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VSC-HVDC Robust LMI Optimization Approaches to Improve Small-Signal and Transient Stability of Highly Interconnected AC grids

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ABSTRACT: In this paper, for the situation of HVDC inserted in meshed AC power grid, a Model-matching robust H_∞ static output error feedback controller (RSOFC) and model-matching dynamic decoupled output feedback controller (DDOFC) are proposed to improve the damping of inter-area oscillation modes and maintain robustness to face the effects of different operating points and unstable zeros. Sufficient conditions for robust stability are derived in the sense of Lyapunov asymptotic stability and presented in the form of linear matrix inequalities to obtain H_∞ RSOFC and DDOFC gains based on the reference model. The efficiency and robustness of the proposed controllers are tested and compared to Linear-Quadratic-Gaussian (LQG) control, mixed sensitivity H_∞ , standard (IEEE) Power Oscillation Damping (POD) controllers on a realistic benchmark of 19 generators connected by a meshed AC grid. The main contributions of this paper are: (i) Compensate the negative effect of unstable zeros (non-minimum phase behavior) on the performances of the closed-loop; (ii) the robustness is improved in order to provide good responses in case of network variations (load evolution, line, and generator trips, etc.) and HVDC line parameters changes; (iii) improve the damping compared with standard controller structures (LQG, mixed sensitivity H_∞ and standard POD controller).

KEYWORDS:LMI, H_∞ , robustness, output feedback controller, HVDC, damping controller, inter-area modes.

1. Introduction

The traditional electricity transmission system based on three-phase AC grids, in general, works well and with good levels of reliability. However, there are challenges arising mainly from environmental impact and the increase in the renewable generation, (according to [1] the next decade will be devoted to the large-scale exploitation of offshore wind energy, which means the need to transport electrical energy over long distances to distances to establish a connection with the main power grid). This will likely increase the level of variability and unpredictability in the operation of power grids, leading to an increased need for power reserves for balancing energy consumption and will require more flexible power flow control. The solution that overcomes these problems is the use of high voltage direct current (HVDC) transmission systems, which are which are more feasible and also more competitive than traditional transmission systems (HVAC), especially with the development of power electronics components. One of the most important advantages of technology over the HVAC technology is that the former is suitable for long distances with minimal losses. The second advantage is the right-of-way; it is often easier to get permission for DC cables due to the reduced environmental impact [2]. The HVDC system is a power electronics technology used in electrical power systems primarily because of ability to transmit large amounts of energy over long distances [3]. In the case of HVAC systems the power transfer is limited because of the power transfer is limited because of the phase angle which increases with distance, this distance is limited to 50km [4], to solve this problem the network operator can use reactive power means of reactive power compensation along the line, such as such as FACTS (Flexible Alternating Current Transmission System) devices. However, these devices have a very high However; these devices are very expensive and cannot always be installed in the most appropriate place. Once the

development of high power switching devices and their devices and their availability at low prices, Line-commutated converters (LCCs) which used thyristors as the basic as a basic component in HVDC were replaced by voltage source converters (VSCs) [3]. Since VSC-HVDC has been gradually incorporated into the grid, they can be utilized to suppress low-frequency oscillations. The modes usually considered in the past were the most spread inter-area ones which are at low frequencies (in Europe about 0.2 Hz). For HVDC inserted in a meshed AC network, such as the recent interconnection reinforcements in Europe, inter-area modes corresponding to a limited number of generators in the area near the HVDC may be involved. They are at a higher frequency, around 1 Hz. However, in this frequency range, inter-area modes are close to other modes of a different nature (see [5, 6]) which are disturbed by the HVDC power oscillation damping (POD) controller. The use of classical Institute of Electrical and Electronics Engineers (IEEE) POD controller structures and tuning methods (see e.g. [7]) are focused on only one mode, and tends to inefficient damping and destabilize other modes.

It is well known that unstable zeros can degrade the performance of the control system. However, there is rare research on the origin of unstable zeros in HVDC links inserted into mesh AC networks. Therefore, it is important in research and practice to analyze network parameters with HVDC links to highlight their influence on unstable zeros. In addition, modeling errors and system uncertainties in plant models are inevitable in many applications. To ensure accuracy, design techniques must take these errors and uncertainties into account to be practical. Therefore, a (*robust*) control approach must be used to deal with the uncertainties arising from operating point changes in the power system, as well as the modeling errors caused by modeling and model reduction of realistic power systems.

Hence, the contributions of this paper, based on the aforementioned works are to develop robust POD controllers which

improve the damping of aforementioned high frequency inter-area modes without deteriorating the damping of the others and to eliminate the impact of unstable zeros. To develop advanced control one usually needs a state-space representation of the system [8], [9]. In [10], it is studied in detail the stability at small perturbations with power stabilizers (PSSs) in order to satisfy some recent objectives and constraints imposed by the evolution of large-scale interconnected power systems. H_∞ or H_2 approaches in the field of robust control are studied in a huge number of publications since the mid-1980s. In the context of robust control of linear systems, modern multivariate synthesis methods integrate a model of the process with a family of systems. They use a deviation model, which is defined either by different types of norms in the frequency or time domain, or by uncertainty domains on the parameters, or by sectors of the complex plane. For some types of error modeling, a synthesis technique is associated. A presentation of these different techniques will be proposed, with particular attention to those based on the use of H_∞ and H_2 . The H_∞ optimal control is used to control a system subject to modeling errors and parametric uncertainties [11]. In [12], an H_∞ controller is compared to a controller obtained by a LQG/LTR (Loop Transfer Recovery) method, allowing to recover some robustness properties of the LQ (in the sense of modulus margin and not parametric robustness). The H_2 methodology was applied in [13], to find state feedback controller offering a satisfactory the required performance. The paper [14] proposes an iterative methodology in order to obtain a static output controller by a mixed H_2/H_∞ synthesis. Many works deal with the analysis of stability and the stabilization to design robust dynamic output-feedback controllers [15], [16] based on Linear matrix inequalities (LMI). LMI are used to solve several problems of automation, (optimization problems in control theory, system identification,...) which are generally difficult to solve analytically. The interest of methods based on LMIs comes from the fact that they can be solved using convex programming [17]-[19]. With this approach, one is no longer limited to problems with an analytical solution. By solving these inequalities, one obtains a domain of feasible solutions, i.e. solutions satisfying these LMIs solutions satisfying these LMIs, larger than the one generated by the search for analytical solutions. Using the fact that an inequality has more solutions than an equation it is possible to use the additional degrees of freedom to include other objectives than those than those initially chosen. The notions of LMIs are found in several works since many years. Thus Lyapunov conditioned the stability of a system by LMI [20]. In the work presented here, two model-matching based methods are proposed to solve above mentioned problems. The contributions and novelty of this paper are: i) *Firstly*, the reference model in this work is proposed as having the desired characteristics, which means to horizontally shift the poles to left in the complex plane until getting the desired damping (over 10 %). Moreover, unstable zeros of the control model is shifted to left plane which is closed to the vertical axis to decrease the control difficulty. ii) *Secondly*, sufficient conditions are derived based on LMIs for robust stabilization, in the sense of Lyapunov method to obtain robust H_∞ static output error feedback controller (RSOFC) and dynamic decoupled output feedback controller (DDOFC) gains based on the reference model. iii) *Thirdly*, different controls from the literature (Linear-quadratic-Gaussian (LQG), mixed sensitivity H_∞ and standard (IEEE) Power Oscillation Damping (POD) controllers) are implemented for the realistic benchmark of 19 generators connected by a meshed AC

grid to compare with the proposed H_∞ RSOFC and DDOFC. The rest of the paper is organized as follows. Section 2 presents the problem statement and control model of the realistic benchmark of 19 generators connected by a meshed AC grid. The stability and the design of the proposed strategies are studied in Section 3. Section 4 introduces the proposed RSOFC and DDOFC. In Section 5, a simulation study to evaluate the performances of the proposed strategies is presented. In the Section 6 we present the conclusions and future works.

