

Intercomparing Superconducting Gravimeter Records in a Dense Meter-Scale Network at the J9 Gravimetric Observatory of Strasbourg, France

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Abstract	This study is a metro These superconductines (32). We first compare compute the amplitude experiments. The relative residual signal. We also analysis for the longer the relationships obset three-channel correlat then compared to a metro The self-noise of iGra- expected, the self-noise	logical investigation of eight superconducting gravimeters that have operated in the Strasbourg gravimetric Observatory. g gravimeters include an older compact C026 model, a new observatory type iOSG23 and six iGravs (6, 15, 29, 30, 31, the amplitude calibration of the meters using measurements from FG5 #206 absolute gravimeter (AG). In a next step we de calibration of all the meters by time regression with respect to iOSG23 itself carefully calibrated by numerous AG tive calibration values are much more precise than absolute calibration for each instrument and strongly reduce any tidal so compare the time lags of the various instruments with respect to iOSG23, either by time cross-correlation or tidal st records (about 1 year). The instrumental drift behavior of the iGravs and iOSG23 is then investigated and we examine rved between gravity and body temperature measurements. Finally, we compare the noise levels of all the instruments. A ion analysis is used to separate the incoherent (instrumental) noise from the coherent (ambient) noise. The self-noise is nodel of thermal noise (Brownian motion) using the known instrumental parameters of the damped harmonic oscillator. av instruments is well-explained by the thermal noise model at seismic frequencies (between 10–3 and 10–2 Hz). As se of iOSG23 with a heavier sphere is also lower than that of iGravs at such frequencies.
Keywords (separated by '-	Superconducting grav	imeter - levitation - calibration - instrumental drift - noise

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Intercomparing Superconducting Gravimeter Records in a Dense Meter-Scale Network at the J9 Gravimetric Observatory of Strasbourg, France

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6 Abstract-This study is a metrological investigation of eight 7 superconducting gravimeters that have operated in the Strasbourg 8 gravimetric Observatory. These superconducting gravimeters 9 include an older compact C026 model, a new observatory type 10 iOSG23 and six iGravs (6, 15, 29, 30, 31, 32). We first compare the 11 amplitude calibration of the meters using measurements from FG5 12 #206 absolute gravimeter (AG). In a next step we compute the 13 amplitude calibration of all the meters by time regression with 14 respect to iOSG23 itself carefully calibrated by numerous AG 15 experiments. The relative calibration values are much more precise 16 than absolute calibration for each instrument and strongly reduce 17 any tidal residual signal. We also compare the time lags of the 18 various instruments with respect to iOSG23, either by time cross-19 correlation or tidal analysis for the longest records (about 1 year). 20 The instrumental drift behavior of the iGravs and iOSG23 is then 21 22 investigated and we examine the relationships observed between gravity and body temperature measurements. Finally, we compare 23 the noise levels of all the instruments. A three-channel correlation 24 analysis is used to separate the incoherent (instrumental) noise 25 from the coherent (ambient) noise. The self-noise is then compared 26 to a model of thermal noise (Brownian motion) using the known 27 instrumental parameters of the damped harmonic oscillator. The 28 self-noise of iGrav instruments is well-explained by the thermal 29 noise model at seismic frequencies (between 10^{-3} and 10^{-2} Hz). As 30 expected, the self-noise of iOSG23 with a heavier sphere is also 31 lower than that of iGravs at such frequencies.

Keywords: Superconducting gravimeter, levitation, calibration, instrumental drift, noise.

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Eight different superconducting gravimeters (SG) 36 manufactured by GWR Instruments, Inc. have been 37 operated at J9 gravimetric Observatory of Strasbourg. 38 A compact C026 was the first SG installed in 1996, 39 an iOSG-type (#23) in January 2016 and iGrav (#29) 40 in July 2016, and five other iGrav-type (#6, #15, #30, 41 #31, #32) at various intervals. Figure 1 shows the 42 three different types of SG used in this intercom-43 44 parison study.

The C026 was installed in July 1996 and proved 45 to have very good time-stability (Calvo et al., 46 2014, 2017; Riccardi et al., 2009) and good perfor-47 mances in terms of noise levels (Rosat & Hinderer, 48 2011) enabling the study of very long-period geo-49 physical phenomena and the analysis of small tidal 50 constituents (e.g. Calvo et al., 2016). Experiences of 51 intercomparison and validation tests of spring 52 gravimeters, conducted in the past at J9, have bene-53 fited from the stability of the C026 and the low noise 54 level in the observatory (Arnoso et al., 2014). Since 55 February 2016 the iOSG23 (see below) operated next 56 to the C026 (Boy et al., 2017; http://doi.org/10.5880/ 57 igets.st.11.001). C026 had experienced many prob-58 lems due to its very old electronics (more than 59 25 years old) and was turned off in November 2018. 60 The C026 data were also not usable between 61 November 2016 and April 2017 because of a failure 62 of the data acquisition system. 63

The latest generation of single-sphere SGs are the iGrav and the iOSG using identical sensors, electronics and refrigeration systems. The iOSG uses a heavier sphere (17.7 g versus 4.3 g) and has a larger dewar (35 L versus 16 L) and consequently has a 68



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69 slightly lower instrumental noise level and a longer hold time during power failures. In contrast, the 70 71 iGrav, which was designed for field use, is easier to 72 move and operate at remote sites (Warburton et al., 73 2011). The iOSG23 was installed at J9 in January 74 2016 and is the second iOSG installed in France; the 75 first one was iOSG24 installed in July 2015 at the low 76 background noise interdisciplinary ground and underground based research laboratory LSBB of 77 78 Rustrel, in the south of France (Rosat et al., 2016). 79 Only three iOSGs have been manufactured and the third, iOSG22, was installed at Metsähovi Geodetic 80 Fundamental Research Station (ME), Finland in 81 82 December 2016. The older compact C026 was a 83 second generation of SG manufactured between 1994 84 and 2002 with a 125 L dewar. The iOSG and iGrav 85 instruments use SHI RKD 101 refrigerating systems to cool below 4 Kelvin and condense helium gas (He) 86 87 to liquid inside the dewar so that there is no He loss and no need to transfer liquid He. In contrast, the 88 89 C026 used an older APD Cryogenics DE202A cold-90 head with only 9 K cooling capability so He gas boils 91 off slowly. As a result, the C026 required regular 92 human intervention (about every 10 months) to refill 93 the dewar with liquid He.

iGrav29, iGrav30 and iGrav31 were purchased in
2016 in the framework of the Equipex CRITEX
recently integrated in OZCAR (https://www.ozcar-ri.
org/ozcar/), which is the French network of Critical
Zone Observatories (Gaillardet et al., 2018). The
iGravs are one type of equipment for this hydrology-

oriented project dedicated to the gravity monitoring 100 of basin catchment and the study of the critical zone. 101 These three iGravs were installed at J9 in July 2016. 102 After operation at J9, iGrav30 was moved to the 103 Strengbach catchment in the Vosges mountains (at 104 70 km from Strasbourg) end of June 2017 and 105 iGrav31 was moved in May 2019 to the surface sta-106 tion at LSBB (https://lsbb.cnrs.fr) in South of France. 107 iGrav30 is used to investigate the water storage 108 changes at the catchment scale (Chaffaut et al., 2020). 109 while iGrav31 establishes together with iOSG24 (the 110 twin meter of iOSG23 studied here) a differential 111 gravity experiment that will be very useful to locate 112 the underground water mass changes already detected 113 by iOSG24 alone (Mouyen et al., 2019; Rosat et al., 114 2016, 2018). The eight SGs were installed in different 115 rooms of the J9 bunker as illustrated in Fig. 2. 116

iGrav6, iGrav15, and iGrav32 were moved to the 117 Strasbourg Observatory by German colleagues for a 118 validation test in 2017 before being sent to Iceland in 119 the frame of the "Microgravimotis" project for 120 gravity monitoring of the Theistareykir geothermal 121 site (Erbaş et al., 2019). The performances of these 3 122 iGravs after transportation to Iceland in terms of 123 calibration, drift and noise levels are investigated in 124 Schäfer et al. (2020). As can be seen in the 125 timetable (Fig. 3), end of August 2017 iGrav32 had 126 to be sent back to the manufacturer GWR for 127 instrumental upgrade and did come back to J9 only 128 for a short time in October 2017; the period before 129 the upgrade refers to 32a and after upgrade 32b. 130



Figure 1

A picture showing the types of SGs operating side by side and their physical installations in the J9 Observatory near Strasbourg (France): from left to right, C026 on a large isolated pillar; iOSG23 straddling a small isolated pillar; iGrav32 operating directly on the concrete floor; and iGrav30 with coldhead frame modified to fit on a small isolated pillar

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Figure 2

Floor plan of the Strasbourg Gravimetric Observatory (J9) indicating the location of the various instruments that are compared in this study



Figure 3 Timetable of the SG and AG measurements in the J9 Observatory

iGrav6 also came only for limited time end ofSeptember 2017 before shipment to Iceland.

