V_b$  is the positive constant bias voltage which is applied (as shown in figure 1). Now using model (2) and piezo gain  $G_p$ , we have:

$$z_t = G_p u_a = G_p c_2 x_2 \tag{5}$$

As for  $z_s$ , it is clear that when operating at a fixed horizontal position of the tip (only vertical motion along *z* axis), then it is a constant  $z_{s0}$ . Notice that in a scanning mode, where the tip is moved in the horizontal direction above the sample, then  $z_s$  will change according to surface variations, that is  $z_s(t) = z_{s0} + \delta z_s(t)$ . Finally, tunneling current model becomes:

$$i_t(t) = \alpha exp(-\beta(\bar{\delta z}_s(t) - x_2(t))) \tag{6}$$

with  $\alpha := gV_b exp(-kz_{s0})$  (if *d* is kept below  $d_i$ ),  $\beta := kG_pc_2$  and  $\delta z_s := \frac{\delta z_s}{G_pc_2}$ .

The main modeling issue we consider is that of getting estimates for  $\alpha$  and  $\beta$ , which both contain parameters a priori unknown. To that end, we will consider a vertical motion operation only (that is with  $\delta z_s = 0$ ), with an appropriate control so that distance *d* allows for tunneling current, giving rise to an overall dynamical model as:

$$\dot{x}_1(t) = -a_1 x_1(t) + \alpha exp(\beta x_2(t)) \dot{x}_2(t) = -a_2 x_2(t) + u(t) y_m(t) = c x_1(t) + v_v(t)$$
(7)

where  $a_1, a_2, c$  are assumed to be known beforehand, and  $\alpha, \beta$  are to be identified.

We will also show how estimates of the latter can then be used to further determine  $\delta z_s$  in case of scanning, and thus the sample surface variations by using the knowledge on piezo and voltage amplifier gains  $G_p c_2$ .

But the preliminary step is to ensure that the tunneling current can indeed be established, and kept under control, prior to any estimation. This is studied in next section.

#### 3. Closed-loop operation with stability

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The purpose in this section, is to show how a simple PI controller can ensure tunneling current regulation with stability. To that end, let us first omit the measurement noise, and use the fact that the sensor dynamics are here faster than the voltage amplifier dynamics. This means that the output can be expressed as:  $y(t) := \frac{c}{a_1} \alpha exp(\beta x_2(t))$ , and model (7) can be reduced to the following one:

$$\dot{x}_{2}(t) = -a_{2}x_{2}(t) + u(t) y(t) = \alpha_{1}exp(\beta x_{2}(t))$$
(8)

with 
$$\alpha_1 := \frac{1}{a_1} \alpha$$
,  $a_2$ ,  $\beta$ , positive constants.  
It is also clear that a regulation target  $i_t^*$  on  $i_t$  directly translates  
into a regulation target  $y^*$  on  $y$ .  
We then have the following:

**Theorem 1.** Given a constant reference  $y^*$  for y in system (8), for any gains  $\lambda_0$ ,  $\lambda_1 > 0$ , and any initial condition in (8), the PI control law:

$$u(t) = -\lambda_0 \int_0^t (y(\tau) - y^*) d\tau - \lambda_1 (y(t) - y^*)$$
(9)

ensures that  $\lim_{t\to\infty} |y(t) - y^*| = 0$ .

**PROOF.** The result can be established by using Lyapunov arguments: notice first that the closed-loop system (8)-(9) can written as follows

$$\begin{aligned} \dot{x}_0(t) &= \alpha_1 \exp(\beta x_2(t)) - y^* \\ \dot{x}_2(t) &= -a_2 x_2(t) - \lambda_0 x_0(t) - \lambda_1 [\alpha_1 \exp(\beta x_2(t)) - y^*)] \\ (10) \\ \text{ith } x_0 &:= \int_0^t (y(\tau) - y^*) d\tau. \end{aligned}$$