2. Problem Formulation, Main Difficulties and Modeling

2.1. Test system

A test system with aforementioned particularities is proposed. It contains an HVDC line inserted into an AC network consisting of 19 generators. All generators are controlled by AVR (Automatic Voltage Regulator) and PSS (Power System Stabilizer). The order of full nonlinear system is 724, which is linearized to obtain the full linear model of the same order. The less damped and highest residue modes found in Table 1 (see details in [21]).

2.2. Control model

In this paper the studied control model is developed in our previous work [21], [22]. By definition, a linear system is a system governed by ordinary linear differential (or even algebraic) equations with non-constant coefficients. They describe the temporal evolution of the constituent variables (state variables) of the physical system. This broad definition explains the complexity, the diversity of linear systems as well as the variety of methods that apply to them. A state representation of a linear system is given by:

$$\begin{aligned}\dot{x} &= Ax + Bu \\ y &= Cx\end{aligned}\quad (1)$$

where $x \in \mathfrak{R}^{n \times 1}$ is the state vector of the system, $y \in \mathfrak{R}^{g \times 1}$ is the measured output vector and $u \in \mathfrak{R}^{m \times 1}$ is the input vector, $C \in \mathfrak{R}^{g \times n}$, $A \in \mathfrak{R}^{n \times n}$ and $B \in \mathfrak{R}^{n \times m}$, are matrices of linear functions.

In our case, $y = \Delta\theta$ and u is Q , where Q is the reactive power, $\Delta\theta = \theta_1 - \theta_2$ is the difference of angles of the terminal voltages [23].

2.3. Classic POD

The detailed classic POD in this paper is proposed based on [7], [21], [22]. It is defined by the transfer function given by (2). The classical adjustment of the parameters of this system is given in the [24]. For the desired damping of 10% set for mode 2 in Table 1, The classic POD tuning parameters K , T_1 , T_2 , T_w and n are defined in [22].

$$H_{POD}(s) = K \left(\frac{T_w s}{1 + T_w s} \right) \left(\frac{1 + T_1 s}{1 + T_2 s} \right)^n \quad (2)$$

2.4. Main objectives and difficulties

1. Particular frequency range of inter-area modes: As mentioned in Introduction, in highly meshed AC grid, the inter-area modes are at higher frequency. In this range of frequency, other types of modes exist: local modes and electric

Table 1: The linearized model

No.	Mode	Damping ξ (%)	Freq. (Hz)	Mode shape (participation mag (%))		Residue	
				+	-	ABS MAG	Phase
1	-1.62+j8.19	19.5	1.30	GE_914 (100)	GE_913 (32.4)	0.0157	35.0
2	-0.24+j5.53	4.5	0.88	GE_911 (100)	GE_917 (68.8)	0.0181	83.4
3	-0.53+j5.29	10.1	0.84	GE_917 (100)	GE_918 (55.1)	0.0129	-56.2
4	-0.40+j4.79	8.3	0.76	GE_918 (44.3)	GE_912 (100)	0.0038	-33.3
5	-0.33+j3.29	10.1	0.52	GE_915 (100)	GE_918 (17.7)	0.0121	104.5
6	-18.83+j7.21	93.3	1.14	GE_921, GE_922 (100)	GE_923, GE_924 (74.1)	0.0034	14.5
7	-1.54+j6.55	22.9	1.04	GE_914 (100)	GE_911 (68.3)	0.0125	151.5
8	-19.32+j6.47	94.8	1.03	GE_921 (100)	GE_922 (37.6)	0.0117	118.9
9	-20.33+j4.86	97.2	0.77	GE_921, GE_922 (84.5)	GE_927 (100)	0.0026	-168.1
10	-18.72+j3.35	98.4	0.53	GE_913 (33.4)	GE_912 (100)	0.0072	136.1

coupling modes or general electric modes linked to other electric phenomena. In the theory of systems, the models used for the design of control laws are often models of reduced size. However, the increase in electrical interconnections has caused the increase in the size of models representing these electrical systems. This makes their use for the design of controllers almost impossible. Moreover, the extension of the European synchronous area to the east of Europe has not only made the volume of numerical calculations in the field of "electrical" systems, but also changed the frequencies of the inter-area modes. These modes are associated with oscillations involving a number of machines distant from the electrical system and will be defined in detail in [5]. More precisely, these modes shift to lower frequencies (by about a decade), which makes the gap between the frequency of the inter-area modes and the local modes (which concern only one generator) which remain in high frequency ranges. This deviation considerably modifies the global transient behavior of the electrical system and makes it difficult to synthesize controllers for a mixed specification, i.e., for both inter-area and local modes. In the previous works, the regulator design approaches use a simplified model consisting of a machine connected through a line of reactance X to the rest of the electrical system modeled by an infinite node. Although this simplified model, also called "infinite node machine", is very small compared to the full model of the electrical system, it cannot reproduce the dynamic phenomena concerning the voltage regulation specifications in the case of the very large systems mentioned above. Indeed, this model has only one inter-area mode whose frequency depends on the parameter X , i.e., the length of the line connecting the machine to the infinite node. It cannot therefore reproduce both local and inter-area local modes and inter-area modes of much lower frequency. Therefore, controllers designed with this model are not very efficient to meet the above-mentioned requirements. In [25], the balanced realization of an electrical system (representation of a complete electrical system by a reduced system containing only the most controllable and observable oscillatory modes) has been used for the construction of a control model allowing an optimal choice of the PSS locations to prevent blackouts in electrical systems. Although the chosen locations of the controls and measures improve the stability of the electrical system in the general case, these models are not optimal from the point of view

of the most controllable and observable modes are not the undamped modes of the system. To answer this problem, we have proposed in this paper to use the control model built from the complete model representing the electrical system. This model allows, by preserving an important set of variables and oscillatory modes of the complete model, to reproduce a given oscillatory behavior of the complete system which has both local and global components, i.e., that involves both local and global modes. Therefore, the controllers designed with this model will have an effective action once implemented in the complete system.

2. *Unstable zeros*: The existence of unstable zeros in the HVDC embedded system depends on the topology of the grids [26]. The effectiveness of POD can be decreased because of these unstable zeros. Furthermore, control community has recognized that the existence of unstable zeros [27].
3. *Uncertainty of system*: The modeling of a physical system is a crucial phase in the synthesis of the controller. Due to uncertainties, the mathematical model may not reflect the physical reality of the system. Nevertheless, if we manage to characterize these uncertainties, it is possible to complete the nominal model with an additional uncertain part. The sources of uncertainties are numerous but they are generally classified in two categories
 - *Non-structural uncertainties* also called non-parametric. They represent external dynamics, for example: measurement noise, external disturbances, etc. disturbances, etc. In general, their dynamics are unknown and we have no information on the way they act on the system. On the other hand, we know that they are bounded in norms.
 - *Structural uncertainties* also called modeling or parametric uncertainties. They are generally due to approximation errors and/or simplifications necessary to obtain an exploitable control model reflecting the real dynamics of the physical system.

In this paper, we design the controller for control model (1) (cf. Fig. 1) subject to the non-structural uncertainties.

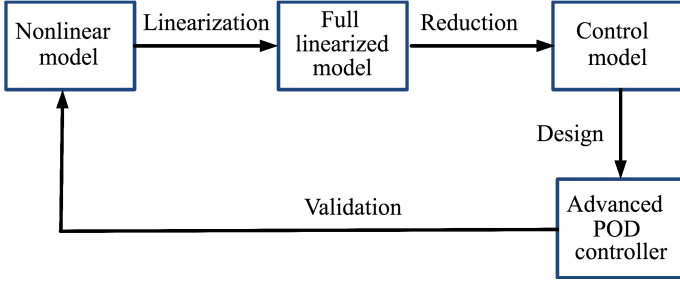


Figure 1: Design process.

It should be noted that all these requirements cannot be fully satisfied neither with the classic POD recalled in Section 2.3, nor with the standard H_2 and H_∞ robust controllers. To overcome this, a new design methodology summed-up in Fig. 1 was proposed.

