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# applied optics

# Mixed scale dense convolutional networks for x-ray phase contrast imaging

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X-ray in-line phase contrast imaging relies on the measurement of Fresnel diffraction intensity patterns due to the phase shift and the attenuation induced by the object. The recovery of phase and attenuation from one or several diffraction patterns is a nonlinear ill-posed inverse problem. In this work, we propose supervised learning approaches using mixed scale dense (MS-D) convolutional neural networks to simultaneously retrieve the phase and the attenuation from x-ray phase contrast images. This network architecture uses dilated convolutions to capture features at different image scales and densely connects all feature maps. The long range information in images becomes quickly available, and greater receptive field size can be obtained without losing resolution. This network architecture seems to account for the effect of the Fresnel operator very efficiently. We train the networks using simulated data of objects consisting of either homogeneous components, characterized by a fixed ratio of the induced refractive phase shifts and attenuation, or heterogeneous components, consisting of various materials. We also train the networks in the image domain by applying a simple initial reconstruction using the adjoint of the Fréchet derivative. We compare the results obtained with the MS-D network to reconstructions using U-Net, another popular network architecture, as well as to reconstructions using the contrast transfer function method, a direct phase and attenuation retrieval method based on linearization of the direct problem. The networks are evaluated using simulated noisy data as well as images acquired at NanoMAX (MAX IV, Lund, Sweden). In all cases, large improvements of the reconstruction errors are obtained on simulated data compared to the linearized method. Moreover, on experimental data, the networks improve the reconstruction quantitatively, improving the low-frequency behavior and the resolution. © 2022 Optical Society of America

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### 30 1. INTRODUCTION

Phase sensitive x-ray imaging techniques with partially coherent 31 radiation permit a significant increase of sensitivity with respect 32 33 to x-ray tomography on the micro and nano scale. Phase contrast imaging is now widely used in material science and biomedical 34 imaging with coherent x rays. The intensity can be measured 35 at one or several propagation distances after the sample. The 36 nonlinear relationship between the attenuation and phase shift 37 induced by a sample and the measured intensity relies on the 38 Fresnel diffraction theory and sets a nonlinear ill-posed inverse 39 40 problem.

To obtain an approximate solution, direct inversion 41 42 approaches based on linearization of the forward problem have been proposed. The contrast transfer function (CTF) [1] 43 44 is one such method that allows to retrieve both attenuation and phase, while others rather rely on assumptions on relationships 45 between phase and attenuation [2,3]. Iterative methods are not 46 47 limited by these constraints; of those are techniques that retrieve the object by alternating projections on constraints between 48

the detector and object space [4]. These also include variational approaches based on the Fréchet derivative of the forward operator [5] in conjunction with the Landweber algorithm. This kind of algorithm permits a flexible inclusion of priors, based on nonnegativity or total variation, for example, but consider the attenuation and the phase as independent unknowns to retrieve. It has recently been extended to other iteration schemes such as iteratively regularized Gauss-Newton (IRGN) [6]. Deep learning methods have been much developed in recent years for signal processing tasks [7]. Recent approaches based on deep learning have yielded promising results for reducing the reconstruction error for several inverse problems [8,9]. Some approaches optimize a reconstruction network trained to map the measured data and the reconstructed image [10]. Several iterative schemes have been proposed using deep learning methods to improve the results obtained with classical iterative approaches for inverse problems [11,12]. Some deep learning architectures applied to the phase problem have been proposed, for instance, to learn a regularization into a CTF-based optimization algorithm [13].

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Others such as PhaseGAN [14] were able to recover both atten-68 uation and phase from a single measured intensity by including 69 explicitly the Fresnel propagator in the training. But few pro-70 posed to retrieve both attenuation and phase directly from the 71 diffraction patterns. Recently, a new network architecture-the 72 mixed scale dense (MS-D) network-has been proposed [15]. 73 This network has been used to improve the reconstruction 74 guality and produce more accurate results over traditional meth-75 ods and other convolutional neural networks for tomographic 76 reconstruction problems [16]. Therefore, the goal of this work 77 is to develop an end-to-end deep learning approach for phase 78 and attenuation retrieval from x-ray phase contrast images using 79 MS-D neural networks. We compare the reconstruction results 80 obtained with those given by the model-based CTF linear 81 82 approach. The network was trained on simulated data of objects consisting of combinations of one or several different homo-83 84 geneous materials at several signal to noise levels, involving a 85 single or several propagation distances.

