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Pseudo-Static Analytical Model For The Static And Seismic Stability Of Dry Stone Retaining Walls

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Abstract - Dry stone retaining walls are made of rubble stones assembled without mortar. They have shaped many regions worldwide and nowadays constitute a high cultural value, aside from their original operational role (agricultural terraces or transportation networks). However, given their high number and old age, they currently need maintenance, whereas only a few tools are available to assess their stability. In particular, the literature lacks a design tool that accounts for seismic loads. In this paper, a pseudo-static approach based on Coulomb's wedge theory is described in detail. General effects of cohesion, water pore pressure and geometrical features of the backfill are considered. On the other hand, the specificities of dry stone retaining walls are introduced through new parameters, whose values are extracted from laboratory and in-situ experiments.

Keywords: Slope stability, Masonry, Earthquake engineering, Coulomb's wedge, Payload, Geotechnical engineering

1. Introduction

Dry stone masonry retaining walls (DSRWs) are made of rubble stones assembled without mortar with definite know-how. They constitute a significant cultural heritage in many regions worldwide. Some emblematic sites have been classified in the UNESCO heritage list (Douro's valley, Portugal or Lavaux's terraces, Switzerland). Most of these structures were built before the twentieth century and therefore require a high level of maintenance today. On the other hand, they bear an important economic role, supporting transporting networks or agricultural terraces. Though abandoned in the middle of the twentieth century for the benefit of steel and concrete materials, dry stone technology recently began to be used again. While fifty years ago, an old DSRW would have been replaced or repaired using concrete, mortar or steel anchors [1]–[3], today, more and more stakeholders choose to rebuild/repair damaged DSRWs engaging specialised dry stone masons. Indeed, their intrinsic low embodied energy, high local social impact, and the small amount of induced waste make them utterly relevant in the global context of sustainable development. In addition, their high cultural value, also enhancing touristic activities (especially in areas literally shaped by dry stone constructions), require their maintenance with original techniques.

Specific research studies regarding dry stone retaining walls (DSRWs) have been mainly conducted in Europe, with experimental [4]–[9], analytical [10]–[17] and numerical works based on the Discrete Element Method (DEM) [18]–[26]. In particular, both free-standing dry stone walls (e.g., [21]), slope retaining walls (e.g., [11]), and road retaining walls (e.g., [19]) have been studied. All the analytical tools already proposed in the literature account for many parameters of actual DSRWs. For example, the various geometrical configurations of the wall-backfill system are considered in almost all analytical studies [10]–[12], [14]–[16]: internal and external batters, as well as the inclination of the retained backfill, are variable. Then, more refinements consider the possibilities to have inclined courses of stones and a different total height between the backfill and the retaining wall [10], [11].

Alejano et al. [12] considered the presence of water pressure through permanent hydrostatic pore pressure. Though pore pressures are hardly expected to accumulate behind a DSRW, it significantly affects the stability of these structures [26]. Preti et al. [27] proposed a more complex hydrological model to account for dynamic pore pressure due to water flows. Though initially excluded from the analytical model developed by Colas et al. [10], [11], the backfill cohesion was added afterwards in the computations presented in the guides for the static design of DSRWs [28]. However, as classically observed for general retaining wall systems, this model does not account for the tension cracks that develop on top of cohesive soils, leading to smaller cohesive forces [29]–[31]. A potential payload placed on the top of the backfill is also accounted for in

are variable, and their optimisation will be detailed in Section 2.5. The geometrical parameters depicted in Figure 1 are enough to characterise the system entirely; all the other dimensions (e.g., the height of the soil's wedge h_{wedge}) and section areas only depend on these primary features. The last parameter required by the model is the interface friction angle δ that determines the inclination of the earth pressure with respect to the internal wall batter. An interface cohesion C_{int} is also envisioned, though almost always null in practice because of the dry drain placed directly behind a DSRW (see Section 2.2).

