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Optimal Energy Storage System-Based Virtual Inertia Placement: A Frequency Stability Point of View

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Abstract-In this paper, the problem of optimal placement of 5 virtual inertia is considered as a techno-economic problem from a 6 frequency stability point of view. First, a data driven-based equiv-7 8 alent model of battery energy storage systems, as seen from the electrical system, is proposed. This experimentally validated model 9 10 takes advantage of the energy storage system special attributes to contribute to inertial response enhancement, via the virtual inertia 11 concept. Then, a new framework is proposed, which considers the 12 battery storage system features, including annual costs, lifetime and 13 state of charge, into the optimal placement formulation to enhance 14 frequency response with a minimum storage capacity. Two well-15 16 known dynamical frequency criteria, the frequency nadir and the rate of change of frequency, are utilized in the optimization formu-17 18 lation to determine minimum energy storage systems. Moreover, a 19 power angle-based stability index is also used to assess the effect of virtual inertia on transient stability. Sensitivity and uncertainty 20 21 analyses are further conducted to assess the applicability of the method. The efficiency of the proposed framework is demonstrated 22 on a linearized model of a three-area power system as well as two 23 nonlinear systems. Simulation results suggest that the proposed 24 method gives improved results in terms of stability measures and 25 26 less ESS capacity, when compared with other methods proposed in 27 the literature.

Index Terms—Optimal placement, frequency nadir, virtual
 inertia, energy storage systems, inertial response, rate of change
 of frequency, transient stability, uncertainty analysis, sensitivity
 analysis.

NOMENCLATURE

33	δ^s	Mechanical rotor angle (<i>rad</i>)
34	ω^s	Mechanical rotor angular speed (rad/s)
35	ω_0	Rated angular speed (<i>rad/s</i>)
36	$T_m(t)$	Mechanical input torque (<i>p.u.</i>)
37	$T_e(t)$	Electrical output torque (<i>p.u.</i>)
38	H	Inertia constant of the system (<i>s</i>)

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Inertia of ESS in area i(s) h_i 39 $h_{i.\;\mathrm{min}}'$ Minimum required ESS inertia, in compliance with 40 RoCof, in area i(s)41 $h_{i.\ \rm min}''$ Minimum required ESS inertia, in compliance with 42 frequency nadir, in area i(s)43 I(t)Impulse response of the system 44 P(n)Data sequence of interest 45 P_{in} Injected power of ESS to the host grid 46 KNumber of sinusoidal components in noise 47 Length of P(n)L48 Magnitude a_k 49 Φ_k Initial phase angle 50 Harmonic frequency in radius ω_k 51 Complex magnitude of the kth-harmonic A_k 52 Eigenvectors associated with the noise subspace s_i 53 Signal eigenvector e54 e^U Complex-conjugate transpose of e 55 Capital costs (\$/kW) C_{cap} 56 C_{PCS} Power conversion system costs (\$/kW)57 C_{stor} Storage section costs (\$/kWh) 58 Power balance costs (\$/kW) C_{BOP} 59 Charging /discharging time (h) t_{ch} 60 Operation and maintenance costs (\$/kW-yr) $C_{O\&M}$ 61 Annualized replacement costs (\$/kW-yr) $C_{R,a}$ 62 Annualized total capital costs (\$/kW-yr) $C_{cap,a}$ 63 Annualized life cycle costs (\$/kW-yr) $C_{LCC,a}$ 64 CRFCapital recovery factor 65 C_R Replacement costs (\$/kWh) 66 $C_{FOM,a}$ Fixed operation and maintenance costs (\$/kW-yr)67 $C_{VOM,a}$ Variable operation and maintenance costs (\$/kWh) 68 Number of discharge cycles per year 69 n_{cycle} Charging efficiency of the battery (%) ζ_c 70 Discharging efficiency of the battery (%) ζ_d 71 Power angle-based stability index 72 η

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I. INTRODUCTION

NERTIAL response is defined as the power associated with 74 changes in kinetic energy of synchronous generator rotors, in 75 response to frequency changes, which is fed(taken) to(from) the 76 grid [1]. Before reaction of traditional ancillary control loops, 77 this energy, provided by system inertia, is the key factor to 78 limit the power imbalance. System inertia has a major influence 79 on frequency stability and the associated rate of change of 80 frequency (RoCoF) and frequency nadir. 81

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Inverter-based renewable sources are increasingly replacing 82 synchronous generators, which in turn decrease overall system 83 inertia. The ever-growing number of frequency incidents, in 84 response to fluctuations of renewable power sources, accompa-85 86 nied with low level inertia feature jeopardize frequency stability 87 [2]–[4]. This motivates the need to develop advanced ancil-88 lary energy balancing services to control frequency changes. Paramount among these, is Virtual Inertia emulation which 89 mitigates undesired frequency dynamics. However, not only 90 insufficient level of inertia, but also its heterogeneous distri-91 92 bution together with time-varying inertia profiles may render frequency dynamics faster. These facts, along with the need to 93 economically keep system secure, make optimal placement of 94 virtual inertia a key factor [2]. This paper addresses the problem 95 of optimal placement of virtual inertia in power grids from a 96 97 fundamentally new perspective.

98 Effects of energy storage systems (ESSs) on frequency regulation have been studied in recent research works such as [5]-99 [7]. They deal with balancing of generation and load to maintain 100 a constant system frequency and to keep tie-line power flows at 101 102 scheduled values. These studies consider long term frequency 103 response as well as steady state metrics, while neglect inertia requirements and primary frequency as the main metrics utilized 104 for system resilience analysis. Some recent studies have inves-105 tigated the effect of low system inertia on frequency stability 106 [8]–[14]. In parallel with these efforts, recent research works 107 108 [15]–[21] demonstrate the way on which virtual inertia could be emulated in different ways, including appropriate control of 109 wind turbines and energy storage systems (ESSs). In [22], an 110 optimization framework to deal with various aspects of inertia 111 emulation and control including how inertia emulation impacts 112 113 system stability, and determining the best places to add virtual inertia is proposed. Some questions about the heterogeneous 114 inertial profiles and how the associated negative impacts are 115 reduced by inertia emulation has been raised in [11]. Poolla 116 et al. [2] and Farmer et al. [19] focus on H₂ performance metric 117 118 to determine optimal placement of virtual inertia. Determination 119 of the optimum size of battery to provide the primary frequency control is addressed in [23], [24]. In particular, ESSs do not 120 constantly participate in primary regulation, due to life-time 121 concerns. Instead, in practice, the ESSs are controlled in a hier-122 archical fashion, dispatched by an optimal function to guarantee 123 the State-of-Charge (SOC) and life-time constraints, which is 124 missed in the so far researches. Some research works, such as 125 [25], deal with optimal placement of virtual inertia in power 126 system considering network structure. It employs DC-power 127 flow to tackle network structure into formulation. 128

