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Experimental and numerical investigation of specific behaviour of fluoride ions during filtration of pure salt water solutions with titania membrane

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Abstract

This work addresses the specific interactions between titania membrane and fluoride anions during ultrafiltration operation. In general, the salt transmission increases with salt concentration when pure salt-water solutions are ultrafiltered, except for fluoride-based salts observed in our study, for which transmission decreased at low concentrations. This phenomenon was only observed with titanium dioxide membrane. A numerical tool based on a physical description of ionic mass transfer in porous material (generalized Nernst-Planck approach) was used to explore the modification-induced changes due to fluoride anions.

33 Numerical investigations showed a modification of the electric charge of the membrane
34 surface in the pore at low fluoride concentrations. This phenomenon screened the electric
35 effect in a completely reversible way, and then enhanced the ion mass transfer through the
36 porous membrane. These modifications can be explained by the substitution of oxygen atom
37 (providing the surface electric charge) with a fluoride ion which was screening the electric
38 charge and facilitated the ion transfer.

39

40 **Keywords**

41 Titanium dioxide; ultrafiltration membrane; electric charge screening; ion transport
42 modelling; interaction titanium-fluoride

43

44 **1. Introduction**

45 Separation processes using membrane technologies are widely used for industrial applications
46 to lower the cost and to increase the effectiveness of the operations [1]. Indeed, these separation
47 technologies are energy efficient, easy to control and do not require additional chemicals
48 compared to other separation methods [2]. Nanofiltration and ultrafiltration are used in industry
49 for various applications (separation, concentration, rectification, etc) of small solutes in low-
50 viscosity solutions. For example, these technologies are widely used for waste water treatment
51 [3-5], for separation or concentration in food industry [6], and for the recovery of a lead
52 compound in pharmaceutical industry [7]. The choice of the membrane (ceramic, polymeric ...)
53 [8,9] and the driving process (pressure / concentration / electric) [10] depends on the intended
54 application and the operating conditions (temperature, pH, organic solvents, etc.). Mineral
55 membranes have many advantages: they can operate in harsh conditions [11], can be easily
56 cleaned [12] and, considering their chemical composition, they are not very suitable for
57 bacterial growth [13]. Nevertheless, in practice, these membranes are less effective and more
58 expensive than polymeric membranes [14]. Thus, they are often used only for specific
59 industrial applications requiring distinctive features [15]. Currently, the most used ceramic
60 membranes on the market are titanium dioxide, zirconia and alumina membranes. They are
61 made from a mineral core on which a thin layer (active layer) of metal oxide is deposited.
62 These membranes are tubular, ensuring good mechanical performances. Titanium dioxide
63 membranes are often used because they offer additional interesting properties (photo-catalytic,
64 antifouling, etc.) [16,17].

65 The membrane performances depend on the operating conditions (T, pH, pressure, salt
66 concentration, etc.) and on the interactions between the surface and ions in solution. Indeed,
67 these interactions are various (e.g., van der Waals forces, adsorption, hydrogen bonding,
68 hydrophobic repulsion) and are responsible of modifying the apparent electric surface charge

69 [18] and the dielectric effects in the pore [19]. Several studies dealing with filtration tests of
70 pure salt-water solutions consider only two exclusion mechanisms (steric and electric) [20,21].
71 However, few studies had focused also on dielectric effects in the pore. These effects can have
72 various causes: the difference of dielectric property between the solution and the pore wall, the
73 polarity of water, the presence of surface charges, dipoles and hydrated ions. [22]. These effects
74 should be taken into account to study membrane performances, especially for a nanoporous
75 active layer [23].

76 It is challenging (if not impossible) to estimate the contribution of each mechanism in a
77 nanopore experimentally. Therefore, numerical investigations using a knowledge-based model
78 can then be considered as an effective way to understand and to study the global influence of
79 these phenomena on the operating performance of a membrane. Such modelling approach
80 requires a physical description of all exclusion contributions reflecting reality as closely as
81 possible. Steric effects can be easily conceptualized by assuming the solvent and solutes
82 transport through the pores of well-defined size. From an experimental point of view, the
83 magnitude of this exclusion phenomena can be approached by filtrating uncharged solutes [24].
84 For the electric and dielectric exclusions, there is no possibility to estimate or well-describe
85 their real influences. Some authors have developed experimental indirect techniques for their
86 estimations, as for example, zetametry, streaming induced potential or electrochemical
87 impedance spectroscopy [25-27]. Likewise, different more or less theoretical models were
88 implemented in the mass transfer modelling [28,29]. Unfortunately, these approaches
89 (experimental and numerical) lead to imperfect descriptions of these two exclusion phenomena.
90 The current trend is to take into account these contributions via a global description (i.e.,
91 effective surface charge and a decrease of apparent permittivity in the pore, results of several
92 effects) [30,31].