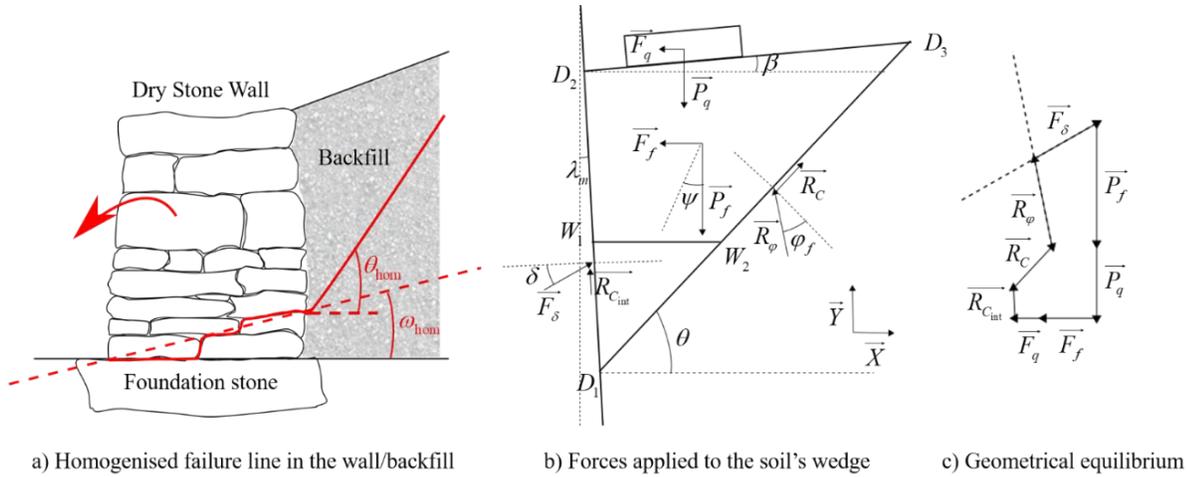


Figure 2: Homogenised failure lines in the wall and backfill (a) and equilibrium of forces applied to the soil's wedge (b-c)

2.2. Forces applied to the Coulomb soil's wedge

The first part of the analytical model determines the pseudo-static earth pressure \vec{F}_δ the backfill applies on the wall. Figure 2b describes all the forces acting on the Coulomb's wedge of soil. ψ represents the orientation of the equivalent gravity and is given by the following formula:

$$\tan \psi = \frac{a_h}{1 + a_v} \quad (1.1)$$

where a_h and a_v are the horizontal and vertical accelerations expressed in proportion to the natural gravity g . The weight of the soil \vec{P}_f , the pseudo-static action of the soil \vec{F}_f , the weight of the payload \vec{P}_q , the pseudo-static action of the payload \vec{F}_q , the cohesive reaction of the soil \vec{R}_C , and the cohesive interface force $\vec{R}_{C_{int}}$ are known and read (Figure 1 & 2):

$$\vec{P}_f = -\gamma_f \times S_{D_1 D_2 D_3} \times (1 + a_v) \vec{Y} \quad \vec{F}_f = -\gamma_f \times S_{D_1 D_2 D_3} \times a_h \vec{X} \quad (1.2)$$

$$\vec{P}_q = -q \times L_q \vec{Y} \quad \vec{F}_q = -q \times L_q \times a_h \vec{X} \quad (1.3)$$

$$\vec{R}_C = \left\| \overline{D_1 D_3} \right\| \times C_f \times (\cos \theta \vec{X} + \sin \theta \vec{Y}) \quad (1.4)$$

$$\vec{R}_{C_{int}} = \left\| \overline{D_1 D_2} \right\| \times C_{int} \times (\sin \lambda_m \vec{X} + \cos \lambda_m \vec{Y}) \quad (1.5)$$

In the equations above, the soil's wedge area $S_{D_1 D_2 D_3}$ and lengths $\left\| \overline{D_1 D_3} \right\|$ and $\left\| \overline{D_1 D_2} \right\|$ only depend on the basic geometrical parameters described in Figure 1. The intensities of the frictional reaction of the stable backfill \vec{R}_φ and the wall reaction (the opposite of earth pressure) \vec{F}_δ are unknown though their directions are given, assuming limit equilibrium conditions:

$$\vec{F}_\delta = \left\| \overline{F_\delta} \right\| \times (\cos(\delta + \lambda_m) \vec{X} + \sin(\delta + \lambda_m) \vec{Y}) \quad \vec{R}_\varphi = \left\| \overline{R_\varphi} \right\| \times (-\sin(\theta - \varphi_f) \vec{X} + \cos(\theta - \varphi_f) \vec{Y}) \quad (1.6)$$

In case water pore pressures exist (i.e., line $(W_1 W_2)$ inside the wedge $(D_1 D_2 D_3)$), Eq. (1.2) becomes:

$$\vec{P}_f = \left[-\gamma_f \times (S_{D_1 D_2 D_3} - S_{D_1 W_1 W_2}) - (\gamma_{sat} - \gamma_w) \times S_{D_1 W_1 W_2} \right] \times (1 + a_v) \vec{Y} \quad (1.7)$$

$$\vec{F}_f = \left[-\gamma_f \times (S_{D_1 D_2 D_3} - S_{D_1 W_1 W_2}) - (\gamma_{sat} - \gamma_w) \times S_{D_1 W_1 W_2} \right] \times a_h \vec{X} \quad (1.8)$$