129 A main limitation of these approaches is the reliance on steady 130 state considerations. It is well known, however, that dynamical frequency indices, such as RoCoF and frequency nadir, are 131 important parameters in assessing frequency stability and the 132 133 activation of protection schemes. This paper re-formulates the virtual inertia placement problem in term of dynamical met-134 135 rics. Using this approach, the effects of virtual inertia on the frequency indices can be assessed using a dynamic equivalent 136 model obtained by mapping the electromechanical behavior of 137 ESSs onto a second-order synchronous generator (SG) model. 138

The main contributions of this paper can be summarized as 139 follows: 140

- An attempt is made to systematically represent the ESS dynamical behavior by a second-order SG model that extends previous work by the authors [15] on the emulation of virual inertia. Within this framework, a new signal processing technique, called MUltiple Signal Classification (MUSIC) algorithm is developed to derive the model.
- As formulating differential equations in the optimization problem is a hard task, a mathematical framework is proposed to represent dynamical metrics by algebraic inequality constraints. In particular, the present paper describes the complex optimization problem of virtual inertia placement by a new simple formulation.
- Since, the ESSs sizing is a difficult problem in practice, and considering the energy capacity, price, life-time and SOC may not be addressed by the proposed synchronous-based model; an attempt is made to tie the virtual inertia to the ESS features.

159

A. General Concept

The main step towards optimal placement of virtual inertia in 160 a power grid is to analyze its effects on the frequency stability 161 behavior. This could be visualized by appropriate modelling 162 of the virtual inertia. Generally, providing virtual inertia and 163 thereby contributing to the overall equivalent grid inertia could 164 be achieved by using the virtual synchronous generator (VSG) 165 concept. VSG relies on similar power-balance-based synchro-166 nization mechanism as SGs to realize such functionality [26], 167 which would be investigated for modeling purpose in this paper. 168

With synchronous generation being displaced with modern 169 power electronic based generation such a solar and wind gen-170 eration, the analysis of inertial response of variable resource 171 generation becomes of fundamental importance. Energy storage 172 systems can, in principle, provide most of its stored energy 173 to support frequency in an interconnected power system and 174 hence a set of large battery ESSs could play the same role as 175 SGs in the inertial response horizon. Conceptually, the charg-176 ing/discharging process of ESS can be interpreted as the initial 177 compensation of a disturbance by the stored kinetic energy of 178 a SG rotating mass. This means that, while the ESSs would be 179 triggered by a command signal, from frequency measurements, 180 for charging/discharging, a SG model could be used to represent 181 the associated dynamics. 182

The classical model of a SG is a second-order model of the 183 form 184

$$\begin{cases} \dot{\delta}^{s} = \omega^{s} (t) - \omega_{0} \\ H \dot{\omega}^{s} = T_{m} (t) - T_{e} (t) \end{cases}$$

$$\tag{1}$$

where δ^s, ω^s , and ω_0 are the mechanical rotor angle, the mechanical rotor angular speed and the initial angular speed, respectively; $H, T_m(t)$ and $T_e(t)$ are the inertia constant, mechanical input torque and electrical output torque, respectively [27].

Taking the slow electromechanical behavior of the battery 189 ESS into account, the associated dynamics could be represented 190 by (1). The problem of interest, however, is to calculate the 191 equivalent inertia constant and mechanical input torque. To deal 192 with this possibility, a data-driven approach in which uncertain 193 194 behavior of the ESS is inherently considered to provide complementary information for the swing equation model of (1), is 195 proposed. 196

197 *B. Data Driven-Based Equivalent Model:* To introduce the 198 proposed equivalent model, assume that the injected power of the 199 ESS to the host grid is a discrete-time signal P(n) of length *L*. Let 200 the time-varying signal P(n) be decomposed into *K* sinusoidal 201 components in noise, as [28], [29]:

$$P(n) = \sum_{k=1}^{K} a_k \cos(n\omega_k + \Phi_k) + w(n)$$
(2)

where, a_k , Φ_k , ω_k and w(n) are the magnitude and the initial phase angle, harmonic frequency in radius and additive white noise, respectively. In the model, a_k and ω_k are assumed to be deterministic and unknown, and Φ_k is unknown and assumed to be random and uniformly distributed in $[-\pi, \pi]$. Alternatively, the model (2) can be expressed in the form of noisy complex exponentials as [19]

$$P(n) = \sum_{k=1}^{K} A_k e^{(jn\omega_k)} + w(n)$$
(3)

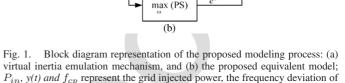
where $A_k = |A_k| e_k^{j\Phi}$ is the complex magnitude of the *k*thharmonic(noise) signal component. As the MUSIC algorithm is a noise subspace-based method, it is a good tool to deal with experimental noisy measured signals. Using this framework, the dimensional space is divided into signal and noise components, which is of high importance to accurately calculate *H* and $T_m(t)$ in (1).

The MUSIC method employs a harmonic model and estimates the frequencies and powers of the harmonics in the signal. Application of the MUSIC method to the data sequence, P(n), gives:

$$P_{MUSIC}\left(e^{j\omega}\right) = \frac{1}{\sum_{i=K+1}^{M} |e^{U}s_i|^2} \tag{4}$$

where the s_i are the eigenvectors associated with the noise 220 subspace that are orthogonal to the signal eigenvector $e = [1 e^{j\omega} e j^{2\omega} e^{j(M-1)\omega}]^{\mathrm{T}}$, and e^{U} denotes the complex-conjugate 221 222 transpose; M is the dimension of space spanned by P(n). It is 223 worth emphasizing that $P_{MUSIC}(e^{j\omega})$ in (4) does not relate to 224 225 any real power spectrum; rather, the only purpose of this pseudospectrum is to generate peaks whose frequencies correspond 226 to those of the dominant frequency components. This feature 227 makes the MUSIC approach interesting to develop equivalent 228 model based on dominant modes. 229

For a given signal of interest and according to (2)–(4), eigenvalues would be calculated. By knowing the eigenvalues and because the impulse response is the inverse Laplace transform of eigenvalues, one could represent a signal of interest with



f_{CP}

(a)

¥

Eqn. (5b)

Inverte

Control

Algorithm

Pseudo

spectrum (PS)

 P_{in} , y(t) and f_{cp} represent the grid injected power, the frequency deviation of the ESS, and the frequency at the point of connection of the ESS, respectively.

a pre-defined model of (1). For this purpose, suppose the impulse response of system is I(t); for the input signal x(t), i.e. 235 $x(t) = T_m(t)$ in (1), one could write y(t), i.e. $\dot{\omega}$, as: 236

$$y(t) = x(t) \int_{t=0}^{\infty} I(t) e^{j\omega t} dt$$
 (5.a)

where,

Storage

Energy

y(t)