93 The main objective of this work is to investigate the specific behavior of fluoride ions

94 throughout filtration with a titanium dioxide ultrafiltration membrane at low cut off. For this
95 purpose, separation performances of pure salt-water solutions at different salt concentrations
96 were experimentally and numerically investigated. The results are interpreted by using the
97 numerical modeling in terms of both electric and dielectric effects.

98

99 **2. Materials and methods**

100 Tangential filtration tests were performed with a laboratory pilot plant provided by
101 Techniques Industrielles Appliquées (Bollène, France) detailed in previous study [32]. The
102 membrane used in this work (TiO₂-1) was a commercial titanium dioxide membrane (1 kDa)
103 provided by TAMI Industries (Nyons, France). Three others membranes were used to validate
104 the results, a titania membrane from the same manufacturer, called TiO₂-2 and two home-
105 made zeolite membranes (Na-Mordenite and bi-layer MFI zeolite), called MOR and MFI.
106 Both membranes were obtained from zeolite synthesis on macroporous tubular support
107 (alumina). The membrane preparations are detailed in our previous papers for Mordenite [33]
108 and for bilayer MFI [34].

109 The membrane technical data are: 7 mm inner diameter and 25 cm length. The feed solution is
110 in a tank (5 L), and the fluid flow is provided by a volumetric pump at 700 L/h (Reynolds
111 number $\approx 35,000$). The concentration polarization effects may be neglected, because the fluid
112 flow is mainly turbulent. The temperature is maintained at 25°C by a cooling unit. The
113 transmembrane pressure is controlled by adjusting a manual valve from $\Delta P = 4$ to 12 bar.
114 Feed and retentate solutions are recycled in the feed tank during filtration in order to operate
115 at constant concentration. Retentate and permeate are sampled for analysis at each operating
116 pressure.

117 The membrane was previously conditioned by filtrating pure water (demineralized water,
118 conductivity < 0.1 $\mu\text{S}/\text{cm}$). Between each experimental filtration, the pilot was flushed with
119 pure water until a residual conductivity inferior to 1 $\mu\text{S}/\text{cm}$ was obtained, and a filtration of
120 pure water was carried out to estimate the hydraulic performances of the membrane. The
121 membrane hydraulic permeability (L_p) was deduced from the slope of the linear curve
122 (permeation flux (J_v) versus transmembrane pressure - Equation 1). μ is the dynamic viscosity
123 of pure water.

$$124 \quad J_v = L_p \frac{\Delta P}{\mu} \quad (1)$$

125 Filtration of vitamin B12 (Alfa Aesar, purity 98%, $9.10^{-4} \text{ mol.m}^{-3}$) – water solution was
126 performed to investigate steric effects via the estimation of a mean pore radius of the
127 membrane. The samples were analyzed by using an UV-visible spectrophotometer (Lambda
128 35, Perkin Elmer Instrument, Waltham, MA, USA) at 362 nm. Filtration of saline aqueous
129 solutions were done with NaF and NaCl (Sigma-Aldrich, St. Quentin Fallavier, France, purity
130 > 99%) at different concentrations (from 0.5 to 100 mol m^{-3}). Retentate and permeate (C_r and
131 C_p , respectively) samples were analyzed by conductimetry (conductimeter PC 5000 L
132 Phenomenal, VWR, Radnor, US). The permeation flux (J_v) was estimated by sample
133 weighting.

134 The observed rejection rate R was deduced from the following equation:

$$135 \quad R = 1 - \frac{C_p}{C_r} \quad (2)$$

136 **3. Numerical modelling**

137 Abundant works were devoted to numerical mass transfer in porous media and especially in
138 membrane filtration. In nanofiltration or ultrafiltration at low cut-off, three modelling

139 approaches are commonly used to describe the transport of ionic and uncharged solutes in the
140 porous medium:

- 141 - The Kedem and Katchalsky equations [35], which derive from the thermodynamic
142 of irreversible processes. This approach can be used at different levels of
143 complexity, but is often used in its simpler form reducing the physical and
144 phenomenological descriptions.
- 145 - The Maxwell-Stefan equations [36], which relate the mass flow of each
146 components to the effects of driving forces. This rigorous approach requires the
147 estimation of different properties and parameters which are not easily accessible or
148 measurable.
- 149 - The Nernst-Planck equations [37] also derived from the thermodynamic of
150 irreversible processes and of systems far off the balance. Flux-force relations are
151 simplified by considering simplified equations with respect to the physical
152 description [38]. Commonly, the mass transfer is assumed to be one-dimensional
153 through uniform and cylindrical pores. The mass transfer in the pores is due to
154 three effects: diffusion (gradient of activity), electro-migration (electrical potential)
155 and convection [39].