The remainder of the paper is organized as follows: in 86 Section 2, we discuss the physical model of propagation based 87 x-ray phase contrast imaging, as well as direct reconstruction 88 methods, and we present the architecture of the network used. 89 In Section 3, we give a detailed description of the implemen-90 tation, including the data used for training. We also discuss 91 the reconstruction quality as well as post-processing of direct 92 reconstructions. Comparison of the results obtained with the 93 various methods for simulated and experimental data is shown. 94 95 In Section 4, we give conclusions about the results obtained and perspectives for future work. 96

#### 97 2. MATERIALS AND METHODS

In this section, we describe the direct problem for phase contrast
 imaging and present the CTF approach as well as the MS-D con volutional neural networks. Additionally, we detail the synthetic
 datasets used for training our networks.

#### 102 A. Direct Problem Definition

The interaction of a coherent and parallel x-ray beam with anobject is related to its complex refractive index:

$$n(x, y, z) = 1 - \delta_r(x, y, z) + i\beta(x, y, z),$$
(1)

105 where  $\delta_r$  is the refractive index decrement, and  $\beta$  is the absorp-106 tion index for the spatial coordinate (x, y, z). Both  $\delta_r$  and  $\beta$ 107 depend on the material as well as the x-ray wavelength  $\lambda$ . For 108 thin objects and straight-line propagation of the beam along the 109 propagation direction z, this interaction can be described by a 110 transmittance function T of the coordinates  $\mathbf{x} = (x, y)$ :

$$T(\mathbf{x}) = \exp[-B(\mathbf{x}) + i\varphi(\mathbf{x})] = a(\mathbf{x}) \exp[i\varphi(\mathbf{x})].$$
 (2)

111  $B(\mathbf{x})$  is the absorption and  $\varphi(\mathbf{x})$  the phase shift induced by 112 the object. The phase shift and the absorption are projections 113 of the absorption and refraction index, respectively, defined with

114 the following line integrals:

$$B(\boldsymbol{x}) = \frac{2\pi}{\lambda} \int \beta(\boldsymbol{x}, z) dz,$$
 (3)

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$$\varphi(\mathbf{x}) = \frac{2\pi}{\lambda} \int (1 - \delta_r(\mathbf{x}, z)) dz.$$
 (4)

In the framework of the Fresnel diffraction theory, letting the116beam propagate in free space over a relatively short distance117D after interaction with the object can be described as a 2D118convolution of the transmittance and of the Fresnel propagator119for a distance D:120

$$u_D(\mathbf{x}) = T(\mathbf{x}) * P_D(\mathbf{x}), \tag{5}$$

where

$$P_D(\boldsymbol{x}) = \frac{1}{i\lambda D} \exp\left(i\frac{\pi}{\lambda D}|\boldsymbol{x}|^2\right).$$
 (6)

The intensity measured at a distance D downstream of the122object is thus given by123

$$I_D(\boldsymbol{x}) = |\boldsymbol{u}_D(\boldsymbol{x})|^2 + \varepsilon(\boldsymbol{x}), \qquad (7)$$

where takes into account noise and artifacts due to the acqui-124 sition conditions. Estimating the phase shift from these 125 intensities, or diffraction patterns, is called phase retrieval. 126 The retrieved phase shift can be used in conjunction with 127 tomography to reconstruct the 3D refractive index. This process 128 is called 3D phase tomography or holotomography. Our aim 129 is to estimate both the phase and the attenuation from one or 130 several intensity measurements whether the object involves one 131 or several materials. 132

#### B. Contrast Transfer Function

The CTF method is based on an assumption of weak absorption and slowly varying phase shift:

$$B(\mathbf{x}) \ll 1, \quad |\varphi(\mathbf{x}) - \varphi(\mathbf{x} + \lambda D\mathbf{f})| \ll 1.$$
 (8)

The forward model is linearized by Taylor expanding the trans-136mittance function to the first order:137

$$T(\mathbf{x}) \approx 1 - B(\mathbf{x}) + i\varphi(\mathbf{x}).$$
(9)