2.3. Equilibrium of the Coulomb's wedge: determination of the earth pressure \overline{F}_δ

Gathering all the forces applied to the soil's wedge expressed in Eqs. (1.3), (1.5), (1.6), (1.7), (1.8) and (1.13), and writing the force equilibrium along the direction $\cos(\theta - \varphi_f)\overline{X} + \sin(\theta - \varphi_f)\overline{Y}$ to nullify the contribution of \overline{R}_φ in Eq. (1.6), one can obtain the intensity of the earth pressure:

$$\|\overline{F}_\delta\| = \frac{\left(\|\overline{P}_f\| + \|\overline{P}_q\|\right) \sin(\theta - \varphi_f) + \left(\|\overline{F}_f\| + \|\overline{F}_q\|\right) \cos(\theta - \varphi_f) - \|\overline{R}_C\| \cos \varphi_r - \|\overline{R}_{C_{int}}\| \sin(\theta - \varphi_r - \lambda_m)}{\cos(\lambda_m + \delta + \varphi_f - \theta)} \quad (1.14)$$

The last unknown that needs to be determined is the application point of the earth pressure y_δ . In the classical case without cohesion, pore pressure, payload or seismic actions, the application point can be calculated at a depth $y_\delta = 1/3 \times h_{wedge}$ (Figure 4a). Whenever pore pressures are considered within the soil's wedge, application point depth decreases following the weighted equation:

$$y_\delta = \frac{1/3 \times h_{wedge} \times \gamma_f \times S_{D_1 D_2 D_3} + 1/3 \times (h_w - (h_f - h_{wedge})) \times (\gamma_{sat} - \gamma_w - \gamma_f) \times S_{D_1 W_1 W_2}}{\gamma_f \times S_{D_1 D_2 D_3} + (\gamma_{sat} - \gamma_w - \gamma_f) \times S_{D_1 W_1 W_2}} \quad (1.15)$$

Classically, when accounting for cohesive soils, the height of the application point of earth pressure diminishes. One can find in a simple case without payload and seismic actions that the application point is located at a height y_δ , given by the following equation:

$$y_\delta = \frac{\gamma_f \sin(\theta - \varphi_f) \cos(\theta) h_{wedge}^2 - 3C_f \cos \varphi_f h_{wedge}}{3\gamma_f \sin(\theta - \varphi_f) \cos(\theta) h_{wedge} - 6C_f \cos \varphi_f} \quad (1.16)$$

In fact, though the application point should not theoretically move when adding pseudo-static actions, the experimental literature found some variations depending on the displacement mode of the wall. In particular, the application point of the dynamic increment can be located higher in the walls, up to $0.7h_f$ [36], [37]. Considering a wall displacement mode with a mixed translation and rotation about its base, very close to the behaviour of DSRWs, Ishibashi and Fang found that the dynamic increment of earth pressure is located at $0.5h_f$ [36]. As recommended in the Eurocode, this last value is considered here (either for the soil's wedges $(D_1 D_2 D_3)$ and $(D_1 W_1 W_2)$ see example Figure 4b). The earth pressure static and dynamic increments due to the payload are assumed to act at point N, projection point of M (middle of the payload) parallel to the failure line (Figure 4c).