156 The flux of an ionic solute (J_i) can be written in steady state according to these previous
157 assumptions as follow:

$$158 \quad J_i = -K_{iD}D_i \frac{dc_i}{dx} - K_{iD}D_i c_i \frac{d \ln \gamma_i}{dx} - K_{iD}D_i z_i c_i \frac{F}{RT} \frac{d\Psi}{dx} + K_{ic}c_i V = VC_{ip} \quad (3)$$

159 The boundary conditions at both sides of the membrane active layer ($x = 0$, $x = L$) is an
160 equality of generalized chemical potentials of each solute at the interfaces between bulk and

161 pore solutions [40]. This equilibrium is often described by the product of three contributions:
 162 a steric, an electric and a dielectric one (equation 4).

163 For $x = 0$ or L
$$\frac{c_i(x)}{c_i} = \phi_i \frac{\gamma_{is}}{\gamma_{ip}} \exp(-\Delta W_i) \exp\left(-\frac{z_i F}{RT} \Delta \Psi_D\right) \quad (4)$$

164 $\Delta \Psi_D$ is the Donnan potential (difference in electrical potential at both sides of the interface
 165 free solution/solution in the pore). The steric effects are taken into account through

166
$$\phi_i = \left(1 - \frac{r_{is}}{r_p}\right)^2$$
 the steric partitioning coefficient which depends on the ratio of pore (r_p) and

167 solute radii (r_{is}) [41].

168 ΔW_i estimates the dielectric effects. This term represents a sum of different interactions
 169 between solutes, solvent and membrane. For example, the confinement of water molecules in
 170 the pore, the difference of dielectric constant between the solvent and the pore surface, the
 171 ions hydration, etc.

172 Faced with the complexity of interacting phenomena, this contribution is often estimated
 173 (Born Model) via a modification of the apparent dielectric permeability (ϵ_p) of the solution in
 174 the pore. [42].

175

176
$$\Delta W_i = \frac{(z_i e)^2}{8\pi\epsilon_0 r_{is} k_B T} \left(\frac{1}{\epsilon_p} - \frac{1}{\epsilon_b} \right) \quad (5)$$

177 Equations 3, 4 and 5 are solved for each ion by taking into account the electroneutrality in the
 178 feed solution and in the pore as follows:

179
$$\sum_{i=1}^n z_i C_i = 0 \quad \text{and for } 0 \leq x \leq L \quad \sum_{i=1}^n z_i c_i(x) + X_d = 0 \quad (6)$$

180 Where X_d is the volumetric membrane charge density in the pore.

181 The permeation flux is calculated from Equation 7. $\Delta\pi$ is the osmotic pressure due to the
182 difference of salt concentrations on both sides of the membrane.

$$183 \quad J_v = \frac{L_p}{\mu} (\Delta P - \Delta\pi) \quad (7)$$

184 In the case of the filtration of a neutral solute, this set of equations is considerably simplified
185 by neglecting electro-migration described in equation 3, electric and dielectric effects in the
186 partitioning equations, the membrane charge and the osmotic pressure. Solving equation 3 and
187 the appropriate boundary conditions (equation 4 at $x = 0$ and $x = L$) leads to an algebraic
188 solution (equation 8) linking the observed rejection R to a mean pore radius r_p .

$$189 \quad R = 1 - \frac{\phi K_c}{1 - (1 - \phi K_c) \exp\left(-\frac{K_c r_p^2 \Delta P}{8\mu K_d D}\right)} \quad (8)$$

190 The pore is discretized according to the pore length (x), and concentration of each ion in the
191 pore is obtained by consecutive integration. The set of equations is solved iteratively owing to
192 the presence of the permeate concentration in the differential mass transfer equation (3). The
193 program is written in Fortran 90.

194 Solving this model requires the estimation of 4 parameters (mean pore radius, hydraulic
195 permeability, membrane charge and apparent dielectric constant in the pore). The hydraulic
196 permeability was estimated from pure water filtration tests using equation 1. The mean pore
197 radius was assessed via the filtration of a neutral molecule (vitamin B12) and the use of
198 equation 8 (numerical approximation by minimizing quadratic error between experimental
199 and calculated rejections). The membrane electric charge and apparent dielectric constant in
200 the pore were estimated by fitting experimental results with the model.