Substituting into (7) and again keeping only first order terms 138 gives 139

$$\tilde{I}_D(\boldsymbol{f}) = \delta(\boldsymbol{f}) - 2\cos(\pi\lambda D|\boldsymbol{f}|^2)\tilde{B}(\boldsymbol{f}) + 2\sin(\pi\lambda D|\boldsymbol{f}|s^2)\tilde{\varphi}(\boldsymbol{f}),$$
(10)

where f is the variable in the Fourier domain,  $\delta(f)$  is the unit 140 impulse function,  $\tilde{B}(f)$  is the Fourier transform of the absorp-141 tion, and  $\tilde{\varphi}(\mathbf{f})$  is the Fourier transform of the phase. Although 142 this expression is obtained by assuming weak object interac-143 tion, it can be shown to be valid for weak absorption and slowly 144 varying phase. Since the phase contrast factor before  $\tilde{\varphi}(f)$  in 145 (10) has zero crossings, several distances have to be used to cover 146 as much of the Fourier domain as possible. Then, a linear least 147 squares optimization problem is considered, taking the different 148 distances into account with the minimization of the sum 149

$$\sum_{D} \left| 2\sin(\pi\lambda D |\boldsymbol{f}|^2) \tilde{\varphi}(\boldsymbol{f}) - 2\cos(\pi\lambda D |\boldsymbol{f}|^2) \tilde{B}(\boldsymbol{f}) - \tilde{I}_D(\boldsymbol{f}) \right|^2.$$
(11)

- 150 This can be solved simultaneously for  $\tilde{B}(f)$  and  $\tilde{\varphi}(f)$  by linear
- 151 least squares optimization. We then have two retrieval formulas

152 for both phase and absorption:

$$\tilde{B}(f) = \frac{1}{2\Delta + \alpha} \left[ A \sum_{D} \tilde{I}_{D}(f) \sin(\pi \lambda D |f|^{2}) - B \sum_{D} \tilde{I}_{D}(f) \cos(\pi \lambda D |f|^{2}) \right], \quad (12)$$

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$$\tilde{\varphi}(f) = \frac{1}{2\Delta + \alpha} \left[ C \sum_{D} \tilde{I}_{D}(f) \sin(\pi \lambda D |f|^{2}) \right]$$

$$4 \sum_{D} \tilde{I}_{D}(f) \cos(\pi \lambda D |f|^{2})$$
(60)

$$-A\sum_{D}\tilde{I}_{D}(\boldsymbol{f})\cos(\pi\lambda D|\boldsymbol{f}|^{2})\right],$$
 (13)

154 with the following coefficients:

$$A = \sum_{D} \sin(\pi \lambda D |\mathbf{f}|^2) \cos(\pi \lambda D |\mathbf{f}|^2)$$
$$B = \sum \sin^2(\pi \lambda D |\mathbf{f}|^2), \qquad (14)$$

$$C = \sum_{D} \cos^2(\pi \lambda D |\boldsymbol{f}|^2) \quad \Delta = BC - A^2,$$
 (15)

156 where the parameter  $\alpha$  is a Tikhonov regularization parameter.

157 Considering the case of a homogeneous object, characterized 158 by a fixed known  $\delta_r / \beta$  ratio of the induced refractive phase shifts 159 and attenuation, both the absorption and phase can be retrieved 160 from a single diffraction pattern [17,18].

## 161 C. Mixed Scale Dense Convolutional Neural162 Networks

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The MS-D neural network has recently been proposed [15]. 163 This network requires fewer trainable parameters and interme-164 diate images than encoder-decoder networks to obtain accurate 165 reconstruction results. The application to large images is pos-166 sible, and the amount of training images needed is reduced. 167 The MS-D convolutional neural network architecture has been 168 used to improve tomographic reconstruction from limited data. 169 170 This network gives more accurate reconstruction results than traditional methods or others convolution neural networks 171 [16]. MS-D networks are densely connected [19]: to compute 172 an image of a certain layer, all previous layer images are used 173 as input instead of only those of the previous layers. MS-D 174 networks use dilated convolutions to retain image features 175 at various scales. The scales are mixed by choosing adapted 176 177 dilation factor distributions to avoid the gridding effect [20]. With dilated convolutional filters, the long range information 178 179 in images becomes quickly available in early layers of network. Greater receptive field size can be obtained earlier, making it 180 possible to use this information to improve the results of deeper 181 layers. This feature seems in line with the action of the Fresnel 182 operator. 183

Each feature map is the result of applying the same set of operations to all previous feature maps: (1) dilated convolutions with  $3 \times 3$  filters with a dilation rate selected from the list 186  $[d_{\min}, d_{\min} + 1, \dots, d_{\max}], (2)$  summing resulting images, (3) 187 adding a constant bias, and (4) applying a rectified linear unit 188 (ReLU) activation function defined as  $\operatorname{ReLu}(x) = \max(0, x)$ . 189 Finally, the output of the network consists of a linear combina-190 tion of all feature maps generated and input channels, after the 191 application of the ReLU activation function. The weight of each 192 feature map, including input channels, is learned according to 193 the receptive field in the generated images that is in line with the 194 desired output. It means feature maps or input channels whose 195 receptive field is more in line with the desired output would be 196 given more weight in the final output formation in processing by 197 pointwise convolution. 198