3. Preliminary

In this section, we first recall the theory of stability in the sense of a quadratic (LQ) and Gaussian quadratic (LQG) linear equation and mixed sensitivity H_∞ . For the LQ, we focus on the problem of free-horizon control. In this context, the Lyapunov theorem is an interesting alternative to demonstrate the results of the LQG regulation and H_∞ based on [21], [24]. We also present the robustness properties and the asymptotic behaviors of the LQG control. Finally, we are interested in the Root Square Locus which is a graphical tool to guide the choice of weights on modal considerations in the complex plane.

3.1. LQG controller

For the system (1), the feedback control that stabilizes the system and minimizes the criterion LQG [8], [27]:

$$J_{LQG} = E \left\{ \lim_{T \rightarrow \infty} \frac{1}{T} \int_0^T [x^T Q x + u^T R u] dt \right\} \quad (3)$$

with the weighting matrices W and V , Q and R and the controller gains K_r and L are given by:

$$K_r = R^{-1} B^T X \quad (4)$$

$$L = Y C^T V^{-1}, \quad (5)$$

and X and Y positive (symmetric) solution of the two Riccati equation:

$$\begin{aligned} XA + A^T X - XBX^{-1}B^T X + Q &= 0 \\ YA^T + AY - YC^T R^{-1}CY + W &= 0. \end{aligned} \quad (6)$$

Fig. 2 shows the proposed LQG POD. The classic POD wash-out filter is added in LQG POD controller to avoid steady-state error. $Q = I, R = 10^{-4}; W = I, V = 10^{-2}$ in this case. The transfer matrix of regulator is:

$$Q_{pod} = -K_r \hat{x} = -K_r (sI - A + LC)^{-1} \begin{bmatrix} B & L \end{bmatrix} \begin{bmatrix} u \\ \Delta\theta_w \end{bmatrix} \quad (7)$$

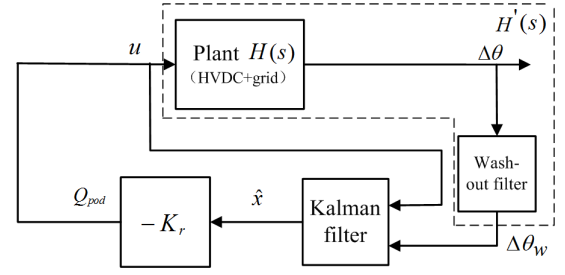


Figure 2: The proposed LQG control implementation.

3.2. Mixed sensitivity H_∞ based on LMI

The interest of this approach lies in the clarity of its formalism and the physical interpretation of the synthesis criterion since it is defined by a transfer function or even a block diagram showing weights placed on the physical inputs and output signals of the system and this independently of the norm that one wishes to minimize (H_2 or H_∞). This formulation is conducive to the introduction of frequency weights on some signals (e.g., the control) to satisfy frequency specifications (e.g., the roll-off at high frequencies) for which the optimal LQG-type approach is poor (note however that the frequency LQG approach proposed a solution since the beginning of the 70's to take into account frequency specifications. Particular standard forms (notably the mixed sensitivity presented in Fig. 3) have been studied and are directly adapted to the formulation of frequency robustness specifications on sensitivity functions. We show here how to formalize the mixed "S/KS" synthesis problem for our application. For that we use frequency weights: W_1 for S and W_2 for KS . The H_∞ problem consists of minimizing:

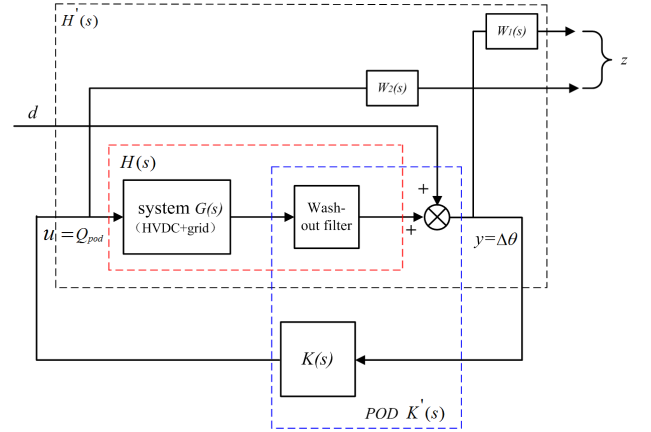


Figure 3: The proposed mixed sensitivity H_∞ based on LMI implementation.

$$\left\| \begin{bmatrix} W_1(s)S(s) \\ W_2(s)KS(s) \end{bmatrix} \right\|_\infty < \gamma, \quad (8)$$

where γ denotes a positive real number. We consider the disturbance d as the only disturbance in the system (Fig. 3). $W_1(s)$ and $W_2(s)$ are the stability and performance specifications respectively and take the following forms [27]:

$$W_1(s) = \left(\frac{s/\sqrt[k]{M_s} + \omega_b}{s + \omega_b \sqrt[k]{\varepsilon}} \right)^k, \quad W_2(s) = \left(\frac{s + \omega_{bc}/\sqrt[k]{M_n}}{\sqrt[k]{\varepsilon_1 s + \omega_{bc}}} \right)^k \quad (9)$$

where the bandwidth are $\omega_b = 0.628$ rad/sec, $\omega_{bc} = 12.56$ rad/sec. M_s, M_n are defined for the peak sensitivity and $\varepsilon = 0.1$,

$\varepsilon_1 = 0.1$ for the steady state error. k is the order of the weighting function. The target damping is set to $\xi_{desired} = 10\%$ for all the modes, as was the case for the design of classic POD. Thus, $\beta = 168^\circ$ (β is the angle of conics in left complex plane directly correlated with damping ratio $\xi = \cos \frac{\beta}{2}$).

The different matrices are combined into a single system, called the *augmented system*. It is defined by the following state equations:

$$\begin{cases} \dot{x}_p = A_p x_p + B_{p1} d + B_{p2} u \\ z = C_1 x_p + D_{p11} d \\ y = C_2 x_p + D_{p21} d \end{cases} \quad (10)$$

be a stable representation of the augmented plant $H'(s)$ of Fig. 3.

The state space parameters of controller $K(s)$ are A_k, B_k, C_k and D_k which can be found via solving LMIs (11), (12), (13).

$$\begin{bmatrix} Q & I \\ I & S \end{bmatrix} < 0 \quad (11)$$

$$\begin{bmatrix} \Pi_{11} & \Pi_{21}^T \\ \Pi_{21} & \Pi_{22} \end{bmatrix} < 0 \quad (12)$$

$$[\eta \otimes \Psi + \eta^T \otimes \Psi^T] < 0 \quad (13)$$

Where

$$\eta = \begin{bmatrix} \sin \frac{\beta}{2} & \cos \frac{\beta}{2} \\ -\cos \frac{\beta}{2} & \sin \frac{\beta}{2} \end{bmatrix} \quad (14)$$

\otimes is the Kronecker product, Q and S are obtained by solving the following $\Pi_{11}, \Pi_{21}, \Pi_{22}$ and Ψ .

$$\Pi_{11} = \begin{bmatrix} A_p Q + Q A_p^T + B_{p2} \hat{C} + \hat{C}^T B_{p2}^T & B_{p1} + B_{p2} \hat{D} D_{p21} \\ (B_{p1} + B_{p2} \hat{D} D_{p21})^T & -\gamma I \end{bmatrix} \quad (15)$$

$$\Pi_{21} = \begin{bmatrix} \hat{A} + (A_p + B_{p2} \hat{D} C_{p2})^T & S B_{p1} + \hat{B} D_{p21} \\ C_{p1} Q + D_{p12} \hat{C} & D_{p11} + D_{p12} \hat{D} D_{p21} \end{bmatrix} \quad (16)$$

$$\Pi_{22} = \begin{bmatrix} A_p^T S + S A_p + \hat{B} C_{p2} + C_{p2}^T \hat{B}^T & (C_{p1} + D_{p12} \hat{D} C_{p2})^T \\ C_{p1} + D_{p12} \hat{D} C_{p2} & -\gamma I \end{bmatrix} \quad (17)$$

$$\Psi = \begin{bmatrix} A_p Q + B_{p2} \hat{C} & A_p + B_{p2} \hat{D} C_{p2} \\ \hat{A} & S A_p + \hat{B} C_{p2} \end{bmatrix} \quad (18)$$