Pin

$$I(t) = y(t) * PS \tag{5.b}$$

and *PS* in (5.b) is the pseudo-spectrum of the signal. Equation, (5.b) reveals that I(t) results from convolution of y(t) and PS. 239

In the modelling procedure and by measuring the output 240 response of the system y(t) and by knowing I(t), the problem 241 of interest is to calculate x(t) in (5). By calculating $T_m(t)$, the 242 ESS could be replaced by the synchronous generator model of (1). Using this approach, o in (5.a) is defined as the dominant 244 frequency components of the pseudo-spectrum in (4). 245

Figure 1 gives a schematic illustration of this model. In this plot, Fig. 1(a) illustrates the process of virtual inertia emulation using the battery ESS, while Fig. 1(b) describes a simplified 248 block diagram representation of the proposed equivalent model. 249 The input to the control algorithm is the frequency at the connection point of the inverter f_{cp} , and P_{in} represents the grid 251 injected power. 250

C. Model Validation: The efficiency of the proposed method is illustrated using the existing battery ESS in the University of Kurdistan Micro-Grid (UOK-MG). Fig. 2 shows a three-phase diagram representation of the UOK-MG. Details of the physical UOK-MG are given in [30].

Figure 3 shows the battery ESS and the main grid power variation behavior, i.e. P_{in} in Fig. 1, recorded for the UOK-MG. 259 As shown in Fig. 3, Event 1 triggers the charging process of the ESS in response to deviations from the minimum SOC. 261

The main grid power deviation during the charging process in Fig. 3 is utilized to calculate the Pseudo-spectrum (see Fig. 4) which, in turn, is used to estimate the dominant frequency components in (4).

237

Power grid

Eqn. (5a)

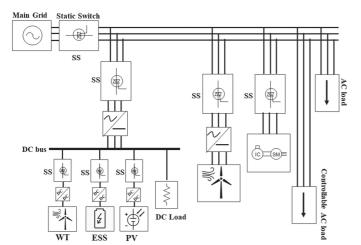


Fig. 2. Three-phase schematic representation of the UOK-MG.

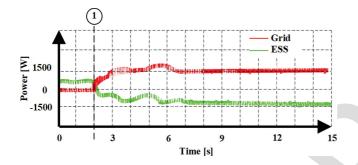


Fig. 3. The ESS and grid experimental dynamic responses.

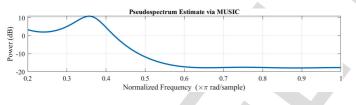


Fig. 4. The Pseudospectrum estimation via MUSIC.

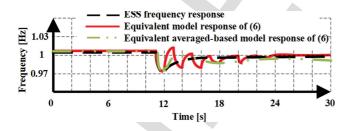


Fig. 5. Comparison of frequency response computed from the experiment and the equivalent frequency response models.

Setting the frequency deviation of the ESS in Fig. 5 as y(t)and the Pseudo-spectrum of Fig. 4 as *PS* for (5) gives:

$$\begin{cases} \dot{\delta}^{s} = \omega^{s} - \omega_{0} \\ 0.53\dot{\omega}^{s} = \left(1 - e^{-0.38t}\right)C - T_{e}\left(t\right) \end{cases}$$
(6)

where, *C* is a constant value and would be set to fit the DC term in
(4). In interpreting this model, note that constant 0.38 in (6) represents the dominant frequency of the Pseudo-spectrum in Fig. 4

which would be fed to (5) to calculate the 0.53 s inertia constant 271 in (6). Figure 5 demonstrates the effectiveness of the equivalent 272 model (6) to approximate the inertial response behavior of the 273 ESS. To exactly mimic frequency behavior of ESS using (6), the 274 oscillatory behavior of the adopted model would be removed 275 using a 20-samples rolling-averaging window. This approach 276 averages the long-term oscillations, and hence, mitigates the 277 oscillatory behavior beyond the inertial response horizon. 278

Results in Fig. 5 show that the dynamic behavior of ESS, 279 especially in the inertial response horizon can be approximated 280 by a simple SG model. It should be emphasized that while a 281 conventional SG is slower and less flexible compared to ESS, 282 developed dynamical equivalent model of ESSs in the grid 283 connected mode is not only affected by the fast-inherent features 284 of ESSs but also is significantly influenced by the external zone, 285 i.e. the host grid, features. 286

III. OPTIMIZATION PROBLEM 287

This section formulates the ESS placement as an optimal techno-economic problem.

A. Costs of Energy Storages and Technologies 290

There are two main approaches for assessing the cost of 291 storage technologies: 1) Total Capital Cost (TCC), and 2) Life 292 Cycle Cost (LCC) [31]. For the sake of generality of the method, 293 no specific ESS technologies are considered in this section. 294

In the TCC approach, all terms associated with the purchase, installation, and delivery of the ESS units, including Power Conversion System (PCS) costs (C_{PCS}), costs of ESS (C_{stor}), and cost of balance of plant (C_{BOP}), are considered as: 298

$$C_{cap} = C_{PCS} + C_{BOP} + C_{stor} \times t_{ch} \quad (\$/kW) \quad (7)$$

where t_{ch} is the charging /discharging time. The balance of the 299 ESS, known as the BOP, includes site wiring, interconnecting 300 transformers, and other additional ancillary equipment and is 301 measured on a \$/kW basis [32]. 302

However, the LCC is a more common metric to evaluate 303 and compare different ESS technologies. The annualized LCC 304 is formulated according to (8) which considers operation and 305 maintenance costs $(C_{o\&M,a})$, replacement cost $(C_{R,a})$ and annualized TCC. 307

$$C_{LCC,a} = C_{cap,a} + C_{O\&M,a} + C_{R,a} \quad (\$/kW - yr) \quad (8)$$

308

in which:

(

$$CRF = \frac{i(1+i)^{T}}{(1+i)^{T} - 1}$$
(9)

$$C_{cap,a} = TCC \times CRF \quad (\$/(kW - yr)) \tag{10}$$

$$C_{O\&M,a} = C_{FOM,a} + C_{VOM,a} \times n_{cycle} \times t_{ch} (\$/kW - yr)$$
(11)

$$C_{R,a} = CRF \times \sum_{k=1}^{r} (1+i)^{-kt} \times \left(\frac{C_R \times t_{ch}}{\eta_{sys}}\right) (\$/kW - yr)$$
(12)

where *CRF*, *i*, *T*, *r*, *t*, and η_{sys} are the capital recovery factor, interest rate and the life time, the number of substitutions in lifetime, the replacement period and the overall efficiency, respectively; $C_{FOM,a}$ and $C_{VOM,a}$ define the fixed and variable operation and maintenance costs. Subscript "a" stands for "annualized" costs.

315 B. Formulation of Objective Function and Constraints

Equation (8) specifies the annual cost per kilowatt of the installed ESS in compliance with the lifetime. However, for optimal placement of virtual inertia, it is necessary to rewrite the cost function in (8) according to the amount of virtual inertia.