Now set  $x_2^* := \frac{1}{\beta} log\left(\frac{y^*}{\alpha_1}\right)$ , and  $x_0^* := -\frac{a_2 x_2^*}{\lambda_0}$ . Then the closed-loop system can be restated in terms of errors  $\tilde{x}_0 := x_0 - x_0^*$  and  $\tilde{x}_2 := x_2 - x_2^*$  as:

$$\dot{\tilde{x}}_{0}(t) = \alpha_{1} \exp(\beta(\tilde{x}_{2}(t) + x_{2}^{*})) - y^{*} \dot{\tilde{x}}_{2}(t) = -a_{2}\tilde{x}_{2}(t) - \lambda_{0}\tilde{x}_{0}(t) - \lambda_{1}(\alpha_{1} \exp(\beta(\tilde{x}_{2}(t) + x_{2}^{*})) - y^{*})]$$
(11)

For this system, let us consider a candidate Lyapunov function of the form:

$$V(\tilde{x}) := \frac{1}{\beta} [\alpha_1 exp(\beta(\tilde{x}_2 + x_2^*)) - y^*] - y^* \tilde{x}_2 + \frac{\lambda_0}{2} \tilde{x}_0^2 \qquad (12)$$

where  $\tilde{x}$  gathers  $\tilde{x}_0$  and  $\tilde{x}_2$ .

Clearly V(0) = 0 and V is positive definite w.r.t.  $\tilde{x}_0$ . Let us now check that this also true for  $\tilde{x}_2$ , that is  $V_2(\tilde{x}_2) := \frac{1}{\beta} [\alpha_1 exp(\beta(\tilde{x}_2 + x_2^*)) - y^*] - y^* \tilde{x}_2$  is always positive when  $\tilde{x}_2 \neq 0$ .

Noting that  $y^* = \alpha_1 exp(\beta x_2^*)$ , by the mean value theorem, we have

$$V_{2}(\tilde{x}_{2}) = \alpha_{1} exp(\beta(x_{2}^{0}))\tilde{x}_{2} - y^{*}\tilde{x}_{2}$$
  
=  $\alpha_{1} [exp(\beta(x_{2}^{0})) - exp(\beta x_{2}^{*})]\tilde{x}_{2}$  (13)

with  $x_2^0$  lying between  $x_2^*$  and  $\tilde{x}_2 + x_2^* = x_2$ .

If  $x_2 < x_2^*$ , then  $x_2^0 < x_2^*$  and consequently  $exp(\beta(x_2^0)) < exp(\beta x_2^*)$ , while  $\tilde{x}_2 < 0$ , meaning that  $V_2(\tilde{x}_2) > 0$ .

Similarly, if  $x_2 > x_2^*$ , then  $x_2^0 > x_2^*$  and consequently  $exp(\beta(x_2^0)) > exp(\beta x_2^*)$ , with  $\tilde{x}_2 > 0$ , leading again to  $V_2(\tilde{x}_2) > 0$ . One can finally conclude that  $V_2$  is indeed positive definite.

So V is a positive definite function, obviously globally defined and radially unbounded. It is also globally differentiable, and we can compute:

$$\dot{V} = [\alpha_1 exp(\beta(\tilde{x}_2 + x_2^*)) - y^*] \times [-a_2 \tilde{x}_2 - \lambda_0 \tilde{x}_0 -\lambda_1 (\alpha_1 exp(\beta(\tilde{x}_2 + x_2^*)) - y^*)] +\lambda_0 \tilde{x}_0 (\alpha_1 exp(\beta(\tilde{x}_2 + x_2^*)) - y^*)$$
(14)

which gives

$$\dot{V} = -\lambda_1 \alpha_1^2 (exp(\beta(\tilde{x}_2 + x_2^*)) - exp(\beta x_2^*))^2 -a_2 \alpha_1 \tilde{x}_2 (exp(\beta(\tilde{x}_2 + x_2^*)) - exp(\beta x_2^*))$$
(15)

From this,  $\dot{V}$  is negative definite in  $\tilde{x}_2$  (it is clear that  $\tilde{x}_2$  and  $exp(\beta(\tilde{x}_2 + x_2^*)) - exp(\beta x_2^*)$  are of same signs).