A state-space representation of the controller $K(s)$ is

$$D_k = \hat{D}; \quad (19)$$

$$C_k = (\hat{C} - D_k C_2 Q)(M^T)^{-1}; \quad (20)$$

$$B_k = N^{-1}(\hat{B} - S B_{p2} D_k); \quad (21)$$

$$A_k = N^{-1}[\hat{A} - S(A + B_{p2} D_k C_{p2})Q](M^T)^{-1} - B_k C_{p2} Q(M^T)^{-1} - N^{-1} S B_{p2} C_k. \quad (22)$$

by solving LMIs (19) to (22), Q, S and $\hat{A}, \hat{B}, \hat{C}, \hat{D}$ are calculated, and M and N are given by

$$M N^T = I - R S. \quad (23)$$

4. Proposed H_∞ RSOFC based on model-matching

4.1. Selection of reference model

The nominal (or reference) model is a realization in the state space and selected in order to give desired damping (over 10%) (cf. Fig. 4) and stable zeros (see details in [21]). It is possible to write the state model in the following form.

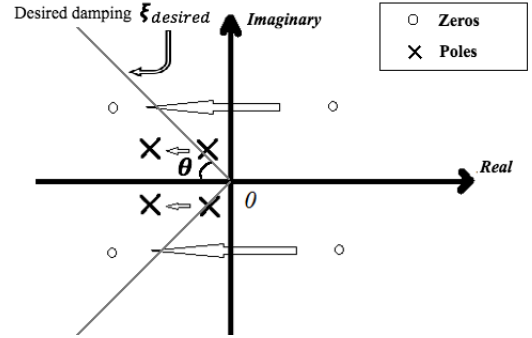


Figure 4: The selection of reference model

$$\begin{aligned} \dot{x}_r &= A_r x_r + B_r u_r \\ y_r &= C_r x_r \end{aligned} \quad (24)$$

The reference model and open-loop comparison validation is shown in Fig. 5. The proposed H_∞ RSOFC based on model-matching is given in Fig. 6.

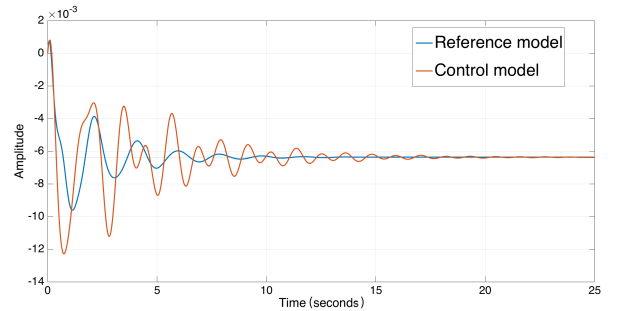


Figure 5: The reference model step response.

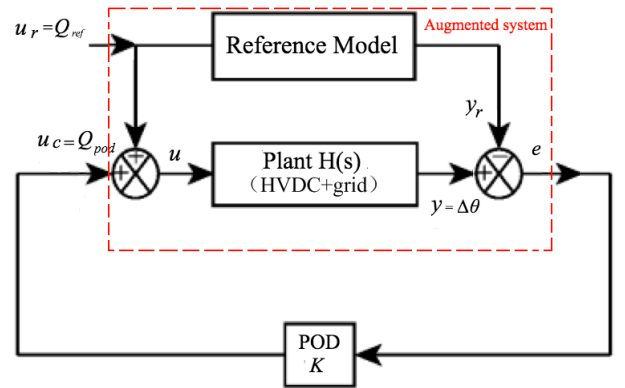


Figure 6: The proposed H_∞ RSOFC.

Based on (1) and (24), the augmented system is defined by the following state equations (cf. Fig. 6).

$$\begin{aligned}\dot{\tilde{X}} &= \tilde{A}\tilde{X} + \tilde{B}u_c + \tilde{B}_r u_r \\ e &= C_e \tilde{X}\end{aligned}\quad (25)$$

where the controlled output is given by $e = y - y_r$ and $\tilde{X} = [x \ x_r \ e]^T$.

$$\begin{aligned}\tilde{A} &= \begin{bmatrix} A & 0 & 0 \\ 0 & A_r & 0 \\ CA & -C_r A_r & 0 \end{bmatrix}, \tilde{B} = \begin{bmatrix} B \\ 0 \\ CB \end{bmatrix} \\ \tilde{B}_r &= \begin{bmatrix} B \\ B_r \\ CB - C_r B_r \end{bmatrix}, C_e = [0 \ 0 \ I]\end{aligned}\quad (26)$$

In this paper, the proposed H_∞ RSOFC is defined by

$$u_c = Ke, \quad (27)$$

where K are the controller gains.

From (25), (26) and (27), the closed-loop system is given by ,

$$\begin{aligned}\dot{\tilde{X}} &= \tilde{A}\tilde{X} + \tilde{B}_r u_r \\ e &= C_e \tilde{X}\end{aligned}\quad (28)$$

where $\tilde{A} = \tilde{A} + \tilde{B}[0 \ 0 \ K]$.

4.2. Proposed H_∞ RSOFC stability and robustness analysis

The conditions of global asymptotic stability to determine the controller gains so that the system (28) is robust is studied in this subsection. This leads to the conditions expressed in Theorem 1.

Theorem 1: The robust control system in the form (28) under the control law (27) is asymptotically stable if and only if $X = X^T > 0$ and Y and below LMIs are verified

$$\min \gamma \quad (29)$$

subject to

$$\begin{bmatrix} \tilde{A}X + X\tilde{A}^T + \tilde{B}Y + Y^T \tilde{B}^T & \tilde{B}_r & (C_e * X)^T \\ & \tilde{B}_r^T & -\gamma I \\ C_e * X & 0 & -\gamma I \end{bmatrix} < 0 \quad (30)$$

$$X > 0$$

Then, based on (30), the controller gains (27) are obtained.

$$K = XY^{-1} \quad (31)$$

Proof. The proof of Theorem 1 is established by using the disturbance u_r to the output e Transfer Function (TF).

$$T_{u_r, e}(s) = C_e(sI - (\tilde{A} + \tilde{B}K))^{-1} \tilde{B}_r \quad (32)$$

By minimizing the H_∞ norm of (32) ($\|T_{u_r, e}\|_\infty \leq \gamma$), the rejection of external disturbances is obtained. Based on bounded real lemma ([17, 28]), the robust control system in the form of a (28) is stable, if and only if the matrix $P = P^T > 0$ is symmetric positive definite and the following LMIs are verified

$$\begin{bmatrix} \tilde{A}^T P + P\tilde{A} & P\tilde{B}_r & C_e^T \\ \tilde{B}_r^T P & -\gamma I & 0 \\ C_e & 0 & -\gamma I \end{bmatrix} < 0. \quad (33)$$

From, (28) and (33),

$$\begin{bmatrix} \phi & P\tilde{B}_r & C_e^T \\ \tilde{B}_r^T P & -\gamma I & 0 \\ C_e & 0 & -\gamma I \end{bmatrix} < 0, \quad (34)$$

where $\phi = [\tilde{A} + \tilde{B}[0 \ 0 \ K]]^T P + P[\tilde{A} + \tilde{B}[0 \ 0 \ K]]$. Define

$$T = \begin{bmatrix} P^{-1} & 0 & 0 \\ 0 & I & 0 \\ 0 & 0 & I \end{bmatrix} \quad (35)$$

where I is the identity matrix. Multiplying left and right sides of the (34) by T and T^T , respectively, with $X = KY$, $X = P^{-1}$, the stability conditions (29) and (30) in Theorem 1 are obtained.

5. Proposed H_∞ DDOFC based on model-matching

To avoid to run the reference model in real-time in order to produce the e signal in the controller, a an output-feedback is proposed. The structure of the resulting model-matching robust H_∞ DDOFC is given in Fig. 7.