The synchronous inertia constant (H) is defined as the ratio of stored kinetic energy to the rated apparent power of the system, as:

$$H = \frac{0.5 J_{VI} \,\omega^2}{S_{base}} \tag{13}$$

where J_{VI} , ω , and S_{base} are the moment of inertia, angular velocity and rated apparent power, respectively. Since the stored energy in ESSs is usually expressed in volt ampere hour (VAh_{ESS}) , it is needed to express the associated value in term of Joule. Considering unity power factor, one could re-write (13) as:

$$KW_{ESS} = KVA_{ESS} = \frac{h_{ESS}S_{base}}{3600 \ s} \rightarrow h_{ESS} = \frac{3600 \ VAsec_{ESS}}{S_{base}}$$
(14.a)

This equation gives the average hourly power that can be injected/absorbed to/from the grid by the ESS. To validate such representation, results obtained from (14.a), for frequency response of Fig. 5, are compared with those of well-established methods of calculating inertia. Using the classical swing equation during 500 ms after fault occurrence, one can conventionally calculate inertia constant as [33]:

$$H_{Conv.} = \frac{\Delta P_L}{2RoCoF_{500ms}} = \frac{\Delta P_L}{2\left(\frac{f(0.5) - f(0)}{0.5}\right)}$$
(14.b)

A comparison with the frequency responses of Fig. 5 shows an error of 3.17% which in turn justifies the proposed formulation in (14.a).

By substituting (14.a) into (8), one could write the optimization problem as:

$$\underset{h_i}{\text{minimize}} \quad F(h_i) = \sum_{i=1}^{n_{ESS}} \left(C_{LCC,a\ i} \times \frac{h_i\ S_{base}}{3600\ \text{sec}} \right) \quad (15.a)$$

:
$$RoCoF_i \le RoCoF_{\max}$$
 (15.b)

$$\Delta f_{\text{nadir }i} \le \Delta f_{nadir \ max} \tag{15.c}$$

$$SOC_{\min} \le SOC_i \le SOC_{\max}$$
 (15.d)

where n_{ESS} is the number of ESSs. Moreover, the SOC should remain within an appropriate range which is addressed in (15.d).

st

The SOC can be calculated as follows [34, 35]

$$SOC(\Delta t) = SOC(0) - \frac{\int_0^{\Delta t} \zeta p(t) dt}{E_{ESS,rated}}$$
(16.a)

where,

$$\zeta = \begin{cases} \zeta_c & P(t) < 0\\ \frac{1}{\zeta_d} & P(t) > 0 \end{cases}$$
(16.b)

and p(t) is battery power which gets negative values for the charging procedure and positive values for the discharging period; $E_{ESS,rated}$, Δt , ζ_c , and ζ_d are the nominal energy capacity, charge/discharge time, charging and discharging efficiencies of the battery, respectively. 349

C. Determining the Bounds of Virtual Inertia 350

Constraints (15.b) and (15.c) explain that the optimization 351 problem (15) enforces the RoCoF and frequency nadir in all 352 areas to be less than standard values. These terms make the 353 optimization problem difficult to deal with as it depends on 354 dynamical indices. Generally, it is common to specify the 355 lower/upper bounds based on different criteria, including capac-356 ity of equipment or budget. Therefore, the problem of interest 357 here is to re-write the upper and lower bounds of (15.b) and 358 (15.c) in terms of the emulated inertia, i.e. h. 359

Rate of Change of Frequency: The RoCoF is a meaningful
 criterion to show ability of a system in the face of a sudden
 power imbalance. Greater RoCoF means that the less time is
 available for system operator to arrest frequency decline [36].
 Time interval of 100 milliseconds to 2 seconds are defined to
 measure the RoCoF [36], [37]. ENTSO standard [37] explains
 that RoCoF is allowed to get a value between 0.5 to 1 Hz/sec.

In order to represent dynamical frequency indices based on lower bounds of inequality constraints of (15.b), the RoCoF 368 would be defined based on the classical swing equation of (1) 369 as [30]: 370

$$2H\frac{d\Delta f(t)}{dt} = \Delta P_m(t) - \Delta P_L(t) - \Delta P_{tie}(t) \qquad (17)$$

Where $\Delta P_m(t)$, $\Delta P_L(t)$, and $\Delta P_{tie}(t)$ represent mechanical 371 power, electrical power and tie line power changes, respectively. 372 Considering the definition of RoCoF, one could write: 373

$$RoCoF = \frac{\Delta P_m(t) - \Delta P_L(t) - \Delta P_{tie}(t)}{2H}$$
(18)

The Taylor series expansion of (18) about the independent 374 variables of H, ΔP_m , ΔP_L , and ΔP_{tie} gives 375

$$\Delta RoCoF_{i} = \frac{\partial RoCoF_{i}}{\partial \Delta P_{mi}} \Delta \Delta P_{mi} + \frac{\partial RoCoF_{i}}{\partial \Delta P_{Li}} \Delta \Delta P_{Li}$$

$$+ \frac{\partial RoCoF_{i}}{\partial \Delta P_{tiei}} \Delta \Delta P_{tiei} + \frac{\partial RoCoF_{i}}{\partial \Delta H_{i}} \Delta H_{i} = \frac{1}{2H_{i}} \Delta \Delta P_{mi}$$

$$+ \frac{-1}{2H_{i}} \Delta \Delta P_{Li} + \frac{-1}{2H_{i}} \Delta \Delta P_{tiei}$$

$$+ \frac{-(\Delta P_{mi} - \Delta P_{Li} - \Delta P_{tiei})}{2H_{i}^{2}} \Delta H_{i}$$
(19)

344

Due to the slow inherent of dynamics of interest, except for the last term of (19), other terms could be neglected. Accordingly, and by replacing (18), one could re-write (19) as:

$$RoCoF_i\left(-\frac{\Delta H_i}{H_i}\right) = \Delta RoCoF_i$$
 (20)

Considering maximum allowable RoCoF, i.e. $RoCoF_{i,max}$, the minimum inertia which guarantees the RoCoF to be within the permitted range is calculated as:

$$h'_{i,\min} = \Delta H_{i,\min}$$

$$= H_i \left(-\frac{\Delta RoCoF_{i,\max}}{RoCoF_i} \right) \xrightarrow{\Delta RoCoF_{i,\max} = RoCoF_{i,\max} - RoCoF_i}{NoCoF_i}$$

$$h'_{i,\min} = H_i \left(-\frac{RoCoF_{i,\max} - RoCoF_i}{RoCoF_i} \right)$$
(21)

where, $h'_{i,\min}$ represents the minimum, in compliance with the RoCof, required inertia which should be emulated by the battery ESS in area *i*. It equals to the difference between the desired inertia to enforce system to follow the standards and the present inertia constant, i.e. $\Delta H_{i,\min}$.