For both historical reasons and convenience, a 133 variety of methods as shown in Fig. 1 were used to 134 135 physically set SGs at J9. C026 was operated in its 136 own room and on a wide and deep pillar 137 $(0.8 \text{ m} \times 0.8 \text{ m} \times 2 \text{ m})$ isolated from the floor that was originally built for operating one of the early 138 GWR TT70 SGs. Two of the rooms at J9 have small 139 140 isolated pillars (0.6 m \times 0.6 m \times 0.6 m) previously 141 used for testing LaCoste and Romberg, Scintrex and gPhone gravity meters. Although the base of the 142 143 iOSG23 dewar fits on the small pillar, its coldhead 144 isolation frame does not. Therefore, the coldhead 145 isolation frame straddles the pillar with two of its feet 146 on the pillar and one on the nearby concrete floor. iGravs 29, 30, 31 and 32b were also operated on 147 small pillars; however, for these iGravs, the con-148 necting angles of the legs to the coldhead support 149 bracket were decreased during installation to reduce 150 their footprints to fit onto the small pillars. The 151 iGrav15, iGrav6 and iGrav32a were installed directly 152 on the concrete ground without any modification to 153 their coldhead frames. As a consequence, some dif-154 ferences between the physical installations for the 155 eight instruments could influence the measured noise 156 levels between them. 157

The timetable showing the available data sets is 158 given in Fig. 3. The maximum number of SGs measuring simultaneously in our study is six because 160 there is no overlap between iGrav30 that left the 161

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SG name	Length of calibration	Absolute calibration and error $(nm/s^2/V)$	Dimensionless error (%)
C026	Numerous experiments with FG5#206 during 1996–2018	-792 ± 1	0.1
iOSG23	6.2 days	-451 ± 2	0.4
iGrav15	7.1 days	-934 ± 3	0.3
iGrav29	6.2 days	-940 ± 4	0.4
iGrav30	6.2 days	-918 ± 4	0.4
iGrav31	6.2 days	-853 ± 4	0.5
iGrav32	7.1 days	-898 ± 3	0.3

Table 1

Results for absolute calibration of SGs using SG/AG parallel records; V stands for volt

162 Observatory for a remote installation before iGrav32163 arrived.

164 In this paper, we compare the accuracy and precision of the time variations of gravity recorded by 165 the various SGs. We start by first testing the precision 166 of the scaling factors used to calibrate the SGs and we 167 168 estimate the time delays (phase lags) between the instruments, either by directly comparing the time 169 170 series and their correlation, or by using tidal admit-171 tances obtained from tidal analyses. Next, the instrumental drift is carefully investigated, particu-172 173 larly the initial drift subsequent to the installation of 174 each gravimeter. And finally, from the few months of parallel records, we finally use a standard procedure 175 to compute power spectral densities (PSDs) using the 176 Welch's overlapped segment averaging estimator in 177 order to give reference noise levels for these instru-178 ments. These PSDs are compared with the 179 180 seismological reference noise models and with other relative mechanical gravimeters and a long-period 181 182 seismometer that have been recorded at J9. Self-noise levels are also estimated and compared with a pre-183 184 dicted thermal noise model.

185 2. Amplitude Calibration and Time Delay

186 2.1. Absolute Calibration

187 SGs are relative instruments that need to be
188 calibrated using an absolute reference. Since the
189 transfer function of the SGs is flat at frequencies
190 much lower than Nyquist frequency (0.5 Hz), the
191 calibration is usually achieved by estimating a scale

factor with tides recorded by parallel co-located 192 absolute gravity measurements performed with a FG5 193 ballistic instrument (Fukuda et al., 2005; Hinderer 194 et al., 1991; Imanishi et al., 2002; Tamura et al., 195 2004). Following recent papers (Crossley et al., 2018; 196 Meurers, 2012; Van Camp et al., 2015), we used 197 parallel FG5 drop measurements to which a L1-norm 198 adjustment of the low-pass filtered SG data decimated 199 to 10 s is performed. This L1-normalization is used in 200 order to avoid the influence of outliers. The FG5 drop 201 standard deviations are considered in the fitting 202 process. Scale factors obtained in this way (absolute 203 calibration factors) are summarized in Table 1 as well 204 as the time periods during which the various instru-205 ments were recording at J9. 206

Two specific AG/SG calibration experiments207were performed during the observation period: the208first one in September 2016 having a duration of209149 h (6.2 days) and used to calibrate iGrav29,210iGrav30, iGrav31, and iOSG23; the second one in211July 2017 having a duration of 170 h (7.1 days) and212used to calibrate iGrav15, iGrav32.213

Note that numerous absolute calibration experiments were done with C026 since 1996 (Amalvict 215 et al., 2001; Calvo et al., 2014; Crossley et al., 2018; 216 Riccardi et al., 2012; Rosat et al., 2009) leading to the 217 very well determined value of $-792 \pm 1 \text{ nm/s}^2/\text{volt.}$ 218

iGrav15 was first calibrated by FG5#206 in J9 and 219 after cold transportation to the Theistareykir geothermal site in Iceland it was calibrated again. The two 221 calibration factors found in J9 and Iceland lead to a 222 nearly identical value $-935 \pm 6 \text{ nm/s}^2/\text{V}$ (Schäfer 223 et al., 2020). No absolute calibration could be 224 performed for iGrav6 at J9. 225

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226 2.2. Relative Calibration

227 It has been shown in previous studies that the 228 internal SG stability ($\sim 0.1\%$) as derived from tidal 229 analyses is more than ten times better than the stability that can be achieved by calibration repeti-230 tions with an absolute gravimeter (Calvo et al., 2014). 231 232 Besides, absolute gravity measurements are affected 233 by noise which will limit the precision of the retrieved scale factor. Assuming one of the SGs 234 operating in our Observatory possesses an accurate 235 calibration, we can estimate the scale factors of other 236 237 SGs by minimizing the differences of raw time 238 records that should measure the same changes in 239 gravity being located at the same place (at least inside 240 the same building). We may hence expect to improve 241 the precision on the scale factor estimates. However, 242 we have to state here that a relative calibration can 243 never be more accurate than the calibration of the 244 instrument used for the relative calibration. It can only enhance the precision of calibration but not the 245 accuracy. Using another relative gravimeter to cali-246 brate an SG was already tested by Meurers (2012) 247 248 and by Riccardi et al. (2012). The latter for instance 249 applied this method to the C026 using the gPhone-54 250 spring gravimeter data. Precision on the SG scale 251 factor was around 0.01% while using absolute FG5 252 measurements it was limited to 0.4%.

253 To obtain the relative scale factors we applied a 254 multi-regression method on the SG raw signal (in volts) with respect to iOSG23 gravity (in nm/s²) and 255 to time (assuming a linear or second order polyno-256 257 mial drift). In addition, we also computed the scale factor for a moving window (2 days shifted by half a 258 259 day) both with unfiltered data and filtered data using a 260 band-pass filter centered on the tides, between 0.5 and 2.5 cycle per day (cpd). The results given in Table 2 261 262 are the mean values and standard deviation of the histogram of the scale factor estimates. In this way 263 264 the error estimate is more robust than the formal error 265 coming from the multi-regression on the entire 266 duration.

A duration of one month of 60 s samples was chosen to have enough precision in the adjustment, except for iGrav32(b) and iGrav6 for which only 11 and 23 days of recording at J9 were available, respectively. Since we do not have all the SG meters running in parallel at the same time we used two different monthly periods: 1–31 May 2017 for 273 iGrav30, iGrav31, iOSG23; 29 July–28 August 274 2017 for iGrav29, iGrav15, iGrav32(a), and C026 275 (GGP1 and TIDE), and additionally: 13–23 October 276 2017 for iGrav32b and 1–23 October 2017 for 277 iGrav6. 278

Different tests done on time spans of various 279 lengths (from 11 to 31 days) have shown that there is 280 a small variability of the relative scale factor (a few 281 per mil) and correlation coefficient (less than 1‰) 282 with time length. We also checked that the results are 283 unchanged when we consider the time shift that may 284 exist between different gravimeters. For instance, the 285 largest time shift that is largely due to the TIDE filter 286 of C026, which delays its signal 33 s with respect to 287 iOSG23 (see section on time delays), causes a 288 relative calibration change of 10^{-2} nm/s²/V which is 289 negligible in Table 2. 290

As expected, the errors in relative calibration are 291 much smaller than the errors in absolute calibration, 292 mostly in the range 1×10^{-4} – 8×10^{-4} (dimensionless); all correlation coefficients are very high (at least > 0.999). 295

It is noticeable that for iGrav6, iGrav15 and 296 iGrav32, the relative scale factors between pairs of 297 instruments did not change after transport from J9 to 298 Iceland, within 0.01% uncertainty (Schäfer et al., 299 2020). 300

2.3. Tidal Calibration Using K1 and M2 301

The aim of our method in this section is to find out 302 whether the ratio of relative calibration versus 303 absolute calibration inferred from the one-month 304 (May 2017) is confirmed by tidal analysis. We used 305 our longest common operation period of nearly 306 1 year of iGravs 29, 30, 31 and iOSG23 from 04 307 August 2016 to 19 June 2017 (321 days) to perform a 308 tidal analysis with the help of ET34-ANA-V61A 309 program (Ducarme & Schüller, 2018; Schüller, 310 2018). To achieve a better determination of the 311 diurnal and semi-diurnal tides we used an identical 312 FIR zero phase high-pass filter (with 0.8 cpd corner 313 frequency), based on Hanning-Window of 3001 min 314 length) for all data sets. We also assume no phase lag 315



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SG and filter	Duration	Rel Cal and error (nm/s²/ V)	Abs Cal and error (nm/s ² /V)	Rel Cal–Abs Cal and error (nm/s ² /V)
iOSG23 (reference)		-451 ± 0	-451 ± 2	0 ± 2
C026 GGP1	1 month	-792.2 ± 0.1	-792 ± 1	0.2 ± 1
No time shift	29/07/17–28/08/ 17			
C026 GGP1 with 2 s time shift	1 month 29/07/17–28/08/ 17	-792.2 ± 0.1	- 792 ± 1	0.2 ± 1
C026 TIDE	1 month	-791.5 ± 0.1	x	Х
No time shift	29/07/17–28/08/ 17			
C026 TIDE with 32 s time	1 month	-791.5 ± 0.1	х	Х
shift	29/07/17–28/08/ 17			
iGrav6	October 2017	-914.2 ± 0.2	x	Х
iGrav15	1 month 29/07/17–28/08/ 17	-932.3 ± 0.1	-934 ± 3	1.7 ± 3
iGrav29	1 month 29/07/17–28/08/ 17	-937.8 ± 0.1	-940 ± 4	2.2 ± 4
iGrav29	1 month 1–31 May 17	-937.7 ± 0.1	-940 ± 4	2.3 ± 4
iGrav30	1 month 1–31 May 17	-917.6 ± 0.1	-918 ± 4	0.3 ± 4
iGrav31	1 month 1–31 May 17	-850.5 ± 0.1	-853 ± 4	2.5 ± 4
iGrav32 (a)	1 month 29/07/17–28/08/ 17	-897.4 ± 0.7	- 898 ± 3	-0.6 ± 3
iGrav32 (b)	OCT 2017 ~ 13 days	-895.9 ± 0.1	х	x

Table	2
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Results for the absolute and relative calibrations of different SG meters in J9

316 between the different SG and use the absolute 317 calibration factor for each gravimeter.

The results for iGrav29, iGrav30 and iGrav31 compared to iOSG23 are shown in Table 3 and plotted in Fig. 4, where we kept only the large tide K1 in the diurnal band and M2 in the semi-diurnal band. As expected, the tidal analysis confirms the discrepancy between absolute and relative scale factors.