201 **So, the salt concentration of the solution C , the hydraulic permeability L_p and the mean pore**
202 **radius r_p are the input parameters. The calculation is done for five applied pressures ranging**

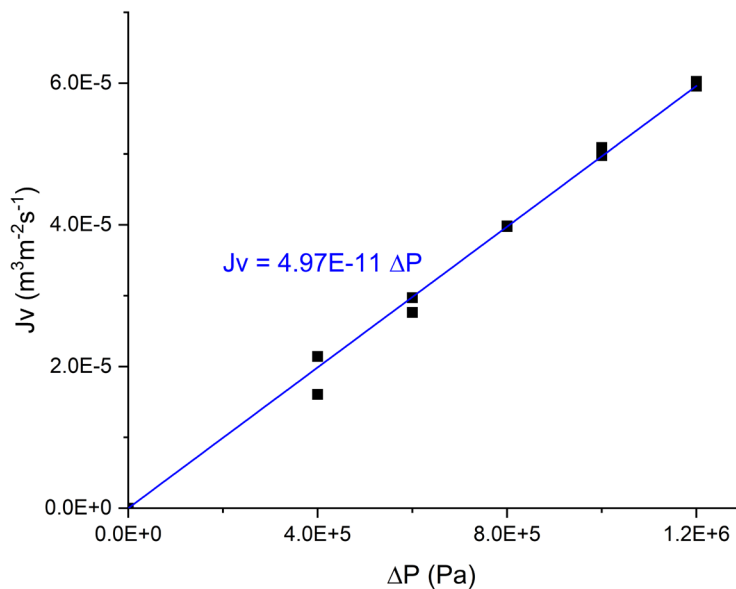
203 from 4 to 12 bar. The simulation results are the permeate concentration and the permeate flow
204 rate for each applied pressure. The calculation is repeated up to the experimental and
205 numerical results are in good agreements by adjusting the membrane electric charge and the
206 dielectric constant.

207

208 **4. Results and Discussion**

209 **4.1. Experimental results**

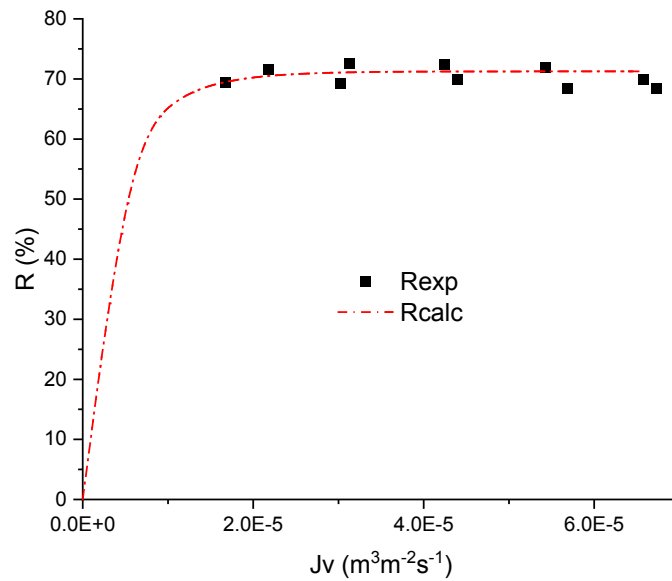
210 Before using the model, the estimation of both, hydraulic permeability and mean pore radius,
211 are required. For this, a filtration test of pure water was performed by increasing and
212 decreasing the applied pressure. The results are shown in figure 1. The water flux is a linear
213 function of the applied pressure. The slope of the curve is the membrane hydraulic
214 permeability divided by the dynamic viscosity ($L_p = 5.1 \cdot 10^{-14} \text{ m}^3 \text{ m}_{mem}^{-2}$).



215

216 Figure 1: filtration of pure water (flow rate vs. transmembrane pressure).

217 Two experimental filtrations of vitamin B12-water solution were performed in order to
218 estimate the steric effects. Figure 2 shows the experimental rejection rate of vitamin B12 as a
219 function of the permeate flux. The mean pore radius was adjusted in equation 8 (red curve) to
220 minimize quadratic difference between experimental and calculated rejection rates. The
221 obtained mean pore radius was $r_p = 1.3 \text{ nm}$.



222

223

Figure 2: Experimental and calculated rejection rate of vitamin B12.