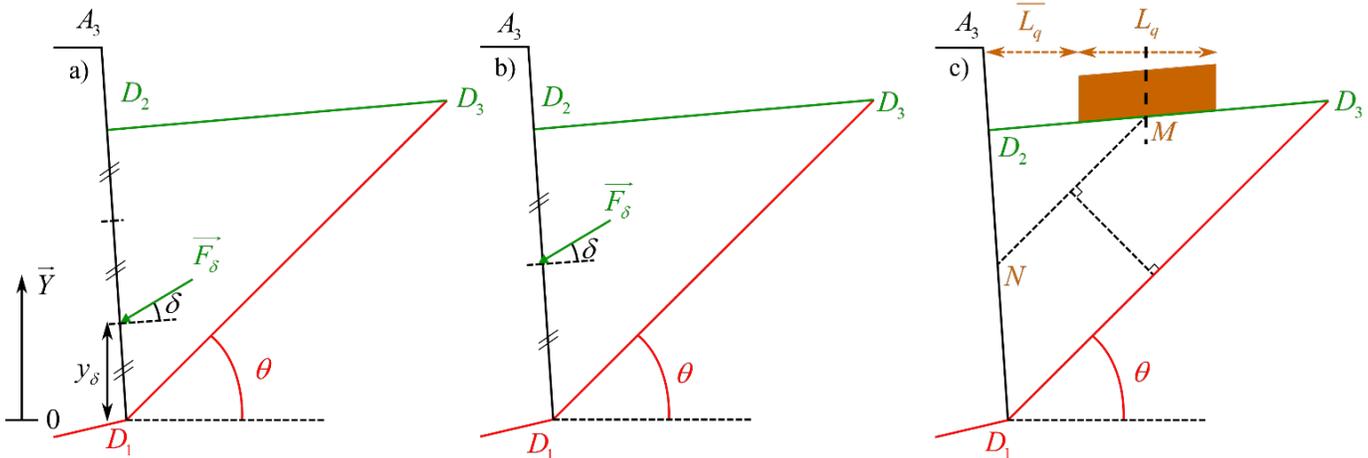


Figure 4: Application point of the earth pressure in some particular cases: a) only static action of the soil; b) only seismic action of the soil, and c) only static action of the payload

The application points of the earth pressure are known if every single destabilising force (\overline{P}_f considering the effect of water and cohesion (\overline{R}_C), \overline{P}_q , \overline{F}_f , or \overline{F}_q) is considered separately. The final application point is computed through a

weighting formula, with the destabilising force intensities ($\|\overline{P}_f\|$, $\|\overline{P}_q\|$, $\|\overline{F}_f\|$, $\|\overline{F}_q\|$) as weights. Note that the exact position of the application point of the cohesive reaction $\overline{R}_{C_{int}}$ is not needed since its line of thrust is known and is already enough to compute the wall's equilibrium. As a final remark, the stabilising effect of $\overline{R}_{C_{int}}$ on the application point of earth pressure \overline{F}_δ is not considered, $\overline{R}_{C_{int}}$ being null in most cases and the assumption being conservative.

2.4. Equilibrium of the DSRW

Figure 5 focuses on the stability of a given wall section ($EA_2A_3D_1$). The failure line (ED_1) crosses the DSRW through the dry joints. \overline{P}_{rw} is the weight of the wall, \overline{F}_{rw} is the wall pseudo-static action, \overline{F}_w is the water force. \overline{F}_δ is the earth pressure and $\overline{R}_{C_{int}}$ is the cohesive interface force, both evaluated in Section 2.3 and finally \overline{R}_b corresponds to the action transmitted to the foundation. They read:

$$\overline{P}_{rw} = -\gamma_{rw} \times S_{EA_2A_3D_1} \times (1 + a_v) \overline{Y}, \quad \overline{F}_{rw} = -\gamma_{rw} \times S_{EA_2A_3D_1} \times a_h \overline{X}, \quad \overline{F}_w = -\gamma_w \times \frac{(h_w - h_f + h_{wedge})^2}{2} \overline{X} \quad (1.17)$$