Frequency Nadir: Frequency nadir mainly depends on the
total inertia of the system and the capability of the power resources to provide primary frequency response [38]. According
to NERC and the Union for the Coordination of the Transmission
of Electricity (UCTE) standards [39, 40], the minimum allowable frequency that a system could instantaneously experience
during the operation is 800 mHz.

Taking the time dependency of the governor response into account, one can write the frequency nadir as [15]:

$$\Delta f_{nadir} = \frac{(\Delta P_L + \Delta P_{tie})^2 T_d}{4HR}$$
(22)

396 where R is the extra power received through the governor and 397 T_d is the response time of the governor. In deriving (22), it is assumed that the mechanical power through the governor 398 increases as a linear function of time with the steady gradient 399 R/T_d [41, 42]. While, this is a conservative assumption, Great 400 Britain and Ireland practices show that this is the case for the 401 power increment within 5 and 10 seconds (T_d) , respectively, 402 following a contingency [43]. Applying Tayloras expansion to 403 (22) gives 404

$$\Delta\Delta f_{nadir,i} = \frac{\partial\Delta f_{nadir,i}}{\partial\Delta P_{Li}} \Delta\Delta P_{Li} + \frac{\partial\Delta f_{nadir,i}}{\partial\Delta P_{tie,i}} \Delta\Delta P_{tie,i}$$
$$+ \frac{\partial\Delta f_{nadir,i}}{\partial\Delta H_i} \Delta H_i = \frac{(\Delta P_{Li} + \Delta P_{tiei}) T_{di}}{2H_i R_i} \Delta\Delta P_{Li}$$
$$+ \frac{(\Delta P_{Li} + \Delta P_{tiei}) T_{di}}{2H_i R_i} \Delta\Delta P_{tiei}$$
$$+ \frac{-(\Delta P_{Li} + \Delta P_{tiei})^2 T_{di}}{4H_i^2 R_i} \Delta H_i$$
(23)

Following the same procedure as that in (21), one could rewrite (23) in the form 405

$$\Delta f_{nadir,i} \left(-\frac{\Delta H_i}{H_i} \right) = \Delta \Delta f_{nadir, i} = \Delta (f_{nadir, i} - f_0)$$
(24)

The minimum inertia, i.e. $h''_{i,\min}$, which guarantees frequency 407 nadir to be in the permitted range is calculated by: 408

$$h_{i,\min}'' = \Delta H_{i,\min} = H_i \left(-\frac{\Delta \Delta f_{nadir \ i, \ max}}{\Delta f_{nadir \ i}} \right)$$
$$= H_i \left(-\frac{f_{nadir \ max} - \Delta f_{nadir \ i}}{\Delta f_{nadir \ i}} \right)$$
(25)

where, $h_{i,\min}''$ represents the minimum, in compliance with frequency nadir, required inertia which should be emulated by the battery ESS in area *i*. In order to simultaneously satisfy both, frequency nadir and RoCoF standards, the lower bound for virtual inertia in the optimization problem and for each area are selected as the maximum value of (21) and (25), namely: 409 410 411 412 413 414

ŀ

$$h_{i,\min} = max\left\{h'_{i,\min}, h''_{i,\min}\right\}$$
(26)

415

Moreover, the overall system inertia has a direct impact on the 416 frequency indices. This means that some considerations should 417 be made regarding overall system inertia and, consequently, 418 (21) and (25) would be completed by adding a new equality 419 constraint. For this purpose, the frequency of the overall Center 420 of Inertia (COI), which should satisfy strict frequency standards, 421 would be employed to determine the overall amount of inertia 422 in the system, as [5]: 423

$$H_{COI} = Q = H \frac{\Delta f_{COI}}{f_{COI}} (61.5) \tag{27}$$

$$\underset{h_i}{\text{minimize}} \quad F(h_i) = \sum_{i=1}^{n_{ESS}} \left(C_{LCC,a\ i} \frac{h_i \ S_{base}}{3600 \text{ sec}} \right)$$
(28.a)

st:
$$H_{COI} = Q$$
 (28.b)

$$h_{i,\min} \le h_i \le h_{i,\max}$$
 (28.c)

$$SOC_{\min} \le SOC_i \le SOC_{\max}$$
 (28.d)

where the dynamic inequality constraints (15.b) and (15.c) are 431 re-formulated as the algebraic inequality constraint (28.c) in 432 terms of the inertia constant. This dramatically increases the 433 simplicity and speed of the calculations. 434

In this section, a framework that incorporates the model (6) 436 and the objective function (28) to optimally place battery ESS 437 in the system is proposed. 438

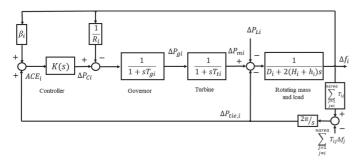


Fig. 6. Block diagram representation of control area *i*. β_i , R_i , T_{gi} , T_{ti} , and D_i are frequency bias, droop characteristic, governor time constant, turbine time constant, and damping property, respectively.

439 The algorithm consists of 4 main steps:

440 *Step 1:* Define PV buses of the system as candidates for battery
441 ESSs placement;

Step 2: Assume the proposed model (6), with unknown inertiaconstant, in each PV bus;

444 *Step 3:* Define the emulated inertia constant, i.e. h, as a decision 445 variable of the objective function (28). Set C in (6) as the 446 product of the ratio of h to the inertia constant of the installed 447 SG, in the associated bus, and the mechanical power of the

tion problem (28). Indeed, the GA determines the amount of
 virtual inertia in each PV bus of the system.

V. SIMULATION AND RESULTS

Three test systems have been used for evaluating the proposed
formulation in this paper: a) a linearized model of a three-area
power system, b) a nonlinear yet simple two-area, four-machine
test system, and c) a large scale16-machine, five-area 68-bus test
model of the New York/New England system.

458 A. Linear System

452

As a first motivating example, a linearized model of a threearea power system is used to assess the efficiency of the proposed
formulation. The block diagram of each area is shown in Fig. 6.