In the last column of Table 3 the formal precision of the tidal ratios is constant for all estimates and very small (1×10^{-5}) . However, the differences between K1 and M2 tidal ratios are 5×10^{-5} for iGrav29, 46×10^{-5} for iGrav30, and 9×10^{-5} for iGrav31 that are larger (and more realistic) values than the formal precision for each wave. Figure 4 shows the excellent agreement of the tidal ratio with the relative332calibration ratio except for K1 in the iGrav30/333iOSG23 comparison; the definite reason for this is334unknown but we show later in Sect. 5.1 that the noise335level of iGrav30 is significantly higher at low336frequencies than the other iGravs.337

2.4. Spectral Analysis of Tidal Residuals 338

Another way to test the calibration factors is to perform a spectral analysis of the difference between two calibrated time series which may reveal tidal residuals. In the following we consider iGrav29 versus iOSG23. We will assume that iOSG23 is well calibrated and will investigate the difference with iGrav29 by using different relative scale factors for 345

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from tidal analysis and time regression				
SG	REL. CAL (nm/s ² /V)	AG CAL (nm/s²/V)	AG CAL/REL CAL	Wave: tidal ratio
iGrav29	-937.8 ± 0.003	-940 ± 4	1.00235 ± 0.004	K1: 1.00239 ± 0.00001 M2: 1.00244 ± 0.00001
iGrav30	-917.6 ± 0.006	-918 ± 4	1.00044 ± 0.004	K1: 1.00003 ± 0.00001 M2: 1.00049 ± 0.00001
iGrav31	-850.5 ± 0.003	-853 ± 4	1.00294 ± 0.004	K1: 1.00291 ± 0.00001 M2: 1.00282 ± 0.00001

Comparison of ratio of relative calibration versus absolute calibration for iGrav29, iGrav30 and iGrav31 with respect to iOSG23 as inferred from tidal analysis and time regression



Figure 4 Ratio of relative calibration versus absolute calibration for iGrav29, iGrav30 and iGrav31 with respect to iOSG23 as inferred from tidal analysis (1 year) and time regression (1 month)

346this meter with increments of $0.4 \text{ nm/s}^2/\text{volt}$ (\approx 3470.04% in proportion) compared to $4 \text{ nm/s}^2/\text{volt}$ 348uncertainty from AG/SG calibration (see Table 3).

The results based on one month (May 2017) 60 s 349 samples of iGrav29 are shown in Fig. 5 for 4 350 351 different relative scale factors close to the value -937.8 nm/s²/volt inferred from the one month 352 353 regression in May 2017 (see Table 3). It is clearly 354 visible that the smallest tidal residuals at 1 and 2 cpd 355 appear for this scale factor. If we correct for the 3 s time shift between iGrav29 and iOSG23 (see Table 4) 356 then the tidal residuals in the spectrum of the gravity 357 difference almost vanish (in magenta in Fig. 5). 358 359 Similarly for iGrav30 and iGrav31 the minimal tidal



Spectral amplitude of residual gravity between iGrav29 (using different relative scale factors) and iOSG23; frequency units are cycle per day (cpd)

residuals correspond to the scale factors found from 360 time regression. 361

It is worth to note that using the absolute 362 calibration factor (- 940 nm/s²/volt) would lead to 363 tidal residuals that are 5–6 times larger when 364 compared to the adjusted relative calibration value 365 as shown on Fig. 6. 366

2.5. *Time Delay* 367

After having discussed the problem of amplitude 368 calibration, we focus now on the time delays that may 369 exist between the different SGs due to different 370 apparent spring constants (from the magnetic gradient 371 adjustment), masses, damping, filters and electronics. 372 The iOSG23 and the iGravs have a built-in Butter-373 worth filter with corner period of 5 s and a time delay 374 of 1.54 s followed by an anti-aliasing lowpass FIR 375



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Table 3

of unarysis perious			
	Time delay (s) 1 month of 1 s samples low pass filtered	Time delay (s) 1 month of 60 s samples after decimation	Time delay (s) 1 year of 60 s samples
iGrav6/iOSG23 ^a	3	3	Х
iGrav15/iOSG23	3	3	Х
iGrav29/iOSG23	3	3	2
iGrav30/iOSG23	2	2	3
iGrav31/iOSG23	2	2	1
iGrav32a/iOSG23	1	1	Х
iGrav32b/iOSG23 ^b	1	1	Х
C026 (GGP1)/iOSG23	3	2	2
C026 (TIDE)/iOSG23	33	32	31
C026(TIDE)/C026(GGP1)	30	30	30

 Table 4

 Time delays (in sec) between different SG using a cross-correlation method based on simultaneous data with various samplings and durations of analysis periods

^aOnly ~ 23 days available in October 2017

^bOnly \sim 13 days available in October 2017

376 filter consisting of 69 terms with a time delay of 377 4.25 s. In addition, there is a timing error of -0.62 s in the firmware implementing the FIR filter so its 378 379 delay is reduced to 3.63 s. The SG C026 has a builtin electronic low-pass filter called "GGP1" with a 380 corner period of 16.3 s and a time delay of 8.2 s 381 382 (Warburton, 1997). A TIDE filter is also integrated to 383 the electronics of the SG C026 with a corner period 384 of 72 s and a time delay of 32 s (Van Camp et al., 385 2000).

As before, we will use the one-month time series in May 2017 of iGrav29, iGrav30 and iGrav31 and iOSG23 sampled at 1 s to investigate this point. We



Figure 6 Spectral amplitude of residual gravity between iGrav29 (using best relative and absolute calibration factors) and iOSG23

also considered the time series of the older compact 389 SG C026 with data low pass filtered by two classical 390 electronic anti-aliasing filters widely used in the past 391 namely GGP1 and TIDE filters. For iGrav32 and 392 iGrav6 all available data in October 2017 were used 393 but one has to keep in mind that the time series are 394 shorter than one month and, even more important, 395 that these data are fully subject to initial drift (see 396 Sect. 3). 397

We apply a cross-correlation method between two398time series and determine the time of maximum399cross-correlation to estimate the time delay between400two time series.401

If the instrumental response as a function of 402 frequency is identical (except timing error) for two 403 systems, calculating a cross-correlation between their 404 output will give a unique estimate of the difference in 405 timing. In the present context, this is not the case. 406 Then, applying a cross-correlation method will only 407 give an estimate of timing difference averaged over a 408 certain range of frequency. A reasonable result was 409 obtained because the largest signals are the semi-410 diurnal and diurnal waves with frequency range 411 below 1e-3 cycle/sec where the phase response is 412 almost flat (inferred from Fig. 7). 413

As expected, the same cross-correlation analysis 414 done on raw (unfiltered) 1 s samples led to slightly 415 different results (not shown) because of the influence 416 of high frequency content (microseisms, earthquakes) 417

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Amplitude and phase transfer function for iGrav29 and iOSG23

(see Table 4). The values of the time delays do not 418 419 depend on the sampling (1 s or 1 min) if the high frequency content of the sec samples has been filtered 420 out. The time delays derived from 1-year correlation 421 422 analysis (August 2016-July 2017) for iGrav29, 423 iGrav30 and iGrav31 are similar to the values 424 inferred from one-month analysis. This analysis implies time invariance of the filter time delays. We 425 426 also checked that the time delay combinations between channels obey the transitivity rule where 427 428 cor(A/C) = cor(A/B) + cor(B/C), as can be seen in Table 4 for the filtered data TIDE and GGP1 429 430 implemented on C026.

431 A phase experiment test using the method
432 outlined in Van Camp et al. (2000) where injecting
433 known voltages (usually a sinusoidal or step-like
434 functions) into the control electronics of the system
435 enables one to determine time delay with a precision

of better than 0.1 s, was done on iGrav29 and 436 iOSG23 to retrieve the full transfer function both in 437 amplitude and phase delay of these two instruments. 438 The time delay becomes constant for frequencies 439 below 10^{-3} cpd (Fig. 7). The phase delay of iGrav29 440 with respect to iOSG23 is found to be 441 9.71 s - 7.16 s = 2.55 s. Since these two SGs have 442 identical electronics, this phase difference must be 443 caused by the different masses of the spheres, the 444 force gradient and damping in these instruments. As 445 done before for the amplitudes, we also use the tidal 446 analysis of 1 year of data to check the respective time 447 delays by computing the M2 and K1 phase lags. The 448 2.55 s phase delay between iGrav29 and iOSG23 is in 449 close agreement with the tidal results (see Fig. 8). 450

A similar experiment that used injected sine 451 waves rather than a step function was done on 452 C026 in 2012 and led to a time delay of 9.7 ± 0.4 s 453 from the GGP1 filtered data. 454

If we assume the time delay of iOSG23 is 7.16 s, 455 the experimental phase delay of C026 with respect to iOSG23 would be 2.54 s. This value is very close to the ones plotted in Fig. 9. 458

3. General Initialization Procedures for SGs 459

Over many years a general procedure has been 460 developed to minimize drift and offsets in SGs. 461





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Comparison of time delays for C026 (TIDE filter) with respect to iOSG23, using time correlation or tidal analysis of major waves K1 and M2 (top); comparison of time delays for C026 (filter GGP1) with respect to iOSG23, using time correlation or tidal analysis of major waves K1 and M2 (bottom)

462 Figure 7 of Hinderer et al. (2015) shows a diagram of 463 the SG sensor and its major components. The main 464 superconducting components are the sphere, the 465 magnet coils, the heat switches and the supercon-466 ducting shield. The sphere position is sensed by the 467 linear transducer consisting of the upper, central and lower capacitance plates. All of these components are 468 mounted on or inside the Al or Cu body of the sensor 469 470 which is positioned inside a vacuum can that is sur-471 rounded by a liquid helium bath at 4.2 K. The body is suspended from the lid of the vacuum can with three 472 473 G-10 fiberglass laminate posts that thermally isolate 474 the body from the helium bath. With this isolation, a 475 Germanium thermometer operating in a Wheatstone 476 bridge with a temperature control heater precisely

controls the temperature of the body at about 4.4 K or 477 0.2 K above the bath temperature. In addition, there 478 are several components used only during the instal-479 lation of the sensor: a Body heater and a Si diode 480 thermometer reside on the top of the magnet form and 481 are used to heat the magnet form (Body) and record 482 its temperature (Body-T); a Mu metal shield sur-483 rounds the vacuum in order to reduce the Earth's 484 magnetic field; and a charcoal getter to add and to 485 extract gas from the vacuum can. The charcoal getter 486 consists of a small Cu or Al cylinder that contains 487 charcoal pellets glued to a heater. The getter cylinder 488 can either be outside the vacuum can and connected 489 by a tube as shown in the diagram or it can be inside 490 the vacuum can. When the charcoal is at cryogenic 491 temperatures it adsorbs He gas from the vacuum can. 492 This gas can be released by activating the getter 493 heater to heat the charcoal above 70 K. 494