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#### D. U-Net

The U-Net architecture was originally designed to solve seg-200 mentation problems [21]. It has been successfully used in image 201 reconstruction as a post-processing tool of direct reconstruction 202 in computed tomography [10]. U-Net is based on: (1) multi-203 level decomposition by dyadic scale decomposition based on 204 max pooling, so that the effective filter size in the middle layers is 205 larger than that of the early and late layers, and (2) multichannel 206 filtering, such that there are multiple feature maps at each layer. 207 More precisely, the U-Net architecture consists of downscaling 208 and upscaling parts that give it the U-shaped network structure. 209 The downscaling follows the typical architecture of a convo-210 lutional neural network. It consists of the repeated application 211 of convolutions with  $3 \times 3$  filters, each followed by a ReLU 212 activation function, batch normalization layer, and then a  $2 \times 2$ 213 max pooling operation with stride 2 for downsampling. At each 214 downsampling step, the number of feature channels is doubled. 215 On the other side, the upscaling part consists of an upsampling 216 of the feature map with a  $3 \times 3$  up-convolution that halves 217 the number of feature channels and a concatenation with the 218 correspondingly cropped feature map from the downscaling 219 path, from which we apply two convolutions with  $3 \times 3$  filters, 220 each followed by ReLU and batch normalization. At the final 221 layer, a  $1 \times 1$  convolution is used to learn a linear combination 222 of all feature maps to reach the desired output. The two main 223 parameters that influence performance are the number of down-224 scaling (and subsequent upscaling) operations and the number 225 of channels per feature map. 226

#### E. Datasets

To compare the performance of the MS-D network and the CTF, we generated synthetic x-ray phase contrast images. The x-ray energy was set to 13 keV for a wavelength of  $\lambda = 0.095$  nm, and the pixel size in object space was set to 6 nm. We created projection datasets from 3D objects created from random combinations of one to 10 shapes, consisting of either one homogeneous material (to create homogenous objects) or three different materials (to create heterogeneous objects). The refractive indices (1) used for the materials are given in Table 1.

The shapes used were ellipsoids and paraboloids with random positions and orientations. 2D analytical tomographic projections of the real and imaginary parts of the refractive

Table 1.Complex Refractive Index Materials at13 keV

Material	Symbol	$\mu(\text{cm}^{-1})$	$\frac{2\pi}{\lambda}\delta_r(\mathrm{cm}^{-1})$	$\delta_r/\beta$
Gold	Au	2790	11 395	8.16
Palladium	Pd	615	8 2 5 1	26.83
Zinc	Zn	859	5 270	12.27

index, corresponding to the phase (4) and the attenuation (3), 241 respectively, were obtained from the 3D objects for an image size 242 of  $2048 \times 2048$  pixels. Objects and projections were generated 243 using the software TomoPhantom [22]. Phase contrast images 244 were generated from the projection images according to (7) at 245 propagation distances D = [10.1, 15.5, 17.8, 19, 20.3]mm 246 and downsampled to  $512 \times 512$  to avoid aliasing in the calcu-247 lation of the diffraction patterns. The datasets were generated 248 249 using different levels of white Gaussian noise to yield a cer-250 tain peak to peak signal to noise ratio (PPSNR) in the longest distance. The noise level was kept the same at all distances, 251 corresponding to usual experimental conditions. We generated 252 two datasets. The first consisted of only homogeneous objects, 253 254 and the material used was gold, The second consisted of heterogeneous objects using the three materials given in Table 1. Each 255 dataset consisted of 12,000 pairs of five input images (phase 256 contrast images at different propagation distances) and two out-257 put images (attenuation and phase). From each dataset, 10,000 258 259 images were used for training, 1000 for validation during training, and 1000 for evaluation. An augmentation of the training 260 data was performed by random 90 deg rotations or flipping, to a 261 factor of two, yielding a total of 20,000 training images. 262