Firstly, a 0.2 per unit load disturbance is applied at areas 1 462 and 3. As a first scenario, the required virtual inertia is calculated 463 only based on (28.b) and arbitrary realized, through the proposed 464 465 model in (6), in area 1. For simulation purposes, it is assumed that the ESS would be triggered upon occurrence of the fault. 466 Comparison of frequency dynamics for the system with and 467 without virtual inertia reveals that while areas 1 and 2 frequency 468 nadirs improved by means of virtual inertia, area 3 shows an 469 undesired behavior. This in turn numerically justifies the need 470 for optimal inertia placement. Within this framework, (28) may 471 be written as: 472

minimize
$$F(h_i) = \sum_{i=1}^{n_{ESS}} \left(C_{LCC,a\ i} \frac{h_i S_{base}}{3600 \text{ sec}} \right)$$
 (29.a)

st:
$$H_{COI} = 0.053$$
 (29.b)

 TABLE I

 Optimization Results in Three Area System

Method	h1	h2	h3	$F(h_i)$
PM^*	0.016	0	0.037	2.5916
Ref. [2]	0.023	0.016	0.022	3.0942
Ref. [44]	0.012	0.009	0.038	2.8735

a.PM: Proposed Method

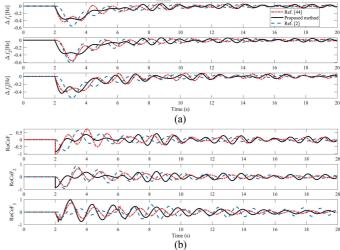


Fig. 7. (a) Frequency behaviors and (b) RoCoF of generators 1, through 3 of three area power system for three cases: proposed formulation, Ref. [44] and Ref. [2].

$$0.0129 \le h_1$$
 (29.c)

$$0 \le h_2 \tag{29.d}$$

$$0.0225 \le h_3$$
 (29.e)

$$30\% \le SOC_i \le 80\% \tag{29.f}$$

where, for instance, the minimum inertia of area 1 in (29.c) is 473 calculated based on (21),(25), and (26) as: 474

$$h'_{1,\min} = 0.08335 \times \left(-\frac{1+1.1870}{-1.1870}\right) = 0.0129$$

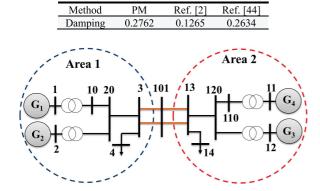
$$h''_{1,\min} = 0$$

$$h_{1,\min} = \max\left\{0, 0.0129\right\} = 0.0129$$
(30)

Note that some other unspecified parameters of (29) would 475 be set as described in Appendix A. The results obtained, using 476 a simple GA with 0.05 and 0.8 mutation and crossover coef-477 ficients, respectively, from optimization of (29) are shown in 478 Table I. In order to further assess efficiency of the proposed 479 formulation, Table I compares the results with those of ob-480 tained from [2] and [44]. Comparison results justify the fact 481 that dynamic behavior of ESS could significantly affect optimal 482 placement problem which is missed in previous research. 483

Figure 7 compares the frequency behavior and RoCoF of generators 1, 2 through 3 for three cases of interest: a) with virtual inertia and according to the proposed formulation, b) with virtual inertia and according to [44], and c) with virtual inertia and according to [2]. It can be seen that while frequency traces

TABLE II MODAL ANALYSIS OF THE SYSTEMS WITH VI



Single-line diagram of two area system. Fig. 8.

of [2], [44] and the proposed method in this paper follow the 489 standards regarding RoCoF and frequency nadir, the proposed 490 formulation results in less ESS capacity. 491

Also of interest, modal analysis of the results, as explained 492 in Table II, shows the efficiency of the proposed formulation in 493 comparison with that of [2] and [44]. 494

Results show that a lower emulated virtual inertia in the 495 proposed formulation not only decreases the cost function but 496 also causes better performance in terms of enhanced damping. 497

498 With virtual inertia, the results from [2] and [44] also seem to perform within the constraints and are almost the same as 499 the results from the proposed method. This could be justified 500 through the fact that set of PV buses for small systems includes a 501 502 few members to be considered as candidates of ESS installation. Therefore, different algorithms may differ a bit from capacity 503 point of view rather than location which in turn causes negligible 504 difference between the results. To further assess simultaneous 505 effects of virtual inertia on frequency and transient stabilities, 506 two non-linear system are used in what follows. 507

B. Two-Area Power System 508

The two-area power system, shown in Fig. 8, is considered to 509 further demonstrate the efficiency of the proposed formulation. 510 Modeling considerations are essentially those described in [45]; 511 all the generating units are modeled with 6th order synchronous 512 machine models with excitation systems. 513

The disturbance of interest is the outage of generator G_4 , at 514 515 the first second of simulation. The lower bounds of virtual inertia are calculated according to (29) and (30) as: 516

minimize
$$F(h_i) = \sum_{i=1}^{n_{ESS}} \left(C_{LCC,a\ i} \frac{h_i \ S_{base}}{3600 \ \text{sec}} \right)$$
 (31.a)

st :
$$H_{COI} = 4.973$$
 (31.b)
 $0.3151 \le h_1$
 $0.3881 \le h_2$
 $0 \le h_3$
 $30\% \le SOC_i \le 80\%$ (31.c)

TABLE III **OPTIMIZATION RESULTS IN TWO AREA SYSTEM**

Method	h1	h2	h3	$F(h_i)$
PM	0.402	0.567	0.004	4.6705
Ref. [2]	0.116	0.332	0.376	6.3104
Ref. [44]	0.212	0.315	0.316	5.7891

TABLE IV FREQUENCY INDICATORS OF TWO AREA SYSTEM BEFORE AND AFTER APPLICATION OF OPTIMAL INERTIA VALUES

	Without VI		With VI (PM)		With VI [2]		With VI [44]	
Gi	RoCoF	Δf_{nadir}	RoCoF	Δf_{nadir}	RoCoF	Δf_{nadir}	RoCoF	Δf_{nadir}
U	(Hz/s)	(Hz)	(Hz/s)	(Hz)	(Hz/s)	(Hz)	(Hz/s)	(Hz)
1	1.187	0.172	0.989	0.143	0.988	0.126	0.973	0.116
2	1.240	0.160	0.989	0.134	0.981	0.112	0.961	0.162
3	0.706	0.267	0.713	0.254	0.730	0.200	0.786	0.198

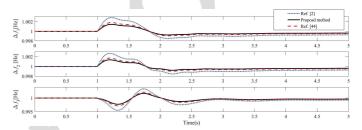


Fig. 9. Frequency response of generators 1, 2 and 3 of the two area power system for three cases: proposed formulation, Ref. [44] and Ref. [2].

in which, equality constraint of (31.b) reveals:

$$H_{COI} + h_{ESS} = 4.973 \rightarrow h_{ESS} = 4.973 - 4 = 0.973$$
(32)

Solving (28) leads to the optimum results of Table III. The 518 results also compared with those of optimum virtual inertia of 519 [2] and [44]. 520

Further, Table IV compares frequency stability indices for 521 different approaches. The results demonstrate high efficiency of 522 the proposed method to optimally allocate virtual inertia in the 523 system. 524

While the frequency nadir of the generators are within the 525 permissible range for the system without virtual inertia, the 526 RoCoFs for the generators 1 and 2 exceed the standard value. 527 Optimal placement of virtual inertia returns generators with undesired frequency dynamics to the normal region. Efficiency of the proposed method is further assessed through time domain 530 simulations of Fig. 9. 531

Also of interest, effects of virtual inertia on transient stability 532 is assessed using a simple power angle-based stability index 533 η [18]: 534 O3

$$\eta = \frac{360 - \delta_{\max}}{360 + \delta_{\max}} \tag{33}$$

where δ_{\max} is the maximum angle separation between any two 535 generators in the system [46]. Generally stated, the use of simple 536 metrics such as (33) may work for some systems but fail for some 537 others. During severe faults, most ESSs, if remain connected and 538 continue to inject active power which is not the case in many 539 regions, get saturated and cannot follow the frequency properly. 540 Using (33) in this paper relies on a conservative assumption that 541

517

 η 0.94

TABLE V

TRANSIENTS STABILITY ASSESSMENT

 δ_{max}

11.02

Fig. 10. Single line diagram of the 68-bus system showing coherent areas and their interconnections.

the occurred fault is not a severe one, which causes ESSs to
be disconnected from the grid. Moreover, saturation of ESSs
in response to sever faults is neglected. Table V demonstrates
better performance of the proposed method in comparison with
those of [2] and [44].