224

Successive filtration tests of pure salt – water solutions were performed for different salt

225

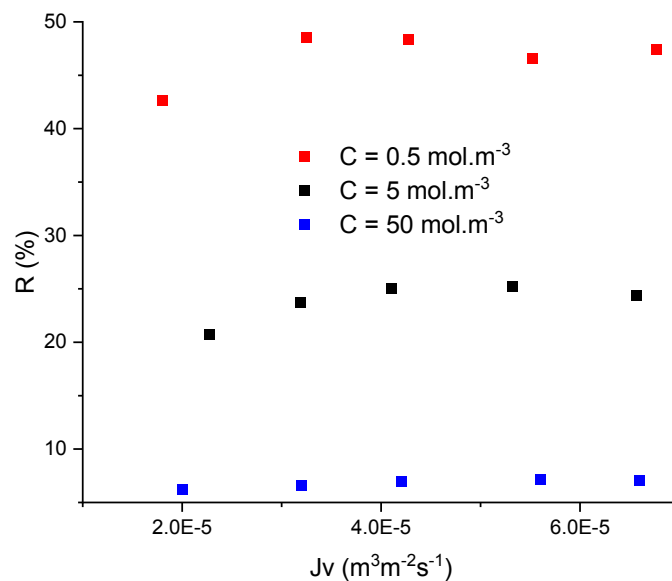
concentrations (from 0.5 to 100 mol.m⁻³). Some tests were repeated (not in chronological

226

order) to exclude a gradual modification of the membrane properties (selectivity and / or

227

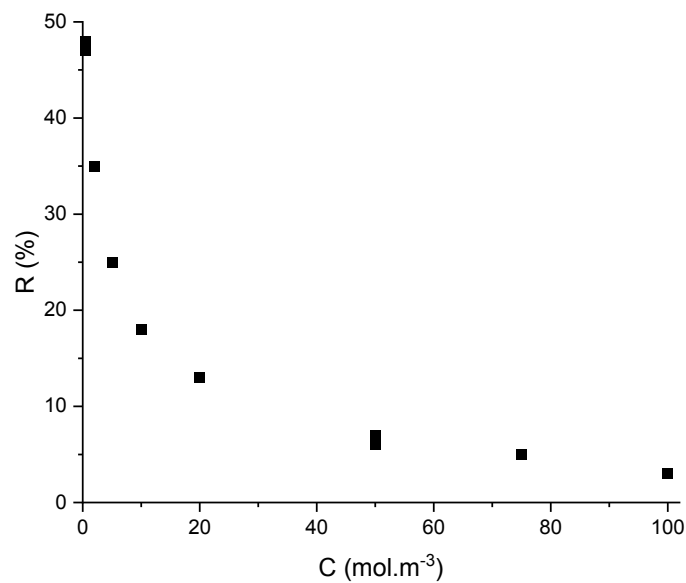
hydraulic).



228

229 Figure 3: Experimental rejection rates of NaCl-water solutions (0.5 / 5 / 50 mol.m⁻³).

230 Figure 3 shows the observed rejection rates obtained for filtration of sodium chloride–water
231 solutions at different salt concentrations. The rejection rate increased up to a maximal value of
232 about 8 bar for the transmembrane pressure. This maximum is plotted for all the filtration
233 experiments in a rejection rate / salt concentration diagram (figure 4).



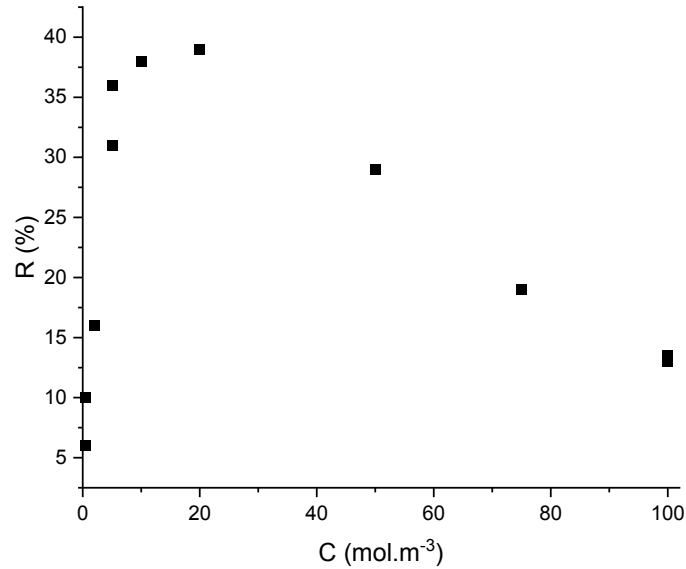
234

235 Figure 4: maximal rejection rates of NaCl-water solutions vs. salt concentration.

236 As it was expected, the maximum rejection rate decreased with the salt concentration
237 increasing. Indeed, this observation [43-45] was explained by the screening of the surface
238 electrical charge in the pore ($\frac{X_d}{C}$ decreases when C increases). The same experiments carried
239 out with other salts (NaI and Na₂SO₄) showed the same behaviour (figure S1 in
240 supplementary materials). Nevertheless, experiments with sodium fluoride show a peculiar
241 behaviour, especially at low salt concentrations. Figure 5 shows the maximum rejection rates
242 obtained with NaF-water solutions.