#### 263 **3. EXPERIMENTS**

For the simulations, we trained different MS-D networks 264 corresponding to different inputs: (1) a single diffraction pat-265 266 tern (the position closest to the focus among the five available, 267 i.e., D = 10.1 mm), (2) all five diffraction patterns, and (3) an initialization with the adjoint of the Fréchet derivative (see 268 Section 3.C). This was done for each dataset, i.e., for both 269 homogeneous and heterogeneous objects. Thus, a total six 270 MS-D networks were trained. Overall, we used the same MS-D 271 network architecture composed of 100 layers and  $3 \times 3$  dilated 272 273 convolutional kernel. The dilation rates were selected in the list [1, 2, ..., 10, 1, 2, ..., 10, 1, 2...]. The networks were 274 trained using the ADAM optimizer with  $l_2$  norm between labels 275 and predictions as a loss function. An independent set of image 276 277 pairs was used as a validation set to monitor the network quality during training and provide a stopping criterion. The network 278 279 parameters that yielded the lowest validation error were saved as output from the training procedure. 280

#### 281 A. Simulation Results

In this section, we evaluate the different trained MS-D networks on synthetic data. We compare results of trained MS-D
networks with the U-Net architecture and to CTF using the
normalized mean square error (NMSE) defined by

NMSE(x) = 
$$\frac{\|x - x_{\text{true}}\|_2}{\|x_{\text{true}}\|_2}$$
. (16)

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Table 2.	Normalized Mean Square Error and Standard
Deviation	(in %) for 1000 Test Images, Heterogeneous
Objects	

	# Distances	# Parameters	Attenuation	Phase
CTF	5	_	42.4 (19.7)	30.3 (8.99)
U-Net	5	$31 \times 10^{6}$	11.1 (12.3)	7.65 (9.35)
MS-D Net	5	$49 \times 10^{3}$	7.67 (10.6)	5.33 (6.74)
MS-D Net	1	$45 \times 10^3$	11.8 (9.05)	7.76 (6.36)

Table 3.Normalized Mean Square Error and StandardDeviation (in %) for 1000 Test Images, HomogeneousObjects

	# Distances	# Parameters	Attenuation	Phase
CTFHomo	5	_	13.5 (3.92)	13.5 (3.92)
CTFHomo	1	_	21.4 (14.0)	21.4 (14.0)
U-Net	5	$31 \times 10^{6}$	4.29 (4.82)	4.29 (4.82)
MS-D Net	5	$49 \times 10^{3}$	3.95 (4.41)	3.95 (4.41)
MS-D Net	1	$45 \times 10^{3}$	4.37 (5.50)	4.37 (5.50)

As quantitative measures of reconstruction quality, we computed the average NMSE on 1000 images that were not used in training or validation. In all cases, the regularization parameter for the CTF method was optimized upstream.

The results obtained on homogeneous objects are summarized in Table 3. The MS-D network correctly reconstructs the attenuation and phase as identical up to a constant factor, as can be seen in the identical reconstruction error in attenuation and phase. On the contrary, U-Net was not able to reconstruct both the attenuation and phase simultaneously. It retrieves only the phase while putting attenuation to zero. This is the reason that we trained only U-Net to output a single channel (phase), and consider the attenuation proportional to the phase, which explains the identical reconstruction error.

The results obtained on heterogeneous objects are summarized in Table 2. The MS-D network performs somewhat worse on heterogeneous objects because of the diversity of the dataset, but the results remain very good. We find that the network retrieves the phase somewhat better than the attenuation. For qualitative evaluation, some examples of reconstructed phase projections are displayed in Fig. 1.

#### **B. Experimental Results**

In this section, we apply the MS-D networks to experimental data [23] acquired at beamline NanoMAX at the MAX IV synchrotron (Lund, Sweden) [24]. The different diffraction patterns were magnified to have the same pixel size, which was measured to be 6 nm. The x-ray energy was set to 13 keV. The sample was placed at different positions relative to the focus and detector positions for different amounts of magnification and consequently different effective propagation distances corresponding to D = [10.1, 15.5, 17.8, 19, 20.3] mm. Those phase contrast images were not directly used as input; they were magnified to have the same pixel size (Fig. 2). The object in question represents a stack of gold, palladium, and zinc with thicknesses of 163 nm, 32 nm, and 10 nm, respectively; thus the expected values for attenuation and phase are 0.0483 and 0.217, respectively.



Fig. 1. Comparison of the different approaches on simulated heterogeneous objects.



Fig. 2. (A)-(E) Phase contrast images acquired at sample positions progressively further from the focus (and thus closer to the detector) showing the varying degree of magnification and phase contrast. (F)–(J) Phase contrast images magnified to have the same pixel size (6 nm).



Fig. 3. Comparison of the different approaches on experimental data when trained on heterogeneous objects.