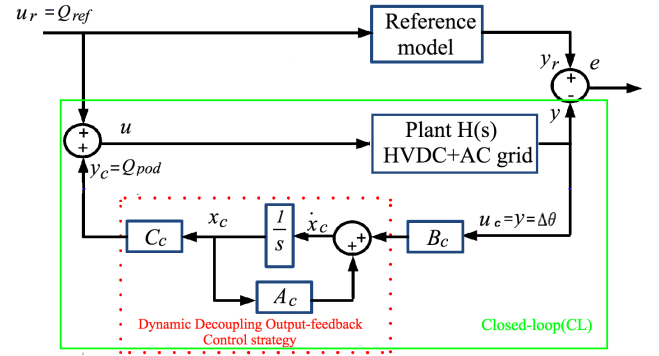


Figure 7: The robust H_∞ DDOFC strategy.

The proposed H_∞ DDOFC dynamic equations are given by the following form

$$\begin{aligned}\dot{x}_c &= A_c x_c + B_c u_c \\ y_c &= C_c x_c\end{aligned}\quad (36)$$

From Fig. 7, it follows,

$$\begin{aligned}u &= u_r - u_c = u_r - y_c = u_r - C_c x_c \\ u_c &= y = C x\end{aligned}\quad (37)$$

From (1), (24) and (36), the virtual system state-space equation is

$$\begin{aligned}\dot{X} &= \tilde{A}X + \tilde{B}u_r \\ Y &= \tilde{C}X\end{aligned}, \quad (38)$$

where $X(t) = \begin{bmatrix} x \\ x_r \\ x_c \end{bmatrix}^T$, and

$$\tilde{A} = \begin{bmatrix} A & 0 & -BC_c \\ 0 & A_r & 0 \\ B_c C & 0 & A_c \end{bmatrix}, \tilde{B} = \begin{bmatrix} B \\ B_r \\ 0 \end{bmatrix}, \tilde{C} = \begin{bmatrix} -C \\ C_r \\ 0 \end{bmatrix}^T.$$

5.1. Proposed H_∞ DDOFC stability and robustness analysis

Theorem 2: The virtual system (VS) in the form (38) subject to the proposed H_∞ DDOFC dynamic law (36) is asymptotically stable if and only if the matrices $Q, Z \in \mathfrak{R}^{(n+n_r) \times (n+n_r)}$ are symmetric positive definite, $\bar{A}, \bar{B}, \bar{C} \in \mathfrak{R}^{(n+n_r) \times (n+n_r)}$, are non singular and scalar γ , and below LMIs are verified,

$$\min \gamma \quad (39)$$

$$\begin{bmatrix} \phi_1 + \phi_1^T & \bar{A}^T + \begin{bmatrix} A & 0 \\ 0 & A_r \end{bmatrix} & \begin{bmatrix} B \\ B_r \end{bmatrix} & Q \begin{bmatrix} -C^T \\ C_r^T \end{bmatrix} \\ * & \phi_2 + \phi_2^T & Z \begin{bmatrix} 0 \\ B_r \end{bmatrix} + \bar{B} & \begin{bmatrix} -C^T \\ C_r^T \end{bmatrix} \\ * & * & -\gamma I & 0 \\ * & * & 0 & -\gamma I \end{bmatrix} \leq 0 \quad (40)$$

$$\begin{bmatrix} Q & I \\ I & Z \end{bmatrix} \geq 0, \quad (41)$$

where

$$\phi_1 = \begin{bmatrix} A & 0 \\ 0 & A_r \end{bmatrix} Q + \begin{bmatrix} -BC \\ 0 \end{bmatrix}, \phi_2 = Z \begin{bmatrix} A & 0 \\ 0 & A_r \end{bmatrix} + \begin{bmatrix} BBC \\ 0 \end{bmatrix}^T,$$

Therefore, by solving LMIs (40)-(41), the H_∞ DDOFC parameters can be written as follows:

$$A_c = N^{-1} \bar{A} M^{-T}, B_c = N^{-1} \bar{B}, C_c = \bar{C} M^{-T}, \quad (42)$$

where

$$\bar{A} = \hat{A} - Z \begin{bmatrix} A & 0 \\ 0 & A_r \end{bmatrix} Q - N \begin{bmatrix} B_c C \\ 0 \end{bmatrix}^T Q - Z \begin{bmatrix} BC_c \\ 0 \end{bmatrix} M^T \quad (43)$$

and

$$NM = I - ZQ. \quad (44)$$

Proof. By minimizing the H_∞ norm of (32) ($\|T_{u,e}\|_\infty \leq \gamma$), the rejection of external disturbances is obtained. Based on bounded real lemma ([17], [28]), the robust control system in the form of a (36) is stable, if and only if the matrix $W \in \mathfrak{R}^{2(n+n_r) \times 2(n+n_r)}$ is symmetric positive definite and LMIs are satisfied,

$$\begin{bmatrix} \bar{A}^T W + W \bar{A} & W \bar{B} & \bar{C}^T \\ \bar{B}^T W & -\gamma I & 0 \\ \bar{C} & 0 & -\gamma I \end{bmatrix} \leq 0 \quad (45)$$

$$W \geq 0. \quad (46)$$

Based on Schur complement method [29]- [32] using W and W^{-1} , we have;

$$W = \begin{bmatrix} Z & N \\ N^T & \star \end{bmatrix}, W^{-1} = \begin{bmatrix} Q & M \\ M^T & \star \end{bmatrix} \quad (47)$$

where \star is unknown matrix. Let

$$\Pi_1 = \begin{bmatrix} Q & I \\ M^T & 0 \end{bmatrix}, \Pi_2 = \begin{bmatrix} I & Z \\ 0 & N^T \end{bmatrix} \quad (48)$$

From $WW^{-1} = I$, it can be inferred

$$\Pi_2 = W \Pi_1 \quad (49)$$

In this case,

$$\Pi_2^T W \bar{A} = \Pi_2^T \bar{A} \Pi_1 \quad (50)$$

So that,

$$\begin{aligned} \Pi_2^T \bar{A} \Pi_1 &= \begin{bmatrix} I & 0 \\ Z & N \end{bmatrix} \begin{bmatrix} A & 0 & -BC_c \\ C & A_r & 0 \\ B_c C & 0 & A_c \end{bmatrix} \begin{bmatrix} Q & I \\ M^T & 0 \end{bmatrix} \\ &= \begin{bmatrix} A & 0 \\ 0 & A_r \end{bmatrix} Q + \begin{bmatrix} -BB_c \\ 0 \end{bmatrix} M^T \begin{bmatrix} A & 0 \\ 0 & A_r \end{bmatrix} \\ &\quad Q_1 \quad \quad \quad Q_2 \end{aligned} \quad (51)$$

and,

$$\Pi_1^T W \bar{B} = \Pi_2^T \bar{B} \Pi_1 = \begin{bmatrix} I & 0 \\ Z & N \end{bmatrix} \begin{bmatrix} B \\ B_r \\ 0 \end{bmatrix} = \begin{bmatrix} B \\ B_r \\ Z \begin{bmatrix} B \\ B_r \end{bmatrix} \end{bmatrix}. \quad (52)$$

Then,

$$\Pi_1^T \bar{C} = \begin{bmatrix} -C & C_r & C \end{bmatrix} \begin{bmatrix} Q & I \\ M^T & 0 \end{bmatrix}^T \begin{bmatrix} Q \\ C_r^T \\ -C_r^T \\ C_r^T \end{bmatrix} \quad (53)$$

where,

$$\begin{aligned} Q_1 &= Z \begin{bmatrix} A & 0 \\ 0 & A_r \end{bmatrix} Q + N \begin{bmatrix} B_c & C & 0 \end{bmatrix} Q + Z \begin{bmatrix} -BC_c \\ 0 \end{bmatrix} M^T + \\ &\quad NA_c M^T, \\ Q_2 &= Z \begin{bmatrix} A & 0 \\ 0 & A_r \end{bmatrix} + N \begin{bmatrix} B_c & C & 0 \end{bmatrix} \end{aligned} \quad (54)$$

Thus,

$$\begin{aligned} \hat{A} &= Z \begin{bmatrix} A & 0 \\ 0 & A_r \end{bmatrix} Q + N \begin{bmatrix} B_c & C & 0 \end{bmatrix} Q + Z \begin{bmatrix} -BC_c \\ 0 \end{bmatrix} M^T \\ &\quad + NA_c M^T, \\ \hat{B} &= NB_c, \hat{C} = C_c M^T \end{aligned} \quad (55)$$

Therefore, (45) and (46) are equivalent to (40) and (41).