243

244



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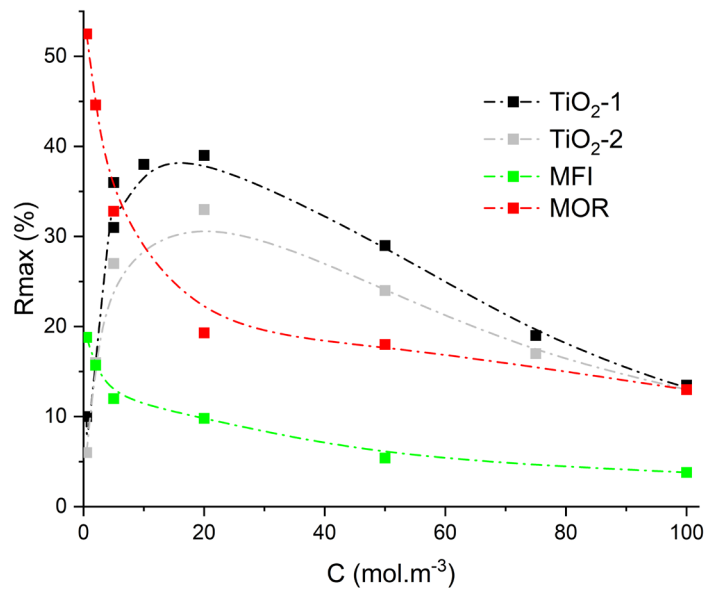
246 Figure 5: maximal rejection rates of NaF-water solutions vs. salt concentration.

247

248 The results showed a phenomenon occurring at low salt concentration facilitating the sodium
249 fluoride transmission. When the salt concentration increased, a competition between this
250 phenomenon and the screening of electrical charge was observed between 5 and 20 mol.m⁻³.
251 Beyond this concentration, the membrane separated in a normal way this saline solution. The
252 observed phenomenon is fully reversible because some experiments at low concentration
253 were additionally performed at the end of the series, and the results were similar.

254 Additional experiments performed with three different ceramic membranes showed the same
255 results (figure 6) for both titanium dioxide membranes (TiO₂-1 and 2) and different results for
256 both zeolite membranes. Indeed, the results obtained with MOR and MFI membranes showed

257 the same tendencies observed with the filtration of other salts, indicating that the peculiar
258 behaviour observed in the case of titania membranes was due to a specific interaction between
259 fluoride ions and titanium atoms.



260

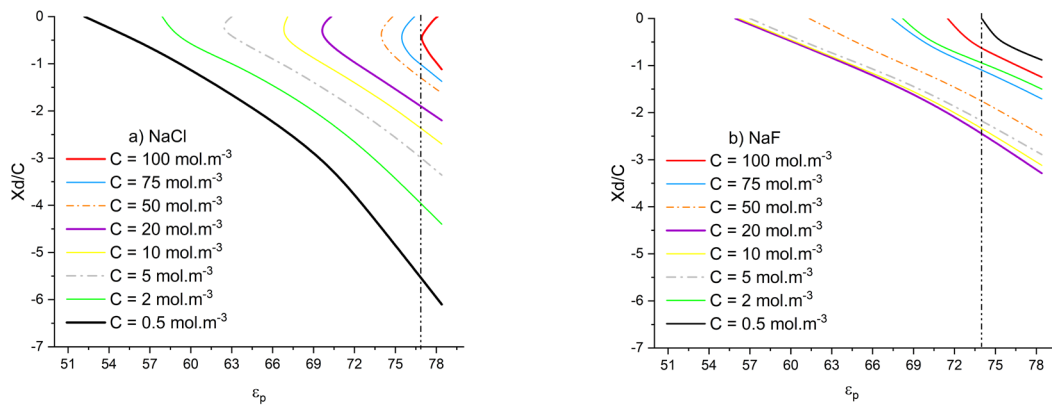
261 Figure 6: maximal rejection rates of NaF-water solutions obtained with different ceramic
262 membranes.

263 4.2. Numerical investigation

264 A numerical approximation of rejection rate curves ($R = f(Jv)$) was performed by using the
265 model previously described. The hydraulic permeability and the mean pore radius estimated
266 from experimental results were used for the simulation, and the fitting was carried out by
267 adjusting electric membrane charge (X_d) and dielectric permeability of the solution in the pore
268 (ϵ_p). The numerical approximation lead to an infinity of couples (X_d, ϵ_p) that allowed a well-
269 fitting of the rejection curves. This set of couples formed a curve. Figure 7 shows the best-
270 fitted parameters' curves for each test performed in an electric charge / dielectric permittivity

271 diagram. Only negative values of the membrane electric charge were considered based on
 272 previous zetametry investigations [46].