547 Note in these results, that a higher value of *** corresponds548 to a more favorable transient stability condition.

549 C. New York/New England System

Method

PM

The New England test system is used to further illustrate the efficiency of the proposed algorithm for large scale power systems. A single-line diagram of the system, showing major coherent areas and their interconnections, is shown in Fig. 10.

Five different contingency scenarios, including tripping of major generating units and load shedding, are considered. Results in Table VI compare the proposed algorithm results with those of [2] and [44]. The results show high efficiency of the proposed method to improve frequency dynamics with minimum cost.

Also of interest, Fig. 11 shows the allocation of virtual inertiaamong the PV buses of the system.

Moreover, Fig. 12 compares the frequency behavior of the system, in response to the outage of generator n1 (scenario 1), for the proposed method, [2] and [44]. It should be noted that while there are negligible deviations between the traces in Fig. 12, significant differences between the cost functions justify the efficiency of the proposed method.

Results show that the optimization problem works better
and more effectively for larger areas. This can be understood
by noting that set of PV buses for large areas includes many
members to be considered as candidates for ESS placement.
As a result, there are a lot of possibilities for both the size and
location.

TABLE VI Optimization Results in New York/New England System

		-					-
		h_I	h_2	h_3	h_4	h_5	$F(h_i)$
	PM	0.412	0.432	0.313	0.092	0.111	9.2141
1	Ref. [2]	0.506	0.332	0.376	0.201	0.112	12.4031
	Ref. [44]	0.378	0.453	0.306	0.115	0.098	11.0817
	PM	0.341	0.513	0.209	0.101	0.098	10.8601
2	Ref. [2]	0.340	0.712	0.301	0.113	0.160	13.0012
	Ref. [44]	0.300	0.798	0.251	0.098	0.161	12.3140
	PM	0.474	0.261	0.160	0.261	0.007	9.7516
3	Ref. [2]	0.596	0.298	0.267	0.271	0.088	11.2113
	Ref. [44]	0.314	0.351	0.294	0.314	~0	10.0087
	PM	0.169	0.203	0.617	0.135	0.072	9.8617
4	Ref. [2]	0.132	0.512	0.694	0.196	0.209	10.5103
	Ref. [44]	0.100	0.374	0.687	0.096	0.101	10.0102
	PM	0.613	0.032	0.116	0.076	~0	9.0412
5	Ref. [2]	0.743	0.215	0.402	0.031	~0	9.9731
	Ref. [44]	0.412	0.354	0.391	0.116	~0	9.4019

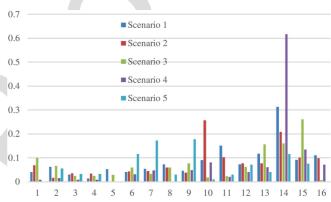


Fig. 11. Virtual inertia allocation for New-England system.

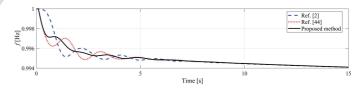


Fig. 12. Frequency responses of New England system for different approaches.

Moreover, the efficiency of the proposed formulation to enhance transient stability is shown in Table VII, using (33). 575

Table VII shows that appropriate placement of virtual inertia 576 in the system, considering dynamical behavior of ESS, could 577 also improve transient stability. This could be justified through 578 the fact that the so far researches, e.g. [2], rely on quasi-steady 579 state phasors for voltages and currents in transient stability 580 assessment. In other words, they consider constant nominal 581 value of frequency in defining system impedances which is far 582 from realistic for system with penetration of inverter based ESSs. 583 This point is successfully addressed in the proposed formulation 584 by explicitly representing the dynamic behavior of ESSs in the 585 problem formulation. 586

TABLE VII Optimization Results in New England System

	Method	η_{12}	η_{13}	η_{14}	η_{15}	η_{25}	η_{35}
	PM	0.92	0.87	0.91	0.89	0.90	0.89
1	Ref. [2]	0.85	0.84	0.91	0.90	0.85	0.87
	Ref. [44]	0.87	0.86	0.91	0.89	0.88	0.88
	PM	0.98	0.83	0.92	0.93	0.95	0.95
2	Ref. [44]	0.94	0.82	0.91	0.90	0.91	0.92
	Ref. [2]	0.91	0.84	0.90	0.88	0.89	0.95
	PM	0.87	0.90	0.90	0.89	0.92	0.92
3	Ref. [44]	0.85	0.88	0.90	0.88	0.88	0.88
	Ref. [2]	0.88	0.85	0.87	0.87	0.87	0.88
	PM	0.96	0.93	0.93	0.93	0.93	0.93
4	Ref. [44]	0.96	0.90	0.91	0.93	0.92	0.89
	Ref. [2]	0.95	0.94	0.93	0.93	0.91	0.85
	PM	0.94	0.85	0.92	0.92	0.91	0.96
5	Ref. [44]	0.89	0.86	0.90	0.90	0.89	0.94
	Ref. [2]	0.93	0.87	0.87	0.87	0.88	0.91

VI. SENSITIVITY AND UNCERTAINTY ANALYSIS

In this section, sensitivity analyses are conducted to understand the effect of operation conditions, including variations of faults magnitude, operating point, and annualized LCC on the optimization problem. For this purpose, (28.a) is used to calculate sensitivity of the cost function to operation condition, as:

$$F(h_i) + \Delta F(h_i) = \sum_{i=1}^{n_{ESS}} \left(C_{LCC,a i} \frac{h_i S_{base}}{3600 \text{ sec}} \right) + \frac{\partial F(h_i)}{\partial \Delta P_L} \Delta \Delta P_L + \frac{\partial F(h_i)}{\partial \Delta P_m} \Delta \Delta P_m + \frac{\partial F(h_i)}{\partial C_{LCC,ai}} \Delta C_{LCC,ai}$$
(34)