After cooling the Dewar and gravity meter sensor 495 to 4.2 K, initialization of SGs generally includes five 496 standard procedures that are followed in a well 497 determined order. First, a body heater is used to heat 498 the sensor body and all the superconducting compo-499 nents inside the vacuum can above 32 K which is 500 well above the superconducting transition tempera-501 ture of Nb and the mu-metal shield is demagnetized. 502 This minimizes the presence of the Earth's magnetic 503 field trapped in the sphere and coils before levitation. 504 Second, the sensor body is fast cooled to 4.2 K by 505 briefly heating the charcoal getter. This releases He 506 gas into the vacuum container which conducts heat 507 directly between the body and the walls of the vac-508 uum can. This cools the body in a few minutes versus 509 the 10 to 12 h if cooling were only via the G-10 posts. 510 After cooling to 4.2 K, the temperature control is 511 turned on which raises the temperature to the control 512 point near to 4.4 K. Third, the sphere is levitated, and 513 the magnetic gradient adjusted. Fourth, the sensor is 514 low temperature annealed by raising the temperature 515 to about 5.2 K and lowered back to 4.2 K. This 516 reduces the magnitude of offsets induced during 517 excursions of the temperature control between 4.2 to 518 5.2 K. Then the temperature control is turned on 519 again and the sensor returns to its control point near 520 to 4.4 K. And fifth, the thermal levelers are used to 521 tilt-desensitize the sensor. 522



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523 Variations to the installation may occur: some 524 iGravs have side coils and the field is trapped after the demagnetization but before the fast cooling; He 525 gas may or may not be released from the getter to 526 527 cool from 5.2 K during the low temperature annealing; and the order of low temperature annealing and 528 529 tilting may be interchanged. In addition, some vari-530 ations may occur due to operator error during set-up and initialization at a new site when site preparation 531 532 is not complete or other difficulties occur. For example, during the July 2016 initialization at J9, two 533 534 errors occurred. For iGrav29, the low temperature 535 annealing was done improperly. The sensor was heated to 5.2 K, but it was then cooled back to its 536 537 control point at 4.4 K rather than being cooled fully 538 to 4.2 K before being returned to the control point 539 while, for iGrav30, the low temperature annealing 540 was omitted entirely.

541

4. Instrumental Drift

542 In this section we investigate the instrumental 543 drift of the iGravs and iOSG23 collocated at J9. Previous studies have reported that the instrumental 544 drift of SGs can be modelled by a short-term expo-545 nential function followed by a linear trend of 10 to 546 547 50 nm/s²/year (Crossley et al., 2004; Hinderer et al., 548 2015; Van Camp & Francis, 2007). However, for 549 records longer than 10 years, Van Camp and Francis (2007) showed that the long-term drift for GWR 550 551 C021 is better modelled by an exponential. More recent work by Schäfer et al. (2020) showed that the 552 553 initial drifts in GWR iGrav SGs require additional short-term exponential functions to model rapid drifts 554 555 that occur immediately after initialization and sphere levitation. In addition, Dykowski et al. (2019) have 556 shown for iGrav27 that drifts also occur in the body 557 558 temperature (Body-T) that are highly correlated 559 (0.98) with the gravity drifts and that these can also 560 be modelled by an initial exponential term followed by a linear drift. 561

In this work, we model the instrumental drift of
SG as the sum of several exponential decaying
functions (up to 3) and a linear term that remains very
stable in time after the exponential terms become
negligible.

The model of instrumental drift is hence as 567 follows: 568

$$g(t) = g_0 + A_1 e^{-\frac{t-t_0}{t_1}} + A_2 e^{-\frac{t-t_0}{t_2}} + A_3 e^{-\frac{t-t_0}{t_3}} + C(t-t_0)$$
(1)

where g(t) is the gravity as a function of time t, with 570 initial values g_0 and t_0 , A_1 , A_2 and A_3 the amplitudes, 571 t₁, t₂ and t₃ the time constants, and C the coefficient 572 of the linear term. A Levenberg-Marquardt iteration 573 algorithm is applied to reach convergence in the fit. 574 The functional drift of the Body-T can also be 575 approximated by exponential terms plus a linear term 576 very similarly to what we do for the gravity signal. 577 Long term changes in the Body-T sensor indicate that 578 thermal gradients continue to change in the sensor 579 over long periods of time. It is hypothesized that this 580 is from the charcoal getter continuing to adsorb He 581 gas out of the vacuum can and that this is one source 582 of drift. 583

We first investigate the long-term behavior of 584 iOSG23 which was installed in February 2016 and 585 still operates today. This meter will act as reference 586 gravimeter throughout this study. We use a series of 587 16 AG measurements taken at J9 with FG5#206 588 during the years 2016-2019 to infer the iOSG23 drift 589 components. In another section we examine the initial 590 drift and Body-T behavior of 3 iGravs (#29, #30 and 591 #31) that were all initialized in June 2016 and re-592 initialized in October 2016. Also, since iGrav29 was 593 re-levitated both in November 2020 and December 594 2020, we can investigate how the initial gravimeter 595 drift and Body-T drift evolve during these additional 596 re-levitations. 597

4.1. Long Term Drift of OSG23

We investigate the drift behavior of iOSG23 using 599 a 4.1 year-long record (1520 days from February 3, 600 2016 to April 20, 2020). To prepare the data, a first 601 decimation filter is used from 1 to 60 s. The major 602 gravity steps in iOSG23 are removed by comparison 603 to a data record prepared in the same way for iGrav29 604 which was operating nearby at J9. Subsequently, 605 spikes and large earthquakes are removed by inter-606 polating over the disturbances. After all corrections 607

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Figure 10 Determination of iOSG23 instrumental linear drift rate using AG (FG5#206) values

are made a second decimation filter reduces the datato hourly intervals.

610 In the following we determine the long-term linear drift by fitting AG data to the last 3 years of 611 iOSG23 data. In this case we are not considering the 612 613 exponential drift that typically occurs immediately 614 after the initialization of the gravimeter. Then, after 615 removing this linear drift from the entire data set, we use a non-linear curve fitting tool based on several 616 617 exponentials.

618 Before applying this procedure, we first need to 619 compare the iOSG23 residual values (observations 620 corrected for the local tide, barometric pressure and 621 polar motion) to measured AG values at J9 using 622 FG5#206 over the same period (corrected exactly in 623 the same way).

624 In Fig. 10, the black squares show the values of 625 the AG measurements minus the mean value of the 626 AG measurements taken in the period from 3 October 627 2016 to 12 June 2019, which covers the record of 628 iOSG23 data. These values are offset by 100 nm/s² so 629 that the 3 plots of the AG (black squares) values, the

Table 5
Drift rates: results of the linear fit to AG (FG5#206] and SG
(iOSG23) data

	Linear trend and error (nm/s ² /year)
AG (FG5#206)	-32.3 ± 7.5
SG (iOSG23)	-6.0 ± 5.1
SG-AG	27.0 ± 6.3

SG (red dots) values and the difference SG-AG (blue630triangles) values do not overlap and provide an easier631visual inspection.632

In the determination of the SG linear drift, we 633 excluded the first 3 points in 2016 which are likely to 634 be affected by getter pump out and are part of the 635 initial exponential drift term. 636

The results of the linear fitting procedure of the637data sets shown in Fig. 10 are given in Table 5.638

For the AG points, we measure a decrease in 639 gravity of $-32.3 \text{ nm/s}^2/\text{year}$ with $R^2 = 0.59 \text{ most}$ 640 probably of hydrological origin since vertical motions 641 due to tectonics are too small as inferred from GPS 642 measurements at J9. For the iOSG23 data we measure 643 a smaller decreasing rate of $-6 \text{ nm/s}^2/\text{year}$ with 644 $R^2 = 0.11$ and for the difference SG-AG, we get a 645 positive rate of + 27.0 nm/s²/year with R² = 0.59. 646

This result indicates that the instrumental linear 647 drift determined for iOSG23 by comparison to the 648 AG measurements is $+ 27.0 \text{ nm/s}^2/\text{year}$ which is a 649 typical value for other SGs. However, there is a high 650 relative uncertainty (23.3%) for this drift rate. The 651 dispersion of the points in Fig. 10 that are not 652 perfectly aligned on a straight line is not clear. It is 653 possible that the AG errors are underestimated or that 654 the AG senses slightly different hydrological effects 655 due to its placement in the vault. 656

After removing the drift inferred from the AG657points, the iOSG23 residual gravity data have been658fitted to a combination of exponential and linear659terms according to Eq. (1). The fit results are given in660Table 6 and Fig. 11 shows the superposition of the661fitted model to the iOSG23 gravity data.662

The fitted iOSG23 instrumental linear drift rate of66324.4 nm/s²/year is close to the value of 27.0 nm/s²/664year in Table 5 but differs because the fitting665procedure uses all the hourly data from iOSG23 in666one case and only the few episodic AG/SG parallel667measurements on the other case.668

After removing a linear term of 0.3 mK/year, a 669 similar method is used to fit to the Body-T data for 670 iOSG23. The Body-T time constants are shown in 671 Table 6 and a comparison of the data and the fit curve 672 are shown in Fig. 12. Two of the time constants for 673 gravity and Body-T are similar with a very short time 674 delay t1 less than half a day and a very long one t3 675 close to 150 days. The fitting process for the Body-T 676



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Table 6

Results for the exponential	and intern fining of	, 1000 <u>2</u> 5 grai	ny ana boay 1	emp signai, sj	moors in me nea	act are the sum	
Data starts 03/02/2016	A ₁	t ₁	A_2	t ₂	A ₃	t ₃	С
Record length 1520 days iOSG23 gravity	nm/s ²	days	nm/s ²	days	nm/s ²	days	nm/s ² /year
3 exp fit	- 131.2	0.4	х	x	- 144.4	153.5	24.4
iOSG23 Body Temp	mK	days	mK	days	mK	days	mK/year
3 exp fit	- 1.8	0.4	- 0.3	57.2	- 0.4	143.2	0.3







677 converges to find the intermediate terms (A2 = -0.3678 mK, t2 = 57.2 days) but does not converge to find 679 similar intermediate terms for the gravity residual 680 signal.

The correlation we already introduced between gravity and body temperature drifts appears very clearly on Fig. 13. The left part is coming from the strong exponential initial drift occurring on both signals. Later during instrument operation, gravity and Body-T are still correlated but the correlation is noisier.