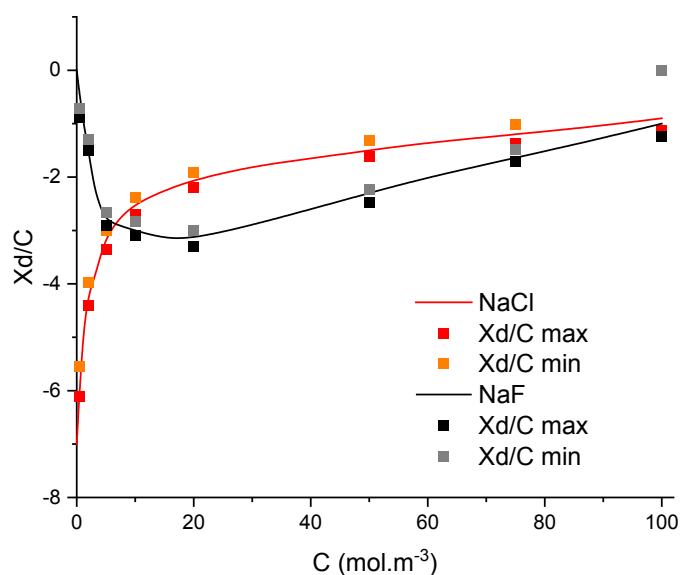
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274

275 Figure 7: best-fitted (X_d, ϵ_p) for a) NaCl-water solutions and b) NaF-water solutions.

276 If the shapes of the curves were similar, the results obtained for NaF-solutions differed in
 277 ascending order. Indeed, for NaCl-water solutions, the increase of salt concentration was
 278 reflected in a diminution of both, electrical charge and dielectric exclusion. For NaF-water
 279 solutions, dielectric exclusion and membrane electrical charge first increased to reach a
 280 maximum (in the range $C_0 = 5\text{-}20 \text{ mol.m}^{-3}$) and then decreased. Theoretically, the dielectric
 281 exclusion is the consequence of confinement, i.e., the difference of dielectric permittivity
 282 between the solvent and the pore wall and the presence of ions in the pore. The more ions in
 283 the pore, the more the dielectric exclusion is important. So, it can be assumed that the
 284 maximal dielectric exclusion can be reached for high concentrations of salt. With this
 285 hypothesis, the range (X_d, ϵ_p) could be reduced for each filtration test. Figure 8 shows the
 286 range of surface membrane charge for each salt concentration.



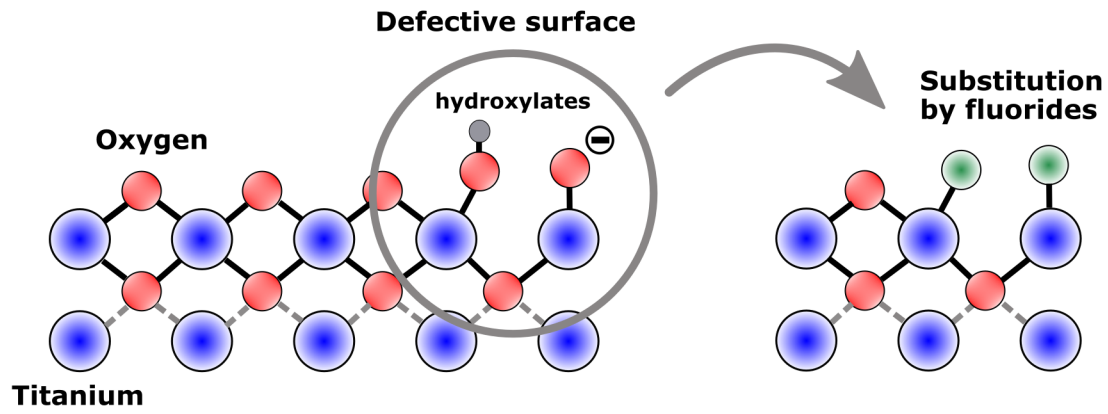
287

288 Figure 8: membrane electric charge for different salt concentrations (red = NaCl, black =
289 NaF).

290 As expected, for NaCl-water solutions, the electric charge of the membrane was gradually
291 screened by the salt concentration, reducing the electric exclusion. This finding was the same
292 for different salts in solution, except sodium fluoride (only with titania membrane). For
293 sodium fluoride – water solutions, it seems that there were two phenomena that drove the salt
294 transmission in opposite directions. At high salt concentration, the behaviour was the same as
295 NaCl (screening of electric charge in the pore). At low concentration, salt transfer was
296 favoured instead as if the membrane electric charge (specific for each material) was screened
297 by ions in the pore (reversible phenomenon).