Consequently, we get stability by Lyapunov's second method. We can finally conclude to (global) asymptotic stability by using La Salle's invariance principle (see e.g. [30]):  $\dot{V} = 0$  indeed means  $\tilde{x}_2 = 0$ , and this being constantly true in time means that  $\tilde{x}_0 = 0$  as well. Hence the set { $\tilde{x} \in \mathbf{R} : \dot{V}(\tilde{x}) = 0$ } contains no other solution than 0, and we can conclude that 0 is globally asymptotically stable.

Notice that if the presence of measurement noise is taken into account, a local version of this stability result can be established as well (that is when the output which is used is  $y_m$  as in (7)). In that case indeed, closed-loop system (11) becomes:

$$\begin{aligned} \tilde{x}_{0}(t) &= \alpha_{1} \exp(\beta(\tilde{x}_{2}(t) + x_{2}^{*})) - y^{*} + v_{y}(t) \\ \dot{\tilde{x}}_{2}(t) &= -a_{2}\tilde{x}_{2}(t) - \lambda_{0}\tilde{x}_{0}(t) \\ &-\lambda_{1}(\alpha_{1} \exp(\beta(\tilde{x}_{2}(t) + x_{2}^{*})) - y^{*})] - \lambda_{1}v_{y}(t) \end{aligned}$$
(16)

where  $v_y$  can be assumed to be a zero-mean white noise. This gives rise to a possible local representation of variations  $\delta \tilde{x}$  of  $\tilde{x}$  around 0 as:

$$\begin{split} \delta \tilde{x}_0(t) &= \alpha_1 \beta \delta \tilde{x}_2(t) + \nu_y(t) \\ \delta \tilde{x}_2(t) &= -a_2 \delta \tilde{x}_2(t) - \lambda_0 \delta \tilde{x}_0(t) - \lambda_1 \alpha_1 \beta \delta \tilde{x}_2(t) - \lambda_1 \nu_y(t) \\ \end{split}$$
(17)

Hence, mean values of  $\delta \tilde{x}_0$  and  $\delta \tilde{x}_2$  satisfy a second order noisefree linear state equation, for which 0 is obviously asymptotically stable for any  $\lambda_0$ ,  $\lambda_1 > 0$ .

It can also be noted that gain  $\lambda_1$  can increase noise effects in the closed-loop system, meaning that low values should be preferred.

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From the above stability analysis, one can finally conclude that no matter what are (positive) values of  $\alpha$ ,  $\beta$ , a proportional-integral control law stabilizes the operation at any desired value for the tunneling current, for any  $\lambda_0$ ,  $\lambda_1 > 0$ .

In practice, they can be tuned experimentally, or based on features of model (17) for instance. But the important point is that<sup>165</sup> this allows to settle experimental conditions for possible estimation of tunneling current model: use vertical motion to get

<sup>45</sup> the current, and use PI control to keep it under control. Next section is dedicated to the actual model estimation in such a context.

#### 4. Tunneling current parameter estimation

#### 4.1. Tunneling current model

- <sup>150</sup> Considering again model (7), and assuming some appropriate closed-loop operation for instance as in previous section, one can now focus on the estimation of parameters  $\alpha$ ,  $\beta$  in tunneling current model (6) (with  $\delta z_s = 0$  in the vertical operation case).
- To that end, the idea here is to proceed in two steps: first estimate the tunneling current itself, and then estimate its parameters  $\alpha$  and  $\beta$ .

*Tunneling current estimation.* For this first step, let us only consider the sensor model (1), for which the problem translates into *unknown input estimation*, where  $i_t$  is the unknown input. There are various possible approaches to solve it, and one can for instance use the so-called *control-based observer* method of [31], in a similar fashion as it was applied in [18] for surface reconstruction: the idea in short is to drive an observer copying the dynamics of (1), by its input copying  $i_t$ , in such a way that its output tracks the measured output  $y_m$ .