As observed by Dykowski et al. (2019), the
instrumental drift highly correlates with Body Temp.
This is true for the exponential part after levitation as
well as for the long-term linear part. The correlation
factor between gravity and Body-T signals for
iOSG23 is rather large (0.88). This suggests that the
long-term linear drift (or part of it) in SGs might in



Body-T signal of iOSG23 as a function of time; the observations are in black and the best fit combining exponential and linear terms according to Table 6 in red

fact be due to this continued adsorbing process of the 695 getter. 696

4.2. Drift Behavior of iGravs 697

iGrav29, iGrav30 and iGrav31 were first initialized in 699 July 2016 at J9. Since there were many disturbances 700 during and after this installation, it was decided to 701 repeat the entire initialization process on iGrav29 and 702 iGrav30 in October 2016; while only low-tempera-703 ture annealing of iGrav31 was done to complete its 704 previous initialization. iGrav #30 and #31 then 705 operated at J9 until the end of June 2017 at which 706 time iGrav30 was shipped cold for installation at the 707 Strengbach catchment in the French Vosges moun-708 tains (Chaffaut et al., 2020) while iGrav31 was 709 warmed to room temperature for its future shipment 710



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Figure 13 Correlation between iOSG23 gravity residuals and body temperature signals using the 4.2-year data set

711 in late March 2019 to a mountain site directly above 712 GWR iOSG24 which is operating in the LSBB 713 underground laboratory in Rustrel. iGrav29 was also 714 scheduled to move to another water catchment of the 715 Ozcar network (Gaillardet et al., 2018) but, due to 716 COVID-19 restrictions, it continues to operate at J9 717 presently. For reasons discussed below, it was 718 warmed to room temperature in October 2019 and 719 reinitialized for a 3rd time. In December 2020 an experiment was done where-without activating the 720 getter-the sphere was lowered, and the magnets 721 purged of currents. Then after a few days the sphere 722 723 was again re-levitated without using the getter.

724 In analyzing data from these iGravs, we used 725 iOSG23 as a reference instrument so that we could look directly at the difference signals iGrav29-726 727 iOSG23, iGrav30-iOS G23 and iGrav31-iOSG23. 728 It is a major advantage to use iOSG23 as a reference 729 rather than a calculated tide model because iOSG23 provides a precise measure of all gravity changes 730 731 while any model is incomplete: the model does not 732 include hydrological signals, it assumes a constant 733 admittance to the atmosphere, and it approximates 734 many of the long-period tidal signals. We first correct 735 the iOSG23 data for the linear and exponential drifts 736 previously found (see Table 6). Then the gravity 737 differences are taken between the three iGravs and 738 the corrected iOSG23 signal using the calibration 739 factors listed in Table 2. Earthquakes, offsets and 740 other disturbances are removed, and the data are further filtered and decimated to hourly intervals. 741

The results for the initial drifts of iGrav29-742 iOSG23, iGrav30-iOSG23 and iGrav31-iOSG23 are 743 plotted in Fig. 14 (where arrows show the initializa-744 tion events) along with the residual gravity signal for 745 iOSG23 calculated with a tidal model and corrected 746 for its exponential and linear drifts from Table 6. 747 Long-period tides, polar motion and hydrology are 748 not corrected for, so they appear clearly on the 749 iOSG23 residual signal but they do not appear on the 750 difference signals. The difference drift curves are 751 very smooth since all the unmodelled signals that 752 show up in the iOSG23 curve are eliminated in the 753 iGrav29, iGrav30 and iGrav31 difference curves. It is 754 not possible to measure such drifts with this high 755 precision without using a reference SG. Figure 15 756 shows the Body temperature data over the same time 757 period as shown for the gravity data in Fig. 14. 758

There are several features on these data that stand 759 out. In Fig. 14, a negative drift is observed immedi-760 ately after the first initialization of iGrav29 in July 761 2016 (red line). After the second initialization in 762 October 2016, the residual drift for iGrav29 looks 763 reasonable at first, but after about 180 days it turns 764 into a negative drift rate of about -51.9 nm/s²/year 765 which was observed for the next 2 years (green line). 766 We also observe increasing noise levels in both 767 iGrav29 and iOSG23 at the start of this negative drift 768 period. This is likely from build-up of ice in neck of 769 iGrav29. In contrast to Fig. 14, all the Body-T drifts 770



Figure 14 Gravity difference signals between iGrav29, iGrav30 and iGrav31 and iOSG23 corrected for its drift curve for the entire 4.5 year-long record at J9, Strasbourg

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Figure 15 Body temperature signals for iGrav29, iGrav30 and iGrav31 and for iOSG23 for 4.5 year-long record at J9, Strasbourg

in Fig. 15 are smooth curves in the positive direction.
The only uncertainly in the Body-T data is the offset
that occurs in the iGrav29 Body-T after the October
2019 re-initialization. This is most likely a problem
with the thermometry circuitry measuring the Body-T
but this remains unproven.

We separate the data into three sections to model the drift curve function according to Eq. 1 and to examine the correlation between the gravity residual and Body-T. The present section includes the July and October 2016 initializations, the next section examines the initialization in October 2019, and the third the re-levitation in December 2020.

784 4.2.2 July and October 2016

785 Figure 16 shows the data from July 28, 2016 to March 5, 2017 in more detail. These data include two 786 787 specific time spans: a first one that lasted about 788 75 days after the installations on July 28, 2016; a second one that lasted 219 days after the re-initial-789 790 izations of iGrav29 and iGrav30 and the low temperature annealing of iGrav31 (that occurred on 791 792 October 23, 2016). The data for iGrav31-iOSG23 are 793 the same as in Fig. 14. However, before fitting the 794 data for iGrav29-iOSG23 to Eq. 1, they must be 795 corrected for its negative drift. Otherwise, the neg-796 ative drift will interfere with the fitting parameters for 797 the longer-term exponential functions. A decision 798 was also made to correct iGrav30-iOSG23 for the 799 same negative drift since it appears that the iGrav30-



Figure 16

Initial drift curves of gravity differences iGrav29-iOSG23, iGrav30-iOSG23, iGrav31-iOSG23 and iOSG23 residual signal after initialization in July and October 2016 through to March 5, 2017 and after correcting iGrav29-iOSG23 and iGrav30-iOSG23 for the negative drift observed in Fig. 14

iOSG23 data was also beginning to trend negative in800Fig. 16. With these corrections made, the drift curves801for all 3 iGravs are similar for the last 100 to802

150 days of Fig. 16. 803 There is a striking difference between the gravity 804 difference data of Fig. 16 and the Body-T data of 805 Fig. 17 in that the Body-T curves behave continu-806 ously across the October 2016 re-levitation while 807 there is a discontinuity in the gravity differences after 808 the October 2016 levitation in terms of generation of 809 a new initial drift. This is slightly misleading since 810 rapid drifts do occur in the Body-T data immediately 811 after the initialization procedures, for example for 812 iGrav29 Body-T rapid drifts of about 50 to 70 mK 813 occur at the beginning of both the July and October 814 installations; however, since they last less than 1 h, 815 they are removed by the filtering and decimation 816 process. Corresponding drifts occur in the gravity 817 differences, but these are difficult to observe since 818 they occur during the initialization procedures. 819 Nonetheless, the long-term Body-T rapidly returns 820 to its previous functional form as displayed in 821 Fig. 17. 822

The continuity of the Body-T data shows that the gas released from the getter and the distribution of gas in the vacuum can may depend upon the history of its use. He gas could be bound more tightly to the 826



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Figure 17 Initial drift curves of Body temperatures for iGrav29, iGrav30 and iGrav31 after the initializations in July and October 2016 through to March 5, 2017

827 getter material after it has remained cold for a long time so that less gas is released when it is heated. 828 829 Also, there are different time constants associated with gas pumped out of or reentering different 830 831 locations inside the gravity sensor. For example, short time constants for the open volume inside the 832 833 vacuum can, intermediate time constants for gas located between the shield and vacuum can, and long-834

time constants for gas trapped inside the magnet 835 coils. 836

In Table 7, we show the fit coefficients of two 837 exponential functions to both the gravity difference 838 and Body-T data shown in Figs. 16 and 17; the used 839 formalism is the same as in Eq. (1), but neglecting 840 the third exponential $(A_3 = 0)$. For the Body-T data, 841 we fit a linear drift to the last 60 days data and 842 subtracted it before fitting with two exponential 843 functions. We see remarkably similar functions for 844 iGrav29, iGrav30 and iGrav31 Body-T exponentials 845 with: A1 varying between -6 to -9 mK; t1 846 between 8 to 12 days; A2 between -8 to -10847 mK; t2 between 40 to 60 days; while the linear terms 848 vary more widely between 0.5 to 2.7 mK/year. 849

A similar fitting procedure was done for the 850 Gravity difference data starting October 2016. In this 851 case, the fitting functions for iGrav29-iOSG23 and 852 iGrav30-iOSG23 were very close: with A1 between 853 -56 and -74 nm/s²; t1 between 3.2 and 3.7 days; 854 A2 between -70 to -74 nm/s²; t2 between 44 and 855 51 days; and linear terms both close to 71 $\text{nm/s}^2/\text{year}$. 856 The amplitudes for the iGrav31-iOSG23 days are 857 smaller (A1 = -12 and A2 = -41 nm/s²) while t2 858 is shorter (1.4 days) and t2 longer (84.9 days) with a 859

Table 7

Amplitude and time constants of the exponential fitting of iGrav29–iOSG23, iGrav30–iOSG23 and iGrav31–iOSG23 gravity signal for 72 days after July 2016 levitation and 219 days after October 2016 levitation and for iGravs 29, 30 and 31 body temperatures after July 2016 initialization (291 days)

		initialization (2	91 auys)		
Gravity differences	A ₁ nm/s ²	t ₁ days	A ₂ nm/s ²	t ₂ days	C nm/s ² /year
July 2016 (72 days) data					
iGrav29-iOSG23 ^a	44.4	0.6	18.1	8.2	N/A
iGrav30-iOSG023	- 33.3	7.1	- 104.8	154.3	N/A
iGrav31-iOSG023 ^b	- 31.7	7.4	- 78.7	71.6	N/A
October 2016 (219 days)					
iGrav29–iOSG23	- 74.1	3.2	- 74.4	50.8	70.8
iGrav30-iOSG023	- 55.6	3.7	- 70.1	43.7	71.1
iGrav31-iOSG023°	- 12.2	14	- 41.4	84.9	77.2
Body temperatures	A1	t1	A2	t2	Linear
	mK	days	mK	days	mK/year
July and October 2016 (291 days	5)				
iGrav29 Body-T	- 6.0	8.1	- 10.0	40.1	2.3
iGrav30 Body-T	- 9.0	12.6	- 10.0	61.3	0.5
iGrav31 Body-T	- 6.0	10.1	- 8.0	40.2	2.7

^aLow temp. annealing done improperly

^bNo low temp. annealing done ^cLow TEMP. annealed only

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Figure 18 Correlation between iGrav–iOSG23 difference signals and Body Temperatures for iGrav29, iGrav30 and iGrav31 for both the July and October 2016 initializations

steeper linear fit of 77 nm/s²/year. It is not surprising 860 that these amplitudes (seen both in Table 7 and 861 Fig. 16) are much smaller for iGrav31 than for iGravs 862 29 and 30. The iGravs 29 and 30 were completely re-863 initialized (sphere lowered and magnet currents 864 865 purged, bodies heated to 32 K and fast cooled to 4.2 K by adding gas from the getter, spheres relevi-866 867 tated, bodies low temperature annealed, and sphere 868 recentered). In contrast iGrav31's body was simply low temperature annealed and then the sphere 869 870 recentered.