The differents results in the case of heterogenous assump-323 tion are displayed in Fig. 3. We see that the CTF method 324 retrieved well the shape of the object but left artifacts on the 325

low-frequency range. On the other hand, U-Net seems to 326 reduce those artifacts but recovers the shape of the object somewhat roughly. The MS-D network reduces the artifacts while 328



**Fig. 4.** Comparison of phase reconstructions using the different approaches on experimental data when trained on homogeneous objects. (A) CTFHomo (five distances). (B) U-Net. (C) MS-D-Net (five distances). (D) CTFHomo (one distance). (E) MS-D-Net (one distance).

Table 4.	Reconstruction Quality for the Different Algorithms for Experimental Data when Traine	d on
Homogen	eous/Heterogeneous Data	

Heterogeneous						
		Atten	Attenuation		Phase	
	# Distances	NE (RSD) in %	Resolution (nm)	NE (RSD) in %	Resolution (nm)	
CTF	5	81.3 (177)	102	21.6 (30.0)	213	
U-Net	5	6.83 (35.5)	96	2.30 (16.0)	159	
MS-D Net	5	33.7 (40.6)	98	3.22 (14.2)	202	
MS-D Net	1	48.2 (32.0)	92	-11.5 (15.2)	208	
		]	Homogeneous			
		Atten	uation	Pł	lase	
	# Distances	NE (RSD) in %	Resolution (nm)	NE (RSD) in %	Resolution (nm)	
CTFHomo	5	4.14 (11.5)	197	4.14 (11.5)	197	
CTFHomo	1	25.3 (16.0)	128	25.3 (16.0)	128	
U-Net	5	14.7 (27.5)	140	14.7 (27.5)	140	
MS-D Net	5	2.03 (11.6)	165	1.84 (11.2)	165	
MS-D Net	1	2.96 (12.5)	93	2.76 (12.3)	93	

reconstructing well the shape of the object, even when a singledistance is given as input.

Assuming homogeneous object composition, we compare the homogeneous version of CTF with the networks. We see in Fig. 4 that both CTF and MS-D networks outperformed the U-Net approach, whether we use one or several distances. The MS-D network reconstructs with fewer artifacts in the low-frequency range than the linearized method, and both are able to recover well the shape of the object compared to U-Net.

For the experimental data, we used as quantitative evaluation
the normalized error (NE) and relative standard deviation
(RSD) calculated as

NE = 
$$\frac{l_t - l_m}{l_t}$$
 and RSD =  $\frac{s_m}{l_m}$ , (17)

where  $l_t$  is the expected value,  $l_m$  the measured mean value, 341 and  $s_m$  the standard deviation in the corresponding material. 342 343 Calculation of  $l_m$  and  $s_m$  was done inside the object to avoid the influence of blur at the edges. We also measured the resolution 344 by fitting an error function to a line profile across an object edge, 345 and then calculating the corresponding Gaussian full width at 346 half maximum (FWHM) based on the error function fitting 347 parameters [3]. The result for experimental data are presented in 348 Table 4. 349

For heterogeneous data, the CTF yields a reconstruction with strong low-frequency noise. All the networks achieve a quantitatively more accurate reconstruction than the CTF. Note that although U-net achieves the best reconstruction quantitatively in terms of reconstructed values, the reconstruction is qualitatively not as good: the shapes of the stars are not correctly reconstructed with some disconnections, rounded corners, and wavy contours. U-net also yields a better resolution since the reconstructions tend to approach a piecewise constant and thus work well for this particular sample.

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For homogeneous data, the CTFHomo algorithm yields a quantitatively very good reconstruction with some remaining low-frequency noise, and the edges are more blurred than in the reconstructions from the networks. It can be noted that this algorithm is perfectly adapted to the imaged object and that we explicitly give the  $\delta_r/\beta$  ratio as input, whereas the networks learn this parameter implicitly. Surprisingly, U-net does somewhat worse than for heterogeneous objects, again with some parts of the star incorrectly reconstructed, despite yielding a very clean background. The MS-D networks on the other hand yield very good reconstructions, using both five distances and a single distance.

Overall, the MS-D network when trained using a single distance propagation achieves better resolution than using several distances. This may be due to uncertainty in the measurement of the physical propagation distances and difficulty to exactly align this kind of phase contrast image. The same remark applies if we compare the results obtained by CTFHomo with one or five distances, albeit with greater improvement in quantitative results when using several distances.