6. Validation Tests

In this section, RSOFC and DDOFC controllers depicted in Sections 4 and 5 are validated in linearized full model and nonlinear model and compared with the other controllers presented in Sections 2 and 3.

6.1. Linearized model validation

The model tested in this section is the linearized model from EUROSTAG and tested in Matlab with a step disturbance on angle difference $\Delta\theta$. They are shown in Fig. 8. The modes can be identified by measuring their frequency from two peaks. The description of these results are shown below:

1. at $t = 8s$, mode 2: compared to the classic POD and RSOFC, DDOFC POD and LQG POD give better damping.
2. from $t = 2s$ to $4s$, mode 5: The performance of DDOFC POD, LQG POD, and mixed sensitivity H_∞ POD give less undershoot and sufficient damping.
3. from $t = 1s$ to $3s$, mode 1 (in zoomed figure of open-loop curve): Only observed in the curve with LQG.

Table 2: Comparison of damping

No.	damping (ξ) without POD (%)	damping (ξ) with classic POD (%)	damping (ξ) with LQG POD (%)	damping (ξ) with Mixed sensitivity H_∞ POD (%)	damping (ξ) with RSOFC POD (%)	damping (ξ) with DDOFC POD (%)
1	19.5	30.5	21.7	20.29	18.6	23.3
2	4.5	6.1	10.9	11.67	4.2	12.6
3	10.1	12.0	14.9	12.33	9.6	10.8
4	8.3	8.1	11.4	12.41	7.9	10.6
5	10.1	12.4	13.6	14.97	14.2	14.1

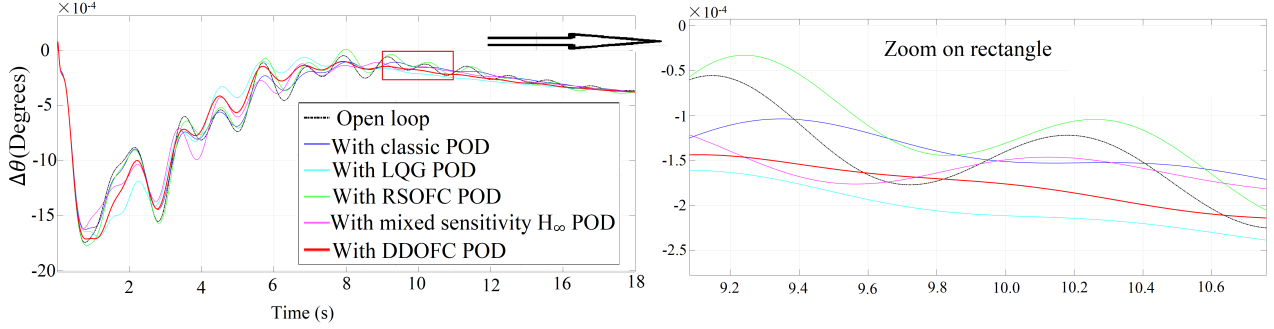


Figure 8: Comparison of linearized model.

Based on Table 2 analysis, It can be observed that, the proposed DDOFC POD gives the desired target damping of modes 1 and 2 without disturbing the others and a better damping in a wide range frequency band. The damping for each mode is over 10% for DDOFC POD, LQG POD, and H_∞ POD while the classic POD enhance the damping of mode 2, but encumber mode 4. Mode 3 damping is reached highest value for LQG POD but it's acceptable for mixed sensitivity POD during mode 4 and 5. On the other hand, damping for each mode is decreased except mode 5 for RSOFC.

6.2. Nonlinear system validation

The study and robustness analysis is more difficult due to the system nonlinearities. In addition, each response curve is the result of several modes mixed with a nonlinear dynamic. It is therefore difficult to highlight each mode individually. Disturbance scenarios must be well chosen. Moreover, the observability of the modes depends on the selected output signal. To validate the performance and robustness of the proposed controllers, two situations are considered: for the first one, called *nominal operation case*, the simulations are carried with the same grid situation considered for the synthesis of the controllers. For the second one, called *robust operation case*, the grid is disturbed (with load variations, line/generators tripping) for simulation without recomputing the controllers.

6.2.1. Nominal operation case

Fig. 9 shows the response of the proposed strategies in the nominal operation case.

According to the zoom of Fig. 9, one can see that for mode 2 (we recognize it by measuring the frequency between the peaks of

the curves from the oscillation 8th), the DDOFC, the mixed sensitivity H_∞ POD and LQG POD give more damping compared to RSOFC and classic POD. In addition, at $t = 3s$, the contributions of several mixed modes with nonlinear dynamics are observable. Moreover, between the 4th and 8th oscillations (the period during which mode 1 can be observed), (cf. table 2).

6.2.2. Robust operation cases

Different disturbed grid situations are considered to validate the proposed strategies in uncertainties case. These cases correspond to the robustness issue: variation of some of its parameters - called *parametric robustness* (see details in [22]).

Responses obtained with the same controllers considered above are now shown in Fig. 10, 11, 12, 13.

• Reverse power flow case (in Fig. 10)

1. at $t = 12s$ (mode 2): RSOFC POD and mixed sensitivity H_∞ POD give more damping.
2. From oscillation 3rd (mode 4): Although the RSOFC POD give more damping compared to the other controllers, but it gives insufficient damping nominal operation case.
3. from $t = 3s$ to $t = 5s$: With the mixed sensitivity H_∞ the POD gives small oscillation at $t = 3.5s$ (cf. Fig. 10).

• Increased load case (in Fig. 11)

1. at $t = 12s$ (mode 2): H_∞ , LQG and DDOFC POD give the same acceptable damping.

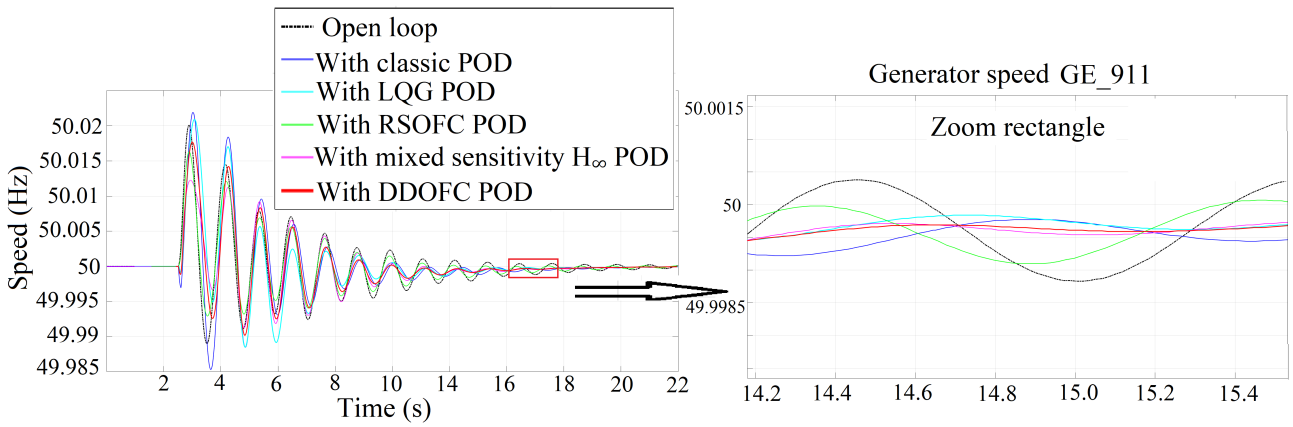


Figure 9: Nominal operation case.