871 We have also fit 2 exponential functions to the gravity differences following the July 2016 initial-872 ization. In these cases, due to the shorter records, we 873 874 chose to fit 2 exponential terms without first 875 subtracting a linear term. In spite of the shorter 876 records, the different analysis techniques and the 877 quality of the data, the fits for iGrav30-iOSG23 and 878 iGrav31-iOSG23 are still similar to the October 2016 fits although both the t1 and t2 time constants are879longer. In contrast, the fit of iGrav29–iOSG23 is880clearly anomalous with positive amplitudes for both881A1 and A2. This is most certainly due to the882incomplete low temperature anneal procedure done883for iGrav29 in July 2016.884

An alternative method to determine the relation-885 ship between the gravity difference signals and the 886 Body temperatures is to measure the correlation 887 between these two data sets directly. Strictly speaking 888 the iGrav-iOSG23 gravity differences should obey a 889 function of the iGrav-iOSG23 Body-Temp differ-890 ences but since the Body-Temp changes for iOSG23 891 are so small (see Fig. 12) compared to the iGrav 892 changes we have neglected them. The results of this 893 analysis are shown in Fig. 18 for both the July and 894 October 2016 initializations and shows a more 895 complicated relationship between the initial drift 896 and the Body-T than the nearly linear relationship 897 that was observed in Fig. 13. 898

For the sake of completeness, we have also 899 indicated in Table 8 the initial drift values we found 900 for iGrav6, iGrav32a and iGrav32b (before and after 901 upgrade at GWR respectively) and iGrav15 which 902 were installed in summer and fall 2017. Notice that 903 some of the fits are done on very short records 904 because of the short availability at J9 (especially 905 iGrav32a and iGrav32b). We do not discuss here the 906 impact of transportation in cold state (or warmed up) 907 on the initial drift rates of SGs. Such a discussion for 908 iGrav6, 15 and 32 after transportation from J9 to 909 Iceland is done in Schäfer et al. (2020). 910

In Table 8 the short time constant t_1 is close to 911 0.4 day and t_2 in the range 1.7–3.3 days. In terms of 912 amplitude, the largest one is for iGrav6 (both for A₁ 913

Table	8
	~

Amplitude and time constants of the initial exponential fitting of iGrav6, iGrav32a, iGrav32b, iGrav15 gravity signal using two exponentials (A_1, t_1, A_2, t_2)

2 exponential fit after linear term removed	$A_1 (nm/s^2)$	t ₁ (days)	$A_2 (nm/s^2)$	t ₂ (days)
iGrav6–iOSG23 (25.1 days)	- 39.3	0.4	- 67.8	3.3
iGrav32a–iOSG23 (15.8 days)	-10.4	0.4	- 40.9	2.1
iGrav32b-iOSG23 (10.4 days)	- 4.4	0.3	- 24.6	2.0
iGrav15-iOSG23 (18.3 days)	- 4.1	0.3	- 33.3	1.7







Figure 19 Gravity difference iGrav29-iOSG23 (top) and Body-T (bottom) for October 2019 re-initialization and December 2020 re-levitation

914 and A_2). Because of the short available durations only 915 short-term exponential terms can be estimated and the long-term drift behavior remains unknown. 916

917 4.2.3 October 2019

918 In October 2019 we decided to re-initialize iGrav29

919 for a 3rd time. The reason was to confirm the premise (Schäfer et al., 2020) that iGravs with negative drifts 920 could be restored to normal operation by warming 921 them to room temperature and re-initializing them. In 922 addition, it was recommended not to trap flux with 923 the side coils if there were plans to move an iGrav in 924 the future. Therefore on September 12, 2019, the 925 refrigeration system was turned off and the liquid He 926 evaporated in about 10 days. On October 1, the 927 Dewar was pumped out for 48 h with a primary and 928 turbomolecular pump to reduce its pressure from 56 929 to 5.6 Pascal; and on October 3, the refrigeration 930 system was turned back on. Cooling and refill with 931 liquid He took an additional 22 days, so the re-932 initialization took place on October 26, 2019. In this 933 case, all the initialization steps were rigorously 934 followed, and no flux was trapped in the side coils. 935

Figure 19 shows the drift analysis of 423 days 936 following the October 2019 initialization. The green 937 trace in the top panel is the direct difference signal 938 iGrav29-iOSG23 while the lower panel shows the 939 Body-T. Since the green curve becomes flat, it means 940 the drift rate of iGrav29 is nearly identical to that of 941 iOSG23. The red curve is the difference curve with 942 the drift correction made to iOSG23, while the blue 943 line is the calculated drift of iOSG23. This important 944 result confirms that the negative drift in iGrav29 had 945 been eliminated by warming it to room temperature 946 and re-cooling and re-initializing it without trapped 947 flux. 948

Table 9 shows the fitting parameters for the 949 gravity difference and the Body-T, while Fig. 20 950 compares the correlation between iGrav29-iOSG23 951 difference and Body-T for October 2019 with the 952

Table	9

Amplitude and time constants of the exponential fitting of iGrav29-iOSG23 and Body-T for 423 days after October 2019 levitation; symbols in the header are the same as in Eq. (1)

			1 ()		
Gravity differences	A_1 nm/s ²	t ₁ days	A_2 nm/s ²	t ₂ days	C nm/s ² /year
October 2019 (423 days) iGrav29- iOSG23	- 22.9	4.9	- 113	62.9	18
Body temperatures	A1 mK	t1 days	A2 mK	t2 days	Linear mK/year
October 2019 (423 days) iGrav29 Body-T	- 3.3	17.1	- 4.8	73.8	0.68

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Figure 20 Gravity differences (iGrav–iOSG23) versus Body Temp signals for iGrav29, iGrav30 and iGrav31 after October 2016 levitation (and October 2019 for iGrav29)

953 correlations between iGrav–iOSG23 differences and
954 Body-T for iGrav29, iGrav30 and iGrav31 for
955 October 2016.

956 From these data and from earlier data (Figs. 18, 957 13), there is clearly a linear relationship between gravity drift and Body-T as the second exponential 958 959 fits (A2 and t2) become dominant (after 2-3 months). There may also be a linear relationship immediately 960 961 after the initialization (for the first 2 months) but it clearly is with a different slope after 2-3 months. We 962 note, however, that a linear slope on the Gravity-963 Body-T plot means that both Gravity and Body-T 964 965 have the same functional form, not that they are both 966 linear. So, a likely interpretation is that both gravity drift and Body-T have nearly identical exponential 967 968 functions early after the initialization (first 2 months) 969 and a combination of different exponential and linear 970 functions after 2-3 months. After 2 months a curva-971 ture is seen in the correlation plot (Fig. 18) which indicates that the gravity drift and Body-T drift 972 functions are not identical. This is also seen by the 973 974 fact that the t1 time constants of the Body-T data are 975 generally longer than that of the gravity drift 976 functions.

977 4.2.4 December 2020

As a final experiment, on December 26, 2020, the
sphere was carefully lowered and the magnet coils
purged of currents without activating the getter, so

that no additional He gas was released. Then after 981 2 days, the sphere was re-levitated, a low temperature 982 annealing performed, and the tilt rechecked. Most 983 importantly, the low temperature annealing was 984 performed without using the getter. As we see from 985 Fig. 19, there is no observable change in drift in 986 either the Body-T or the gravity difference signals. 987 While this test positively confirms that initial drifts in 988 iGravs are due to the getter adsorbing gas out of the 989 vacuum can, it cannot establish with certainty that 990 remaining linear drifts (10-50 nm/s²/year) are caused 991 by continued gas removal or if there is some 992 additional drift mechanism. 993

4.2.5 Moving SGs 994

From the data in Schäfer et al. (2020) and the data of 995 this study, we can recommend preferable methods for 996 moving SGs. 997

- 1. As a rule, it is always safest to move an SG warm998and at room temperature and to re-evacuate the999dewar before cooling it at a new site.1000
- 2. Any iGrav that uses trapped flux should be 1001 warmed to room temperature before it is moved. 1002 As discussed in Schäfer et al. (2020), shipping cold iGravs with flux trapping coils activated has produced large negative drifts. 1005
- 3. Some users may want to move their SG cold at 1006 4.2 K and with the dewar filled with liquid He. 1007 First, this eliminates the requirement to cool and 1008 fill the dewar with liquid He at a remote site which 1009 takes about 10 days. Second—in both cases (1) 1010 and (2) above-the initial drift curve will return at 1011 the new site and more frequent AG measurements 1012 will be necessary to determine the drift curve. In 1013 this case, the user can lower the sphere and 1014 carefully purge the coils of superconducting 1015 currents before moving the instrument, then re-1016 levitate and low temperature anneal at the new 1017 site. If this is done carefully-without using the 1018 getter to release He gas-either when lowering the 1019 sphere or re-levitating the sphere at the new site, it 1020 will eliminate the repetition of the initial drift 1021 curve of the iGrav at the new location. 1022



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1023 5. Environmental and Instrumental Noise Levels

1024 5.1. Observed Noise Levels

1025 In order to have a complete comparison of the SG recording at J9 during a certain amount of time (from 1026 1027 a few weeks to several years), we applied a standardized procedure to estimate a noise level that 1028 1029 was statistically significant, knowing that these instruments did not always record simultaneously. 1030 We focus here on the SGs but include some other 1031 instruments. These are the absolute gravimeter 1032 FG5#206 of Micro-g LaCoste, the three spring 1033 1034 gravimeters (LaCoste & Romberg Earth Tide 1035 gravimeter ET-11, Micro-g LaCoste gPhone-54, 1036 LaCoste-Romberg Graviton-EG1194) and the long 1037 period seismometers STS-2 which were also operated 1038 in J9 in parallel to the SG C026 and analyzed in Riccardi et al. (2011), Arnoso et al. (2014), Rosat 1039 1040 et al. (2015) and Rosat and Hinderer (2018).