Then, according to (19) and (23), one could write the sensitivity matrix (26) as:

$$\begin{bmatrix} \partial h'_{i,\min} \\ \partial h''_{i,\min} \end{bmatrix} = \begin{bmatrix} \frac{\partial RoCoF_i}{\partial \Delta P_{Li}} & \frac{\partial RoCoF_i}{\partial \Delta P_{mi}} \\ \frac{\partial \Delta f_{nadir,i}}{\partial \Delta P_{Li}} & 0 \end{bmatrix} \begin{bmatrix} \Delta \Delta P_{Li} \\ \Delta \Delta P_{mi} \end{bmatrix}$$
(35)

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6 Considering (35) in (34) gives:

$$\Delta F(h_i) = \frac{\partial F(h_i)}{\partial h_i} \frac{\partial h_i}{\partial \Delta P_L} \Delta \Delta P_L + \frac{\partial F(h_i)}{\partial h_i} \frac{\partial h_i}{\partial \Delta P_m} \Delta \Delta P_m$$

$$= \sum_{i=1}^{n_{ESS}} \left(C_{LCC,a} \cdot \frac{S_{base}}{3600 \text{ sec}} \right) \times \max \left\{ \frac{\partial RoCoF_i}{\partial \Delta P_{Li}} \Delta \Delta P_L + \frac{\partial RoCoF_i}{\partial \Delta P_{mi}} \Delta \Delta P_m, \frac{\partial \Delta F_{nadir,i}}{\partial \Delta P_{Li}} \Delta \Delta P_{Li} \right\}$$

$$+ \sum_{i=1}^{n_{ESS}} \left(\frac{h_i S_{base}}{3600 \text{ sec}} \right) \Delta C_{LCC,ai}$$
(36)

The usefulness of (36) is now assessed for the New-England system. For this purpose, contingency 1, i.e. the outage of generator 1 in area 1, is considered as the base case. Cost function for outage of generator 7 in area 1, i.e. scenario 2, and generator 11 in area 2, i.e. scenario 3, are calculated using (36). Table VIII

TABLE VIII Sensitivity Analysis

Scenario	Cost function of (28)	Cost function of (35)
2	9.7516	9.5913
3	9.8617	9.9302

compares the results which clearly justify effectiveness of the proposed sensitivity analysis. 603

For uncertainty analysis, the equality constraint of (28.b) is 604 represented in the objective function (28.a), as: 605

$$\underset{h_i}{\text{inimize}} \quad F(h_i) = \sum_{i=1}^{n_{ESS}} \left(C_{LCC,a \ i} \frac{h_i \ S_{base}}{3600 \text{ sec}} \right) \\ + \beta(H_{COI} - Q)$$
(37)

where *b* is arbitrary chosen high with the aim of enforcing the results to follow the equality constraint of (28.b). Considering parametric uncertainty for inertia constant i.e. H_{COI} , one could write (37) as: 609

$$\underset{h_{i}}{\text{minimize } F(h_{i})} = \sum_{i=1}^{n_{ESS}} \left(C_{LCC,a} \cdot \frac{h_{i} \cdot S_{base}}{3600 \text{ sec}} \right) \\ + \beta (H_{COI} + \gamma - Q) \rightarrow$$
$$\underset{h_{i}}{\text{minimize } F(h_{i})} = \sum_{i=1}^{n_{ESS}} \left(C_{LCC,a} \cdot \frac{h_{i} \cdot S_{base}}{3600 \text{ sec}} \right) \\ + \beta (H_{COI} - Q) + \beta \gamma$$
(38)

where g expressed in percentage of H_{COI} . To deal with uncer-610 tainty analysis, a simple interval approach is utilized. It assumes 611 that the uncertain parameters take value in a specified interval. 612 It could be reinterpreted as the probabilistic modeling with a 613 uniform probability density function (PDF). In this method, 614 the upper and lower bounds for the uncertain inertia parameter 615 are defined. The aim is to find the lower and upper bounds of 616 objective function [47]. 617

Using the proposed framework, assume that the maximum uncertainty of inertia constant is considered to be 5p. This means that the interval of interest can be defined as: 620

$$\gamma = [H_{COI} - 0.05(H_{COI}), H_{COI} + 0.05(H_{COI})] \quad (39)$$

which in turn causes $F(h_i)$ as:

$$F(h_i) = [3.8298, 5.5112] \tag{40}$$

with a uniform PDF.

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VII. CONCLUSION 623

While rotational inertia stabilizes the frequency of power grids 624 against small and large disturbances, it leads for oscillations 625 between generators. This paper provides a framework for opti-626 mal placement of virtual inertia in low inertia power systems 627 which in turn improves host grid frequency stability. In this 628 way, the ESSs are used to emulate virtual inertia placement. 629 On the other hand, the proposed method in this paper tackles 630 dynamical behavior of the ESSs into problem formulation and 631

thus causes less, in comparison with the literature, virtual inertia 632 to be implemented in the system. This in turn causes better rotor 633 angle stability features. Of note that the proposed algorithm can 634 be a valuable tool in generation expansion planning of power 635 system and inertia deployment. 636

A data driven-based approach to represent the ESS dynamics 637 using conventional synchronous generator is proposed. This in 638 turn causes the gathered data, from the field setup, provides 639 complementary information to the conventional based model of 640 synchronous generator. Simulation results validate accuracy and 641 efficiency of the proposed modelling procedure. 642

Using the proposed strategy in a linear three-area power 643 system and two non-linear systems, the required ESS for each 644 area with the lowest cost and capacity are determined. It was 645 found that the calculated values could well maintain the fre-646 quency indices within the permissible range. Also, the results 647 648 showed that the optimal virtual inertia arrangement could have a positive effect on the transient stability and the amount of 649 power exchange between control areas. 650

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APPENDIX

TABLE IX ECONOMICAL PARAMETERS RELATED TO THE OPTIMIZATION PROBLEM [25], [26]

Parameter	Value	Parameter	Value
i(%)	8	C _{FOM,a} (\$/kw-yr)	10
C_{PSC} (\$/kw)	200	$C_{VOM,a}$ (kwh)	5
C_{BOP} (\$/kw)	50	R	2
C_{stor} (\$/kw)	300	t(yr)	6
C_R (\$/kw)	300	$\eta_{svs}(\%)$	75

TABLE X TECHNICAL PARAMETERS RELATED TO THE OPTIMIZATION PROBLEM [22], [24].

Parameter	Value	Parameter	Value
S_{base} (MVA)	1000	$P_{ESS}(MW)$	1
$RoCoF_{max}(Hz/s)$	1	E _{ESS, rated} (MVAh)	0.25
$\Delta f_{nadir, max} (Hz)$	0.8	$\eta_d = \eta_c(\%)$	75
$SOC(\theta)$	0.5	t(yr)	15
SOC_{min}	0.3	$t_{ch}(hrs)$	0.25
SOC_{max}	0.8	n _{cycle}	1000

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