Table 5.Normalized Mean Square Error and StandardDeviation for 1000 Test Images (in %), Initializedwith (19)

	Homogeneous		Heterogeneous	
	Attenuation	Phase	Attenuation	Phase
U-Net MS-D Net	9.60 (13.8) 1.96 (3.05)	4.74 (8.85) 1.96 (3.05)	16.2 (12.3) 8.19 (6.68)	5.77 (7.94) 4.83 (5.17)

#### 380 C. MS-D Network as Post-Processing

Finally, we trained the networks in the reconstruction domain
by performing a preliminary reconstruction by applying the
adjoint of the Fréchet derivative [5] of the forward operator (7)

$$\begin{bmatrix} I'_D(B,\varphi) \end{bmatrix}^* (u) = \left\{ \begin{bmatrix} \left( -ue^{B-i\varphi} * P_D \right) * \overline{P_D} \end{bmatrix} e^{-B+i\varphi}, \\ \times \begin{bmatrix} \left( ue^{B-i\varphi} * P_D \right) * \overline{P_D} \end{bmatrix} i e^{-B+i\varphi} \right\}$$
(18)

384 directly on the data as initialization.

The inputs to the networks then consist of the average of (18) over all distances at the point  $(B, \varphi) = (0, 0)$ :

$$(B_0, \varphi_0) = \sum_{i=1}^{N_D} \left[ I'_{D_i}(0, 0) \right]^* (I_{D_i}^{\text{obs}}).$$
(19)

Performing this operation before training allows us to take into
account prior knowledge on the physics of the inverse problem,
and transforms the input data to the same domain as the output.

On simulated data, we see that initializing with this direct
reconstruction using the adjoint of the derivative improves
the reconstruction quality of the phase, but makes the reconstruction quality of the attenuation somewhat worse (Table 5).
Initialization given by (19), as well as the reconstruction for the
networks are displayed in Fig. 5.

Quantitative evaluation of the networks on the experimental 396 397 data, trained by initializing with the adjoint of the derivative, are given in Table 6. When trained on heterogeneous data, the 398 399 MS-D network yields better reconstruction quantitatively and 400 in terms of resolution for the phase, while U-Net performs 401 better for the attenuation reconstruction, and the reconstructed images no longer show the artifacts mentioned in Section 3.B. 402 On the other hand, on homogeneous data, we see that the MS-403 D network yields a very good reconstruction quantitatively and 404 405 achieves better resolution than U-Net.

Table 6.Reconstruction Quality for the DifferentAlgorithms for Experimental Data when Trained onObjects Initialized with the Adjoint of Fréchet Derivative

Heterogeneous					
_	Attent	ation	Pha	ase	
	NE (RSD) in %	Resolution (nm)	NE (RSD) in %	Resolution (nm)	
Initialization	31.6(93.9)	371	22.5(19.6)	192	
U-Net	15.1(24.3)	72	7.37(12.9)	135	
MS-D Net -	-27.5(34.2)	107	-4.14(11.5)	116	

Homogeneous					
_	Attenuation		Phase		
	NE (RSD) in %	Resolution (nm)	NE (RSD) in %	Resolution (nm)	
Initialization	31.6(93.9)	371	22.5(19.6)	192	
U-Net MS-D Net	7.04(11.6) 1.45(7.18)	133 122	8.34(8.64) 1.38(7.15)	133 122	

#### 4. DISCUSSION

We used MS-D networks to perform attenuation and phase retrieval from x-ray in-line near-field phase contrast images. The network was trained and evaluated on simulated data with noise using relatively simple objects consisting of combinations of ellipsoids and paraboloids, involving one or several materials. None of the parameters of the physical model such as the energy of the x ray, propagation distance, or pixel size was given explicitly to the network. They were implicitly captured in the intensity images. The aim of the network was to learn an inverse without such information.

We illustrated the MS-D network's potential on synthetic data generated with *TomoPhantom* software and compared the results with the linearized CTF method and another neural network implementation using U-Net. The results are reported in Tables 2 and 3 and in Fig. 1. Both the MS-D network and U-Net performed better than the CTF method, both quantitatively and qualitatively. The MS-D network was able to retrieve both attenuation and phase from a single diffraction pattern with similar quality as U-Net when using five measured intensities. On homogeneous objects, the MS-D network retrieves phase and attenuation as identical up to a constant factor, which means that it learned the constant  $\delta_r/\beta$  ratio while U-Net did not. Since U-net yielded zeros in the attenuation channel, we



Fig. 5. Comparison of the different approaches on experimental data when initialized with the adjoint of Fréchet derivative.

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430 implemented a single output channel for this network and 431 calculated the corresponding attenuation image by multiply-432 ing with the  $\delta_r/\beta$  ratio. Both networks performed better than 433 the homogeneous version of CTF whose  $\delta_r/\beta$  ratio was given 434 explicitly. On heterogeneous objects, both networks performed 435 better than the CTF, and recovered the phase better than the 436 attenuation.