298 The surface chemistry of titanium dioxide was often studied for photocatalytic applications.
299 Several teams [47, 48] have studied F-doped TiO₂. They explained the increase of the
300 catalytic properties by the creation of oxygen gaps and consequently an increase of surface
301 acidity. Indeed, the surface charge (negative) is mainly due to oxygen. The substitution of O²⁻

302 ions by F^- requires that $TiO_{2-x}(O^-)_x$ becomes $(TiO_{2-x})^+-(F^-)_x$ for maintaining the electro
303 neutrality [49,50]. In this case, the interaction between fluoride ions and titania surface (figure
304 9) is due to electrostatic forces.



305

306

Figure 9: scheme of surface interaction.

307 This explanation agrees with all our observations, namely, the negative surface charge and a
308 comparatively weak attraction explaining the reversibility and an increase of surface acidity.
309 This phenomenon thus provides a less repulsive surface for fluoride anion and consequently
310 an increase of salt transmission at low concentrations. Indeed, oxygen has an electric charge
311 directed towards the fluid, while the fluoride charge is directed towards the surface attracted
312 by the charge of the titanium atom.

313 5. Conclusion

314 Filtration of fluoride ions with a titanium dioxide membrane showed a specific behaviour
315 different from the other salts. Indeed, at low salt concentrations, fluoride ions were mainly
316 transmitted while chloride, iodide and other ions were predominantly rejected. The numerical
317 study of these filtration tests indicated that the electric charge in the pore (scaled by the salt
318 concentration) was very low at low concentrations in contrast with sodium chloride (the ratio
319 between the electric charge in the pore and the salt concentration is maximal at low

320 concentrations). This can be explained by a specific and reversible interaction between
 321 titanium and fluoride ions modifying the surface chemistry in the pores. A partial substitution
 322 of O^{2-} ions by F^- imparted a quasi-neutral electric charge in the pore facilitating the transfer of
 323 ions.

324

325

326 **Glossary**

c_i	Concentration of ion i in the pore (mol m^{-3})
C_{ip}	Permeate concentration of ion i (mol m^{-3})
C_{ir}	Bulk concentration of ion i (mol m^{-3})
C_0	Average salt concentration in the feed solution (mol m^{-3})
D_i	Diffusion coefficient of ion i at infinite dilution ($\text{m}^2 \text{s}^{-1}$)
e	Electronic charge ($1.602 \cdot 10^{-19} \text{ C}$)
F	Faraday constant (96487 C mol^{-1})
J_i	Flux of ion i ($\text{mol m}^{-2} \text{s}^{-1}$)
J_v	Permeation flux ($\text{m}^3 \text{m}^{-2} \text{s}^{-1}$)
J_w	Permeation flux of pure water ($\text{m}^3 \text{m}^{-2} \text{s}^{-1}$)
k_B	Boltzmann constant ($1,381 \cdot 10^{-23} \text{ m}^2 \text{kg s}^{-2} \text{K}^{-1}$)
K_{ic}	Hindrance factor for convection relative to ion i (dimensionless)
K_{id}	Hindrance factor for diffusion of ion i (dimensionless)
L_p	Hydraulic permeability ($\text{m}^3 \text{m}^{-2} \text{s}^{-1}$)
R	Gas constant ($8.314 \text{ J mol}^{-1} \text{K}^{-1}$)
r_{is}	Stokes radius of ion i (m)
R_i	Observed rejection of ion i (dimensionless)
r_p	Average pore radius (m)
T	Temperature (K)
V	Solvent velocity in the pore ($\text{m} \cdot \text{s}^{-1}$)
x	Axial position within the pore (m)
X_d	Apparent electric charge density in the membrane pore (eq m^{-3})
z_i	Valence of ion i (dimensionless)

327 • Greek letters

γ_{ip}	Activity coefficient of ion i in the pore (dimensionless)
γ_{is}	Activity coefficient of ion i in the feed solution at the pore inlet (dimensionless)
ΔP	Transmembrane pressure (Pa)
ΔW_i	Dielectric exclusion energy (J)
$\Delta \psi_D$	Donnan potential (V)
$\Delta \pi$	Osmotic pressure difference (Pa)
ϵ_0	Permittivity of free space ($8.85419 \cdot 10^{-12} \text{ F} \cdot \text{m}^{-1}$)
ϵ_b	Bulk dielectric constant (dimensionless) = 78.4
ϵ_p	Pore dielectric constant (dimensionless)

μ Dynamic viscosity (Pa s)
 ϕ_i Steric partition coefficient (dimensionless)
 ψ Electrical potential within the pore (V)

328

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