1041 Similar to the procedure by Berger et al. (2004) for stations of the global seismographic network 1042 1043 (GSN), we computed power spectral densities (PSDs) of calibrated raw data (1 s sampling) using a modified 1044 1045 Welch periodogram (Welch 1967) method applied on 1046 12 h time windows overlapped by 6 h. From the 1047 density distribution of PSDs, we computed the 1st, 1048 5th, 25th and 50th percentiles but we have selected 1049 only the 5th-tile for the plots in Figs. 21 and 22 to be compared with the GSN noise models of Berger et al. 1050 1051 (2004). The new low noise model (NLNM) of 1052 Peterson (1993) and the more recent statistical low noise model (SLNM) by Castellaro and Mulargia 1053 (2012) are also plotted for reference. Note that the 1054 NLNM corresponds to the lower envelope of seismic 1055 1056 PSDs computed at that time, so it represents the 1057 lowest noise level reached by seismometers anywhere 1058 in the world.

Fifth percentile of PSD noise levels of the eight
GWR Superconducting Gravimeters (C026, iOSG23,
iGrav6, iGrav15, iGrav29, iGrav30, iGrav31,
iGrav32) that were recording at the J9 Gravimetric
Observatory of Strasbourg are shown on Fig. 21.

1064 The SGs present the lowest noise magnitude in 1065 the seismic band between 10^{-3} and 10^{-2} Hz for 1066 gravimeters. However, STS-1 long period seismome-1067 ters provide lower noise above 1.5×10^{-3} Hz as



Figure 21

Fifth percentile of PSD noise levels computed on 1-s sampling data of the eight GWR Superconducting Gravimeters (C026, iOSG23, iGrav6, iGrav15, iGrav29, iGrav30 and iGrav31 and iGrav32) that were recording at the J9 Gravimetric Observatory of Strasbourg (France). The new low noise model (NLNM) of Peterson (1993) is represented by the thick brown line. In solid gray lines, we have plotted the 5th percentile of the PSD levels obtained by Berger et al. (2004) for the Global Seismographic Network (GSN 5th-tile)



Figure 22

Fifth percentile of PSD noise levels computed on 1-s sampling data of the 3 GWR Superconducting Gravimeters (C026, iOSG23, iGrav29), of the STS-2 seismometer, of the Micro-g LaCoste gPhone-54 and of the LaCoste and Romberg ET-11 gravimeter that were recording at the J9 Gravimetric Observatory of Strasbourg (France). The FG5#206 drop files were also used to compute the corresponding PSD. The New Low Noise Model (NLNM) of Peterson (1993) is represented by the thick brown line and the SLNM of Castellaro and Mulargia (2012) is represented by the thick dashed pink line. In gray lines, we have plotted the 5th percentile of the PSD levels obtained by Berger et al. (2004) for the Global Seismographic Network (GSN 5th-tile). Figure modified from Rosat and Hinderer (2018)

indicated by the NLNM (Widmer-Schnidrig, 2003).1068Noise increases at the right part of Fig. 21 because of
the microseismic signals. At the high frequency end
of the spectrum there is a steep roll-off (drop in
10711069

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amplitude) till the Nyquist frequency of 0.5 Hz
because of the built-in low pass anti-aliasing filters
of the SGs. Some individual lines sticking out of the
noise are the so-called parasitic modes of the SG
(Imanishi, 2009).

1077 The excellent agreement between the noise levels 1078 of six of the eight SGs as shown in Fig. 21 is one of 1079 the most important results of this study. Indeed the 1080 noise levels of C026, iOSG023 and iGravs 15, 29, 31 1081 and 32 all agree within a few dB (relative to 1 (m/ 1082 $s^{2})^{2}/Hz$ in the seismic band. From this result, we 1083 conclude that the various pillar designs used at J9 and 1084 shown in Fig. 1 do not significantly affect the noise 1085 of the SGs. Mounting an iGrav directly on the floor operates as quietly as an SG installed on an isolated 1086 pillar. In addition, the noise levels of the iGravs and 1087 iOSG match that of the older Compact C026, so the 1088 1089 performance of the iGravs remains equal to previous 1090 SGs.

1091 In contrast, we observe that the noise levels of two 1092 iGravs (iGrav30 and iGrav6) are significantly higher 1093 (5 db and 8 db) than the other six SGs. The auxiliary 1094 channels show that both the tilt noise and dewar 1095 pressure noise are 15 dB higher for iGrav30 than for 1096 iGrav31. This was later diagnosed as caused by a faulty pressure sensor in the head of the dewar 1097 leading to a tension of the vibration isolation 1098 1099 diaphragm larger than nominal and hence transmit-1100 ting coldhead and tilt noise to the gravity sensor; this 1101 pressure sensor was replaced before iGrav30 was 1102 moved to Strengbach. And, the iGrav06 was installed 1103 during the shortest time-period (~ 25 days) in which several earthquakes occurred. Since we have picked 1104 1105 the 5th tile among these 25 days, it is more difficult to obtain quiet days in such a short time window. For 1106 1107 other SGs, we have picked up the 5th-tile among at least 100 daily PSDs. Because the iOSG23, C026 and 1108 1109 iGrav instruments are located in a similar environ-1110 ment, differences in the observed noise levels can be 1111 investigated by extracting the coherent and incoher-1112 ent noise from the observed noise. We refer to the 1113 work by Rosat et al. (2015) and Rosat and Hinderer 1114 (2018) for detailed comparisons of SG noise levels 1115 with other spring gravimeters (ET-11, gPhone-054), a 1116 STS-2 seismometer and the absolute gravimeter FG5#206 recording at J9. 1117

iGrav30 and iGrav6 provide a note of caution to 1118 all users of iGravs, SGs and other scientific instru-1119 ments that are designed to operate for years to 1120 decades. It is wise to periodically check the perfor-1121 mance of SGs to make sure they are meeting their 1122 noise specifications rather than wait until the end of a 1123 project to analyze data and then find problems that 1124 interfere with the project goals. Checking the noise 1125 levels is very easy with iGravs that were designed 1126 compatible to TSoft (Van Camp & Vauterin, 2005) 1127 and feature software can be set up to reassure users 1128 that all is well, or to warn of pending instrumental 1129 problems. It is highly recommended that all users of 1130 iGravs activate the data system feature that automat-1131 ically send emails to the user(s) that include both a 1132 summary table of operating variables and a short 1133 TSoft file. The TSoft file is automatically calculated 1134 at the end of the day and a GWR 'summaryScript' 1135 (iGrav User's Guide, 2019). This summaryScript 1136 immediately provides the daily residual and temporal 1137 noise throughout the day and can easily be edited by 1138 the user. 1139

For the sake of completeness, we have plotted in 1140 Fig. 22 the fifth percentile of PSD noise levels of SGs 1141 together with other spring gravimeters (ET-11, 1142 gPhone-054), the STS-2 seismometer and the abso-1143 lute gravimeter FG5#206. For this meter we used 1144 drop measurements performed every 10 s. Each drop 1145 corresponds to one free fall of the test mass. In Rosat 1146 et al. (2015), the PSD for the FG5 was computed on 1147 set values at an hourly sampling with a noise level of 1148 -125 dB at 10^{-4} Hz. Here we can see that using 1149 10-s drop values, we have slightly reduced the noise 1150 level to around -130 dB. This level is still the 1151 largest of all meters in the seismic band and comes 1152 from the fact that absolute measurements are con-1153 taminated by aliased microseismic noise (see e.g. 1154 Crossley et al., 2001) which explains the rather flat 1155 FG5 noise spectrum. A similar aliasing is observed in 1156 the gPhone-54 PSD. 1157

The spring relative meters have lower noise levels1158than the FG5#206 and range from -145 dB for the1159gPhone-54 to -175 dB for ET-11 and the STS-21160seismometer.1161

At higher frequencies, the STS-2 shows similar 1162 performances like the SGs. At sub-seismic frequencies (below 10^{-3} Hz), the SGs show lowest noise 1164



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levels; while the ET-11 spring gravimeter noise is
10 dB higher and the gPhone is 30 dB higher. We
refer to the work by Rosat et al. (2015) for detailed
comparisons and self-noise analysis for these instruments. In the following we only focus on the SGs and
their instrumental performances.

1171 5.2. Self-Noise Levels

1172 The observed noise level for an instrument at a 1173 site consists of the Earth's environmental background 1174 noise (containing all geophysical processes) and the instrumental noise, including the noise coming from 1175 1176 the digital acquisition system and the electronics and 1177 some possible effects of the physical installation 1178 itself (e.g. placement in a building, or an installation 1179 directly on the building floor or on a pillar isolated 1180 from the building vibrations). In order to separate the 1181 instrumental noise from the ambient noise, Sleeman 1182 et al. (2006) have proposed a three-channel correla-1183 tion analysis. Compared to a two-channel analysis, 1184 this technique has the advantage that we do not need 1185 to know the transfer functions of the instruments. The main assumption is that the internal noise between 1186 1187 two channels is uncorrelated to each other and to the 1188 common input signal. The self-noise power spectral density of channel *i* can hence be written as: 1189

$$N_{ii} = P_{ii} - P_{ji}P_{ik}/P_{jk}, \qquad (2)$$

1191 where P_{ii} is the PSD of channel *i*, and P_{ji} (respec-1192 tively P_{ik} , P_{jk}) is the cross-PSD between channels *j* 1193 and *i* (*i* and *k*, *j* and *k*). The equation for self-noise 1194 PSD can also be expressed as:

$$N_{ii} = P_{ii}(1 - C_{ji}C_{ik}/C_{jk}),$$
(3)

1196 where C_{ji} (respectively C_{ik} , C_{jk}) is the coherency 1197 between channels j and i (i and k, j and k). The noise 1198 cross-power spectra N_{ij} (resp. N_{ik} , N_{jk}) of internal 1199 noise for channels i and j (i and k, j and k) are 1200 assumed to be zero for $i \neq j$ $(i \neq k, j \neq k)$. 1201 According to these conventions, the instrumental 1202 self-noise will be defined by N_{ii} and the common 1203 geophysical noise viewed by the instruments is rep-1204 resented by P_{ii} — N_{ii} .