A simple control strategy for this tracking problem can clearly take the form of a Proportional-Integral one, giving rise to the following observer for  $i_i$ :

$$\begin{aligned}
\hat{x}_{0}(t) &= c\hat{x}_{1}(t) - y_{m}(t) \\
\hat{x}_{1}(t) &= -a_{1}\hat{x}_{1} + v(t) \\
v(t) &= -k_{0}\hat{x}_{0}(t) - k_{1}(c\hat{x}_{1}(t) - y_{m}(t)) \\
\hat{i}_{t} &= v(t)
\end{aligned}$$
(18)

for some  $k_0, k_1 > 0$ .

In the noise-free case, it has been shown in [31] that this system indeed provides an estimate  $\hat{i}_t$  for  $i_t$  as accurately as desired by appropriate tuning of  $k_0$ ,  $k_1$ .

In order to take noise into account, let us more precisely state the following:

**Proposition 1.** System (18) for model (1) (with  $i_t$  bounded) ensures that for any  $k_0 > 0$ ,  $k_1 \ge 0$ , and any initial conditions,  $\hat{x}_0$ ,  $\hat{x}_1$  remain bounded, and  $\hat{i}_t$  approaches  $i_t$  according to the following transfer functions:

$$\begin{aligned}
\hat{I}_{t}(s) &= F_{i}(s)I_{t}(s) + F_{\nu}(s)N(s) \\
with : \\
F_{i}(s) &= \frac{k_{1}cs + k_{0}c}{s^{2} + (a_{1} + k_{1}c)s + k_{0}c} \\
F_{\nu}(s) &= \frac{k_{1}s^{2} + (k_{1}a_{1} + k_{0})s + k_{0}a_{1}}{s^{2} + (a_{1} + k_{1}c)s + k_{0}c}
\end{aligned} \tag{19}$$

where s stands for Laplace variable, and  $\hat{I}_t$ ,  $I_t$ , N refer to Laplace transforms of  $\hat{i}_t$ ,  $i_t$ , v respectively.

The proof is obtained by direct computations, and the remark that for any positive  $k_0, k_1$ , all transfer functions only have poles with strictly negative real parts.

One can then notice that  $k_0$ ,  $k_1$  can be chosen according to desired tracking performances, with appropriate attenuation of noise effect. A simple tuning can for instance be as follows:

$$k_0 = \frac{a_1^2}{4c}, \quad k_1 = 0 \tag{20}$$

which yields a second order behaviour with characteristic polynomial

$$P(s) = s^2 + a_1 s + \frac{a_1^2}{4}$$

that is a natural pulsation equal to  $\frac{a_1}{2}$  and a damping coefficient equal to 1.

Notice that various other tuning strategies could be used, including  $H_{\infty}$  optimal design as in [32] for instance.

From this, the measurement noise effect can be attenuated on the tunneling current estimate (see also [33] for a subsequent interest in surface imaging). However if the noise level is low<sub>190</sub> enough, then this first estimation step can be skipped, and an estimate for tunneling current can simply result from approximation (8).

*Tunneling parameter estimation.* As soon as an estimate  $\hat{i}_t$  is obtained for tunneling current  $i_t$ , a new output can be built from 195 its Logarithm  $y_i := log(\hat{i}_t)$ .

From equation (6) indeed (with  $\delta z_s = 0$ ), we obviously have:

$$log(i_t) = log(\alpha) + \beta x_2 \tag{21}$$

and from dynamics of  $x_2$  in equation (7), we get:

$$\frac{dlog(i_t)}{dt}(t) = -a_2 log(i_t(t)) + a_2 log(\alpha) + \beta u(t) \qquad (22)^{200}$$

Setting  $\xi := \begin{pmatrix} log(i_t) \\ log(\alpha) \\ \beta \end{pmatrix}$ , we obtain a linear state equation of the

form

$$\dot{\xi}(t) = A(u(t))\xi(t) \tag{23}$$

with

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$$A(u(t)) = \begin{pmatrix} -a_2 & a_2 & u(t) \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