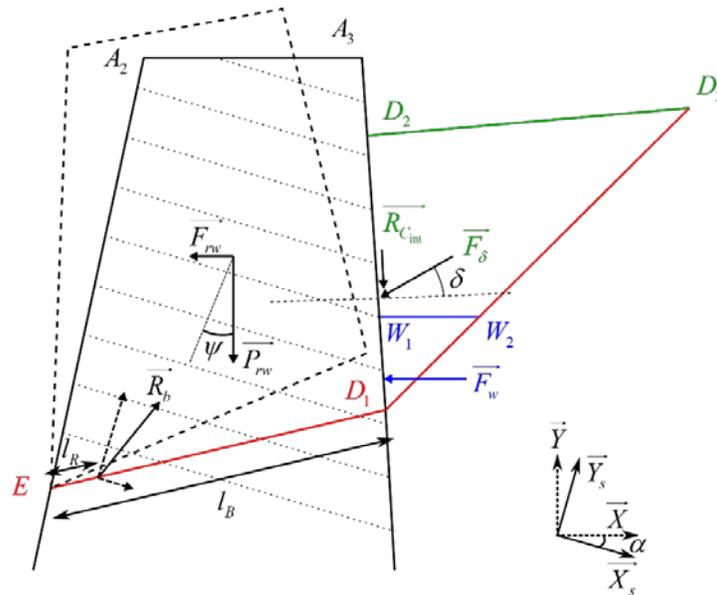


Figure 5: Equilibrium of the wall section $S_{EA_2A_3D_1}$

Forces \overline{P}_{rw} and \overline{F}_{rw} are applied at the centre of gravity of the studied wall section $S_{EA_2A_3D_1}$, while \overline{F}_w is applied at one-third of the height of the triangle ($D_1W_1W_2$). The stability of the section is then computed in both sliding and overturning failure mechanisms. Overturning is prevented if the moment of the destabilising forces (\overline{F}_{rw} , \overline{F}_w and \overline{F}_δ) is smaller than that of stabilising forces (\overline{P}_{rw} and eventually $\overline{R}_{C_{int}}$). It corresponds to checking that the application point of the reaction force \overline{R}_b lies within the line (ED_1). The sliding equilibrium is based on the dry contact friction resistance between courses of stones. First, the equilibrium along \overline{X} and \overline{Y} directions gives the intensity of the base reaction \overline{R}_b , which is then projected in directions \overline{X}_s and \overline{Y}_s , parallel and respectively perpendicular to the stone bed's inclination α . Then, the classical Mohr-Coulomb criterium is computed:

$$\overline{R}_b \cdot \overline{X}_s < \overline{R}_b \cdot \overline{Y}_s \times \tan \varphi_{rw} \quad (1.18)$$

As mentioned earlier, DSRWs are also characterised by the possibility for stones to rotate when loaded, given DSRW's porosity [4]–[6]. From real DSRWs tested during the experimental campaigns of Colas et al. [4], [5] and Villemus et al. [6],

all the walls that fell purely in sliding had an eccentricity of the base reaction \overline{R}_b , equal to $e_b = 1 - l_R/l_B \approx 0.3$ (Figure 5). These walls also displayed local rotations of stones. Though specific full-scale tests should confirm it, $e_b \approx 0.3$ seems to play a critical role in the local rotation of stones. The more the stones are loaded far from the central part of the wall/stones, the more they tend to rotate and rearrange their system of contact points. The internal rotation of stones is called η and, according to these experiments, can be taken between 5° and 10° . Eq. (1.18) becomes:

$$\overline{R}_b \cdot \overline{X}_s < \overline{R}_b \cdot \overline{Y}_s \times \tan(\varphi_{rw} - \eta) \quad (1.19)$$

To account for the influence of the eccentricity, the authors propose to fully activate the internal rotation $\eta_{mob} = \eta$ when the eccentricity is greater than $e_b > 0.3$. On the contrary, no rotation ($\eta_{mob} = 0^\circ$) is activated when the eccentricity is less than $e_b < 0.25$. Between these two thresholds, a linear weighting function is used:

$$\eta_{mob} = \eta \frac{e_b - 0.25}{0.3 - 0.25} \quad (1.20)$$

2.5. Optimisation of the stability: find the actual failure line

After both sliding and overturning stabilities are expressed depending on the system's parameters and the unknowns of the failure line (h_g , ω and θ), one can optimise these three parameters to find the most critical situation, determining the factors of safety. One should note that the optimisation should be done for both sliding and overturning phenomena, leading to two sets of optimised failure line parameters ($h_{g,opt}$, ω_{opt} and θ_{opt}).

As noted by several authors, the inclination ω is crucial for the overturning stability and is also constrained by the arrangement of stones ($\omega_{opt} < \omega_{max}$, see Figure 2a) [12], [17], [26]. The formula $\tan \omega_{max} = h_u/b_u$ has been proposed recently [17], with h_u and b_u the mean height and length, respectively, of stone units. It leads to $\omega_{max} \approx 20^\circ$ for DSRWs assembled with rubble stones [4]–[6], [17], and a bit larger values $\omega_{max} \approx 25 - 45^\circ$ for DSRWs built with higher units [26].

4. Conclusion

In summary, the present work proposes a unified methodology to design slope dry stone masonry retaining walls. It accounts for almost all idealised geometries. The effect of eventual payloads, water pore pressure, as well as soil cohesion and the associated tension cracks, are included. Similarly, seismic actions are modelled through the classical pseudo-static approach. However, it is reminded that permanent payloads and water accumulation behind DSRWs need to be prevented. Another improvement of the paper is that it proposes an analytical formula and a practical methodology to introduce the internal rotation of stones when the DSRW is loaded. The latter states that the rotation occurs when the loads are concentrated in the downstream part of the DSRW, forcing stones to rearrange themselves locally to find new contacts. Dedicated full-scale experiments are envisioned to assess the validity of this proposal. Finally, the above-presented tool allows doing complete parametric analysis to support the design of such structures, being very fast to run.

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