1205 In order to apply the three-channel correlation 1206 analysis of Sleeman et al. (2006), we compute the 1207 PSDs and the cross-PSDs of the various calibrated SG records using a modified Welch periodogram 1208 method applied by averaging 9 segments of 48-h SG 1209 time-windows overlapped by 75% on two selected 1210 time-periods of 15 days. Two time-periods, April 1211 8-23, 2017 and August 10-25, 2017 were selected 1212 because of the joint availability of records from at 1213 least three instruments free of disturbances due to 1214 human intervention. 1215

Theoretically, the noise of the SG sensor is due to1216the thermal noise associated with Brownian motion of1217the levitating sphere. The expression of the power1218spectral density of a damped harmonic oscillator due1219to Brownian motion can be written as (Richter et al.,12201995; Aki & Richards, 2009eqn. 12.40):1221

$$P_{thermal} = 4k_B T \frac{\omega_0}{mQ},\tag{4}$$

where ω_0 is the natural angular frequency of the 1223 oscillator, Q its quality factor and m is the mass of the 1224 oscillating sphere; k_B is the Boltzmann constant and 1225 T the absolute temperature within the sensor. When 1226 there is no difference in the noise characteristics 1227 between three instruments (if instruments are equally 1228 installed at the same site for instance), the self-noise 1229 should be well explained by the thermal noise model. 1230

In Eq. (4) we use the Q value of the magnetic 1231 levitation system of the SG modeled as a mechanical 1232 damped oscillator. The measured Q value (Table 10) 1233 is low (0.109 for iOSG23 and 0.055 for iGrav29) 1234 because the sphere's motion is strongly damped by 1235 eddy currents in the non-superconducting materials in 1236 the sensor (in the nearby Al plates and in the magnet 1237 form). This damping is much larger than that caused 1238 by the viscous drag on the sphere moving in the 1239 surrounding helium gas. Moreover there are other 1240 noise sources that include temperature control noise, 1241 tilt noise, electronic noise, noise from the boiling He, 1242 coldhead vibrations, and digitization noise; some of 1243 which are difficult to quantify. However these noise 1244 sources seem below the thermal noise of the iGrav as 1245 is discussed hereafter. 1246

The parameters that are needed to compute the1247thermal noise PSD of iGrav29 and iOSG23 are given1248in Table 10.1249

The three-channel correlation analysis was 1250 already applied by Rosat et al. (2015) on the STS-2 1251 seismometer, the LaCoste-Romberg ET-11 1252

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pectral acceleration-noise power density due to Brownian motion				
Parameter	Unit	iGrav29	iOSG23	
Mass m	kg	$4.02 \ 10^{-3}$	17.7 10-3	
Frequency f_0	Hz	0.238	0.105	
Q		0.109	0.055	
Spring constant k	N/m	0.0090	0.0077	

0.055

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gravimeter and the SG C026 recording at J9. Because 1253 of different band-pass frequencies and different 1254 1255 digital acquisition system (DAS), it was however not possible to extract the sensor noise from the noise 1256 1257 of the DAS. Here, we have the possibility to evaluate the sensor noise since the DAS used for every iGrav 1258 1259 and for the iOSG23 is identical. A similar study was already done in Rosat and Hinderer (2018) but on a 1260 1261 more limited number of iGrav instruments.

kg/s

dB

Damping factor b

Mean PSD

1262 The results of the three-channel correlation anal-1263 ysis applied to the iGravs and the iOSG recording at J9 are shown in Fig. 23. We can see that at seismic 1264 frequencies higher than 1 mHz and lower than than 1265 1266 the start of the roll-off due to the low-pass antialiasing filter, the thermal noise model (-181 dB,1267 1268 Table 10) agrees well with the extracted self-noise PSD for iGravs with a difference of a few dB 1269 1270 (< 5 dB), except for iGrav30, which had a problem 1271 due to a faulty dewar pressure sensor previously 1272 discussed in Sect. 4.2 and previously shown in 1273 Fig. 21. The close matching of the thermal noise to 1274 the observed noise of the SG simply means that other noise sources of the SG are below its thermal noise. 1275 1276 Because of its heavier levitated sphere, the

thermal noise for iOSG23 should be just below the
NLNM seismic noise and a few decibels lower than
the thermal noise of iGrav instruments (- 188 dB,
Table 10).

1281 The fact that the self-noise of iOSG23 results to 1282 be about 5 dB larger than its thermal noise model in 1283 the seismic band (mHz frequency range) is likely due 1284 to additional noise sources previously mentioned. 1285 That the iOSG noise is lower than the iGrav self-1286 noise is likely the influence of its larger mass in agreement with Eq. (4). We also point out that the1287thermal noise of the STS1 long-period seismometer is1288lower than that of the SG, and that this also is likely1289due to its mass being much larger (600 g) and1290perhaps its lower damping (Richter et al., 1995).1291

We can see that the self-noise for iGrav15 and 32 1292 which were installed directly on the ground are 1293 similar to the one of the iOSG23 at periods larger 1294 than 1 h and similar to the one of iGrav29 at seismic 1295 frequencies. We conclude that the variations in 1296 physical installations at J9 did not significantly affect 1297 the noise levels and that installation on the concrete 1298 ground is as good as on a small or large isolated 1299 pillar. 1300

Two parasitic noise peaks around $2 \cdot 10^{-2}$ Hz (one 1301 at 57 s for iGrav30 and one at 48 s for iGrav29 and 1302 iGrav31) are visible in the PSDs (Fig. 23). These 1303 vibrations correspond to the low-frequency parasitic 1304 mode (Richter et al., 1995; Van Camp, 1999) due to 1305 horizontal displacements of the sphere that turn into 1306 an orbital mode (Hinderer et al., 2015). For iGrav32, 1307 this mode appears at 20 mHz (Schäfer et al., 2020). 1308 Peaks at 0.24 Hz and harmonics may be due to some 1309 other parasitic modes associated with other degrees of 1310 freedom of the sphere (Imanishi, 2009), coldhead 1311 noise, or other unidentified effects. 1312



Figure 23

Results of the three-channel correlation analysis applied on the 1-s data for iGrav30 and iGrav31 and iOSG23 on the 15-day time period 2017, April 8th to 23rd and for iGrav32, iGrav29 and iGrav15 on the 15-day time period between 2017, August 10th and 25th. Common noise was removed by this method and only self-noise PSDs are plotted

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 Table 10

 Harmonic oscillator parameter values used in Eq. 4 to compute the

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6. Conclusion

1314 Superconducting gravimeters (SG) are currently 1315 the most sensitive relative gravimeters with the 1316 lowest drift rates which, as demonstrated in our study, can be modelled and reduced with the help of abso-1317 lute gravity measurements. Therefore, these sensors 1318 1319 are particularly suitable for studying a wide range of geophysical processes which induce weak gravity 1320 1321 effects over time intervals of minutes to years.

We compared in detail eight SGs located inside 1322 1323 the Strasbourg Gravimetric Observatory including 1324 five of the latest generation of field SGs, the so-called 1325 iGravs, one iOSG with a heavier sphere and an older 1326 compact meter C026. The calibration of the instru-1327 ments was investigated both in an absolute way, by parallel absolute measurements, as well as in a rela-1328 1329 tive way by computing the regression between 1330 parallel SG time series. We found out that relative 1331 calibration determined from different SGs at the same 1332 site can be much more precise than absolute calibration. We could also demonstrate that using relative 1333 1334 scale factors strongly reduces the tidal residuals 1335 between two different SGs which is not the case when 1336 using absolute calibration.

1337 We checked the instrumental time delays (phase lag) of the various SGs from cross-correlation anal-1338 ysis between different parallel time series. All the 1339 iGravs have similar time delays of a few seconds with 1340 1341 respect to iOSG23. Moreover, the time delays for a 1342 specific gravimeter inferred from a one year long 1343 tidal analysis, step experiments and time regression were all found to agree. 1344

1345 We discussed the instrumental drift of the SGs 1346 and found that all the meters exhibit an initial expo-1347 nential drift best approximated by two exponentials 1348 with different time constants, followed by a longterm linear drift. We could also show the conse-1349 quences of the initialization/levitation procedures on 1350 the instrumental drift, especially for iGrav29 that was 1351 1352 used as test instrument in this study. A rather strong correlation was found between the gravity drift and 1353 1354 the body-temperature signal but it is not a straightforward or linear relationship. 1355

1356Furthermore, we have performed a noise level1357analysis of all the iGravs and the iOSG023. A three-1358channel correlation technique was applied to identify

the common noise and the self-noise of the various1359iGravs and the iOSG. However, small differences in1360self noise are not caused by the installation method1361(on concrete pillars or directly on the floor) or1362instrumental configurations; but they may be caused1363by differences in their transfer functions.1364

Small differences in self-noise could possibly be1365interpreted in terms of local noise effects that are1366incoherent between the various instruments separated1367by a few meters. For example, lateral contrast in local1368soil moisture in the loess layer above the Observatory1369could lead to slightly different signals of each1370gravimeter.1371

The present metrological study is of importance 1372 for several geophysical applications. A good knowl-1373 edge of the instrumental drift is essential for the study 1374 involving long-period gravity changes. We can 1375 mention for instance the difficulty of separating post-1376 glacial rebound effects from present-day ice-melting 1377 where the combination of AG and SG observations 1378 helped considerably to reduce the uncertainty in the 1379 AG estimated decrease due to ice melting in Svalbard 1380 (Memin et al. 2014). Furthermore, studies on slow 1381 recharge processes in magma chambers could benefit 1382 greatly from a thorough knowledge of the drift of the 1383 gravimeters used to monitor active volcanoes 1384 (Okubo, 2020; Riccardi et al., 2008). Knowledge of 1385 the purely instrumental noise and separation from 1386 environmental noise can help to detect small signals 1387 which are hidden in the overall noise (e.g. Rosat & 1388 Hinderer, 2018). Accurate calibration of the SGs is 1389 essential for the determination of tidal amplitudes and 1390 phases that is fundamental for tidal tomography and 1391 1392 investigation of lateral heterogeneity effects (Metivier et al. 2007; Latychev et al., 2009). 1393

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