Now considering  $y_i = log(\hat{i}_t)$  as the measurement for this system, and the fact that  $\hat{i}_t$  approaches very well  $i_t$  after some transient (from equation (19)), a first order approximation allows to consider:

$$y_i(t) = \log(i_t(t)) + \delta(t) = C\xi(t) + \delta(t)$$
(24)

where  $C = \begin{pmatrix} 1 & 0 & 0 \end{pmatrix}$  and  $\delta$  is a disturbance due to possible mismatch between  $\hat{i}_t$  and  $i_t$  (formally indeed, if  $\hat{i}_t = i_t + \bar{\nu}$  for small disturbance  $\bar{\nu}$ , then  $log(\hat{i}_t) = log(i_t) + \frac{1}{i_t}\bar{\nu} + O(\bar{\nu}^2)$ ).

Since state-space representation (23)-(24) becomes linear timevarying whenever u is chosen, a Kalman observer can be directly designed to get estimates for  $log(\alpha)$  and  $\beta$ , with the following result:

Proposition 2. An observer for system (23)-(24) of the form:

$$\hat{\xi}(t) = A(u(t))\hat{\xi}(t) - K(t)[C\hat{\xi}(t) - y_i(t)]$$

$$K(t) = M(t)C^T/w$$

$$\dot{M}(t) = \gamma M(t) + A(u(t))M(t) + M(t)A^T(u(t))$$

$$-M(t)C^TCM(t)/w + V$$
(25)

ensures that:

(i) if  $\delta$  is a zero mean white noise of intensity  $\Delta$ , then  $(\hat{\xi}(t) - \xi(t))^2$  is minimized in mean value when  $\gamma = 0$ , V = 0,  $w = \Delta$ ;

(ii) if  $\delta$  vanishes, then  $\|\hat{\xi}(t) - \xi(t)\|$  exponentially decays to zero for any  $\gamma > 0$ , w > 0,  $V \ge 0$  whenever u is bounded and satisfies the regular persistency condition:

$$\exists T, \alpha > 0 \text{ and } t_0 \ge 0 \text{ s.t. } \forall t \ge t_0, \\ \int_t^{t+T} \Phi_u(\tau, t)^T C^T C \Phi_u(\tau, t) d\tau \ge \alpha I$$
<sup>(26)</sup>

where  $\Phi_u(t, \tau)$  is the transition matrix for (23).

(iii) if  $\delta$  is bounded, then  $\|\hat{\xi}(t) - \xi(t)\|$  remains bounded under same conditions as in item (ii) (ISS property of the error system w.r.t. input  $\delta$ ).

Item (*i*) is a direct consequence of Kalman result (see e.g. [34]), while items (*ii*) and (*iii*) result from the fact that under condition (26),  $M^{-1}$  can define a quadratic Lyapunov function for the error system (in  $\hat{\xi} - \xi$ ) [35, 36]. Notice that one could even enhance the estimation, by taking into account filter model of (19) for noise  $\delta$ . One can also im-

into account filter model of (19) for noise  $\delta$ . One can also implement a reduced order version of this observer (as in [37]) or a directly reduced design (as in [2]).

#### 4.2. Surface variation estimation

Let us finally notice here that whenever  $\alpha$  and  $\beta$  are estimated at a given horizontal position of the tip above the sample, then the tip can be moved in a scanning way, and the same observer approach allows to get an estimate for sample vertical variations  $\delta z_s$  with respect to the value of the original position. In that case indeed, the tunneling current will vary as in equation (6), which means that:

$$log(i_t(t)) = -\beta \bar{\delta z}_s(t) + \beta x_2(t) + log(\alpha)$$

Using again the dynamics of  $x_2$ , and considering that time variations of  $\delta z_s$  can be neglected for the observer design, we get a state equation as:

$$\dot{\bar{\xi}}(t) = \begin{pmatrix} -a_2 & -a_2\beta \\ 0 & 0 \end{pmatrix} \bar{\xi}(t) + \begin{pmatrix} \beta u(t) + a_2 log(\alpha) \\ 0 \end{pmatrix}$$
(27)

with  $\bar{\xi} = \begin{pmatrix} log(i_t) \\ \bar{\delta z}_s \end{pmatrix}$ .