The different networks were also applied on experimental 437 data (Figs. 3 and 4, Tables 2 and 3). Although U-Net per-438 formed very well quantitatively-the reconstructed values 439 very close to the expected ones in the interior region of the 440 441 sample-qualitatively, it reconstructed the shape of the stars in an unsatisfactory manner with rounded corners, some dis-442 connections, and wavy contours. The low-frequency noise 443 444 compared to CTF reconstruction was substantially improved, however. On the other hand, the reconstructions from the 445 446 MS-D network, while yielding a quantitatively less accurate 447 reconstruction with some ringing artifacts in the background, 448 qualitatively reconstructed correctly the shape of the sample and 449 also improved substantially the low-frequency artifacts compared to the CFT. The MS-D network correctly reconstructed 450 the shape of the sample despite this kind of shape not being 451 explicitly present in the training data. Note that U-net used 452 approximately a factor 600 more coefficients than the MS-D 453 454 networks.

Additionally, we showed using the methods as post-455 456 processing of images from a simple direct reconstruction 457 using directly the adjoint of the Fréchet derivative. The results (Fig. 5, Table 5) show that the MS-D network performed better 458 than U-Net in this case. For U-net, the qualitative aspect of the 459 reconstruction was substantially improved, but quantitatively, it 460 performed somewhat worse. The MS-D network performance 461 462 was improved in all aspects using this initialization. For the presented data, the reconstruction using the MS-D network 463 trained on homogeneous objects and initialized as described 464 465 yielded the best reconstruction in quantitative terms.

#### 466 **5. CONCLUSION**

We used MS-D networks, an architecture of convolutional 467 468 neural networks, to perform phase retrieval from x-ray in-line phase contrast images. The MS-D network combines short and 469 470 long range information, which seems to be appropriate with respect to the action of the Fresnel propagator. We compared 471 the reconstruction results obtained with the MS-D network to 472 a classical linearized algorithm, the CTF method, as well as to 473 474 another deep learning method based on the U-net architecture. 475 The MS-D network performed better than the CTF and U-net on simulated data. 476

477 On simulated data, the MS-D networks give better recon-478 structions than the CTF method and U-Net, despite U-net 479 using a factor of 600 more parameters. Moreover, the MS-D networks were able to simultaneously reconstruct the phase and 480 481 attenuation of heterogeneous objects from a single distance, 482 with similar reconstruction errors to U-Net using five distances. The MS-D network was able to learn the correct  $\delta_r/\beta$  ratio 483 when trained on homogeneous data and performed better than 484 U-Net, despite that U-net was trained with a single output and 485 the correct  $\delta_r / \beta$  ratio was applied to this reconstruction. 486

On experimental data, all three methods performed well, with a trade-off between the high-frequency artifacts of neural networks and the low-frequency artifacts of CTF. When using networks trained on heterogeneous objects, the MS-D network and the CTF method give the qualitatively best reconstructions with the morphology of the object well preserved. The U-Net reconstruction, while quantitatively very accurate, was qualitatively less acceptable with some disconnections and less accurate reconstruction of the object shape. When using networks trained on homogeneous objects, the MS-D network yields qualitatively and quantitatively the best reconstruction, while U-Net performed somewhat worse, with some parts of the object not reconstructed and values in the interior reconstructed less accurately.

Finally, we compared networks trained in the image domain by making a simple initialization reconstruction using the adjoint of the Fréchet derivative. The MS-D network showed excellent performance for phase and attenuation retrieval on both experimental and simulated data and improved the reconstruction compared to both the CTF and U-net.

As with all learning approaches, the reconstruction quality is limited by the quality and precision of the training data. Here, the networks are dependent on the training data to learn different physical parameters such as energy, propagation distance, and pixel size. The implementation of the simulation might also introduce its own artifacts, for example, from implementation issues such as sampling and numerical precision, and from incomplete modeling of the physics, for example, not taking into account scattering in the sample [25]. In future work, we will consider including networks in iterative schemes that incorporate some knowledge of the direct model into a data driven model. This will be done by unrolling a knowledge-driven iterative scheme and replacing the iterations with CNNs taking into account the forward operator. We will also investigate the case of a partially known forward operator by including some of the physical parameters in the optimization scheme.

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**Disclosures.** The authors declare no conflicts of interest.

**Data availability.** Data underlying the simulated results presented in this paper can be generated using *TomoPhantom* software [22]. Data underlying the experimental results presented are available through the *PyPhase* package [26].

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