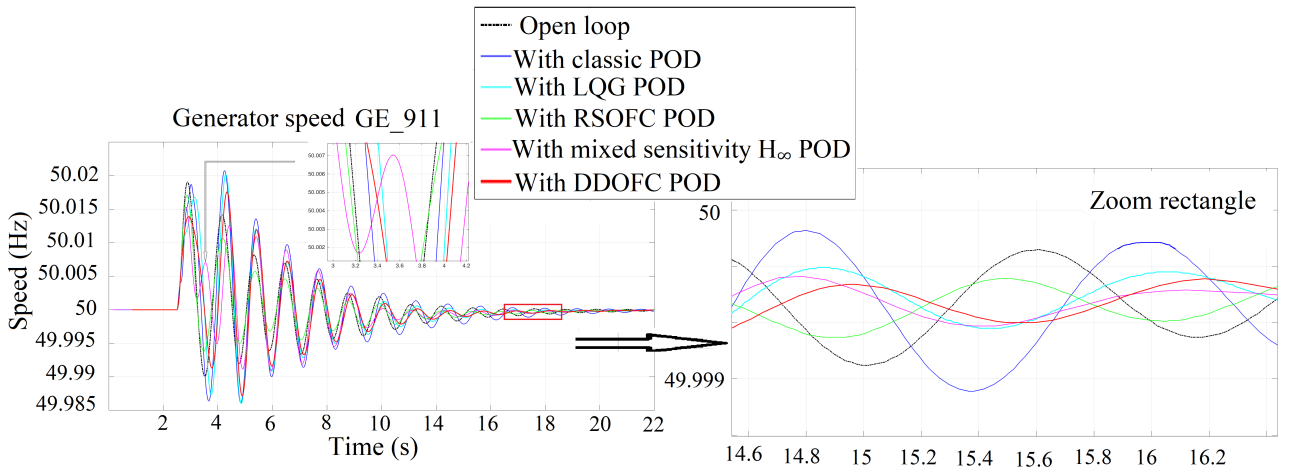


Figure 10: Reverse power flow case.

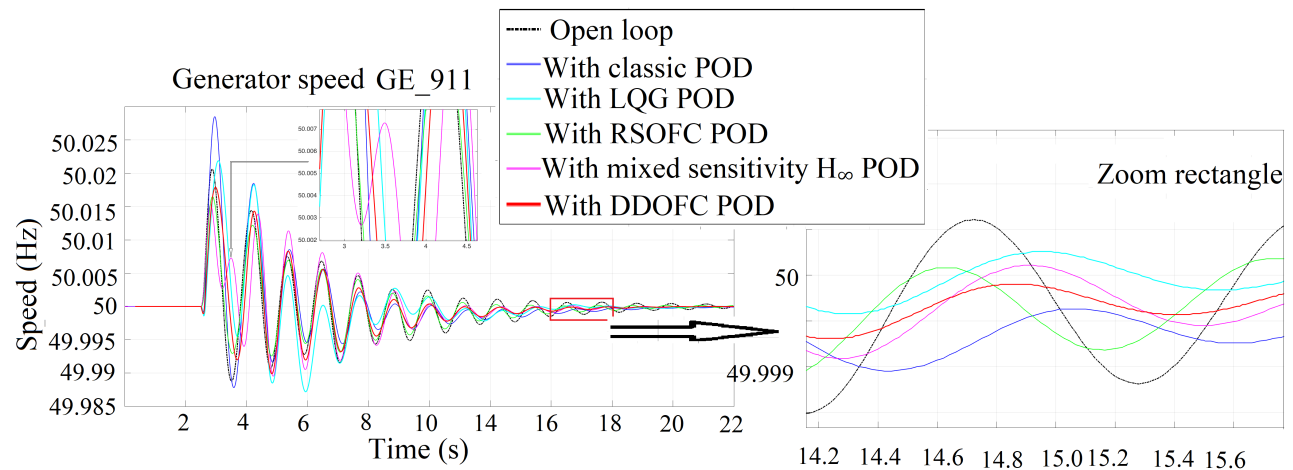


Figure 11: Increase load case.

2. From the oscillation 3rd to 5th: the damping provided by the H_∞ POD is not sufficient for mode 4. In addition, the overshoot with LQG POD in the first oscillation is undesirable. i.e.

• **Tripping generator case (in Fig. 12)**

1. During the first two oscillations: the POD LQG as well as the classic POD even increase the oscillations

during the first two swings.

2. From $t = 12s$ (mode 2): The DDOFC, the mixed sensitivity H_∞ and the LQG POD, have more damping compared to the other controllers.

3. DDOFC POD gives more damping than the other controllers during the 3th to the 6th swing (mode 1).

• **Tripping lines case (In Fig. 13)**

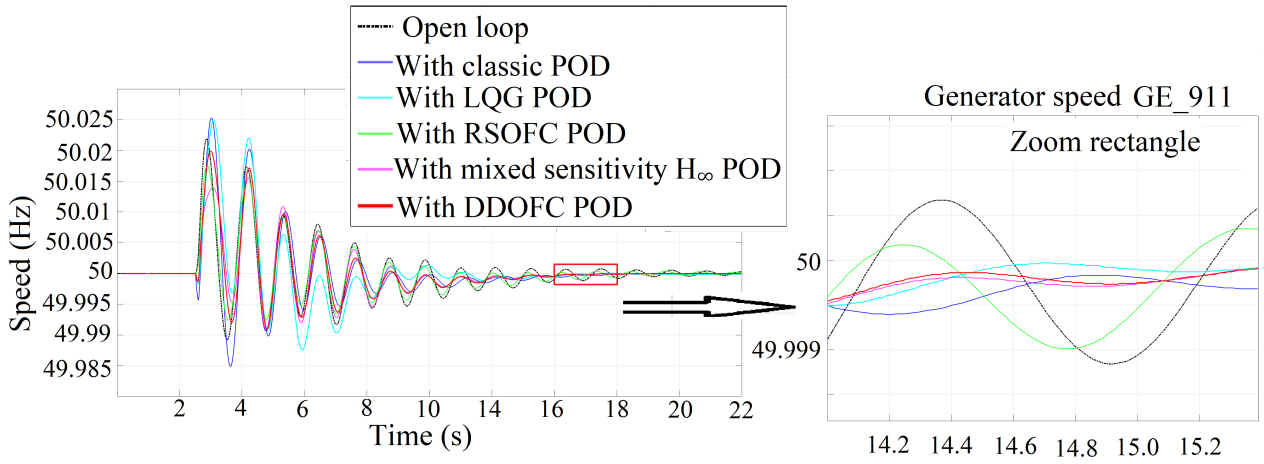


Figure 12: Tripping generator case.

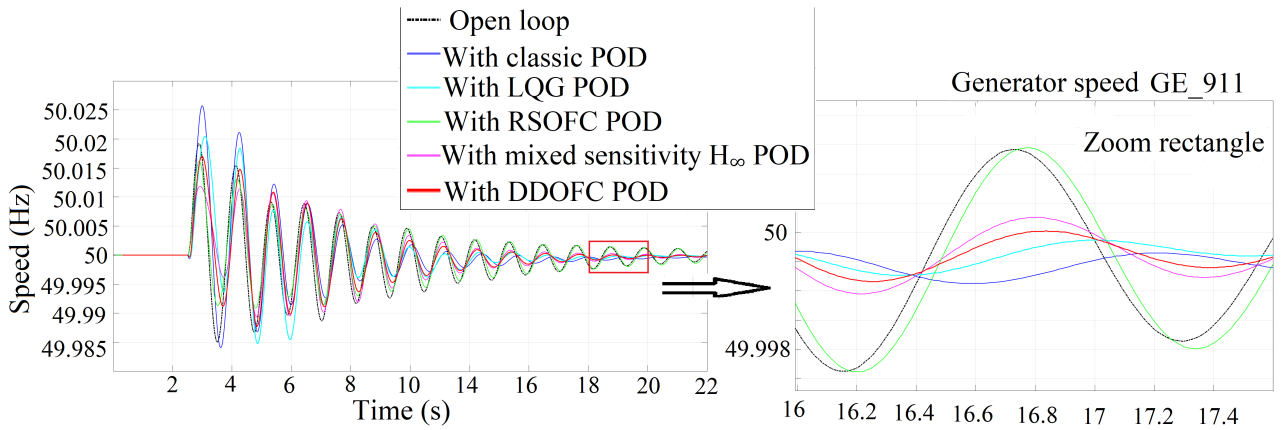


Figure 13: Tripping lines case.