Using again output equation (24), we obtain a linear model for which a Kalman observer can be again designed, with similar properties as in proposition 2 regarding the effect of mesurement disturbance.

More precisely, the observer can be built for model (27) restated as:

$$\begin{split} \dot{\bar{\xi}}(t) &= \begin{pmatrix} -a_2 & -a_2\hat{\beta} \\ 0 & 0 \end{pmatrix} \bar{\xi}(t) + \begin{pmatrix} \hat{\beta}u(t) + a_2 \widehat{\log(\alpha)} \\ 0 \end{pmatrix} + \delta_z(t) \\ y(t) &= \begin{pmatrix} 1 & 0 \end{pmatrix} \bar{\xi}(t) + \delta(t) \end{split}$$

where  $\hat{\beta}$  and  $\widehat{log(\alpha)}$  are the obtained parameter estimates, and  $\delta_z$  gathers the effects of possible estimation errors  $\delta_{\beta}$ ,  $\delta_{\alpha}$  on those parameters:  $\begin{pmatrix} (a_2 \delta z_s - u) \delta_{\beta} - a_2 \delta_{\alpha} \\ 0 \end{pmatrix}$ .

Here, clearly condition (26) is satisfied whenever  $\hat{\beta}$  has converged (or is replaced by its steady state estimate), and all properties of proposition 2 (*i*) to (*iii*) hold w.r.t. disturbance vector

 $\begin{pmatrix} \delta_z \\ \delta \end{pmatrix}$ . Finally, an estimate for  $\delta z_s$  can be obtained from the one

$$\delta z_s$$
 of  $\delta z_s$  as  $G_p c_2 \delta z_s$ .

The overall estimation methodolgy can be summarized by figure 4 hereafter.



Figure 4: Overall observer structure.

#### 5. Experimental results

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Let us illustrate here the proposed methodology with experiments on our prototype of figure 2. In this propotype, the known parameters of current sensor and voltage amplifier models (1), (2) can be summarized as in Table 1 below.

$a_1$	$26\pi \times 1e3$	$[s^{-1}]$
$a_2$	$8\pi \times 1e3$	$[s^{-1}]$
С	$8.17 \times 1e13$	$[V.A^{-1}.s^{-1}]$

Table 1: STM known parameters.

The approach consists in operating the STM in closed-loop to obtain tunneling current as discussed in section 3, and in such a way that the corresponding control signal u(t) satisfies condition (26) of proposition 2 in section 4, so that parameter esti-

mation can indeed be achieved.

Let us first point that an operation under a simple square reference profile for the output is appropriate for this estimation<sup>240</sup> purpose: in that case indeed, u chosen as in (9) will also clearly

have a square profile, and it can be checked that condition (26) is in its turn satisfied for system (23) in that case.
Let us then consider a closed-loop operation for vertical tip mo-

tion, with a Proportional-Integral controller as in proposition  $1,^{245}$  and with a square wave as a reference, of 1Hz, and varying between 0.25 and 2V.



Figure 5: Measured output under PI control (solid line) vs square wave reference (dotted line).

The PI parameters are chosen empirically as  $\lambda_0 = 1.5$ , and  $\lambda_1 = 0.007$  (much smaller than  $\lambda_0$ , as commented before). The corresponding regulation performance is shown in figure 5, with reference in dashed (red) line and output in solid (blue) line. The corresponding control input *u* is presented in figure 6. Notice that in order to better emphasize the proposed estimation methodology, some drift effects which are quite common with such devices [38] have been removed beforehand in those signals.



Figure 6: Control input under square reference variations.

The estimation step can then be addressed: first obtaining an estimate for tunneling current, via system (18), with parameters as in (20), and then estimating its parameters as in (25), here choosing empirically w = 0.04,  $V = Id_{3\times3}$ , and  $\gamma = 25$ . The corresponding results are displayed in figures 7 and 8 respectively (where  $\beta/a_2$  is shown instead of  $\beta$ , for scaling reasons).



Figure 7: Estimation result for tunneling current  $i_t$  under square reference variations.



Figure 8: Estimate for parameter  $log(\alpha)$  (top dashed line) and  $\beta/a_2$  (bottom solid line).

It can be seen that an estimate  $\hat{i}_t$  for tunneling current is<sup>285</sup> indeed very rapidly obtained, and estimates for its parameters converge to some steady values in less than one second: the estimate for  $log(\alpha)$  reaches the value of about -891, and that of  $\beta/a_2$  the value of 297.

In order to get some validation for those values, let us first underline that from the knowledge on piezo and voltage amplifier gains, we have  $G_p c_2/a_2 = 18$ , from which the tunneling exponential rate is identified as  $\hat{k} = 16.5$ , and this value is fully consistent with the one formerly obtained by some offline iden-

tification with the same prototype [22] (a theoretical value is about 20 [16]).

On the other hand, if we consider that g reduces to so-called conductance quantum equal to 77.5 $\mu$ S [16], we can get from

260  $\widehat{log}(\alpha)$  and  $\hat{k}$  (together with known bias voltage  $V_b$ , of about 1V here) an estimate for  $z_{s0}$ , and combine it with an estimate of  $z_t$ , which can be obtained from  $log(\hat{i}_t)$ ,  $\widehat{log(\alpha)}$  and  $\hat{\beta}$ , to get an estimate of the tip-sample distance: it is shown in figure 9, where it can be checked to be consistent with expected values (here

varying between about 0.8 and 0.65 nm).

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Figure 9: Estimated tip-sample distance under square reference variations.

Finally, in order to illustrate the possible estimation of surface variations with the same approach, such variations are simulated in the control values. This simulation is made so as to emulate surface variations consistent with graphite atom organization (see e.g. [14]), and with a scanning speed of about 100 nm/s: referring to the distance of about 250 pm between two atoms seen as at 'highest positions' in such a case, and a height variation in between chosen as 0.2 nm in view of typical STM pictures, the control used in the observer is modified as if the tip had to follow a sine profile variation with peak-to-peak magnitude of 0.2 nm, and frequency of 400 Hz.

The observer is then designed as in subsection 4.2, based on estimates of tunneling current and its parameters, and under the Kalman form of (25), keeping w = 0.04,  $V = Id_{3\times 3}$  and increasing  $\gamma$  to 25 × 1000 so as to make the observer fast enough. The corresponding estimation results are shown in figures 10 and 11: the first one presents the surface estimation vs its 'simulated' sine reference (where a zoom on very first times emphasizes the estimation speed), and the second one focuses on the related error (which can be seen to be roughly lower than 10% of the sine magnitude, as highlighted by dashed lines).



Figure 10: Estimated surface variations (solid line) vs its emulated sine wave (dashed line).

Remark. As an extension comment, let us notice that in the 290 case when parameter k may vary during scanning, as emphasized for instance in [12], the methodology here proposed could be adapted, by considering some updates of tunneling current parameters from time to time over the fly. By adjusting observer tuning coefficients indeed, estimates can in fact be ob-295 tained here in less than 0.01s (picking  $\gamma$  larger than 25x100 for instance), as illustrated by figure 12 hereafter. As a consequence, with a scanning rate of about 100 nm/s, current parameters could be adjusted about every nanometer. Going up to video rate, as dicussed in [39] for instance, can be part of future 300 developments.



Figure 11: Estimation error in surface variation estimation.



#### 6. Conclusion

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The problem of parameter estimation in tunneling current exponential model has been considered. Since obtaining tunneling current needs closed-loop operation prior to any pos-<sup>370</sup> sible identification, a stability analysis when using a simple Proportional-Integral controller has been first presented. On the basis of such an operation, an observer approach has then been proposed for the current model, further extended to sur-<sup>375</sup> face variations estimation. All the methodology has been illustrated with experimental data, and the use of such a calibration

approach will be next studied in various possible applications

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