1. 4th to 8th oscillation (mode 1): Classic, LQG, and DDOFC POD give more damping during the 4th to the 8th swing (mode 1).
2. In the zoomed figure (mode 2), the damping is greater with the DDOFC than with the mixed sensitivity H_∞ and the RSOFC POD.
3. The overshoots is greater with LQG POD than with open-loop during the first two swings.

In summary, the proposed DDOFC POD is more robustness and better damping for all the cases.

7. Conclusion

In this paper two robust model-matching based POD are studied. Sufficient conditions are derived for robust stabilization, in the sense of Lyapunov method series stability based on a reference model and have been formulated using an LMI format to obtain the controllers' gains. The robustness of the proposed controller is finally tested and compared to LQG, mixed sensitivity H_∞ and standard (IEEE) POD controllers on a realistic benchmark of 19 generators connected by a meshed AC grid. Paper contributions are: (i) improves damping and robustness subject to the unstable zeros compared with standard controller structures (LQG, mixed sensitivity H_∞ and standard POD controllers); (ii) The proposed controller is validated using Eurostag, which is more realistic ;

(iii) It can be easily implemented in real case and it consists in a simple output-feedback. The control methodology is applied here for Q modulation but can be extended to coordinate P and Q modulation of the HVDC link.

It is planned in the near future to implement the overall proposed control strategy on the France-Spain and France-Italy HVDC interconnection in real grid situations.

8. Appendix

8.1. LQG controller:

Based on LQG 3.1, the gains are given by:

$$L = [-164.18 \quad 47.48 \quad 80.33 \quad 57.635 \quad 96.34 \quad -19.51 \quad 2.81 \quad 48.01 \quad 35.078 \quad 8.58 \quad -7.82 \quad -0.33 \quad -9.20]^T;$$

$$K_r = \begin{bmatrix} 13.7682 & & -3.3704 & & -4.0354 & & 6.5771 \\ 7.0691 & 4.3546 & 2.4524 & -1.5362 & 1.1628 & 0.7133 & - \\ 0.4256 & -0.6244 & -0.5161 & & & & \end{bmatrix}$$

u to Q_{pod} Transfer Function(TF) is H_1 , and TF from $\Delta\theta$ to u is H_2 :

$$H_1 = \sum_{i=0}^{n-1} \sum_{j=0}^n \frac{N1_i(s)}{D1_j(s)} = \frac{N1_{n-1}s^n + \dots + N1_1s + N1_0}{D1_ns^n + \dots + D1_1s + D1_0} \quad (56)$$

$$H_2 = \frac{N2_{n-1}s^{n-1} + \dots + N2_1s + N2_0}{D2_ns^n + \dots + D2_1s + D2_0} \quad (57)$$

$n = 13$ (including the wash-out filter (dimension 1))(cf. Table 3).

Table 3: TF of LQG POD paramaters

i,j=	N1	D1	N2	D2
13	/	1	/	1
12	-3.681	43.19	1781	43.19
11	-189.3	785.2	1.814e04	785.2
10	-3051	1.092e04	3.614e05	1.092e04
9	-3.894e04	1.087e05	2.343e06	1.087e05
8	-3.575e05	8.942e05	2.358e07	8.942e05
7	-2.571e06	5.837e06	9.686e07	5.837e06
6	-1.513e07	3.203e07	6.336e08	3.203e07
5	-7.04e07	1.431e08	1.381e09	1.431e08
4	-2.672e08	5.266e08	6.488e09	5.266e08
3	-8.032e08	1.557e09	-3.658e08	1.557e09
2	-1.735e09	3.469e09	5.733e09	3.469e09
1	-2.923e09	5.716e09	-9.87e10	5.716e09
0	-1.42e09	4.454e09	-1.387e11	4.454e09

8.2. Mixed sensitivity H_∞ controller:

The H_∞ controller TF in 3.2 is:

$$K(s) = \frac{N_{n-1}s^{n-1} + \dots + N_1s + N_0}{D_n s^n + \dots + D_1s + D_0} \quad (58)$$

In (58), $n = 15$ (including the wash-out filter (dimension 1) and frequency weights (dimension 2)). H_∞ controller parameters are given in Table 4

Table 4: TF of H_∞ POD paramaters

i=	N	D
15	/	1
14	9.4e05	4.6e05
13	9.4e7	7.8e06
12	1.1e9	1.5e08
11	1.9e10	1.5e09
10	1.38e11	1.5e10
9	1.3e12	9.8e10
8	5.95e12	6.3e11
7	3.51e13	2.91e12
6	1.1e14	1.3e13
5	4.3e14	3.9e13
4	7.4e14	1.17e14
3	1.8e15	2.15e14
2	1.1e15	3.9e14
1	-3.3e13	2.6e14
0	3.3e14	1.1e13

8.3. Reference model:

The reference model TF used in proposed two controller:

$$f_r(s) = \frac{Nr_{n-1}s^{n-1} + \dots + Nr_1s + Nr_0}{Dr_n s^n + \dots + Dr_1s + Dr_0} \quad (59)$$

$n = 12$ (cf. Table 5).

Table 5: Reference model TF

i=	Nr	Dr
12	/	1
11	0.02143	19.54
10	0.1264	355.5
9	0.9629	3773
8	- 1.255	3.6e4
7	- 126.5	2.5e5
6	- 1088	1.6e6
5	- 9771	7.2e6
4	- 5.1e4	3.1e7
3	- 2.3e5	9.2e7
2	- 8.7e5	2.7e8
1	- 1.8e6	4.1e8
0	- 4.7e6	7.3e8

8.4. ROSCF controller:

The gains calculated in (31):

$Y=1.150696148547366e-12$;

$X=2.009746646814367e-13$.

Then, the gain of the controller is: $K = 5.725578148724988$. Notice that the dimension of the ROSCF controller is 13 (equal to the dimension of the reference model (12) + the one of the wash-out filter (1)).

8.5. DDOFC controller:

The transfer function of controller DDOFC $K(s)$:

$$K(s) = \frac{Nd_{n-1}s^{n-1} + \dots + Nd_1s + Nd_0}{Dd_n s^n + \dots + Dd_1s + Dd_0} \quad (60)$$

Since the order of the controller depends on the control model plus reference model, $n = 26$ (dimension of the plant (12) + dimension of the reference model (12) + wash-out filters for the plant and reference model (2)). Parameters are shown in Table 6

Table 6: Transfer function of DDOFC POD parameters

i=	Nd	Dd
26	/	1
25	5.267e05	4.057e04
24	1.713e07	1.465e06
23	4.532e08	4.032e07
22	8.033e09	7.692e08
21	1.225e11	1.234e10
20	1.496e12	1.621e11
19	1.616e13	1.865e12
18	1.481e14	1.856e13
17	1.217e15	1.65e14
16	8.672e15	1.3e15
15	5.573e16	9.242e15
14	3.119e17	5.888e16
13	1.568e18	3.402e17
12	6.764e18	1.768e18
11	2.567e19	8.326e18
10	7.833e19	3.519e19
9	1.879e20	1.341e20
8	1.951e20	4.546e20
7	- 7.141e20	1.372e21
6	- 6.079e21	3.617e21
5	- 2.359e22	8.277e21
4	- 6.919e22	1.593e22
3	-1.507e23	2.516e22
2	- 2.483e23	3.057e22
1	- 2.907e23	2.551e22
0	- 1.568e23	1.08e22

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